

# Illustrating ordinary amplitude modulation power efficiency

## Initialization Code (optional)

## Manipulate

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Manipulate[
  am[ $\mu$ , fc, fm, showCarrier, showMessage],

  Style["modulation parameters", Bold],
  {{ $\mu$ , 0.8, " $\mu$ "}, 0, 1.3, .1, Appearance -> "Labeled", ImageMargins -> -2, ImageSize -> Small},
  {{fc, 7000, " $f_c$  (hz)"}, 5000, 10000, 100, Appearance -> "Labeled", ImageMargins -> -2, ImageSize -> Small},
  {{fm, 500, " $f_m$  (hz)"}, 300, 1000, 10, Appearance -> "Labeled", ImageMargins -> -2, ImageSize -> Small},
  Delimiter,
  Style["modulated carrier plot options", Bold],
  {{showCarrier, True, "show carrier "}, {True, False}},
  {{showMessage, True, "show message "}, {True, False}}
,
  ControlPlacement -> Left,
  Initialization ->
  (
    maxCarrierFreq = 10000;
    maxMessageFreq = 1000;
    tmax = 3;
    fontSizeForTitles = 14;
    fontSizeForSubTitles = 11;

    am[ $\mu_$ , fc_, fm_, showCarrier_, showMessage_] :=
      Module[{plotStyleForCarrier, messagePlot, envelopePlot, carrierPlot, p},

        carrierPlot = (1 +  $\mu$  Cos[2 Pi fm t / 1000]) Cos[2 Pi fc t / 1000];
        messagePlot = Cos[2 Pi fm t / 1000];
        envelopePlot = 1 +  $\mu$  Cos[2 Pi fm t / 1000];

        If[showCarrier == True && showMessage == True, {plotStyleForCarrier = {Red, Blue, {Black, Dashed, Thin}},
          p = {carrierPlot, messagePlot, envelopePlot}}];

        If[showCarrier == True && showMessage == False, {plotStyleForCarrier = {Red, {Black, Dashed, Thin}},
          p = {carrierPlot, envelopePlot}}];

        If[showCarrier == False && showMessage == True, {plotStyleForCarrier = {Blue, {Black, Dashed, Thin}},
          p = {messagePlot, envelopePlot}}];

        If[showCarrier == False && showMessage == False, {plotStyleForCarrier = {{Black, Dashed, Thin}},
          p = envelopePlot}];

        GraphicsGrid[{
          { Plot[ Cos[2 Pi fc t / 1000] , {t, 0, 2}, TicksStyle -> Small,
            Ticks -> {{0, 1, 2}, {-1, 0, 1}}, AxesLabel -> {Style[Row[{Style["t", Italic], " (ms)"}], Larger]},
            PlotLabel -> Style["carrier signal", fontSizeForTitles], PlotStyle -> Red, Exclusions -> {1}},

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Plot[ Cos[2 Pi fm t/1000] , {t, 0, 2}, TicksStyle -> Small,
  Ticks -> {{0, 1, 2}, {-1, 0, 1}}, AxesLabel -> {Style[Row[{Style["t", Italic], " (ms)"}], Larger]},
  PlotLabel -> Style["message signal", fontSizeForTitles], PlotStyle -> Blue, Exclusions -> {1}
},

{Plot[p,
  {t, 0, tmax},
  PlotRange -> {All, {-2.5, 2.5}},
  TicksStyle -> Small, AxesLabel -> {Style[Row[{Style["t", Italic], " (ms)"}], Larger]},
  PlotLabel -> Column[{Style["modulated carrier", fontSizeForTitles],
    Style["with envelope and original message superimposed", fontSizeForSubTitles]}, Center],
  PlotStyle -> plotStyleForCarrier, ImagePadding -> Full, Exclusions -> {1}], SpanFromLeft
},

