Kamke differential equations. Mathematica 10.4 and Maple 2016

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February 3, 2024 Compiled on February 3, 2024 at 3:11am

Contents

1 Introduction and summary of results

This report gives the result of solving the 1,940 differential equations from Kamke book in Mathematica 10.4 and Maple 2016 on windows 7, 64 bit OS. The PC used is an Intel i7-3930k running at 3.20 GHz with 16 GB memory.

The command `AboluteTiming[]` was used in Mathematica to obtain the CPU time. In Maple the following commands were used for this purpose

```
t0 := time[real]():
timeOut := 5*60;
result_of_solve := timelimit(timeOut,dsolve(ode[i]));
cpu_time := time[real]()-t0:
```

Both Maple and Mathematica had a CPU time limit of 5 minutes to complete each problem else the problem is considered not solved and marked as timed out.

When Mathematica returned `DifferentialRoot` as a solution to an ODE this was counted as not solved. Similarly, when Maple returned `DESol` this was also counted as not solved.

Table 1 below summarizes the performance of each CAS system

system	% solved	mean CPU time (sec)	mean leaf size of result	total CPU (minutes)	total leaf
Mathematica	75.93	28.53	2197.13	922.61	42624
Maple	91.96	1.12	190.72	36.29	36999

Table 1: Summary of final results

Table 2 summarizes the Kamke equations used

book chapter	kamke book numbering of equations	Numbering in this doc
Chapter 1, linear first order	1.1—1.576	1—576
Additional non-linear first order	N/A	577—1000
Chapter 2, linear second order	2.1—2.448	1001—1448
Chapter 3, linear third order	3.1—3.85	1449—1533
Chapter 4, linear fourth order	4.1—4.44	1534—1577
Chapter 5, linear fifth and higher order	5.1—5.13	1578—1590
Chapter 6, non-linear second order	6.1—6.246	1591—1836
Chapter 7, non-linear third and higher order	7.1—7.19	1837—1855
Chapter 8, system of ode, first order	8.1—8.57	1856—1912
Chapter 9, system of ode, higher order	9.1—9.28	1913–1940

Table 2: Kamke equation numbering

The following summarizes which equations are solved by each system

Not solved by Mathematica 16, 22, 38, 47, 48, 49, 50, 55, 56, 63, 66, 74, 79, 80, 81, 82, 83, 86, 87, 110, 121, 127, 188, 202, 203, 205, 206, 219, 234, 237, 250, 253, 265, 266, 269, 331, 340, 365, 367, 368, 370, 383, 385, 394, 395, 400, 402, 404, 413, 414, 416, 428, 429, 451, 452, 460, 461, 465, 467, 468, 470, 476, 479, 480, 482, 485, 487, 489, 494, 503, 504, 506, 508, 509, 510, 513, 515, 523, 524, 527, 528, 530, 531, 532, 533, 534, 535, 537, 538, 541, 542, 543, 544, 546, 550, 555, 561, 562, 566, 567, 570, 572, 575, 576, 592, 607, 613, 620, 638, 639, 640, 672, 696, 701, 702, 703, 704, 706, 707, 710, 714, 730, 733, 735, 743, 745, 746, 747, 752, 759, 765, 766, 769, 776, 782, 783, 784, 785, 786, 788, 789, 790, 791, 792, 807, 835, 837, 854, 855, 862, 865, 885, 889, 892, 894, 909, 913, 915, 916, 917, 918, 919, 922, 923, 925, 929, 932, 942, 953, 961, 993, 996, 1000, 1015, 1019, 1026, 1027, 1028, 1029, 1030, 1031, 1032, 1038, 1072, 1073, 1074, 1075, 1076, 1077, 1080, 1081, 1082, 1083, 1084, 1085, 1099, 1126, 1128, 1156, 1157, 1177, 1205, 1212, 1216, 1219, 1232, 1233, 1236, 1248, 1261, 1263, 1267, 1268, 1270, 1278, 1303, 1306, 1323, 1329, 1330, 1341, 1343, 1348, 1362, 1367, 1372, 1373, 1398, 1402, 1403, 1406, 1407, 1408, 1413, 1418, 1419, 1427, 1439, 1440, 1441, 1442, 1443, 1444, 1445, 1450, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1470, 1471, 1472, 1473, 1474, 1476, 1482, 1484, 1487, 1489, 1500, 1505, 1506, 1507, 1510, 1515, 1516, 1520, 1526, 1527, 1529, 1530, 1531, 1540, 1541, 1542, 1543, 1544, 1547, 1552, 1569, 1572, 1573, 1574, 1575, 1576, 1581, 1583, 1586, 1590, 1593, 1595, 1596, 1598, 1599, 1601, 1603, 1605, 1606, 1608, 1609, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1617, 1618, 1619, 1620, 1621, 1622, 1623, 1624, 1625, 1626, 1627, 1628, 1629, 1631, 1633, 1634, 1635, 1636, 1637, 1638, 1639, 1640, 1642, 1643, 1644, 1645, 1648, 1649, 1652, 1656, 1658, 1659, 1660, 1662, 1663, 1664, 1665, 1666, 1667, 1672, 1673, 1675, 1677, 1678, 1680, 1681, 1682, 1684, 1685, 1686, 1690, 1691, 1692, 1693, 1695, 1696, 1702, 1704, 1705, 1706, 1708, 1709, 1710, 1711, 1713, 1719, 1720, 1721, 1729, 1732, 1734, 1735, 1737, 1738, 1739, 1742, 1746, 1751, 1755, 1757, 1760, 1761, 1762, 1776, 1777, 1779, 1780, 1787, 1788, 1789, 1797, 1798, 1801, 1802, 1806, 1807, 1809, 1811, 1813, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1823, 1825, 1827, 1831, 1832, 1833, 1834, 1836, 1837, 1838, 1839, 1840, 1841, 1844, 1845, 1848, 1850, 1851, 1853, 1854, 1855, 1875, 1880, 1885, 1890, 1893, 1894, 1905, 1911, 1912, 1915, 1916, 1917, 1918, 1919, 1920, 1921, 1922, 1925, 1926, 1927, 1928, 1929, 1932, 1933, 1934, 1935, 1936, 1937, 1939, 1940

Not solved by Maple 38, 47, 48, 49, 50, 55, 56, 74, 79, 82, 87, 110, 121, 202, 203, 205, 206, 219, 234, 237, 250, 253, 265, 269, 331, 340, 367, 368, 370, 383, 395, 460, 461, 480, 482, 485, 503, 506, 507, 510, 531, 572, 575, 576, 708, 733, 789, 790, 835, 837, 878, 885, 894, 909, 912, 920, 1015, 1019, 1026, 1028, 1030, 1031, 1038, 1072, 1073, 1075, 1076, 1077, 1081, 1157, 1205, 1212, 1216, 1234, 1236, 1278, 1408, 1439, 1440, 1441, 1443, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1473, 1474, 1476, 1484, 1489, 1510, 1515, 1531, 1540, 1541, 1542, 1543, 1581, 1582, 1586, 1593, 1595, 1596, 1598, 1599, 1606, 1608, 1609, 1617, 1619, 1623, 1625, 1628, 1634, 1642, 1643, 1645, 1649, 1675, 1685, 1698, 1702, 1704, 1705, 1706, 1721, 1729, 1732, 1734, 1735, 1737, 1738, 1739, 1751, 1757, 1761, 1788, 1789, 1797, 1801, 1802, 1807, 1835, 1851, 1854, 1855, 1890, 1905, 1921, 1922, 1927, 1928, 1940

Solved by Mathematica but not by Maple 507, 708, 878, 912, 920, 1234, 1582, 1698,

1835

Solved by Maple but not by Mathematica 16, 22, 63, 66, 80, 81, 83, 86, 127, 188, 266, 365, 385, 394, 400, 402, 404, 413, 414, 416, 428, 429, 451, 452, 465, 467, 468, 470, 476, 479, 487, 489, 494, 504, 508, 509, 513, 515, 523, 524, 527, 528, 530, 532, 533, 534, 535, 537, 538, 541, 542, 543, 544, 546, 550, 555, 561, 562, 566, 567, 570, 592, 607, 613, 620, 638, 639, 640, 672, 696, 701, 702, 703, 704, 706, 707, 710, 714, 730, 735, 743, 745, 746, 747, 752, 759, 765, 766, 769, 776, 782, 783, 784, 785, 786, 788, 791, 792, 807, 854, 855, 862, 865, 889, 892, 913, 915, 916, 917, 918, 919, 922, 923, 925, 929, 932, 942, 953, 961, 993, 996, 1000, 1027, 1029, 1032, 1074, 1080, 1082, 1083, 1084, 1085, 1099, 1126, 1128, 1156, 1177, 1219, 1232, 1233, 1248, 1261, 1263, 1267, 1268, 1270, 1303, 1306, 1323, 1329, 1330, 1341, 1343, 1348, 1362, 1367, 1372, 1373, 1398, 1402, 1403, 1406, 1407, 1413, 1418, 1419, 1427, 1442, 1444, 1445, 1450, 1470, 1471, 1472, 1482, 1487, 1500, 1505, 1506, 1507, 1516, 1520, 1526, 1527, 1529, 1530, 1544, 1547, 1552, 1569, 1572, 1573, 1574, 1575, 1576, 1583, 1590, 1601, 1603, 1605, 1610, 1611, 1612, 1613, 1614, 1615, 1616, 1618, 1620, 1621, 1622, 1624, 1626, 1627, 1629, 1631, 1633, 1635, 1636, 1637, 1638, 1639, 1640, 1644, 1648, 1652, 1656, 1658, 1659, 1660, 1662, 1663, 1664, 1665, 1666, 1667, 1672, 1673, 1677, 1678, 1680, 1681, 1682, 1684, 1686, 1690, 1691, 1692, 1693, 1695, 1696, 1708, 1709, 1710, 1711, 1713, 1719, 1720, 1742, 1746, 1755, 1760, 1762, 1776, 1777, 1779, 1780, 1787, 1798, 1806, 1809, 1811, 1813, 1815, 1816, 1817, 1818, 1819, 1820, 1821, 1823, 1825, 1827, 1831, 1832, 1833, 1834, 1836, 1837, 1838, 1839, 1840, 1841, 1844, 1845, 1848, 1850, 1853, 1875, 1880, 1885, 1893, 1894, 1911, 1912, 1915, 1916, 1917, 1918, 1919, 1920, 1925, 1926, 1929, 1932, 1933, 1934, 1935, 1936, 1937, 1939

Solved by both Maple and Mathematica 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 17, 18, 19, 20, 21, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 39, 40, 41, 42, 43, 44, 45, 46, 51, 52, 53, 54, 57, 58, 59, 60, 61, 62, 64, 65, 67, 68, 69, 70, 71, 72, 73, 75, 76, 77, 78, 84, 85, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97, 98, 99, 100, 101, 102, 103, 104, 105, 106, 107, 108, 109, 111, 112, 113, 114, 115, 116, 117, 118, 119, 120, 122, 123, 124, 125, 126, 128, 129, 130, 131, 132, 133, 134, 135, 136, 137, 138, 139, 140, 141, 142, 143, 144, 145, 146, 147, 148, 149, 150, 151, 152, 153, 154, 155, 156, 157, 158, 159, 160, 161, 162, 163, 164, 165, 166, 167, 168, 169, 170, 171, 172, 173, 174, 175, 176, 177, 178, 179, 180, 181, 182, 183, 184, 185, 186, 187, 189, 190, 191, 192, 193, 194, 195, 196, 197, 198, 199, 200, 201, 204, 207, 208, 209, 210, 211, 212, 213, 214, 215, 216, 217, 218, 220, 221, 222, 223, 224, 225, 226, 227, 228, 229, 230, 231, 232, 233, 235, 236, 238, 239, 240, 241, 242, 243, 244, 245, 246, 247, 248, 249, 251, 252, 254, 255, 256, 257, 258, 259, 260, 261, 262, 263, 264, 267, 268, 270, 271, 272, 273, 274, 275, 276, 277, 278, 279, 280, 281, 282, 283, 284, 285, 286, 287, 288, 289, 290, 291, 292, 293, 294, 295, 296, 297, 298, 299, 300, 301, 302, 303, 304, 305, 306, 307, 308, 309, 310, 311, 312, 313, 314, 315, 316, 317, 318, 319, 320, 321, 322, 323, 324, 325, 326, 327, 328, 329, 330, 332, 333, 334, 335, 336, 337, 338, 339, 341, 342, 343, 344, 345, 346, 347, 348, 349, 350, 351, 352, 353, 354, 355, 356, 357, 358, 359, 360, 361, 362, 363, 364, 366, 369, 371, 372, 373, 374, 375, 376, 377, 378, 379, 380, 381, 382, 384, 386, 387, 388, 389, 390, 391, 392, 393, 396, 397, 398, 399, 401,

403, 405, 406, 407, 408, 409, 410, 411, 412, 415, 417, 418, 419, 420, 421, 422, 423, 424, 425, 426, 427, 430, 431, 432, 433, 434, 435, 436, 437, 438, 439, 440, 441, 442, 443, 444, 445, 446, 447, 448, 449, 450, 453, 454, 455, 456, 457, 458, 459, 462, 463, 464, 466, 469, 471, 472, 473, 474, 475, 477, 478, 481, 483, 484, 486, 488, 490, 491, 492, 493, 495, 496, 497, 498, 499, 500, 501, 502, 505, 511, 512, 514, 516, 517, 518, 519, 520, 521, 522, 525, 526, 529, 536, 539, 540, 545, 547, 548, 549, 551, 552, 553, 554, 556, 557, 558, 559, 560, 563, 564, 565, 568, 569, 571, 573, 574, 577, 578, 579, 580, 581, 582, 583, 584, 585, 586, 587, 588, 589, 590, 591, 593, 594, 595, 596, 597, 598, 599, 600, 601, 602, 603, 604, 605, 606, 608, 609, 610, 611, 612, 614, 615, 616, 617, 618, 619, 621, 622, 623, 624, 625, 626, 627, 628, 629, 630, 631, 632, 633, 634, 635, 636, 637, 641, 642, 643, 644, 645, 646, 647, 648, 649, 650, 651, 652, 653, 654, 655, 656, 657, 658, 659, 660, 661, 662, 663, 664, 665, 666, 667, 668, 669, 670, 671, 673, 674, 675, 676, 677, 678, 679, 680, 681, 682, 683, 684, 685, 686, 687, 688, 689, 690, 691, 692, 693, 694, 695, 697, 698, 699, 700, 705, 709, 711, 712, 713, 715, 716, 717, 718, 719, 720, 721, 722, 723, 724, 725, 726, 727, 728, 729, 731, 732, 734, 736, 737, 738, 739, 740, 741, 742, 744, 748, 749, 750, 751, 753, 754, 755, 756, 757, 758, 760, 761, 762, 763, 764, 767, 768, 770, 771, 772, 773, 774, 775, 777, 778, 779, 780, 781, 787, 793, 794, 795, 796, 797, 798, 799, 800, 801, 802, 803, 804, 805, 806, 808, 809, 810, 811, 812, 813, 814, 815, 816, 817, 818, 819, 820, 821, 822, 823, 824, 825, 826, 827, 828, 829, 830, 831, 832, 833, 834, 836, 838, 839, 840, 841, 842, 843, 844, 845, 846, 847, 848, 849, 850, 851, 852, 853, 856, 857, 858, 859, 860, 861, 863, 864, 866, 867, 868, 869, 870, 871, 872, 873, 874, 875, 876, 877, 879, 880, 881, 882, 883, 884, 886, 887, 888, 890, 891, 893, 895, 896, 897, 898, 899, 900, 901, 902, 903, 904, 905, 906, 907, 908, 910, 911, 914, 921, 924, 926, 927, 928, 930, 931, 933, 934, 935, 936, 937, 938, 939, 940, 941, 943, 944, 945, 946, 947, 948, 949, 950, 951, 952, 954, 955, 956, 957, 958, 959, 960, 962, 963, 964, 965, 966, 967, 968, 969, 970, 971, 972, 973, 974, 975, 976, 977, 978, 979, 980, 981, 982, 983, 984, 985, 986, 987, 988, 989, 990, 991, 992, 994, 995, 997, 998, 999, 1001, 1002, 1003, 1004, 1005, 1006, 1007, 1008, 1009, 1010, 1011, 1012, 1013, 1014, 1016, 1017, 1018, 1020, 1021, 1022, 1023, 1024, 1025, 1033, 1034, 1035, 1036, 1037, 1039, 1040, 1041, 1042, 1043, 1044, 1045, 1046, 1047, 1048, 1049, 1050, 1051, 1052, 1053, 1054, 1055, 1056, 1057, 1058, 1059, 1060, 1061, 1062, 1063, 1064, 1065, 1066, 1067, 1068, 1069, 1070, 1071, 1078, 1079, 1086, 1087, 1088, 1089, 1090, 1091, 1092, 1093, 1094, 1095, 1096, 1097, 1098, 1100, 1101, 1102, 1103, 1104, 1105, 1106, 1107, 1108, 1109, 1110, 1111, 1112, 1113, 1114, 1115, 1116, 1117, 1118, 1119, 1120, 1121, 1122, 1123, 1124, 1125, 1127, 1129, 1130, 1131, 1132, 1133, 1134, 1135, 1136, 1137, 1138, 1139, 1140, 1141, 1142, 1143, 1144, 1145, 1146, 1147, 1148, 1149, 1150, 1151, 1152, 1153, 1154, 1155, 1158, 1159, 1160, 1161, 1162, 1163, 1164, 1165, 1166, 1167, 1168, 1169, 1170, 1171, 1172, 1173, 1174, 1175, 1176, 1178, 1179, 1180, 1181, 1182, 1183, 1184, 1185, 1186, 1187, 1188, 1189, 1190, 1191, 1192, 1193, 1194, 1195, 1196, 1197, 1198, 1199, 1200, 1201, 1202, 1203, 1204, 1206, 1207, 1208, 1209, 1210, 1211, 1213, 1214, 1215, 1217, 1218, 1220, 1221, 1222, 1223, 1224, 1225, 1226, 1227, 1228, 1229, 1230, 1231, 1235, 1237, 1238, 1239, 1240, 1241, 1242, 1243, 1244, 1245, 1246, 1247, 1249, 1250, 1251, 1252, 1253, 1254, 1255, 1256, 1257, 1258, 1259, 1260, 1262, 1264, 1265,

1266, 1269, 1271, 1272, 1273, 1274, 1275, 1276, 1277, 1279, 1280, 1281, 1282, 1283, 1284, 1285, 1286, 1287, 1288, 1289, 1290, 1291, 1292, 1293, 1294, 1295, 1296, 1297, 1298, 1299, 1300, 1301, 1302, 1304, 1305, 1307, 1308, 1309, 1310, 1311, 1312, 1313, 1314, 1315, 1316, 1317, 1318, 1319, 1320, 1321, 1322, 1324, 1325, 1326, 1327, 1328, 1331, 1332, 1333, 1334, 1335, 1336, 1337, 1338, 1339, 1340, 1342, 1344, 1345, 1346, 1347, 1349, 1350, 1351, 1352, 1353, 1354, 1355, 1356, 1357, 1358, 1359, 1360, 1361, 1363, 1364, 1365, 1366, 1368, 1369, 1370, 1371, 1374, 1375, 1376, 1377, 1378, 1379, 1380, 1381, 1382, 1383, 1384, 1385, 1386, 1387, 1388, 1389, 1390, 1391, 1392, 1393, 1394, 1395, 1396, 1397, 1399, 1400, 1401, 1404, 1405, 1409, 1410, 1411, 1412, 1414, 1415, 1416, 1417, 1420, 1421, 1422, 1423, 1424, 1425, 1426, 1428, 1429, 1430, 1431, 1432, 1433, 1434, 1435, 1436, 1437, 1438, 1446, 1447, 1448, 1449, 1451, 1452, 1453, 1454, 1455, 1456, 1464, 1465, 1466, 1467, 1468, 1469, 1475, 1477, 1478, 1479, 1480, 1481, 1483, 1485, 1486, 1488, 1490, 1491, 1492, 1493, 1494, 1495, 1496, 1497, 1498, 1499, 1501, 1502, 1503, 1504, 1508, 1509, 1511, 1512, 1513, 1514, 1517, 1518, 1519, 1521, 1522, 1523, 1524, 1525, 1528, 1532, 1533, 1534, 1535, 1536, 1537, 1538, 1539, 1545, 1546, 1548, 1549, 1550, 1551, 1553, 1554, 1555, 1556, 1557, 1558, 1559, 1560, 1561, 1562, 1563, 1564, 1565, 1566, 1567, 1568, 1570, 1571, 1577, 1578, 1579, 1580, 1584, 1585, 1587, 1588, 1589, 1591, 1592, 1594, 1597, 1600, 1602, 1604, 1607, 1630, 1632, 1641, 1646, 1647, 1650, 1651, 1653, 1654, 1655, 1657, 1661, 1668, 1669, 1670, 1671, 1674, 1676, 1679, 1683, 1687, 1688, 1689, 1694, 1697, 1699, 1700, 1701, 1703, 1707, 1712, 1714, 1715, 1716, 1717, 1718, 1722, 1723, 1724, 1725, 1726, 1727, 1728, 1730, 1731, 1733, 1736, 1740, 1741, 1743, 1744, 1745, 1747, 1748, 1749, 1750, 1752, 1753, 1754, 1756, 1758, 1759, 1763, 1764, 1765, 1766, 1767, 1768, 1769, 1770, 1771, 1772, 1773, 1774, 1775, 1778, 1781, 1782, 1783, 1784, 1785, 1786, 1790, 1791, 1792, 1793, 1794, 1795, 1796, 1799, 1800, 1803, 1804, 1805, 1808, 1810, 1812, 1814, 1822, 1824, 1826, 1828, 1829, 1830, 1842, 1843, 1846, 1847, 1849, 1852, 1856, 1857, 1858, 1859, 1860, 1861, 1862, 1863, 1864, 1865, 1866, 1867, 1868, 1869, 1870, 1871, 1872, 1873, 1874, 1876, 1877, 1878, 1879, 1881, 1882, 1883, 1884, 1886, 1887, 1888, 1889, 1891, 1892, 1895, 1896, 1897, 1898, 1899, 1900, 1901, 1902, 1903, 1904, 1906, 1907, 1908, 1909, 1910, 1913, 1914, 1923, 1924, 1930, 1931, 1938

Both systems unable to solve 38, 47, 48, 49, 50, 55, 56, 74, 79, 82, 87, 110, 121, 202, 203, 205, 206, 219, 234, 237, 250, 253, 265, 269, 331, 340, 367, 368, 370, 383, 395, 460, 461, 480, 482, 485, 503, 506, 510, 531, 572, 575, 576, 733, 789, 790, 835, 837, 885, 894, 909, 1015, 1019, 1026, 1028, 1030, 1031, 1038, 1072, 1073, 1075, 1076, 1077, 1081, 1157, 1205, 1212, 1216, 1236, 1278, 1408, 1439, 1440, 1441, 1443, 1457, 1458, 1459, 1460, 1461, 1462, 1463, 1473, 1474, 1476, 1484, 1489, 1510, 1515, 1531, 1540, 1541, 1542, 1543, 1581, 1586, 1593, 1595, 1596, 1598, 1599, 1606, 1608, 1609, 1617, 1619, 1623, 1625, 1628, 1634, 1642, 1643, 1645, 1649, 1675, 1685, 1702, 1704, 1705, 1706, 1721, 1729, 1732, 1734, 1735, 1737, 1738, 1739, 1751, 1757, 1761, 1788, 1789, 1797, 1801, 1802, 1807, 1851, 1854, 1855, 1890, 1905, 1921, 1922, 1927, 1928, 1940

2 Problems table lookup

Final conclusion table for each equation is given by table 3 below. Clicking on the problem opens a new page that shows the result and links to download each problem as well.

Table 3: Breakdown of results for each Kamke differential equation

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1	✓	0.658	1117	✓	0.022	1089	Linear first order, To Do
Kamke 2	✓	0.014	34	✓	0.013	25	Linear first order, integrating factor $y'(x)+ay(x)=f(x)$
Kamke 3	✓	0.033	40	✓	0.021	37	Linear first order, integrating factor $y'(x)+ay(x)=f(x)$
Kamke 4	✓	0.009	30	✓	0.005	18	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 5	✓	2.39	38	✓	0.087	21	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 6	✓	0.023	18	✓	0.021	15	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 7	✓	0.023	23	✓	0.006	13	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 8	✓	0.026	17	✓	0.011	13	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 9	✓	0.018	19	✓	0.011	14	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 10	✓	0.009	18	✓	0.01	15	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 11	✓	0.457	62	✓	0.017	24	Linear first order, integrating factor $y'(x)+g(x)y(x)=f(x)$
Kamke 12	✓	0.029	34	✓	0.03	8	Non-linear first order, Riccati, separable $y'(x)+y^2(x)=1$
Kamke 13	✓	0.024	79	✓	0.22	79	Non-linear first order, Riccati, transform to second order Airy ODE using $y=-\frac{u'(x)}{uR(x)}$
Kamke 14	✓	0.013	254	✓	0.109	187	Non-linear first order, Riccati, transform to second order Airy ODE using $y=-\frac{u'(x)}{uR(x)}$
Kamke 15	✓	0.02	25	✓	0.29	35	Non-linear first order, Riccati, transform to separable first order
Kamke 16	✗	0	0	✓	0.146	49	Non-linear first order, Riccati, transform to first order separable using $y=y_p+\frac{1}{u}$
Kamke 17	✓	0.024	34	✓	0.109	24	Non-linear first order, Riccati, transform to second order standard ODE using $y=-\frac{u'(x)}{uR(x)}$

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 18	✓	0.022	50	✓	0.07	39	Non-linear first order, Riccati, transform to first order ODE solved using integrating factor using transformtion $y = y_p + \frac{1}{u}$
Kamke 19	✓	0.011	30	✓	0.037	16	Non-linear first order, Riccati, transform to first order separable
Kamke 20	✓	0.734	48	✓	0.082	34	Non-linear first order, Riccati, transform to Bernoulli first order non-linear first order then solve Bernoulli
Kamke 21	✓	6.39	69	✓	0.141	25	Non-linear first order, Riccati, transform to first order ODE solved using integrating factor using transformtion $y = y_p + \frac{1}{u}$
Kamke 22	✗	0	0	✓	0.408	128	Non-linear first order, Riccati, transform to first order ODE solved using integrating factor using transformtion $y = y_p + \frac{1}{u}$
Kamke 23	✓	0.023	43	✓	0.036	23	Non-linear first order, Riccati, Separable
Kamke 24	✓	0.014	277	✓	0.076	201	Non-linear first order, Riccati, transform to second order Emden-Fowler ODE using $y = -\frac{u'(x)}{uR(x)}$ solution in terms of Bessel functions
Kamke 25	✓	0.233	1835	✓	0.309	348	Non-linear first order, Riccati. To do

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Table 3 – continued from previous page

#	Mathematica			Maple			note on solution
	solved	cpu	leaf	solved	cpu	leaf	
Kamke 26	✓	0.077	68	✓	0.064	45	Non-Linear first order, Riccati, transform to second order standard ODE using $y=-\frac{u'(x)}{uR(x)}$
Kamke 27	✓	0.045	120	✓	0.196	72	Non-linear first order, Riccati, transform to Bernoulli first order non-linear first order then solve Bernoulli
Kamke 28	✓	0.048	96	✓	0.095	51	Non-linear first order, Riccati, transform to Bernoulli first order non-linear first order then solve Bernoulli
Kamke 29	✓	0.023	39	✓	0.012	19	Non-linear first order, Bernoulli
Kamke 30	✓	0.066	230	✓	0.085	54	Non-Linear first order, Riccati, transform to second order Bessel like ODE using $y=-\frac{u'(x)}{uR(x)}$, solution uses Bessel functions
Kamke 31	✓	0.029	21	✓	0.036	23	Non-Linear first order, Riccati, separable
Kamke 32	✓	0.142	34	✓	0.279	28	Non-Linear first order, Riccati, has particular solution, solution using $y=y_p+\frac{1}{u}$ leads to first order solved using integrating factor
Kamke 33	✓	27.278	157	✓	0.544	58	Non-Linear first order, Riccati. Complicated algebra, will do later
Kamke 34	✓	0.508	51	✓	0.026	28	Non-Linear first order, Bernoulli. Standard method.

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 35	✓	0.058	60	✓	0.042	35	Non-Linear first order, Riccati. Transform to second order ODE using $y(x) = -\frac{u'(x)}{u(x)R(x)}$
Kamke 36	✓	0.218	195	✓	0.098	62	Non-Linear first order of Abel first kind with None constant invariant. Transform to a reverse Riccati then Solve the resulting second order Airy ODE, and transform solution back. Lots of algebra involved. Hardest ODE so far
Kamke 37	✓	0.665	78	✓	0.096	50	To Do
Kamke 38	✗	0	0	✗	0	0	To Do
Kamke 39	✓	0.037	54	✓	0.014	30	To Do
Kamke 40	✓	0.236	185	✓	0.083	48	To Do
Kamke 41	✓	0.079	103	✓	0.207	103	To Do
Kamke 42	✓	0.939	485	✓	0.027	40	To Do
Kamke 43	✓	8.652	490	✓	1.825	373	To Do
Kamke 44	✓	0.017	72	✓	0.02	53	Non-Linear first order Bernoulli. Solved using standard method of solving Bernoulli.
Kamke 45	✓	0.518	133	✓	0.122	123	To Do
Kamke 46	✓	0.246	258	✓	0.095	956	To Do
Kamke 47	✗	0	0	✗	0	0	To Do
Kamke 48	✗	0	0	✗	0	0	To Do
Kamke 49	✗	0	0	✗	0	0	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 50	✗	0	0	✗	0	0	To Do
Kamke 51	✓	0.742	354	✓	0.217	237	To Do
Kamke 52	✓	144.8	115	✓	0.205	61	To Do
Kamke 53	✓	79.52	95	✓	0.062	281	To Do
Kamke 54	✓	0.117	74	✓	0.159	38	To Do
Kamke 55	✗	0	0	✗	0	0	To Do
Kamke 56	✗	0	0	✗	0	0	To Do
Kamke 57	✓	98.581	283	✓	0.071	31	To Do
Kamke 58	✓	0.155	119	✓	0.071	68	To Do
Kamke 59	✓	0.181	96	✓	0.05	26	To Do
Kamke 60	✓	0.049	55	✓	0.016	29	Non-Linear first order, separable.
Kamke 61	✓	0.177	75	✓	0.014	50	To Do
Kamke 62	✓	3.839	40	✓	0.412	34	Non-Linear first order, special transformation makes it exact differential.
Kamke 63	✗	0	0	✓	0.141	35	To Do
Kamke 64	✓	0.177	269	✓	0.082	124	To Do
Kamke 65	✓	1.496	312	✓	0.042	47	To Do
Kamke 66	✗	0	0	✓	0.07	40	To Do
Kamke 67	✓	0.17	14	✓	0.014	51	To Do
Kamke 68	✓	0.837	373	✓	0.063	77	To Do
Kamke 69	✓	52.577	12750	✓	0.146	111	To Do
Kamke 70	✓	158.63	23353	✓	0.163	113	To Do
Kamke 71	✓	2.314	2237	✓	0.13	113	To Do
Kamke 72	✓	0.821	87	✓	0.012	64	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 73	✓	1.006	733	✓	0.349	91	To Do
Kamke 74	✗	0	0	✗	0	0	To Do
Kamke 75	✓	0.049	18	✓	0.132	20	Non-Linear first order, Separable
Kamke 76	✓	0.21	116	✓	0.043	41	Non-Linear first order, Separable, integral requires the tangent half-angle substitution (Weierstrass substitution)
Kamke 77	✓	0.315	124	✓	0.068	54	Non-Linear first order, transform to Separable, becomes same as problem 76 above. Transform back after soluion.
Kamke 78	✓	0.831	1317	✓	2.176	89	Non-Linear first order, transform to Separable, integral requires the tangent half-angle substitution (Weierstrass substitution). Kamke calls this d'Alembertsche differential equation
Kamke 79	✗	0	0	✗	0	0	To Do
Kamke 80	✗	0	0	✓	1.497	41	To Do
Kamke 81	✗	0	0	✓	1.296	78	To Do
Kamke 82	✗	0	0	✗	0	0	To Do
Kamke 83	✗	0	0	✓	0.449	44	To Do
Kamke 84	✓	8.731	244	✓	0.037	37	To Do
Kamke 85	✓	155.858	235	✓	0.468	153	To Do
Kamke 86	✗	0	0	✓	0.499	52	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 87	✗	0	0	✗	0	0	To Do
Kamke 88	✓	0.283	2831	✓	0.233	256	To Do
Kamke 89	✓	0.032	48	✓	0.016	56	To Do
Kamke 90	✓	0.015	24	✓	0.012	17	To Do
Kamke 91	✓	0.007	15	✓	0.006	11	To Do
Kamke 92	✓	0.014	15	✓	0.005	12	To Do
Kamke 93	✓	0.02	16	✓	0.015	12	To Do
Kamke 94	✓	0.015	25	✓	0.009	23	To Do
Kamke 95	✓	0.016	32	✓	0.068	27	To Do
Kamke 96	✓	0.024	33	✓	0.031	11	To Do
Kamke 97	✓	0.028	46	✓	0.03	25	To Do
Kamke 98	✓	0.026	442	✓	0.046	38	To Do
Kamke 99	✓	0.019	244	✓	0.119	171	To Do
Kamke 100	✓	0.009	157	✓	0.08	59	To Do
Kamke 101	✓	0.01	18	✓	0.01	16	To Do
Kamke 102	✓	0.02	36	✓	0.036	22	To Do
Kamke 103	✓	0.101	90	✓	0.033	29	To Do
Kamke 104	✓	0.018	43	✓	0.093	63	To Do
Kamke 105	✓	0.185	473	✓	0.337	844	To Do
Kamke 106	✓	0.038	40	✓	0.039	41	To Do
Kamke 107	✓	0.26	1415	✓	0.239	174	To Do
Kamke 108	✓	0.012	15	✓	0.011	13	To Do
Kamke 109	✓	0.012	17	✓	0.012	15	To Do
Kamke 110	✗	0	0	✗	0	0	To Do
Kamke 111	✓	0.284	55	✓	0.128	54	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 112	✓	0.022	13	✓	0.038	27	To Do
Kamke 113	✓	0.024	16	✓	0.028	33	To Do
Kamke 114	✓	0.021	12	✓	2.378	28	To Do
Kamke 115	✓	0.125	99	✓	0.227	49	To Do
Kamke 116	✓	0.46	143	✓	0.229	86	To Do
Kamke 117	✓	0.055	21	✓	0.119	20	To Do
Kamke 118	✓	0.012	13	✓	0.054	8	To Do
Kamke 119	✓	0.031	17	✓	0.09	14	To Do
Kamke 120	✓	0.052	20	✓	0.178	17	To Do
Kamke 121	✗	0	0	✗	0	0	To Do
Kamke 122	✓	0.124	21	✓	0.457	16	To Do
Kamke 123	✓	0.059	19	✓	0.051	44	To Do
Kamke 124	✓	0.027	16	✓	0.032	12	To Do
Kamke 125	✓	0.038	16	✓	0.062	14	To Do
Kamke 126	✓	15.337	112	✓	0.024	29	To Do
Kamke 127	✗	0	0	✓	0.11	39	To Do
Kamke 128	✓	4.314	39	✓	0.283	33	To Do
Kamke 129	✓	0.03	44	✓	0.027	33	To Do
Kamke 130	✓	0.007	21	✓	0.007	15	To Do
Kamke 131	✓	0.018	20	✓	0.193	31	To Do
Kamke 132	✓	0.013	115	✓	0.028	153	To Do
Kamke 133	✓	0.008	27	✓	0.01	16	To Do
Kamke 134	✓	0.013	27	✓	0.009	17	To Do
Kamke 135	✓	0.008	14	✓	0.006	11	To Do
Kamke 136	✓	0.014	28	✓	0.018	18	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 137	✓	0.01	16	✓	0.013	14	To Do
Kamke 138	✓	0.015	13	✓	0.035	11	To Do
Kamke 139	✓	0.133	821	✓	0.142	219	To Do
Kamke 140	✓	0.01	17	✓	0.045	20	To Do
Kamke 141	✓	0.028	67	✓	0.051	51	To Do
Kamke 142	✓	0.192	113	✓	0.094	52	To Do
Kamke 143	✓	0.01	51	✓	0.049	41	To Do
Kamke 144	✓	0.17	1787	✓	0.118	219	To Do
Kamke 145	✓	0.382	267	✓	0.122	117	To Do
Kamke 146	✓	0.52	78	✓	0.176	84	To Do
Kamke 147	✓	0.519	343	✓	0.215	178	To Do
Kamke 148	✓	0.014	30	✓	0.01	16	To Do
Kamke 149	✓	0.013	27	✓	0.011	20	To Do
Kamke 150	✓	0.009	30	✓	0.006	23	To Do
Kamke 151	✓	0.435	203	✓	0.072	85	To Do
Kamke 152	✓	0.238	40	✓	0.859	25	To Do
Kamke 153	✓	0.017	21	✓	0.014	20	To Do
Kamke 154	✓	0.015	26	✓	0.01	16	To Do
Kamke 155	✓	0.019	46	✓	0.114	14	To Do
Kamke 156	✓	0.016	21	✓	0.017	20	To Do
Kamke 157	✓	0.089	158	✓	0.279	231	To Do
Kamke 158	✓	0.037	31	✓	0.017	22	To Do
Kamke 159	✓	0.018	22	✓	0.125	13	To Do
Kamke 160	✓	0.021	27	✓	0.031	21	To Do
Kamke 161	✓	0.015	53	✓	0.018	27	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 162	✓	0.266	133	✓	0.199	58	To Do
Kamke 163	✓	0.014	43	✓	0.038	26	To Do
Kamke 164	✓	0.082	131	✓	0.217	102	To Do
Kamke 165	✓	0.018	22	✓	0.022	17	To Do
Kamke 166	✓	0.088	71	✓	0.174	97	To Do
Kamke 167	✓	0.023	35	✓	0.035	20	To Do
Kamke 168	✓	0.096	234	✓	0.191	140	To Do
Kamke 169	✓	2.264	149	✓	0.158	153	To Do
Kamke 170	✓	0.023	43	✓	0.018	23	To Do
Kamke 171	✓	0.011	17	✓	0.01	15	To Do
Kamke 172	✓	0.042	35	✓	0.275	26	To Do
Kamke 173	✓	0.017	29	✓	0.046	27	To Do
Kamke 174	✓	0.008	17	✓	0.005	13	To Do
Kamke 175	✓	0.021	24	✓	0.025	20	To Do
Kamke 176	✓	0.127	82	✓	0.103	30	To Do
Kamke 177	✓	0.018	22	✓	0.026	17	To Do
Kamke 178	✓	0.072	62	✓	0.122	63	To Do
Kamke 179	✓	1.683	2816	✓	0.167	112	To Do
Kamke 180	✓	0.124	132	✓	0.052	58	To Do
Kamke 181	✓	0.013	347	✓	0.082	28	To Do
Kamke 182	✓	0.175	96	✓	0.14	18	To Do
Kamke 183	✓	0.015	22	✓	0.013	18	To Do
Kamke 184	✓	1.516	704	✓	0.385	493	To Do
Kamke 185	✓	0.385	123	✓	0.059	63	To Do
Kamke 186	✓	0.031	19	✓	0.037	17	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 187	✓	0.074	328	✓	0.053	60	To Do
Kamke 188	✗	0	0	✓	0.028	32	To Do
Kamke 189	✓	82.158	90	✓	0.247	60	To Do
Kamke 190	✓	0.052	55	✓	0.01	29	To Do
Kamke 191	✓	0.032	52	✓	0.017	16	To Do
Kamke 192	✓	0.03	57	✓	0.018	36	To Do
Kamke 193	✓	0.009	16	✓	0.007	14	To Do
Kamke 194	✓	0.078	98	✓	0.024	23	To Do
Kamke 195	✓	0.059	27	✓	0.124	28	To Do
Kamke 196	✓	0.058	53	✓	0.153	29	To Do
Kamke 197	✓	0.043	98	✓	0.082	237	To Do
Kamke 198	✓	0.026	15	✓	0.013	13	To Do
Kamke 199	✓	0.187	15	✓	0.165	102	To Do
Kamke 200	✓	0.053	77	✓	0.062	53	To Do
Kamke 201	✓	0.08	38	✓	0.04	23	To Do
Kamke 202	✗	0	0	✗	0	0	To Do
Kamke 203	✗	0	0	✗	0	0	To Do
Kamke 204	✓	0.071	70	✓	0.316	91	To Do
Kamke 205	✗	0	0	✗	0	0	To Do
Kamke 206	✗	0	0	✗	0	0	To Do
Kamke 207	✓	0.013	47	✓	0.02	37	To Do
Kamke 208	✓	0.072	118	✓	0.073	106	To Do
Kamke 209	✓	0.023	84	✓	0.011	21	To Do
Kamke 210	✓	0.017	47	✓	0.019	33	To Do
Kamke 211	✓	38.855	40	✓	0.032	31	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 212	✓	22.607	92	✓	0.135	30	To Do
Kamke 213	✓	0.101	71	✓	0.713	66	To Do
Kamke 214	✓	0.11	78	✓	0.161	48	To Do
Kamke 215	✓	0.121	80	✓	0.184	51	To Do
Kamke 216	✓	0.102	82	✓	0.174	51	To Do
Kamke 217	✓	0.02	29	✓	0.03	23	To Do
Kamke 218	✓	0.101	257	✓	0.203	57	To Do
Kamke 219	✗	0	0	✗	0	0	To Do
Kamke 220	✓	0.015	57	✓	0.021	43	To Do
Kamke 221	✓	0.019	35	✓	0.051	21	To Do
Kamke 222	✓	0.059	65	✓	0.052	32	To Do
Kamke 223	✓	0.027	55	✓	0.169	51	To Do
Kamke 224	✓	0.02	29	✓	0.058	35	To Do
Kamke 225	✓	0.019	33	✓	0.046	20	To Do
Kamke 226	✓	0.018	35	✓	0.049	21	To Do
Kamke 227	✓	0.013	107	✓	0.183	33	To Do
Kamke 228	✓	0.296	3357	✓	0.329	271	To Do
Kamke 229	✓	0.013	121	✓	0.174	32	To Do
Kamke 230	✓	0.123	96	✓	0.042	100	To Do
Kamke 231	✓	2.548	252	✓	0.215	178	To Do
Kamke 232	✓	0.01	56	✓	0.016	39	To Do
Kamke 233	✓	0.025	38	✓	0.023	30	To Do
Kamke 234	✗	0	0	✗	0	0	To Do
Kamke 235	✓	0.043	40	✓	0.051	30	To Do
Kamke 236	✓	0.017	114	✓	0.063	141	To Do

