

My first Manipulate program. Simulate of a pendulum which is being pulled up as it swings.

```
Remove["Global`*"];
```

```
maxLength = 1000;
u = Manipulate[Module[{g, r, simRate = 0.001},
  r = 1 -  $\alpha$  t;
  eq = r  $\theta''$ [t] - 2  $\alpha$   $\theta'$ [t] + g Sin[ $\theta$ [t]];
  g = 9.8;
  maxTime =  $\frac{1}{\alpha}$ ;
  s =  $\theta$  /. First[NDSolve[{eq == 0,  $\theta$ [0] ==  $\theta_0$  * Pi / 180,  $\theta'$ [0] == v0},  $\theta$ , {t, 0,
    maxTime - 0.001}, MaxSteps -> 200000, MaxStepFraction -> 0.0001]];

  getNormalizedAngle[ $\theta$ _] := Module[{q =  $\theta$ },
    {
      If[q >= 0, q = Mod[q, 2 Pi], {q = -q;
        q = Mod[q, 2 Pi];
        q = -q;
        q = q + 2 Pi}];
      q * 180 / Pi
    }
  ];

  getQuadrant[a_] := Module[{q},
    {
      If[a >= 0 && a <= Pi / 2, q = 1];
      If[a > Pi / 2 && a <= Pi, q = 2];
      If[a > Pi && a <=  $\frac{3}{2}$  Pi, q = 3];
      If[a >  $\frac{3}{2}$  Pi && a <= 2 Pi, q = 4];
      q
    }
  ];

  coordinates[s_, t_, l_,  $\alpha$ _] := Module[{ $\theta$ , p = False, q},
    { $\theta$  = s[t];
      If[p, Print["t=", t, "  $\theta$ =",  $\theta$  * 180 / Pi]];
      If[ $\theta$  >= 0,  $\theta$  = Mod[ $\theta$ , 2 Pi], { $\theta$  = - $\theta$ ;
         $\theta$  = Mod[ $\theta$ , 2 Pi];
         $\theta$  = - $\theta$ ;
         $\theta$  =  $\theta$  + 2 Pi}];
      q = First[getQuadrant[ $\theta$ ]];
      If[p, Print["after mod t=", t, "  $\theta$ =",  $\theta$  * 180 / Pi]];
      If[p, Print["q=", q]];

      r = 1 -  $\alpha$  t;
```

```

If[p, Print["r=", r]];
If[q == 1, {x = r Sin[θ], y = -r Cos[θ]}];
If[q == 2, {θ = θ - Pi/2; x = r Cos[θ], y = r Sin[θ]}];
If[q == 3, {θ = θ - Pi; x = -r Sin[θ], y = r Cos[θ]}];
If[q == 4, {θ = θ -  $\frac{3}{2}$  Pi; x = -r Cos[θ], y = -r Sin[θ]}];
If[p, Print["x=", x, " y=", y]];
If[p, Print["*****"]];
{x, y}
}
];
d = coordinates[s, ts, l, α];
Graphics[ { {Gray, Dashed, Line[{{-maxLength, 0}, {maxLength, 0}}]},
{Gray, Dashed, Line[{{0, -maxLength}, {0, maxLength}}]},
Text["θ= " <> ToString[First[getNormalizedAngle[s[ts]]]], {.4 l, .9 l}],
Text["current string length L(t)=L0-α t=" <> ToString[r], {.4 l, .8 l}],
Text["current time t (sec)=" <> ToString[ts], {.4 l, .7 l}],
Text["L[t] θ'[t]-2 α θ'[t]+g Sin[θ[t]]=0", {.4 l, .6 l}],
Line[{ {0, 0}, First[d] } ],
PointSize[.03], Red, Point[First[d]]],
PlotRange → {{-1 - .1 l, 1 + .1 l}, {-1 - .1 l, 1 + .1 l}}, ImageSize → {450, 325}
],
{{1, 0.9 maxLength, "L0, Initial string"}, 1, maxLength, 1, Appearance → "Labeled"},
{{α, 1, "α (rate of string shrinkage)"}, 0.1, 10, 0.1, Appearance → "Labeled"},
{{θ0, 45, "initial position in degrees θ(0)"}, 0, 360, 1, Appearance → "Labeled"},
{{vθ, 0, "initial angular speed in rad/sec θ'(0)"},
0, 100, 1, Appearance → "Labeled"},
{ts, 0, "current simulation time (sec)"}, 0,  $\frac{1}{\alpha} - 0.001$ ,  $\left(0.0001 \frac{1}{\alpha}\right)$ ,
Appearance → "Labeled"}, ContinuousAction → True, AutorunSequencing → {{5, 60}},
FrameLabel → "A shrinking Pendulum. by Nasser Abbasi, July 2007"]

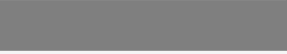
```

L_0 , Initial string  $9. \times 10^2$

α (rate of string shrinkage) 

initial position in degrees $\theta(0)$ 

initial angular speed in rad/sec $\theta'(0)$ 

current simulation time (sec) 



A shrinking Pendulum. by Nasser Abbasi, July 2007

```
(*Export["shrink_pendulum3.swf",u];*)
```

