

# quizz 7, ME 240 Dynamics, Fall 2017

Nasser M. Abbasi

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## 0.1 Problem 1

Question 1

1 pts

The drone hovers for 41 seconds at a height of 40 meters above the ground while taking a picture of a crowd.

What is the vertical impulse by the lift force (combined force of the four rotors) during this time (in Newton-seconds)?

Report your answer to the nearest whole number

$$\begin{aligned} I &= \int_0^t F dt \\ &= \int_0^t mg dt \\ &= mgt \\ &= (1)(9.81)(41) \\ &= 402.21 \text{ N-s} \end{aligned}$$

## 0.2 Problem 2

Question 2	1 pts
<p>A sudden gust of wind propels the drone against the side of a nearby building at 4.48 m/s. Inertial sensors onboard the drone determine that it bounces back from the building with a speed of 1.10 m/s. Assume this event is a direct central impact.</p> <p><b>What is the coefficient of restitution between the drone and the building during this collision?</b></p> <p>Report your answer to three decimal places.</p> <div style="border: 1px solid #ccc; height: 20px; width: 150px; margin-top: 10px;"></div>	

$$-e = \frac{V_B^+ - V_A^+}{V_B^- - V_A^-}$$

Where  $B$  is the wall. Hence  $V_B^+ = V_B^- = 0$  since wall do not move. Therefore

$$\begin{aligned} -e &= \frac{-V_A^+}{-V_A^-} \\ &= \frac{-(-1.10)}{-(+4.48)} \\ &= \frac{1.10}{-4.48} \\ &= -0.24554 \end{aligned}$$

Hence

$$e = 0.24554$$

### 0.3 Problem 3

Question 3	1 pts
<p>Another gust of wind blows the drone against the building a second time. This time, the impact speed is 5.13 m/s and the rebound speed is 1.47 m/s. It collision takes 0.29 seconds to complete.</p> <p>What is the magnitude of the average force applied by the building to the drone during this collision (in Newtons)?</p> <p>Report your answer to one decimal place.</p> <input data-bbox="316 674 621 726" type="text"/>	

$$mv_A^- + \int_0^{0.29} F_{av} dt = mv_A^+$$

But  $m = 1$  then

$$\begin{aligned} \int_0^{0.29} F_{av} dt &= v_A^+ - v_A^- \\ &= -1.47 - 5.13 \\ &= -6.6 \end{aligned}$$

Hence

$$\begin{aligned} F_{av}(0.29) &= -6.6 \\ F_{av} &= -\frac{6.6}{0.29} \\ &= -22.759 \end{aligned}$$

The magnitude is 22.759 N. The negative sign, since force is in negative  $x$  direction.

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## 0.4 Problem 4

Question 4	1 pts
<p>A third gust of wind blows the drone against the building a third time. This time the impact speed is 6.4 m/s and the rebound speed is 0.12 m/s.</p> <p><b>What is the magnitude of the energy dissipated in this collision (in Joules)?</b></p> <p>Report your answer to one decimal place.</p> <input type="text"/>	

Energy lost is

$$\begin{aligned}\Delta &= \frac{1}{2}m(v_A^-)^2 - \frac{1}{2}m(v_A^+)^2 \\ &= \frac{1}{2}(6.4)^2 - \frac{1}{2}(0.12)^2 \\ &= 20.473 \text{ J}\end{aligned}$$

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## 0.5 Problem 5

When blown against the building repeatedly, the drone came dangerously close to a nest of peregrine falcons. It therefore drew the attention of the mother falcon, with mass 1.023 kg, circling above. The falcon, diving at 107 m/s straight down, collides with the drone, which is hovering at a stationary position prior to impact. After they collide the falcon becomes entangled with the drone.

**What is the post-impact speed of the drone-plus-falcon system (in m/s)?**

Report your answer to one decimal place.

Let  $A$  be the falcon and  $B$  be the drone. Hence

$$\begin{aligned}m_A v_A^- + m_B v_B^- &= (m_A + m_B) v^+ \\(1.023)(107) + 0 &= (1.023 + 1) v^+ \\v^+ &= \frac{(1.023)(107)}{2.023} \\&= 54.108 \text{ m/s}\end{aligned}$$