Continued on next page

Table 3 – continued from previous page

#	Mathematica			Maple			note on solution
	solved	cpu	leaf	solved	cpu	leaf	
Kamke 237	✗	0	0	✗	0	0	To Do
Kamke 238	✓	0.045	192	✓	0.08	91	To Do
Kamke 239	✓	0.03	54	✓	0.176	59	To Do
Kamke 240	✓	0.01	41	✓	0.021	34	To Do
Kamke 241	✓	0.011	41	✓	0.014	33	To Do
Kamke 242	✓	0.016	60	✓	0.015	39	To Do
Kamke 243	✓	14.93	487	✓	0.137	391	To Do
Kamke 244	✓	14.896	484	✓	0.12	391	To Do
Kamke 245	✓	0.406	1453	✓	0.322	31	To Do
Kamke 246	✓	0.032	80	✓	0.168	63	To Do
Kamke 247	✓	14.874	693	✓	0.222	517	To Do
Kamke 248	✓	0.015	106	✓	0.022	75	To Do
Kamke 249	✓	5.015	115	✓	0.209	232	To Do
Kamke 250	✗	0	0	✗	0	0	To Do
Kamke 251	✓	0.013	60	✓	0.02	51	To Do
Kamke 252	✓	14.778	819	✓	0.873	1338	To Do
Kamke 253	✗	0	0	✗	0	0	To Do
Kamke 254	✓	0.017	99	✓	0.031	59	To Do
Kamke 255	✓	4.83	30	✓	0.226	74	To Do
Kamke 256	✓	0.02	21	✓	0.045	31	To Do
Kamke 257	✓	0.363	38	✓	0.113	98	To Do
Kamke 258	✓	0.014	43	✓	0.021	33	To Do
Kamke 259	✓	0.02	50	✓	0.026	51	To Do
Kamke 260	✓	0.015	80	✓	0.033	59	To Do
Kamke 261	✓	0.939	32	✓	0.156	18	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 262	✓	0.067	101	✓	0.317	65	To Do
Kamke 263	✓	0.042	121	✓	0.148	173	To Do
Kamke 264	✓	0.36	680	✓	0.531	574	To Do
Kamke 265	✗	0	0	✗	0	0	To Do
Kamke 266	✗	0	0	✓	1.716	55	To Do
Kamke 267	✓	0.048	36	✓	0.023	32	To Do
Kamke 268	✓	0.977	140	✓	0.099	118	To Do
Kamke 269	✗	0	0	✗	0	0	To Do
Kamke 270	✓	0.022	327	✓	0.025	319	To Do
Kamke 271	✓	0.116	370	✓	0.185	352	To Do
Kamke 272	✓	0.05	42	✓	0.151	43	To Do
Kamke 273	✓	0.026	297	✓	0.023	401	To Do
Kamke 274	✓	0.037	411	✓	0.031	657	To Do
Kamke 275	✓	0.035	18	✓	0.104	30	To Do
Kamke 276	✓	0.037	61	✓	0.064	47	To Do
Kamke 277	✓	0.022	53	✓	0.35	41	To Do
Kamke 278	✓	0.075	39	✓	0.058	28	To Do
Kamke 279	✓	0.796	107	✓	0.18	116	To Do
Kamke 280	✓	0.047	21	✓	0.054	24	To Do
Kamke 281	✓	0.067	75	✓	0.069	55	To Do
Kamke 282	✓	0.176	2129	✓	0.235	71	To Do
Kamke 283	✓	0.058	477	✓	0.069	407	To Do
Kamke 284	✓	0.035	59	✓	0.151	21	To Do
Kamke 285	✓	0.035	402	✓	0.177	432	To Do
Kamke 286	✓	0.202	3501	✓	1.803	1337	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 287	✓	0.92	77	✓	0.074	56	To Do
Kamke 288	✓	0.024	534	✓	0.031	579	To Do
Kamke 289	✓	0.018	115	✓	0.034	115	To Do
Kamke 290	✓	0.083	831	✓	0.203	1388	To Do
Kamke 291	✓	0.526	39	✓	0.17	50	To Do
Kamke 292	✓	61.716	760	✓	0.052	115	To Do
Kamke 293	✓	0.101	661	✓	0.373	35	To Do
Kamke 294	✓	0.035	71	✓	0.108	112	To Do
Kamke 295	✓	0.037	31	✓	0.234	29	To Do
Kamke 296	✓	0.6	102	✓	0.779	135	To Do
Kamke 297	✓	0.056	216	✓	0.332	29	To Do
Kamke 298	✓	0.01	72	✓	0.017	73	To Do
Kamke 299	✓	0.022	371	✓	0.183	276	To Do
Kamke 300	✓	0.011	99	✓	0.019	83	To Do
Kamke 301	✓	0.041	64	✓	0.206	25	To Do
Kamke 302	✓	0.018	70	✓	0.153	133	To Do
Kamke 303	✓	0.048	25	✓	0.204	34	To Do
Kamke 304	✓	45.176	59	✓	0.225	44	To Do
Kamke 305	✓	0.102	1277	✓	0.023	21	To Do
Kamke 306	✓	0.053	201	✓	0.382	231	To Do
Kamke 307	✓	0.028	149	✓	0.052	125	To Do
Kamke 308	✓	0.009	55	✓	0.017	37	To Do
Kamke 309	✓	0.015	151	✓	0.04	113	To Do
Kamke 310	✓	0.048	159	✓	0.22	125	To Do
Kamke 311	✓	0.177	2201	✓	0.191	50	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 312	✓	0.252	204	✓	1.655	240	To Do
Kamke 313	✓	0.089	537	✓	0.22	748	To Do
Kamke 314	✓	0.045	188	✓	0.051	158	To Do
Kamke 315	✓	0.113	368	✓	0.089	376	To Do
Kamke 316	✓	0.041	48	✓	0.053	53	To Do
Kamke 317	✓	0.333	23	✓	0.124	29	To Do
Kamke 318	✓	0.152	4284	✓	0.022	28	To Do
Kamke 319	✓	0.025	302	✓	0.036	35	To Do
Kamke 320	✓	0.06	76	✓	0.095	78	To Do
Kamke 321	✓	0.183	47	✓	0.173	42	To Do
Kamke 322	✓	0.212	2077	✓	0.03	29	To Do
Kamke 323	✓	0.047	463	✓	0.135	630	To Do
Kamke 324	✓	0.036	723	✓	0.137	815	To Do
Kamke 325	✓	0.054	139	✓	0.508	124	To Do
Kamke 326	✓	4.932	13289	✓	0.494	160	To Do
Kamke 327	✓	0.404	669	✓	0.175	583	To Do
Kamke 328	✓	0.099	42	✓	0.193	33	To Do
Kamke 329	✓	0.331	102	✓	0.355	71	To Do
Kamke 330	✓	32.466	49	✓	0.03	22	To Do
Kamke 331	✗	0	0	✗	0	0	To Do
Kamke 332	✓	0.083	24	✓	0.014	33	To Do
Kamke 333	✓	0.17	72	✓	0.102	32	To Do
Kamke 334	✓	0.037	39	✓	0.025	19	To Do
Kamke 335	✓	0.18	75	✓	0.011	50	To Do
Kamke 336	✓	0.063	53	✓	0.033	41	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 337	✓	0.059	52	✓	0.059	28	To Do
Kamke 338	✓	102.971	17681	✓	0.744	129	To Do
Kamke 339	✓	0.108	27	✓	0.183	27	To Do
Kamke 340	✗	0	0	✗	0	0	To Do
Kamke 341	✓	0.054	33	✓	0.065	30	To Do
Kamke 342	✓	0.265	163	✓	0.04	17	To Do
Kamke 343	✓	0.039	35	✓	0.047	27	To Do
Kamke 344	✓	0.021	23	✓	0.026	19	To Do
Kamke 345	✓	0.043	35	✓	0.063	36	To Do
Kamke 346	✓	0.058	24	✓	0.276	19	To Do
Kamke 347	✓	0.126	32	✓	0.153	16	To Do
Kamke 348	✓	0.05	17	✓	0.101	15	To Do
Kamke 349	✓	0.042	15	✓	0.033	17	To Do
Kamke 350	✓	0.578	53	✓	1.077	226	To Do
Kamke 351	✓	0.37	61	✓	0.504	55	To Do
Kamke 352	✓	0.134	43	✓	0.302	33	To Do
Kamke 353	✓	0.021	14	✓	0.06	12	To Do
Kamke 354	✓	0.066	145	✓	0.042	108	To Do
Kamke 355	✓	0.048	17	✓	0.1	15	To Do
Kamke 356	✓	0.065	21	✓	0.122	19	To Do
Kamke 357	✓	0.308	35	✓	0.58	13	To Do
Kamke 358	✓	0.045	29	✓	0.072	11	To Do
Kamke 359	✓	0.059	45	✓	0.051	28	To Do
Kamke 360	✓	53.007	6218	✓	0.2	48	To Do
Kamke 361	✓	0.208	31	✓	0.253	22	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 362	✓	0.068	23	✓	0.231	23	To Do
Kamke 363	✓	0.036	33	✓	0.067	35	To Do
Kamke 364	✓	0.065	31	✓	0.106	23	To Do
Kamke 365	✗	0	0	✓	0.304	42	To Do
Kamke 366	✓	201.488	88	✓	0.071	45	To Do
Kamke 367	✗	0	0	✗	0	0	To Do
Kamke 368	✗	0	0	✗	0	0	To Do
Kamke 369	✓	0.049	107	✓	0.728	68	To Do
Kamke 370	✗	0	0	✗	0	0	To Do
Kamke 371	✓	0.026	37	✓	0.676	20	To Do
Kamke 372	✓	0.006	27	✓	0.661	232	To Do
Kamke 373	✓	0.1	71	✓	0.411	49	To Do
Kamke 374	✓	0.065	73	✓	0.659	85	To Do
Kamke 375	✓	0.044	71	✓	0.654	49	To Do
Kamke 376	✓	0.322	110	✓	1.237	219	To Do
Kamke 377	✓	0.005	19	✓	0.641	24	To Do
Kamke 378	✓	0.006	18	✓	0.638	20	To Do
Kamke 379	✓	0.005	18	✓	0.648	22	To Do
Kamke 380	✓	0.433	1757	✓	0.654	619	To Do
Kamke 381	✓	0.436	1757	✓	0.662	579	To Do
Kamke 382	✓	0.255	201	✓	0.661	146	To Do
Kamke 383	✗	0	0	✗	0	0	To Do
Kamke 384	✓	2.061	183	✓	0.025	50	To Do
Kamke 385	✗	0	0	✓	0.274	169	To Do
Kamke 386	✓	0.199	56	✓	0.429	27	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 387	✓	0.523	134	✓	0.676	115	To Do
Kamke 388	✓	0.628	53	✓	0.087	223	To Do
Kamke 389	✓	0.046	57	✓	0.57	71	To Do
Kamke 390	✓	2.112	142	✓	0.262	281	To Do
Kamke 391	✓	0.008	29	✓	0.007	22	To Do
Kamke 392	✓	0.249	27	✓	0.465	50	To Do
Kamke 393	✓	0.032	31	✓	0.119	77	To Do
Kamke 394	✗	0	0	✓	5.143	164	To Do
Kamke 395	✗	0	0	✗	0	0	To Do
Kamke 396	✓	0.01	29	✓	0.011	20	To Do
Kamke 397	✓	0.441	143	✓	0.353	128	To Do
Kamke 398	✓	0.802	258	✓	2.454	138	To Do
Kamke 399	✓	0.006	20	✓	0.019	22	To Do
Kamke 400	✗	0	0	✓	0.19	74	To Do
Kamke 401	✓	0.334	1093	✓	0.032	580	To Do
Kamke 402	✗	0	0	✓	0.177	101	To Do
Kamke 403	✓	0.297	116	✓	0.627	197	To Do
Kamke 404	✗	0	0	✓	0.266	389	To Do
Kamke 405	✓	0.967	53	✓	0.218	378	To Do
Kamke 406	✓	0.805	49	✓	0.079	262	To Do
Kamke 407	✓	0.017	51	✓	0.027	39	To Do
Kamke 408	✓	0.534	166	✓	0.053	73	To Do
Kamke 409	✓	30.764	66	✓	0.055	63	To Do
Kamke 410	✓	31.571	80	✓	0.056	64	To Do
Kamke 411	✓	0.554	181	✓	0.041	65	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 412	✓	27.581	16145	✓	0.04	146	To Do
Kamke 413	✗	0	0	✓	0.193	269	To Do
Kamke 414	✗	0	0	✓	0.199	269	To Do
Kamke 415	✓	0.214	133	✓	0.181	95	To Do
Kamke 416	✗	0	0	✓	0.059	136	To Do
Kamke 417	✓	0.401	430	✓	0.032	35	To Do
Kamke 418	✓	0.441	165	✓	0.038	42	To Do
Kamke 419	✓	1.473	9073	✓	0.04	109	To Do
Kamke 420	✓	1.711	11757	✓	0.038	689	To Do
Kamke 421	✓	0.032	27	✓	0.036	32	To Do
Kamke 422	✓	0.047	49	✓	0.038	30	To Do
Kamke 423	✓	0.079	59	✓	0.042	44	To Do
Kamke 424	✓	0.408	223	✓	0.072	193	To Do
Kamke 425	✓	0.261	59	✓	0.039	45	To Do
Kamke 426	✓	0.387	310	✓	0.038	51	To Do
Kamke 427	✓	0.626	479	✓	0.042	60	To Do
Kamke 428	✗	0	0	✓	0.07	66	To Do
Kamke 429	✗	0	0	✓	0.069	72	To Do
Kamke 430	✓	270.593	478	✓	1.064	1602	To Do
Kamke 431	✓	0.038	111	✓	0.149	62	To Do
Kamke 432	✓	1.744	64	✓	10.948	242	To Do
Kamke 433	✓	0.506	22	✓	0.235	34	To Do
Kamke 434	✓	0.034	27	✓	0.004	7	To Do
Kamke 435	✓	0.038	61	✓	0.233	22	To Do
Kamke 436	✓	0.035	26	✓	1.738	61	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 437	✓	0.282	47	✓	0.045	36	To Do
Kamke 438	✓	0.009	21	✓	0.011	17	To Do
Kamke 439	✓	0.015	49	✓	0.052	33	To Do
Kamke 440	✓	0.007	19	✓	0.011	15	To Do
Kamke 441	✓	0.073	65	✓	1.188	83	To Do
Kamke 442	✓	0.009	28	✓	0.012	21	To Do
Kamke 443	✓	0.552	1921	✓	1.733	221	To Do
Kamke 444	✓	0.148	75	✓	0.877	120	To Do
Kamke 445	✓	0.011	49	✓	0.015	35	To Do
Kamke 446	✓	0.494	201	✓	0.054	57	To Do
Kamke 447	✓	0.017	41	✓	0.026	33	To Do
Kamke 448	✓	0.09	109	✓	266.143	166	To Do
Kamke 449	✓	0.011	27	✓	0.012	23	To Do
Kamke 450	✓	0.444	26	✓	0.455	51	To Do
Kamke 451	✗	0	0	✓	0.054	78	To Do
Kamke 452	✗	0	0	✓	1.744	37	To Do
Kamke 453	✓	0.59	395	✓	0.742	229	To Do
Kamke 454	✓	0.155	118	✓	0.123	106	To Do
Kamke 455	✓	0.398	123	✓	0.18	66	To Do
Kamke 456	✓	0.123	79	✓	0.392	33	To Do
Kamke 457	✓	0.957	410	✓	0.778	45	To Do
Kamke 458	✓	0.064	139	✓	0.053	90	To Do
Kamke 459	✓	2.744	272	✓	0.614	65	To Do
Kamke 460	✗	0	0	✗	0	0	To Do
Kamke 461	✗	0	0	✗	0	0	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 462	✓	0.017	43	✓	0.026	27	To Do
Kamke 463	✓	0.019	47	✓	0.075	50	To Do
Kamke 464	✓	0.063	52	✓	0.443	70	To Do
Kamke 465	✗	0	0	✓	0.07	210	To Do
Kamke 466	✓	0.253	145	✓	0.391	71	To Do
Kamke 467	✗	0	0	✓	0.069	148	To Do
Kamke 468	✗	0	0	✓	0.081	181	To Do
Kamke 469	✓	0.329	247	✓	0.092	264	To Do
Kamke 470	✗	0	0	✓	0.29	87	To Do
Kamke 471	✓	0.009	47	✓	0.015	33	To Do
Kamke 472	✓	0.189	127	✓	0.475	121	To Do
Kamke 473	✓	0.379	165	✓	0.641	71	To Do
Kamke 474	✓	0.237	135	✓	1.041	152	To Do
Kamke 475	✓	0.069	57	✓	0.454	67	To Do
Kamke 476	✗	0	0	✓	0.304	87	To Do
Kamke 477	✓	0.306	146	✓	0.517	622	To Do
Kamke 478	✓	0.166	141	✓	0.079	88	To Do
Kamke 479	✗	0	0	✓	0.304	929	To Do
Kamke 480	✗	0	0	✗	0	0	To Do
Kamke 481	✓	0.01	49	✓	0.018	35	To Do
Kamke 482	✗	0	0	✗	0	0	To Do
Kamke 483	✓	0.162	71	✓	0.08	103	To Do
Kamke 484	✓	0.153	81	✓	0.08	115	To Do
Kamke 485	✗	0	0	✗	0	0	To Do
Kamke 486	✓	0.025	117	✓	0.098	54	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 487	✗	0	0	✓	0.417	100	To Do
Kamke 488	✓	0.35	85	✓	0.434	111	To Do
Kamke 489	✗	0	0	✓	2.375	551	To Do
Kamke 490	✓	0.584	70	✓	0.434	145	To Do
Kamke 491	✓	1.	79	✓	0.75	195	To Do
Kamke 492	✓	0.271	111	✓	0.421	122	To Do
Kamke 493	✓	8.46	553	✓	1.113	111	To Do
Kamke 494	✗	0	0	✓	0.173	161	To Do
Kamke 495	✓	0.109	83	✓	0.465	61	To Do
Kamke 496	✓	95.137	65	✓	0.241	130	To Do
Kamke 497	✓	0.172	203	✓	0.462	203	To Do
Kamke 498	✓	0.1	107	✓	0.696	99	To Do
Kamke 499	✓	0.288	212	✓	0.19	189	To Do
Kamke 500	✓	1.289	100	✓	0.936	220	To Do
Kamke 501	✓	31.22	913	✓	4.984	215	To Do
Kamke 502	✓	1.693	100	✓	0.39	195	To Do
Kamke 503	✗	0	0	✗	0	0	To Do
Kamke 504	✗	0	0	✓	0.824	247	To Do
Kamke 505	✓	0.013	73	✓	0.037	52	To Do
Kamke 506	✗	0	0	✗	0	0	To Do
Kamke 507	✓	29.247	443	✗	0	0	To Do
Kamke 508	✗	0	0	✓	1.838	60	To Do
Kamke 509	✗	0	0	✓	1.46	212	To Do
Kamke 510	✗	0	0	✗	0	0	To Do
Kamke 511	✓	1.57	229	✓	5.059	199	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 512	✓	4.577	725	✓	11.819	135	To Do
Kamke 513	✗	0	0	✓	2.854	1134	To Do
Kamke 514	✓	15.106	605	✓	0.228	87	To Do
Kamke 515	✗	0	0	✓	2.286	113	To Do
Kamke 516	✓	2.906	251	✓	1.141	72	To Do
Kamke 517	✓	3.006	281	✓	1.198	155	To Do
Kamke 518	✓	0.777	236	✓	0.195	126	To Do
Kamke 519	✓	1.754	473	✓	0.423	197	To Do
Kamke 520	✓	224.251	3323	✓	0.178	245	To Do
Kamke 521	✓	0.004	14	✓	0.031	33	To Do
Kamke 522	✓	0.005	20	✓	0.042	44	To Do
Kamke 523	✗	0	0	✓	0.057	231	To Do
Kamke 524	✗	0	0	✓	0.058	261	To Do
Kamke 525	✓	0.063	135	✓	0.06	122	To Do
Kamke 526	✓	0.01	45	✓	0.013	32	To Do
Kamke 527	✗	0	0	✓	0.847	43	To Do
Kamke 528	✗	0	0	✓	0.072	86	To Do
Kamke 529	✓	52.835	1758	✓	0.04	1251	To Do
Kamke 530	✗	0	0	✓	0.12	432	To Do
Kamke 531	✗	0	0	✗	0	0	To Do
Kamke 532	✗	0	0	✓	0.157	848	To Do
Kamke 533	✗	0	0	✓	0.035	76	To Do
Kamke 534	✗	0	0	✓	0.074	84	To Do
Kamke 535	✗	0	0	✓	0.056	51	To Do
Kamke 536	✓	0.025	86	✓	0.035	52	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 537	✗	0	0	✓	598.448	209	To Do
Kamke 538	✗	0	0	✓	10.397	1532	To Do
Kamke 539	✓	0.03	45	✓	3.576	32	To Do
Kamke 540	✓	0.022	69	✓	0.35	109	To Do
Kamke 541	✗	0	0	✓	3.656	103	To Do
Kamke 542	✗	0	0	✓	3.376	107	To Do
Kamke 543	✗	0	0	✓	12.393	277	To Do
Kamke 544	✗	0	0	✓	15.838	4201	To Do
Kamke 545	✓	0.732	383	✓	0.926	144	To Do
Kamke 546	✗	0	0	✓	2.064	171	To Do
Kamke 547	✓	1.349	490	✓	3.52	118	To Do
Kamke 548	✓	1.017	569	✓	0.768	246	To Do
Kamke 549	✓	0.247	406	✓	4.315	545	To Do
Kamke 550	✗	0	0	✓	3.802	60	To Do
Kamke 551	✓	0.38	84	✓	1.128	55	To Do
Kamke 552	✓	0.243	39	✓	1.036	43	To Do
Kamke 553	✓	0.12	51	✓	0.308	36	To Do
Kamke 554	✓	0.076	49	✓	1.642	32	To Do
Kamke 555	✗	0	0	✓	0.137	15	To Do
Kamke 556	✓	6.425	60	✓	1.483	581	To Do
Kamke 557	✓	0.017	39	✓	1.015	74	To Do
Kamke 558	✓	0.597	395	✓	1.734	223	To Do
Kamke 559	✓	0.31	212	✓	1.228	215	To Do
Kamke 560	✓	21.296	110	✓	2.583	1120	To Do
Kamke 561	✗	0	0	✓	5.855	50	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 562	✗	0	0	✓	1.398	3306	To Do
Kamke 563	✓	0.114	59	✓	1.438	66	To Do
Kamke 564	✓	0.042	28	✓	3.761	32	To Do
Kamke 565	✓	0.011	25	✓	4.548	17	To Do
Kamke 566	✗	0	0	✓	0.113	16	To Do
Kamke 567	✗	0	0	✓	0.159	18	To Do
Kamke 568	✓	0.039	28	✓	0.106	32	To Do
Kamke 569	✓	0.043	59	✓	2.899	147	To Do
Kamke 570	✗	0	0	✓	0.303	30	To Do
Kamke 571	✓	0.103	114	✓	4.12	169	To Do
Kamke 572	✗	0	0	✗	0	0	To Do
Kamke 573	✓	0.019	42	✓	3.723	16	To Do
Kamke 574	✓	0.015	102	✓	0.508	41	To Do
Kamke 575	✗	0	0	✗	0	0	To Do
Kamke 576	✗	0	0	✗	0	0	To Do
Kamke 577	✓	12.022	240	✓	1.804	28	To Do
Kamke 578	✓	16.31	97	✓	6.828	22	To Do
Kamke 579	✓	12.683	510	✓	4.297	35	To Do
Kamke 580	✓	24.648	200	✓	0.504	31	To Do
Kamke 581	✓	39.138	141	✓	0.37	32	To Do
Kamke 582	✓	16.531	139	✓	1.818	30	To Do
Kamke 583	✓	41.336	123	✓	2.022	31	To Do
Kamke 584	✓	18.994	112	✓	5.504	35	To Do
Kamke 585	✓	121.002	202	✓	9.802	122	To Do
Kamke 586	✓	158.944	972	✓	1.078	39	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 587	✓	250.009	120	✓	0.594	29	To Do
Kamke 588	✓	29.946	110	✓	0.773	53	To Do
Kamke 589	✓	18.911	242	✓	1.869	38	To Do
Kamke 590	✓	30.335	91	✓	1.005	28	To Do
Kamke 591	✓	17.691	250	✓	2.249	108	To Do
Kamke 592	✗	0	0	✓	0.31	33	To Do
Kamke 593	✓	36.643	218	✓	0.559	35	To Do
Kamke 594	✓	17.841	233	✓	1.821	67	To Do
Kamke 595	✓	18.722	201	✓	0.37	72	To Do
Kamke 596	✓	227.738	153	✓	1.519	26	To Do
Kamke 597	✓	25.3	127	✓	1.647	37	To Do
Kamke 598	✓	0.075	36	✓	0.781	29	To Do
Kamke 599	✓	22.023	92	✓	0.423	57	To Do
Kamke 600	✓	22.532	243	✓	6.479	38	To Do
Kamke 601	✓	32.468	187	✓	0.335	61	To Do
Kamke 602	✓	224.967	164	✓	2.294	33	To Do
Kamke 603	✓	16.924	114	✓	1.204	27	To Do
Kamke 604	✓	23.187	140	✓	0.512	30	To Do
Kamke 605	✓	207.679	142	✓	0.2	29	To Do
Kamke 606	✓	61.691	358	✓	1.879	34	To Do
Kamke 607	✗	0	0	✓	1.092	22	To Do
Kamke 608	✓	298.102	271	✓	2.772	40	To Do
Kamke 609	✓	49.526	114	✓	0.859	22	To Do
Kamke 610	✓	0.059	24	✓	0.019	20	To Do
Kamke 611	✓	38.163	188	✓	1.11	28	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 612	✓	44.808	196	✓	3.195	27	To Do
Kamke 613	✗	0	0	✓	0.749	23	To Do
Kamke 614	✓	68.827	174	✓	3.014	60	To Do
Kamke 615	✓	15.443	74	✓	1.848	26	To Do
Kamke 616	✓	45.11	174	✓	1.794	26	To Do
Kamke 617	✓	257.676	612	✓	1.109	47	To Do
Kamke 618	✓	0.137	25	✓	5.764	34	To Do
Kamke 619	✓	247.316	327	✓	2.099	81	To Do
Kamke 620	✗	0	0	✓	5.51	37	To Do
Kamke 621	✓	0.085	445	✓	4.549	59	To Do
Kamke 622	✓	0.375	134	✓	2.735	77	To Do
Kamke 623	✓	0.154	77	✓	3.777	49	To Do
Kamke 624	✓	48.904	9837	✓	6.144	46	To Do
Kamke 625	✓	0.197	76	✓	4.48	55	To Do
Kamke 626	✓	0.181	104	✓	7.711	115	To Do
Kamke 627	✓	0.849	25	✓	14.909	35	To Do
Kamke 628	✓	0.077	33	✓	10.563	23	To Do
Kamke 629	✓	0.702	47	✓	20.097	62	To Do
Kamke 630	✓	0.478	101	✓	19.011	98	To Do
Kamke 631	✓	0.085	31	✓	45.07	23	To Do
Kamke 632	✓	0.155	65	✓	11.1	54	To Do
Kamke 633	✓	0.179	85	✓	14.888	52	To Do
Kamke 634	✓	0.169	33	✓	10.351	26	To Do
Kamke 635	✓	0.112	33	✓	6.954	22	To Do
Kamke 636	✓	0.05	24	✓	4.838	19	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 637	✓	15.763	59	✓	27.176	84	To Do
Kamke 638	✗	0	0	✓	1.461	35	To Do
Kamke 639	✗	0	0	✓	1.004	50	To Do
Kamke 640	✗	0	0	✓	0.566	47	To Do
Kamke 641	✓	0.16	35	✓	2.438	26	To Do
Kamke 642	✓	0.124	105	✓	1.088	286	To Do
Kamke 643	✓	0.105	31	✓	0.189	22	To Do
Kamke 644	✓	0.252	34	✓	0.666	27	To Do
Kamke 645	✓	0.034	20	✓	0.66	14	To Do
Kamke 646	✓	0.162	35	✓	0.467	23	To Do
Kamke 647	✓	0.371	115	✓	0.461	460	To Do
Kamke 648	✓	0.312	128	✓	0.857	41	To Do
Kamke 649	✓	0.162	37	✓	0.29	27	To Do
Kamke 650	✓	0.224	40	✓	0.202	28	To Do
Kamke 651	✓	0.032	16	✓	0.069	13	To Do
Kamke 652	✓	1.798	101	✓	0.181	27	To Do
Kamke 653	✓	0.168	34	✓	0.162	24	To Do
Kamke 654	✓	0.15	37	✓	0.207	23	To Do
Kamke 655	✓	19.967	82	✓	1.842	66	To Do
Kamke 656	✓	0.037	20	✓	0.067	15	To Do
Kamke 657	✓	0.171	37	✓	0.326	26	To Do
Kamke 658	✓	0.223	45	✓	0.279	28	To Do
Kamke 659	✓	0.404	60	✓	0.441	41	To Do
Kamke 660	✓	0.242	42	✓	0.293	29	To Do
Kamke 661	✓	0.384	61	✓	0.214	39	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 662	✓	0.177	37	✓	0.183	26	To Do
Kamke 663	✓	2.174	101	✓	0.17	27	To Do
Kamke 664	✓	0.175	36	✓	0.164	25	To Do
Kamke 665	✓	0.246	41	✓	0.52	28	To Do
Kamke 666	✓	0.067	29	✓	0.146	24	To Do
Kamke 667	✓	0.945	90	✓	0.305	82	To Do
Kamke 668	✓	0.509	78	✓	1.044	58	To Do
Kamke 669	✓	0.785	264	✓	1.24	72	To Do
Kamke 670	✓	0.339	99	✓	1.01	70	To Do
Kamke 671	✓	0.366	192	✓	0.832	231	To Do
Kamke 672	✗	0	0	✓	0.458	36	To Do
Kamke 673	✓	0.074	23	✓	1.068	17	To Do
Kamke 674	✓	0.212	40	✓	0.276	27	To Do
Kamke 675	✓	0.05	48	✓	0.063	37	To Do
Kamke 676	✓	0.292	144	✓	0.626	43	To Do
Kamke 677	✓	0.032	80	✓	0.036	48	To Do
Kamke 678	✓	0.225	101	✓	0.277	37	To Do
Kamke 679	✓	0.029	59	✓	0.063	37	To Do
Kamke 680	✓	0.213	39	✓	0.259	28	To Do
Kamke 681	✓	0.04	84	✓	0.075	45	To Do
Kamke 682	✓	0.082	39	✓	0.395	28	To Do
Kamke 683	✓	0.346	84	✓	0.299	152	To Do
Kamke 684	✓	0.023	20	✓	3.328	30	To Do
Kamke 685	✓	0.034	87	✓	0.116	48	To Do
Kamke 686	✓	15.666	68	✓	3.229	85	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 687	✓	0.057	130	✓	0.193	39	To Do
Kamke 688	✓	0.103	78	✓	0.086	42	To Do
Kamke 689	✓	0.067	60	✓	0.168	25	To Do
Kamke 690	✓	0.285	127	✓	0.346	40	To Do
Kamke 691	✓	0.063	21	✓	0.727	17	To Do
Kamke 692	✓	0.023	20	✓	2.739	30	To Do
Kamke 693	✓	0.162	146	✓	0.216	40	To Do
Kamke 694	✓	0.269	66	✓	0.279	30	To Do
Kamke 695	✓	0.052	34	✓	0.07	39	To Do
Kamke 696	✗	0	0	✓	0.386	32	To Do
Kamke 697	✓	0.119	114	✓	0.152	40	To Do
Kamke 698	✓	0.129	108	✓	0.174	34	To Do
Kamke 699	✓	0.222	101	✓	0.393	36	To Do
Kamke 700	✓	0.062	76	✓	0.175	62	To Do
Kamke 701	✗	0	0	✓	6.756	71	To Do
Kamke 702	✗	0	0	✓	0.247	35	To Do
Kamke 703	✗	0	0	✓	0.602	44	To Do
Kamke 704	✗	0	0	✓	0.048	38	To Do
Kamke 705	✓	0.053	30	✓	0.159	24	To Do
Kamke 706	✗	0	0	✓	0.633	65	To Do
Kamke 707	✗	0	0	✓	0.539	105	To Do
Kamke 708	✓	0.277	89	✗	0	0	To Do
Kamke 709	✓	4.278	217	✓	0.302	39	To Do
Kamke 710	✗	0	0	✓	2.625	31	To Do
Kamke 711	✓	0.065	28	✓	0.139	31	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 712	✓	0.258	115	✓	0.335	38	To Do
Kamke 713	✓	0.121	649	✓	0.447	86	To Do
Kamke 714	✗	0	0	✓	2.222	96	To Do
Kamke 715	✓	0.241	104	✓	0.312	39	To Do
Kamke 716	✓	4.077	133	✓	0.361	37	To Do
Kamke 717	✓	0.302	46	✓	0.381	33	To Do
Kamke 718	✓	0.118	127	✓	0.068	44	To Do
Kamke 719	✓	0.088	49	✓	0.193	57	To Do
Kamke 720	✓	4.486	314	✓	0.244	48	To Do
Kamke 721	✓	0.018	27	✓	0.095	19	To Do
Kamke 722	✓	30.179	493	✓	0.372	70	To Do
Kamke 723	✓	0.066	663	✓	0.085	856	To Do
Kamke 724	✓	45.7	422	✓	0.056	18	To Do
Kamke 725	✓	0.24	19	✓	0.866	25	To Do
Kamke 726	✓	0.082	625	✓	0.305	83	To Do
Kamke 727	✓	0.427	29	✓	0.403	25	To Do
Kamke 728	✓	0.371	72	✓	0.358	50	To Do
Kamke 729	✓	0.308	327	✓	0.108	404	To Do
Kamke 730	✗	0	0	✓	2.161	41	To Do
Kamke 731	✓	0.185	47	✓	0.194	42	To Do
Kamke 732	✓	0.454	110	✓	0.405	43	To Do
Kamke 733	✗	0	0	✗	0	0	To Do
Kamke 734	✓	0.109	37	✓	0.152	39	To Do
Kamke 735	✗	0	0	✓	0.069	78	To Do
Kamke 736	✓	0.094	31	✓	0.2	43	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 737	✓	0.029	36	✓	0.083	29	To Do
Kamke 738	✓	0.467	1347	✓	0.904	1054	To Do
Kamke 739	✓	0.12	39	✓	0.18	35	To Do
Kamke 740	✓	0.06	74	✓	0.104	72	To Do
Kamke 741	✓	2.86	175	✓	1.023	246	To Do
Kamke 742	✓	4.206	3913	✓	1.95	239	To Do
Kamke 743	✗	0	0	✓	0.57	301	To Do
Kamke 744	✓	0.043	510	✓	0.243	621	To Do
Kamke 745	✗	0	0	✓	0.071	78	To Do
Kamke 746	✗	0	0	✓	0.489	243	To Do
Kamke 747	✗	0	0	✓	0.358	75	To Do
Kamke 748	✓	0.305	285	✓	0.107	404	To Do
Kamke 749	✓	0.1	126	✓	0.135	192	To Do
Kamke 750	✓	0.327	72	✓	0.265	49	To Do
Kamke 751	✓	0.073	30	✓	0.114	26	To Do
Kamke 752	✗	0	0	✓	1.624	723	To Do
Kamke 753	✓	0.101	41	✓	0.155	38	To Do
Kamke 754	✓	0.032	47	✓	0.019	26	To Do
Kamke 755	✓	0.187	2633	✓	0.165	44	To Do
Kamke 756	✓	0.077	95	✓	0.034	37	To Do
Kamke 757	✓	0.031	36	✓	0.067	26	To Do
Kamke 758	✓	0.929	459	✓	0.247	41	To Do
Kamke 759	✗	0	0	✓	0.704	315	To Do
Kamke 760	✓	1.273	112	✓	1.639	136	To Do
Kamke 761	✓	0.025	33	✓	0.056	18	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 762	✓	0.06	26	✓	0.112	22	To Do
Kamke 763	✓	0.058	22	✓	0.101	14	To Do
Kamke 764	✓	0.095	50	✓	0.126	36	To Do
Kamke 765	✗	0	0	✓	0.208	106	To Do
Kamke 766	✗	0	0	✓	0.256	89	To Do
Kamke 767	✓	0.027	38	✓	0.081	26	To Do
Kamke 768	✓	0.986	66	✓	0.11	26	To Do
Kamke 769	✗	0	0	✓	0.547	251	To Do
Kamke 770	✓	0.127	705	✓	0.132	1105	To Do
Kamke 771	✓	0.034	46	✓	0.111	84	To Do
Kamke 772	✓	0.063	21	✓	0.119	18	To Do
Kamke 773	✓	0.048	61	✓	0.247	48	To Do
Kamke 774	✓	0.03	45	✓	0.089	51	To Do
Kamke 775	✓	0.1	943	✓	0.091	32	To Do
Kamke 776	✗	0	0	✓	0.934	96	To Do
Kamke 777	✓	0.091	39	✓	0.139	51	To Do
Kamke 778	✓	0.07	95	✓	0.03	37	To Do
Kamke 779	✓	0.032	57	✓	0.11	50	To Do
Kamke 780	✓	0.025	15	✓	0.408	27	To Do
Kamke 781	✓	0.509	82	✓	0.29	61	To Do
Kamke 782	✗	0	0	✓	1.546	96	To Do
Kamke 783	✗	0	0	✓	0.238	75	To Do
Kamke 784	✗	0	0	✓	36.043	24	To Do
Kamke 785	✗	0	0	✓	123.082	24	To Do
Kamke 786	✗	0	0	✓	0.063	33	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 787	✓	26.701	484	✓	0.619	191	To Do
Kamke 788	✗	0	0	✓	0.706	108	To Do
Kamke 789	✗	0	0	✗	0	0	To Do
Kamke 790	✗	0	0	✗	0	0	To Do
Kamke 791	✗	0	0	✓	35.476	306	To Do
Kamke 792	✗	0	0	✓	0.852	112	To Do
Kamke 793	✓	15.154	399	✓	0.109	32	To Do
Kamke 794	✓	0.086	67	✓	2.51	32	To Do
Kamke 795	✓	0.168	111	✓	0.042	37	To Do
Kamke 796	✓	16.171	102	✓	1.451	143	To Do
Kamke 797	✓	2.064	349	✓	0.425	252	To Do
Kamke 798	✓	0.591	27	✓	0.154	30	To Do
Kamke 799	✓	0.304	70	✓	0.43	147	To Do
Kamke 800	✓	0.188	128	✓	0.03	41	To Do
Kamke 801	✓	0.107	126	✓	0.072	63	To Do
Kamke 802	✓	0.077	98	✓	0.147	27	To Do
Kamke 803	✓	0.087	634	✓	0.598	65	To Do
Kamke 804	✓	0.484	43	✓	1.401	38	To Do
Kamke 805	✓	0.035	37	✓	0.68	42	To Do
Kamke 806	✓	0.276	23	✓	0.802	22	To Do
Kamke 807	✗	0	0	✓	0.821	43	To Do
Kamke 808	✓	1.319	149	✓	0.096	45	To Do
Kamke 809	✓	0.168	128	✓	0.029	41	To Do
Kamke 810	✓	0.016	40	✓	0.05	16	To Do
Kamke 811	✓	2.204	33	✓	2.608	32	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 812	✓	0.323	70	✓	0.483	32	To Do
Kamke 813	✓	0.478	66	✓	0.542	40	To Do
Kamke 814	✓	0.016	72	✓	0.042	38	To Do
Kamke 815	✓	17.133	103	✓	1.298	168	To Do
Kamke 816	✓	0.144	74	✓	1.025	190	To Do
Kamke 817	✓	0.369	63	✓	0.869	27	To Do
Kamke 818	✓	0.047	34	✓	0.155	34	To Do
Kamke 819	✓	0.228	65	✓	0.258	30	To Do
Kamke 820	✓	0.33	63	✓	0.864	27	To Do
Kamke 821	✓	0.156	2093	✓	0.173	25	To Do
Kamke 822	✓	0.042	32	✓	0.144	25	To Do
Kamke 823	✓	0.402	39	✓	0.145	38	To Do
Kamke 824	✓	0.055	68	✓	0.512	61	To Do
Kamke 825	✓	0.207	148	✓	0.119	48	To Do
Kamke 826	✓	0.592	70	✓	0.401	51	To Do
Kamke 827	✓	0.124	111	✓	0.273	49	To Do
Kamke 828	✓	0.21	56	✓	0.353	54	To Do
Kamke 829	✓	0.382	74	✓	0.491	40	To Do
Kamke 830	✓	0.462	37	✓	0.153	38	To Do
Kamke 831	✓	4.433	145	✓	0.376	35	To Do
Kamke 832	✓	3.291	2497	✓	0.214	31	To Do
Kamke 833	✓	0.117	105	✓	0.22	49	To Do
Kamke 834	✓	0.72	90	✓	0.46	60	To Do
Kamke 835	✗	0	0	✗	0	0	To Do
Kamke 836	✓	11.659	379	✓	0.261	73	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 837	✗	0	0	✗	0	0	To Do
Kamke 838	✓	0.029	31	✓	0.119	25	To Do
Kamke 839	✓	0.073	28	✓	0.093	19	To Do
Kamke 840	✓	0.085	30	✓	0.082	19	To Do
Kamke 841	✓	1.319	236	✓	0.378	97	To Do
Kamke 842	✓	0.121	186	✓	0.029	43	To Do
Kamke 843	✓	0.125	198	✓	0.028	43	To Do
Kamke 844	✓	15.864	386	✓	0.286	97	To Do
Kamke 845	✓	4.957	227	✓	0.301	44	To Do
Kamke 846	✓	1.387	362	✓	0.221	40	To Do
Kamke 847	✓	0.356	69	✓	0.323	34	To Do
Kamke 848	✓	0.112	154	✓	0.741	27	To Do
Kamke 849	✓	0.319	68	✓	0.302	33	To Do
Kamke 850	✓	0.197	1478	✓	1.39	32	To Do
Kamke 851	✓	0.165	145	✓	0.076	42	To Do
Kamke 852	✓	0.157	145	✓	0.079	42	To Do
Kamke 853	✓	0.018	76	✓	0.044	63	To Do
Kamke 854	✗	0	0	✓	0.277	51	To Do
Kamke 855	✗	0	0	✓	0.271	51	To Do
Kamke 856	✓	0.909	100	✓	0.359	65	To Do
Kamke 857	✓	0.338	69	✓	0.315	32	To Do
Kamke 858	✓	0.165	145	✓	0.075	42	To Do
Kamke 859	✓	1.307	102	✓	0.355	63	To Do
Kamke 860	✓	0.148	33	✓	2.612	29	To Do
Kamke 861	✓	1.823	155	✓	0.205	26	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 862	✗	0	0	✓	0.253	27	To Do
Kamke 863	✓	0.035	30	✓	7.155	38	To Do
Kamke 864	✓	0.042	137	✓	0.12	162	To Do
Kamke 865	✗	0	0	✓	0.276	23	To Do
Kamke 866	✓	0.487	74	✓	0.565	37	To Do
Kamke 867	✓	0.063	77	✓	0.073	30	To Do
Kamke 868	✓	0.048	79	✓	0.075	28	To Do
Kamke 869	✓	0.037	42	✓	0.083	37	To Do
Kamke 870	✓	1.668	35	✓	1.234	30	To Do
Kamke 871	✓	0.023	22	✓	0.089	26	To Do
Kamke 872	✓	0.048	215	✓	0.072	49	To Do
Kamke 873	✓	0.345	53	✓	0.29	50	To Do
Kamke 874	✓	0.072	101	✓	0.064	40	To Do
Kamke 875	✓	0.292	285	✓	0.332	73	To Do
Kamke 876	✓	0.019	135	✓	0.05	41	To Do
Kamke 877	✓	0.017	49	✓	0.052	73	To Do
Kamke 878	✓	0.286	130	✗	0	0	To Do
Kamke 879	✓	0.159	135	✓	0.282	55	To Do
Kamke 880	✓	0.138	131	✓	0.07	41	To Do
Kamke 881	✓	0.018	75	✓	0.054	77	To Do
Kamke 882	✓	0.077	119	✓	0.072	41	To Do
Kamke 883	✓	1.457	164	✓	0.848	352	To Do
Kamke 884	✓	0.365	71	✓	0.423	107	To Do
Kamke 885	✗	0	0	✗	0	0	To Do
Kamke 886	✓	0.059	82	✓	0.042	42	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 887	✓	0.026	106	✓	0.058	72	To Do
Kamke 888	✓	0.019	78	✓	0.059	79	To Do
Kamke 889	✗	0	0	✓	1.447	49	To Do
Kamke 890	✓	0.139	103	✓	1.19	34	To Do
Kamke 891	✓	0.024	135	✓	0.072	56	To Do
Kamke 892	✗	0	0	✓	0.645	40	To Do
Kamke 893	✓	0.063	80	✓	0.039	41	To Do
Kamke 894	✗	0	0	✗	0	0	To Do
Kamke 895	✓	0.025	81	✓	0.064	79	To Do
Kamke 896	✓	0.219	106	✓	0.928	63	To Do
Kamke 897	✓	0.027	79	✓	0.093	87	To Do
Kamke 898	✓	0.022	106	✓	0.056	87	To Do
Kamke 899	✓	0.069	106	✓	0.049	47	To Do
Kamke 900	✓	0.093	381	✓	0.082	48	To Do
Kamke 901	✓	0.09	33	✓	0.675	30	To Do
Kamke 902	✓	0.099	295	✓	0.297	183	To Do
Kamke 903	✓	0.05	19	✓	0.081	48	To Do
Kamke 904	✓	0.051	23	✓	0.056	64	To Do
Kamke 905	✓	0.062	85	✓	0.056	46	To Do
Kamke 906	✓	0.052	326	✓	0.421	37	To Do
Kamke 907	✓	0.051	22	✓	0.178	20	To Do
Kamke 908	✓	1.467	1278	✓	0.484	1742	To Do
Kamke 909	✗	0	0	✗	0	0	To Do
Kamke 910	✓	0.061	98	✓	0.043	42	To Do
Kamke 911	✓	4.271	56	✓	0.681	30	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 912	✓	1.526	205	✗	0	0	To Do
Kamke 913	✗	0	0	✓	3.729	43	To Do
Kamke 914	✓	1.578	401	✓	4.	71	To Do
Kamke 915	✗	0	0	✓	0.072	43	To Do
Kamke 916	✗	0	0	✓	1.471	73	To Do
Kamke 917	✗	0	0	✓	0.398	38	To Do
Kamke 918	✗	0	0	✓	2.477	41	To Do
Kamke 919	✗	0	0	✓	0.316	82	To Do
Kamke 920	✓	0.244	301	✗	0	0	To Do
Kamke 921	✓	2.785	52	✓	0.367	30	To Do
Kamke 922	✗	0	0	✓	0.885	47	To Do
Kamke 923	✗	0	0	✓	0.526	36	To Do
Kamke 924	✓	0.88	55	✓	0.144	46	To Do
Kamke 925	✗	0	0	✓	0.29	38	To Do
Kamke 926	✓	0.025	128	✓	0.116	67	To Do
Kamke 927	✓	0.121	112	✓	0.142	68	To Do
Kamke 928	✓	1.403	23	✓	0.517	20	To Do
Kamke 929	✗	0	0	✓	0.06	42	To Do
Kamke 930	✓	1.624	39	✓	0.679	36	To Do
Kamke 931	✓	0.024	80	✓	0.049	73	To Do
Kamke 932	✗	0	0	✓	0.396	54	To Do
Kamke 933	✓	0.081	99	✓	0.043	39	To Do
Kamke 934	✓	0.113	102	✓	0.082	39	To Do
Kamke 935	✓	10.191	248	✓	0.316	55	To Do
Kamke 936	✓	0.102	99	✓	0.081	39	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 937	✓	0.027	124	✓	0.066	79	To Do
Kamke 938	✓	0.065	108	✓	0.036	39	To Do
Kamke 939	✓	0.403	136	✓	0.184	70	To Do
Kamke 940	✓	0.021	80	✓	0.056	63	To Do
Kamke 941	✓	0.365	53	✓	0.063	35	To Do
Kamke 942	✗	0	0	✓	0.63	43	To Do
Kamke 943	✓	0.407	53	✓	0.057	40	To Do
Kamke 944	✓	1.73	233	✓	0.091	47	To Do
Kamke 945	✓	1.291	213	✓	0.08	41	To Do
Kamke 946	✓	0.082	150	✓	0.187	85	To Do
Kamke 947	✓	0.107	30	✓	0.39	44	To Do
Kamke 948	✓	0.256	39	✓	0.313	68	To Do
Kamke 949	✓	0.022	76	✓	0.048	81	To Do
Kamke 950	✓	0.174	141	✓	0.104	42	To Do
Kamke 951	✓	0.154	140	✓	0.084	41	To Do
Kamke 952	✓	0.138	189	✓	0.67	62	To Do
Kamke 953	✗	0	0	✓	0.454	145	To Do
Kamke 954	✓	0.094	115	✓	0.093	53	To Do
Kamke 955	✓	0.041	112	✓	0.116	101	To Do
Kamke 956	✓	0.211	28	✓	0.113	79	To Do
Kamke 957	✓	0.198	28	✓	0.057	79	To Do
Kamke 958	✓	0.063	82	✓	0.05	40	To Do
Kamke 959	✓	0.044	20	✓	0.09	16	To Do
Kamke 960	✓	0.035	14	✓	0.049	16	To Do
Kamke 961	✗	0	0	✓	0.451	45	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 962	✓	5.689	1191	✓	1.996	79	To Do
Kamke 963	✓	0.122	108	✓	0.26	39	To Do
Kamke 964	✓	5.057	264	✓	3.314	80	To Do
Kamke 965	✓	0.057	29	✓	0.126	25	To Do
Kamke 966	✓	0.444	292	✓	0.829	50	To Do
Kamke 967	✓	0.133	151	✓	0.099	91	To Do
Kamke 968	✓	0.083	30	✓	0.158	29	To Do
Kamke 969	✓	0.057	19	✓	0.155	26	To Do
Kamke 970	✓	0.484	66	✓	1.079	181	To Do
Kamke 971	✓	0.104	157	✓	0.35	86	To Do
Kamke 972	✓	0.026	32	✓	0.096	27	To Do
Kamke 973	✓	0.169	146	✓	0.451	134	To Do
Kamke 974	✓	0.011	39	✓	0.05	57	To Do
Kamke 975	✓	0.012	47	✓	0.046	59	To Do
Kamke 976	✓	0.08	101	✓	0.872	57	To Do
Kamke 977	✓	0.196	139	✓	0.217	122	To Do
Kamke 978	✓	0.048	60	✓	0.191	71	To Do
Kamke 979	✓	0.012	37	✓	0.046	57	To Do
Kamke 980	✓	0.013	43	✓	0.019	35	To Do
Kamke 981	✓	0.017	49	✓	0.028	41	To Do
Kamke 982	✓	0.107	132	✓	0.548	145	To Do
Kamke 983	✓	0.256	238	✓	0.409	233	To Do
Kamke 984	✓	3.027	428	✓	0.322	40	To Do
Kamke 985	✓	0.215	103	✓	0.046	43	To Do
Kamke 986	✓	0.015	44	✓	0.028	36	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 987	✓	0.092	40	✓	0.075	22	To Do
Kamke 988	✓	0.318	104	✓	0.052	29	To Do
Kamke 989	✓	0.099	55	✓	0.038	29	To Do
Kamke 990	✓	0.444	49	✓	0.743	44	To Do
Kamke 991	✓	0.241	101	✓	0.033	29	To Do
Kamke 992	✓	0.102	42	✓	0.038	25	To Do
Kamke 993	✗	0	0	✓	0.033	35	To Do
Kamke 994	✓	0.121	198	✓	0.023	43	To Do
Kamke 995	✓	0.017	17	✓	0.146	14	To Do
Kamke 996	✗	0	0	✓	0.089	15	To Do
Kamke 997	✓	0.029	18	✓	0.066	16	To Do
Kamke 998	✓	0.43	27	✓	0.498	27	To Do
Kamke 999	✓	0.024	24	✓	0.063	36	To Do
Kamke 1000	✗	0	0	✓	0.187	19	To Do
Kamke 1001	✓	0.004	12	✓	0.022	9	To Do
Kamke 1002	✓	0.006	16	✓	0.005	13	To Do
Kamke 1003	✓	0.113	45	✓	0.078	26	To Do
Kamke 1004	✓	0.097	47	✓	0.049	27	To Do
Kamke 1005	✓	0.522	1163	✓	0.123	82	To Do
Kamke 1006	✓	0.005	20	✓	0.013	15	To Do
Kamke 1007	✓	0.069	135	✓	0.016	26	To Do
Kamke 1008	✓	0.042	48	✓	0.081	41	To Do
Kamke 1009	✓	0.005	28	✓	0.016	21	To Do
Kamke 1010	✓	0.007	46	✓	0.039	31	To Do
Kamke 1011	✓	0.008	33	✓	0.032	17	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1012	✓	0.009	47	✓	0.095	29	To Do
Kamke 1013	✓	0.021	43	✓	0.039	22	To Do
Kamke 1014	✓	0.039	170	✓	0.086	63	To Do
Kamke 1015	✗	0	0	✗	0	0	To Do
Kamke 1016	✓	0.142	312	✓	0.204	91	To Do
Kamke 1017	✓	0.028	46	✓	0.043	17	To Do
Kamke 1018	✓	0.023	55	✓	0.042	39	To Do
Kamke 1019	✗	0	0	✗	0	0	To Do
Kamke 1020	✓	0.682	180	✓	0.186	58	To Do
Kamke 1021	✓	0.051	44	✓	0.214	39	To Do
Kamke 1022	✓	0.028	28	✓	0.201	21	To Do
Kamke 1023	✓	0.016	44	✓	0.193	29	To Do
Kamke 1024	✓	0.165	84	✓	0.139	30	To Do
Kamke 1025	✓	0.946	615	✓	0.204	102	To Do
Kamke 1026	✗	0	0	✗	0	0	To Do
Kamke 1027	✗	0	0	✓	0.349	69	To Do
Kamke 1028	✗	0	0	✗	0	0	To Do
Kamke 1029	✗	0	0	✓	0.128	22	To Do
Kamke 1030	✗	0	0	✗	0	0	To Do
Kamke 1031	✗	0	0	✗	0	0	To Do
Kamke 1032	✗	0	0	✓	0.112	48	To Do
Kamke 1033	✓	0.018	37	✓	0.01	27	To Do
Kamke 1034	✓	0.012	20	✓	0.008	15	To Do
Kamke 1035	✓	0.006	58	✓	0.011	41	To Do
Kamke 1036	✓	0.487	207	✓	0.093	124	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1037	✓	0.03	101	✓	0.102	64	To Do
Kamke 1038	✗	0	0	✗	0	0	To Do
Kamke 1039	✓	0.013	47	✓	0.013	25	To Do
Kamke 1040	✓	0.031	53	✓	0.042	33	To Do
Kamke 1041	✓	0.01	55	✓	0.072	41	To Do
Kamke 1042	✓	0.009	61	✓	0.065	41	To Do
Kamke 1043	✓	0.045	69	✓	0.211	39	To Do
Kamke 1044	✓	0.01	39	✓	0.067	35	To Do
Kamke 1045	✓	0.023	39	✓	0.008	21	To Do
Kamke 1046	✓	0.008	31	✓	0.067	31	To Do
Kamke 1047	✓	0.015	27	✓	0.03	16	To Do
Kamke 1048	✓	0.011	45	✓	0.069	37	To Do
Kamke 1049	✓	0.07	109	✓	0.167	66	To Do
Kamke 1050	✓	0.014	23	✓	0.028	14	To Do
Kamke 1051	✓	0.035	44	✓	0.037	27	To Do
Kamke 1052	✓	0.022	78	✓	0.082	58	To Do
Kamke 1053	✓	0.03	57	✓	0.046	35	To Do
Kamke 1054	✓	0.048	172	✓	0.049	98	To Do
Kamke 1055	✓	0.157	421	✓	0.233	262	To Do
Kamke 1056	✓	0.039	66	✓	0.108	48	To Do
Kamke 1057	✓	0.865	55	✓	0.132	50	To Do
Kamke 1058	✓	0.886	55	✓	0.117	29	To Do
Kamke 1059	✓	0.056	72	✓	0.088	56	To Do
Kamke 1060	✓	0.037	83	✓	0.155	81	To Do
Kamke 1061	✓	0.095	70	✓	0.088	28	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1062	✓	0.029	35	✓	0.024	19	To Do
Kamke 1063	✓	0.046	28	✓	0.36	61	To Do
Kamke 1064	✓	0.578	1400	✓	0.296	125	To Do
Kamke 1065	✓	0.161	114	✓	0.237	60	To Do
Kamke 1066	✓	0.035	18	✓	0.067	15	To Do
Kamke 1067	✓	0.033	21	✓	0.046	17	To Do
Kamke 1068	✓	0.151	20	✓	0.223	45	To Do
Kamke 1069	✓	0.036	19	✓	0.089	15	To Do
Kamke 1070	✓	0.32	143	✓	0.174	60	To Do
Kamke 1071	✓	0.098	59	✓	0.047	24	To Do
Kamke 1072	✗	0	0	✗	0	0	To Do
Kamke 1073	✗	0	0	✗	0	0	To Do
Kamke 1074	✗	0	0	✓	0.017	21	To Do
Kamke 1075	✗	0	0	✗	0	0	To Do
Kamke 1076	✗	0	0	✗	0	0	To Do
Kamke 1077	✗	0	0	✗	0	0	To Do
Kamke 1078	✓	0.071	73	✓	0.031	33	To Do
Kamke 1079	✓	0.239	135	✓	0.018	37	To Do
Kamke 1080	✗	0	0	✓	0.329	74	To Do
Kamke 1081	✗	0	0	✗	0	0	To Do
Kamke 1082	✗	0	0	✓	0.131	74	To Do
Kamke 1083	✗	0	0	✓	0.106	31	To Do
Kamke 1084	✗	0	0	✓	0.083	20	To Do
Kamke 1085	✗	0	0	✓	0.079	24	To Do
Kamke 1086	✓	0.006	42	✓	0.024	29	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1087	✓	0.009	36	✓	0.076	33	To Do
Kamke 1088	✓	0.103	180	✓	0.14	31	To Do
Kamke 1089	✓	0.046	99	✓	0.052	58	To Do
Kamke 1090	✓	0.033	50	✓	0.043	40	To Do
Kamke 1091	✓	0.028	41	✓	0.043	35	To Do
Kamke 1092	✓	0.1	72	✓	0.052	29	To Do
Kamke 1093	✓	0.006	13	✓	0.006	10	To Do
Kamke 1094	✓	0.024	41	✓	0.01	29	To Do
Kamke 1095	✓	0.01	30	✓	0.032	23	To Do
Kamke 1096	✓	0.014	61	✓	0.066	39	To Do
Kamke 1097	✓	0.028	46	✓	0.013	31	To Do
Kamke 1098	✓	0.011	41	✓	0.01	27	To Do
Kamke 1099	✗	0	0	✓	0.044	25	To Do
Kamke 1100	✓	0.031	44	✓	0.039	23	To Do
Kamke 1101	✓	0.028	51	✓	0.033	29	To Do
Kamke 1102	✓	0.008	42	✓	0.033	33	To Do
Kamke 1103	✓	0.029	64	✓	0.01	33	To Do
Kamke 1104	✓	0.038	104	✓	0.013	41	To Do
Kamke 1105	✓	0.023	64	✓	0.04	39	To Do
Kamke 1106	✓	0.054	441	✓	0.081	71	To Do
Kamke 1107	✓	0.031	40	✓	0.074	30	To Do
Kamke 1108	✓	0.036	37	✓	0.072	26	To Do
Kamke 1109	✓	0.054	45	✓	0.028	33	To Do
Kamke 1110	✓	0.044	36	✓	0.043	23	To Do
Kamke 1111	✓	0.019	20	✓	0.021	13	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1112	✓	0.027	30	✓	0.029	22	To Do
Kamke 1113	✓	0.023	24	✓	0.058	17	To Do
Kamke 1114	✓	0.042	39	✓	0.043	34	To Do
Kamke 1115	✓	0.065	76	✓	0.091	47	To Do
Kamke 1116	✓	0.053	43	✓	0.081	31	To Do
Kamke 1117	✓	0.095	107	✓	0.11	82	To Do
Kamke 1118	✓	0.096	51	✓	0.099	39	To Do
Kamke 1119	✓	0.178	77	✓	0.041	20	To Do
Kamke 1120	✓	0.065	166	✓	0.216	109	To Do
Kamke 1121	✓	9.736	40	✓	0.024	23	To Do
Kamke 1122	✓	9.451	56	✓	0.151	28	To Do
Kamke 1123	✓	0.013	91	✓	0.053	45	To Do
Kamke 1124	✓	0.065	65	✓	0.079	29	To Do
Kamke 1125	✓	0.188	48	✓	0.05	36	To Do
Kamke 1126	✗	0	0	✓	0.04	19	To Do
Kamke 1127	✓	0.041	36	✓	0.021	21	To Do
Kamke 1128	✗	0	0	✓	0.223	32	To Do
Kamke 1129	✓	0.039	42	✓	0.034	30	To Do
Kamke 1130	✓	0.013	46	✓	0.013	31	To Do
Kamke 1131	✓	0.012	58	✓	0.075	33	To Do
Kamke 1132	✓	0.012	48	✓	0.072	29	To Do
Kamke 1133	✓	0.091	92	✓	0.099	37	To Do
Kamke 1134	✓	0.095	78	✓	0.044	21	To Do
Kamke 1135	✓	0.01	27	✓	0.01	17	To Do
Kamke 1136	✓	0.021	30	✓	0.031	16	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1137	✓	0.097	74	✓	0.05	25	To Do
Kamke 1138	✓	0.03	38	✓	0.069	26	To Do
Kamke 1139	✓	0.013	74	✓	0.074	37	To Do
Kamke 1140	✓	0.048	190	✓	0.023	66	To Do
Kamke 1141	✓	0.129	70	✓	0.054	55	To Do
Kamke 1142	✓	0.06	108	✓	0.099	53	To Do
Kamke 1143	✓	0.046	93	✓	0.101	57	To Do
Kamke 1144	✓	0.04	88	✓	0.083	60	To Do
Kamke 1145	✓	0.373	398	✓	0.2	248	To Do
Kamke 1146	✓	0.023	18	✓	0.007	15	To Do
Kamke 1147	✓	0.018	18	✓	0.008	15	To Do
Kamke 1148	✓	0.011	77	✓	0.012	35	To Do
Kamke 1149	✓	0.067	212	✓	0.014	45	To Do
Kamke 1150	✓	0.011	53	✓	0.067	27	To Do
Kamke 1151	✓	0.019	129	✓	0.09	43	To Do
Kamke 1152	✓	0.019	114	✓	0.243	53	To Do
Kamke 1153	✓	0.034	56	✓	0.029	31	To Do
Kamke 1154	✓	0.021	88	✓	0.122	57	To Do
Kamke 1155	✓	0.052	225	✓	0.04	67	To Do
Kamke 1156	✗	0	0	✓	0.136	71	To Do
Kamke 1157	✗	0	0	✗	0	0	To Do
Kamke 1158	✓	14.34	42	✓	0.224	178	To Do
Kamke 1159	✓	0.017	44	✓	0.016	19	To Do
Kamke 1160	✓	0.01	30	✓	0.013	23	To Do
Kamke 1161	✓	0.049	78	✓	0.012	31	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1162	✓	0.059	18	✓	0.01	15	To Do
Kamke 1163	✓	0.339	70	✓	0.033	49	To Do
Kamke 1164	✓	0.022	30	✓	0.025	23	To Do
Kamke 1165	✓	0.05	37	✓	0.014	19	To Do
Kamke 1166	✓	0.014	23	✓	0.013	21	To Do
Kamke 1167	✓	0.083	326	✓	0.026	63	To Do
Kamke 1168	✓	0.006	15	✓	0.009	11	To Do
Kamke 1169	✓	0.072	236	✓	0.025	49	To Do
Kamke 1170	✓	0.024	58	✓	0.036	43	To Do
Kamke 1171	✓	0.054	142	✓	0.122	49	To Do
Kamke 1172	✓	0.058	158	✓	0.03	47	To Do
Kamke 1173	✓	0.066	74	✓	0.076	37	To Do
Kamke 1174	✓	0.019	33	✓	0.021	25	To Do
Kamke 1175	✓	0.175	38	✓	0.052	29	To Do
Kamke 1176	✓	0.018	33	✓	0.029	15	To Do
Kamke 1177	✗	0	0	✓	0.071	34	To Do
Kamke 1178	✓	0.059	74	✓	0.027	23	To Do
Kamke 1179	✓	0.042	53	✓	0.03	19	To Do
Kamke 1180	✓	0.219	73	✓	0.047	49	To Do
Kamke 1181	✓	0.029	37	✓	0.017	25	To Do
Kamke 1182	✓	0.017	24	✓	0.013	20	To Do
Kamke 1183	✓	0.028	27	✓	0.016	22	To Do
Kamke 1184	✓	0.02	38	✓	0.027	25	To Do
Kamke 1185	✓	0.04	67	✓	0.027	33	To Do
Kamke 1186	✓	0.035	42	✓	0.024	36	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1187	✓	0.013	99	✓	0.012	53	To Do
Kamke 1188	✓	0.09	266	✓	0.155	114	To Do
Kamke 1189	✓	0.073	445	✓	0.028	79	To Do
Kamke 1190	✓	0.031	122	✓	0.09	38	To Do
Kamke 1191	✓	0.01	110	✓	0.015	23	To Do
Kamke 1192	✓	11.087	39	✓	0.132	51	To Do
Kamke 1193	✓	0.049	44	✓	0.036	38	To Do
Kamke 1194	✓	0.052	65	✓	0.055	48	To Do
Kamke 1195	✓	0.029	80	✓	0.12	93	To Do
Kamke 1196	✓	0.026	37	✓	0.035	31	To Do
Kamke 1197	✓	0.019	78	✓	0.041	43	To Do
Kamke 1198	✓	0.03	41	✓	0.039	37	To Do
Kamke 1199	✓	0.013	41	✓	0.02	35	To Do
Kamke 1200	✓	0.022	62	✓	0.016	27	To Do
Kamke 1201	✓	0.055	44	✓	0.02	34	To Do
Kamke 1202	✓	0.015	22	✓	0.031	14	To Do
Kamke 1203	✓	0.023	124	✓	0.02	28	To Do
Kamke 1204	✓	0.021	132	✓	0.049	35	To Do
Kamke 1205	✗	0	0	✗	0	0	To Do
Kamke 1206	✓	0.115	120	✓	0.069	76	To Do
Kamke 1207	✓	0.124	294	✓	0.221	110	To Do
Kamke 1208	✓	0.04	59	✓	0.043	35	To Do
Kamke 1209	✓	0.023	67	✓	0.055	41	To Do
Kamke 1210	✓	0.27	252	✓	0.679	81	To Do
Kamke 1211	✓	0.058	68	✓	0.056	36	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1212	✗	0	0	✗	0	0	To Do
Kamke 1213	✓	0.082	54	✓	0.053	53	To Do
Kamke 1214	✓	0.295	260	✓	0.62	71	To Do
Kamke 1215	✓	0.163	664	✓	0.176	148	To Do
Kamke 1216	✗	0	0	✗	0	0	To Do
Kamke 1217	✓	0.147	30	✓	0.037	24	To Do
Kamke 1218	✓	0.151	38	✓	0.038	30	To Do
Kamke 1219	✗	0	0	✓	0.082	69	To Do
Kamke 1220	✓	193.071	96	✓	0.02	40	To Do
Kamke 1221	✓	0.059	40	✓	0.026	35	To Do
Kamke 1222	✓	0.022	30	✓	0.013	23	To Do
Kamke 1223	✓	0.02	25	✓	0.014	39	To Do
Kamke 1224	✓	0.02	30	✓	0.016	23	To Do
Kamke 1225	✓	0.032	29	✓	0.037	23	To Do
Kamke 1226	✓	0.019	30	✓	0.045	25	To Do
Kamke 1227	✓	0.034	21	✓	0.014	16	To Do
Kamke 1228	✓	0.016	82	✓	0.086	53	To Do
Kamke 1229	✓	0.045	48	✓	0.017	31	To Do
Kamke 1230	✓	0.027	82	✓	0.106	36	To Do
Kamke 1231	✓	0.078	58	✓	0.049	52	To Do
Kamke 1232	✗	0	0	✓	0.19	409	To Do
Kamke 1233	✗	0	0	✓	0.154	409	To Do
Kamke 1234	✓	0.029	38	✗	0	0	To Do
Kamke 1235	✓	0.029	50	✓	0.021	45	To Do
Kamke 1236	✗	0	0	✗	0	0	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1237	✓	0.011	30	✓	0.019	20	To Do
Kamke 1238	✓	0.019	36	✓	0.018	26	To Do
Kamke 1239	✓	0.014	46	✓	0.049	35	To Do
Kamke 1240	✓	0.018	18	✓	0.04	15	To Do
Kamke 1241	✓	0.016	30	✓	0.048	24	To Do
Kamke 1242	✓	0.077	68	✓	0.077	41	To Do
Kamke 1243	✓	0.031	45	✓	0.04	21	To Do
Kamke 1244	✓	0.031	42	✓	0.071	27	To Do
Kamke 1245	✓	0.022	42	✓	0.053	27	To Do
Kamke 1246	✓	0.021	42	✓	0.158	28	To Do
Kamke 1247	✓	0.216	97	✓	0.029	27	To Do
Kamke 1248	✗	0	0	✓	0.221	134	To Do
Kamke 1249	✓	0.176	193	✓	0.078	134	To Do
Kamke 1250	✓	0.052	41	✓	0.03	41	To Do
Kamke 1251	✓	0.037	25	✓	0.052	20	To Do
Kamke 1252	✓	0.153	151	✓	0.056	124	To Do
Kamke 1253	✓	0.027	34	✓	0.007	16	To Do
Kamke 1254	✓	0.091	69	✓	0.084	42	To Do
Kamke 1255	✓	0.213	118	✓	0.026	42	To Do
Kamke 1256	✓	0.024	26	✓	0.113	51	To Do
Kamke 1257	✓	0.05	33	✓	0.23	27	To Do
Kamke 1258	✓	0.166	146	✓	0.054	110	To Do
Kamke 1259	✓	0.144	120	✓	0.059	92	To Do
Kamke 1260	✓	0.171	65	✓	0.566	76	To Do
Kamke 1261	✗	0	0	✓	0.234	105	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1262	✓	41.085	87	✓	0.263	53	To Do
Kamke 1263	✗	0	0	✓	0.086	52	To Do
Kamke 1264	✓	0.064	23	✓	0.045	19	To Do
Kamke 1265	✓	0.044	64	✓	0.131	93	To Do
Kamke 1266	✓	0.03	22	✓	0.009	19	To Do
Kamke 1267	✗	0	0	✓	0.072	41	To Do
Kamke 1268	✗	0	0	✓	0.111	39	To Do
Kamke 1269	✓	0.086	60	✓	0.095	40	To Do
Kamke 1270	✗	0	0	✓	0.185	46	To Do
Kamke 1271	✓	0.013	27	✓	0.007	14	To Do
Kamke 1272	✓	0.013	32	✓	0.036	23	To Do
Kamke 1273	✓	0.018	20	✓	0.074	17	To Do
Kamke 1274	✓	0.043	38	✓	0.01	19	To Do
Kamke 1275	✓	0.036	120	✓	0.159	53	To Do
Kamke 1276	✓	0.059	55	✓	0.066	31	To Do
Kamke 1277	✓	0.027	51	✓	0.056	27	To Do
Kamke 1278	✗	0	0	✗	0	0	To Do
Kamke 1279	✓	0.172	74	✓	0.167	32	To Do
Kamke 1280	✓	0.039	52	✓	0.055	40	To Do
Kamke 1281	✓	0.02	28	✓	0.046	15	To Do
Kamke 1282	✓	0.023	39	✓	0.046	21	To Do
Kamke 1283	✓	0.106	90	✓	0.138	48	To Do
Kamke 1284	✓	0.045	47	✓	0.022	41	To Do
Kamke 1285	✓	0.318	134	✓	0.102	52	To Do
Kamke 1286	✓	0.103	101	✓	0.022	32	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1287	✓	0.019	83	✓	0.027	27	To Do
Kamke 1288	✓	0.036	47	✓	0.026	21	To Do
Kamke 1289	✓	0.079	53	✓	0.085	33	To Do
Kamke 1290	✓	0.165	103	✓	0.02	47	To Do
Kamke 1291	✓	0.073	92	✓	0.058	62	To Do
Kamke 1292	✓	0.04	53	✓	0.06	31	To Do
Kamke 1293	✓	0.324	44	✓	0.073	33	To Do
Kamke 1294	✓	0.066	44	✓	0.072	33	To Do
Kamke 1295	✓	0.257	310	✓	0.302	106	To Do
Kamke 1296	✓	0.531	356	✓	0.347	150	To Do
Kamke 1297	✓	0.034	52	✓	0.023	63	To Do
Kamke 1298	✓	0.078	162	✓	0.125	124	To Do
Kamke 1299	✓	0.014	19	✓	0.019	27	To Do
Kamke 1300	✓	0.016	41	✓	0.054	31	To Do
Kamke 1301	✓	0.034	31	✓	0.023	19	To Do
Kamke 1302	✓	0.084	243	✓	0.061	98	To Do
Kamke 1303	✗	0	0	✓	0.225	501	To Do
Kamke 1304	✓	0.034	50	✓	0.036	38	To Do
Kamke 1305	✓	0.072	47	✓	0.055	44	To Do
Kamke 1306	✗	0	0	✓	0.158	69	To Do
Kamke 1307	✓	0.086	54	✓	0.058	36	To Do
Kamke 1308	✓	0.022	41	✓	0.019	40	To Do
Kamke 1309	✓	0.083	84	✓	0.094	85	To Do
Kamke 1310	✓	0.013	31	✓	0.013	20	To Do
Kamke 1311	✓	0.134	63	✓	0.15	52	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1312	✓	0.025	32	✓	0.021	19	To Do
Kamke 1313	✓	0.211	87	✓	0.095	35	To Do
Kamke 1314	✓	0.189	87	✓	0.083	33	To Do
Kamke 1315	✓	0.028	44	✓	0.02	45	To Do
Kamke 1316	✓	0.094	38	✓	0.041	18	To Do
Kamke 1317	✓	0.127	38	✓	0.039	13	To Do
Kamke 1318	✓	0.296	172	✓	0.141	122	To Do
Kamke 1319	✓	0.1	118	✓	0.116	31	To Do
Kamke 1320	✓	0.069	21	✓	0.047	17	To Do
Kamke 1321	✓	0.028	18	✓	0.03	15	To Do
Kamke 1322	✓	0.033	44	✓	0.03	44	To Do
Kamke 1323	✗	0	0	✓	0.02	17	To Do
Kamke 1324	✓	0.03	25	✓	0.032	18	To Do
Kamke 1325	✓	0.267	52	✓	0.137	86	To Do
Kamke 1326	✓	0.026	29	✓	0.03	22	To Do
Kamke 1327	✓	0.169	104	✓	0.127	81	To Do
Kamke 1328	✓	0.023	36	✓	0.03	27	To Do
Kamke 1329	✗	0	0	✓	0.377	64	To Do
Kamke 1330	✗	0	0	✓	1.211	1147	To Do
Kamke 1331	✓	0.046	55	✓	0.026	19	To Do
Kamke 1332	✓	0.026	26	✓	0.021	17	To Do
Kamke 1333	✓	0.116	70	✓	0.078	45	To Do
Kamke 1334	✓	0.203	114	✓	0.1	89	To Do
Kamke 1335	✓	0.324	893	✓	0.055	57	To Do
Kamke 1336	✓	0.056	70	✓	0.054	44	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1337	✓	0.088	62	✓	0.035	27	To Do
Kamke 1338	✓	0.069	40	✓	0.037	27	To Do
Kamke 1339	✓	0.277	66	✓	0.142	76	To Do
Kamke 1340	✓	0.037	32	✓	0.033	20	To Do
Kamke 1341	✗	0	0	✓	0.182	201	To Do
Kamke 1342	✓	0.044	51	✓	0.027	31	To Do
Kamke 1343	✗	0	0	✓	0.108	58	To Do
Kamke 1344	✓	0.565	173	✓	0.048	23	To Do
Kamke 1345	✓	0.03	52	✓	0.049	25	To Do
Kamke 1346	✓	0.325	87	✓	0.054	25	To Do
Kamke 1347	✓	0.086	31	✓	0.029	19	To Do
Kamke 1348	✗	0	0	✓	0.207	73	To Do
Kamke 1349	✓	0.097	76	✓	0.075	85	To Do
Kamke 1350	✓	0.011	25	✓	0.008	21	To Do
Kamke 1351	✓	0.028	50	✓	0.033	24	To Do
Kamke 1352	✓	0.015	89	✓	0.043	43	To Do
Kamke 1353	✓	0.108	119	✓	0.211	66	To Do
Kamke 1354	✓	0.072	108	✓	0.256	33	To Do
Kamke 1355	✓	0.13	59	✓	0.142	30	To Do
Kamke 1356	✓	0.303	90	✓	0.084	29	To Do
Kamke 1357	✓	0.667	288	✓	0.128	97	To Do
Kamke 1358	✓	0.066	66	✓	0.046	20	To Do
Kamke 1359	✓	0.105	86	✓	0.098	57	To Do
Kamke 1360	✓	0.097	68	✓	0.079	47	To Do
Kamke 1361	✓	0.485	38	✓	0.035	33	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1362	✗	0	0	✓	0.252	109	To Do
Kamke 1363	✓	0.803	236	✓	0.153	161	To Do
Kamke 1364	✓	0.17	42	✓	0.114	25	To Do
Kamke 1365	✓	0.096	72	✓	0.064	59	To Do
Kamke 1366	✓	0.024	31	✓	0.01	17	To Do
Kamke 1367	✗	0	0	✓	0.26	88	To Do
Kamke 1368	✓	0.028	106	✓	0.078	71	To Do
Kamke 1369	✓	0.104	75	✓	0.055	55	To Do
Kamke 1370	✓	0.031	53	✓	0.011	19	To Do
Kamke 1371	✓	0.023	48	✓	0.054	37	To Do
Kamke 1372	✗	0	0	✓	0.297	110	To Do
Kamke 1373	✗	0	0	✓	0.244	84	To Do
Kamke 1374	✓	0.039	32	✓	0.058	23	To Do
Kamke 1375	✓	0.053	54	✓	0.081	29	To Do
Kamke 1376	✓	0.099	82	✓	0.031	73	To Do
Kamke 1377	✓	0.237	109	✓	0.132	83	To Do
Kamke 1378	✓	0.054	65	✓	0.052	48	To Do
Kamke 1379	✓	0.082	99	✓	0.069	59	To Do
Kamke 1380	✓	0.305	132	✓	0.089	67	To Do
Kamke 1381	✓	0.716	589	✓	0.177	175	To Do
Kamke 1382	✓	0.704	154	✓	0.121	104	To Do
Kamke 1383	✓	0.141	50	✓	0.052	39	To Do
Kamke 1384	✓	0.034	110	✓	0.27	73	To Do
Kamke 1385	✓	0.02	78	✓	0.066	55	To Do
Kamke 1386	✓	0.093	108	✓	0.072	58	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1387	✓	0.041	50	✓	0.032	28	To Do
Kamke 1388	✓	0.305	235	✓	0.083	76	To Do
Kamke 1389	✓	0.385	217	✓	0.081	68	To Do
Kamke 1390	✓	0.042	51	✓	0.045	25	To Do
Kamke 1391	✓	0.059	27	✓	0.028	20	To Do
Kamke 1392	✓	92.845	1763961	✓	0.237	561	To Do
Kamke 1393	✓	19.1	413606	✓	0.161	272	To Do
Kamke 1394	✓	0.051	115	✓	0.12	79	To Do
Kamke 1395	✓	0.161	78	✓	0.06	39	To Do
Kamke 1396	✓	1.425	211	✓	0.161	178	To Do
Kamke 1397	✓	0.028	38	✓	0.089	27	To Do
Kamke 1398	✗	0	0	✓	0.189	69	To Do
Kamke 1399	✓	0.054	72	✓	0.085	34	To Do
Kamke 1400	✓	0.051	60	✓	0.048	35	To Do
Kamke 1401	✓	0.014	93	✓	0.054	45	To Do
Kamke 1402	✗	0	0	✓	0.305	58	To Do
Kamke 1403	✗	0	0	✓	1.052	298	To Do
Kamke 1404	✓	0.024	33	✓	0.048	19	To Do
Kamke 1405	✓	0.075	77	✓	0.074	42	To Do
Kamke 1406	✗	0	0	✓	0.158	44	To Do
Kamke 1407	✗	0	0	✓	2.766	2597	To Do
Kamke 1408	✗	0	0	✗	0	0	To Do
Kamke 1409	✓	0.025	43	✓	0.016	39	To Do
Kamke 1410	✓	0.133	481	✓	0.296	253	To Do
Kamke 1411	✓	0.332	42	✓	0.021	27	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1412	✓	0.017	29	✓	0.009	23	To Do
Kamke 1413	✗	0	0	✓	0.05	12	To Do
Kamke 1414	✓	1.137	231	✓	0.267	97	To Do
Kamke 1415	✓	0.847	273	✓	0.145	36	To Do
Kamke 1416	✓	0.205	46	✓	0.183	26	To Do
Kamke 1417	✓	0.14	52	✓	0.148	31	To Do
Kamke 1418	✗	0	0	✓	15.536	59	To Do
Kamke 1419	✗	0	0	✓	0.239	12	To Do
Kamke 1420	✓	0.441	134	✓	0.325	123	To Do
Kamke 1421	✓	0.248	67	✓	0.076	27	To Do
Kamke 1422	✓	0.087	64	✓	0.254	50	To Do
Kamke 1423	✓	0.072	70	✓	0.28	132	To Do
Kamke 1424	✓	0.173	90	✓	0.289	120	To Do
Kamke 1425	✓	0.761	236	✓	0.47	91	To Do
Kamke 1426	✓	6.089	4128	✓	0.643	549	To Do
Kamke 1427	✗	0	0	✓	1.68	179	To Do
Kamke 1428	✓	0.405	104	✓	0.323	183	To Do
Kamke 1429	✓	0.058	51	✓	0.036	25	To Do
Kamke 1430	✓	0.475	22	✓	0.366	101	To Do
Kamke 1431	✓	0.221	80	✓	0.233	30	To Do
Kamke 1432	✓	0.097	37	✓	0.045	22	To Do
Kamke 1433	✓	0.257	46	✓	0.116	28	To Do
Kamke 1434	✓	107.712	1596424	✓	0.68	517	To Do
Kamke 1435	✓	0.143	70	✓	0.171	38	To Do
Kamke 1436	✓	0.54	42	✓	0.281	113	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1437	✓	0.281	44	✓	0.177	29	To Do
Kamke 1438	✓	0.938	615	✓	0.181	102	To Do
Kamke 1439	✗	0	0	✗	0	0	To Do
Kamke 1440	✗	0	0	✗	0	0	To Do
Kamke 1441	✗	0	0	✗	0	0	To Do
Kamke 1442	✗	0	0	✓	0.07	30	To Do
Kamke 1443	✗	0	0	✗	0	0	To Do
Kamke 1444	✗	0	0	✓	0.015	37	To Do
Kamke 1445	✗	0	0	✓	0.279	20	To Do
Kamke 1446	✓	0.023	33	✓	0.046	22	To Do
Kamke 1447	✓	0.021	29	✓	0.06	20	To Do
Kamke 1448	✓	0.325	149	✓	0.103	77	To Do
Kamke 1449	✓	0.016	53	✓	0.013	47	To Do
Kamke 1450	✗	0	0	✓	0.233	1616	To Do
Kamke 1451	✓	0.023	168	✓	0.092	114	To Do
Kamke 1452	✓	0.008	54	✓	0.008	35	To Do
Kamke 1453	✓	0.629	128	✓	0.138	122	To Do
Kamke 1454	✓	0.01	79	✓	0.056	55	To Do
Kamke 1455	✓	0.029	127	✓	0.145	71	To Do
Kamke 1456	✓	0.036	183	✓	0.066	73	To Do
Kamke 1457	✗	0	0	✗	0	0	To Do
Kamke 1458	✗	0	0	✗	0	0	To Do
Kamke 1459	✗	0	0	✗	0	0	To Do
Kamke 1460	✗	0	0	✗	0	0	To Do
Kamke 1461	✗	0	0	✗	0	0	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1462	✗	0	0	✗	0	0	To Do
Kamke 1463	✗	0	0	✗	0	0	To Do
Kamke 1464	✓	0.006	34	✓	0.006	27	To Do
Kamke 1465	✓	0.088	95	✓	0.077	214	To Do
Kamke 1466	✓	0.017	46	✓	0.02	27	To Do
Kamke 1467	✓	0.007	84	✓	0.022	590	To Do
Kamke 1468	✓	0.086	57	✓	0.082	59	To Do
Kamke 1469	✓	0.035	72	✓	0.026	37	To Do
Kamke 1470	✗	0	0	✓	0.087	36	To Do
Kamke 1471	✗	0	0	✓	0.204	36	To Do
Kamke 1472	✗	0	0	✓	0.285	33	To Do
Kamke 1473	✗	0	0	✗	0	0	To Do
Kamke 1474	✗	0	0	✗	0	0	To Do
Kamke 1475	✓	0.028	38	✓	0.021	23	To Do
Kamke 1476	✗	0	0	✗	0	0	To Do
Kamke 1477	✓	0.178	48	✓	0.02	41	To Do
Kamke 1478	✓	0.034	104	✓	0.127	48	To Do
Kamke 1479	✓	0.149	153	✓	0.244	92	To Do
Kamke 1480	✓	0.221	93	✓	0.267	35	To Do
Kamke 1481	✓	0.997	431	✓	0.053	44	To Do
Kamke 1482	✗	0	0	✓	0.328	1616	To Do
Kamke 1483	✓	0.156	112	✓	0.273	37	To Do
Kamke 1484	✗	0	0	✗	0	0	To Do
Kamke 1485	✓	0.119	66	✓	0.379	51	To Do
Kamke 1486	✓	0.17	65	✓	0.25	51	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1487	✗	0	0	✓	0.086	38	To Do
Kamke 1488	✓	0.562	102	✓	0.553	132	To Do
Kamke 1489	✗	0	0	✗	0	0	To Do
Kamke 1490	✓	0.019	33	✓	0.064	18	To Do
Kamke 1491	✓	0.046	102	✓	0.09	88	To Do
Kamke 1492	✓	0.414	43	✓	0.114	39	To Do
Kamke 1493	✓	7.457	2582	✓	0.323	1033	To Do
Kamke 1494	✓	0.029	43	✓	0.022	32	To Do
Kamke 1495	✓	0.019	24	✓	0.013	16	To Do
Kamke 1496	✓	0.274	63	✓	0.028	57	To Do
Kamke 1497	✓	0.49	135	✓	0.277	77	To Do
Kamke 1498	✓	8.46	584	✓	0.267	53	To Do
Kamke 1499	✓	0.238	97	✓	0.277	25	To Do
Kamke 1500	✗	0	0	✓	0.227	55	To Do
Kamke 1501	✓	0.203	86	✓	0.246	37	To Do
Kamke 1502	✓	0.06	98	✓	0.49	103	To Do
Kamke 1503	✓	0.12	62	✓	0.029	67	To Do
Kamke 1504	✓	0.114	43	✓	0.216	18	To Do
Kamke 1505	✗	0	0	✓	0.157	79	To Do
Kamke 1506	✗	0	0	✓	0.06	43	To Do
Kamke 1507	✗	0	0	✓	0.651	1210	To Do
Kamke 1508	✓	0.842	143	✓	0.153	81	To Do
Kamke 1509	✓	0.011	34	✓	0.057	29	To Do
Kamke 1510	✗	0	0	✗	0	0	To Do
Kamke 1511	✓	0.038	51	✓	0.033	49	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1512	✓	0.039	29	✓	0.013	18	To Do
Kamke 1513	✓	0.08	25	✓	0.226	18	To Do
Kamke 1514	✓	0.742	102	✓	0.546	132	To Do
Kamke 1515	✗	0	0	✗	0	0	To Do
Kamke 1516	✗	0	0	✓	0.477	188	To Do
Kamke 1517	✓	0.404	30686	✓	0.519	866	To Do
Kamke 1518	✓	0.244	106	✓	0.474	60	To Do
Kamke 1519	✓	0.031	65	✓	0.155	19	To Do
Kamke 1520	✗	0	0	✓	0.596	288	To Do
Kamke 1521	✓	0.069	35	✓	0.454	28	To Do
Kamke 1522	✓	0.021	44	✓	0.043	34	To Do
Kamke 1523	✓	0.124	74	✓	0.469	23	To Do
Kamke 1524	✓	0.155	96	✓	0.536	98	To Do
Kamke 1525	✓	0.448	102	✓	0.502	133	To Do
Kamke 1526	✗	0	0	✓	0.238	19	To Do
Kamke 1527	✗	0	0	✓	0.598	437	To Do
Kamke 1528	✓	0.625	72	✓	0.199	71	To Do
Kamke 1529	✗	0	0	✓	0.087	25	To Do
Kamke 1530	✗	0	0	✓	0.252	113	To Do
Kamke 1531	✗	0	0	✗	0	0	To Do
Kamke 1532	✓	0.018	103	✓	0.102	58	To Do
Kamke 1533	✓	0.019	113	✓	0.099	58	To Do
Kamke 1534	✓	0.005	24	✓	0.009	21	To Do
Kamke 1535	✓	1.357	219	✓	0.019	36	To Do
Kamke 1536	✓	0.006	76	✓	0.013	50	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1537	✓	0.949	1722	✓	0.147	67	To Do
Kamke 1538	✓	0.261	66	✓	0.523	51	To Do
Kamke 1539	✓	0.008	44	✓	0.027	35	To Do
Kamke 1540	✗	0	0	✗	0	0	To Do
Kamke 1541	✗	0	0	✗	0	0	To Do
Kamke 1542	✗	0	0	✗	0	0	To Do
Kamke 1543	✗	0	0	✗	0	0	To Do
Kamke 1544	✗	0	0	✓	0.017	41	To Do
Kamke 1545	✓	0.177	40	✓	0.137	27	To Do
Kamke 1546	✓	0.71	301	✓	0.053	73	To Do
Kamke 1547	✗	0	0	✓	0.023	87	To Do
Kamke 1548	✓	0.095	50	✓	0.069	32	To Do
Kamke 1549	✓	0.013	34	✓	0.02	26	To Do
Kamke 1550	✓	4.926	262	✓	0.789	157	To Do
Kamke 1551	✓	0.442	110	✓	0.265	62	To Do
Kamke 1552	✗	0	0	✓	0.076	89	To Do
Kamke 1553	✓	0.024	29	✓	0.011	17	To Do
Kamke 1554	✓	0.024	29	✓	0.013	18	To Do
Kamke 1555	✓	0.069	156	✓	0.181	61	To Do
Kamke 1556	✓	0.023	30	✓	0.014	19	To Do
Kamke 1557	✓	0.073	146	✓	0.142	61	To Do
Kamke 1558	✓	0.167	319	✓	0.194	67	To Do
Kamke 1559	✓	0.3	100	✓	0.185	33	To Do
Kamke 1560	✓	0.022	29	✓	0.011	18	To Do
Kamke 1561	✓	3.961	400	✓	0.285	69	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1562	✓	1.118	140	✓	0.408	77	To Do
Kamke 1563	✓	1.873	232	✓	0.283	87	To Do
Kamke 1564	✓	1.371	230	✓	0.263	88	To Do
Kamke 1565	✓	0.562	242	✓	0.437	71	To Do
Kamke 1566	✓	0.666	238	✓	0.399	35	To Do
Kamke 1567	✓	0.023	30	✓	0.017	19	To Do
Kamke 1568	✓	0.013	122	✓	0.03	89	To Do
Kamke 1569	✗	0	0	✓	0.55	63	To Do
Kamke 1570	✓	0.155	470	✓	0.102	49	To Do
Kamke 1571	✓	0.096	390	✓	0.204	143	To Do
Kamke 1572	✗	0	0	✓	0.464	35	To Do
Kamke 1573	✗	0	0	✓	0.049	41	To Do
Kamke 1574	✗	0	0	✓	0.886	252	To Do
Kamke 1575	✗	0	0	✓	0.5	719	To Do
Kamke 1576	✗	0	0	✓	0.027	67	To Do
Kamke 1577	✓	1.087	44	✓	0.007	21	To Do
Kamke 1578	✓	289.847	139	✓	1.366	89	To Do
Kamke 1579	✓	0.678	104	✓	0.414	69	To Do
Kamke 1580	✓	0.985	234	✓	0.803	147	To Do
Kamke 1581	✗	0	0	✗	0	0	To Do
Kamke 1582	✓	0.648	787	✗	0	0	To Do
Kamke 1583	✗	0	0	✓	0.03	40	To Do
Kamke 1584	✓	2.906	216	✓	0.274	118	To Do
Kamke 1585	✓	0.228	214	✓	0.032	679	To Do
Kamke 1586	✗	0	0	✗	0	0	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1587	✓	0.377	492	✓	0.556	174	To Do
Kamke 1588	✓	6.223	114	✓	0.151	90	To Do
Kamke 1589	✓	0.052	670	✓	9.116	4339	To Do
Kamke 1590	✗	0	0	✓	2.786	553	To Do
Kamke 1591	✓	0.065	26	✓	0.017	12	To Do
Kamke 1592	✓	0.032	14	✓	0.013	10	To Do
Kamke 1593	✗	0	0	✗	0	0	To Do
Kamke 1594	✓	0.369	373	✓	0.099	59	To Do
Kamke 1595	✗	0	0	✗	0	0	To Do
Kamke 1596	✗	0	0	✗	0	0	To Do
Kamke 1597	✓	2.406	242	✓	0.026	21	To Do
Kamke 1598	✗	0	0	✗	0	0	To Do
Kamke 1599	✗	0	0	✗	0	0	To Do
Kamke 1600	✓	2.246	1017	✓	0.097	89	To Do
Kamke 1601	✗	0	0	✓	3.115	151	To Do
Kamke 1602	✓	87.998	46	✓	0.244	73	To Do
Kamke 1603	✗	0	0	✓	71.214	8411	To Do
Kamke 1604	✓	0.097	34	✓	0.353	23	To Do
Kamke 1605	✗	0	0	✓	1.309	104	To Do
Kamke 1606	✗	0	0	✗	0	0	To Do
Kamke 1607	✓	0.172	79	✓	0.122	49	To Do
Kamke 1608	✗	0	0	✗	0	0	To Do
Kamke 1609	✗	0	0	✗	0	0	To Do
Kamke 1610	✗	0	0	✓	0.295	92	To Do
Kamke 1611	✗	0	0	✓	0.529	57	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1612	✗	0	0	✓	1.318	57	To Do
Kamke 1613	✗	0	0	✓	0.023	27	To Do
Kamke 1614	✗	0	0	✓	0.066	33	To Do
Kamke 1615	✗	0	0	✓	4.878	91	To Do
Kamke 1616	✗	0	0	✓	1.356	63	To Do
Kamke 1617	✗	0	0	✗	0	0	To Do
Kamke 1618	✗	0	0	✓	1.736	56	To Do
Kamke 1619	✗	0	0	✗	0	0	To Do
Kamke 1620	✗	0	0	✓	0.125	253	To Do
Kamke 1621	✗	0	0	✓	1.625	1088	To Do
Kamke 1622	✗	0	0	✓	0.527	817	To Do
Kamke 1623	✗	0	0	✗	0	0	To Do
Kamke 1624	✗	0	0	✓	2.	131	To Do
Kamke 1625	✗	0	0	✗	0	0	To Do
Kamke 1626	✗	0	0	✓	0.232	48	To Do
Kamke 1627	✗	0	0	✓	0.961	58	To Do
Kamke 1628	✗	0	0	✗	0	0	To Do
Kamke 1629	✗	0	0	✓	0.039	38	To Do
Kamke 1630	✓	11.1	3227	✓	0.625	783	To Do
Kamke 1631	✗	0	0	✓	0.049	38	To Do
Kamke 1632	✓	0.062	46	✓	0.095	23	To Do
Kamke 1633	✗	0	0	✓	0.279	97	To Do
Kamke 1634	✗	0	0	✗	0	0	To Do
Kamke 1635	✗	0	0	✓	0.178	79	To Do
Kamke 1636	✗	0	0	✓	0.89	59	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1637	✗	0	0	✓	0.554	58	To Do
Kamke 1638	✗	0	0	✓	0.192	115	To Do
Kamke 1639	✗	0	0	✓	3.636	56	To Do
Kamke 1640	✗	0	0	✓	0.191	70	To Do
Kamke 1641	✓	1.996	57	✓	0.039	29	To Do
Kamke 1642	✗	0	0	✗	0	0	To Do
Kamke 1643	✗	0	0	✗	0	0	To Do
Kamke 1644	✗	0	0	✓	0.556	56	To Do
Kamke 1645	✗	0	0	✗	0	0	To Do
Kamke 1646	✓	10.725	262	✓	0.178	94	To Do
Kamke 1647	✓	52.167	59	✓	0.461	60	To Do
Kamke 1648	✗	0	0	✓	2.059	205	To Do
Kamke 1649	✗	0	0	✗	0	0	To Do
Kamke 1650	✓	0.022	30	✓	0.238	16	To Do
Kamke 1651	✓	0.263	414	✓	0.163	31	To Do
Kamke 1652	✗	0	0	✓	0.309	36	To Do
Kamke 1653	✓	0.067	75	✓	0.135	41	To Do
Kamke 1654	✓	0.277	308	✓	0.187	38	To Do
Kamke 1655	✓	0.817	350	✓	0.22	84	To Do
Kamke 1656	✗	0	0	✓	0.78	771	To Do
Kamke 1657	✓	0.15	33	✓	0.268	35	To Do
Kamke 1658	✗	0	0	✓	0.143	115	To Do
Kamke 1659	✗	0	0	✓	0.093	60	To Do
Kamke 1660	✗	0	0	✓	0.944	125	To Do
Kamke 1661	✓	0.032	92	✓	0.085	51	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1662	✗	0	0	✓	0.4	56	To Do
Kamke 1663	✗	0	0	✓	0.959	125	To Do
Kamke 1664	✗	0	0	✓	3.272	155	To Do
Kamke 1665	✗	0	0	✓	0.617	84	To Do
Kamke 1666	✗	0	0	✓	0.963	93	To Do
Kamke 1667	✗	0	0	✓	1.548	121	To Do
Kamke 1668	✓	0.072	60	✓	0.162	24	To Do
Kamke 1669	✓	103.623	126	✓	0.119	32	To Do
Kamke 1670	✓	83.764	50	✓	0.398	35	To Do
Kamke 1671	✓	0.036	59	✓	0.092	35	To Do
Kamke 1672	✗	0	0	✓	1.094	65	To Do
Kamke 1673	✗	0	0	✓	0.813	60	To Do
Kamke 1674	✓	0.059	106	✓	0.069	25	To Do
Kamke 1675	✗	0	0	✗	0	0	To Do
Kamke 1676	✓	53.353	133	✓	0.28	72	To Do
Kamke 1677	✗	0	0	✓	2.267	101	To Do
Kamke 1678	✗	0	0	✓	0.265	60	To Do
Kamke 1679	✓	0.077	33	✓	0.152	27	To Do
Kamke 1680	✗	0	0	✓	0.638	103	To Do
Kamke 1681	✗	0	0	✓	0.056	31	To Do
Kamke 1682	✗	0	0	✓	0.638	94	To Do
Kamke 1683	✓	0.073	26	✓	0.056	23	To Do
Kamke 1684	✗	0	0	✓	1.717	100	To Do
Kamke 1685	✗	0	0	✗	0	0	To Do
Kamke 1686	✗	0	0	✓	1.18	128	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1687	✓	0.068	262	✓	0.104	21	To Do
Kamke 1688	✓	249.261	166	✓	0.113	32	To Do
Kamke 1689	✓	0.64	329	✓	0.162	37	To Do
Kamke 1690	✗	0	0	✓	0.837	99	To Do
Kamke 1691	✗	0	0	✓	1.267	254	To Do
Kamke 1692	✗	0	0	✓	3.955	156	To Do
Kamke 1693	✗	0	0	✓	0.329	68	To Do
Kamke 1694	✓	0.188	115	✓	0.135	54	To Do
Kamke 1695	✗	0	0	✓	0.627	103	To Do
Kamke 1696	✗	0	0	✓	0.513	100	To Do
Kamke 1697	✓	0.062	94	✓	0.044	39	To Do
Kamke 1698	✓	0.041	72	✗	0	0	To Do
Kamke 1699	✓	0.038	40	✓	0.096	33	To Do
Kamke 1700	✓	0.077	44	✓	0.331	86	To Do
Kamke 1701	✓	0.18	97	✓	0.289	42	To Do
Kamke 1702	✗	0	0	✗	0	0	To Do
Kamke 1703	✓	0.092	63	✓	0.07	25	To Do
Kamke 1704	✗	0	0	✗	0	0	To Do
Kamke 1705	✗	0	0	✗	0	0	To Do
Kamke 1706	✗	0	0	✗	0	0	To Do
Kamke 1707	✓	0.072	31	✓	0.066	39	To Do
Kamke 1708	✗	0	0	✓	1.043	73	To Do
Kamke 1709	✗	0	0	✓	1.977	84	To Do
Kamke 1710	✗	0	0	✓	2.734	91	To Do
Kamke 1711	✗	0	0	✓	0.553	81	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1712	✓	10.59	70	✓	0.092	61	To Do
Kamke 1713	✗	0	0	✓	0.333	54	To Do
Kamke 1714	✓	0.065	25	✓	0.063	68	To Do
Kamke 1715	✓	0.037	26	✓	0.045	25	To Do
Kamke 1716	✓	0.68	172	✓	0.216	68	To Do
Kamke 1717	✓	1.592	290	✓	0.272	107	To Do
Kamke 1718	✓	1.499	744	✓	0.276	133	To Do
Kamke 1719	✗	0	0	✓	0.579	70	To Do
Kamke 1720	✗	0	0	✓	0.339	173	To Do
Kamke 1721	✗	0	0	✗	0	0	To Do
Kamke 1722	✓	1.964	797	✓	0.44	98	To Do
Kamke 1723	✓	0.86	259	✓	0.13	16	To Do
Kamke 1724	✓	0.224	38	✓	0.587	21	To Do
Kamke 1725	✓	0.353	75	✓	0.577	105	To Do
Kamke 1726	✓	0.717	75	✓	0.112	39	To Do
Kamke 1727	✓	0.182	129	✓	0.222	87	To Do
Kamke 1728	✓	0.007	31	✓	0.035	24	To Do
Kamke 1729	✗	0	0	✗	0	0	To Do
Kamke 1730	✓	0.489	127	✓	0.098	53	To Do
Kamke 1731	✓	1.423	359	✓	0.102	61	To Do
Kamke 1732	✗	0	0	✗	0	0	To Do
Kamke 1733	✓	2.562	437	✓	0.101	71	To Do
Kamke 1734	✗	0	0	✗	0	0	To Do
Kamke 1735	✗	0	0	✗	0	0	To Do
Kamke 1736	✓	8.488	285	✓	0.099	49	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1737	✗	0	0	✗	0	0	To Do
Kamke 1738	✗	0	0	✗	0	0	To Do
Kamke 1739	✗	0	0	✗	0	0	To Do
Kamke 1740	✓	0.027	16	✓	0.036	13	To Do
Kamke 1741	✓	0.094	17	✓	0.075	34	To Do
Kamke 1742	✗	0	0	✓	0.191	60	To Do
Kamke 1743	✓	18.107	2761	✓	0.111	71	To Do
Kamke 1744	✓	0.987	173	✓	0.225	87	To Do
Kamke 1745	✓	0.311	204	✓	0.386	117	To Do
Kamke 1746	✗	0	0	✓	0.596	207	To Do
Kamke 1747	✓	0.029	20	✓	0.018	17	To Do
Kamke 1748	✓	0.097	43	✓	0.125	67	To Do
Kamke 1749	✓	0.553	181	✓	0.289	57	To Do
Kamke 1750	✓	3.507	2281	✓	0.426	87	To Do
Kamke 1751	✗	0	0	✗	0	0	To Do
Kamke 1752	✓	0.129	26	✓	0.096	33	To Do
Kamke 1753	✓	0.323	43	✓	0.135	147	To Do
Kamke 1754	✓	0.034	17	✓	0.038	15	To Do
Kamke 1755	✗	0	0	✓	0.341	418	To Do
Kamke 1756	✓	0.288	111	✓	0.121	75	To Do
Kamke 1757	✗	0	0	✗	0	0	To Do
Kamke 1758	✓	0.066	36	✓	0.059	42	To Do
Kamke 1759	✓	0.036	18	✓	0.027	31	To Do
Kamke 1760	✗	0	0	✓	0.083	114	To Do
Kamke 1761	✗	0	0	✗	0	0	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1762	✗	0	0	✓	0.911	108	To Do
Kamke 1763	✓	0.139	35	✓	0.053	148	To Do
Kamke 1764	✓	0.062	52	✓	0.195	18	To Do
Kamke 1765	✓	0.124	24	✓	0.03	27	To Do
Kamke 1766	✓	0.045	21	✓	0.033	64	To Do
Kamke 1767	✓	0.075	55	✓	0.345	50	To Do
Kamke 1768	✓	0.114	87	✓	0.058	43	To Do
Kamke 1769	✓	0.045	18	✓	0.035	21	To Do
Kamke 1770	✓	0.757	28	✓	0.062	26	To Do
Kamke 1771	✓	0.081	21	✓	0.162	22	To Do
Kamke 1772	✓	0.925	37	✓	0.151	37	To Do
Kamke 1773	✓	0.185	44	✓	0.043	30	To Do
Kamke 1774	✓	1.368	93	✓	0.253	136	To Do
Kamke 1775	✓	0.13	29	✓	0.1	31	To Do
Kamke 1776	✗	0	0	✓	0.352	49	To Do
Kamke 1777	✗	0	0	✓	0.74	79	To Do
Kamke 1778	✓	0.523	75	✓	0.469	245	To Do
Kamke 1779	✗	0	0	✓	0.543	112	To Do
Kamke 1780	✗	0	0	✓	0.599	160	To Do
Kamke 1781	✓	0.081	19	✓	0.053	11	To Do
Kamke 1782	✓	0.086	93	✓	0.048	33	To Do
Kamke 1783	✓	1.374	26	✓	0.174	23	To Do
Kamke 1784	✓	0.261	74	✓	0.569	82	To Do
Kamke 1785	✓	0.356	95	✓	0.359	83	To Do
Kamke 1786	✓	0.994	95	✓	0.164	42	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1787	✗	0	0	✓	0.283	80	To Do
Kamke 1788	✗	0	0	✗	0	0	To Do
Kamke 1789	✗	0	0	✗	0	0	To Do
Kamke 1790	✓	22.697	182	✓	0.255	119	To Do
Kamke 1791	✓	22.471	164	✓	0.364	90	To Do
Kamke 1792	✓	25.731	222	✓	0.905	194	To Do
Kamke 1793	✓	1.343	113	✓	0.069	40	To Do
Kamke 1794	✓	1.256	98	✓	0.093	46	To Do
Kamke 1795	✓	0.252	116	✓	1.037	529	To Do
Kamke 1796	✓	0.32	66	✓	0.227	51	To Do
Kamke 1797	✗	0	0	✗	0	0	To Do
Kamke 1798	✗	0	0	✓	0.242	166	To Do
Kamke 1799	✓	1.882	88	✓	0.135	46	To Do
Kamke 1800	✓	0.493	84	✓	0.05	60	To Do
Kamke 1801	✗	0	0	✗	0	0	To Do
Kamke 1802	✗	0	0	✗	0	0	To Do
Kamke 1803	✓	18.365	10387	✓	2.665	115620	To Do
Kamke 1804	✓	2.925	415	✓	0.034	31	To Do
Kamke 1805	✓	1.803	436	✓	0.046	34	To Do
Kamke 1806	✗	0	0	✓	5.365	718	To Do
Kamke 1807	✗	0	0	✗	0	0	To Do
Kamke 1808	✓	103.879	172	✓	0.141	72	To Do
Kamke 1809	✗	0	0	✓	0.705	336	To Do
Kamke 1810	✓	0.103	1677	✓	0.119	91	To Do
Kamke 1811	✗	0	0	✓	3.85	1862	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1812	✓	0.027	29	✓	0.037	19	To Do
Kamke 1813	✗	0	0	✓	0.421	138	To Do
Kamke 1814	✓	13.034	116	✓	0.183	87	To Do
Kamke 1815	✗	0	0	✓	0.999	71	To Do
Kamke 1816	✗	0	0	✓	1.231	46	To Do
Kamke 1817	✗	0	0	✓	0.234	40	To Do
Kamke 1818	✗	0	0	✓	0.4	66	To Do
Kamke 1819	✗	0	0	✓	0.063	42	To Do
Kamke 1820	✗	0	0	✓	1.209	88	To Do
Kamke 1821	✗	0	0	✓	2.286	54	To Do
Kamke 1822	✓	1.038	371	✓	1.215	291	To Do
Kamke 1823	✗	0	0	✓	0.434	289	To Do
Kamke 1824	✓	0.35	347	✓	0.988	96	To Do
Kamke 1825	✗	0	0	✓	1.053	49	To Do
Kamke 1826	✓	0.596	119	✓	0.375	173	To Do
Kamke 1827	✗	0	0	✓	9.289	81	To Do
Kamke 1828	✓	0.01	32	✓	0.597	59	To Do
Kamke 1829	✓	0.006	24	✓	0.391	32	To Do
Kamke 1830	✓	0.028	24	✓	0.552	304	To Do
Kamke 1831	✗	0	0	✓	1.269	163	To Do
Kamke 1832	✗	0	0	✓	0.976	117	To Do
Kamke 1833	✗	0	0	✓	3.877	145	To Do
Kamke 1834	✗	0	0	✓	0.497	82	To Do
Kamke 1835	✓	0.113	143	✗	0	0	To Do
Kamke 1836	✗	0	0	✓	0.451	100	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1837	✗	0	0	✓	0.369	95	To Do
Kamke 1838	✗	0	0	✓	0.657	73	To Do
Kamke 1839	✗	0	0	✓	0.911	116	To Do
Kamke 1840	✗	0	0	✓	0.976	129	To Do
Kamke 1841	✗	0	0	✓	0.625	60	To Do
Kamke 1842	✓	0.167	286	✓	0.655	190	To Do
Kamke 1843	✓	2.885	409	✓	0.316	77	To Do
Kamke 1844	✗	0	0	✓	0.292	17	To Do
Kamke 1845	✗	0	0	✓	0.27	17	To Do
Kamke 1846	✓	0.041	51	✓	0.011	28	To Do
Kamke 1847	✓	0.123	95	✓	0.27	49	To Do
Kamke 1848	✗	0	0	✓	1.503	789	To Do
Kamke 1849	✓	0.584	426	✓	0.19	197	To Do
Kamke 1850	✗	0	0	✓	1.597	164	To Do
Kamke 1851	✗	0	0	✗	0	0	To Do
Kamke 1852	✓	0.035	28	✓	0.321	30	To Do
Kamke 1853	✗	0	0	✓	0.681	110	To Do
Kamke 1854	✗	0	0	✗	0	0	To Do
Kamke 1855	✗	0	0	✗	0	0	To Do
Kamke 1856	✓	0.006	22	✓	0.033	19	To Do
Kamke 1857	✓	0.037	39	✓	0.048	35	To Do
Kamke 1858	✓	0.01	182	✓	0.053	64	To Do
Kamke 1859	✓	0.007	51	✓	0.039	37	To Do
Kamke 1860	✓	0.046	696	✓	0.084	177	To Do
Kamke 1861	✓	0.013	183	✓	0.109	152	To Do

