These are small animations of the solutions to the 2 ODE's from lecture 2/9/17 for the small parameter. Nasser M. Abbasi

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0.0 0.0

0.2

0.4

```
Manipulate[
 Labeled[
   Plot \left[\frac{-1 + e^{x/z}}{1}, \{x, 0, 2\}, \text{PlotRange} \rightarrow \{\{0, 1.1\}, \{0, 1\}\}, \frac{1}{2}\right]
    GridLines \rightarrow Automatic, GridLinesStyle \rightarrow LightGray, PlotStyle \rightarrow Red],
   Row[{"solution to ", TraditionalForm[e y''[x] - y'[x] == 0]}], Top],
 \{\{z, 0.1, "e"\}, .1, 0.001, -0.001, Appearance \rightarrow "Labeled"\}
1
                                                                                0
                                               0.1
   € ₌
                     solution to \in y^{\prime\prime}(x) - y^{\prime}(x) = 0
     1.0
    0.8
    0.6
    0.4
    0.2
```

0.6

For eps*y"+y=0 ode, we notice global variations showing up in frequency as well as in amplitude as eps become very small

1.0

0.8

Manipulate[Labeled[$Plot\left[\frac{Sin\left[\frac{x}{\sqrt{z}}\right]}{Sin\left[\frac{1}{\sqrt{z}}\right]}, \{x, 0, 2\}, PlotRange \rightarrow \{\{0, 2\}, \{-10, 10\}\},$

 $\begin{array}{l} \mbox{GridLines} \rightarrow \mbox{Automatic, GridLinesStyle} \rightarrow \mbox{LightGray, PlotStyle} \rightarrow \mbox{Red}], \\ \mbox{Style}[\mbox{Row}[{"solution to ", TraditionalForm}[zy''[x] + y[x] == 0]}], 16], \mbox{Top}], \\ \mbox{\{z, 0.01, "$e"$}, 0.01, 0.0001, -0.0001\} \end{array}$

