

Unit simplex animation showing feasibility region

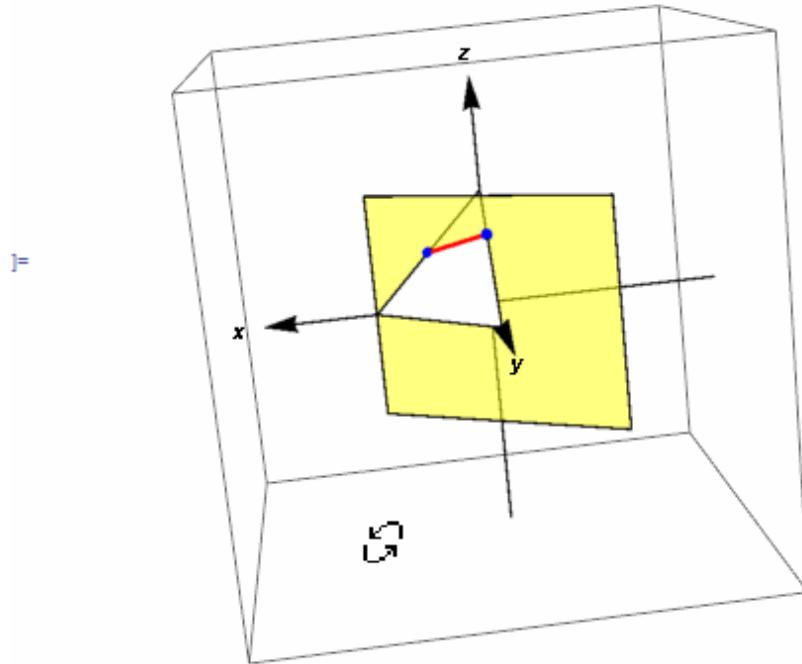
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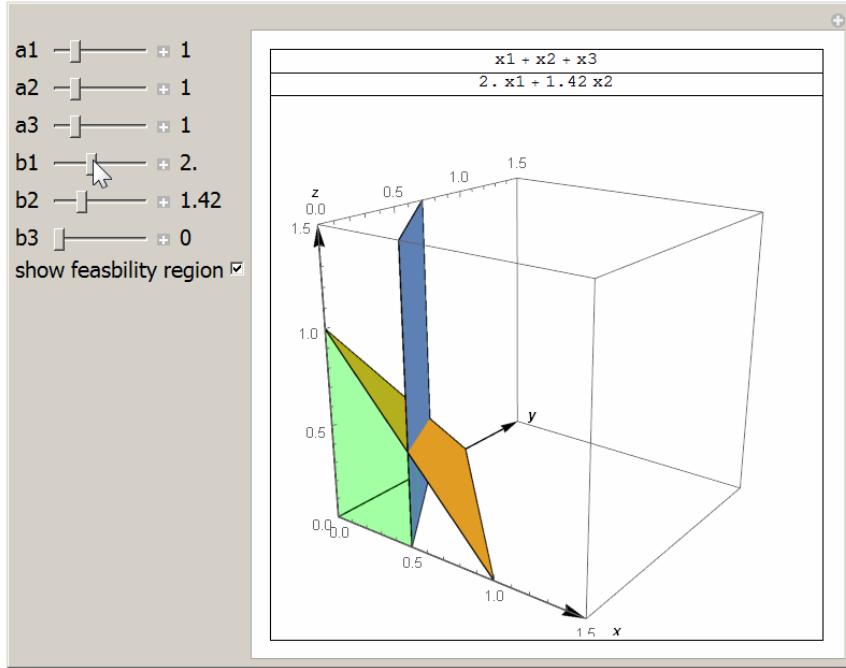
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This small animation shows the feasibility region and the intersection line between $a_1x_1 + a_2x_2 + a_3x_3 = 1$ and $b_1x_1 + b_2x_2 + b_3x_3 = 1$ and with $x_i \geq 0$. The light Green region is the one in which $a_1x_1 + a_2x_2 + a_3x_3 \leq 1$ and $b_1x_1 + b_2x_2 + b_3x_3 \leq 1$. The optimal solution will be on a vertex on the line of intersection between the two planes shown. Done for class HW.

$$\begin{aligned} 2x_1 + 3x_2 &= 1 \\ x_1 + x_2 + x_3 &= 1 \end{aligned}$$





This small animation shows the feasibility region which is the intersection line between unit simplex given by $x_1 + x_2 + x_3 = 1$ and plane $2x_1 + 3x_2 = 1$.