Continued on next page

Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1862	✓	0.057	52	✓	0.04	39	To Do
Kamke 1863	✓	0.008	84	✓	0.038	35	To Do
Kamke 1864	✓	0.013	59	✓	0.041	44	To Do
Kamke 1865	✓	1.197	2062	✓	0.136	224	To Do
Kamke 1866	✓	0.028	132	✓	0.04	39	To Do
Kamke 1867	✓	0.082	124	✓	0.036	42	To Do
Kamke 1868	✓	0.045	162	✓	0.073	64	To Do
Kamke 1869	✓	0.108	118	✓	0.06	51	To Do
Kamke 1870	✓	0.126	122	✓	0.113	47	To Do
Kamke 1871	✓	0.16	180	✓	0.077	62	To Do
Kamke 1872	✓	0.058	162	✓	0.068	65	To Do
Kamke 1873	✓	0.045	322	✓	0.063	52	To Do
Kamke 1874	✓	0.141	131	✓	0.458	57	To Do
Kamke 1875	✗	0	0	✓	1.264	1447	To Do
Kamke 1876	✓	0.105	41	✓	0.139	18	To Do
Kamke 1877	✓	0.006	31	✓	0.036	31	To Do
Kamke 1878	✓	0.012	39	✓	0.058	39	To Do
Kamke 1879	✓	0.063	58	✓	0.056	54	To Do
Kamke 1880	✗	0	0	✓	0.083	23	To Do
Kamke 1881	✓	0.032	44	✓	0.029	48	To Do
Kamke 1882	✓	0.444	928	✓	0.086	99	To Do
Kamke 1883	✓	0.579	614	✓	0.112	80	To Do
Kamke 1884	✓	0.189	226	✓	0.107	69	To Do
Kamke 1885	✗	0	0	✓	0.098	47	To Do
Kamke 1886	✓	0.021	115	✓	0.065	49	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1887	✓	0.534	5748	✓	0.14	360	To Do
Kamke 1888	✓	24.995	37858	✓	0.269	457	To Do
Kamke 1889	✓	0.101	554	✓	0.062	60	To Do
Kamke 1890	✗	0	0	✗	0	0	To Do
Kamke 1891	✓	0.438	766	✓	0.059	64	To Do
Kamke 1892	✓	0.393	4815	✓	0.155	463	To Do
Kamke 1893	✗	0	0	✓	1.276	1579	To Do
Kamke 1894	✗	0	0	✓	1.103	1056	To Do
Kamke 1895	✓	0.454	7517	✓	0.25	1008	To Do
Kamke 1896	✓	0.196	1132	✓	0.068	67	To Do
Kamke 1897	✓	0.109	284	✓	0.169	86	To Do
Kamke 1898	✓	0.042	420	✓	0.074	71	To Do
Kamke 1899	✓	0.011	112	✓	0.089	52	To Do
Kamke 1900	✓	0.01	94	✓	0.084	50	To Do
Kamke 1901	✓	0.011	105	✓	0.072	43	To Do
Kamke 1902	✓	0.015	226	✓	0.065	51	To Do
Kamke 1903	✓	0.089	1304	✓	0.155	299	To Do
Kamke 1904	✓	0.066	1445	✓	0.098	257	To Do
Kamke 1905	✗	0	0	✗	0	0	To Do
Kamke 1906	✓	0.05	278	✓	0.086	120	To Do
Kamke 1907	✓	0.01	179	✓	0.069	66	To Do
Kamke 1908	✓	0.021	551	✓	0.749	1213	To Do
Kamke 1909	✓	0.058	1630	✓	27.579	33085	To Do
Kamke 1910	✓	0.01	39	✓	0.109	37	To Do
Kamke 1911	✗	0	0	✓	0.159	308	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1912	✗	0	0	✓	2.798	2956	To Do
Kamke 1913	✓	0.037	64	✓	0.135	57	To Do
Kamke 1914	✓	0.649	201	✓	0.411	92	To Do
Kamke 1915	✗	0	0	✓	11.342	147	To Do
Kamke 1916	✗	0	0	✓	0.579	180	To Do
Kamke 1917	✗	0	0	✓	0.858	109	To Do
Kamke 1918	✗	0	0	✓	2.155	184	To Do
Kamke 1919	✗	0	0	✓	3.442	203	To Do
Kamke 1920	✗	0	0	✓	3.463	205	To Do
Kamke 1921	✗	0	0	✗	0	0	To Do
Kamke 1922	✗	0	0	✗	0	0	To Do
Kamke 1923	✓	0.012	53	✓	0.04	35	To Do
Kamke 1924	✓	0.071	191	✓	0.331	180	To Do
Kamke 1925	✗	0	0	✓	0.312	194	To Do
Kamke 1926	✗	0	0	✓	0.115	96	To Do
Kamke 1927	✗	0	0	✗	0	0	To Do
Kamke 1928	✗	0	0	✗	0	0	To Do
Kamke 1929	✗	0	0	✓	4.038	116	To Do
Kamke 1930	✓	0.041	308	✓	0.05	45	To Do
Kamke 1931	✓	5.511	10101	✓	0.828	1117	To Do
Kamke 1932	✗	0	0	✓	1.132	383	To Do
Kamke 1933	✗	0	0	✓	2.514	17738	To Do
Kamke 1934	✗	0	0	✓	1.358	377	To Do
Kamke 1935	✗	0	0	✓	2.187	741	To Do
Kamke 1936	✗	0	0	✓	0.778	704	To Do

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Table 3 – continued from previous page

	Mathematica			Maple			
#	solved	cpu	leaf	solved	cpu	leaf	note on solution
Kamke 1937	✗	0	0	✓	0.93	242	To Do
Kamke 1938	✓	0.009	137	✓	0.127	101	To Do
Kamke 1939	✗	0	0	✓	1.591	899	To Do
Kamke 1940	✗	0	0	✗	0	0	To Do

2.1 ODE No. 1

$$y'(x) - \frac{1}{\sqrt{\text{a0} + \text{a1}x + \text{a2}x^2 + \text{a3}x^3 + \text{a4}x^4}} = 0$$

✓ **Mathematica** : cpu = 0.657664 (sec), leaf count = 1117

$$\left\{\left\{y(x) \to c_1 - \frac{2F\left(\sin^{-1}\left(\sqrt{\frac{(x-\text{Root}\left[\text{a4}\#1^4+\text{a3}\#1^3+\text{a2}\#1^2+\text{a1}\#1+\text{a0}\&,1\right])(\text{Root}\left[\text{a4}\#1^4+\text{a3}\#1^3+\text{a2}\#1^2+\text{a1}\#1+\text{a0}\&,2\right]-\text{Root}}{(x-\text{Root}\left[\text{a4}\#1^4+\text{a3}\#1^3+\text{a2}\#1^2+\text{a1}\#1+\text{a0}\&,2\right])(\text{Root}\left[\text{a4}\#1^4+\text{a3}\#1^3+\text{a2}\#1^2+\text{a1}\#1+\text{a0}\&,1\right]-\text{Root}}\right)\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 1089

$$\left\{y(x) = 2\,\frac{(-RootOf\left(a4\_Z^4 + a3\_Z^3 + a2\_Z^2 + a1\_Z + \right.}{\left(RootOf\left(a4\_Z^4 + a3\_Z^3 + a2\_Z^2 + a1\_Z + a0, index = 4\right) - RootOf\left(a4\_Z^4 + a3\_Z^3 + a2\right.\right.}\right.$$

Hand solution

$$y' - \frac{1}{\sqrt{a_0 + a_1 x + a_2 x^2 + a_3 x^3 + a_4 x^4}} = 0 \tag{1}$$

To Do.

