

Convolution - integral

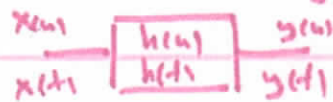


$$y(t) = x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau) h(t-\tau) d\tau = \int_{-\infty}^{\infty} h(\tau) x(t-\tau) d\tau$$

- Q1: obtain $y(t)$ when $x(t) = \sin t$; $h(t) = \sin t$
 by (a) Convolution operation.
 (b) Frequency domain operation.

- Q2: obtain Fundamental period / Fundamental frequency
 of number of Discrete / Cont. Signals

- Q3: impulse response & step response of a system
 Cont / Discrete



Impulse response $y(t)$ when $x(t) = \delta(t)$ $x_c(t) = \delta_c(t)$

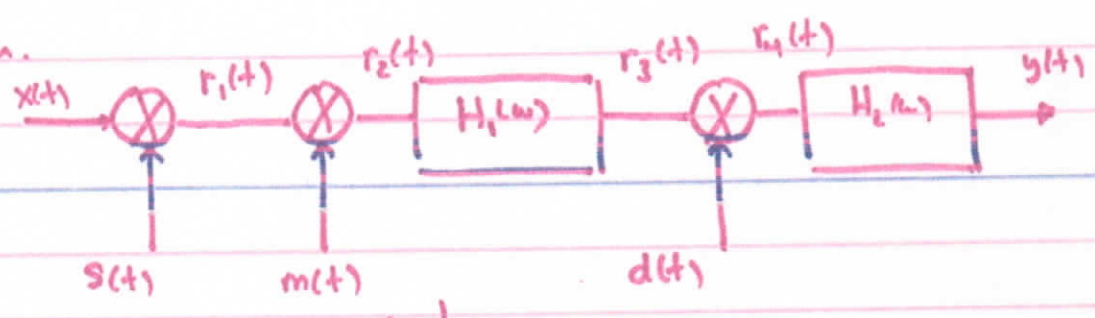
Step response $y(t)$ " $x(t) = u(t)$ $x_c(t) = u_c(t)$

- | | | |
|-------------------|----------|-------------|
| Q4: Chapt 3, 4, 5 | periodic | nonperiodic |
| | FS | FT |
| | DTFS | DTFT |

- Q5: Magnitude & phase.

Given profile of frequency response of a Transfer function (filter)
 obtain output.

problem.