{frequencyPlot[fm, fc, μ], SpanFromLeft}},
Spacings -> {Scaled[.1], Scaled[.1]},
Frame -> {False, All}, Dividers -> None, AspectRatio -> Full, ImageSize -> 320
];

frequencyPlot[fm_, fc_, μ_] := Module[{carrierRight, carrierLeft, upperRight, upperleft,
  lowerRight, lowerleft, carrierPower, sidePower, z = 0.7*maxCarrierFreq, g, plotLabel},
  carrierRight = {Red, Arrow[{{fc, 0}, {fc, .5*fc}}]};
  carrierLeft = {Red, Arrow[{{-fc, 0}, {-fc, 0.5*fc}}]};
  upperRight = {Blue, Arrow[{{fc + fm, 0}, {fc + fm, fc*μ/4.}}]};
  upperleft = {Blue, Arrow[{{fc - fm, 0}, {fc - fm, fc*μ/4.}}]};
  lowerRight = {Blue, Arrow[{{-fc + fm, 0}, {-fc + fm, fc*μ/4.}}]};
  lowerleft = {Blue, Arrow[{{-fc - fm, 0}, {-fc - fm, fc*μ/4.}}]};
  carrierPower = 0.5;
  sidePower =  $\frac{\mu^2}{4.}$ ;

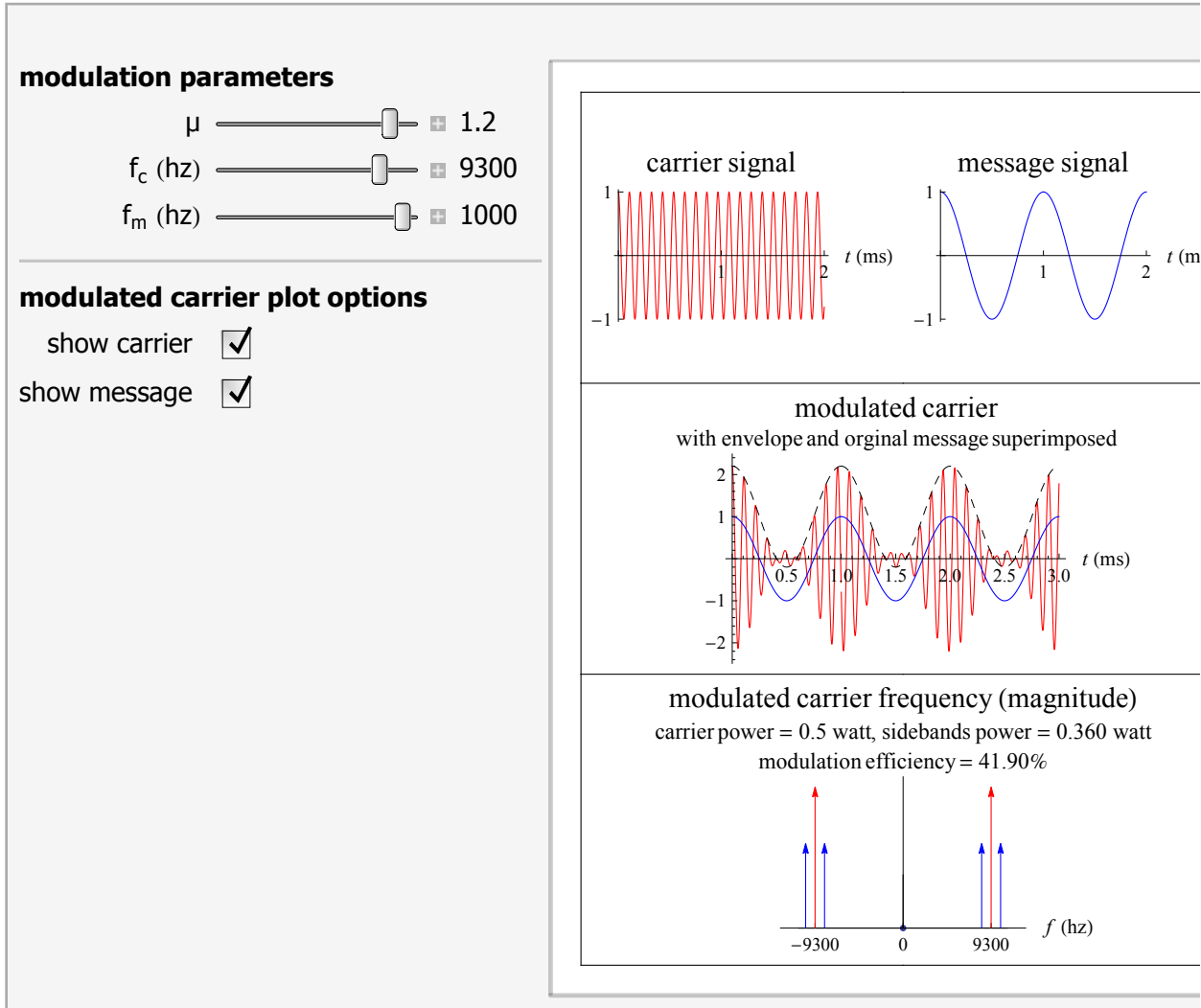
  g = { Line[{{-maxCarrierFreq - 0.1*maxCarrierFreq, 0}, {maxCarrierFreq + 0.1*maxCarrierFreq, 0}}],
    Line[{{0, 0}, {0, .25*z}}],
    carrierRight,
    carrierLeft,
    upperRight,
    upperleft,
    lowerRight,
    lowerleft,
    Text[Style["-fc", Small], {-fc, -0.1*z}],
    Text[Style["fc", Small], {fc, -0.1*z}],
    Text[Style["0", Small], {0, -0.1*z}]
  };