2.2 ODE No. 2

$$ay(x) + c\left(-e^{bx}\right) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0142178 (sec), leaf count = 34

$$\left\{\left\{y(x) \to \frac{ce^{x(a+b)-ax}}{a+b} + c_1 e^{-ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 25

$$\left\{y(x) = \left(\frac{c\mathrm{e}^{(a+b)x}}{a+b} + \_C1\right)\mathrm{e}^{-ax}\right\}$$

Hand solution

$$\frac{dy}{dx} + ay(x) = ce^{bx} \tag{1}$$

Integrating factor $\mu = e^{\int a dx} = e^{ax}$. Hence (1) becomes

$$\frac{d}{dx}(\mu y(x)) = \mu c e^{bx}$$
$$\mu y(x) = \int \mu c e^{bx} dx + C$$

Replacing μ by e^{ax}

$$\begin{aligned} y(x) &= ce^{-ax} \int e^{(a+b)x} dx + Ce^{-ax} \\ &= ce^{-ax} \frac{e^{(a+b)x}}{a+b} + Ce^{-ax} \\ &= \frac{ce^{(a+b)x-ax}}{a+b} + Ce^{-ax} \end{aligned}$$

Can be reduced to

$$y(x) = c\frac{e^{bx}}{a+b} + Ce^{-ax}$$

2.3 ODE No. 3

$$ay(x) - b\sin(cx) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0334829 (sec), leaf count = 40

$$\left\{\left\{y(x) \to \frac{b(a\sin(cx) - c\cos(cx))}{a^2 + c^2} + c_1 e^{-ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 37

$$\left\{y(x) = \mathrm{e}^{-ax}\_C1 + \frac{b(\sin(cx)\,a - c\cos(cx))}{a^2 + c^2}\right\}$$

Hand solution

$$\frac{dy}{dx} + ay(x) = b\sin(cx) \tag{1}$$

Integrating factor $\mu = e^{\int a dx} = e^{ax}$. Hence (1) becomes

$$\frac{d}{dx}(\mu y(x)) = \mu b\sin(cx)$$
$$\mu y(x) = b\int \mu\sin(cx)\,dx + C$$

Replacing μ by e^{ax}

$$y(x) = be^{-ax}\int e^{ax}\sin(cx)\,dx + Ce^{-ax} \tag{2}$$

Using $\sin(cx) = \frac{e^{icx} - e^{-icx}}{2i}$ then

$$\begin{aligned}
\int e^{ax} \sin(cx)\, dx &= \int \frac{e^{(ic+a)x} - e^{(-ic+a)x}}{2i} dx \\
&= \frac{1}{2i}\left(\frac{e^{(ic+a)x}}{ic+a} - \frac{e^{(-ic+a)x}}{-ic+a} \right) \\
&= \frac{1}{2i} e^{ax} \left(\frac{e^{icx}}{ic+a} - \frac{e^{-icx}}{-ic+a} \right) \\
&= \frac{1}{2i} e^{ax} \left(\frac{e^{icx}(-ic+a) - e^{-icx}(ic+a)}{(ic+a)(-ic+a)} \right) \\
&= \frac{1}{2i} e^{ax} \left(\frac{-ice^{icx} + ae^{icx} - ice^{-icx} - ae^{-icx}}{(c^2+a^2)} \right) \\
&= \frac{1}{2i} e^{ax} \left(\frac{-ic\left(e^{icx} + e^{-icx}\right) + a\left(e^{icx} - e^{-icx}\right)}{(c^2+a^2)} \right) \\
&= \frac{e^{ax}}{(c^2+a^2)} \left(\frac{-ic\left(e^{icx} + e^{-icx}\right)}{2i} + \frac{a\left(e^{icx} - e^{-icx}\right)}{2i} \right) \\
&= \frac{e^{ax}}{(c^2+a^2)} (-c\cos cx + a \sin cx)
\end{aligned}$$

Therefore (2) becomes

$$\begin{aligned}
y(x) &= be^{-ax}\left[\frac{e^{ax}}{(c^2+a^2)} (-c\cos cx + a\sin cx) \right] + Ce^{-ax} \\
&= \frac{b}{(c^2+a^2)} (-c\cos cx + a\sin cx) + Ce^{-ax}
\end{aligned}$$

2.4 ODE No. 4

$$-e^{-x^2}x + y'(x) + 2xy(x) = 0$$

✓ **Mathematica** : cpu = 0.00943147 (sec), leaf count = 30

$$\left\{\left\{y(x) \to c_1 e^{-x^2} + \frac{1}{2}e^{-x^2}x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.005 (sec), leaf count = 18

$$\left\{y(x) = \left(\frac{x^2}{2} + \_C1\right)\mathrm{e}^{-x^2}\right\}$$

Hand solution

$$\frac{dy}{dx} + 2xy(x) = e^{-x^2}x \tag{1}$$

Integrating factor $\mu = e^{\int 2x dx} = e^{x^2}$. Hence (1) becomes

$$\frac{d}{dx}\left(e^{x^2}y(x)\right) = e^{x^2}e^{-x^2}x$$
$$\frac{d}{dx}\left(e^{x^2}y(x)\right) = x$$

Integrating both sides

$$e^{x^2}y(x) = \frac{x^2}{2} + C$$
$$y(x) = e^{-x^2}\left(\frac{x^2}{2} + C\right)$$

2.5 ODE No. 5

$$y'(x) + y(x)\cos(x) - e^{2x} = 0$$

✓ **Mathematica** : cpu = 2.38995 (sec), leaf count = 38

$$\left\{\left\{y(x) \to e^{-\sin(x)} \int_1^x e^{2K[1]+\sin(K[1])}\, dK[1] + c_1 e^{-\sin(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.087 (sec), leaf count = 21

$$\left\{y(x) = \mathrm{e}^{-\sin(x)}\left(\int \mathrm{e}^{2x+\sin(x)}\,\mathrm{d}x + \_C1\right)\right\}$$

Hand solution

$$\frac{dy}{dx} + y(x)\cos(x) = e^{2x} \tag{1}$$

Integrating factor $\mu = e^{\int \cos(x)dx} = e^{\sin(x)}$. Hence (1) becomes

$$\frac{d}{dx}\left(e^{\sin(x)}y(x)\right) = e^{\sin(x)}e^{2x}$$

Integrating both sides

$$\begin{aligned} e^{\sin(x)}y(x) &= \int e^{\sin(x)}e^{2x} + C \\ y(x) &= e^{-\sin(x)}\int e^{2x+\sin(x)} + Ce^{-\sin(x)} \end{aligned}$$

2.6 ODE No. 6

$$y'(x) + y(x)\cos(x) - \frac{1}{2}\sin(2x) = 0$$

✓ **Mathematica** : cpu = 0.0228838 (sec), leaf count = 18

$$\left\{\left\{y(x) \to c_1 e^{-\sin(x)} + \sin(x) - 1\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 15

$$\left\{y(x) = \sin(x) - 1 + \mathrm{e}^{-\sin(x)}\_C1\right\}$$

Hand solution

$$\frac{dy}{dx} + y(x)\cos(x) = \frac{1}{2}\sin(2x) \tag{1}$$

Integrating factor $\mu = e^{\int \cos dx} = e^{\sin(x)}$. Therefore (1) becomes2

$$\frac{d}{dx}\left(e^{\sin(x)} y(x)\right) = \frac{1}{2} e^{\sin(x)} \sin(2x)$$

Integrating

$$\begin{aligned} e^{\sin(x)} y(x) &= \frac{1}{2}\int e^{\sin(x)} \sin(2x) + C \\ y(x) &= \frac{e^{-\sin(x)}}{2}\int e^{\sin(x)} \sin(2x) + e^{-\sin(x)} C \end{aligned}$$

But $e^{\sin(x)} \sin(2x)$ can be integrated by parts which gives $e^{\sin(x)}(-2 + 2\sin(x))$. Hence the above becomes

$$\begin{aligned} y(x) &= \frac{e^{-\sin(x)}}{2}\left(e^{\sin(x)}(-2 + 2\sin(x))\right) + e^{-\sin(x)} C \\ &= -1 + \sin(x) + e^{-\sin(x)} C \end{aligned}$$

2.7 ODE No. 7

$$y'(x) + y(x)\cos(x) - e^{-\sin(x)} = 0$$

✓ **Mathematica** : cpu = 0.0232352 (sec), leaf count = 23

$$\left\{\left\{y(x) \to c_1 e^{-\sin(x)} + x e^{-\sin(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.006 (sec), leaf count = 13

$$\left\{y(x) = (x + \_C1)\,\mathrm{e}^{-\sin(x)}\right\}$$

Hand solution

$$\frac{dy}{dx} + y(x)\cos(x) = e^{-\sin(x)} \tag{1}$$

Integrating factor $\mu = e^{\int \cos dx} = e^{\sin x}$. Hence (1) becomes

$$\frac{d}{dx}(\mu y(x)) = \mu e^{-\sin(x)}$$

Replacing μ by $e^{\sin x}$ and integrating both sides

$$\begin{aligned} e^{\sin x} y(x) &= \int e^{\sin x} e^{-\sin(x)} dx + C \\ e^{\sin x} y(x) &= \int dx + C \\ e^{\sin x} y(x) &= x + C \\ y(x) &= x e^{-\sin x} + C e^{-\sin(x)} \end{aligned}$$

2.8 ODE No. 8

$$y'(x) + y(x)\tan(x) - \sin(2x) = 0$$

✓ **Mathematica** : cpu = 0.0257531 (sec), leaf count = 17

$$\{\{y(x) \to c_1 \cos(x) - 2\cos^2(x)\}\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 13

$$\{y(x) = \cos(x)(-2\cos(x) + \_C1)\}$$

Hand solution

$$\frac{dy}{dx} + y(x)\tan(x) = \sin(2x) \tag{1}$$

Integrating factor $\mu = e^{\int \tan dx} = e^{-\ln(\cos(x))} = \frac{1}{\cos(x)}$. Hence (1) becomes

$$\frac{d}{dx}\left(y(x)\frac{1}{\cos(x)}\right) = \frac{1}{\cos(x)}\sin(2x)$$

Integrating both sides

$$\begin{aligned} y(x)\frac{1}{\cos(x)} &= \int \frac{1}{\cos(x)}\sin(2x)\,dx + C \\ y(x) &= \cos(x)\int \frac{\sin(2x)}{\cos(x)}dx + C\cos(x) \end{aligned}$$

But $\sin(2x) = 2\sin(x)\cos(x)$ hence

$$\begin{aligned} y(x) &= \cos(x)\int \frac{2\sin(x)\cos(x)}{\cos(x)}dx + C\cos(x) \\ &= 2\cos(x)\int \sin(x)\,dx + C\cos(x) \\ &= -2\cos^2(x) + C\cos(x) \end{aligned}$$

2.9 ODE No. 9

$$y'(x) - y(x)(a + \sin(\log(x)) + \cos(\log(x))) = 0$$

✓ **Mathematica** : cpu = 0.0183929 (sec), leaf count = 19

$$\left\{\left\{y(x) \to c_1 e^{ax + x\sin(\log(x))}\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 14

$$\left\{y(x) = \_C1\, \mathrm{e}^{x(\sin(\ln(x)) + a)}\right\}$$

Hand solution

$$\frac{dy}{dx} - y(x)\left[a + \sin\left(\log\left(x\right)\right) + \cos\left(\log\left(x\right)\right)\right] = 0 \tag{1}$$

Integrating factor $\mu = e^{-\int a - \sin(\log(x)) - \cos(\log(x))dx} = e^{-ax} e^{-\int \sin(\log(x)) + \cos(\log(x))dx}$. To integrate $\int \sin\left(\log\left(x\right)\right) + \cos\left(\log\left(x\right)\right) dx$, let $r = \log\left(x\right)$, $\frac{dr}{dx} = \frac{1}{x}$, then $dx = xdr$, But $x = e^r$, hence the integral becomes

$$\begin{aligned}\int \sin\left(\log\left(x\right)\right) + \cos\left(\log\left(x\right)\right) dx &= \int \left[\sin\left(r\right) + \cos\left(r\right)\right] e^r dr \\ &= \int e^r \sin\left(r\right) dr + \int e^r \cos\left(r\right) dr \end{aligned} \tag{2}$$

Integrating by parts $\int e^r \cos\left(r\right) dr$, $\int udv = uv - \int vdu$, Let $u = e^r \to du = e^r$ and $dv = \cos\left(r\right) \to v = \sin\left(r\right)$, hence (2) becomes

$$\begin{aligned}\int e^r \sin\left(r\right) dr + \int e^r \cos\left(r\right) dr &= \int e^r \sin\left(r\right) dr + e^r \sin\left(r\right) - \int \sin\left(r\right) e^r dr \\ &= e^r \sin\left(r\right)\end{aligned}$$

Therefore, substituting back $r = \log\left(x\right)$ gives

$$\begin{aligned}\int \sin\left(\log\left(x\right)\right) + \cos\left(\log\left(x\right)\right) dx &= e^{\log(x)} \sin\left(\log\left(x\right)\right) \\ &= x \sin\left(\log\left(x\right)\right)\end{aligned}$$

Hence the integration factor is

$$\begin{aligned}\mu &= e^{-ax} e^{-\int \sin(\log(x))+\cos(\log(x))dx} \\ &= e^{-ax} e^{-x\sin(\log(x))}\end{aligned}$$

Therefore (1) becomes

$$\frac{d}{dx}(\mu y(x)) = 0$$

Integrating

$$\begin{aligned}y(x)\, e^{-ax} e^{-x\sin(\log(x))} &= C \\ y(x) &= C e^{ax} e^{x\sin(\log(x))} \\ &= C e^{ax + x\sin(\log(x))} \\ &= C e^{x(a+\sin(\log(x)))}\end{aligned}$$

2.10 ODE No. 10

$$y(x)f'(x) - f(x)f'(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.00885774 (sec), leaf count = 18

$$\left\{\left\{y(x) \to c_1 e^{-f(x)} + f(x) - 1\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 15

$$\left\{y(x) = f(x) - 1 + \mathrm{e}^{-f(x)} \_C1\right\}$$

Hand solution

$$\frac{dy}{dx} + y(x)\frac{df}{dx} = f(x)\frac{df}{dx} \tag{1}$$

Integrating factor $\mu = e^{\int \frac{df}{dx} dx} = e^f$. Therefore (1) becomes

$$\frac{d}{dx}\left(e^f y(x)\right) = e^f f(x)\frac{df}{dx}$$

Integrating

$$e^f y(x) = \int e^f f(x)\frac{df}{dx}dx + C$$
$$y(x) = e^{-f}\int e^f f df + e^{-f}C$$

But $\int e^f f df$ is the same as $\int e^x x dx$ which by integration by parts gives $e^x(x-1)$ or in terms of f, gives $e^f(f-1)$. Hence the above becomes

$$y(x) = e^{-f}\left(e^f(f-1)\right) + e^{-f}C$$
$$= f - 1 + e^{-f}C$$

2.11 ODE No. 11

$$f(x)y(x) - g(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.457402 (sec), leaf count = 62

$$\left\{\left\{y(x) \to c_1 e^{\int_1^x -f(K[1])\,dK[1]} + e^{\int_1^x -f(K[1])\,dK[1]} \int_1^x g(K[2]) e^{-\int_1^{K[2]} -f(K[1])\,dK[1]}\,dK[2]\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 24

$$\left\{y(x) = \left(\int g(x)\,\mathrm{e}^{\int f(x)\,\mathrm{d}x}\,\mathrm{d}x + \_C1\right)\mathrm{e}^{\int -f(x)\,\mathrm{d}x}\right\}$$

Hand solution

$$\frac{dy}{dx} + y(x)\,f(x) = g(x) \tag{1}$$

Integrating factor $\mu = e^{\int f(x)dx}$. Therefore (1) becomes

$$\frac{d}{dx}\left(e^{\int f(x)dx} y(x)\right) = e^{\int f(x)dx} g(x)$$

Integrating

$$\begin{aligned} e^{\int f(x)dx} y(x) &= \int e^{\int f(x)dx} g(x)\,dx + C \\ y(x) &= e^{-\int f(x)dx} \int e^{\int f(x)dx} g(x)\,dx + e^{-\int f(x)dx} C \\ &= \left(\int e^{\int f(x)dx} g(x)\,dx + C\right) e^{-\int f(x)dx} \end{aligned}$$

2.12 ODE No. 12

$$y'(x) + y(x)^2 - 1 = 0$$

✓ **Mathematica** : cpu = 0.0286653 (sec), leaf count = 34

$$\left\{\left\{y(x) \to \frac{e^{2x} - e^{2c_1}}{e^{2c_1} + e^{2x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 8

$$\{y(x) = \tanh(x + \_C1)\}$$

Hand solution

$$\frac{dy}{dx} + y^2(x) - 1 = 0$$

$$\frac{dy}{dx} = 1 - y^2(x) \tag{1}$$

This is separable. Hence

$$\frac{dy}{dx}\frac{1}{1 - y^2(x)} = 1$$

$$\frac{dy}{1 - y^2(x)} = dx$$

Integrating

$$\int \frac{dy}{1 - y^2(x)} = x + C$$

Using $\int \frac{1}{a+by^2} dy = \frac{\sqrt{-\frac{a}{b}} \tanh^{-1}\left(\frac{y}{\sqrt{\frac{-a}{b}}}\right)}{a}$ and since $a = 1, b = -1$, then $\int \frac{dy}{1-y^2(x)} = \tanh^{-1}(y)$ and the above becomes

$$\tanh^{-1}(y) = x + C$$

Therefore

$$y = \tanh(x + C) \tag{2}$$

In terms of exponential, since $\tanh(u) = \frac{e^u - e^{-u}}{e^u + e^{-u}}$ then (2) can also be written as

$$y = \frac{e^{x+C} - e^{-(x+C)}}{e^{x+C} + e^{-(x+C)}} = \frac{e^x e^C - e^{-x} e^{-C}}{e^x e^C + e^{-x} e^{-C}}$$

Multiplying numerator and denominator by $e^{-C} e^x$

$$y = \frac{e^{2x} - e^{-2C}}{e^{2x} + e^{-2C}}$$

To get same answer as Mathematica, since C is constant, let $C_1 = -C$, then

$$y = \frac{e^{2x} - e^{2C_1}}{e^{2x} + e^{2C_1}}$$

2.13 ODE No. 13

$$-ax - b + y'(x) + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0240694 (sec), leaf count = 79

$$\left\{\left\{y(x) \to -\frac{\sqrt[3]{a}c_1 \text{Ai}'\left(\frac{b+ax}{a^{2/3}}\right) + \sqrt[3]{a}\text{Bi}'\left(\frac{b+ax}{a^{2/3}}\right)}{-c_1 \text{Ai}\left(\frac{b+ax}{a^{2/3}}\right) - \text{Bi}\left(\frac{b+ax}{a^{2/3}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.22 (sec), leaf count = 79

$$\left\{y(x) = -i\sqrt[3]{-ia}\left(\text{Ai}^{(1)}\left(-(ax+b)(-ia)^{-\frac{2}{3}}\right)\_C1 + \text{Bi}^{(1)}\left(-(ax+b)(-ia)^{-\frac{2}{3}}\right)\right)\left(\text{Ai}\left(-(ax+b)(-ia)^{-\frac{2}{3}}\right)\_C1\right.\right.$$

Hand solution

$$\begin{aligned} y'(x) + y^2(x) - ax - b &= 0 \\ y'(x) &= b + ax - y^2(x) \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE of the form

$$y'(x) = P(x) + Q(x)\, y + R(x)\, y^2(x) \tag{2}$$

where in this case $Q(x) = 0, R(x) = -1, P(x) = b + ax$. We can solve this in two ways. If we know one particular solution $y_p(x)$ for (1) then we use the substitution $y = y_p + \frac{1}{u}$ and convert (1) to new associated linear ODE of the form $u' + (Q(x) + 2R(x))\, y_p + R(x) = 0$. If we do not know a particular solution, then we use the standard substitution $y = \frac{-u'}{uR(x)} = \frac{u'}{u}$ since $R(x) = -1$ and this is what we will do here.

Since $u' = yu$ then

$$\begin{aligned} u'' &= yu' + y'u \\ &= y(yu) + \left(b + ax - y^2\right) u \\ &= y^2 u + (b + ax)\, u - y^2 u \\ &= (b + ax)\, u \end{aligned}$$

So we have new second order ODE

$$u'' - (b + ax)\, u = 0 \tag{3}$$

which we solve for u. This ODE is of the form $u'' - q(x)\, u = 0$ which has solutions in terms of Airy function of first $Ai(x)$ and second kind $Bi(x)$, where

$$Ai(x) = \frac{1}{\pi}\int_0^\infty \cos\left(\frac{t^3}{3} + xt\right) dt$$
$$Bi(x) = \frac{1}{\pi}\int_0^\infty \exp\left(-\frac{t^3}{3} + xt\right) + \sin\left(\frac{t^3}{3} + xt\right) dt$$

Therefore the solution to (3) is

$$u(x) = c_1 Ai\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) + c_2 Bi\left(\frac{b+ax}{a^{\frac{2}{3}}}\right)$$

We need to find $u'(x)$ now. Using $Ai'(x), Bi'(x)$ for derivative of Airy functions of first and second kind, then

$$u'(x) = c_1 Ai'\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) a^{\frac{1}{3}} + c_2 Bi'\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) a^{\frac{1}{3}}$$

Therefore since $u' = yu$ then

$$\begin{aligned} y &= \frac{u'}{u} \\ &= \frac{c_1 A'i\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) a^{\frac{1}{3}} + c_2 Bi'\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) a^{\frac{1}{3}}}{c_1 Ai\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) + c_2 Bi\left(\frac{b+ax}{a^{\frac{2}{3}}}\right)} \end{aligned}$$

Let $C_1 = \frac{c_1}{c_2}$ then the above can be written as

$$y = \frac{C_1 A'i\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) a^{\frac{1}{3}} + Bi'\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) a^{\frac{1}{3}}}{C_1 Ai\left(\frac{b+ax}{a^{\frac{2}{3}}}\right) + Bi\left(\frac{b+ax}{a^{\frac{2}{3}}}\right)}$$

Reference: Airy function

2.14 ODE No. 14

$$ax^m + y'(x) + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0129126 (sec), leaf count = 254

$$\left\{\left\{y(x) \to -\frac{i\sqrt{-a}x^{\frac{m+2}{2}}\left(c_1 J_{\frac{m+1}{m+2}}\left(\frac{2i\sqrt{-a}x^{\frac{m}{2}+1}}{m+2}\right) - c_1 J_{-\frac{m+3}{m+2}}\left(\frac{2i\sqrt{-a}x^{\frac{m+2}{2}}}{m+2}\right) - 2J_{\frac{1}{m+2}-1}\left(\frac{2i\sqrt{-a}x^{\frac{m+2}{2}}}{m+2}\right)\right) - c_1 J_{-\frac{1}{m+2}}\left(\frac{2i\sqrt{-a}x^{\frac{m+2}{2}}}{m+2}\right) - J_{\frac{1}{m+2}}\left(\frac{2i\sqrt{-a}x^{\frac{m+2}{2}}}{m+2}\right)\right)}{2x\left(c_1 J_{-\frac{1}{m+2}}\left(\frac{2i\sqrt{-a}x^{\frac{m+2}{2}}}{m+2}\right) + J_{\frac{1}{m+2}}\left(\frac{2i\sqrt{-a}x^{\frac{m+2}{2}}}{m+2}\right)\right)}\right.\right.$$

✓ **Maple** : cpu = 0.109 (sec), leaf count = 187

$$\left\{y(x) = \frac{1}{x}\left(-J_{\frac{3+m}{m+2}}\left(2\,\frac{\sqrt{a}x^{m/2+1}}{m+2}\right)\sqrt{a}x^{\frac{m}{2}+1}\_C1 - Y_{\frac{3+m}{m+2}}\left(2\,\frac{\sqrt{a}x^{m/2+1}}{m+2}\right)\sqrt{a}x^{\frac{m}{2}+1} + \_C1\, J_{(m+2)^{-1}}\left(2\,\frac{\sqrt{a}x^{m/2}\right.\right.\right.$$

Hand solution

$$\begin{aligned} y'(x) + y^2(x) + ax^m &= 0 \\ y'(x) &= -ax^m - y^2(x) \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE of the form

$$y'(x) = P(x) + Q(x)\,y + R(x)\,y^2(x) \tag{2}$$

where in this case $Q(x) = 0, R(x) = -1, P(x) = -ax^m$. We can solve this in two ways. If we know one particular solution $y_p(x)$ for (1) then we use the substitution $y = y_p + \frac{1}{u}$ and convert (1) to new associated linear ODE of the form $u' + (Q(x) + 2R(x))\,y_p + R(x) = 0$. If we do not know a particular solution, then we use the standard substitution $y = \frac{-u'}{uR(x)} = \frac{u'}{u}$ since $R(x) = -1$ and this is what we will do here.

Since $u' = yu$ then

$$\begin{aligned} u'' &= yu' + y'u \\ &= y(yu) + \left(-ax^m - y^2\right)u \\ &= y^2u - ax^m u - y^2 u \\ &= -ax^m u \end{aligned}$$

So we have new second order ODE

$$u'' + ax^m u = 0 \tag{3}$$

which we solve for u. This is Airy ODE but with a positive sign. Of the form $u''+q(x)\,u=0$.

Recall that the solution to $u''-axu=0$ is

$$u=c_1 Ai\left(a^{\frac{1}{3}}x\right)+c_2 Bi\left(a^{\frac{1}{3}}x\right)$$

When x has power on it (there are restriction on what values the power can take), the solution is written in terms of Bessel functions. The solution to $u''-ax^m u=0$ is

$$u=c_1\sqrt{x}BesselI\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)+c_2\sqrt{x}BesselK\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)$$

When the sign is positive, the solution to $u''+ax^m u=0$ is

$$u(x)=c_1\sqrt{x}BesselJ\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)+c_2\sqrt{x}BesselY\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\tag{4}$$

We need to find $u'(x)$ now. From (4)

$$\frac{d}{dx}\left[c_1\sqrt{x}BesselJ\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right]=c_1\frac{BesselJ\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)-\sqrt{a}x^{\frac{m+1}{2}}BesselJ\left(\frac{m+3}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{\sqrt{x}}$$

And

$$\frac{d}{dx}\left[c_2\sqrt{x}BesselY\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right]=c_2\frac{BesselY\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)-\sqrt{a}x^{\frac{m+1}{2}}BesselY\left(\frac{m+3}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{\sqrt{x}}$$

Therefore

$$\begin{aligned}u'(x)=c_1&\frac{BesselJ\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)-\sqrt{a}x^{\frac{m+1}{2}}BesselJ\left(\frac{m+3}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{\sqrt{x}}\\+c_2&\frac{BesselY\left(\frac{1}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)-\sqrt{a}x^{\frac{m+1}{2}}BesselY\left(\frac{m+3}{m+2},\frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{\sqrt{x}}\end{aligned}$$

Since $u'=yu$ then

$$
\begin{aligned}
y &= \frac{u'}{u} \\
&= \frac{c_1 \frac{BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselJ\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{\sqrt{x}} + c_2 \frac{BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselY\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{\sqrt{x}}}{c_1\sqrt{x}BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) + c_2\sqrt{x}BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)} \\
&= \frac{c_1\left[BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselJ\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right] + c_2\left[BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselY\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right]}{\sqrt{x}\left[c_1\sqrt{x}BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) + c_2\sqrt{x}BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right]} \\
&= \frac{c_1\left[BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselJ\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right] + c_2\left[BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselY\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right]}{c_1 xBesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) + c_2 xBesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}
\end{aligned}
$$

Let $C_1 = \frac{c_1}{c_2}$ then the above can be written as

$$
y = \frac{1}{x} \frac{C_1\left[BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselJ\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)\right] + BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) - \sqrt{a}x^{\frac{m+1}{2}} BesselY\left(\frac{m+3}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}{C_1 BesselJ\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right) + BesselY\left(\frac{1}{m+2}, \frac{2\sqrt{a}x^{\frac{m+1}{2}}}{m+2}\right)}
$$

2.15 ODE No. 15

$$x^4 - 2x^2 y(x) + y'(x) + y(x)^2 - 2x - 1 = 0$$

✓ **Mathematica** : cpu = 0.0200216 (sec), leaf count = 25

$$\left\{\left\{y(x) \to \frac{1}{c_1 \left(-e^{2x}\right) - \frac{1}{2}} + x^2 + 1\right\}\right\}$$

✓ **Maple** : cpu = 0.29 (sec), leaf count = 35

$$\left\{y(x) = \frac{x^2 (\mathrm{e}^x)^2 - x^2 \_C1 + (\mathrm{e}^x)^2 + \_C1}{(\mathrm{e}^x)^2 - \_C1}\right\}$$

Hand solution

$$x^4 - 2x^2 y(x) + y'(x) + y^2(x) - 2x - 1 = 0$$

$$y'(x) = -x^4 + 2x + 1 + 2x^2 y(x) - y^2(x) \tag{1}$$

This is Riccati first order non-linear ODE of the form

$$y'(x) = P(x) + Q(x)\, y + R(x)\, y^2(x) \tag{2}$$

where in this case $Q(x) = 2x^2, R(x) = -1, P(x) = -x^4 + 2x + 1$.

Let $u = y - x^2$ or $y = u + x^2$ then

$$\begin{aligned} u' &= y' - 2x \\ &= \left(-x^4 + 2x + 1 + 2x^2 y - y^2\right) - 2x \\ &= \left(-x^4 + 2x + 1 + 2x^2 \left(u + x^2\right) - \left(u + x^2\right)^2\right) - 2x \\ &= \left(-x^4 + 2x + 1 + 2x^2 u + 2x^4 - \left(u^2 + x^4 + 2u x^2\right)\right) - 2x \\ &= -x^4 + 2x + 1 + 2x^2 u + 2x^4 - u^2 - x^4 - 2u x^2 - 2x \\ &= 1 - u^2 \end{aligned}$$

Hence

$$u' = 1 - u^2$$

This is separable

$$\frac{du}{dx} = 1 - u^2$$

$$\frac{du}{1 - u^2} = dx$$

Integrating both sides

$$\begin{aligned}\tanh^{-1}(u) &= x + C \\ u(x) &= \tanh(x + C) \\ &= \frac{e^{x+C} - e^{-x-C}}{e^{x+C} + e^{-x-C}} \\ &= \frac{e^x e^C - e^{-x} e^{-C}}{e^x e^C + e^{-x} e^{-C}}\end{aligned}$$

Multiplying numerator and denominator by $e^{-C} e^x$

$$u(x) = \frac{e^{2x} - e^{-2C}}{e^{2x} + e^{-2C}}$$

Let $e^{-2C} = C_1$

$$u(x) = \frac{e^{2x} - C_1}{e^{2x} + C_1}$$

Since $u = y - x^2$ then

$$\begin{aligned}y &= u + x^2 \\ &= \frac{e^{2x} - C_1}{e^{2x} + C_1} + x^2 \\ &= \frac{e^{2x} - C_1 + x^2 e^{2x} + x^2 C_1}{e^{2x} + C_1}\end{aligned}$$

To obtain same solution as Maple, we divide by C_1

$$y = \frac{\frac{1}{C_1} e^{2x} - 1 + \frac{1}{C_1} x^2 e^{2x} + x^2}{\frac{1}{C_1} e^{2x} + 1}$$

Let $\frac{1}{C_1} = -C$ then

$$\begin{aligned}y &= \frac{-Ce^{2x} - 1 - Cx^2 e^{2x} + x^2}{-Ce^{2x} + 1} \\ &= \frac{Ce^{2x} + 1 + Cx^2 e^{2x} - x^2}{Ce^{2x} - 1}\end{aligned}$$

Which now agrees with the Maple solution form. Mathematica solution also verified to be correct.

2.16 ODE No. 16

$$f(x)(xy(x)-1)+y'(x)+y(x)^2=0$$

✗ **Mathematica** : cpu = 20.7792 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]^2 + f[x]*(-1 + x*y[x]) + Derivative[1][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.146 (sec), leaf count = 49

$$\left\{y(x)=1\mathrm{e}^{\int \frac{-x^2 f(x)-2}{x}\,\mathrm{d}x}\left(-\_C1+\int \mathrm{e}^{\int \frac{-x^2 f(x)-2}{x}\,\mathrm{d}x}\,\mathrm{d}x\right)^{-1}+x^{-1}\right\}$$

Hand solution

$$y'+y^2+(xy-1)f=0$$
$$y'(x)=(-xy+1)f-y^2 \tag{1}$$

This is Riccati first order non-linear ODE of the form. We can see a particular solution is $y_p=\frac{1}{x}$, therefore, we use the substitution

$$\begin{aligned} y(x) &= y_p(x)+\frac{1}{u(x)} \\ &= \frac{1}{x}+\frac{1}{u} \end{aligned}$$

Hence

$$\begin{aligned} y'(x) &= y_p'(x)-\frac{u'(x)}{u^2(x)} \\ &= \frac{-1}{x^2}-\frac{u'(x)}{u^2(x)} \end{aligned} \tag{2}$$

Equating (1) and (2) gives

$$\begin{aligned} (-xy+1)f-y^2 &= \frac{-1}{x^2}-\frac{u'}{u^2} \\ \left(-x\left(\frac{1}{x}+\frac{1}{u}\right)+1\right)f-\left(\frac{1}{x}+\frac{1}{u}\right)^2 &= \frac{-1}{x^2}-\frac{u'}{u^2} \\ \left(\left(-1-\frac{x}{u}\right)+1\right)f-\left(\frac{1}{x^2}+\frac{1}{u^2}+\frac{2}{xu}\right) &= \frac{-1}{x^2}-\frac{u'}{u^2} \\ -\frac{x}{u}f-\left(\frac{1}{x^2}+\frac{1}{u^2}+\frac{2}{xu}\right) &= \frac{-1}{x^2}-\frac{u'}{u^2} \\ -\frac{x}{u}f-\frac{1}{x^2}-\frac{1}{u^2}-\frac{2}{xu} &= \frac{-1}{x^2}-\frac{u'}{u^2} \\ -xuf-1-\frac{2u}{x} &= -u' \\ u' &= xuf+1+\frac{2u}{x} \end{aligned}$$

Hence

$$u' - \left(xf + \frac{2}{x} \right) u = 1$$

Integrating factor is $\mu = e^{\int (xf + \frac{2}{x}) dx}$, hence the solution is

$$d(\mu u) = \mu$$

Integrating both sides

$$\begin{aligned}
\mu u &= \int \mu dx + C \\
u &= e^{-\int (xf + \frac{2}{x}) dx} \int e^{\int (xf + \frac{2}{x}) dx} dx + C e^{-\int (xf + \frac{2}{x}) dx} \\
&= e^{-\int (xf + \frac{2}{x}) dx} \left(\int e^{\int (xf + \frac{2}{x}) dx} dx + C \right)
\end{aligned}$$

Hence

$$\begin{aligned}
y &= y_p + \frac{1}{u} \\
&= \frac{1}{x} + \frac{1}{e^{-\int (xf + \frac{2}{x}) dx} \left(\int e^{\int (xf + \frac{2}{x}) dx} dx + C \right)}
\end{aligned}$$

Hence

$$y(x) = \frac{1}{x} + e^{\int (xf + \frac{2}{x}) dx} \left(\int e^{\int (xf + \frac{2}{x}) dx} dx + C \right)^{-1}$$

2.17 ODE No. 17

$$y'(x) - y(x)^2 - 3y(x) + 4 = 0$$

✓ **Mathematica** : cpu = 0.0242934 (sec), leaf count = 34

$$\left\{\left\{y(x) \to \frac{-4e^{5c_1+5x} - 1}{e^{5c_1+5x} - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.109 (sec), leaf count = 24

$$\left\{y(x) = \frac{-4\,\mathrm{e}^{5x}\_C1 - 1}{-1 + \mathrm{e}^{5x}\_C1}\right\}$$

Hand solution

$$\begin{aligned} y' - y^2 - 3y + 4 &= 0 \\ y' &= 3y - 4 + y^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE of the form. The general form is

$$y' = P(x) + Q(x)\,y + R(x)\,y^2$$

Where $P(x) = -4, Q(x) = 3, R(x) = 1$. Using the substitution $y = -\frac{u'}{uR(x)} = \frac{-u'}{u}$ then

$$\begin{aligned} u' &= -yu \\ u'' &= -yu' - y'u \\ &= -y(-yu) - \left(3y - 4 + y^2\right) u \\ &= y^2 u - 3\left(-\frac{u'}{u}\right) u + 4u - y^2 u \\ &= 3u' + 4u \end{aligned}$$

Hence

$$u'' - 3u' - 4u = 0$$

This is standard second order ODE. The characteristic equation is $\lambda^2 - 3\lambda - 4 = 0$, with roots $\frac{-b \pm \sqrt{b^2-4ac}}{2a} = \frac{3 \pm \sqrt{9+16}}{2} = \frac{3 \pm 5}{2} = \{4, -1\}$, hence

$$u(x) = c_1 e^{4x} + c_2 e^{-x}$$

And

$$u'(x) = c_1 4e^{4x} - c_2 e^{-x}$$

Since $y = \frac{-u'}{u}$ then

$$\begin{aligned} y(x) &= \frac{-c_1 4e^{4x} + c_2 e^{-x}}{c_1 e^{4x} + c_2 e^{-x}} \\ &= \frac{-\frac{c_1}{c_2} 4e^{4x} + e^{-x}}{\frac{c_1}{c_2} e^{4x} + e^{-x}} \end{aligned}$$

Let $\frac{c_1}{c_2} = C_1$ then

$$y(x) = \frac{-4C_1 e^{4x} + e^{-x}}{C_1 e^{4x} + e^{-x}}$$

Dividing by e^{-x}

$$y(x) = \frac{-4C_1 e^{5x} + 1}{C_1 e^{5x} + 1}$$

This is the same result given by CAS. To see it better, let $C_2 = -C_1$ then the above becomes

$$\begin{aligned} y(x) &= \frac{4C_2 e^{5x} + 1}{-C_2 e^{5x} + 1} \\ &= -\frac{4C_2 e^{5x} + 1}{C_2 e^{5x} - 1} \end{aligned}$$

2.18 ODE No. 18

$$y'(x) - y(x)^2 - xy(x) - x + 1 = 0$$

✓ **Mathematica** : cpu = 0.0222304 (sec), leaf count = 50

$$\left\{\left\{y(x) \to \frac{e^{\frac{x^2}{2}-2x}}{c_1 - \frac{\sqrt{\frac{\pi}{2}}\text{erfi}\left(\frac{x-2}{\sqrt{2}}\right)}{e^2}} - 1\right\}\right\}$$

✓ **Maple** : cpu = 0.07 (sec), leaf count = 39

$$\left\{y(x) = -1 + \frac{1}{\_C1 + \frac{i}{2}\sqrt{\pi}\mathrm{e}^{-2}\sqrt{2}Erf\left(\frac{i}{2}\sqrt{2}\,(x-2)\right)}\mathrm{e}^{\frac{x(x-4)}{2}}\right\}$$

Hand solution

$$y' - y^2 - xy - x + 1 = 0$$

$$y' = x - 1 + xy + y^2 \tag{1}$$

This is Riccati first order non-linear ODE of the form. The general form is

$$y' = P(x) + Q(x)\,y + R(x)\,y^2$$

Where $P(x) = x - 1, Q(x) = x, R(x) = 1$. We see that $y_p = -1$ is a particular solution, therefore we use the substitution $y = y_p + \frac{1}{u}$, hence $y' = -\frac{u'}{u^2}$ and equating this to (1) we obtain

$$\begin{aligned}
-\frac{u'}{u^2} &= x - 1 + xy + y^2 \\
&= x - 1 + x\left(-1 + \frac{1}{u}\right) + \left(-1 + \frac{1}{u}\right)^2 \\
&= x - 1 - x + \frac{x}{u} + \left(1 + \frac{1}{u^2} - \frac{2}{u}\right) \\
&= \frac{x}{u} + \frac{1}{u^2} - \frac{2}{u}
\end{aligned}$$

Hence

$$\begin{aligned}
u' &= -u^2\left(\frac{x}{u} + \frac{1}{u^2} - \frac{2}{u}\right) \\
&= -xu - 1 + 2u \\
u' + xu - 2u &= -1 \\
u' + u(x-2) &= -1
\end{aligned}$$

Integration factor is $e^{\int (x-2)dx} = e^{\frac{x^2}{2}-2x} = e^{\frac{1}{2}x(x-4)}$, therefore

$$d\left(e^{\frac{1}{2}x(x-4)}u\right) = -e^{\frac{1}{2}x(x-4)}$$

Integrating both sides

$$e^{\frac{1}{2}x(x-4)}u = -\int e^{\frac{1}{2}x(x-4)} + C$$

But

$$\int e^{\frac{1}{2}x(x-4)} = \frac{1}{e^2}\sqrt{\frac{\pi}{2}}\operatorname{erfi}\left(\frac{x-2}{\sqrt{2}}\right)$$

Hence

$$u(x) = e^{\frac{-1}{2}x(x-4)}\left(\frac{-1}{e^2}\sqrt{\frac{\pi}{2}}\operatorname{erfi}\left(\frac{x-2}{\sqrt{2}}\right) + C\right)$$

Since $y = y_p + \frac{1}{u}$ then

$$y = -1 + \frac{1}{e^{\frac{-1}{2}x(x-4)}\left(\frac{-1}{e^2}\sqrt{\frac{\pi}{2}}\operatorname{erfi}\left(\frac{x-2}{\sqrt{2}}\right) + C\right)}$$

Or

$$y = \frac{e^{\frac{1}{2}x(x-4)}}{C - \frac{1}{e^2}\sqrt{\frac{\pi}{2}}\operatorname{erfi}\left(\frac{x-2}{\sqrt{2}}\right)} - 1$$

2.19 ODE No. 19

$$y'(x) - (y(x) + x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0106791 (sec), leaf count = 30

$$\left\{\left\{y(x) \to \frac{1}{c_1 e^{2ix} - \frac{i}{2}} - x - i\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 16

$$\{y(x) = -x - \tan(-x + \_C1)\}$$

Hand solution

$$\begin{aligned} y' - (y + x)^2 &= 0 \\ y' &= (y + x)^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE of the form. Let $u = y + x$, then $u' = y' + 1$ and (1) becomes

$$\begin{aligned} u' - 1 &= u^2 \\ u' &= 1 + u^2 \end{aligned}$$

This is separable

$$\begin{aligned} \frac{du}{dx}\frac{1}{1+u^2} &= 1 \\ \int \frac{du}{1+u^2} &= \int dx \\ \tan^{-1} u &= x + C \\ u &= \tan(x + C) \end{aligned}$$

Since $u = y + x$ then

$$y = \tan(x + C) - x$$

2.20 ODE No. 20

$$\left(x^2+1\right) y(x)+y'(x)-y(x)^2-2x=0$$

✓ **Mathematica** : cpu = 0.734198 (sec), leaf count = 48

$$\left\{\left\{y(x)\to \frac{e^{\frac{x^3}{3}+x}}{c_1-\int_1^x e^{\frac{K[1]^3}{3}+K[1]}\,dK[1]}+x^2+1\right\}\right\}$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 34

$$\left\{y(x)=x^2+1+1\mathrm{e}^{\frac{x^3}{3}+x}\left(\_C1-\int \mathrm{e}^{\frac{x^3}{3}+x}\,\mathrm{d}x\right)^{-1}\right\}$$

Hand solution

$$\left(x^2+1\right) y+y'-y^2-2x=0$$

$$y'=-\left(x^2+1\right) y+y^2+2x \tag{1}$$

This is Riccati first order non-linear ODE of the form of the general form $y'=P(x)+Q(x)\,y+R(x)\,y^2$ where $P(x)=2x, Q(x)=-\left(x^2+1\right), R(x)=1$. We can convert this to Bernoulli first order ODE in $u(x)$, which is little easier to solve by using $u=y-x^2-1$. The difference between Bernoulli and Riccati is that the term $P(x)=0$ in Bernoulli. If $P(x)\neq 0$ and $R(x)\neq 0$ then it is called Riccati.

