

EE 3015 Midterm 1 exam Friday Feb 28th. 2020

Duration 50 Minutes, One Crib sheet (8 x 11 inches) allowed – calculator allowed no use of cell phone. Close book and notes.

Problem 1 (25 pts.)

Given an input $x(t) = u(t) - u(t-3)$ to a LTI system with impulse response $h(t) = u(t) - u(t-2)$, Obtain the output of this system $y(t)$ utilizing convolution method. Show all steps in obtaining the results.

Problem 2. (25pts)

Given the impulse response of a discrete time LTI system: $h(n)$ with $h(n) = [1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 0]$ Obtain the output of this discrete system $y(n)$ using the convolution method when the input sequence is given by

$$x(n) = [0 \ 0 \ 1 \ 0 \ -1 \ 0].$$

(hint: assume the first element starts at $n = 0$ index point).

You can use either graphical method or analytical method however you must show all your steps in computation.

Problem 3 (30 pts.)

The Fourier transform of a signal $x(t)$ is given by the following expression:

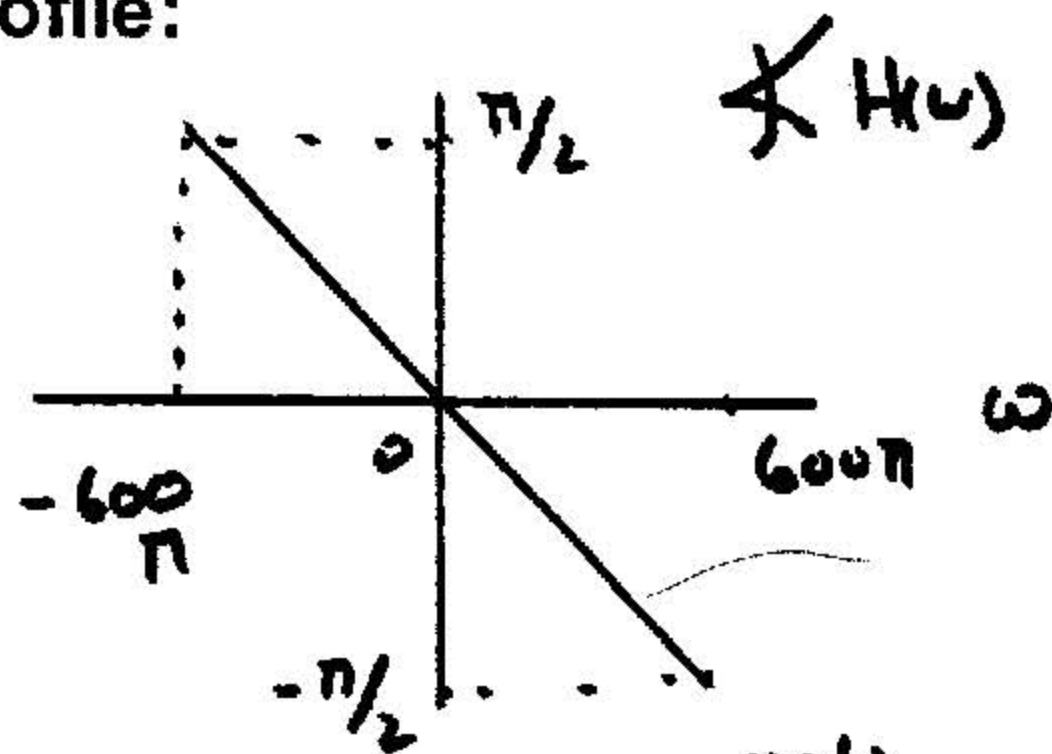
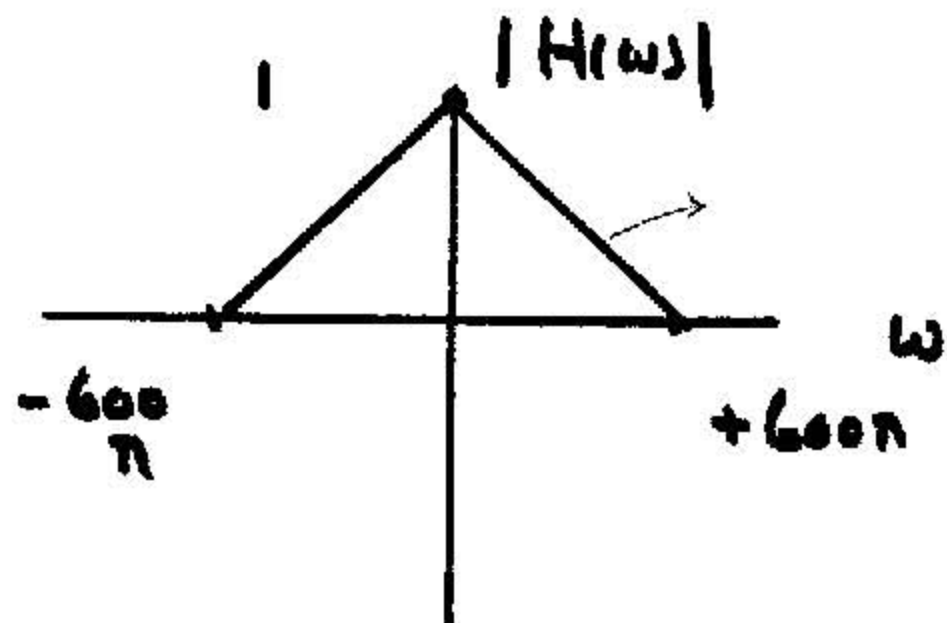
$$X(\omega) = Y(\omega) \cdot e^{-j2\omega t}$$

where $Y(\omega) = 2$ for $-2 < \omega < 0$ and $Y(\omega) = -2$ for $0 < \omega < 2$

Find time domain representation of $x(t)$.

Problem 4. (20 pts.)

The frequency response of a continuous time LTI system is given by the following magnitude and phase profile:



What is the steady state time domain output $y(t)$ for input

$$x(t) = \cos(1000\pi t) + 2 \cos(\underbrace{50}_{\omega_0}\pi t) + 3 \cos(500\pi t)$$