  plotLabel = Style[Column[{ Style["modulated carrier frequency (magnitude)", fontSizeForTitles],
    Row[{Style["carrier power = 0.5 watt", ], fontSizeForSubTitles],
      Style["sidebands power = " <> ToString[NumberForm[sidePower, {3, 3}] <> " watt",
        fontSizeForSubTitles]}], Style["modulation efficiency = " <>
      ToString[NumberForm[ $\frac{\mu^2}{\mu^2 + 2}$  * 100, {3, 2}]] <> "%", fontSizeForSubTitles]
    }, Center]];

  ListPlot[{{0, 0}}, PlotRange -> {{-maxCarrierFreq - 0.3*maxCarrierFreq,
    maxCarrierFreq + 0.3*maxCarrierFreq}, {-10, 0.5*maxCarrierFreq}},
  PlotLabel -> plotLabel, Ticks -> {{-fc, 0, fc}, None},
  AxesLabel -> {Style[Row[{Style["f", Italic], " (hz)"}], Larger]}, ImagePadding -> Full,
  Epilog -> g]
]

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)  
]



**Caption**

This demonstration illustrates the effect of changing the modulation factor  $\mu$  (also called the modulation depth) on the power efficiency of ordinary amplitude modulation (AM) technique. This demonstration also shows that a modulation factor  $\mu$  greater than unity will result in envelope distortion causing difficulties during demodulation. Hence  $\mu$  must be kept less than unity. At 100% modulation ( $\mu=1$ ), the power efficiency of AM is 33.33%. This means that at  $\mu=1$ , the total power carried by the sidebands is 1/3 of the total power. The modulated carrier  $s(t)$ , shown in the middle graph in this demonstration is defined as  $s(t) = (1 + \mu m(t)) \cos(2\pi f_c t)$  where  $m(t)$  is the message signal defined as  $m(t) = \cos(2\pi f_m t)$  and  $\mu$  is the modulation factor. For simplicity, the amplitude of the carrier signal and the amplitude of the message signal are both kept as unity.

- Drag Locators
- Create and Delete Locators
- Slider Zoom
- Gamepad Controls
- Automatic Animation
- Bookmark Animation

### **Search Terms** (optional)

Amplitude Modulation

### **Related Links** (optional)

<http://scienceworld.wolfram.com/physics/AmplitudeModulation.html>

<http://demonstrations.wolfram.com/AmplitudeModulation/>

<http://demonstrations.wolfram.com/ModulacionesAMSpanish/>

### **Authoring Information**

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