Using $u=y-x^2-1$ gives

$$\begin{aligned}
u' &= y'-2x \\
u' &= \left[-\left(x^2+1\right) y+y^2+2x\right]-2x \\
&= -\left(x^2+1\right)\left(u+x^2+1\right)+\left(u+x^2+1\right)^2 \\
&= \left(u+x^2+1\right)\left[\left(u+x^2+1\right)-\left(x^2+1\right)\right] \\
&= \left(u+x^2+1\right) u \\
&= u^2+u\left(1+x^2\right)
\end{aligned}$$

We see now this is Bernoulli since $P(x)=0$. To solve Bernoulli we always start by dividing by u^2 giving

$$\frac{u'}{u^2}=1+\frac{1}{u}\left(1+x^2\right)$$

Next we let $v=\frac{1}{u}$, hence $v'=-\frac{u'}{u^2}$therefore the above becomes

$$\begin{aligned}
-v' &= 1+v\left(1+x^2\right) \\
v'+v\left(1+x^2\right) &= -1
\end{aligned}$$

Integrating factor is $e^{\int (1+x^2)dx} = e^{\left(x+\frac{x^3}{2}\right)}$, therefore

$$d\left(e^{\left(x+\frac{x^3}{2}\right)}v\right) = -e^{\left(x+\frac{x^3}{2}\right)}$$

Integrating

$$e^{\left(x+\frac{x^3}{2}\right)}v = -\int e^{\left(x+\frac{x^3}{2}\right)}dx + C$$

$$v(x) = e^{-\left(x+\frac{x^3}{2}\right)}\left(C - \int e^{\left(x+\frac{x^3}{2}\right)}dx\right)$$

Therefore

$$u = \frac{1}{v} = \frac{e^{\left(x+\frac{x^3}{2}\right)}}{\left(C - \int e^{\left(x+\frac{x^3}{2}\right)}dx\right)}$$

And since $u = y - x^2 - 1$ then

$$\begin{aligned} y(x) &= u + 1 + x^2 \\ &= \frac{e^{\left(x+\frac{x^3}{2}\right)}}{\left(C - \int e^{\left(x+\frac{x^3}{2}\right)}dx\right)} + 1 + x^2 \end{aligned}$$

2.21 ODE No. 21

$$y'(x) - y(x)^2 + y(x)\sin(x) - \cos(x) = 0$$

✓ **Mathematica** : cpu = 6.39037 (sec), leaf count = 69

$$\left\{\left\{y(x) \to -\frac{c_1\left(1 - \sin(x)e^{\cos(x)}\left(\int_1^x e^{-\cos(K[1])}\,dK[1]\right)\right) - \sin(x)e^{\cos(x)}}{c_1 e^{\cos(x)}\int_1^x e^{-\cos(K[1])}\,dK[1] + e^{\cos(x)}}\right\}\right\}$$

✓ **Maple** : cpu = 0.141 (sec), leaf count = 25

$$\left\{y(x) = -\frac{\mathrm{e}^{-\cos(x)}}{\_C1 + \int \mathrm{e}^{-\cos(x)}\,\mathrm{d}x} + \sin(x)\right\}$$

Hand solution

$$y' - y^2 + y\sin(x) - \cos(x) = 0$$

$$y' = y^2 - y\sin(x) + \cos(x) \tag{1}$$

This is Riccati first order non-linear ODE of the form of the general form $y' = P(x) + Q(x)\,y + R(x)\,y^2$ where $P(x) = \cos(x), Q(x) = -\sin(x), R(x) = 1$. It is best to first try to spot a particular solution y_p and use the transformation $y = y_p + \frac{1}{u}$ otherwise we use $y = -\frac{u'}{yR(x)}$ transformation. For this problem

$$y_p = \sin(x)$$

Therefore

$$y = \sin x + \frac{1}{u}$$
$$y' = \cos x - \frac{u'}{u^2}$$

Equating this to (1) gives

$$y^2 - y\sin(x) + \cos(x) = \cos x - \frac{u'}{u^2}$$
$$\left(\sin x + \frac{1}{u}\right)^2 - \left(\sin x + \frac{1}{u}\right)\sin x + \cos x = \cos x - \frac{u'}{u^2}$$
$$\sin^2 x + \frac{1}{u^2} + \frac{2}{u}\sin x - \sin^2 x - \frac{1}{u}\sin x = -\frac{u'}{u^2}$$
$$\frac{1}{u^2} + \frac{1}{u}\sin x = -\frac{u'}{u^2}$$
$$1 + u\sin x = -u'$$
$$u' + u\sin x = -1$$

Integrating factor is $e^{\int \sin x} = e^{-\cos x}$, hence

$$d\left(e^{-\cos x} u\right) = -e^{-\cos x}$$

Integrating both sides

$$\begin{aligned} e^{-\cos x} u &= -\int e^{-\cos x} dx + C \\ u &= e^{\cos x}\left(C - \int e^{-\cos x} dx\right) \end{aligned}$$

Since $y = \sin x + \frac{1}{u}$ then

$$y = \sin x + \frac{e^{-\cos x}}{C - \int e^{-\cos x} dx}$$

Or letting $C_1 = -C$ to make match Maple form, we obtain

$$y = -\frac{e^{-\cos x}}{C_1 + \int e^{-\cos x} dx} + \sin x$$

2.22 ODE No. 22

$$y'(x) - y(x)^2 - y(x)\sin(2x) - \cos(2x) = 0$$

✗ **Mathematica** : cpu = 0 (sec), leaf count = 0 , crash

```
Kernel Crash
```

✓ **Maple** : cpu = 0.408 (sec), leaf count = 128

$$\left\{ y(x) = 2\frac{\sin(2x)}{\sqrt{2\cos(2x)+2}}\left(\_C1\,(\cos(2x)+1)\,HeunCPrime\left(1,1/2,-1/2,-1,\frac{7}{8},1/2\cos(2x)+1/2\right) + Heu\right.\right.$$

Hand solution

$$y' - y^2 - y\sin(2x) - \cos(2x) = 0$$

$$y' = y^2 + y\sin(2x) + \cos(2x) \tag{1}$$

This is Riccati first order non-linear ODE of the form of the general form $y' = P(x) + Q(x)\,y + R(x)\,y^2$ where $P(x) = \cos(2x), Q(x) = \sin(2x), R(x) = 1$. It is best to first try to spot a particular solution y_p and use the transformation $y = y_p + \frac{1}{u}$ otherwise we use $y = -\frac{u'}{yR(x)}$ transformation. For this problem

$$y_p = \tan(x)$$

To verify, since $y_p' = \frac{1}{\cos^2 x}$ then plugging this particular in (1) gives

$$\frac{1}{\cos^2 x} - \tan^2(x) - \tan(x)\sin(2x) - \cos(2x) = 0$$

But $\cos(2x) = \cos^2 x - \sin^2 x$ and $\sin(2x) = 2\sin x\cos x$ and $\tan(x) = \frac{\sin x}{\cos x}$ therefore the above becomes

$$\begin{aligned}
\frac{1}{\cos^2 x} - \frac{\sin^2 x}{\cos^2 x} - \frac{\sin x}{\cos x}(2\sin x \cos x) - \left(\cos^2 x - \sin^2 x\right) &= 0 \\
\frac{1}{\cos^2 x} - \frac{\sin^2 x}{\cos^2 x} - 2\sin^2 x - \cos^2 x + \sin^2 x &= 0 \\
\frac{1}{\cos^2 x} - \frac{\sin^2 x}{\cos^2 x} - \sin^2 x - \cos^2 x &= 0 \\
\frac{1}{\cos^2 x} - \frac{\sin^2 x}{\cos^2 x} - 1 &= 0 \\
\frac{1 - \sin^2 x}{\cos^2 x} - 1 &= 0 \\
\frac{\cos^2 x}{\cos^2 x} - 1 &= 0 \\
1 - 1 &= 0 \\
0 &= 0
\end{aligned}$$

Therefore we, we can use $y = y_p + \frac{1}{u}$

$$\begin{aligned}
y &= \tan x + \frac{1}{u} \\
y' &= \frac{1}{\cos^2 x} - \frac{u'}{u^2}
\end{aligned}$$

Equating this to (1) gives

$$\begin{aligned}
-\frac{u'}{u^2} &= y^2 + y\sin(2x) + \cos(2x) \\
-\frac{u'}{u^2} &= -\frac{1}{\cos^2 x} + \left(\tan x + \frac{1}{u}\right)^2 + \left(\tan x + \frac{1}{u}\right)\sin(2x) + \cos(2x)
\end{aligned}$$

Using $\sin(2x) = 2\sin x \cos x$ and $\cos 2x = \cos^2 x - \sin^2 x$ then above becomes

$$
\begin{aligned}
-\frac{u'}{u^2} &= -\frac{1}{\cos^2 x} + \left(\tan^2 x + \frac{1}{u^2} + \frac{2}{u}\tan x\right) + \left(\frac{\sin x}{\cos x} + \frac{1}{u}\right) 2\sin x\cos x + \left(\cos^2 x - \sin^2 x\right) \\
u' &= \frac{u^2}{\cos^2 x} - \left(u^2\frac{\sin^2 x}{\cos^2 x} + 1 + 2u\frac{\sin x}{\cos x}\right) - \left(u^2\frac{\sin x}{\cos x} + u\right) 2\sin x\cos x - u^2\cos^2 x + u^2\sin^2 x \\
&= \frac{u^2}{\cos^2 x} - u^2\frac{\sin^2 x}{\cos^2 x} - 1 - 2u\frac{\sin x}{\cos x} - 2u^2\frac{\sin x}{\cos x}\sin x\cos x - 2u\sin x\cos x - u^2\cos^2 x + u^2\sin^2 x \\
&= \frac{u^2}{\cos^2 x} - u^2\frac{\sin^2 x}{\cos^2 x} - 1 - 2u\frac{\sin x}{\cos x} - 2u^2\sin^2 x - 2u\sin x\cos x - u^2\cos^2 x + u^2\sin^2 x \\
&= \frac{u^2}{\cos^2 x} - u^2\frac{\sin^2 x}{\cos^2 x} - 1 - 2u\frac{\sin x}{\cos x} - u^2\sin^2 x - 2u\sin x\cos x - u^2\cos^2 x \\
&= u^2\left(\frac{1}{\cos^2 x} - \frac{\sin^2 x}{\cos^2 x} - \left(\sin^2 x + \cos^2 x\right)\right) - 1 + u\left(-2\frac{\sin x}{\cos x} - 2\sin x\cos x\right) \\
&= u^2\left(\frac{1-\sin^2 x}{\cos^2 x} - 1\right) - 1 + u\left(-2\frac{\sin x}{\cos x} - 2\sin x\cos x\right) \\
&= u^2\left(\frac{\cos^2 x}{\cos^2 x} - 1\right) - 1 + u\left(-2\frac{\sin x}{\cos x} - 2\sin x\cos x\right) \\
&= -1 + 2u\left(-\frac{\sin x}{\cos x} - \sin x\cos x\right)
\end{aligned}
$$

Hence

$$u' + 2u(\tan x + \sin x\cos x) = -1$$

Integrating factor is $e^{2\int \tan x + \sin x\cos x dx}$. But

$$\int \tan x dx = -\ln(\cos x)$$

And

$$\int \sin x\cos x dx = \frac{-1}{2}\cos^2 x$$

Hence $\mu = e^{-2\ln\cos x}e^{-\cos^2 x} = \frac{1}{\cos^2 x}e^{-\cos^2 x}$, therefore

$$d\left(\frac{1}{\cos^2 x}e^{-\cos^2 x}u\right) = \frac{-1}{\cos^2 x}e^{-\cos^2 x}$$

Integrating both sides

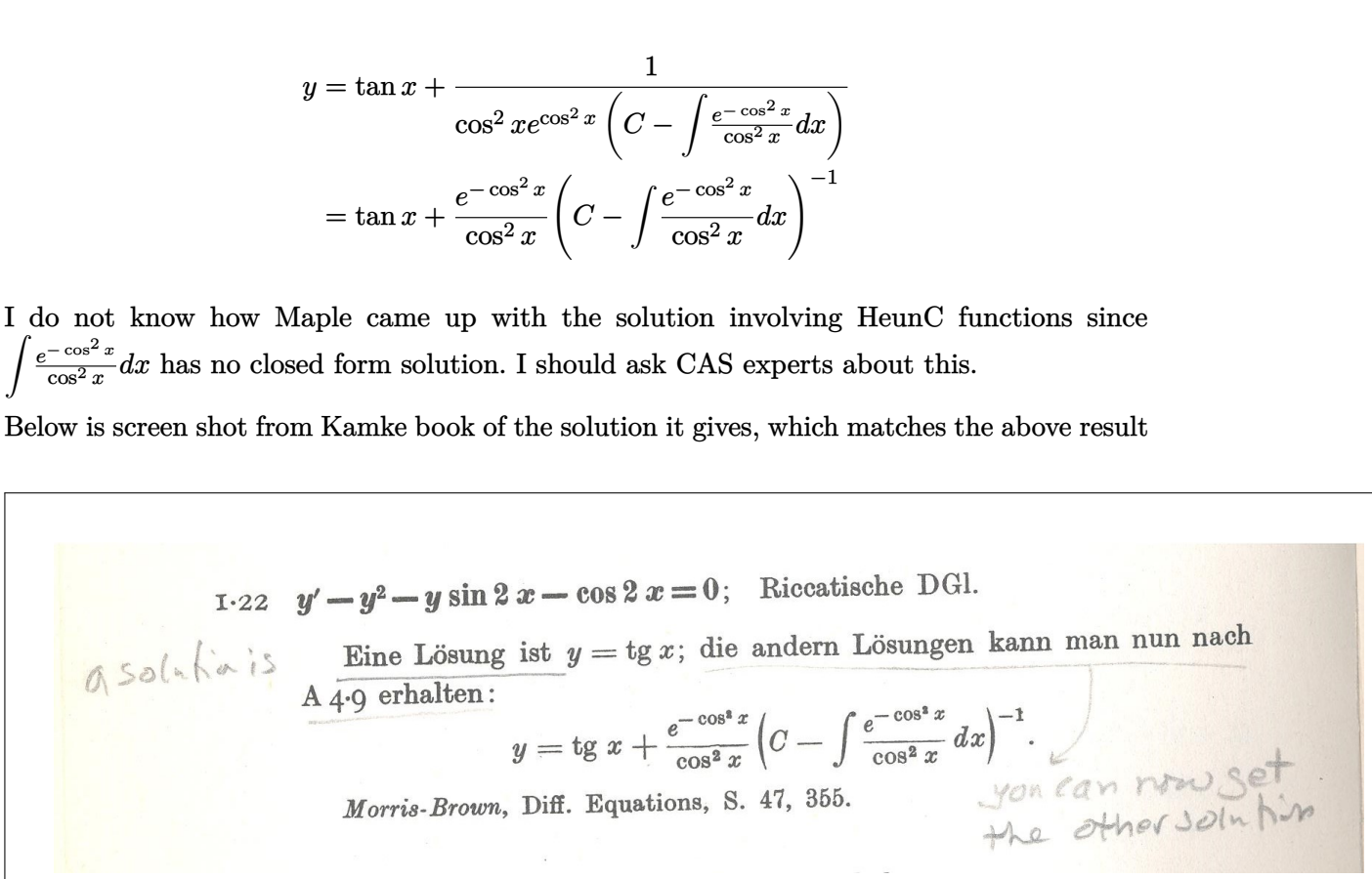
$$
\begin{aligned}
\frac{1}{\cos^2 x}e^{-\cos^2 x}u &= -\int \frac{e^{-\cos^2 x}}{\cos^2 x}dx + C \\
u &= \cos^2 x e^{\cos^2 x}\left(C - \int \frac{e^{-\cos^2 x}}{\cos^2 x}dx\right)
\end{aligned}
$$

Since $y = \tan x + \frac{1}{u}$ then

$$\begin{aligned} y &= \tan x + \frac{1}{\cos^2 x e^{\cos^2 x}\left(C - \int \frac{e^{-\cos^2 x}}{\cos^2 x} dx\right)} \\ &= \tan x + \frac{e^{-\cos^2 x}}{\cos^2 x}\left(C - \int \frac{e^{-\cos^2 x}}{\cos^2 x} dx\right)^{-1} \end{aligned}$$

I do not know how Maple came up with the solution involving HeunC functions since $\int \frac{e^{-\cos^2 x}}{\cos^2 x} dx$ has no closed form solution. I should ask CAS experts about this.

Below is screen shot from Kamke book of the solution it gives, which matches the above result



1·22 $y' - y^2 - y \sin 2x - \cos 2x = 0$; Riccatische DGl.

a solution is

Eine Lösung ist $y = \operatorname{tg} x$; die andern Lösungen kann man nun nach A 4·9 erhalten:

$$y = \operatorname{tg} x + \frac{e^{-\cos^2 x}}{\cos^2 x}\left(C - \int \frac{e^{-\cos^2 x}}{\cos^2 x} dx\right)^{-1}.$$

Morris-Brown, Diff. Equations, S. 47, 355.

you can now set the other solution

2.23 ODE No. 23

$$ay(x)^2 - b + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0225357 (sec), leaf count = 43

$$\left\{\left\{y(x) \to \frac{\sqrt{b}\tanh\left(\sqrt{a}\sqrt{b}c_1 + \sqrt{a}\sqrt{b}x\right)}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 23

$$\left\{y(x) = \frac{1}{a}\tanh\left(\sqrt{ab}(x + \_C1)\right)\sqrt{ab}\right\}$$

Hand solution

$$y' + ay^2 - b = 0$$
$$\frac{dy}{dx} = b - ay^2$$

Separable,

$$\frac{dy}{b - ay^2} = dx$$
$$\int \frac{dy}{b - ay^2} = \int dx$$

But

$$\int \frac{dy}{b - ay^2} = \frac{1}{\sqrt{ab}}\tanh^{-1}\left(\sqrt{\frac{a}{b}}y\right)$$

Hence

$$\frac{1}{\sqrt{ab}}\tanh^{-1}\left(\sqrt{\frac{a}{b}}y\right) = x + C$$
$$\tanh^{-1}\left(\sqrt{\frac{a}{b}}y\right) = \sqrt{ab}(x + C)$$
$$\sqrt{\frac{a}{b}}y = \tanh\left(\sqrt{ab}(x + C)\right)$$
$$y = \sqrt{\frac{b}{a}}\tanh\left(\sqrt{ab}(x + C)\right)$$

2.24 ODE No. 24

$$ay(x)^2 - bx^\nu + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0136367 (sec), leaf count = 277

$$\left\{\left\{y(x) \to -\frac{\sqrt{-a}\sqrt{b}x^{\frac{\nu+2}{2}}\left(c_1 J_{\frac{\nu+1}{\nu+2}}\left(\frac{2\sqrt{-a}\sqrt{b}x^{\frac{\nu}{2}+1}}{\nu+2}\right) - c_1 J_{-\frac{\nu+3}{\nu+2}}\left(\frac{2\sqrt{-a}\sqrt{b}x^{\frac{\nu+2}{2}}}{\nu+2}\right) - 2J_{\frac{1}{\nu+2}-1}\left(\frac{2\sqrt{-a}\sqrt{b}x^{\frac{\nu+2}{2}}}{\nu+2}\right)\right) - c_1 J_{-}}{2ax\left(c_1 J_{-\frac{1}{\nu+2}}\left(\frac{2\sqrt{-a}\sqrt{b}x^{\frac{\nu+2}{2}}}{\nu+2}\right) + J_{\frac{1}{\nu+2}}\left(\frac{2\sqrt{-a}\sqrt{b}x^{\frac{\nu+2}{2}}}{\nu+2}\right)\right)}\right.\right.$$

✓ **Maple** : cpu = 0.076 (sec), leaf count = 201

$$\left\{y(x) = \frac{1}{ax}\left(-\left(J_{\frac{3+\nu}{\nu+2}}\left(2\frac{\sqrt{-ab}x^{\nu/2+1}}{\nu+2}\right)\_C1 + Y_{\frac{3+\nu}{\nu+2}}\left(2\frac{\sqrt{-ab}x^{\nu/2+1}}{\nu+2}\right)\right)\sqrt{-ab}x^{\frac{\nu}{2}+1} + \_C1\, J_{(\nu+2)^{-1}}\left(2\frac{\sqrt{-abx}}{\nu+\right.\right.\right.$$

Hand solution

$$\begin{aligned} y' + ay^2 - bx^v &= 0 \\ y' &= bx^v - ay^2 \\ &= P(x) + Q(x)\, y + R(x)\, y^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE with $P(x) = bx^v, Q(x) = 0, R(x) = -a$. Using the standard substitution

$$y = -\frac{u'}{uR\,(x)} = \frac{u'}{au}$$

Hence

$$y' = \frac{u''}{au} - \frac{(u')^2}{au^2}$$

Therefore (1) becomes

$$\begin{aligned} \frac{u''}{au} - \frac{(u')^2}{au^2} &= bx^v - ay^2 \\ &= bx^v - a\left(\frac{u'}{au}\right)^2 \\ &= bx^v - \frac{(u')^2}{au^2} \end{aligned}$$

Hence

$$\frac{u''}{au} = bx^v$$
$$u'' - abx^v u = 0$$

This is an Emden-Fowler equation, of the general form $u'' = Ax^n u^m$, where here $m = 1$ and $n = v$ and $A = ab$.

For any n, the solution uses Bessel functions and modified Bessel functions of first and second kind. From Handbook of exact solutions for ODE, page 237, equation 2.1.2.7 we see the solution is given as

$$u = \begin{cases} C_1\sqrt{x}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right) + C_2\sqrt{x}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right) & ab < 0 \\ C_1\sqrt{x}I_{\frac{1}{2q}}\left(\frac{\sqrt{ab}}{q}x^q\right) + C_2\sqrt{x}K_{\frac{1}{2q}}\left(\frac{\sqrt{ab}}{q}x^q\right) & ab > 0 \end{cases}$$

Where $q = \frac{n+1}{2}$. J is Bessel function of first kind and Y is Bessel function of second kind. I is modified Besself function of first kind and K is modified Besself function of second kind. To find y we now use $y = \frac{u'}{au}$. Derivative of Bessel functions is given by

$$\begin{aligned} J'_m(x) &= \frac{1}{2}(J_{m-1}(x) - J_{m+1}(x)) \\ Y'_m(x) &= \frac{1}{2}(Y_{m-1}(x) - Y_{m+1}(x)) \\ I'_m(x) &= \frac{1}{2}(I_{m-1}(x) + I_{m+1}(x)) \\ K'_m(x) &= -\frac{1}{2}(K_{m-1}(x) + K_{m+1}(x)) \end{aligned}$$

Using these, then

$$u' = \begin{cases} C_1\left[\frac{1}{2\sqrt{x}}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right) + \sqrt{x}J'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right] + C_2\left[\frac{1}{2\sqrt{x}}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right) + \sqrt{x}Y'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right] & ab < 0 \\ C_1\left[\frac{1}{2\sqrt{x}}I_{\frac{1}{2q}}\left(\frac{\sqrt{ab}}{q}x^q\right) + \sqrt{x}I'_{\frac{1}{2q}}\left(\frac{\sqrt{ab}}{q}x^q\right)\right] + C_2\left[\frac{1}{2\sqrt{x}}K_{\frac{1}{2q}}\left(\frac{\sqrt{ab}}{q}x^q\right) + \sqrt{x}K'_{\frac{1}{2q}}\left(\frac{\sqrt{ab}}{q}x^q\right)\right] & ab > 0 \end{cases}$$

Hence for $ab < 0$

$$
\begin{aligned}
y &= \frac{u'}{au} \\
&= \frac{C_1\left[\frac{1}{2\sqrt{x}}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+\sqrt{x}J'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right]+C_2\left[\frac{1}{2\sqrt{x}}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+\sqrt{x}Y'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right]}{aC_1\sqrt{x}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+aC_2\sqrt{x}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)} \\
&= \frac{\sqrt{x}C_1\left[\frac{1}{2x}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+J'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right]+\sqrt{x}C_2\left[\frac{1}{2x}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+Y'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right]}{aC_1\sqrt{x}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+aC_2\sqrt{x}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)} \\
&= \frac{C_1\left[\frac{1}{2x}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+J'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right]+C_2\left[\frac{1}{2x}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+Y'_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right]}{aC_1J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+aC_2Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)}
\end{aligned}
$$

Using derivatives the above becomes

$$
\begin{aligned}
y &= \frac{C_1\left[\frac{1}{2x}J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+\frac{1}{2}\left(J_{\frac{1}{2q}-1}\left(\frac{\sqrt{-ab}}{q}x^q\right)-J_{\frac{1}{2q}+1}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right)\right]}{aC_1J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+aC_2Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)} \\
&+ \frac{C_2\left[\frac{1}{2x}Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+\frac{1}{2}\left(Y_{\frac{1}{2q}-1}\left(\frac{\sqrt{-ab}}{q}x^q\right)-Y_{\frac{1}{2q}+1}\left(\frac{\sqrt{-ab}}{q}x^q\right)\right)\right]}{aC_1J_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)+aC_2Y_{\frac{1}{2q}}\left(\frac{\sqrt{-ab}}{q}x^q\right)}
\end{aligned}
$$

Similar result can be found for $ab > 0$

2.25 ODE No. 25

$$ay(x)^2 - bx^{2\nu} - cx^{\nu-1} + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.232605 (sec), leaf count = 1835

$$\left\{\left\{y(x) \to \frac{-2^{\frac{\nu}{2(\nu+1)}-1} e^{-\frac{\sqrt{a}\sqrt{b}x^{\nu+1}}{\sqrt{\nu^2+2\nu+1}}} \nu \left(x^{\nu+1}\right)^{\frac{\nu}{2(\nu+1)}} L_{-\frac{\frac{\sqrt{a}\sqrt{b}\nu c}{\sqrt{(\nu+1)^2}}+\frac{\sqrt{a}\sqrt{b}c}{\sqrt{(\nu+1)^2}}+b\nu}{2(\nu b+b)}}^{\frac{\nu}{\nu+1}-1}\left(\frac{2\sqrt{a}\sqrt{b}x^{\nu+1}}{\sqrt{\nu^2+2\nu+1}}\right) x^{-\frac{\nu}{2}-1} - \frac{2^{\frac{\nu}{2(\nu+1)}}\sqrt{a}\sqrt{b}e^{-\frac{\sqrt{a}\sqrt{b}x^{\nu}}{\sqrt{\nu^2+2\nu}}}\cdots}{\cdots}}{\cdots}\right.\right.$$

✓ **Maple** : cpu = 0.309 (sec), leaf count = 348

$$\left\{y(x) = -\frac{1}{2\,ax}\left(\left(\left(-\nu-2\right)b^{\frac{3}{2}}+\sqrt{a}bc\right)M_{-\frac{1}{2\,\nu+2}\left(\left(-2\,\nu-2\right)\sqrt{b}+\sqrt{a}c\right)\frac{1}{\sqrt{b}},\,(2\,\nu+2)^{-1}}\left(2\,\frac{\sqrt{a}\sqrt{b}x^{\nu+1}}{\nu+1}\right)+2\,b^{3/2}\_C1\,(\nu+\cdots\right.\right.$$

Hand solution

$$\begin{aligned} y' + ay^2 - bx^{2v} - cx^{v-1} &= 0 \\ y' &= bx^v + cx^{v-1} - ay^2 \\ &= P(x) + Q(x)\,y + R(x)\,y^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE with $P(x) = bx^v + cx^{v-1}, Q(x) = 0, R(x) = -a$.

Need to do this later.

2.26 ODE No. 26

$$y'(x) - (Ay(x) - a)(By(x) - b) = 0$$

✓ **Mathematica** : cpu = 0.0769893 (sec), leaf count = 68

$$\left\{\left\{y(x) \to \frac{ae^{Abc_1+Abx} - be^{aBc_1+aBx}}{Ae^{Abc_1+Abx} - Be^{aBc_1+aBx}}\right\}\right\}$$

✓ **Maple** : cpu = 0.064 (sec), leaf count = 45

$$\left\{y(x) = \frac{\mathrm{e}^{(x+\_C1)(Ab-aB)}a - b}{\mathrm{e}^{(x+\_C1)(Ab-aB)}A - B}\right\}$$

Hand solution

$$\begin{aligned} y' - (Ay - a)(By - b) &= 0 \\ y' &= (Ay - a)(By - b) \\ &= ab - y(Ab + Ba) + ABy^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE with $P(x) = ab, Q(x) = -(Ab + Ba), R(x) = AB$. Let $y = -\frac{u'}{uR(x)} = -\frac{u'}{ABu}$, hence

$$y' = \frac{-u''}{ABu} - \frac{(u')^2}{ABu^2}$$

Comparing to (1) results in

$$\begin{aligned} \frac{-u''}{ABu} - \frac{(u')^2}{ABu^2} &= ab - y(Ab + Ba) + ABy^2 \\ &= ab - \left(-\frac{u'}{ABu}\right)(Ab + Ba) + AB\left(-\frac{u'}{ABu}\right)^2 \\ &= ab + \frac{u'}{ABu}(Ab + Ba) + AB\frac{(u')^2}{(ABu)^2} \\ &= ab + \frac{u'}{ABu}(Ab + Ba) + \frac{(u')^2}{ABu^2} \end{aligned}$$

Hence

$$\begin{aligned}\frac{-u''}{ABu} &= ab + \frac{u'}{ABu}(Ab + Ba)\\ -u'' &= ABabu + u'(Ab + Ba)\\ u'' + u'(Ab + Ba) + u(ABab) &= 0\end{aligned}$$

This is second order ODE with constant coefficient. Solution is

$$u = c_1 e^{-aBx} + c_2 e^{-Abx}$$

Therefore

$$u' = -aBc_1 e^{-aBx} - c_2 Abe^{-Abx}$$

And therefore the solution is

$$\begin{aligned}y &= -\frac{u'}{ABu} = -\frac{1}{AB}\frac{-aBc_1 e^{-aBx} - c_2 Abe^{-Abx}}{c_1 e^{-aBx} + c_2 e^{-Abx}}\\ &= \frac{aBc_1 e^{-aBx} + c_2 Abe^{-Abx}}{AB\left(c_1 e^{-aBx} + c_2 e^{-Abx}\right)}\end{aligned}$$

Dividing by c_2 and letting $c = \frac{c_1}{c_2}$

$$y = \frac{aBce^{-aBx} + Abe^{-Abx}}{AB\left(ce^{-aBx} + e^{-Abx}\right)}$$

Verification

```
eq:=diff(y(x),x)-(A*y(x)-a)*(B*y(x)-b) = 0;
sol:=(a*B*_C1*exp(-a*B*x)+A*b*exp(-A*b*x))/(A*B*(_C1*exp(-a*B*x)+exp(-A*b*x)));
odetest(y(x)=sol,eq);
0
```

2.27 ODE No. 27

$$ay(x)(y(x)-x)+y'(x)-1=0$$

✓ **Mathematica** : cpu = 0.0445405 (sec), leaf count = 120

$$\left\{\left\{y(x)\to \frac{c_1\left(\sqrt{\frac{\pi}{2}}\sqrt{a}xe^{\frac{ax^2}{2}}\text{erf}\left(\frac{\sqrt{a}x}{\sqrt{2}}\right)+1\right)+axe^{\frac{ax^2}{2}}}{a\left(\frac{\sqrt{\frac{\pi}{2}}c_1e^{\frac{ax^2}{2}}\text{erf}\left(\frac{\sqrt{a}x}{\sqrt{2}}\right)}{\sqrt{a}}+e^{\frac{ax^2}{2}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.196 (sec), leaf count = 72

$$\left\{y(x)=1\left(2\sqrt{a}\mathrm{e}^{-1/2\,ax^2}+x\left(\sqrt{2}\sqrt{\pi}Erf\left(\frac{\sqrt{2}x}{2}\sqrt{a}\right)a+2\,a^{3/2}\_C1\right)\right)\left(\sqrt{2}\sqrt{\pi}Erf\left(\frac{\sqrt{2}x}{2}\sqrt{a}\right)a+2\,a^{3/2}\_C1\right)\right.$$

Hand solution

$$\begin{aligned} y'+ay(y-x)-1&=0\\ y'&=1-\left(ay^2-ayx\right)\\ &=1+ayx-ay^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE $y'=P(x)+A(x)\,y+R(x)\,y^2$ with $P(x)=1,Q(x)=-ax,R(x)=-a$. We can convert Riccati to Bernoulli which is easier to solve using the substitution $u=y-x$

$$\begin{aligned} u'&=y'-1\\ &=\left(1+ayx-ay^2\right)-1\\ &=\left(1+a(u+x)\,x-a(u+x)^2\right)-1\\ &=1+aux+ax^2-a\left(u^2+x^2+2ux\right)-1\\ &=1+aux+ax^2-au^2-ax^2-2aux-1\\ &=-aux-au^2\\ u'&=-aux-au^2 \end{aligned}$$

This is of the form $u'=P(x)+Q(x)\,u+R(x)\,u^2$ and since $P(x)=0$ then it is Bernoulli differential equation. (when $P(x)\neq 0$ and $R(x)\neq 0$ it is Riccati). To solve Bernoulli we always start by dividing by u^2

$$\frac{u'}{u^2}=-\frac{ax}{u}-a$$

Then we let $\zeta = \frac{1}{u}$, hence $\zeta' = -\frac{u'}{u^2}$, therefore the above becomes

$$\begin{aligned} -\zeta' &= -ax\zeta - a \\ \zeta' - ax\zeta &= a \end{aligned}$$

Integrating factor is $e^{-\int axdx} = e^{-a\frac{x^2}{2}}$, hence $d\left(e^{-a\frac{x^2}{2}}\zeta\right) = ae^{-a\frac{x^2}{2}}$. Integrating both sides gives

$$e^{-a\frac{x^2}{2}}\zeta = a\int e^{-a\frac{x^2}{2}}dx + C$$

But

$$\int e^{-a\frac{x^2}{2}}dx = \sqrt{\frac{\pi}{2a}}\operatorname{erf}\left(\sqrt{\frac{a}{2}}x\right)$$

Therefore

$$\begin{aligned} e^{-a\frac{x^2}{2}}\zeta &= a\sqrt{\frac{\pi}{2a}}\operatorname{erf}\left(\sqrt{\frac{a}{2}}x\right) + C \\ \zeta &= e^{a\frac{x^2}{2}}\left(a\sqrt{\frac{\pi}{2a}}\operatorname{erf}\left(\sqrt{\frac{a}{2}}x\right) + C\right) \end{aligned}$$

Hence

$$\begin{aligned} u &= \frac{1}{\zeta} \\ &= e^{-a\frac{x^2}{2}}\left(a\sqrt{\frac{\pi}{2a}}\operatorname{erf}\left(\sqrt{\frac{a}{2}}x\right) + C\right)^{-1} \end{aligned}$$

Since $u = y - x$ then

$$\begin{aligned} y &= u + x \\ &= e^{-a\frac{x^2}{2}}\left(a\sqrt{\frac{\pi}{2a}}\operatorname{erf}\left(\sqrt{\frac{a}{2}}x\right) + C\right)^{-1} + x \\ &= \frac{e^{-a\frac{x^2}{2}}}{\sqrt{\frac{a\pi}{2}}\operatorname{erf}\left(\sqrt{\frac{a}{2}}x\right) + C} + x \end{aligned}$$

Verification

```
eq:=diff(y(x),x)+a*y(x)*(y(x)-x)-1 = 0;
sol:=exp(-a*x^2/2)/(sqrt(a*Pi/2)*erf(sqrt(a/2)*x)+_C1)+x;
odetest(y(x)=sol,eq);
0
```

2.28 ODE No. 28

$$x^3(-y(x)) + y'(x) + xy(x)^2 - 2x = 0$$

✓ **Mathematica** : cpu = 0.0484709 (sec), leaf count = 96

$$\left\{\left\{y(x) \to \frac{c_1 e^{\frac{x^4}{4}} x^3 + \frac{1}{2}\sqrt{\pi} e^{\frac{x^4}{4}} x^3 \text{erf}\left(\frac{x^2}{2}\right) + x}{x\left(c_1 e^{\frac{x^4}{4}} + \frac{1}{2}\sqrt{\pi} e^{\frac{x^4}{4}} \text{erf}\left(\frac{x^2}{2}\right)\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 51

$$\left\{y(x) = \frac{1}{\sqrt{\pi}}\left(Erf\left(\frac{x^2}{2}\right)\sqrt{\pi}\_C1\, x^2 + x^2\sqrt{\pi} + 2\,\mathrm{e}^{-1/4\,x^4}\_C1\right)\left(Erf\left(\frac{x^2}{2}\right)\_C1 + 1\right)^{-1}\right\}$$

Hand solution

$$\begin{aligned} y' - yx^3 + xy^2 - 2x &= 0 \\ y' &= 2x + yx^3 - xy^2 \\ &= P(x) + Q(x)\,y + R(x)\,y^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE with $P(x) = 2x, Q(x) = x^3, R(x) = -x$. We can convert Riccati to Bernoulli which is easier to solve using the substitution $u = x^2 - y$ or $y = x^2 - u$

$$\begin{aligned} u' &= 2x - y' \\ &= 2x - \left(2x + yx^3 - xy^2\right) \\ &= 2x - \left(2x + \left(x^2 - u\right)x^3 - x\left(x^2 - u\right)^2\right) \\ &= 2x - \left(2x + \left(x^5 - ux^3\right) - x\left(x^4 + u^2 - 2x^2u\right)\right) \\ u' &= 2x - \left(2x + \left(x^5 - ux^3\right) - \left(x^5 + xu^2 - 2x^3u\right)\right) \\ &= 2x - 2x - \left(x^5 - ux^3\right) + \left(x^5 + xu^2 - 2x^3u\right) \\ &= -x^5 + ux^3 + x^5 + xu^2 - 2x^3u \\ &= -ux^3 + xu^2 \end{aligned}$$

This is of the form $u' = P(x) + Q(x)\,u + R(x)\,u^2$ and since $P(x) = 0$ then it is Bernoulli differential equation. (when $P(x) \neq 0$ and $R(x) \neq 0$ it is Riccati). To solve Bernoulli we always start by dividing by u^2

$$\frac{u'}{u^2} = -\frac{1}{u}x^3 + x$$

Then we let $\zeta = -\frac{1}{u}$, hence $\zeta' = \frac{u'}{u^2}$, therefore the above becomes

$$\begin{aligned} \zeta' &= x^3\zeta + x \\ \zeta' - x^3\zeta &= x \end{aligned}$$

Integrating factor is $e^{-\int x^3 dx} = e^{-\frac{x^4}{4}}$, hence

$$d\left(e^{-\frac{x^4}{4}}\zeta\right) = xe^{-\frac{x^4}{4}}$$

Integrating both sides gives

$$e^{-\frac{x^4}{4}}\zeta = \int xe^{-\frac{x^4}{4}}dx + C$$

$\int xe^{-\frac{x^4}{4}}dx = \frac{\sqrt{\pi}}{2}\operatorname{erf}\left(\frac{x^2}{2}\right)$, hence from above

$$\begin{aligned} e^{-\frac{x^4}{4}}\zeta &= \frac{\sqrt{\pi}}{2}\operatorname{erf}\left(\frac{x^2}{2}\right) + C \\ \zeta &= e^{\frac{x^4}{4}}\left(\frac{\sqrt{\pi}}{2}\operatorname{erf}\left(\frac{x^2}{2}\right) + C\right) \end{aligned}$$

Since $\zeta = -\frac{1}{u}$ then

$$u = -e^{-\frac{x^4}{4}}\left(\frac{\sqrt{\pi}}{2}\operatorname{erf}\left(\frac{x^2}{2}\right) + C\right)^{-1}$$

And since $y = x^2 - u$ then

$$\begin{aligned} y &= x^2 + e^{-\frac{x^4}{4}}\left(\frac{\sqrt{\pi}}{2}\operatorname{erf}\left(\frac{x^2}{2}\right) + C\right)^{-1} \\ &= x^2 + \frac{e^{-\frac{x^4}{4}}}{\frac{\sqrt{\pi}}{2}\operatorname{erf}\left(\frac{x^2}{2}\right) + C} \end{aligned}$$

Verification

```
eq:=diff(y(x),x)+x*y(x)^2-x^3*y(x)-2*x = 0;
sol:=x^2+ exp(-x^4/4)/(_C1+ sqrt(Pi)/2*erf(x^2/2));
odetest(y(x)=sol,eq);
0
```

2.29 ODE No. 29

$$y'(x) - xy(x)^2 - 3xy(x) = 0$$

✓ **Mathematica** : cpu = 0.0226202 (sec), leaf count = 39

$$\left\{\left\{y(x) \to -\frac{3e^{3c_1+\frac{3x^2}{2}}}{e^{3c_1+\frac{3x^2}{2}}-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 19

$$\left\{y(x) = 3\left(-1+3\,\mathrm{e}^{-3/2\,x^2}\_C1\right)^{-1}\right\}$$

Hand solution

$$\begin{aligned} y' - xy^2 - 3xy &= 0 \\ y' &= 3xy + xy^2 \\ &= P(x) + Q(x)\,y + R(x)\,y^2 \end{aligned} \tag{1}$$

This is Bernoulli first order non-linear ODE since $P(x) = 0$. To solve Bernoulli we always start by dividing by y^2

$$\frac{y'}{y^2} = \frac{3x}{y} + x$$

Then we let $u = \frac{1}{y}$, hence $u' = \frac{-y'}{y^2}$, therefore the above becomes

$$\begin{aligned} -u' &= 3xu + x \\ u' + 3ux &= -x \end{aligned}$$

Integrating factor is $e^{\int 3x dx} = e^{\frac{3x^2}{2}}$, hence

$$d\left(e^{\frac{3x^2}{2}}u\right) = -xe^{\frac{3x^2}{2}}$$

Integrating both sides gives

$$\begin{aligned} e^{\frac{3x^2}{2}}u &= \int -xe^{\frac{3x^2}{2}}dx + C \\ &= -\frac{1}{3}e^{\frac{3x^2}{2}} + C \end{aligned}$$

Hence from above

$$u = e^{\frac{-3x^2}{2}}\left(-\frac{1}{3}e^{\frac{3x^2}{2}} + C\right)$$

And since $y = \frac{1}{u}$ then

$$y = \frac{e^{\frac{3x^2}{2}}}{C - \frac{1}{3}e^{\frac{3x^2}{2}}}$$

Verification

```
eq:=diff(y(x),x)-x*y(x)^2-3*x*y(x) = 0;
sol:=exp(3*x^2/2)/(_C1- 1/3*exp(3*x^2/2));
odetest(y(x)=sol,eq);
0
```

2.30 ODE No. 30

$$x^{-a-1}y(x)^2 - x^a + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0655547 (sec), leaf count = 230

$$\left\{\left\{y(x) \to \frac{x^{a+1}\left(c_1\left(\frac{1}{2}x^{-\frac{a}{2}-\frac{1}{2}}\Gamma(a+1)\left(I_{a-1}\left(2\sqrt{x}\right)+I_{a+1}\left(2\sqrt{x}\right)\right)-\frac{1}{2}ax^{-\frac{a}{2}-1}\Gamma(a+1)I_a\left(2\sqrt{x}\right)\right)-\frac{1}{2}(-1)^{-a}ax^{-}\right.}{c_1x^{-a/2}\Gamma(a+1)I_a\left(2\sqrt{x}\right)+(-1)^{-a}x^{-a/2}}\right.\right.$$

✓ **Maple** : cpu = 0.085 (sec), leaf count = 54

$$\left\{y(x) = x^{a+1}\left(-K_{a+1}\left(2\sqrt{x}\right)\_C1 + I_{a+1}\left(2\sqrt{x}\right)\right)\frac{1}{\sqrt{x}}\left(K_a\left(2\sqrt{x}\right)\_C1 + I_a\left(2\sqrt{x}\right)\right)^{-1}\right\}$$

Hand solution

$$\begin{aligned} y' + x^{-a-1}y^2 - x^a &= 0 \\ y' &= x^a - x^{-a-1}y^2 \\ &= P(x) + Q(x)\,y + R(x)\,y^2 \end{aligned} \tag{1}$$

This is Ricatti first order non-linear ODE. Using standard transformation

$$y = -\frac{u'}{uR(x)} = x^{a+1}\frac{u'}{u}$$

Hence

$$y' = (a+1)\,x^a\frac{u'}{u} + x^{a+1}\frac{u''}{u} - x^{a+1}\frac{(u')^2}{u^2}$$

Comparing to (1) gives

$$\begin{aligned} x^a - x^{-a-1}y^2 &= (a+1)\,x^a\frac{u'}{u} + x^{a+1}\frac{u''}{u} - x^{a+1}\frac{(u')^2}{u^2} \\ x^a - x^{-a-1}\left(x^{a+1}\frac{u'}{u}\right)^2 &= (a+1)\,x^a\frac{u'}{u} + x^{a+1}\frac{u''}{u} - x^{a+1}\frac{(u')^2}{u^2} \\ 1 - \frac{x^{-a-1}}{x^a}x^{2a+2}\frac{(u')^2}{u^2} &= (a+1)\,\frac{u'}{u} + x\frac{u''}{u} - x\frac{(u')^2}{u^2} \\ 1 - x\frac{(u')^2}{u^2} &= (a+1)\,\frac{u'}{u} + x\frac{u''}{u} - x\frac{(u')^2}{u^2} \\ 1 &= (a+1)\,\frac{u'}{u} + x\frac{u''}{u} \\ xu'' + (1+a)\,u' - u &= 0 \end{aligned} \tag{2}$$

This is Bessel like second order linear ODE. The solution is

$$u = C_1 \frac{1}{\sqrt{x^a}} \operatorname{BesselI}\left(a, 2\sqrt{x}\right) + C_2 \frac{1}{\sqrt{x^a}} \operatorname{BesselK}\left(a, 2\sqrt{x}\right)$$

But

$$\begin{aligned}
\frac{d}{dx} \frac{1}{\sqrt{x^a}} \operatorname{BesselI}\left(a, 2\sqrt{x}\right) &= \frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselI}\left(1+a, 2\sqrt{x}\right) \\
\frac{d}{dx} \frac{1}{\sqrt{x^a}} \operatorname{BesselI}\left(a, 2\sqrt{x}\right) &= -\frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselK}\left(1+a, 2\sqrt{x}\right)
\end{aligned}$$

Hence

$$u' = C_1 \frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselI}\left(1+a, 2\sqrt{x}\right) - C_2 \frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselK}\left(1+a, 2\sqrt{x}\right)$$

And from $y = x^{a+1} \frac{u'}{u}$

$$y = x^{1+a} \frac{C_1 \frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselI}\left(1+a, 2\sqrt{x}\right) - C_2 \frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselK}\left(1+a, 2\sqrt{x}\right)}{C_1 \frac{1}{\sqrt{x^a}} \operatorname{BesselI}\left(a, 2\sqrt{x}\right) + C_2 \frac{1}{\sqrt{x^a}} \operatorname{BesselK}\left(a, 2\sqrt{x}\right)}$$

Let $C = \frac{C_2}{C_1}$ hence

$$y = x^{1+a} \frac{\frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselI}\left(1+a, 2\sqrt{x}\right) - C \frac{1}{\sqrt{x^{1+a}}} \operatorname{BesselK}\left(1+a, 2\sqrt{x}\right)}{\frac{1}{\sqrt{x^a}} \operatorname{BesselI}\left(a, 2\sqrt{x}\right) + C \frac{1}{\sqrt{x^a}} \operatorname{BesselK}\left(a, 2\sqrt{x}\right)}$$

Or

$$\begin{aligned}
y &= x^{1+a} \frac{x^{-\frac{1}{2}} \operatorname{BesselI}\left(1+a, 2\sqrt{x}\right) - C x^{-\frac{1}{2}} \operatorname{BesselK}\left(1+a, 2\sqrt{x}\right)}{\operatorname{BesselI}\left(a, 2\sqrt{x}\right) + C \operatorname{BesselK}\left(a, 2\sqrt{x}\right)} \\
&= \frac{x^{\frac{1}{2}+a} \operatorname{BesselI}\left(1+a, 2\sqrt{x}\right) - C x^{\frac{1}{2}+a} \operatorname{BesselK}\left(1+a, 2\sqrt{x}\right)}{\operatorname{BesselI}\left(a, 2\sqrt{x}\right) + C \operatorname{BesselK}\left(a, 2\sqrt{x}\right)}
\end{aligned}$$

Verification

```
eq:=diff(y(x),x)+x^(-a-1)*y(x)^2-x^a = 0;
num:=x^(1/2+a)*BesselI(1+a,2*sqrt(x))-_C1*x^(1/2+a)*BesselK(1+a,2*sqrt(x));
den:=BesselI(a,2*sqrt(x))+_C1*BesselK(a,2*sqrt(x));
my_sol:=num/den;
odetest(y(x)=my_sol,eq);
0
```

2.31 ODE No. 31

$$y'(x) - ax^n\left(y(x)^2 + 1\right) = 0$$

✓ **Mathematica** : cpu = 0.0294915 (sec), leaf count = 21

$$\left\{\left\{y(x) \to \tan\left(\frac{ax^{n+1}}{n+1} + c_1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 23

$$\left\{y(x) = \tan\left(\frac{\left(x^{n+1} + (n+1)\_C1\right)a}{n+1}\right)\right\}$$

Hand solution

$$\begin{aligned} y' - ax^n\left(y^2 + 1\right) &= 0 \\ y' &= ax^n + ax^n y^2 \\ &= P(x) + Q(x)\, y + R(x)\, y^2 \end{aligned} \tag{1}$$

This is Ricatti first order non-linear ODE. $P(x) = ax^n, Q(x) = 0, R(x) = ax^n$. But this is separable also. Hence

$$\frac{y'}{(y^2+1)} = ax^n$$
$$\frac{dy}{(y^2+1)} = ax^n dx$$

Integrating

$$\arctan\left(y(x)\right) = a\frac{x^{n+1}}{n+1} + C$$

Or

$$y(x) = \tan\left(a\frac{x^{n+1}}{n+1} + C\right)$$

Verification

```
restart;
eq:=diff(y(x),x)-a*x^n*(y(x)^2+1) = 0;
sol:=tan(a*x^(n+1)/(n+1)+_C1);
odetest(y(x)=sol,eq);
0
```

2.32 ODE No. 32

$$y'(x) + y(x)^2 \sin(x) - 2\tan(x)\sec(x) = 0$$

✓ **Mathematica** : cpu = 0.142283 (sec), leaf count = 34

$$\left\{\left\{y(x) \to \frac{\csc(x)\left(c_1 \tan(x)\sec(x) - 2\sin(x)\cos(x)\right)}{c_1 \sec(x) + \cos^2(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.279 (sec), leaf count = 28

$$\left\{y(x) = \frac{-2\left(\cos\left(x\right)\right)^3 \_C1 - 2}{\left(\left(\cos\left(x\right)\right)^3 \_C1 - 2\right)\cos\left(x\right)}\right\}$$

Hand solution

$$y' + y^2 \sin(x) - 2\frac{\sin x}{\cos^2 x} = 0$$

$$\begin{aligned} y' &= 2\frac{\sin x}{\cos^2 x} - y^2 \sin(x) \\ &= P(x) + Q(x)\, y + R(x)\, y^2 \end{aligned} \tag{1}$$

This is Ricatti first order non-linear ODE. $P(x) = 2\frac{\sin x}{\cos^2 x}, Q(x) = 0, R(x) = -\sin(x)$. A particular solution is $y_p = \frac{1}{\cos x}$, therefore the solution is

$$\begin{aligned} y &= y_p + \frac{1}{u} \\ y &= \frac{1}{\cos x} + \frac{1}{u} \end{aligned}$$

Hence

$$y' = \frac{\sin x}{\cos^2 x} - \frac{u'}{u^2}$$

Equating this to RHS of (1) gives

$$\begin{aligned} \frac{\sin x}{\cos^2 x} - \frac{u'}{u^2} &= 2\frac{\sin x}{\cos^2 x} - y^2 \sin(x) \\ &= 2\frac{\sin x}{\cos^2 x} - \left(\frac{1}{\cos x} + \frac{1}{u}\right)^2 \sin(x) \\ &= 2\frac{\sin x}{\cos^2 x} - \left(\frac{1}{\cos^2 x} + \frac{1}{u^2} + \frac{2}{u\cos x}\right)\sin(x) \end{aligned}$$

Hence

$$\begin{aligned} -\frac{u'}{u^2} &= -\frac{\sin x}{\cos^2 x} + 2\frac{\sin x}{\cos^2 x} - \frac{\sin(x)}{\cos^2 x} - \frac{\sin(x)}{u^2} - \frac{2\sin(x)}{u\cos x} \\ &= -\frac{\sin(x)}{u^2} - \frac{2\sin(x)}{u\cos x} \end{aligned}$$

Or

$$u' = \sin(x) + \frac{2u\sin(x)}{\cos x}$$
$$u' - 2u\tan(x) = \sin(x)$$

Integrating factor is $e^{-2\int \tan x dx} = e^{2\ln(\cos x)} = \cos^2(x)$. Hence the above becomes

$$d\left(u\cos^2 x\right) = \cos^2(x)\sin(x)$$

Integrating both sides

$$\begin{aligned} u\cos^2 x &= \int \cos^2(x)\sin(x)\,dx + C \\ &= \frac{-1}{3}\cos^3(x) + C \end{aligned}$$

Hence

$$u = \frac{-1}{3}\cos(x) + \frac{C}{\cos^2 x}$$

Therefore

$$\begin{aligned} y &= y_p + \frac{1}{u} \\ &= \frac{1}{\cos x} + \frac{1}{\frac{-1}{3}\cos(x) + \frac{C}{\cos^2 x}} \\ &= \frac{1}{\cos x} + \frac{3\cos^2 x}{3C - \cos^3(x)} \end{aligned}$$

Let $3C = C_1$

$$y = \frac{1}{\cos x} + \frac{3\cos^2 x}{C_2 - \cos^3(x)}$$

Verification

```
restart;
ode:=diff(y(x),x)+y(x)^2*sin(x)-2*sin(x)/cos(x)^2 = 0;
my_sol:=1/cos(x)+ 3*cos(x)^2/(_C1-cos(x)^3);
odetest(y(x)=my_sol,ode);
0
```

2.33 ODE No. 33

$$-\frac{y(x)^2 f'(x)}{g(x)}+\frac{g'(x)}{f(x)}+y'(x)=0$$

✓ **Mathematica** : cpu = 27.2779 (sec), leaf count = 157

$$\text{Solve}\left[\int_1^{y(x)}\left(\frac{1}{(f(x)K[2]+g(x))^2}-\int_1^{x}\left(\frac{2\left(K[2]^2 f(K[1])f'(K[1])-g(K[1])g'(K[1])\right)}{g(K[1])(K[2]f(K[1])+g(K[1]))^3}-\frac{2K[2]f'(K[1]\right.\right.\right.$$

✓ **Maple** : cpu = 0.544 (sec), leaf count = 58

$$\left\{y(x)=\frac{1}{(f(x))^2}\left(-f(x)\,g(x)\int\frac{\frac{\mathrm{d}}{\mathrm{d}x}f(x)}{g(x)\,(f(x))^2}\,\mathrm{d}x-g(x)\,f(x)\_C1-1\right)\left(\_C1+\int\frac{\frac{\mathrm{d}}{\mathrm{d}x}f(x)}{g(x)\,(f(x))^2}\,\mathrm{d}x\right)^{-1}\right\}$$

Hand solution

$$-\frac{f'}{g}y^2+\frac{g'}{f}+y'=0$$

$$\begin{aligned}y'&=-\frac{g'}{f}+\frac{f'}{g}y^2\\&=P(x)+Q(x)\,y+R(x)\,y^2\end{aligned}\tag{1}$$

This is Ricatti first order non-linear ODE. $P(x)=-\frac{g'}{f},Q(x)=0,R(x)=\frac{f'}{g}$.

To do.