Both

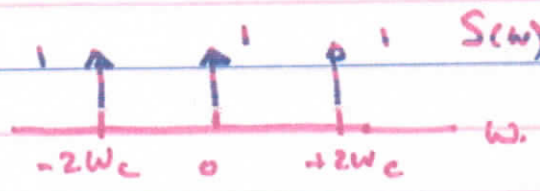
have

$H_1(\omega)$
 $H_2(\omega)$

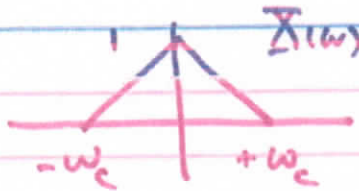


$H_1(\omega) = H_2(\omega)$

$s(t)$ has frequency profile \Rightarrow



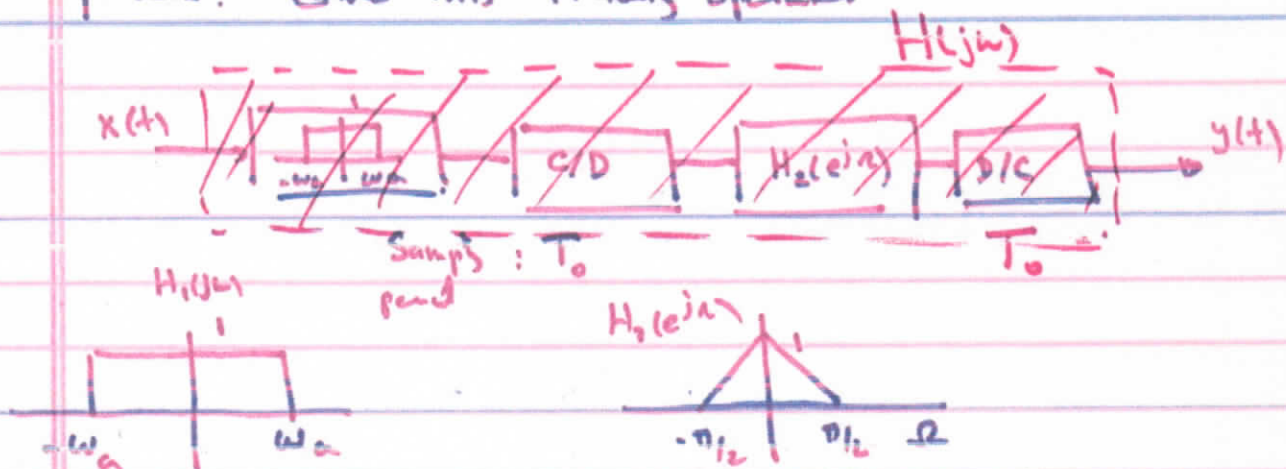
$x(t)$ has frequency profile



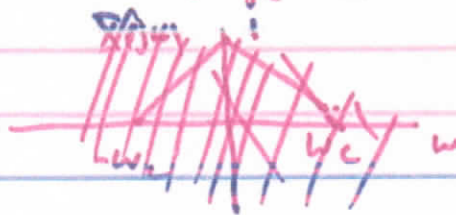
Question: For which of the following choices for $m(t)$ and $d(t)$ $y(t)$ is non zero.

- (a) $m(t) = 1$ $d(t) = 1$ *
- (b) $m(t) = \cos(\omega_c t)$ $d(t) = \cos(\omega_c t)$ *
- (c) $\sin(\omega_c t) = m(t)$ $d(t) = \sin(\omega_c t)$
- (d) $m(t) = \cos(2\omega_c t)$ $d(t) = \cos(2\omega_c t)$
- (e) $m(t) = \cos(2\omega_c t)$ $d(t) = \cos(\omega_c t)$

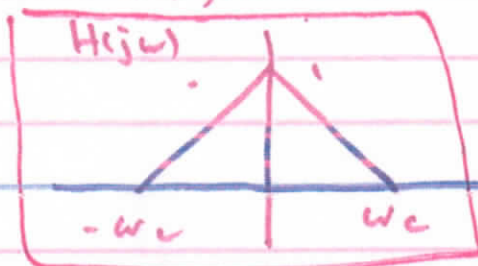
problem: Give This Filtering operation.



input signal $x(t)$ has Fourier transform as



Q: Find in terms of ω_c The value of The sampling period T_0 and corresponding ω_a such that The total continuous filter has.

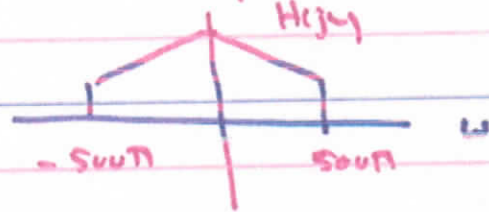


$$T_0 = \frac{\pi/2}{\omega_c} ?$$

$$\frac{2\pi}{T_0} = \frac{2\pi}{(\pi/2)/\omega_c} = 4\omega_c$$

$$\omega_a = 2\omega_c ?$$

problem. Consider that the frequency response $H_c(j\omega)$



we want to implement this continuous filter using
Discrete-time processing

- (a) what is the maximum value of sampling period T required $T = ?$
- (b) what is the required $H_d(e^{j\omega})$
- (c) sketch the total system

$$T_{max} = \frac{\pi}{500\pi} = 2 \text{ msec.} \quad \Omega = 2\pi$$



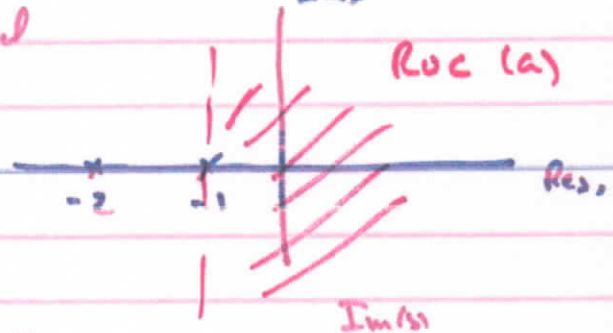
Laplace - Transform.

problem. Determine The following \mathcal{L}

$$X(s) = \frac{1}{(s+1)(s+2)}$$

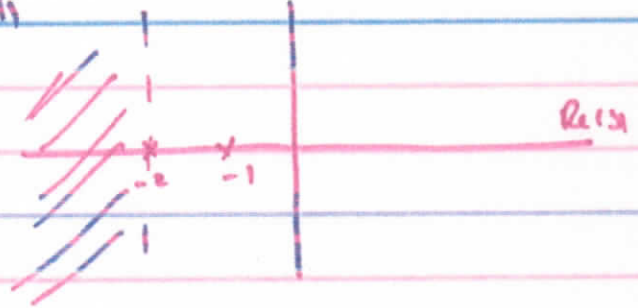
- (a) $x(t)$ is right handed t > 0
- (b) $x(t)$ is left handed t < 0
- (c) $x(t)$ is two sided