Source code used to generate the first movie is

```

Manipulate[
  len = 1.5;
  h = a1 x1 + a2 x2 + a3 x3;
  g = b1 x1 + b2 x2 + b3 x3;

  g1 = ContourPlot3D[{h == 1, g == 1}, {x1, 0, len}, {x2, 0, len}, {x3, 0, len},
    PlotRange -> {{0, len}, {0, len}, {0, len}},
    SphericalRegion -> True, MeshStyle -> {{Thick, Blue}}, Mesh -> {{0}},
    Lighting -> {"Ambient", White}];

  g2 = RegionPlot3D[h <= 1 && g <= 1, {x1, 0, len}, {x2, 0, len}, {x3, 0, len},
    PlotRange -> {{0, len}, {0, len}, {0, len}},
    SphericalRegion -> True, Mesh -> 0,
    PlotStyle -> Directive[Green, Opacity[0.2]],
    Lighting -> {"Ambient", White}];

  g3 = Graphics3D[{
    Arrow[{{0, 0, -len}, {0, 0, len}}],
    Text[Style[z, Bold], {0, 0, 1.1 len}],
    Arrow[{{0, -len, 0}, {0, len, 0}}],
    Text[Style[y, Bold], {0, 1.1 len, 0}],
    Arrow[{{-len, 0, 0}, {len, 0, 0}}],
    Text[Style[x, Bold], {1.1 len, 0, 0}]
  }];

  Grid[{
    {h},
    {g}
  }]
]

```

```
{
  If[showRegion,
    Show[g1, g2, g3, ImageSize -> 400, ImagePadding -> 5]
  ,
    Show[g1, g3, ImageSize -> 400, ImagePadding -> 5]
  ]
  }}, Frame -> All],
{{a1, 1, "a1"}, 0, 5, .01, Appearance -> "Labeled", ImageSize -> Tiny},
{{a2, 1, "a2"}, 0, 5, .01, Appearance -> "Labeled", ImageSize -> Tiny},
{{a3, 1, "a3"}, 0, 5, .01, Appearance -> "Labeled", ImageSize -> Tiny},
{{b1, 2, "b1"}, 0, 5, .01, Appearance -> "Labeled", ImageSize -> Tiny},
{{b2, 3, "b2"}, 0, 5, .01, Appearance -> "Labeled", ImageSize -> Tiny},
{{b3, 0, "b3"}, 0, 5, .01, Appearance -> "Labeled", ImageSize -> Tiny},
Row[{"show feasibility region ", Checkbox[Dynamic[showRegion]]}],
ControlPlacement -> Left
]
```

Source code used to generate the second movie is

```
eq1 = 2 x1 + 3 x2 == 1;
eq2 = x1 + x2 + x3 == 1;
len = 2;
g2 = Graphics3D[Simplex[{{1, 0, 0}, {0, 1, 0}, {0, 0, 1}}]];
g1 = ContourPlot3D[Evaluate@eq1, {x1, -1, 1}, {x2, -1, 1}, {x3, -1, 1},
  ContourStyle -> Directive[FaceForm[Yellow], Opacity[.5]], Mesh -> None,
  Lighting -> {"Ambient", White}, Boxed -> True, Axes -> False];
g3 = Graphics3D[{Arrow[{{0, 0, -len}, {0, 0, len}}], Text[Style[z, Bold], {0, 0, 1.1 len}],
  Arrow[{{0, -len, 0}, {0, len, 0}}], Text[Style[y, Bold], {0, 1.1 len, 0}],
  Arrow[{{-len, 0, 0}, {len, 0, 0}}], Text[Style[x, Bold], {1.1 len, 0, 0}],
  {Blue, Sphere[{0, 1/3, 2/3}, .05]},
  {Blue, Sphere[{1/2, 0, 1/2}, .05]},
  {Red, Thick, Line[{{0, 1/3, 2/3}, {1/2, 0, 1/2}}]}
 }];
Grid[{{Column[{eq1, eq2}],
{Show[g1, g2, g3, PlotRange -> All, ImageSize -> 400,
SphericalRegion -> True]}}}]
```