2.34 ODE No. 34

$$f(x)y(x)^2+g(x)y(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.507831 (sec), leaf count = 51

$$\left\{\left\{y(x)\to \frac{e^{\int_1^x -g(K[1])\,dK[1]}}{c_1-\int_1^x f(K[2])\left(-e^{\int_1^{K[2]} -g(K[1])\,dK[1]}\right)\,dK[2]}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 28

$$\left\{y(x)=\frac{\mathrm{e}^{\int -g(x)\,\mathrm{d}x}}{\int \mathrm{e}^{\int -g(x)\,\mathrm{d}x} f\left(x\right)\,\mathrm{d}x+\_C1}\right\}$$

Hand solution

$$\begin{aligned} y^2 f+gy+y' &= 0 \\ y' &= -gy-y^2 f \\ &= P(x)+Q(x)\,y+R(x)\,y^2 \end{aligned} \tag{1}$$

This is Bernoulli first order non-linear ODE. $P(x)=0, Q(x)=-g, R(x)=f$. First step is to divide by y^2

$$\frac{y'}{y^2}=-g\frac{1}{y}-f \tag{2}$$

Let $u=\frac{1}{y}$, then $u'=\frac{-y'}{y^2}$ and (2) becomes

$$\begin{aligned} -u' &= -gu-f \\ u'-gu &= f \end{aligned}$$

Integrating factor is $e^{-\int g dx}$ hence

$$\begin{aligned} d\left(e^{-\int g dx}u\right) &= fe^{-\int g dx} \\ e^{-\int g dx}u &= \int fe^{-\int g dx}dx+C \\ u &= e^{\int g dx}\left(\int fe^{-\int g dx}dx+C\right) \end{aligned}$$

Hence

$$\begin{aligned} y &= \frac{1}{e^{\int g dx}\left(\int fe^{-\int g dx}+C\right)} \\ &= \frac{e^{-\int g dx}}{\int fe^{-\int g dx}dx+C} \end{aligned}$$

Let $\beta = e^{-\int g dx}$ then

$$y = \frac{\beta}{\int f \beta dx + C}$$

Verification

```
restart;
eq:=diff(y(x),x)+f(x)*y(x)^2+g(x)*y(x) = 0;
beta:=exp(-Int(g(x),x)):
my_sol:=beta/(Int(f(x)*beta,x)+_C1);
odetest(y(x)=my_sol,eq);
0
```

2.35 ODE No. 35

$$f(x)\left(2ay(x)+b+y(x)^2\right)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0575571 (sec), leaf count = 60

$$\left\{\left\{y(x)\to \sqrt{b-a^2}\tan\left(\sqrt{b-a^2}\int_1^x -f(K[1])\,dK[1]+c_1\sqrt{b-a^2}\right)-a\right\}\right\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 35

$$\left\{y(x)=\tanh\left(\sqrt{a^2-b}\left(\_C1+\int f(x)\,\mathrm{d}x\right)\right)\sqrt{a^2-b}-a\right\}$$

Hand solution

$$\begin{aligned} y'(x)+f(x)\left(2ay(x)+b+y^2(x)\right)&=0\\ y'(x)&=-2af(x)\,y(x)-bf(x)-f(x)\,y^2(x)\\ &=P(x)+Q(x)\,y+R(x)\,y^2 \end{aligned} \tag{1}$$

This is Riccati first order non-linear ODE. $P(x)=-bf(x)\,,Q(x)=-2af(x)\,,R(x)=-f(x)$.

Let

$$y(x)=-\frac{u'(x)}{u\,(x)\,R\,(x)}=\frac{u'(x)}{u\,(x)\,f\,(x)}$$

Hence

$$y'(x)=\frac{u''(x)}{u\,(x)\,f\,(x)}-\frac{\left(u'(x)\right)^2}{u^2\,(x)\,f\,(x)}-\frac{u'(x)\,f'(x)}{u\,(x)\,f^2\,(x)}$$

Equating this to RHS of (1) gives

$$\begin{aligned} \frac{u''(x)}{u\,(x)\,f\,(x)}-\frac{\left(u'(x)\right)^2}{u^2\,(x)\,f\,(x)}-\frac{u'(x)\,f'(x)}{u\,(x)\,f^2\,(x)}&=-2af(x)\,y(x)-bf(x)-f(x)\,y^2(x)\\ &=-2af(x)\left[\frac{u'(x)}{u\,(x)\,f\,(x)}\right]-bf(x)-f(x)\left[\frac{u'(x)}{u\,(x)\,f\,(x)}\right]^2\\ &=-2a\frac{u'(x)}{u\,(x)}-bf(x)-\frac{u'(x)^2}{u^2\,(x)\,f\,(x)} \end{aligned}$$

Simplifying

$$u''(x)-\frac{(u'(x))^2}{u(x)}-\frac{u'(x)f'(x)}{f(x)}=-2au'(x)f(x)-u(x)bf^2(x)-\frac{u'(x)^2}{u(x)}$$
$$u''(x)-\frac{u'(x)f'(x)}{f(x)}=-2au'(x)f(x)-u(x)bf^2(x)$$
$$u''(x)+u'(x)\left(-\frac{f'(x)}{f(x)}+2af(x)\right)+u(x)bf^2(x)=0$$

Second order ODE with variable coefficients. Since coefficients are variables and not constants, a power series method is the standard way to continue. When I tried solving this now pretending the coefficients are constants in time, using the standard auxiliary equation method, the solution did verify OK. I need to look more into this. For now, this is solved using standard method for solving second order ODE with constant coefficients.

$$u(x)=C_1\exp\left(\frac{\int f(x)\sqrt{-b}dx\left(\sqrt{\frac{b-a^2}{b}}b+a\sqrt{-b}\right)}{b}\right)+C_2\exp\left(\frac{\int f(x)\sqrt{-b}dx\left(-\sqrt{\frac{b-a^2}{b}}b+a\sqrt{-b}\right)}{b}\right)$$

Hence

$$u'(x)=\frac{C_1f(x)\sqrt{-b}}{b}\left(\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)e^{\frac{\int f(x)\sqrt{-b}\,dx}{b}\left(\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)}$$
$$+\frac{C_2f(x)\sqrt{-b}}{b}\left(-\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)e^{\frac{\int f(x)\sqrt{-b}\,dx}{b}\left(-\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)}$$

Therefore

$$y=\frac{u'(x)}{u(x)f(x)}$$
$$=\frac{\frac{C_1f(x)\sqrt{-b}}{b}\left(\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)e^{\frac{\int f(x)\sqrt{-b}\,dx}{b}\left(\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)}+\frac{C_2f(x)\sqrt{-b}}{b}\left(-\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)e^{\frac{\int f(x)\sqrt{-b}\,dx}{b}\left(-\sqrt{\frac{-a^2+b}{b}}b+\sqrt{-b}a\right)}}{f(x)\left[C_1\exp\left(\frac{\int f(x)\sqrt{-b}dx\left(\sqrt{\frac{b-a^2}{b}}b+a\sqrt{-b}\right)}{b}\right)+C_2\exp\left(\frac{\int f(x)\sqrt{-b}dx\left(-\sqrt{\frac{b-a^2}{b}}b+a\sqrt{-b}\right)}{b}\right)\right]}$$

Verification

```
restart;
book:=diff(y(x),x)+f(x)*(2*a*y(x)+b+y(x)^2)=0;
eqU:=diff(u(x),x$2)+diff(u(x),x)*(- diff(f(x),x)/f(x)+2*a*f(x))+u(x)*f(x)^2*b=0;
solU:=dsolve(eqU,u(x));
```

```
my_sol:=diff(rhs(solU),x)/(rhs(solU)*f(x));
odetest(y(x)=my_sol,book);
0
```

2.36 ODE No. 36

$$axy(x)^2 + y'(x) + y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.217917 (sec), leaf count = 195

$$\text{Solve}\left[\frac{\text{Ai}'\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right) - \left(-\frac{1}{2}\right)^{2/3}a^{2/3}x\text{Ai}\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right)}{\text{Bi}'\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right) - \left(-\frac{1}{2}\right)^{2/3}a^{2/3}x\text{Bi}\left(\frac{\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}}{y(x)} - \frac{1}{2}\sqrt[3]{-\frac{1}{2}}a^{4/3}x^2\right)} + c_1 = 0, y(x)\right]$$

✓ **Maple** : cpu = 0.098 (sec), leaf count = 62

$$\left\{y(x) = 2\frac{a}{a^2x^2 + 2\,RootOf\left(\text{Bi}\left(\_Z\right)\sqrt[3]{-2\,a^2}\_C1\,x + \sqrt[3]{-2\,a^2}x\text{Ai}\left(\_Z\right) + 2\,\text{Bi}^{(1)}\left(\_Z\right)\_C1 + 2\,\text{Ai}^{(1)}\left(\_Z\right)\right)\sqrt[3]{-}\right.$$

Hand solution

$$y'(x) = -axy^2 - y^3 \tag{1}$$

This is Abel first order non-linear. The general form is of Abel first kind is

$$y'(x) = f_0(x) + f_1(x)\,y(x) + f_2(x)\,y^2(x) + f_3(x)\,y^3(x)$$

In this case, $f_0(x) = 0, f_1(x) = 0, f_2(x) = -ax, f_3(x) = -1$. Note $\left(\frac{f_3}{f_2}\right)' = \left(\frac{1}{ax}\right)' = -\frac{1}{a}$. While Abel second kind has the form

$$(y + g(x))\,y'(x) = f_0(x) + f_1(x)\,y(x) + f_2(x)\,y^2(x)$$

For $g(x) \neq 0$.

Looking at (1) again, using the transformation suggested in Kamke $u = \frac{1}{y} - \frac{1}{2}ax^2$ or $y = \frac{1}{u+\frac{1}{2}ax^2}$Then

$$y' = \frac{-u' - ax}{\left(u + \frac{1}{2}ax^2\right)^2}$$

Equating the above to the RHS of (1) gives

$$\begin{aligned}\frac{-u' - ax}{\left(u + \frac{1}{2}ax^2\right)^2} &= -ax\left(\frac{1}{u + \frac{1}{2}ax^2}\right)^2 - \left(\frac{1}{u + \frac{1}{2}ax^2}\right)^3 \\ -u' - ax &= -ax - \frac{1}{u + \frac{1}{2}ax^2} \\ \frac{du}{dx} &= \frac{1}{u + \frac{1}{2}ax^2}\end{aligned}$$

Writing as

$$\frac{dx}{du} = u + \frac{1}{2}ax^2 \tag{2}$$

This can now be viewed as reverse Riccati in x. Using the standard transformation

$$x = -\frac{z'}{z\left(\frac{1}{2}a\right)} = -\frac{2z'}{az} \tag{3}$$

Hence

$$\frac{dx}{du} = -\frac{2}{a}\left(\frac{z''}{z} - \frac{(z')^2}{z^2}\right)$$

Equating this to RHS of (2) gives a second order Airy ODE where the dependent variable is z and the independent variable is u

$$\begin{aligned}
-\frac{2}{a}\left(\frac{z''}{z} - \frac{(z')^2}{z^2}\right) &= u + \frac{1}{2}a\left(-\frac{2z'}{az}\right)^2 \\
-\frac{2}{a}\frac{z''}{z} + \frac{2}{a}\frac{(z')^2}{z^2} &= u + \frac{1}{2}a\frac{4(z')^2}{a^2z^2} \\
-\frac{2}{a}\frac{z''}{z} + \frac{2}{a}\frac{(z')^2}{z^2} &= u + \frac{2}{a}\frac{(z')^2}{z^2} \\
-\frac{2}{a}\frac{z''}{z} &= u \\
z''(u) + \frac{a}{2}uz(u) &= 0
\end{aligned}$$

This is Airy ODE whose solution is found using power series method. The solution is

$$z(u) = C_1 \operatorname{AiryAI}\left(-\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) + C_2 \operatorname{AiryBI}\left(-\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) \tag{4}$$

We now go back to (3) and find x

$$x = -\frac{2z'}{az}$$

Since

$$\begin{aligned}
\frac{d}{du}\operatorname{AiryAI}\left(-\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) &= -\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}\operatorname{AiryAI}\left(1, -\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) \\
\frac{d}{du}\operatorname{AiryBI}\left(-\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) &= -\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}\operatorname{AiryBI}\left(1, -\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right)
\end{aligned}$$

Then

$$x = -\frac{2}{a}\frac{-C_1\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}\operatorname{AiryAI}\left(1, -\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) - C_2\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}\operatorname{AiryBI}\left(1, -\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right)}{C_1\operatorname{AiryAI}\left(-\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right) + C_2\operatorname{AiryBI}\left(-\frac{1}{2}2^{\frac{2}{3}}a^{\frac{1}{3}}u\right)}$$

Therefore $\frac{dx}{du}$ is now found from above. Once we find $\frac{dx}{du}$ then $\frac{du}{dx}$ is also found. Using $\frac{du}{dx} = \frac{1}{u+\frac{1}{2}ax^2}$ now $u(x)$ is found. Once $u(x)$ is found then $y(x)$ is found from the original transformation $y = \frac{1}{u+\frac{1}{2}ax^2}$. This is all now just algebra.

2.37 ODE No. 37

$$-ae^x y(x)^2 + y'(x) - y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.664872 (sec), leaf count = 78

$$\text{Solve}\left[-iae^x = \frac{2e^{\frac{1}{2}\left(-iae^x - \frac{i}{y(x)}\right)^2}}{2c_1 + \sqrt{2\pi}\,\text{erfi}\left(\frac{-iae^x - \frac{i}{y(x)}}{\sqrt{2}}\right)}, y(x)\right]$$

✓ **Maple** : cpu = 0.096 (sec), leaf count = 50

$$\left\{ \_C1 + \frac{1}{\mathrm{e}^x a}\mathrm{e}^{-\frac{\left(\mathrm{e}^x a + (y(x))^{-1}\right)^2}{2}} + \frac{\sqrt{2}\sqrt{\pi}}{2} Erf\left(\frac{\left(\mathrm{e}^x a + (y(x))^{-1}\right)\sqrt{2}}{2}\right) = 0 \right\}$$

2.38 ODE No. 38

$$-ay(x)^3 - bx^{3/2} + y'(x) = 0$$

✗ **Mathematica** : cpu = 8.55533 (sec), leaf count = 0 , could not solve

```
DSolve[-(b*x^(3/2)) - a*y[x]^3 + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-a*y(x)^3-b*x^(3/2) = 0,y(x))
```

2.39 ODE No. 39

$$-\mathrm{a0} - \mathrm{a1}y(x) - \mathrm{a2}y(x)^2 - \mathrm{a3}y(x)^3 + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0365061 (sec), leaf count = 54

$$\text{Solve}\left[\text{RootSum}\left[\#1^3\mathrm{a3} + \#1^2\mathrm{a2} + \#1\mathrm{a1} + \mathrm{a0}\&, \frac{\log(y(x) - \#1)}{3\#1^2\mathrm{a3} + 2\#1\mathrm{a2} + \mathrm{a1}}\&\right] = c_1 + x, y(x)\right]$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 30

$$\left\{ x - \int^{y(x)} \left(\_a^3 a3 + \_a^2 a2 + \_a\, a1 + a0\right)^{-1} d\_a + \_C1 = 0 \right\}$$

2.40 ODE No. 40

$$3ay(x)^3+6axy(x)^2+y'(x)=0$$

✓ **Mathematica** : cpu = 0.235581 (sec), leaf count = 185

$$\text{Solve}\left[\frac{\sqrt[3]{-3}\sqrt[3]{a}x\text{Ai}\left((-3)^{2/3}a^{2/3}x^2-\frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{a}y(x)}\right)+\text{Ai}'\left((-3)^{2/3}a^{2/3}x^2-\frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{a}y(x)}\right)}{\sqrt[3]{-3}\sqrt[3]{a}x\text{Bi}\left((-3)^{2/3}a^{2/3}x^2-\frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{a}y(x)}\right)+\text{Bi}'\left((-3)^{2/3}a^{2/3}x^2-\frac{(-1)^{2/3}}{\sqrt[3]{3}\sqrt[3]{a}y(x)}\right)}+c_1=0,y(x)\right]$$

✓ **Maple** : cpu = 0.083 (sec), leaf count = 48

$$\left\{y(x)=\left(3\,ax^2+RootOf\left(\text{Bi}(\_Z)\sqrt[3]{-3\,a}\_C1\,x+\sqrt[3]{-3\,a}x\text{Ai}(\_Z)+\text{Bi}^{(1)}(\_Z)\_C1+\text{Ai}^{(1)}(\_Z)\right)\sqrt[3]{-3\,a}\right)^{-1}\right\}$$

2.41 ODE No. 41

$$axy(x)^3+by(x)^2+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0790964 (sec), leaf count = 103

$$\text{Solve}\left[-\frac{b^2\left(\frac{2\tan^{-1}\left(\frac{-2axy(x)-b}{b\sqrt{-\frac{4a}{b^2}-1}}\right)}{\sqrt{-\frac{4a}{b^2}-1}}-\log\left(\frac{a(-x)y(x)(-axy(x)-b)-a}{a^2x^2y(x)^2}\right)\right)}{2a}=c_1-\frac{b^2\log(x)}{a},y(x)\right]$$

✓ **Maple** : cpu = 0.207 (sec), leaf count = 103

$$\left\{y(x)=\frac{1}{x}\text{e}^{RootOf\left(2\sqrt{b^2+4\,a}abArtanh\left(\frac{2\,a\text{e}^{-\_Z}+b}{\sqrt{b^2+4\,a}}\right)-\ln\left(x^2\left(a\text{e}^{2\,-\_Z}+b\text{e}^{-\_Z}-1\right)\right)b^2+2\_C1\,b^2+2\_Z\,b^2-4\,\ln\left(x^2\left(a\text{e}^{2\,-\_Z}+b\text{e}^{-\_Z}-1\right)\right)a+8\_C1\,a\right.}\right.$$

2.42 ODE No. 42

$$y'(x) - x(x+2)y(x)^3 - (x+3)y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.938553 (sec), leaf count = 485

$$\text{Solve}\left[c_1 = -\frac{\frac{i\sqrt{\frac{2}{\pi}}\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\left(\frac{\sinh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)}{\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}-\cosh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)\right)}{\sqrt{-i\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}} - \frac{i\sqrt{\frac{2}{\pi}}\left(\frac{x+1}{2}+\frac{1}{2}\right)\sinh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}}\right.}{\sqrt{-i\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2}}}}{\frac{i\sqrt{\frac{2}{\pi}}\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\left(i\sinh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)-\frac{i\cosh\left(\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}\right)}{\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}\right)}{\sqrt{-i\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)^2-\frac{1}{4}}}} - \frac{\sqrt{\frac{2}{\pi}}\left(\frac{x+1}{2}+\frac{1}{2}\right)\cosh\left(\sqrt{\frac{1}{2y(x)}+\right.}{\sqrt{-i\sqrt{\frac{1}{2y(x)}+\frac{1}{4}(x+1)}}}}\right]$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 40

$$\left\{ \_C1 + Artanh\left(x\sqrt{y(x)}\frac{1}{\sqrt{x(x+2)y(x)+2}}\right) + \frac{1}{2}\sqrt{x(x+2)y(x)+2}\frac{1}{\sqrt{y(x)}} = 0 \right\}$$

2.43 ODE No. 43

$$y(x)^3\left(4a^2x+3ax^2+b\right) + y'(x) + 3xy(x)^2 = 0$$

✓ **Mathematica** : cpu = 8.65201 (sec), leaf count = 490

$$\text{Solve}\left[c_1 = -\frac{i\sqrt{-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}+\frac{(-2a-3x)^2}{4a^2}}J_{\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}+1}\left(-i\sqrt{\frac{(-2a-3x)^2}{4a^2}-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}}\right)+\left(\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}+\right.}{i\sqrt{-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}+\frac{(-2a-3x)^2}{4a^2}}Y_{\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}+1}\left(-i\sqrt{\frac{(-2a-3x)^2}{4a^2}-\frac{4a^3-3b}{4a^3}-\frac{3}{2a^2y(x)}}\right)+\left(\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}+\right.}\right]$$

✓ **Maple** : cpu = 1.825 (sec), leaf count = 373

$$\left\{ \_C1 + 1\left(-K_{\frac{1}{2}\sqrt{\frac{4a^3-3b}{a^3}}+1}\left(-\frac{\sqrt{3}}{2}\sqrt{\frac{4y(x)a^2x+3ax^2y(x)+by(x)-2a}{a^3y(x)}}\right)\sqrt{3}\sqrt{\frac{4y(x)a^2x+3ax^2y(x)+by(x)}{a^3y(x)}}\right.\right.$$

2.44 ODE No. 44

$$2ax^3y(x)^3+y'(x)+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.0174886 (sec), leaf count = 72

$$\left\{\left\{y(x)\to -\frac{\sqrt{2}}{\sqrt{-2ax^2-a+2c_1e^{2x^2}}}\right\},\left\{y(x)\to \frac{\sqrt{2}}{\sqrt{-2ax^2-a+2c_1e^{2x^2}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 53

$$\left\{y(x)=-2\frac{1}{\sqrt{-4\,ax^2+4\,\mathrm{e}^{2\,x^2}\_C1-2\,a}},y(x)=2\frac{1}{\sqrt{-4\,ax^2+4\,\mathrm{e}^{2\,x^2}\_C1-2\,a}}\right\}$$

Hand solution

$$y'=-2xy-2ax^3y^3 \tag{1}$$

This is of the form $y'=f_0+f_1y+f_2y^2+f_3y^3$ where $f_0=0,f_2=0$. Hence this is Bernoulli first order non-linear ODE. We start by diving by y^3

$$\frac{y'}{y^3}=-2x\frac{1}{y^2}-2ax^3$$

Let $u=\frac{1}{y^2}$, hence $u'=-2\frac{y'}{y^3}$ and the above becomes

$$\begin{aligned}-\frac{1}{2}u'&=-2xu-2ax^3\\ u'-4xu&=4ax^3\end{aligned}$$

Integrating factor is $e^{-4\int xdx}=e^{-2x^2}$ hence

$$\frac{d}{dx}\left(e^{-2x^2}u\right)=4ax^3e^{-2x^2}$$

Integrating

$$\begin{aligned}e^{-2x^2}u&=4a\int x^3e^{-2x^2}dx+C\\ &=4a\left(\frac{-1}{8}\left(2x^2+1\right)e^{-2x^2}\right)+C\end{aligned}$$

Therefore

$$u=-\frac{1}{2}a\left(2x^2+1\right)+Ce^{2x^2}$$

Hence

$$y^2=\frac{1}{u}=\frac{1}{-\frac{1}{2}a\left(2x^2+1\right)+Ce^{2x^2}}$$

Or

$$y = \pm \frac{\sqrt{2}}{\sqrt{-a\left(2x^2+1\right)+Ce^{2x^2}}}$$

Verification

```
ode:=2*a*x^3*y(x)^3+diff(y(x),x)+2*x*y(x)=0;
my_sol:=sqrt(2)/sqrt(-a*(2*x^2+1)+_C1*exp(2*x^2));
odetest(y(x)=my_sol,ode);
0
my_sol:=-sqrt(2)/sqrt(-a*(2*x^2+1)+_C1*exp(2*x^2));
odetest(y(x)=my_sol,ode);
0
```

2.45 ODE No. 45

$$2y(x)^3\left(a^2x^3-b^2x\right)+3by(x)^2+y'(x)=0$$

✓ **Mathematica** : cpu = 0.518445 (sec), leaf count = 133

$$\text{Solve}\left[c_1=\sqrt[4]{\left(\frac{b}{ax}-\frac{1}{ax^2y(x)}\right)^2-1}\left(-\frac{\left(\frac{b}{ax}-\frac{1}{ax^2y(x)}\right)\,{}_2F_1\left(\frac{1}{2},\frac{3}{4};\frac{3}{2};\left(\frac{b}{ax}-\frac{1}{ax^2y(x)}\right)^2\right)}{2\sqrt[4]{1-\left(\frac{b}{ax}-\frac{1}{ax^2y(x)}\right)^2}}-\frac{ax}{b}\right),y(x)\right]$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 123

$$\left\{\_C1+1\sqrt[4]{\left(\frac{ax}{b}+\left(\frac{b^2y\left(x\right)}{a}-\frac{b}{ax}\right)^{-1}\right)^2-1}\left(\frac{b^2y(x)}{a}-\frac{b}{ax}\right)^{-1}\frac{1}{\sqrt{\frac{ax}{b}+\left(\frac{b^2y(x)}{a}-\frac{b}{ax}\right)^{-1}}}-\int^{\frac{ax^2y(x)}{bxy(x)-1}}1\sqrt[4]{\_a^2-\right.\right.$$

2.46 ODE No. 46

$$-x^{-a}y(x)+ax^{-a-1}-x^{-2a}-x^ay(x)^3+y'(x)+3y(x)^2=0$$

✓ **Mathematica** : cpu = 0.246205 (sec), leaf count = 258

$$\left\{\left\{y(x)\to x^{-a}-\frac{e^{-\frac{2x^{1-a}}{1-a}}}{\sqrt{c_1-\frac{2x\left(\frac{4^{\frac{a+1}{a-1}}x\left(\frac{x^{1-a}}{1-a}\right)^{\frac{2}{a-1}}\Gamma\left(-\frac{2}{a-1},-\frac{4x^{1-a}}{a-1}\right)}{a-1}+e^{\frac{4x^{1-a}}{a-1}}x^a\right)}{a+1}}}\right\},\left\{y(x)\to\frac{e^{-\frac{2}{}}}{\sqrt{c_1-\frac{2x\left(\frac{4^{\frac{a+1}{a-1}}x\left(\frac{x^{1-a}}{1-a}\right)^{\frac{2}{a-1}}}{a-\right.}\right.}}\right.\right.$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 956

$$\left\{y(x)=-1\mathrm{e}^{2\,\frac{x}{(a-1)x^a}}\frac{}{\sqrt{\_C1-2\,\frac{1}{1-a}2^{-2\,\frac{a}{1-a}-2\,(1-a)^{-1}}\left((1-a)^{-1}\right)^{-\frac{a}{1-a}-(1-a)^{-1}}\left(-\frac{(a-1)(1-a)}{(a+1)(-3+a)}2^{-3+2\,\frac{a}{1-a}+2\,(1-a)^{-}\right.}}\right.\right.$$

2.47 ODE No. 47

$$-a(x^n - x)\,y(x)^3 + y'(x) - y(x)^2 = 0$$

✗ **Mathematica** : cpu = 33.4501 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^2 - a*(-x + x^n)*y[x]^3 + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-a*(x^n-x)*y(x)^3-y(x)^2 = 0,y(x))
```

2.48 ODE No. 48

$$y(x)^3\left(-(ax^n + bx)\right) - cy(x)^2 + y'(x) = 0$$

✗ **Mathematica** : cpu = 36.7845 (sec), leaf count = 0 , could not solve

```
DSolve[-(c*y[x]^2) - (b*x + a*x^n)*y[x]^3 + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-(a*x^n+b*x)*y(x)^3-c*y(x)^2 = 0,y(x))
```

2.49 ODE No. 49

$$ay(x)^3\phi'(x) + \frac{(2a+1)y(x)\phi''(x)}{\phi'(x)} + 6a\phi(x)y(x)^2 + 2a + y'(x) + 2 = 0$$

✗ **Mathematica** : cpu = 29.1971 (sec), leaf count = 0 , could not solve

```
DSolve[2 + 2*a + 6*a*phi[x]*y[x]^2 + a*y[x]^3*Derivative[1][phi][x] + Derivative[1][y][x] +
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)+a*diff(phi(x),x)*y(x)^3+6*a*phi(x)*y(x)^2+(2*a+1)*y(x)*diff(diff(phi(x),
```

2.50 ODE No. 50

$$-\mathrm{f0}(x) - \mathrm{f1}(x)y(x) - \mathrm{f2}(x)y(x)^2 - \mathrm{f3}(x)y(x)^3 + y'(x) = 0$$

✗ **Mathematica** : cpu = 132.694 (sec), leaf count = 0 , could not solve

```
DSolve[-f0[x] - f1[x]*y[x] - f2[x]*y[x]^2 - f3[x]*y[x]^3 + Derivative[1][y][x] == 0, y[x], x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-f3(x)*y(x)^3-f2(x)*y(x)^2-f1(x)*y(x)-f0(x) = 0,y(x))
```

2.51 ODE No. 51

$$-h(x)(y(x)-f(x))(y(x)-g(x))\left(y(x)-\frac{af(x)+bg(x)}{a+b}\right)-\frac{f'(x)(y(x)-g(x))}{f(x)-g(x)}-\frac{(y(x)-f(x))g'(x)}{g(x)-f(x)}+y'(x)=0$$

✓ **Mathematica** : cpu = 0.741986 (sec), leaf count = 354

$$\text{Solve}\left[-\frac{1}{3}(a-b)^{2/3}(2a+b)^{2/3}(a+2b)^{2/3}\text{RootSum}\left[\#1^3(a-b)^{2/3}(2a+b)^{2/3}(a+2b)^{2/3}-3\#1a^2-3\#1ab-3\#\right.\right.$$

✓ **Maple** : cpu = 0.217 (sec), leaf count = 237

$$\left\{y(x)=\frac{1}{9\,a^3+18\,a^2b+18\,ab^2+9\,b^3}\left(2\,(f(x)-g(x))\,(b/2+a)\,(a+2\,b)\,(a-b)\,RootOf\left(-27\int^{\_Z}\frac{}{(2\,\_a\,a^2-\_\right.\right.\right.$$

2.52 ODE No. 52

$$-ay(x)^n-bx^{\frac{n}{1-n}}+y'(x)=0$$

✓ **Mathematica** : cpu = 144.8 (sec), leaf count = 115

$$\text{Solve}\left[\int_1^{y(x)\left(\frac{ax^{-\frac{n}{1-n}}}{b}\right)^{\frac{1}{n}}}\frac{1}{-K[1]\left(\frac{(-1)^n(n-1)^{-n}b^{1-n}}{a}\right)^{\frac{1}{n}}+K[1]^n+1}\,dK[1]=\int_1^x bK[2]^{\frac{n}{1-n}}\left(\frac{aK[2]^{-\frac{n}{1-n}}}{b}\right)^{\frac{1}{n}}\,dK[2]-\right.$$

✓ **Maple** : cpu = 0.205 (sec), leaf count = 61

$$\left\{-\int_{\_b}^{y(x)}1x^{\frac{n}{n-1}}\left((ax(n-1)\,\_a^n+\_a)\,x^{\frac{n}{n-1}}+b(n-1)\,x\right)^{-1}\mathrm{d}\_a(n-1)+\ln(x)-\_C1=0\right\}$$

2.53 ODE No. 53

$$f(x)^{1-n}g'(x)y(x)^n\left(-(ag(x)+b)^{-n}\right)-\frac{y(x)f'(x)}{f(x)}-f(x)g'(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 79.5196 (sec), leaf count = 95

$$\text{Solve}\left[\int_1^{y(x)\left(f(x)^{-n}(ag(x)+b)^{-n}\right)^{\frac{1}{n}}}\frac{1}{-\left(a^n\right)^{\frac{1}{n}}K[1]+K[1]^n+1}\,dK[1]=\frac{f(x)(ag(x)+b)\log(ag(x)+b)\left(f(x)^{-n}(ag(x)\right.}{a}\right.$$

✓ **Maple** : cpu = 0.062 (sec), leaf count = 281

$$\left\{y(x)=\frac{f(x)\left(ag(x)+b\right)}{a}RootOf\left(-\int^{\_Z}\frac{\left((f\right.}{\_a\left(\left(f\left(x\right)\right)^{1-n}\left(\frac{\mathrm{d}}{\mathrm{d}x}g\left(x\right)\right)\left(ag\left(x\right)+b\right)^{-n}\right)^{-n-1}\left(f\left(x\right)\frac{\mathrm{d}}{\mathrm{d}x}g\left(x\right)\right)^{-2n+1}\left(\right.}\right.$$

2.54 ODE No. 54

$$-a^nf(x)^{1-n}g'(x)y(x)^n-\frac{y(x)f'(x)}{f(x)}-f(x)g'(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.116803 (sec), leaf count = 74

$$\text{Solve}\left[y(x)\left(a^nf(x)^{-n}\right)^{\frac{1}{n}}\,{}_2F_1\left(1,\frac{1}{n};1+\frac{1}{n};-\left(\left(a^nf(x)^{-n}\right)^{\frac{1}{n}}y(x)\right)^n\right)=f(x)g(x)\left(a^nf(x)^{-n}\right)^{\frac{1}{n}}+c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.159 (sec), leaf count = 38

$$\left\{\frac{ay(x)}{nf\left(x\right)}LerchPhi\left(-\left(\frac{ay(x)}{f\left(x\right)}\right)^n,1,n^{-1}\right)-ag(x)+\_C1=0\right\}$$

2.55 ODE No. 55

$$-f(x)y(x)^n-g(x)y(x)-h(x)+y'(x)=0$$

✗ **Mathematica** : cpu = 4.08967 (sec), leaf count = 0 , could not solve

```
DSolve[-h[x] - g[x]*y[x] - f[x]*y[x]^n + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-f(x)*y(x)^n-g(x)*y(x)-h(x) = 0,y(x))
```

2.56 ODE No. 56

$$-f(x)y(x)^a - g(x)y(x)^b + y'(x) = 0$$

✗ **Mathematica** : cpu = 2.32207 (sec), leaf count = 0 , could not solve

```
DSolve[-(f[x]*y[x]^a) - g[x]*y[x]^b + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-f(x)*y(x)^a-g(x)*y(x)^b = 0,y(x))
```

2.57 ODE No. 57

$$y'(x) - \sqrt{|y(x)|} = 0$$

✓ **Mathematica** : cpu = 98.5807 (sec), leaf count = 283

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{2\ 2^{3/4}(1-\#1)\sqrt[4]{|\Im(\#1)|+i(1-\Re(\#1))}(i|\Im(\#1)|-\Re(\#1)+1)\ {}_2F_1\left(\frac{1}{4},\frac{3}{4};\frac{7}{4};\frac{2|\Im}{3\sqrt[4]{|\Im(\#1)|}\,(\Im(\#1)^2+(1-\Re(\#1))^2)}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.071 (sec), leaf count = 31

$$\left\{x - \begin{cases} -2\sqrt{-y(x)} & y(x) \le 0 \\ 2\sqrt{y(x)} & 0 < y(x) \end{cases} + \_C1 = 0\right\}$$

2.58 ODE No. 58

$$a\left(-\sqrt{y(x)}\right) - bx + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.154549 (sec), leaf count = 119

$$\text{Solve}\left[\frac{a^2\left(-\log\left(a^2\left(\sqrt{\frac{a^2y(x)}{b^2x^2}}+1\right)-\frac{2a^2y(x)}{bx^2}\right)-\frac{2a\tanh^{-1}\left(\frac{a^2-4b\sqrt{\frac{a^2y(x)}{b^2x^2}}}{a\sqrt{a^2+8b}}\right)}{\sqrt{a^2+8b}}\right)}{2b} = \frac{a^2\log(x)}{b} + c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.071 (sec), leaf count = 68

$$\left\{-\frac{1}{2}\ln\left(\sqrt{y\left(x\right)}ax+bx^{2}-2\,y(x)\right)+a\sqrt{y\left(x\right)}Artanh\left(1\left(a\sqrt{y\left(x\right)}+2\,bx\right)\frac{1}{\sqrt{y\left(x\right)\left(a^{2}+8\,b\right)}}\right)\frac{1}{\sqrt{y\left(x\right)\left(a^{2}+8\,b\right)}}\right.$$

2.59 ODE No. 59

$$a\left(-\sqrt{y(x)^2+1}\right)-b+y'(x)=0$$

✓ **Mathematica** : cpu = 0.181155 (sec), leaf count = 96

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[\frac{b\tan^{-1}\left(\frac{\#1b}{\sqrt{\#1^2+1\sqrt{a^2-b^2}}}\right)}{\sqrt{a^2-b^2}}-\frac{b\tan^{-1}\left(\frac{\#1a}{\sqrt{a^2-b^2}}\right)}{\sqrt{a^2-b^2}}+\sinh^{-1}(\#1)}{a}\&\right][c_1+x]\right\}\right\}$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 26

$$\left\{x-\int^{y(x)}\left(a\sqrt{\_a^2+1}+b\right)^{-1}d\_a+\_C1=0\right\}$$

2.60 ODE No. 60

$$y'(x)-\frac{\sqrt{y(x)^2-1}}{\sqrt{x^2-1}}=0$$

✓ **Mathematica** : cpu = 0.0494219 (sec), leaf count = 55

$$\left\{\left\{y(x)\to\frac{1}{2}\left(-e^{-c_1}\sqrt{x^2-1}+e^{c_1}\sqrt{x^2-1}+e^{-c_1}x+e^{c_1}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 29

$$\left\{\ln\left(x+\sqrt{x^2-1}\right)-\ln\left(y(x)+\sqrt{\left(y\left(x\right)\right)^2-1}\right)+\_C1=0\right\}$$

Hand solution

$$y'=\pm\frac{\sqrt{y^2-1}}{\sqrt{x^2-1}} \tag{1}$$

Separable. For the positive case

$$\begin{aligned}\frac{dy}{dx}\frac{1}{\sqrt{y^2-1}} &= \frac{1}{\sqrt{x^2-1}} \\ \frac{dy}{(y^2-1)^{\frac{1}{2}}} &= \frac{dx}{(x^2-1)^{\frac{1}{2}}}\end{aligned}$$

Integrating

$$\int \frac{dy}{(y^2-1)^{\frac{1}{2}}} = \int \frac{dx}{(x^2-1)^{\frac{1}{2}}} + C$$

But $\int \frac{dy}{(y^2-1)^{\frac{1}{2}}} = \tanh^{-1} \frac{y}{(y^2-1)^{\frac{1}{2}}} = \ln\left(y + \sqrt{y^2-1}\right)$, hence

$$\ln\left(y + \sqrt{y^2-1}\right) = \ln\left(x + \sqrt{x^2-1}\right) + C$$

For the negative case

$$\begin{aligned}\frac{dy}{dx}\frac{1}{\sqrt{y^2-1}} &= -\frac{1}{\sqrt{x^2-1}} \\ \frac{dy}{(y^2-1)^{\frac{1}{2}}} &= -\frac{dx}{(x^2-1)^{\frac{1}{2}}}\end{aligned}$$

Integrating

$$\int \frac{dy}{(y^2-1)^{\frac{1}{2}}} = -\int \frac{dx}{(x^2-1)^{\frac{1}{2}}} + C$$

But $\int \frac{dy}{(y^2-1)^{\frac{1}{2}}} = \tanh^{-1} \frac{y}{(y^2-1)^{\frac{1}{2}}} = \ln\left(y + \sqrt{y^2-1}\right)$, hence

$$\ln\left(y + \sqrt{y^2-1}\right) = -\ln\left(x + \sqrt{x^2-1}\right) + C$$

Therefore

$$\ln\left(y + \sqrt{y^2-1}\right) = \pm\ln\left(x + \sqrt{x^2-1}\right) + C$$

2.61 ODE No. 61

$$y'(x) - \frac{\sqrt{x^2-1}}{\sqrt{y(x)^2-1}} = 0$$

✓ **Mathematica** : cpu = 0.177118 (sec), leaf count = 75

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{1}{2}\#1\sqrt{\#1^2-1} - \frac{1}{2}\log\left(\sqrt{\#1^2-1}+\#1\right)\&\right]\left[c_1 + \frac{1}{2}\sqrt{x^2-1}x - \frac{1}{2}\log\left(\sqrt{x^2-1}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 50

$$\left\{\_C1 + x\sqrt{x^2-1} - \ln\left(x+\sqrt{x^2-1}\right) - y(x)\sqrt{(y(x))^2-1} + \ln\left(y(x)+\sqrt{(y(x))^2-1}\right) = 0\right\}$$

2.62 ODE No. 62

$$y'(x) - \frac{y(x) - x^2\sqrt{x^2-y(x)^2}}{xy(x)\sqrt{x^2-y(x)^2}+x} = 0$$

✓ **Mathematica** : cpu = 3.83883 (sec), leaf count = 40

$$\text{Solve}\left[\tan^{-1}\left(\frac{y(x)}{\sqrt{x^2-y(x)^2}}\right) + \frac{x^2}{2} + \frac{y(x)^2}{2} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.412 (sec), leaf count = 34

$$\left\{\frac{(y(x))^2}{2} + \arctan\left(y(x)\frac{1}{\sqrt{x^2-(y(x))^2}}\right) + \frac{x^2}{2} - \_C1 = 0\right\}$$

Hand solution

$$y' = \frac{y - x^2\sqrt{x^2-y^2}}{xy\sqrt{x^2-y^2}+x} \tag{1}$$

Let $y = ux$ then $y' = u + xu'$ therefore

$$\begin{aligned} u + xu' &= \frac{y - x^2\sqrt{x^2 - y^2}}{xy\sqrt{x^2 - y^2} + x} \\ &= \frac{ux - x^2\sqrt{x^2 - (ux)^2}}{x\,(ux)\sqrt{x^2 - (ux)^2} + x} \\ &= \frac{ux - x^3\sqrt{1 - u^2}}{x^3u\sqrt{1 - u^2} + x} \\ &= \frac{u - x^2\sqrt{1 - u^2}}{x^2u\sqrt{1 - u^2} + 1} \end{aligned}$$

Hence

$$\begin{aligned} u\left(x^2u\sqrt{1 - u^2} + 1\right) + xu'\left(x^2u\sqrt{1 - u^2} + 1\right) &= u - x^2\sqrt{1 - u^2} \\ x^2u^2\sqrt{1 - u^2} + u + u'\left(x^3u\sqrt{1 - u^2} + x\right) &= u - x^2\sqrt{1 - u^2} \\ x^2u^2\sqrt{1 - u^2} + u'\left(x^3u\sqrt{1 - u^2} + x\right) &= -x^2\sqrt{1 - u^2} \\ xu^2\sqrt{1 - u^2} + u'\left(x^2u\sqrt{1 - u^2} + 1\right) &= -x\sqrt{1 - u^2} \\ xu^2 + u'\left(x^2u + \frac{1}{\sqrt{1 - u^2}}\right) &= -x \\ x\left(1 + u^2\right) + u'\left(x^2u + \frac{1}{\sqrt{1 - u^2}}\right) &= 0 \end{aligned}$$

Hence

$$x\left(1 + u^2\right)dx + \left(x^2u + \frac{1}{\sqrt{1 - u^2}}\right)du = 0 \tag{2}$$

Let $M = x\left(1 + u^2\right), N = \left(x^2u + \frac{1}{\sqrt{1 - u^2}}\right)$.

$$\begin{aligned} \frac{\partial M}{\partial u} &= 2xu \\ \frac{\partial N}{\partial x} &= 2xu \end{aligned}$$

Therefore (2) is exact. Let

$$x\left(1 + u^2\right)dx + \left(x^2u + \frac{1}{\sqrt{1 - u^2}}\right)du = dU$$

Since $dU = \frac{\partial U}{\partial x}dx + \frac{\partial U}{\partial u}du$. Comparing with the above, we see that

$$\frac{\partial U}{\partial x} = x\left(1 + u^2\right) \tag{3}$$

$$\frac{\partial U}{\partial u} = x^2u + \frac{1}{\sqrt{1 - u^2}} \tag{4}$$

From (3)

$$\begin{aligned} U &= \int x(1+u^2)\,dx \\ &= \frac{x^2}{2}(1+u^2) + f(u) \end{aligned} \tag{5}$$

From (4)

$$\begin{aligned} \frac{d}{\partial u}\left(\frac{x^2}{2}(1+u^2) + f(u)\right) &= x^2u + \frac{1}{\sqrt{1-u^2}} \\ x^2u + f'(u) &= x^2u + \frac{1}{\sqrt{1-u^2}} \\ f'(u) &= \frac{1}{\sqrt{1-u^2}} \end{aligned}$$

Therefore

$$f(u) = \arcsin(u)$$

From (5) we find

$$U(x,u) = \frac{x^2}{2}(1+u^2) + \arcsin(u)$$

Since $dU = 0$ then

$$\begin{aligned} \frac{x^2}{2}(1+u^2) + \arcsin(u) &= C \\ \frac{x^2}{2}(1+u^2) + \arcsin(u) - C &= 0 \end{aligned}$$

Since $y = ux$ then the above can be written as

$$\begin{aligned} \frac{x^2}{2}\left(1 + \left(\frac{y}{x}\right)^2\right) + \arcsin\left(\frac{y}{x}\right) - C &= 0 \\ \frac{x^2}{2}\left(\frac{x^2+y^2}{x^2}\right) + \arcsin\left(\frac{y}{x}\right) - C &= 0 \\ \frac{1}{2}(x^2+y^2) + \arcsin\left(\frac{y}{x}\right) - C &= 0 \\ \arcsin\left(\frac{y}{x}\right) &= C - \frac{1}{2}(x^2+y^2) \end{aligned}$$

Hence

$$\begin{aligned} \frac{y}{x} &= \sin\left(C - \frac{1}{2}(x^2+y^2)\right) \\ y(x) &= x\sin\left(C - \frac{1}{2}(x^2+y^2)\right) \end{aligned}$$

2.63 ODE No. 63

$$y'(x) - \frac{y(x)^2+1}{(x+1)^{3/2}\left|y(x)+\sqrt{y(x)+1}\right|} = 0$$

✗ **Mathematica** : cpu = 300.005 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.141 (sec), leaf count = 35

$$\left\{-2\frac{1}{\sqrt{1+x}} - \int^{y(x)} \frac{1}{\_a^2+1}\left|\_a+\sqrt{\_a+1}\right| d\_a + \_C1 = 0\right\}$$

2.64 ODE No. 64

$$y'(x) - \sqrt{\frac{ay(x)^2+by(x)+c}{ax^2+bx+c}} = 0$$

✓ **Mathematica** : cpu = 0.176566 (sec), leaf count = 269

$$\left\{\left\{y(x) \to \frac{e^{-\sqrt{a}c_1}\left(8a^{3/2}ce^{2\sqrt{a}c_1}\sqrt{ax^2+bx+c} - 8a^{3/2}c\sqrt{ax^2+bx+c} + 8a^2cxe^{2\sqrt{a}c_1} + 8a^2cx + 2b^3e^{\sqrt{a}c_1} - b^3e^{2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 124

$$\left\{-1\sqrt{\frac{a\left(y\left(x\right)\right)^2+by\left(x\right)+c}{ax^2+bx+c}}\sqrt{ax^2+bx+c}\ln\left(\frac{1}{2}\left(2\sqrt{ax^2+bx+c}\sqrt{a}+2ax+b\right)\frac{1}{\sqrt{a}}\right)\frac{1}{\sqrt{a\left(y\left(x\right)\right)^2+by\left(x\right)+}}\right.$$

2.65 ODE No. 65

$$y'(x) - \sqrt{\frac{y(x)^3+1}{x^3+1}} = 0$$

✓ **Mathematica** : cpu = 1.49643 (sec), leaf count = 312

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{i(\#1+1)\sqrt{1+\frac{6i}{\left(\sqrt{3}-3i\right)(\#1+1)}}\sqrt{\frac{2}{3}-\frac{4i}{\left(\sqrt{3}+3i\right)(\#1+1)}}F\left(i\sinh^{-1}\left(\frac{\sqrt{-\frac{6i}{3i+\sqrt{3}}}}{\sqrt{\#1+1}}\right)\middle|\frac{3i+\sqrt{3}}{3i-\sqrt{3}}\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 47

$$\left\{\int^{y(x)} \frac{1}{\sqrt{\_a^3+1}} d\_a + \int^{x} -1 \sqrt{\frac{(y(x))^3+1}{\_a^3+1}} \frac{1}{\sqrt{(y(x))^3+1}} d\_a + \_C1 = 0\right\}$$

2.66 ODE No. 66

$$y'(x) - \frac{\sqrt{|(1-y(x))y(x)(1-ay(x))|}}{\sqrt{|(1-x)x(1-ax)|}} = 0$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.07 (sec), leaf count = 40

$$\left\{\int \frac{1}{\sqrt{|x(x-1)(ax-1)|}} \mathrm{d}x - \int^{y(x)} \frac{1}{\sqrt{|\_a(\_a-1)(\_a a-1)|}} d\_a + \_C1 = 0\right\}$$

2.67 ODE No. 67

$$y'(x) - \frac{\sqrt{1-y(x)^4}}{\sqrt{1-x^4}} = 0$$

✓ **Mathematica** : cpu = 0.170109 (sec), leaf count = 14

$$\{\{y(x) \to \mathrm{sn}\left(c_1 + F\left(\sin^{-1}(x)\middle|-1\right)\middle|-1\right)\}\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 51

$$\left\{EllipticF(x,i)\sqrt{-x^2+1}\sqrt{x^2+1}\frac{1}{\sqrt{-x^4+1}} - \int^{y(x)} \frac{1}{\sqrt{-\_a^4+1}} d\_a + \_C1 = 0\right\}$$

2.68 ODE No. 68

$$y'(x) - \sqrt{\frac{ay(x)^4 + by(x)^2 + 1}{ax^4 + bx^2 + 1}} = 0$$

✓ **Mathematica** : cpu = 0.837201 (sec), leaf count = 373

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{i\sqrt{\frac{2\#1^2a+\sqrt{b^2-4a}+b}{\sqrt{b^2-4a}+b}}\sqrt{\frac{2\#1^2a}{b-\sqrt{b^2-4a}}+1}F\left(i\sinh^{-1}\left(\sqrt{2}\sqrt{\frac{a}{b+\sqrt{b^2-4a}}}\#1\right)|\frac{b+\sqrt{b^2-4a}}{b-\sqrt{b^2-4a}}\right)}{\sqrt{2}\sqrt{\frac{a}{\sqrt{b^2-4a}+b}}\sqrt{\#1^4a+\#1^2b+1}}\&\right.\right.\right.$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 77

$$\left\{\int^{y(x)} \frac{1}{\sqrt{\_a^4a + \_a^2b + 1}}d\_a + \int^{x} -1\sqrt{\frac{a\left(y\left(x\right)\right)^4 + b\left(y\left(x\right)\right)^2 + 1}{\_a^4a + \_a^2b + 1}}\frac{1}{\sqrt{a\left(y\left(x\right)\right)^4 + b\left(y\left(x\right)\right)^2 + 1}}d\_a + \_C1 = 0\right.$$

2.69 ODE No. 69

$$y'(x) - \sqrt{(\mathrm{a0} + \mathrm{a1}x + \mathrm{a2}x^2 + \mathrm{a3}x^3 + \mathrm{a4}x^4)\left(\mathrm{b0} + \mathrm{b1}y(x) + \mathrm{b2}y(x)^2 + \mathrm{b3}y(x)^3 + \mathrm{b4}y(x)^4\right)} = 0$$

✓ **Mathematica** : cpu = 52.577 (sec), leaf count = 12750

too large to display

✓ **Maple** : cpu = 0.146 (sec), leaf count = 111

$$\left\{\int^{y(x)} \frac{1}{\sqrt{\_a^4b4 + \_a^3b3 + \_a^2b2 + \_a\,b1 + b0}}d\_a + \int^{x} -1\sqrt{\left(b4\ \left(y\left(x\right)\right)^4 + b3\ \left(y\left(x\right)\right)^3 + b2\ \left(y\left(x\right)\right)^2 + b1\right.}\right.$$

2.70 ODE No. 70

$$y'(x) - \sqrt{\frac{\mathrm{a0} + \mathrm{a1}x + \mathrm{a2}x^2 + \mathrm{a3}x^3 + \mathrm{a4}x^4}{\mathrm{b0} + \mathrm{b1}y(x) + \mathrm{b2}y(x)^2 + \mathrm{b3}y(x)^3 + \mathrm{b4}y(x)^4}} = 0$$

✓ **Mathematica** : cpu = 158.63 (sec), leaf count = 23353

too large to display

✓ **Maple** : cpu = 0.163 (sec), leaf count = 113

$$\left\{\int^{y(x)} \sqrt{\_a^4b4 + \_a^3b3 + \_a^2b2 + \_a\,b1 + b0}d\_a + \int^{x} -\sqrt{\frac{\_a^4a4 + \_a^3a3 + \_a^2a2 + \_a\,a1 + a0}{b4\ \left(y\left(x\right)\right)^4 + b3\ \left(y\left(x\right)\right)^3 + b2\ \left(y\left(x\right)\right)^2 + b1\ y(}}\right.$$

2.71 ODE No. 71

$$y'(x)-\sqrt{\frac{\text{b0}+\text{b1}y(x)+\text{b2}y(x)^2+\text{b3}y(x)^3+\text{b4}y(x)^4}{\text{a0}+\text{a1}x+\text{a2}x^2+\text{a3}x^3+\text{a4}x^4}}=0$$

✓ **Mathematica** : cpu = 2.3145 (sec), leaf count = 2237

$$\text{Solve}\left[-\frac{2F\left(\sin^{-1}\left(\sqrt{\frac{(\text{Root}\left[\text{b4}\#1^4+\text{b3}\#1^3+\text{b2}\#1^2+\text{b1}\#1+\text{b0}\&,2\right]-\text{Root}\left[\text{b4}\#1^4+\text{b3}\#1^3+\text{b2}\#1^2+\text{b1}\#1+\text{b0}\&,4\right])(y(x)-\text{Root}\left[\text{b4}\#1\right.}{(\text{Root}\left[\text{b4}\#1^4+\text{b3}\#1^3+\text{b2}\#1^2+\text{b1}\#1+\text{b0}\&,1\right]-\text{Root}\left[\text{b4}\#1^4+\text{b3}\#1^3+\text{b2}\#1^2+\text{b1}\#1+\text{b0}\&,4\right])(y(x)-\text{Root}\left[\text{b4}\#1\right.}\right)\right.\right.\right.$$

✓ **Maple** : cpu = 0.13 (sec), leaf count = 113

$$\left\{\int^{y(x)}\frac{1}{\sqrt{\_a^4 b4+\_a^3 b3+\_a^2 b2+\_a\, b1+b0}}d\_a+\int^{x}-1\sqrt{\frac{b4\ (y\,(x))^4+b3\ (y\,(x))^3+b2\ (y\,(x))^2+b1\ y}{\_a^4 a4+\_a^3 a3+\_a^2 a2+\_a\, a1+a}}\right.$$

2.72 ODE No. 72

$$y'(x)-\text{R1}\left(x,\sqrt{\text{a0}+\text{a1}x+\text{a2}x^2+\text{a3}x^3+\text{a4}x^4}\right)\text{R2}\left(y(x),\sqrt{\text{b0}+\text{b1}y(x)+\text{b2}y(x)^2+\text{b3}y(x)^3+\text{b4}y(x)^4}\right)=0$$

✓ **Mathematica** : cpu = 0.820994 (sec), leaf count = 87

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[\int_1^{\#1}\frac{1}{\text{R2}\left(K[1],\sqrt{\text{b1}K[1]+\text{b2}K[1]^2+\text{b3}K[1]^3+\text{b4}K[1]^4+\text{b0}}\right)}dK[1]\&\right]\left[\int_1^{x}\text{R1}\right.\right.\right.$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 64

$$\left\{\int R1\left(x,\sqrt{a4\ x^4+a3\ x^3+a2\ x^2+a1\ x+a0}\right)\,\text{d}x-\int^{y(x)}\left(R2\left(\_a,\sqrt{\_a^4 b4+\_a^3 b3+\_a^2 b2+\_a\, b1+b}\right.\right.\right.$$

2.73 ODE No. 73

$$y'(x) - \left(\frac{\text{a0} + \text{a1}x + \text{a2}x^2 + \text{a3}x^3}{\text{a0} + \text{a1}y(x) + \text{a2}y(x)^2 + \text{a3}y(x)^3}\right)^{2/3} = 0$$

✓ **Mathematica** : cpu = 1.00632 (sec), leaf count = 733

$$\text{Solve}\left[\frac{3(\text{a0} + y(x)(\text{a1} + y(x)(\text{a2} + \text{a3}y(x))))^{2/3}\left(y(x) - \text{Root}\left[\#1^3\text{a3} + \#1^2\text{a2} + \#1\text{a1} + \text{a0}\&, 1\right]\right) F_1\left(\frac{5}{3}; -\frac{2}{3}, -\frac{2}{3};\right.}{5\left(\frac{y(x) - \text{Root}\left[\#1^3\text{a3}+\#1^2\text{a2}+\#1\text{a1}+\text{a0}\&,2\right]}{\text{Root}\left[\#1^3\text{a3}+\#1^2\text{a2}+\#1\text{a1}+\text{a0}\&,1\right] - \text{Root}\left[\#1^3\text{a3}+\#1^2\text{a2}+\#1\text{a1}+\right.}$$

✓ **Maple** : cpu = 0.349 (sec), leaf count = 91

$$\left\{\int^{y(x)} \left(\_a^3 a3 + \_a^2 a2 + \_a\, a1 + a0\right)^{\frac{2}{3}} d\_a + \int^{x} -\left(\frac{\_a^3 a3 + \_a^2 a2 + \_a\, a1 + a0}{a3\ (y(x))^3 + a2\ (y(x))^2 + a1\, y(x) + a0}\right)^{\frac{2}{3}} \left(a3\,(y(x))\right.$$

2.74 ODE No. 74

$$y'(x) - f(x)(y(x) - g(x))\sqrt{(y(x) - a)(y(x) - b)} = 0$$

✗ **Mathematica** : cpu = 2.98944 (sec), leaf count = 0 , could not solve