$$X(s) = \frac{1}{s+1} - \frac{1}{s+2}$$

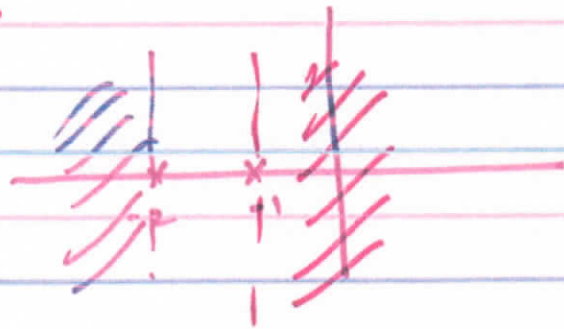


(a) $x(t) = e^{-t} u(t) - e^{-2t} u(t)$

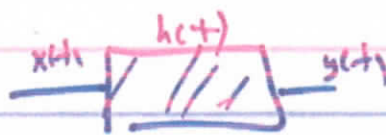
(b) $x(t) = -e^{-t} u(-t) + e^{-2t} u(-t)$



(c) $x(t) = e^{-t} u(t) + e^{-2t} u(-t)$



problem: Given LTI Causal Syst



when

$$\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 6y(t) = x(t) + 2 \frac{dx(t)}{dt}$$

(a) Determine the system transfer function $H_c(s)$ and obtain $h_c(t)$ Assuming all initial cond. are at zero.

(b) Determine the system $H_d(z)$ of a discrete-time LTI causal system obtained from $H_c(s)$ via impulse invariant method

$$\Omega = \omega \cdot T$$

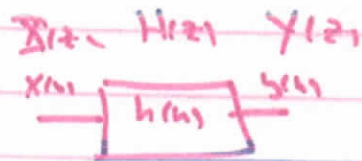
$$H_c(s) \quad s = j\omega \quad z = e^{j\Omega} \quad z = e^{sT}$$

$$H_c(s) = \frac{2s+1}{s^2+5s+6} \quad ? \quad H_d(z)$$

$$s = \frac{1}{T} \ln(z)$$

$$H_d(z) = \frac{z(\frac{1}{T} \ln(z)) + 1}{(\frac{1}{T} \ln(z))^2 + 5(\frac{1}{T} \ln(z)) + 6}$$

in Discrete LTI causal system
 problem Given the difference eq.



$$y(n] - 3y(n-1) + 2y(n-2) = x(n]$$

(a) Find $H(z) = \frac{1}{(1-zz^{-1})(1-z^{-1})} = \frac{z}{1-zz^{-1}} + \frac{-1}{1-z^{-1}}$

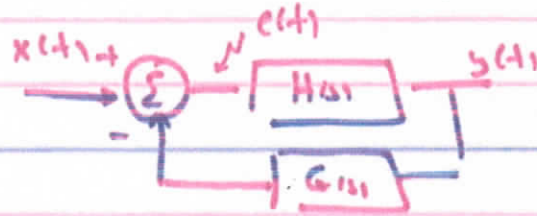
(b) Find impulse response $h(n] = ? = z(2^n)u(n] + (-1)(1^n)u(n]$

(b) response

(c) is this stable (unstable) $z_1=1, z_2=2$

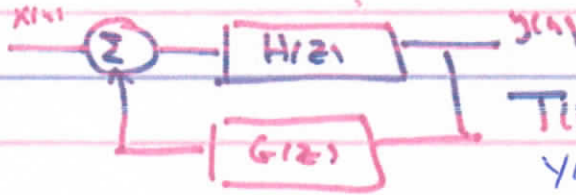
problem - Consider two feedback sys

$x(t) = \delta(t)$ $X(s) = 1$
 $y(t) =$



$T(s) = \frac{H(s)}{1 + G(s)H(s)}$
 $\frac{Y(s)}{X(s)} = \frac{H(s)}{1 + G(s)H(s)}$

$x(n) = \delta(n)$
 $X(z) = 1$



$T(z) = \frac{H(z)}{1 + G(z)H(z)}$
 $\frac{Y(z)}{X(z)} = \frac{H(z)}{1 + G(z)H(z)}$

if $H(s) = \frac{1}{s+3}$, $G(s) = s+1$

d. $H(z) = \frac{z}{s} - \frac{1}{2} z^{-1}$ $G(z) = \frac{z^{-1}}{1 - \frac{1}{2} z^{-1}}$

Find The impulse responses of each closed loop system