

HW 4  
EE 409 (Linear Systems), CSUF spring 2010  
Spring 2010  
CSUF

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Date due and handed in March 18,2010

## 1 Problem 3.23 (a)

Write the state variable equation for the following

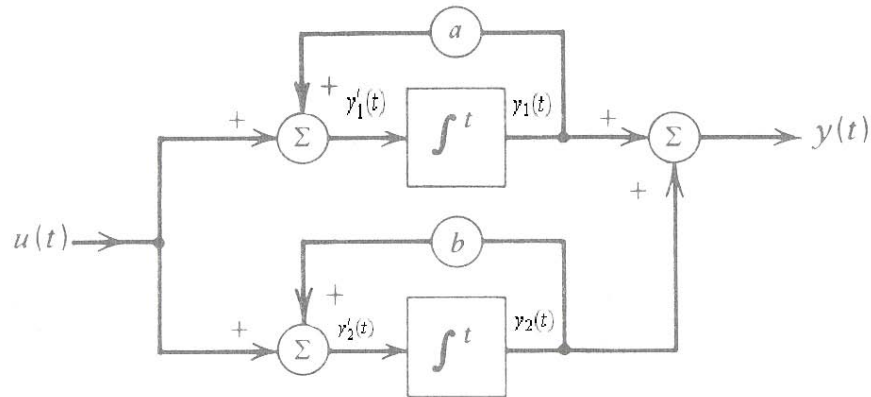


Figure 1: System description

### Solution

Let  $x_1(t)$  and  $x_2(t)$  be the state variables. Hence from the diagram we see the following

$$\begin{aligned}x_1'(t) &= ax_1(t) + u(t) \\x_2'(t) &= bx_2(t) + u(t)\end{aligned}$$

And

$$y(t) = x_1(t) + x_2(t)$$

Hence

$$\begin{aligned}\begin{pmatrix} x_1'(t) \\ x_2'(t) \end{pmatrix} &= \overbrace{\begin{pmatrix} a & 0 \\ 0 & b \end{pmatrix}}^A \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix} + \overbrace{\begin{pmatrix} 1 \\ 1 \end{pmatrix}}^B u(t) \\ y(t) &= \overbrace{\begin{pmatrix} 1 & 1 \end{pmatrix}}^C \begin{pmatrix} x_1(t) \\ x_2(t) \end{pmatrix}\end{aligned}$$