```
DSolve[-(f[x]*Sqrt[(-a + y[x])*(-b + y[x])]*(-g[x] + y[x])) + Derivative[1][y][x] == 0, y[x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-f(x)*(y(x)-g(x))*((y(x)-a)*(y(x)-b))^(1/2) = 0,y(x))
```

2.75 ODE No. 75

$$y'(x) - e^{x - y(x)} + e^x = 0$$

✓ **Mathematica** : cpu = 0.0485493 (sec), leaf count = 18

$$\left\{\left\{y(x) \to \log\left(e^{c_1 - e^x} + 1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.132 (sec), leaf count = 20

$$\left\{y(x) = -\mathrm{e}^x + \ln\left(-1 + \mathrm{e}^{\mathrm{e}^x + \_C1}\right) - \_C1\right\}$$

Hand solution

$$\begin{aligned} y' &= e^{x-y} - e^x \\ y' &= e^x\left(e^{-y}-1\right) \\ \frac{1}{e^{-y}-1}dy &= e^x dx \end{aligned} \tag{1}$$

Integrating both sides. $\int \frac{1}{e^{-y}-1}dy$. Let $e^{-y}=u$, then $\frac{du}{dy} = -e^{-y} = -u$. Hence $dy = -\frac{du}{u}$, therefore the integral becomes

$$\int \frac{1}{u-1}\left(-\frac{du}{u}\right) = -\int \frac{1}{u\left(u-1\right)}du$$

But $\frac{1}{u(u-1)} = -\left(\frac{1}{u} - \frac{1}{u-1}\right)$, hence

$$\begin{aligned} -\int \frac{1}{u\left(u-1\right)}du &= \int \left(\frac{1}{u} - \frac{1}{u-1}\right)du \\ &= \ln u - \ln\left(u-1\right) \\ &= \ln e^{-y} - \ln\left(e^{-y}-1\right) \\ &= -\left(\ln\left(e^{-y}-1\right) - \ln e^{-y}\right) \end{aligned}$$

But $\ln x - \ln y = \ln\left(\frac{x}{y}\right)$ and the above becomes

$$\begin{aligned} \int \frac{1}{e^{-y}-1}dy &= -\left[\ln\left(\frac{e^{-y}-1}{e^{-y}}\right)\right] \\ &= -\ln\left(1-e^{y}\right) \end{aligned}$$

Back to (1), when we integrate both sides, and since $\int e^x dx = e^x + C$

$$\begin{aligned} -\ln\left(1-e^y\right) &= e^x + C \\ \ln\left(1-e^y\right) &= -e^x + C_1 \end{aligned}$$

Hence

$$\begin{aligned} 1-e^y &= \exp\left(-e^x + C_1\right) \\ e^y &= 1 - \exp\left(-e^x + C_1\right) \end{aligned}$$

Taking logs

$$y = \ln\left(1-\exp\left(-e^x + C_1\right)\right)$$

Let $e^{C_1} = C_2$ then

$$y = \ln\left(1 - C_2 e^{-e^x}\right)$$

Verification

```
ode:=diff(y(x),x)=exp(x-y(x))-exp(x);
my_sol:=log(1-_C1*exp(-exp(x)));
odetest(y(x)=my_sol,ode);
0
```

2.76 ODE No. 76

$$-a\cos(y(x))+b+y'(x)=0$$

✓ **Mathematica** : cpu = 0.209702 (sec), leaf count = 116

$$\left\{\left\{y(x)\to 2\tan^{-1}\left(\frac{a\tanh\left(\frac{1}{2}\left(x\sqrt{(a-b)(a+b)}-c_1\sqrt{(a-b)(a+b)}\right)\right)}{\sqrt{(a-b)(a+b)}}-\frac{b\tanh\left(\frac{1}{2}\left(x\sqrt{(a-b)(a+b)}-c_1\sqrt{}\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 41

$$\left\{y(x)=2\arctan\left(\frac{\tanh\left(1/2\sqrt{a^2-b^2}(x+\_C1)\right)\sqrt{a^2-b^2}}{a+b}\right)\right\}$$

Hand solution

$$y'=a\cos y+b$$

This is separable.

$$\frac{dy}{a\cos y+b}=dx$$
$$\int\frac{dy}{a\cos y+b}=x+C \tag{1}$$

Using standard Tangent half-angle substitution, let $t=\tan\frac{y}{2},\cos y=\frac{1-t^2}{1+t^2},dy=\frac{2}{1+t^2}dt$, then the integral becomes

$$\begin{aligned}\int\frac{dy}{a\cos y+b}&=\int\frac{2}{1+t^2}\frac{1}{\left(a\frac{1-t^2}{1+t^2}+b\right)}dt\\&=2\int\frac{1+t^2}{(1+t^2)\left(a\left(1-t^2\right)+b\left(1+t^2\right)\right)}dt\\&=2\int\frac{dt}{a-at^2+b+bt^2}\\&=2\int\frac{dt}{(a+b)+t^2\left(b-a\right)}\\&=2\int\frac{dt}{(a+b)\left(1+\frac{t^2(b-a)}{(a+b)}\right)}\\&=\frac{2}{a+b}\int\frac{dt}{\left(1+\frac{t^2(b-a)}{(a+b)}\right)}\end{aligned}$$

Let $z^2 = \frac{t^2(b-a)}{(a+b)}$, or $z = \frac{t\sqrt{b-a}}{\sqrt{a+b}}$, then $\frac{dz}{dt} = \frac{\sqrt{b-a}}{\sqrt{a+b}}$ and the above integral becomes

$$\begin{aligned}
\frac{2}{a+b}\int \frac{dt}{\left(1+\frac{t^2(b-a)}{(a+b)}\right)} &= \frac{2}{a+b}\int \frac{\sqrt{a+b}}{\sqrt{b-a}}\frac{dz}{(1+z^2)} \\
&= \frac{2}{a+b}\frac{\sqrt{a+b}}{\sqrt{b-a}}\int \frac{dz}{(1+z^2)} \\
&= \frac{2}{\sqrt{a+b}}\frac{1}{\sqrt{b-a}}\int \frac{dz}{(1+z^2)} \\
&= \frac{2}{\sqrt{(a+b)(b-a)}}\int \frac{dz}{(1+z^2)} \\
&= \frac{2}{\sqrt{b^2-a^2}}\int \frac{dz}{(1+z^2)}
\end{aligned}$$

Now, $\int \frac{dz}{(1+z^2)} = \arctan(z)$, hence

$$\begin{aligned}
\frac{2}{\sqrt{b^2-a^2}}\int \frac{dz}{(1+z^2)} &= \frac{2}{\sqrt{b^2-a^2}}\arctan(z) \\
&= \frac{2}{\sqrt{b^2-a^2}}\arctan\left(\frac{t\sqrt{b-a}}{\sqrt{a+b}}\right)
\end{aligned}$$

But $t = \tan\frac{y}{2}$ therefore

$$\frac{2}{\sqrt{b^2-a^2}}\arctan\left(\frac{t\sqrt{b-a}}{\sqrt{a+b}}\right) = \frac{2}{\sqrt{b^2-a^2}}\arctan\left(\frac{\tan\left(\frac{y}{2}\right)\sqrt{b-a}}{\sqrt{a+b}}\right)$$

Going back to (1)

$$\int \frac{dy}{a\cos y+b} = x+C$$

$$\frac{2}{\sqrt{b^2-a^2}}\arctan\left(\frac{\tan\left(\frac{y}{2}\right)\sqrt{b-a}}{\sqrt{a+b}}\right) = x+C$$

$$\arctan\left(\frac{\tan\left(\frac{y}{2}\right)\sqrt{b-a}}{\sqrt{a+b}}\right) = \frac{1}{2}\sqrt{b^2-a^2}(x+C)$$

$$\frac{\tan\left(\frac{y}{2}\right)\sqrt{b-a}}{\sqrt{a+b}} = \tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)$$

$$\tan\left(\frac{y}{2}\right) = \frac{\sqrt{a+b}}{\sqrt{b-a}}\tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)$$

$$\begin{aligned}\frac{y}{2} &= \arctan\left(\frac{(a+b)}{\sqrt{(a+b)(b-a)}}\tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)\right)\\ &= \arctan\left(\frac{(a+b)}{\sqrt{b^2-a^2}}\tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)\right)\end{aligned}$$

$$y = 2\arctan\left(\frac{a+b}{\sqrt{b^2-a^2}}\tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)\right)$$

Verification

```
ode:=diff(y(x),x)=a*cos(y(x))+b;
my_sol:=2*arctan( (a+b)/sqrt(b^2-a^2) * tan(1/2*sqrt(b^2-a^2)*(x+_C1)));
odetest(y(x)=my_sol,ode);
0
```

2.77 ODE No. 77

$$y'(x) - \cos(ay(x) + bx) = 0$$

✓ **Mathematica** : cpu = 0.315428 (sec), leaf count = 124

$$\left\{\left\{y(x) \to \frac{-2\tan^{-1}\left(\frac{a\tanh\left(\frac{1}{2}\left(c_1\sqrt{a^2-b^2}-x\sqrt{a^2-b^2}\right)\right)}{\sqrt{a^2-b^2}} + \frac{b\tanh\left(\frac{1}{2}\left(c_1\sqrt{a^2-b^2}-x\sqrt{a^2-b^2}\right)\right)}{\sqrt{a^2-b^2}}\right) - bx}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.068 (sec), leaf count = 54

$$\left\{y(x) = \frac{1}{a}\left(-bx + 2\arctan\left(\frac{\tanh\left(1/2\sqrt{a^2-b^2}(x - \_C1)\right)\sqrt{a^2-b^2}}{a-b}\right)\right)\right\}$$

Hand solution

$$y' = \cos(ay + bx)$$

This is separable after transformation of $u = ay + bx$, hence $u' = ay' + b$ or $y' = \frac{1}{a}(u' - b)$. Therefore the above becomes

$$\begin{aligned}\frac{1}{a}(u' - b) &= \cos(u)\\ u' &= a\cos u + b\\ \frac{du}{a\cos u + b} &= dx\end{aligned}$$

This is the same as Kamke 76 (the problem before this), which we solved using half angle tan transformation, and the answer is

$$u = 2\arctan\left(\frac{a+b}{\sqrt{b^2-a^2}}\tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)\right)$$

Since $u = ay + bx$ then $y = \frac{u-bx}{a}$, hence

$$y = \frac{1}{a}\left(2\arctan\left(\frac{a+b}{\sqrt{b^2-a^2}}\tan\left(\frac{1}{2}\sqrt{b^2-a^2}(x+C)\right)\right) - bx\right)$$

Verification

```
ode:=diff(y(x),x)=cos(a*y(x)+b*x);
my_sol:=(1/a)*(2*arctan( (a+b)/sqrt(b^2-a^2) * tan(1/2*sqrt(b^2-a^2)*(x+_C1)))-b*x);
odetest(y(x)=my_sol,ode);
0
```

2.78 ODE No. 78

$$a\sin(\alpha y(x)+\beta x)+b+y'(x)=0$$

✓ **Mathematica** : cpu = 0.830646 (sec), leaf count = 1317

$$\left\{\left\{y(x)\to 2\tan^{-1}\left(\frac{a^2\sqrt{-(a\alpha+b\alpha-\beta)(a\alpha-b\alpha+\beta)}\tan\left(\frac{1}{2}\left(\frac{a^2x\alpha^2}{\sqrt{-(a\alpha+b\alpha-\beta)(a\alpha-b\alpha+\beta)}}-\frac{b^2x\alpha^2}{\sqrt{-(a\alpha+b\alpha-\beta)(a\alpha-b\alpha+\beta)}}-\frac{a^2c_1\alpha^2}{\sqrt{-(a\alpha+b\alpha-\beta)(a\alpha-b\alpha+\beta)}}+\right.\right.\right.\right.$$

✓ **Maple** : cpu = 2.176 (sec), leaf count = 89

$$\left\{y(x)=\frac{1}{\alpha}\left(-\beta\,x+2\,\arctan\left(\frac{-\tan\left(1/2\,\sqrt{(-a^2+b^2)\,\alpha^2-2\,\alpha\,b\beta+\beta^2}(x-\_C1)\right)\sqrt{(-a^2+b^2)\,\alpha^2-2\,\alpha\,b\beta+}\right.\right.\right.$$

Hand solution

$$y'=-a\sin(\alpha y+\beta x)-b$$

This is separable after transformation of $u=\alpha y+\beta x$, hence $u'=\alpha y'+\beta$ or $y'=\frac{1}{\alpha}(u'-\beta)$. Therefore the above becomes

$$\begin{aligned}\frac{1}{\alpha}(u'-\beta)&=-a\sin(u)-b\\ u'&=-\alpha(a\sin(u)+b)+\beta\\ \frac{du}{\beta-\alpha(a\sin(u)+b)}&=dx\end{aligned}\tag{1}$$

Using half angle tan transformation where $\tan\left(\frac{u}{2}\right)=t, \sin(u)=\frac{2t}{t^2+1}, du=\frac{2}{1+t^2}dt$ then

$$\begin{aligned}
\int \frac{du}{\beta-\alpha\left(a\sin(u)+b\right)} &= \int \frac{2}{1+t^2}\frac{dt}{\beta-\alpha\left(a\frac{2t}{t^2+1}+b\right)} \\
&= 2\int \frac{dt}{\beta\left(t^2+1\right)-\alpha\left(a2t+b\left(t^2+1\right)\right)} \\
&= 2\int \frac{dt}{t\beta^2+\beta-\left(\alpha a2t+t^2\alpha b+\alpha b\right)} \\
&= 2\int \frac{dt}{\left(\beta-\alpha b\right)\left(\frac{t\beta^2-\alpha a2t-t^2\alpha b}{(\beta-\alpha b)}+1\right)} \\
&= \frac{2}{(\beta-\alpha b)}\int \frac{dt}{\frac{t\beta^2-\alpha a2t-t^2\alpha b}{(\beta-\alpha b)}+1} \\
&= \frac{2}{(\beta-\alpha b)}\frac{-(\alpha b-\beta)}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\tanh^{-1}\left(\frac{\left(t+\frac{a\alpha}{b\alpha-\beta}\right)(b\alpha-\beta)}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\right) \\
&= \frac{2}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\tanh^{-1}\left(\frac{t(b\alpha-\beta)+a\alpha}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\right)
\end{aligned}$$

But $t=\tan\left(\frac{u}{2}\right)$ therefore

$$\int \frac{du}{\beta-\alpha\left(a\sin(u)+b\right)} = \frac{2}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\tanh^{-1}\left(\frac{\tan\left(\frac{u}{2}\right)(b\alpha-\beta)+a\alpha}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\right)$$

But $u=\alpha y+\beta x$, and the above becomes

$$\int \frac{du}{\beta-\alpha\left(a\sin(u)+b\right)} = \frac{2\tanh^{-1}\left(\frac{\tan\left(\frac{\alpha y+\beta x}{2}\right)(b\alpha-\beta)+a\alpha}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\right)}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}$$

Back to (1), therefore after integrating both sides

$$\frac{2\tanh^{-1}\left(\frac{\tan\left(\frac{\alpha y+\beta x}{2}\right)(b\alpha-\beta)+a\alpha}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}}\right)}{\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}} = x+C$$

Let

$$A=\sqrt{\alpha^2a^2-\left(\alpha^2b^2+\beta^2-2\alpha b\beta\right)}$$

Then

$$\tanh^{-1}\left(\frac{\tan\left(\frac{\alpha y+\beta x}{2}\right)(b\alpha-\beta)+a\alpha}{A}\right)=\frac{1}{2}A(x+C)$$

$$\frac{\tan\left(\frac{\alpha y+\beta x}{2}\right)(b\alpha-\beta)+a\alpha}{A}=\tanh\left(\frac{1}{2}A(x+C)\right)$$

$$\tan\left(\frac{\alpha y+\beta x}{2}\right)(b\alpha-\beta)+a\alpha=A\tanh\left(\frac{1}{2}A(x+C)\right)$$

$$\tan\left(\frac{\alpha y+\beta x}{2}\right)=\frac{A}{(b\alpha-\beta)}\tanh\left(\frac{1}{2}A(x+C)\right)-\frac{a\alpha}{(b\alpha-\beta)}$$

$$\frac{\alpha y+\beta x}{2}=\arctan\left(\frac{A}{(b\alpha-\beta)}\tanh\left(\frac{1}{2}A(x+C)\right)-\frac{a\alpha}{(b\alpha-\beta)}\right)$$

$$y=\frac{2}{\alpha}\arctan\left(\frac{A}{(b\alpha-\beta)}\tanh\left(\frac{1}{2}A(x+C)\right)-\frac{a\alpha}{(b\alpha-\beta)}\right)-\frac{\beta x}{\alpha}$$

Verification

```
ode:=diff(y(x),x)=-a*sin(alpha*y(x)+beta*x)-b;
A0:=sqrt(alpha^2*a^2-(alpha^2*b^2+beta^2-2*alpha*b*beta));
B0:=(alpha*b-beta);
my_sol:=2/alpha*arctan(A0/B0*tanh((1/2)*A0*(x+_C1))-a*alpha/(B0))-beta*x/alpha;
odetest(y(x)=my_sol,ode);
0
```

2.79 ODE No. 79

$$f(x)\cos(ay(x)) + g(x)\sin(ay(x)) + h(x) + y'(x) = 0$$

✗ **Mathematica** : cpu = 25.2582 (sec), leaf count = 0 , could not solve

```
DSolve[Cos[a*y[x]]*f[x] + h[x] + g[x]*Sin[a*y[x]] + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)+f(x)*cos(a*y(x))+g(x)*sin(a*y(x))+h(x) = 0,y(x))
```

2.80 ODE No. 80

$$(1 - f'(x))\cos(y(x)) - f'(x) + f(x)\sin(y(x)) + y'(x) - 1 = 0$$

✗ **Mathematica** : cpu = 23.8384 (sec), leaf count = 0 , could not solve

```
DSolve[-1 + f[x]*Sin[y[x]] + Cos[y[x]]*(1 - Derivative[1][f][x]) - Derivative[1][f][x] + Der
```

✓ **Maple** : cpu = 1.497 (sec), leaf count = 41

$$\left\{y(x) = 2\arctan\left(\frac{-e^{\int f(x)\,dx} + \int e^{\int f(x)\,dx}\,dx f(x) + f(x)\_C1}{\_C1 + \int e^{\int f(x)\,dx}\,dx}\right)\right\}$$

2.81 ODE No. 81

$$y'(x) + 2\tan(x)\tan(y(x)) - 1 = 0$$

✗ **Mathematica** : cpu = 43.3467 (sec), leaf count = 0 , could not solve

```
DSolve[-1 + 2*Tan[x]*Tan[y[x]] + Derivative[1][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.296 (sec), leaf count = 78

$$\left\{\_C1 + \tan(x)\frac{1}{\sqrt[4]{\frac{\left(1+(\tan(y(x)))^2\right)\left(1+(\tan(x))^2\right)}{(\tan(y(x))\tan(x)-1)^2}}} + \frac{\tan(y(x)) + \tan(x)}{2\tan(y(x))\tan(x) - 2}{}_2\mathrm{F}_1\left(\frac{1}{2}, \frac{5}{4}; \frac{3}{2}; -\frac{(\tan(y(x)) + \tan(x))^2}{(\tan(y(x))\tan(x) - 1)}\right.\right.$$

2.82 ODE No. 82

$$-a\left(\tan^2(y(x))+1\right)+y'(x)+\tan(x)\tan(y(x))=0$$

✗ **Mathematica** : cpu = 49.9558 (sec), leaf count = 0 , could not solve

```
DSolve[Tan[x]*Tan[y[x]] - a*(1 + Tan[y[x]]^2) + Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-a*(1+tan(y(x))^2)+tan(y(x))*tan(x) = 0,y(x))
```

2.83 ODE No. 83

$$y'(x)-\tan(xy(x))=0$$

✗ **Mathematica** : cpu = 40.398 (sec), leaf count = 0 , could not solve

```
DSolve[-Tan[x*y[x]] + Derivative[1][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.449 (sec), leaf count = 44

$$\left\{y(x)=-iRootOf\left(-Erf\left(\frac{(-x+\_Z)\sqrt{2}}{2}\right)\sqrt{\pi}-\sqrt{\pi}Erf\left(\frac{\sqrt{2}(x+\_Z)}{2}\right)+\sqrt{2}\_C1\right)\right\}$$

2.84 ODE No. 84

$$y'(x)-f(ax+by(x))=0$$

✓ **Mathematica** : cpu = 8.73091 (sec), leaf count = 244

$$\text{Solve}\left[\int_1^{y(x)}-\frac{bf(bK[2]+ax)\left(\int_1^x\left(\frac{b^2f'(aK[1]+bK[2])}{bf(aK[1]+bK[2])+a}-\frac{b^3f(aK[1]+bK[2])f'(aK[1]+bK[2])}{(bf(aK[1]+bK[2])+a)^2}\right)dK[1]\right)+a\int_1^x\left(\frac{b^2f'(aK[1]+\right.}{bf(bK[2]+ax)+a}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 37

$$\left\{y(x)=\frac{RootOf\left(\int^Z(f(\_a\,b)\,b+a)^{-1}\,d\_ab-x+\_C1\right)b-ax}{b}\right\}$$

2.85 ODE No. 85

$$y'(x) - x^{a-1} y(x)^{1-b} f\left(\frac{x^a}{a} + \frac{y(x)^b}{b}\right) = 0$$

✓ **Mathematica** : cpu = 155.858 (sec), leaf count = 235

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \left(\frac{K[1]^{a-1} K[2]^{b-1} f'\left(\frac{K[1]^a}{a} + \frac{K[2]^b}{b}\right)}{f\left(\frac{K[1]^a}{a} + \frac{K[2]^b}{b}\right) + 1} - \frac{K[1]^{a-1} K[2]^{b-1} f\left(\frac{K[1]^a}{a} + \frac{K[2]^b}{b}\right) f'\left(\frac{K[1]^a}{a} + \frac{K[2]^b}{b}\right)}{\left(f\left(\frac{K[1]^a}{a} + \frac{K[2]^b}{b}\right) + 1\right)^2}\right)\right.\right.$$

✓ **Maple** : cpu = 0.468 (sec), leaf count = 153

$$\left\{y(x) = \sqrt[b]{-\frac{1}{a}\left(-RootOf\left(\int^{-Z}\left(\left(\sqrt[b]{-b+\_a}\right)^{-b}\left(\sqrt[a]{a}\right)^a f\left(\frac{\left(\sqrt[a]{a}\right)^a b + \left(\sqrt[b]{-b+\_a}\right)^b a}{ab}\right)\_a - \left(\sqrt[b]{-b+\_a}\right)\right.\right.\right.\right.$$

2.86 ODE No. 86

$$y'(x) - \frac{y(x) - x f\left(a y(x)^2 + x^2\right)}{a y(x) f\left(a y(x)^2 + x^2\right) + x} = 0$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.499 (sec), leaf count = 52

$$\left\{1 \arctan\left(x\sqrt{a}\frac{1}{\sqrt{a^2 \left(y\left(x\right)\right)^2}}\right)\frac{1}{\sqrt{a}} - \frac{1}{2}\int^{(y(x))^2 + \frac{x^2}{a}} \frac{f(\_a\, a)}{\_a} d\_a - \_C1 = 0\right\}$$

2.87 ODE No. 87

$$y'(x) - \frac{c x^a y(x)^b + a y(x) f\left(x^c y(x)\right)}{b x f\left(x^c y(x)\right) - x^a y(x)^b} = 0$$

✗ **Mathematica** : cpu = 15.3651 (sec), leaf count = 0 , could not solve

```
DSolve[-((a*f[x^c*y[x]]*y[x] + c*x^a*y[x]^b)/(b*x*f[x^c*y[x]] - x^a*y[x]^b)) + Derivative[1]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)-(y(x)*a*f(x^c*y(x))+c*x^a*y(x)^b)/(x*b*f(x^c*y(x))-x^a*y(x)^b) = 0,y(x))
```

2.88 ODE No. 88

$$-ce^{-2ax} - 4ay(x) - b + 2y'(x) - 3y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.28252 (sec), leaf count = 2831

$$\left\{\left\{y(x) \to -\frac{2\left(-2^{-\frac{a\sqrt{4a^2-3b}-2a^2}{a^2}+\frac{\sqrt{4a^4-3a^2b}}{a^2}+1}3^{\frac{a\sqrt{4a^2-3b}-2a^2}{4a^2}-\frac{\sqrt{4a^4-3a^2b}}{4a^2}}a^{-\frac{a\sqrt{4a^2-3b}-2a^2}{2a^2}+\frac{\sqrt{4a^4-3a^2b}}{2a^2}+1}b^{\frac{a\sqrt{4a^2-3b}-2a^2}{4a^2}-\sqrt{}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.233 (sec), leaf count = 256

$$\left\{y(x) = 1\left(-\mathrm{e}^{-ax}\sqrt{3}\left(Y_{-\frac{1}{2a}\left(\sqrt{4a^2-3b}-2a\right)}\left(\frac{\mathrm{e}^{-ax}\sqrt{3}}{2a}\sqrt{c}\right)\_C1 + J_{-\frac{1}{2a}\left(\sqrt{4a^2-3b}-2a\right)}\left(\frac{\mathrm{e}^{-ax}\sqrt{3}}{2a}\sqrt{c}\right)\right)\sqrt{c} - \left(\sqrt{4\right.\right.\right.\right.$$

2.89 ODE No. 89

$$xy'(x) - \sqrt{a^2 - x^2} = 0$$

✓ **Mathematica** : cpu = 0.0318571 (sec), leaf count = 48

$$\left\{\left\{y(x) \to \sqrt{a^2 - x^2} - a\log\left(a\sqrt{a^2 - x^2} + a^2\right) + a\log(x) + c_1\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 56

$$\left\{y(x) = \sqrt{a^2 - x^2} - a^2\ln\left(\frac{1}{x}\left(2a^2 + 2\sqrt{a^2}\sqrt{a^2 - x^2}\right)\right)\frac{1}{\sqrt{a^2}} + \_C1\right\}$$

2.90 ODE No. 90

$$xy'(x) + y(x) - x\sin(x) = 0$$

✓ **Mathematica** : cpu = 0.0146305 (sec), leaf count = 24

$$\left\{\left\{y(x) \to \frac{c_1}{x} + \frac{\sin(x) - x\cos(x)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 17

$$\left\{y(x) = \frac{\sin(x) - \cos(x)x + \_C1}{x}\right\}$$

2.91 ODE No. 91

$$xy'(x) - y(x) - \frac{x}{\log(x)} = 0$$

✓ **Mathematica** : cpu = 0.00725559 (sec), leaf count = 15

$$\{\{y(x) \to c_1 x + x \log(\log(x))\}\}$$

✓ **Maple** : cpu = 0.006 (sec), leaf count = 11

$$\{y(x) = (\ln(\ln(x)) + \_C1)\, x\}$$

2.92 ODE No. 92

$$x^2(-\sin(x)) + xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0144808 (sec), leaf count = 15

$$\{\{y(x) \to c_1 x - x \cos(x)\}\}$$

✓ **Maple** : cpu = 0.005 (sec), leaf count = 12

$$\{y(x) = x(\_C1 - \cos(x))\}$$

2.93 ODE No. 93

$$xy'(x) - y(x) - \frac{x \cos(\log(\log(x)))}{\log(x)} = 0$$

✓ **Mathematica** : cpu = 0.0201989 (sec), leaf count = 16

$$\{\{y(x) \to c_1 x + x \sin(\log(\log(x)))\}\}$$

✓ **Maple** : cpu = 0.015 (sec), leaf count = 12

$$\{y(x) = x(\sin(\ln(\ln(x))) + \_C1)\}$$

2.94 ODE No. 94

$$ay(x) + bx^n + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0154967 (sec), leaf count = 25

$$\left\{\left\{y(x) \to c_1 x^{-a} - \frac{bx^n}{a+n}\right\}\right\}$$

✓ **Maple** : cpu = 0.009 (sec), leaf count = 23

$$\left\{y(x) = -\frac{bx^n}{n+a} + x^{-a}\_C1\right\}$$

2.95 ODE No. 95

$$x^2 + xy'(x) + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0158567 (sec), leaf count = 32

$$\left\{\left\{y(x) \to \frac{x(-c_1 J_1(x) - Y_1(x))}{c_1 J_0(x) + Y_0(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.068 (sec), leaf count = 27

$$\left\{y(x) = -\frac{(\_C1\, Y_1(x) + J_1(x))\, x}{\_C1\, Y_0(x) + J_0(x)}\right\}$$

2.96 ODE No. 96

$$xy'(x) - y(x)^2 + 1 = 0$$

✓ **Mathematica** : cpu = 0.0238185 (sec), leaf count = 33

$$\left\{\left\{y(x) \to \frac{1 - e^{2c_1} x^2}{e^{2c_1} x^2 + 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 11

$$\{y(x) = -\tanh(\ln(x) + \_C1)\}$$

2.97 ODE No. 97

$$ay(x)^2 + bx^2 + xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0275994 (sec), leaf count = 46

$$\left\{\left\{y(x) \to -\frac{\sqrt{b}x \tan\left(\sqrt{a}\sqrt{b}x - \sqrt{a}\sqrt{b}c_1\right)}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 25

$$\left\{y(x) = -\frac{x}{a}\tan\left(\sqrt{ab}(x + \_C1)\right)\sqrt{ab}\right\}$$

2.98 ODE No. 98

$$ay(x)^2 + cx^{2b} - by(x) + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0257224 (sec), leaf count = 442

$$\left\{\left\{y(x) \to -\frac{\sqrt{-a}\sqrt{-c}x^b\left(\frac{\sqrt{\frac{2}{\pi}}c_1 \sin\left(\frac{\sqrt{-a}\sqrt{-c}x^b}{b}\right)}{\sqrt{\frac{\sqrt{-a}\sqrt{-c}x^b}{b}}} - \frac{2\sqrt{\frac{2}{\pi}}\cos\left(\frac{\sqrt{-a}\sqrt{-c}x^b}{b}\right)}{\sqrt{\frac{\sqrt{-a}\sqrt{-c}x^b}{b}}} - \frac{\sqrt{\frac{2}{\pi}}c_1\left(-\sin\left(\frac{\sqrt{-a}\sqrt{-c}x^b}{b}\right) - \frac{\sqrt{-a}b\sqrt{-c}x^{-b}\cos\left(\frac{\sqrt{-}}{ac}\right.\right.\right.\right.}{\sqrt{\frac{\sqrt{-a}\sqrt{-c}x^b}{b}}}}{2a\left(\frac{\sqrt{\frac{2}{\pi}}\sin\left(\frac{\sqrt{-a}\sqrt{-c}x^b}{b}\right)}{\sqrt{\frac{\sqrt{-a}\sqrt{-c}x^b}{b}}} + \frac{\sqrt{\frac{2}{\pi}}c_1\cos\left(\frac{\sqrt{-a}\sqrt{-c}x^b}{b}\right)}{\sqrt{\frac{\sqrt{-a}\sqrt{-c}x^b}{b}}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 38

$$\left\{y(x) = -\frac{1}{x^{-b}}\tan\left(\frac{1}{b}\left(x^b\sqrt{c}\sqrt{a} + \_C1\, b\right)\right)\sqrt{c}\frac{1}{\sqrt{a}}\right\}$$

2.99 ODE No. 99

$$ay(x)^2 - by(x) - cx^\beta + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0186201 (sec), leaf count = 244

$$\left\{\left\{y(x) \to -\frac{\sqrt{-a}\sqrt{c}x^{\beta/2}\left(-2J_{\frac{b}{\beta}-1}\left(\frac{2\sqrt{-a}\sqrt{c}x^{\beta/2}}{\beta}\right) + c_1 J_{1-\frac{b}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{c}x^{\beta/2}}{\beta}\right) - c_1 J_{-\frac{b+\beta}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{c}x^{\beta/2}}{\beta}\right)\right) - bc_1 J_{-\frac{b}{\beta}}\left(\right.\right.\right.$$
$$\left.\left.\left.2a\left(J_{\frac{b}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{c}x^{\beta/2}}{\beta}\right) + c_1 J_{-\frac{b}{\beta}}\left(\frac{2\sqrt{-a}\sqrt{c}x^{\beta/2}}{\beta}\right)\right)\right.\right.$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 171

$$\left\{y(x) = \frac{1}{a}\left(-\left(Y_{\frac{b+\beta}{\beta}}\left(2\frac{\sqrt{-ac}x^{\beta/2}}{\beta}\right)\_C1 + J_{\frac{b+\beta}{\beta}}\left(2\frac{\sqrt{-ac}x^{\beta/2}}{\beta}\right)\right)\sqrt{-ac}x^{\frac{\beta}{2}} + b\left(Y_{\frac{b}{\beta}}\left(2\frac{\sqrt{-ac}x^{\beta/2}}{\beta}\right)\_C1 + J_{\frac{b}{\beta}}\right.\right.\right.$$

2.100 ODE No. 100

$$a + xy'(x) + xy(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.00910829 (sec), leaf count = 157

$$\left\{\left\{y(x) \to -\frac{c_1 J_1\left(2i\sqrt{-a}\sqrt{x}\right) + i\sqrt{-a}\sqrt{x}\left(c_1 J_0\left(2i\sqrt{-a}\sqrt{x}\right) - c_1 J_2\left(2i\sqrt{-a}\sqrt{x}\right) - 2J_0\left(2i\sqrt{-a}\sqrt{x}\right)\right)}{2x\left(J_1\left(2i\sqrt{-a}\sqrt{x}\right) - c_1 J_1\left(2i\sqrt{-a}\sqrt{x}\right)\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.08 (sec), leaf count = 59

$$\left\{y(x) = 1\sqrt{a}\left(J_0\left(2\sqrt{a}\sqrt{x}\right)\_C1 + Y_0\left(2\sqrt{a}\sqrt{x}\right)\right)\frac{1}{\sqrt{x}}\left(\_C1\, J_1\left(2\sqrt{a}\sqrt{x}\right) + Y_1\left(2\sqrt{a}\sqrt{x}\right)\right)^{-1}\right\}$$

2.101 ODE No. 101

$$xy'(x) + xy(x)^2 - y(x) = 0$$

✓ **Mathematica** : cpu = 0.00990953 (sec), leaf count = 18

$$\left\{\left\{y(x) \to \frac{2x}{2c_1 + x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 16

$$\left\{y(x) = 2\frac{x}{x^2 + 2\_C1}\right\}$$

2.102 ODE No. 102

$$-ax^3 + xy'(x) + xy(x)^2 - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0202862 (sec), leaf count = 36

$$\left\{\left\{y(x) \to \sqrt{a}x \tanh\left(\frac{1}{2}\left(2\sqrt{a}c_1 + \sqrt{a}x^2\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 22

$$\left\{y(x) = \tanh\left(\frac{x^2 + 2\_C1}{2}\sqrt{a}\right)x\sqrt{a}\right\}$$

2.103 ODE No. 103

$$-x^3 - \left(2x^2 + 1\right)y(x) + xy'(x) + xy(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.100959 (sec), leaf count = 90

$$\left\{\left\{y(x) \to \frac{x\left(e^{2\sqrt{2}c_1} - \sqrt{2}e^{2\sqrt{2}c_1} + e^{\sqrt{2}x^2} + \sqrt{2}e^{\sqrt{2}x^2}\right)}{e^{2\sqrt{2}c_1} + e^{\sqrt{2}x^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 29

$$\left\{y(x) = \frac{\sqrt{2}x}{2}\left(\sqrt{2} + 2\tanh\left(1/2\left(x^2 + 2\_C1\right)\sqrt{2}\right)\right)\right\}$$

2.104 ODE No. 104

$$axy(x)^2 + bx + xy'(x) + 2y(x) = 0$$

✓ **Mathematica** : cpu = 0.0175414 (sec), leaf count = 43

$$\left\{\left\{y(x) \to -\sqrt{\frac{b}{a}}\tan\left(ax\sqrt{\frac{b}{a}} - c_1\right) - \frac{1}{ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.093 (sec), leaf count = 63

$$\left\{y(x) = -\frac{1}{a}\left(-\frac{1}{x}\left(i\sqrt{a}\sqrt{b}x - 1\right) + 1\mathrm{e}^{-2\,ix\sqrt{a}\sqrt{b}}\left(\_C1 - \frac{i}{2}\mathrm{e}^{-2\,ix\sqrt{a}\sqrt{b}}\frac{1}{\sqrt{a}}\frac{1}{\sqrt{b}}\right)^{-1}\right)\right\}$$

2.105 ODE No. 105

$$axy(x)^2 + by(x) + cx + d + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.184994 (sec), leaf count = 473

$$\left\{\left\{y(x) \to \frac{c_1\left(i\sqrt{a}e^{-i\sqrt{a}\sqrt{c}x}\left(b(-\sqrt{c}) - i\sqrt{a}d\right)U\left(1 - \frac{-\sqrt{c}b - i\sqrt{a}d}{2\sqrt{c}}, b+1, 2i\sqrt{a}\sqrt{c}x\right) - i\sqrt{a}\sqrt{c}e^{-i\sqrt{a}\sqrt{c}x}U\left(-\frac{-\sqrt{c}b-}{2\sqrt{}}\right.\right.}{a\left(c_1 e^{-i\sqrt{a}\sqrt{c}x}U\left(-\frac{-\sqrt{c}b - i\sqrt{a}d}{2\sqrt{c}}, b, 2i\right.\right.}\right.\right.$$

✓ **Maple** : cpu = 0.337 (sec), leaf count = 844

$$\left\{y(x) = -4\,c^2\left(-1/4\_C1\,\left(a^3c^2d^2 + a^2b^2c^3 - 2\,(-ac)^{3/2}\,abcd - 2\,(-ac)^{5/2}\,bd\right)U\left(1/2\,\frac{(-ac)^{3/2}\,d + c(2\,\sqrt{-ac}d}{c^2a}\right.\right.\right.$$

2.106 ODE No. 106

$$\frac{1}{2}(a-b)y(x) + x^a y(x)^2 + x^b + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0376181 (sec), leaf count = 40

$$\left\{\left\{y(x) \to -x^{\frac{b-a}{2}}\tan\left(\frac{2x^{\frac{a+b}{2}}}{a+b} - c_1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 41

$$\left\{y(x) = -1\tan\left(\frac{1}{a+b}\left(2\,x^{a/2+b/2} + \_C1\,(a+b)\right)\right)\left(x^{\frac{a}{2}-\frac{b}{2}}\right)^{-1}\right\}$$

2.107 ODE No. 107

$$ax^\alpha y(x)^2 + by(x) - cx^\beta + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.259862 (sec), leaf count = 1415

$$\left\{\left\{y(x) \to \frac{x^{1-\alpha}\left((-1)^{\frac{\alpha-b}{\alpha+\beta}}a^{\frac{\alpha-b}{\alpha+\beta}+\frac{1}{2}\left(\frac{b}{\alpha+\beta}-\frac{\alpha}{\alpha+\beta}\right)}(\alpha+\beta)^{\frac{\alpha}{\alpha+\beta}-\frac{b}{\alpha+\beta}+1}\left(\alpha^2+2\beta\alpha+\beta^2\right)^{-\frac{\alpha-b}{\alpha+\beta}}\left(\frac{\alpha-b}{\alpha+\beta}+\frac{1}{2}\left(\frac{b}{\alpha+\beta}-\frac{\alpha}{\alpha+\beta}\right)\right.\right.}{}\right.\right.$$

✓ **Maple** : cpu = 0.239 (sec), leaf count = 174

$$\left\{y(x)=-\frac{x^{1-\alpha}}{ax}\left(Y_{\frac{b+\beta}{\alpha+\beta}}\left(2\,\frac{\sqrt{-ac}x^{\alpha/2+\beta/2}}{\alpha+\beta}\right)\_C1+J_{\frac{b+\beta}{\alpha+\beta}}\left(2\,\frac{\sqrt{-ac}x^{\alpha/2+\beta/2}}{\alpha+\beta}\right)\right)x^{\frac{\alpha}{2}+\frac{\beta}{2}}\sqrt{-ac}\left(Y_{\frac{b-\alpha}{\alpha+\beta}}\left(2\,\frac{\sqrt{-ac}x^{\alpha/2}\right.\right.\right.$$

2.108 ODE No. 108

$$xy'(x)+y(x)+y(x)^2(-\log(x))=0$$

✓ **Mathematica** : cpu = 0.0122192 (sec), leaf count = 15

$$\left\{\left\{y(x)\to\frac{1}{c_1x+\log(x)+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 13

$$\left\{y(x)=\left(1+\_C1\,x+\ln\left(x\right)\right)^{-1}\right\}$$

2.109 ODE No. 109

$$xy'(x)-y(x)(2y(x)\log(x)-1)=0$$

✓ **Mathematica** : cpu = 0.012287 (sec), leaf count = 17

$$\left\{\left\{y(x)\to\frac{1}{c_1x+2\log(x)+2}\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 15

$$\left\{y(x)=\left(2+\_C1\,x+2\,\ln\left(x\right)\right)^{-1}\right\}$$

2.110 ODE No. 110

$$f(x)\left(y(x)^2-x^2\right)+xy'(x)=0$$

✗ **Mathematica** : cpu = 16.6203 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*(-x^2 + y[x]^2) + x*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x*diff(y(x),x)+f(x)*(y(x)^2-x^2) = 0,y(x))
```

2.111 ODE No. 111

$$xy'(x)+y(x)^3+3xy(x)^2=0$$

✓ **Mathematica** : cpu = 0.284017 (sec), leaf count = 55

$$\text{Solve}\left[-3x=\frac{2e^{\frac{1}{2}\left(\frac{1}{y(x)}-3x\right)^2}}{2c_1+\sqrt{2\pi}\text{erfi}\left(\frac{\frac{1}{y(x)}-3x}{\sqrt{2}}\right)},y(x)\right]$$

✓ **Maple** : cpu = 0.128 (sec), leaf count = 54

$$\left\{\_C1-\frac{i}{3}\mathrm{e}^{\frac{(3xy(x)-1)^2}{2(y(x))^2}}+\frac{\sqrt{2}\sqrt{\pi}}{2}Erf\left(\frac{(-i+3iy(x)x)\sqrt{2}}{2y(x)}\right)=0\right\}$$

2.112 ODE No. 112

$$-\sqrt{x^2+y(x)^2}+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0222455 (sec), leaf count = 13

$$\{\{y(x)\to x\sinh(c_1+\log(x))\}\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 27

$$\left\{\frac{1}{x^2}\sqrt{(y(x))^2+x^2}+\frac{y(x)}{x^2}-\_C1=0\right\}$$

2.113 ODE No. 113

$$a\sqrt{x^2+y(x)^2}+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0235148 (sec), leaf count = 16

$$\{\{y(x)\to x\sinh(c_1-a\log(x))\}\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 33

$$\left\{\frac{x^a}{x}\sqrt{(y(x))^2+x^2}+\frac{x^a y(x)}{x}-\_C1=0\right\}$$

2.114 ODE No. 114

$$-x\sqrt{x^2+y(x)^2}+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.020796 (sec), leaf count = 12

$$\{\{y(x)\to x\sinh(c_1+x)\}\}$$

✓ **Maple** : cpu = 2.378 (sec), leaf count = 28

$$\left\{\ln\left(\sqrt{(y(x))^2+x^2}+y(x)\right)-x-\ln(x)-\_C1=0\right\}$$

2.115 ODE No. 115

$$-x(y(x)-x)\sqrt{x^2+y(x)^2}+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.124501 (sec), leaf count = 99

$$\left\{\left\{y(x)\to\frac{x\left(-2e^{\sqrt{2}c_1+\frac{x^2}{\sqrt{2}}}+e^{2\sqrt{2}c_1+\sqrt{2}x^2}-1\right)}{2e^{\sqrt{2}c_1+\frac{x^2}{\sqrt{2}}}+e^{2\sqrt{2}c_1+\sqrt{2}x^2}-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.227 (sec), leaf count = 49

$$\left\{\ln\left(2\frac{\left(\sqrt{2\left(y(x)\right)^2+2x^2}+y(x)+x\right)x}{y(x)-x}\right)+\frac{\sqrt{2}x^2}{2}-\ln(x)-\_C1=0\right\}$$

2.116 ODE No. 116

$$-x\sqrt{\left(y(x)^2-4x^2\right)\left(y(x)^2-x^2\right)}+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.460488 (sec), leaf count = 143

$$\text{Solve}\left[\frac{2\left(\frac{y(x)}{x}-2\right)^{3/2}\sqrt{-\frac{4}{\frac{y(x)}{x}-2}-1}\sqrt{-\frac{3}{\frac{y(x)}{x}-2}-1}\sqrt{\frac{1}{\frac{y(x)}{x}-2}+1}F\left(\sin^{-1}\left(\frac{\sqrt{-1-\frac{3}{\frac{y(x)}{x}-2}}}{\sqrt{2}}\right)\middle|-8\right)}{\sqrt{\frac{y(x)}{x}-1}\sqrt{\frac{y(x)}{x}+1}\sqrt{\frac{y(x)}{x}+2}}=c_1+\frac{x^2}{2},y(x\right.$$

✓ **Maple** : cpu = 0.229 (sec), leaf count = 86

$$\left\{\int_{\_b}^{x}1\left(\_a\sqrt{4\_a^4-5\_a^2\left(y\left(x\right)\right)^2+\left(y\left(x\right)\right)^4}+y(x)\right)\frac{1}{\sqrt{4\_a^4-5\_a^2\left(y\left(x\right)\right)^2+\left(y\left(x\right)\right)^4}}\mathrm{d}\_a+\int^{y(x)}-\_b\frac{}{\sqrt{}}\right.$$

2.117 ODE No. 117

$$xy'(x)+x\left(-e^{\frac{y(x)}{x}}\right)-y(x)-x=0$$

✓ **Mathematica** : cpu = 0.0554187 (sec), leaf count = 21

$$\left\{\left\{y(x)\to -x\log\left(\frac{e^{-c_1}}{x}-1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 20

$$\left\{y(x)=\left(\ln\left(-\frac{x}{-1+x\mathrm{e}^{\_C1}}\right)+\_C1\right)x\right\}$$

2.118 ODE No. 118

$$xy'(x)-y(x)\log(y(x))=0$$

✓ **Mathematica** : cpu = 0.0124863 (sec), leaf count = 13

$$\left\{\left\{y(x)\to e^{e^{c_1}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 8

$$\left\{y(x)=\mathrm{e}^{\_C1\,x}\right\}$$

2.119 ODE No. 119

$$xy'(x) - y(x)(\log(xy(x)) - 1) = 0$$

✓ **Mathematica** : cpu = 0.0307784 (sec), leaf count = 17

$$\left\{\left\{y(x) \to \frac{e^{e^{c_1} x}}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.09 (sec), leaf count = 14

$$\left\{y(x) = \frac{1}{x} \mathrm{e}^{\frac{x}{\_C1}}\right\}$$

2.120 ODE No. 120

$$xy'(x) - y(x)\left(x \log\left(\frac{x^2}{y(x)}\right) + 2\right) = 0$$

✓ **Mathematica** : cpu = 0.0522435 (sec), leaf count = 20

$$\left\{\left\{y(x) \to x^2 e^{-2c_1 e^{-x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.178 (sec), leaf count = 17

$$\left\{y(x) = x^2 \left(\mathrm{e}^{\frac{\_C1}{\mathrm{e}^x}}\right)^{-1}\right\}$$

2.121 ODE No. 121

$$xy'(x) - \sin(x - y(x)) = 0$$

✗ **Mathematica** : cpu = 3.0387 (sec), leaf count = 0 , could not solve

```
DSolve[-Sin[x - y[x]] + x*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x*diff(y(x),x)-sin(x-y(x)) = 0,y(x))
```

2.122 ODE No. 122

$$\cos(y(x))\left(\sin(y(x))-3x^2\cos(y(x))\right)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.123998 (sec), leaf count = 21

$$\left\{\left\{y(x)\to \tan^{-1}\left(\frac{c_1+2x^3}{2x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.457 (sec), leaf count = 16

$$\left\{y(x)=\arctan\left(\frac{x^3+2\_C1}{x}\right)\right\}$$

2.123 ODE No. 123

$$xy'(x)-y(x)-x\sin\left(\frac{y(x)}{x}\right)=0$$

✓ **Mathematica** : cpu = 0.0585967 (sec), leaf count = 19

$$\left\{\left\{y(x)\to 2x\cot^{-1}\left(\frac{e^{-c_1}}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.051 (sec), leaf count = 44

$$\left\{y(x)=\arctan\left(2\,\frac{\_C1\,x}{\_C1^2x^2+1},\frac{-\_C1^2x^2+1}{\_C1^2x^2+1}\right)x\right\}$$

2.124 ODE No. 124

$$xy'(x)-y(x)+x\cos\left(\frac{y(x)}{x}\right)+x=0$$

✓ **Mathematica** : cpu = 0.0274909 (sec), leaf count = 16

$$\left\{\left\{y(x)\to 2x\tan^{-1}\left(c_1-\log(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 12

$$\left\{y(x)=-2\arctan\left(\ln\left(x\right)+\_C1\right)x\right\}$$

2.125 ODE No. 125

$$xy'(x) - y(x) + x \tan\left(\frac{y(x)}{x}\right) = 0$$

✓ **Mathematica** : cpu = 0.0375461 (sec), leaf count = 16

$$\left\{\left\{y(x) \to x \sin^{-1}\left(\frac{e^{c_1}}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.062 (sec), leaf count = 14

$$\left\{y(x) = \arcsin\left(\frac{1}{\_C1\, x}\right) x\right\}$$

2.126 ODE No. 126

$$xy'(x) - y(x) f(xy(x)) = 0$$

✓ **Mathematica** : cpu = 15.3367 (sec), leaf count = 112

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{1}{K[2](-f(xK[2])-1)} - \int_1^x \left(\frac{f'(K[1]K[2])}{f(K[1]K[2])+1} - \frac{f(K[1]K[2])f'(K[1]K[2])}{(f(K[1]K[2])+1)^2}\right) dK[1]\right) dK[2] + \int_1$$

✓ **Maple** : cpu = 0.024 (sec), leaf count = 29

$$\left\{y(x) = \frac{1}{x} RootOf\left(-\ln(x) + \_C1 + \int^{\_Z} \frac{1}{\_a\,(1+f(\_a))} d\_a\right)\right\}$$

2.127 ODE No. 127

$$xy'(x) - y(x) f\left(x^a y(x)^b\right) = 0$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.11 (sec), leaf count = 39

$$\left\{\int_{\_b}^{y(x)} \frac{1}{(f(x^a \_a^b)\, b + a)\, \_a} \,\mathrm{d}\_a - \frac{\ln(x)}{b} - \_C1 = 0\right\}$$

2.128 ODE No. 128

$$-f(x)g(x^a y(x)) + ay(x) + xy'(x) = 0$$

✓ **Mathematica** : cpu = 4.31431 (sec), leaf count = 39

$$\text{Solve}\left[\int_1^{x^a y(x)} \frac{1}{g(K[1])}\,dK[1] = \int_1^x K[2]^{a-1} f(K[2])\,dK[2] + c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.283 (sec), leaf count = 33

$$\left\{y(x) = \frac{RootOf\left(-\int f(x)\,x^{a-1}\,\mathrm{d}x + \int^{-Z} (g(\_a))^{-1}\,d\_a + \_C1\right)}{x^a}\right\}$$

2.129 ODE No. 129

$$(x+1)y'(x) + y(x)(y(x) - x) = 0$$

✓ **Mathematica** : cpu = 0.0297001 (sec), leaf count = 44

$$\left\{\left\{y(x) \to -\frac{e^{x+1}}{-ec_1 x - ec_1 - x\text{Ei}(x+1) - \text{Ei}(x+1) + e^{x+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 33

$$\left\{y(x) = \frac{\mathrm{e}^x}{-\mathrm{e}^{-1}\,(1+x)\,Ei\,(1,-1-x) - \mathrm{e}^x + \_C1\ (1+x)}\right\}$$

2.130 ODE No. 130

$$-2x^3 + 2xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.00718232 (sec), leaf count = 21

$$\left\{\left\{y(x) \to c_1\sqrt{x} + \frac{2x^3}{5}\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 15

$$\left\{y(x) = \frac{2\,x^3}{5} + \sqrt{x}\_C1\right\}$$

2.131 ODE No. 131

$$(2x+1)y'(x) - 4e^{-y(x)} + 2 = 0$$

✓ **Mathematica** : cpu = 0.018135 (sec), leaf count = 20

$$\left\{\left\{y(x) \to \log\left(\frac{e^{c_1}}{2x+1} + 2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.193 (sec), leaf count = 31

$$\left\{y(x) = -\ln\left(\frac{2\,x+1}{-1+(4\,x+2)\,\mathrm{e}^{2\_C1}}\right) - 2\,\_C1\right\}$$

2.132 ODE No. 132

$$3xy'(x) - y(x) - 3xy(x)^4 \log(x) = 0$$

✓ **Mathematica** : cpu = 0.012878 (sec), leaf count = 115

$$\left\{\left\{y(x) \to \frac{(-2)^{2/3}\sqrt[3]{x}}{\sqrt[3]{4c_1 + 3x^2 - 6x^2\log(x)}}\right\}, \left\{y(x) \to \frac{2^{2/3}\sqrt[3]{x}}{\sqrt[3]{4c_1 + 3x^2 - 6x^2\log(x)}}\right\}, \left\{y(x) \to -\frac{\sqrt[3]{-1}2^{2/3}\sqrt[3]{x}}{\sqrt[3]{4c_1 + 3x^2 - 6x^2\log}}\right.\right.$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 153

$$\left\{y(x) = \frac{1}{6\,x^2\ln(x) - 3\,x^2 - 4\,\_C1}\sqrt[3]{-4\,x\,(6\,x^2\ln(x) - 3\,x^2 - 4\,\_C1)^2}, y(x) = \frac{i\sqrt{3}-1}{12\,x^2\ln(x) - 6\,x^2 - 8\,\_C1}\sqrt[3]{-}\right.$$

2.133 ODE No. 133

$$x^2y'(x) + y(x) - x = 0$$

✓ **Mathematica** : cpu = 0.00797555 (sec), leaf count = 27

$$\left\{\left\{y(x) \to c_1 e^{\frac{1}{x}} - e^{\frac{1}{x}}\mathrm{Ei}\left(-\frac{1}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 16

$$\left\{y(x) = \left(Ei\left(1, x^{-1}\right) + \_C1\right)\mathrm{e}^{x^{-1}}\right\}$$

2.134 ODE No. 134

$$x^2y'(x) + e^{x-\frac{1}{x}}x^2 - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0126604 (sec), leaf count = 27

$$\left\{\left\{y(x) \to c_1e^{-1/x} - e^{x-\frac{1}{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.009 (sec), leaf count = 17

$$\left\{y(x) = \left(-\mathrm{e}^{x} + \_C1\right)\mathrm{e}^{-x^{-1}}\right\}$$

2.135 ODE No. 135

$$x^2y'(x) - (x-1)y(x) = 0$$

✓ **Mathematica** : cpu = 0.007805 (sec), leaf count = 14

$$\left\{\left\{y(x) \to c_1e^{\frac{1}{x}}x\right\}\right\}$$

✓ **Maple** : cpu = 0.006 (sec), leaf count = 11

$$\left\{y(x) = \_C1\ x\mathrm{e}^{x^{-1}}\right\}$$

2.136 ODE No. 136

$$x^2y'(x) + x^2 + xy(x) + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0140367 (sec), leaf count = 28

$$\left\{\left\{y(x) \to \frac{-c_1x - x + x\log(x)}{c_1 - \log(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 18

$$\left\{y(x) = -\frac{x(\ln(x) + \_C1 - 1)}{\ln(x) + \_C1}\right\}$$

2.137 ODE No. 137

$$x^2 y'(x) - xy(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.00986761 (sec), leaf count = 16

$$\left\{\left\{y(x) \to \frac{x}{c_1 - \log(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 14

$$\left\{y(x) = \frac{x}{-\ln(x) + \_C1}\right\}$$

2.138 ODE No. 138

$$x^2 y'(x) - x^2 - xy(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.015426 (sec), leaf count = 13

$$\{\{y(x) \to x \tan(c_1 + \log(x))\}\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 11

$$\{y(x) = \tan(\ln(x) + \_C1)\, x\}$$

2.139 ODE No. 139

$$ax^k - (b-1)b + x^2\left(y'(x) + y(x)^2\right) = 0$$

✓ **Mathematica** : cpu = 0.133419 (sec), leaf count = 821

$$\left\{\left\{y(x) \to -\frac{a^{\frac{b}{k}+\frac{1}{2}\left(\frac{1}{k}-\frac{2b}{k}\right)}\left(\frac{b}{k}+\frac{1}{2}\left(\frac{1}{k}-\frac{2b}{k}\right)\right)x^{k-1}\left(x^k\right)^{\frac{b}{k}+\frac{1}{2}\left(\frac{1}{k}-\frac{2b}{k}\right)-1} J_{\frac{2b-1}{k}}\left(\frac{2\sqrt{a}\sqrt{x^k}}{k}\right)\Gamma\left(\frac{2b}{k}-\frac{1}{k}+1\right)k^{1-\frac{1}{k}} + \frac{1}{2}a^{\frac{b}{k}+\frac{1}{2}}\right.\right.$$

✓ **Maple** : cpu = 0.142 (sec), leaf count = 219

$$\left\{y(x) = \frac{1}{2\,x}\left(-2\,J_{\frac{\sqrt{(-1+2\,b)^2}+k}{k}}\left(2\,\frac{\sqrt{a}x^{k/2}}{k}\right)\sqrt{a}x^{k/2} - 2\,\sqrt{a}x^{k/2}Y_{\frac{\sqrt{(-1+2\,b)^2}+k}{k}}\left(2\,\frac{\sqrt{a}x^{k/2}}{k}\right)\_C1 + 2\,(1/2 + (b-1/\right.\right.$$

2.140 ODE No. 140

$$x^2\left(y'(x)+y(x)^2\right)+4xy(x)+2=0$$

✓ **Mathematica** : cpu = 0.0103476 (sec), leaf count = 17

$$\left\{\left\{y(x)\to \frac{1}{c_1+x}-\frac{2}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 20

$$\left\{y(x)=\frac{-2\_C1+x}{x\left(-x+\_C1\right)}\right\}$$

2.141 ODE No. 141

$$axy(x)+b+x^2\left(y'(x)+y(x)^2\right)=0$$

✓ **Mathematica** : cpu = 0.0280064 (sec), leaf count = 67

$$\left\{\left\{y(x)\to -\frac{\sqrt{a^2-2a-4b+1}\left(\frac{2c_1}{x^{\sqrt{a^2-2a-4b+1}}+c_1}-1\right)-1}{2x}-\frac{a}{2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.051 (sec), leaf count = 51

$$\left\{y(x)=\frac{1}{2\,x}\left(-\tanh\left(\frac{-\ln\left(x\right)+\_C1}{2}\sqrt{a^2-2\,a-4\,b+1}\right)\sqrt{a^2-2\,a-4\,b+1}-a+1\right)\right\}$$

2.142 ODE No. 142

$$-ax^2y(x)+ax+x^2\left(y'(x)-y(x)^2\right)+2=0$$

✓ **Mathematica** : cpu = 0.191571 (sec), leaf count = 113

$$\left\{\left\{y(x)\to -\frac{\frac{1}{a^3x^2}+c_1\left(\frac{e^{ax}\left(a^2x+a(ax-2)\right)}{x}-\frac{e^{ax}(ax(ax-2)+2)}{x^2}+\frac{ae^{ax}(ax(ax-2)+2)}{x}\right)}{\frac{c_1e^{ax}(ax(ax-2)+2)}{x}-\frac{1}{a^3x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.094 (sec), leaf count = 52

$$\left\{y(x)=\frac{-\left(ax-1\right)\left(a^2x^2+2\right)\mathrm{e}^{ax}+\_C1}{\left(\left(a^2x^2-2\,ax+2\right)\mathrm{e}^{ax}+\_C1\right)x}\right\}$$

2.143 ODE No. 143

$$x^2\left(ay(x)^2+y'(x)\right)-b=0$$

✓ **Mathematica** : cpu = 0.0101326 (sec), leaf count = 51

$$\left\{\left\{y(x)\to -\frac{\sqrt{4ab+1}\left(\frac{2c_1}{x^{\sqrt{4ab+1}}+c_1}-1\right)-1}{2ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 41

$$\left\{y(x)=\frac{1}{2\,ax}\left(-\tanh\left(\frac{-\ln\left(x\right)+\_C1}{2}\sqrt{4\,ab+1}\right)\sqrt{4\,ab+1}+1\right)\right\}$$

2.144 ODE No. 144

$$x^2\left(ay(x)^2+y'(x)\right)+bx^{\alpha}+c=0$$

✓ **Mathematica** : cpu = 0.170274 (sec), leaf count = 1787

$$\left\{\left\{y(x)\to \frac{a^{\frac{i\sqrt{4ac-1}\alpha+\alpha}{2\alpha^2}-\frac{\sqrt{\alpha^2-4a\alpha^2c}}{2\alpha^2}}\alpha^{-\frac{i\sqrt{4ac-1}\alpha+\alpha}{\alpha^2}+\frac{\sqrt{\alpha^2-4a\alpha^2c}}{\alpha^2}+1}b^{\frac{i\sqrt{4ac-1}\alpha+\alpha}{2\alpha^2}-\frac{\sqrt{\alpha^2-4a\alpha^2c}}{2\alpha^2}}\left(\frac{i\sqrt{4ac-1}\alpha+\alpha}{2\alpha^2}-\frac{\sqrt{\alpha^2-4a\alpha^2c}}{2\alpha^2}\right)(x^{\right.}\right.\right.$$

✓ **Maple** : cpu = 0.118 (sec), leaf count = 219

$$\left\{y(x)=\frac{1}{2\,ax}\left(-2\sqrt{ab}\left(Y_{\frac{\sqrt{-4\,ac+1}+\alpha}{\alpha}}\left(2\,\frac{\sqrt{ab}x^{\alpha/2}}{\alpha}\right)\_C1+J_{\frac{\sqrt{-4\,ac+1}+\alpha}{\alpha}}\left(2\,\frac{\sqrt{ab}x^{\alpha/2}}{\alpha}\right)\right)x^{\alpha/2}+\left(\sqrt{-4\,ac+1}+1\right)\right.\right.$$

2.145 ODE No. 145

$$-ax^2y(x)^2+ay(x)^3+x^2y'(x)=0$$

✓ **Mathematica** : cpu = 0.381577 (sec), leaf count = 267

$$\text{Solve}\left[\frac{\left(-\frac{1}{2^{2/3}a^{2/3}y(x)}-\frac{\sqrt[3]{a}x}{2^{2/3}}\right)\text{Ai}\left(\left(-\frac{\sqrt[3]{a}x}{2^{2/3}}-\frac{1}{2^{2/3}a^{2/3}y(x)}\right)^2+\frac{1}{\sqrt[3]{2}\sqrt[3]{a}x}\right)+\text{Ai}'\left(\left(-\frac{\sqrt[3]{a}x}{2^{2/3}}-\frac{1}{2^{2/3}a^{2/3}y(x)}\right)^2+\frac{1}{\sqrt[3]{2}\sqrt[3]{a}x}\right)}{\left(-\frac{1}{2^{2/3}a^{2/3}y(x)}-\frac{\sqrt[3]{a}x}{2^{2/3}}\right)\text{Bi}\left(\left(-\frac{\sqrt[3]{a}x}{2^{2/3}}-\frac{1}{2^{2/3}a^{2/3}y(x)}\right)^2+\frac{1}{\sqrt[3]{2}\sqrt[3]{a}x}\right)+\text{Bi}'\left(\left(-\frac{\sqrt[3]{a}x}{2^{2/3}}-\frac{1}{2^{2/3}a^{2/3}y(x)}\right)^2+\frac{1}{\sqrt[3]{2}\sqrt[3]{a}x}\right)}\right.$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 117

$$\left\{y(x)=-\left(ax+(-2\,a)^{\frac{2}{3}}\,RootOf\left(\mathrm{Bi}\left(\frac{1}{x}(\_Z^2\sqrt[3]{-2\,a}x-1)\,\frac{1}{\sqrt[3]{-2\,a}}\right)\_C1\,\_Z+\_Z\,\mathrm{Ai}\left(\frac{1}{x}(\_Z^2\sqrt[3]{-2\,a}x-1)\,\frac{\sqrt[3]}{}\right.\right.\right.$$

2.146 ODE No. 146

$$ay(x)^2+x^2y'(x)+xy(x)^3=0$$

✓ **Mathematica** : cpu = 0.519557 (sec), leaf count = 78

$$\text{Solve}\left[-\frac{ia}{x}=\frac{2e^{\frac{1}{2}\left(-\frac{ia}{x}-\frac{i}{y(x)}\right)^2}}{2c_1+\sqrt{2\pi}\text{erfi}\left(\frac{-\frac{ia}{x}-\frac{i}{y(x)}}{\sqrt{2}}\right)},y(x)\right]$$

✓ **Maple** : cpu = 0.176 (sec), leaf count = 84

$$\left\{\frac{1}{2}\left(a\sqrt{\pi}\sqrt{2}Erf\left(\frac{\sqrt{2}(ay(x)+x)}{2\,xy\,(x)}\right)\mathrm{e}^{\frac{(ay(x)+x)^2}{2\,x^2(y(x))^2}}+2\,x\right)\mathrm{e}^{-\frac{((a-x)y(x)+x)((x+a)y(x)+x)}{2\,x^2(y(x))^2}}+\_C1=0\right\}$$

2.147 ODE No. 147

$$ax^2y(x)^3+by(x)^2+x^2y'(x)=0$$

✓ **Mathematica** : cpu = 0.51872 (sec), leaf count = 343

$$\text{Solve}\left[\frac{\left(\frac{b^{2/3}}{2^{2/3}\sqrt[3]{a}x}+\frac{1}{2^{2/3}\sqrt[3]{a}\sqrt[3]{b}y(x)}\right)\text{Ai}\left(\left(\frac{b^{2/3}}{2^{2/3}\sqrt[3]{a}x}+\frac{1}{2^{2/3}\sqrt[3]{a}y(x)\sqrt[3]{b}}\right)^2-\frac{\sqrt[3]{a}x}{\sqrt[3]{2}b^{2/3}}\right)+\text{Ai}'\left(\left(\frac{b^{2/3}}{2^{2/3}\sqrt[3]{a}x}+\frac{1}{2^{2/3}\sqrt[3]{a}y(x)\sqrt[3]{b}}\right)^2-\right.}{\left(\frac{b^{2/3}}{2^{2/3}\sqrt[3]{a}x}+\frac{1}{2^{2/3}\sqrt[3]{a}\sqrt[3]{b}y(x)}\right)\text{Bi}\left(\left(\frac{b^{2/3}}{2^{2/3}\sqrt[3]{a}x}+\frac{1}{2^{2/3}\sqrt[3]{a}y(x)\sqrt[3]{b}}\right)^2-\frac{\sqrt[3]{a}x}{\sqrt[3]{2}b^{2/3}}\right)+\text{Bi}'\left(\left(\frac{b^{2/3}}{2^{2/3}\sqrt[3]{a}x}+\frac{1}{2^{2/3}\sqrt[3]{a}y(x)\sqrt[3]{b}}\right)^2-\right.},y(x)\right]$$

✓ **Maple** : cpu = 0.215 (sec), leaf count = 178

$$\left\{y(x)=-\sqrt[3]{2}abx\left(\sqrt[3]{2}ab^2-2\left(a^2b^2\right)^{2/3}\,RootOf\left(\mathrm{Bi}\left(-1/2\,\frac{a2^{2/3}x-2\_Z^2\sqrt[3]{a^2b^2}}{\sqrt[3]{a^2b^2}}\right)\_C1\,\_Z+\_Z\,\mathrm{Ai}\left(-1/2\,\frac{a2^{2}}{}\right.\right.\right.$$

2.148 ODE No. 148

$$\left(x^2+1\right)y'(x)+xy(x)-1=0$$

✓ **Mathematica** : cpu = 0.0137234 (sec), leaf count = 30

$$\left\{\left\{y(x)\to \frac{c_1}{\sqrt{x^2+1}}+\frac{\sinh^{-1}(x)}{\sqrt{x^2+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 16

$$\left\{y(x)=(Arcsinh(x)+\_C1)\frac{1}{\sqrt{x^2+1}}\right\}$$

2.149 ODE No. 149

$$\left(x^2+1\right)y'(x)-x\left(x^2+1\right)+xy(x)=0$$

✓ **Mathematica** : cpu = 0.0127743 (sec), leaf count = 27

$$\left\{\left\{y(x)\to \frac{c_1}{\sqrt{x^2+1}}+\frac{1}{3}\left(x^2+1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 20

$$\left\{y(x)=\frac{x^2}{3}+\frac{1}{3}+\_C1\frac{1}{\sqrt{x^2+1}}\right\}$$

2.150 ODE No. 150

$$\left(x^2+1\right)y'(x)-2x^2+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.00898958 (sec), leaf count = 30

$$\left\{\left\{y(x)\to \frac{c_1}{x^2+1}+\frac{2x^3}{3\left(x^2+1\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.006 (sec), leaf count = 23

$$\left\{y(x)=\frac{2\,x^3+3\,\_C1}{3\,x^2+3}\right\}$$

2.151 ODE No. 151

$$\left(x^2+1\right)y'(x)+(2xy(x)-1)\left(y(x)^2+1\right)=0$$

✓ **Mathematica** : cpu = 0.435463 (sec), leaf count = 203

$$\text{Solve}\left[c_1=\frac{\frac{1}{2}\left(\frac{1}{\frac{ix}{x^2+1}-\frac{ix^2y(x)}{x^2+1}}+\frac{i}{x}\right)\sqrt[4]{1-\left(\frac{1}{\frac{ix}{x^2+1}-\frac{ix^2y(x)}{x^2+1}}+\frac{i}{x}\right)^2}\,{}_2F_1\left(\frac{1}{2},\frac{5}{4};\frac{3}{2};\left(\frac{1}{\frac{ix}{x^2+1}-\frac{ix^2y(x)}{x^2+1}}+\frac{i}{x}\right)^2\right)+ix}{\sqrt[4]{-1+\left(\frac{1}{\frac{ix}{x^2+1}-\frac{ix^2y(x)}{x^2+1}}+\frac{i}{x}\right)^2}},y(x)\right]$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 85

$$\left\{\_C1+x\frac{1}{\sqrt[4]{\left(x^{-1}+x^2\left(\frac{y(x)x^4}{x^2+1}-\frac{x^3}{x^2+1}\right)^{-1}\right)^2+1}}+\frac{y(x)+x}{2\,xy\,(x)-2}{}_2\mathrm{F}_1(\frac{1}{2},\frac{5}{4};\,\frac{3}{2};\,-\frac{(y(x)+x)^2}{(xy\,(x)-1)^2})=0\right\}$$

2.152 ODE No. 152

$$\left(x^2+1\right)y'(x)-x\left(x^2+1\right)\cos^2(y(x))+x\sin(y(x))\cos(y(x))=0$$

✓ **Mathematica** : cpu = 0.237705 (sec), leaf count = 40

$$\left\{\left\{y(x)\to\tan^{-1}\left(\frac{-6c_1\sqrt{x^2+1}+x^4+2x^2+1}{3\left(x^2+1\right)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.859 (sec), leaf count = 25

$$\left\{y(x)=\arctan\left(\frac{1}{3}\left(\left(x^2+1\right)^{\frac{3}{2}}+3\_C1\right)\frac{1}{\sqrt{x^2+1}}\right)\right\}$$

2.153 ODE No. 153

$$a + \left(x^2 - 1\right) y'(x) - xy(x) = 0$$

✓ **Mathematica** : cpu = 0.0171622 (sec), leaf count = 21

$$\left\{\left\{y(x) \to ax + c_1 \sqrt{x^2 - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 20

$$\left\{y(x) = \sqrt{1 + x}\sqrt{x - 1}\_C1 + ax\right\}$$

2.154 ODE No. 154

$$\left(x^2 - 1\right) y'(x) + 2xy(x) - \cos(x) = 0$$

✓ **Mathematica** : cpu = 0.0151851 (sec), leaf count = 26

$$\left\{\left\{y(x) \to \frac{c_1}{x^2 - 1} + \frac{\sin(x)}{x^2 - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 16

$$\left\{y(x) = \frac{\sin(x) + \_C1}{x^2 - 1}\right\}$$

2.155 ODE No. 155

$$\left(x^2 - 1\right) y'(x) + y(x)^2 - 2xy(x) + 1 = 0$$

✓ **Mathematica** : cpu = 0.0189401 (sec), leaf count = 46

$$\left\{\left\{y(x) \to \frac{1}{c_1 + \frac{1}{2}\log(1 - x) - \frac{1}{2}\log(x + 1)} - \frac{x\left(1 - x^2\right)}{x^2 - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.114 (sec), leaf count = 14

$$\left\{y(x) = x + \left(\_C1 - Artanh(x)\right)^{-1}\right\}$$

2.156 ODE No. 156

$$\left(x^2-1\right)y'(x)-y(x)(y(x)-x)=0$$

✓ **Mathematica** : cpu = 0.0164423 (sec), leaf count = 21

$$\left\{\left\{y(x)\to \frac{1}{c_1\sqrt{x^2-1}+x}\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 20

$$\left\{y(x)=\left(\sqrt{x-1}\sqrt{1+x}\_C1+x\right)^{-1}\right\}$$

2.157 ODE No. 157

$$a\left(y(x)^2-2xy(x)+1\right)+\left(x^2-1\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0893016 (sec), leaf count = 158

$$\left\{\left\{y(x)\to \frac{\left(x^2-1\right)\left(c_1\left(ax\left(x^2-1\right)^{\frac{a}{2}-1}P_{a-1}(x)+\left(x^2-1\right)^{\frac{a}{2}-1}\left(aP_a(x)-axP_{a-1}(x)\right)\right)+ax\left(x^2-1\right)^{\frac{a}{2}-1}Q_{a-1}(\right.\right.}{a\left(c_1\left(x^2-1\right)^{a/2}P_{a-1}(x)+\left(x^2-1\right)^{a/2}Q_{a-1}(x)\right)}$$

✓ **Maple** : cpu = 0.279 (sec), leaf count = 231

$$\left\{y(x)=\frac{1}{(4+4x)a}\left(8\left((a-1/2)x-a/2+1/2\right)(1+x)\_C1\ HeunC\left(0,-2a+1,0,0,a^2-a+1/2,2(1+x)^{-1}\right.\right.\right.$$

2.158 ODE No. 158

$$axy(x)^2+\left(x^2-1\right)y'(x)+xy(x)=0$$

✓ **Mathematica** : cpu = 0.0368395 (sec), leaf count = 31

$$\left\{\left\{y(x)\to -\frac{e^{c_1}}{ae^{c_1}-\sqrt{x^2-1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 22

$$\left\{y(x)=\left(\sqrt{x-1}\sqrt{1+x}\_C1-a\right)^{-1}\right\}$$

2.159 ODE No. 159

$$\left(x^2-1\right)y'(x)-2xy(x)\log(y(x))=0$$

✓ **Mathematica** : cpu = 0.0181955 (sec), leaf count = 22

$$\left\{\left\{y(x)\to e^{e^{c_1}x^2-e^{c_1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.125 (sec), leaf count = 13

$$\left\{y(x)=\mathrm{e}^{-\mathit{C1}\,(x-1)(1+x)}\right\}$$

2.160 ODE No. 160

$$\left(x^2-4\right)y'(x)+(x+2)y(x)^2-4y(x)=0$$

✓ **Mathematica** : cpu = 0.0213409 (sec), leaf count = 27

$$\left\{\left\{y(x)\to\frac{2-x}{(x+2)\left(c_1-\log(x+2)\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 21

$$\left\{y(x)=\frac{x-2}{(x+2)\left(\ln\left(x+2\right)+\_C1\right)}\right\}$$

2.161 ODE No. 161

$$\left(x^2-5x+6\right)y'(x)+x^2+3xy(x)-8y(x)=0$$

✓ **Mathematica** : cpu = 0.0150139 (sec), leaf count = 53

$$\left\{\left\{y(x)\to\frac{c_1}{(2-x)^2(3-x)}+\frac{\frac{x^4}{4}-\frac{2x^3}{3}}{(2-x)^2(3-x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 27

$$\left\{y(x)=\frac{1}{\left(x-2\right)^2\left(x-3\right)}\left(-\frac{x^4}{4}+\frac{2\,x^3}{3}+\_C1\right)\right\}$$

2.162 ODE No. 162

$$k(-a+y(x)+x)(-b+y(x)+x)+(x-a)(x-b)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.266428 (sec), leaf count = 133

$$\left\{\left\{y(x)\to \frac{1}{2}\sqrt{\frac{-a^2k^2+2abk^2-b^2k^2}{(k+1)^2}}\tan\left(\frac{(k+1)\sqrt{\frac{-a^2k^2+2abk^2-b^2k^2}{(k+1)^2}}(\log(x-b)-\log(x-a))}{2(a-b)}+c_1\right)-\frac{-ak-\right.\right.$$

✓ **Maple** : cpu = 0.199 (sec), leaf count = 58

$$\left\{y(x)=\frac{\left(\_C1\,(a-x)\,(a-x)^k+(b-x)^k\,(b-x)\right)k}{(k+1)\left(\_C1\,\,(a-x)^k+(b-x)^k\right)}\right\}$$

2.163 ODE No. 163

$$2a^2x+2x^2y'(x)-2y(x)^2-xy(x)=0$$

✓ **Mathematica** : cpu = 0.0140949 (sec), leaf count = 43

$$\left\{\left\{y(x)\to -\sqrt{-a^2}\sqrt{x}\tan\left(\frac{2\sqrt{-a^2}}{\sqrt{x}}-c_1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 26

$$\left\{y(x)=i\tan\left(1(\_C1\,\sqrt{x}-2\,ia)\,\frac{1}{\sqrt{x}}\right)\sqrt{x}a\right\}$$

2.164 ODE No. 164

$$2a^2x+2x^2y'(x)-2y(x)^2-3xy(x)=0$$

✓ **Mathematica** : cpu = 0.081957 (sec), leaf count = 131

$$\left\{\left\{y(x)\to -\frac{x^2\left(c_1\left(\frac{ae^{-\frac{2a}{\sqrt{x}}}}{x}+\frac{e^{-\frac{2a}{\sqrt{x}}}}{2\sqrt{x}}\right)-\frac{e^{\frac{2a}{\sqrt{x}}}}{4a\sqrt{x}}+\frac{e^{\frac{2a}{\sqrt{x}}}}{2x}\right)}{c_1\sqrt{x}e^{-\frac{2a}{\sqrt{x}}}-\frac{\sqrt{x}e^{\frac{2a}{\sqrt{x}}}}{2a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.217 (sec), leaf count = 102

$$\left\{y(x)=1\left(\left(-2\,x\_C1\,\sqrt{-\frac{a^2}{x}}-x\right)\sin\left(2\sqrt{-\frac{a^2}{x}}\right)-x\left(\_C1-2\sqrt{-\frac{a^2}{x}}\right)\cos\left(2\sqrt{-\frac{a^2}{x}}\right)\right)\left(2\cos\left(2\sqrt{-\frac{a^2}{x}}\right.\right.\right.$$

2.165 ODE No. 165

$$x(2x-1)y'(x)+y(x)^2-(4x+1)y(x)+4x=0$$

✓ **Mathematica** : cpu = 0.0177299 (sec), leaf count = 22

$$\left\{\left\{y(x)\to \frac{(1-2x)x}{c_1-x}+1\right\}\right\}$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 17

$$\left\{y(x)=\frac{2\,x^2+\_C1}{x+\_C1}\right\}$$

2.166 ODE No. 166

$$2(x-1)xy'(x)+(x-1)y(x)^2-x=0$$

✓ **Mathematica** : cpu = 0.0881199 (sec), leaf count = 71

$$\left\{\left\{y(x)\to \frac{2x\left(\frac{c_1(E(x)-K(x))}{\pi x}-G^{2,0}_{2,2}\left(x\left|\begin{array}{c}-\frac{1}{2},\frac{1}{2}\\-1,0\end{array}\right.\right)\right)}{G^{2,0}_{2,2}\left(x\left|\begin{array}{c}\frac{1}{2},\frac{3}{2}\\0,0\end{array}\right.\right)+\frac{2c_1E(x)}{\pi}}\right\}\right\}$$

✓ **Maple** : cpu = 0.174 (sec), leaf count = 97

$$\left\{y(x)=\frac{x}{2\,x-2}\left(LegendreQ\left(-\frac{1}{2},1,\frac{2-x}{x}\right)\_C1-LegendreQ\left(\frac{1}{2},1,\frac{2-x}{x}\right)\_C1+LegendreP\left(-\frac{1}{2},1,\frac{2-x}{x}\right)\right.\right.$$

2.167 ODE No. 167

$$3x^2y'(x)-x^2-3xy(x)-7y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0231152 (sec), leaf count = 35

$$\left\{\left\{y(x)\to \frac{x\tan\left(\frac{1}{3}\left(3\sqrt{7}c_1+\sqrt{7}\log(x)\right)\right)}{\sqrt{7}}\right\}\right\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 20

$$\left\{y(x)=\frac{x\sqrt{7}}{7}\tan\left(\frac{\left(\ln\left(x\right)+\_C1\right)\sqrt{7}}{3}\right)\right\}$$

2.168 ODE No. 168

$$3\left(x^2-4\right)y'(x)+y(x)^2-xy(x)-3=0$$

✓ **Mathematica** : cpu = 0.0961953 (sec), leaf count = 234

$$\left\{\left\{y(x)\to \frac{3\left(x^2-4\right)\left(c_1\left(\frac{xP^{\frac{1}{3}}_{-\frac{1}{6}}\left(\frac{x}{2}\right)}{6(x^2-4)^{11/12}}+\frac{\sqrt[12]{x^2-4}\left(\frac{1}{2}P^{\frac{1}{3}}_{\frac{5}{6}}\left(\frac{x}{2}\right)-\frac{5}{12}xP^{\frac{1}{3}}_{-\frac{1}{6}}\left(\frac{x}{2}\right)\right)}{2\left(\frac{x^2}{4}-1\right)}\right)+\frac{xQ^{\frac{1}{3}}_{-\frac{1}{6}}\left(\frac{x}{2}\right)}{6(x^2-4)^{11/12}}+\frac{\sqrt[12]{x^2-4}\left(\frac{1}{2}Q^{\frac{1}{3}}_{\frac{5}{6}}\left(\frac{x}{2}\right)-\frac{5}{12}xQ^{\frac{1}{3}}_{-}\right.\right.\right.}{2\left(\frac{x^2}{4}-1\right)}}{c_1\sqrt[12]{x^2-4}P^{\frac{1}{3}}_{-\frac{1}{6}}\left(\frac{x}{2}\right)+\sqrt[12]{x^2-4}Q^{\frac{1}{3}}_{-\frac{1}{6}}\left(\frac{x}{2}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.191 (sec), leaf count = 140

$$\left\{y(x)=-3\left(x+2\right)\left(HeunC\left(0,4/3,-1/3,0,\frac{25}{36},4\left(x+2\right)^{-1}\right)\_C1-1/3\left(-x/4-1/2\right)^{4/3}HeunC\left(0,-4/3,-1\right.\right.\right.$$

2.169 ODE No. 169

$$(ax+b)^2y'(x)+y(x)^3(ax+b)+cy(x)^2=0$$

✓ **Mathematica** : cpu = 2.26372 (sec), leaf count = 149

$$\text{Solve}\left[-\frac{c}{\sqrt{-a(ax+b)^2}}=\frac{2\exp\left(\frac{1}{2}\left(-\frac{c}{\sqrt{-a(ax+b)^2}}-\frac{\sqrt{-a(ax+b)^2}}{y(x)(-ax-b)}\right)^2\right)}{\sqrt{2\pi}\text{erfi}\left(\frac{-\frac{c}{\sqrt{-a(ax+b)^2}}-\frac{\sqrt{-a(ax+b)^2}}{y(x)(-ax-b)}}{\sqrt{2}}\right)+2c_1},y(x)\right]$$

✓ **Maple** : cpu = 0.158 (sec), leaf count = 153

$$\left\{\frac{1}{2}\left(\left(\sqrt{2}\sqrt{\pi}Erf\left(\frac{\left(cy(x)+a(ax+b)\right)\sqrt{2}}{2\left(ax+b\right)y\left(x\right)}\frac{1}{\sqrt{a}}\right)e^{\frac{\left(cy(x)+a(ax+b)\right)^2}{2\left(y(x)\right)^2(ax+b)^2a}}ac+2\left(ax+b\right)a^{3/2}\right)e^{-\frac{((ax+b+c)y(x)+a(ax+b))((-ax-b+}{2\left(y(x)\right)^2(ax+b)^2a}}\right.\right.$$

2.170 ODE No. 170

$$-x^4+x^3y'(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0229875 (sec), leaf count = 43

$$\left\{\left\{y(x)\to -\frac{x^3\left(-\frac{c_1}{x^2}+\frac{1}{x^2}-\frac{\log(x)}{x^2}\right)}{\frac{c_1}{x}+\frac{\log(x)}{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 23

$$\left\{y(x)=\frac{(\ln(x)-\_C1-1)\,x^2}{\ln(x)-\_C1}\right\}$$

2.171 ODE No. 171

$$x^3y'(x)-x^2y(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0110061 (sec), leaf count = 17

$$\left\{\left\{y(x)\to \frac{x^2}{c_1x+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 15

$$\left\{y(x)=\frac{x^2}{\_C1\,x+1}\right\}$$

2.172 ODE No. 172

$$x^4\left(-y(x)^2\right)+x^3y'(x)+x^2y(x)+20=0$$

✓ **Mathematica** : cpu = 0.0423906 (sec), leaf count = 35

$$\left\{\left\{y(x)\to -\frac{5c_1x^4-\frac{4}{x^5}}{x\left(c_1x^5+\frac{1}{x^4}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.275 (sec), leaf count = 26

$$\left\{y(x)=\frac{5\,x^9+4\,\_C1}{(-x^9+\_C1)\,x^2}\right\}$$

2.173 ODE No. 173

$$x^6\left(-y(x)^2\right)+x^3y'(x)-(2x-3)x^2y(x)+3=0$$

✓ **Mathematica** : cpu = 0.0168826 (sec), leaf count = 29

$$\left\{\left\{y(x)\to \frac{1}{x^3\left(c_1e^{4x}+\frac{1}{4}\right)}-\frac{3}{x^3}\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 27

$$\left\{y(x)=\frac{-3\left(\mathrm{e}^x\right)^4\_C1-3}{x^3\left(\left(\mathrm{e}^x\right)^4\_C1-3\right)}\right\}$$

2.174 ODE No. 174

$$\left(x^2+1\right)xy'(x)+x^2y(x)=0$$

✓ **Mathematica** : cpu = 0.00763765 (sec), leaf count = 17

$$\left\{\left\{y(x)\to \frac{c_1}{\sqrt{x^2+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.005 (sec), leaf count = 13

$$\left\{y(x)=\_C1\frac{1}{\sqrt{x^2+1}}\right\}$$

2.175 ODE No. 175

$$ax^3+\left(x^2-1\right)xy'(x)-\left(2x^2-1\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0207672 (sec), leaf count = 24

$$\left\{\left\{y(x)\to ax+c_1\sqrt{1-x^2}x\right\}\right\}$$

✓ **Maple** : cpu = 0.025 (sec), leaf count = 20

$$\left\{y(x)=x\left(\sqrt{x-1}\sqrt{1+x}\_C1+a\right)\right\}$$

2.176 ODE No. 176

$$\left(x^2-1\right)xy'(x)+\left(x^2-1\right)y(x)^2-x^2=0$$

✓ **Mathematica** : cpu = 0.12749 (sec), leaf count = 82

$$\left\{\left\{y(x)\to \frac{x\left(\frac{2c_1\left(E\left(x^2\right)-K\left(x^2\right)\right)}{\pi x}-2xG^{2,0}_{2,2}\left(x^2\middle|\begin{array}{c}-\frac{1}{2},\frac{1}{2}\\-1,0\end{array}\right)\right)}{G^{2,0}_{2,2}\left(x^2\middle|\begin{array}{c}\frac{1}{2},\frac{3}{2}\\0,0\end{array}\right)+\frac{2c_1E\left(x^2\right)}{\pi}}\right\}\right\}$$

✓ **Maple** : cpu = 0.103 (sec), leaf count = 30

$$\left\{y(x)=\frac{\_C1\ EllipticCE(x)+EllipticE(x)-EllipticK(x)}{\_C1\ EllipticCE\left(x\right)-\_C1\ EllipticCK\left(x\right)+EllipticE\left(x\right)}\right\}$$

2.177 ODE No. 177

$$(x-1)x^2y'(x)-(x-2)xy(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0176224 (sec), leaf count = 22

$$\left\{\left\{y(x)\to -\frac{x^2}{c_1x-c_1-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 17

$$\left\{y(x)=\frac{x^2}{1+\_C1\ (x-1)}\right\}$$

2.178 ODE No. 178

$$2\left(x^2-1\right)xy'(x)+2\left(x^2-1\right)y(x)^2-\left(3x^2-5\right)y(x)+x^2-3=0$$

✓ **Mathematica** : cpu = 0.0724295 (sec), leaf count = 62

$$\left\{\left\{y(x)\to \frac{\sqrt{x}}{\sqrt{1-x^2}\left(c_1-\frac{2\sqrt{1-\frac{1}{x^2}}xF\left(\sin^{-1}\left(\frac{1}{\sqrt{x}}\right)\middle|-1\right)}{\sqrt{1-x^2}}\right)}+1\right\}\right\}$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 63

$$\left\{y(x) = 1 - 2\,\frac{\sqrt{x}}{\sqrt{x-1}\sqrt{1+x}}\left(\_C1 - 2\,\frac{EllipticF\left(\sqrt{1+x}, 1/2\,\sqrt{2}\right)\sqrt{-x}\sqrt{-2\,x+2}\sqrt{2}}{\sqrt{2\,x-2}\sqrt{x}}\right)^{-1}\right\}$$

2.179 ODE No. 179

$$3x\left(x^2-1\right)y'(x) - \left(x^2+1\right)y(x) + xy(x)^2 - 3x = 0$$

✓ **Mathematica** : cpu = 1.68264 (sec), leaf count = 2816

$$\left\{\left\{y(x) \to \frac{3\left(x^2-1\right)\left(e^{\int_1^x \text{Root}\left[125K[1]^8-164K[1]^6+70K[1]^4-20K[1]^2+\left(1296K[1]^{12}-5184K[1]^{10}+7776K[1]^8-5184K[1]^6+1296K[1]^4\right)\#1^4+\left(-345\right.\right.\right.\right.}}{\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.167 (sec), leaf count = 112

$$\left\{y(x) = 35\,\frac{1}{\sqrt[3]{x}\left(8\,x^{2/3}{}_2\mathrm{F}_1(5/6, 7/6;\, 4/3;\, x^2)\_C1 + 8\,{}_2\mathrm{F}_1(1/2, 5/6;\, 2/3;\, x^2)\right)}\left(\_C1\left(\frac{8\,x^2}{7} - \frac{16}{35}\right){}_2\mathrm{F}_1(5/6, 7/6;\right.\right.$$

2.180 ODE No. 180

$$\left(xy'(x) - y(x)\right)\left(ax^2+bx+c\right) + x^2 - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.123975 (sec), leaf count = 132

$$\left\{\left\{y(x) \to -\frac{x\left(\exp\left(\frac{4\tan^{-1}\left(\frac{2ax}{\sqrt{4ac-b^2}}+\frac{b}{\sqrt{4ac-b^2}}\right)}{\sqrt{4ac-b^2}} + 2c_1\right) - 1\right)}{\exp\left(\frac{4\tan^{-1}\left(\frac{2ax}{\sqrt{4ac-b^2}}+\frac{b}{\sqrt{4ac-b^2}}\right)}{\sqrt{4ac-b^2}} + 2c_1\right) + 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 58

$$\left\{y(x) = -\tanh\left(1\left(\_C1\,\sqrt{4\,ac-b^2} + 2\,\arctan\left(\frac{2\,ax+b}{\sqrt{4\,ac-b^2}}\right)\right)\frac{1}{\sqrt{4\,ac-b^2}}\right)x\right\}$$

2.181 ODE No. 181

$$a + x^4\left(y'(x) + y(x)^2\right) = 0$$

✓ **Mathematica** : cpu = 0.0131417 (sec), leaf count = 347

$$\left\{\left\{y(x) \to -\frac{\frac{i\sqrt{\frac{2}{\pi}}c_1 \sinh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} + \frac{i\sqrt{-a}\left(-\frac{\sqrt{\frac{2}{\pi}}c_1\cosh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} + \frac{\sqrt{\frac{2}{\pi}}c_1\left(-\frac{\sqrt{-a}x\sinh\left(\frac{\sqrt{-a}}{x}\right)}{a} - \cosh\left(\frac{\sqrt{-a}}{x}\right)\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} - \frac{2\sqrt{\frac{2}{\pi}}\left(i\sinh\left(\frac{\sqrt{-a}}{x}\right) + \frac{i\sqrt{-a}x}{\sqrt{-\frac{i\sqrt{-a}}{x}}}\right.\right.\right.}{x}}{2x\left(\frac{\sqrt{\frac{2}{\pi}}\cosh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}} - \frac{i\sqrt{\frac{2}{\pi}}c_1\sinh\left(\frac{\sqrt{-a}}{x}\right)}{\sqrt{-\frac{i\sqrt{-a}}{x}}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 28

$$\left\{y(x) = \frac{1}{x^2}\left(-\tan\left(\frac{\_C1\,x - 1}{x}\sqrt{a}\right)\sqrt{a} + x\right)\right\}$$

2.182 ODE No. 182

$$\left(x^3 - 1\right)xy'(x) + x^2 - 2xy(x)^2 + y(x) = 0$$

✓ **Mathematica** : cpu = 0.174967 (sec), leaf count = 96

$$\left\{\left\{y(x) \to -\frac{\left(x^3-1\right)\left(\frac{2c_1x^2}{(1-x^3)^{5/3}} + \frac{x}{(1-x^3)^{2/3}} + \frac{x^4}{(1-x^3)^{5/3}}\right)}{2\left(\frac{c_1}{(1-x^3)^{2/3}} + \frac{x^2}{2(1-x^3)^{2/3}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.14 (sec), leaf count = 18

$$\left\{y(x) = \frac{x(x + \_C1)}{\_C1\,x^2 + 1}\right\}$$

2.183 ODE No. 183

$$\left(2x^4 - x\right) y'(x) - 2\left(x^3 - 1\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.0152635 (sec), leaf count = 22

$$\left\{\left\{y(x) \to \frac{c_1 x^2}{\sqrt[3]{1 - 2x^3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 18

$$\left\{y(x) = \_C1\, x^2 \frac{1}{\sqrt[3]{2\,x^3 - 1}}\right\}$$

2.184 ODE No. 184

$$\left(y'(x) + y(x)^2\right) \left(ax^2 + bx + c\right)^2 + A = 0$$

✓ **Mathematica** : cpu = 1.51556 (sec), leaf count = 704

$$\left\{\left\{y(x) \to -\frac{-\frac{2a\sqrt{ax^2+bx+c}\exp\left(-\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}}\tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}}\right)}{(b^2-4ac)\left(\frac{(2ax+b)^2}{4ac-b^2}+1\right)} + \frac{(2ax+b)\exp\left(-\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}}\tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}} \cdots\right.}{2\sqrt{b^2-4ac}\sqrt{1-\frac{4A}{b^2-4ac}}\sqrt{ax^2+bx+c}} \cdots}{c_1\sqrt{x(ax+b)+c}\left(-\exp\left(\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}}\tan^{-1} \cdots}{\sqrt{b^2-4ac}} \cdots\right.\right.}\right.\right.$$

✓ **Maple** : cpu = 0.385 (sec), leaf count = 493

$$\left\{y(x) = 2\frac{a}{\sqrt{-4\,ac+b^2}\left(2\,ax+b+i\sqrt{4\,ac-b^2}\right)\left(i\sqrt{4\,ac-b^2}-2\,ax-b\right)}\left(\left(i\sqrt{\frac{-4\,ac+b^2-4\,A}{a^2}}a\sqrt{4\,ac-b^2} \cdots\right.\right.\right.$$

2.185 ODE No. 185

$$x^7 y'(x) + 5x^3 y(x)^2 + 2\left(x^2+1\right) y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.384795 (sec), leaf count = 123

$$\text{Solve}\left[c_1 = \frac{\frac{1}{2}\sqrt[4]{1-\left(\frac{ix^2}{y(x)}+\frac{i}{x}\right)^2}\left(\frac{ix^2}{y(x)}+\frac{i}{x}\right)\,{}_2F_1\left(\frac{1}{2},\frac{5}{4};\frac{3}{2};\left(\frac{ix^2}{y(x)}+\frac{i}{x}\right)^2\right)+ix}{\sqrt[4]{-1+\left(\frac{ix^2}{y(x)}+\frac{i}{x}\right)^2}}, y(x)\right]$$

✓ **Maple** : cpu = 0.059 (sec), leaf count = 63

$$\left\{ \_C1 + x\frac{1}{\sqrt[4]{\left(x^{-1}+\frac{x^2}{y(x)}\right)^2+1}} + \frac{x^3+y(x)}{2\,xy\,(x)}\,{}_2\mathrm{F}_1\left(\frac{1}{2},\frac{5}{4};\ \frac{3}{2};\ -\frac{\left(x^3+y(x)\right)^2}{x^2\left(y\,(x)\right)^2}\right) = 0 \right\}$$

2.186 ODE No. 186

$$-(n-1)x^{n-1}y(x) + x^{2n-2} + x^n y'(x) + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0308476 (sec), leaf count = 19

$$\left\{\left\{y(x) \to x^{n-1}\tan\left(c_1 - \log(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 17

$$\left\{y(x) = \tan\left(-\ln\left(x\right) + \_C1\right)x^{n-1}\right\}$$

2.187 ODE No. 187

$$-ay(x)^2 - bx^{2n-2} + x^n y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0739011 (sec), leaf count = 328

$$\left\{\left\{y(x) \to -\frac{x^n\left(\frac{1}{2}\sqrt{a}\sqrt{b}c_1\left(-\frac{n-1}{\sqrt{a}\sqrt{b}}-\sqrt{\frac{(n-1)^2}{ab}-4}\right)x^{\frac{1}{2}\sqrt{a}\sqrt{b}\left(-\frac{n-1}{\sqrt{a}\sqrt{b}}-\sqrt{\frac{(n-1)^2}{ab}-4}\right)-1} + \frac{1}{2}\sqrt{a}\sqrt{b}\left(\sqrt{\frac{(n-1)^2}{ab}-4}-\right.\right.}{a\left(c_1 x^{\frac{1}{2}\sqrt{a}\sqrt{b}\left(-\frac{n-1}{\sqrt{a}\sqrt{b}}-\sqrt{\frac{(n-1)^2}{ab}-4}\right)} + x^{\frac{1}{2}\sqrt{a}\sqrt{b}\left(\sqrt{\frac{(n-1)^2}{ab}-4}-\frac{n-1}{\sqrt{a}\sqrt{b}}\right)}\right.}\right\}\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 60

$$\left\{y(x) = \frac{x^{n-1}}{2\,a}\left(-\sqrt{4\,ab-n^2+2\,n-1}\tan\left(\frac{-\ln(x)+\_C1}{2}\sqrt{4\,ab-n^2+2\,n-1}\right)+n-1\right)\right\}$$

2.188 ODE No. 188

$$-ay(x)^3 - bnx^3 + x^{2n+1}y'(x) = 0$$

✗ **Mathematica** : cpu = 21.0797 (sec), leaf count = 0 , could not solve

```
DSolve[-(b*n*x^3) - a*y[x]^3 + x^(1 + 2*n)*Derivative[1][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.028 (sec), leaf count = 32

$$\left\{y(x) = RootOf\left(-\ln(x) + \_C1 + \int^{\_Z}\left(\_a^3 a - n\_a + b\right)^{-1} d\_a\right)x^n\right\}$$

2.189 ODE No. 189

$$-ay(x)^n - bx^{(m+1)n} + x^{m(n-1)+n}y'(x) = 0$$

✓ **Mathematica** : cpu = 82.1576 (sec), leaf count = 90

$$\text{Solve}\left[\int_1^{y(x)\left(\frac{ax^{-(m+1)n}}{b}\right)^{\frac{1}{n}}} \frac{1}{-K[1]\left(\frac{b^{1-n}(m+1)^n}{a}\right)^{\frac{1}{n}} + K[1]^n + 1}\,dK[1] = bx^{m+1}\log(x)\left(\frac{ax^{-(m+1)n}}{b}\right)^{\frac{1}{n}} + c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.247 (sec), leaf count = 60

$$\left\{\int_{\_b}^{y(x)} -\frac{x^{mn}x^n}{\left(bx^m x-(m+1)\,\_a\right)x^n x^{mn}+a\,\_a^n x^m x}\,\mathrm{d}\_a + \ln(x) - \_C1 = 0\right\}$$

2.190 ODE No. 190

$$\sqrt{x^2-1}y'(x) - \sqrt{y(x)^2-1} = 0$$

✓ **Mathematica** : cpu = 0.0522019 (sec), leaf count = 55

$$\left\{\left\{y(x) \to \frac{1}{2}\left(-e^{-c_1}\sqrt{x^2-1} + e^{c_1}\sqrt{x^2-1} + e^{-c_1}x + e^{c_1}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 29

$$\left\{\ln\left(x+\sqrt{x^2-1}\right) - \ln\left(y(x)+\sqrt{(y(x))^2-1}\right) + \_C1 = 0\right\}$$

2.191 ODE No. 191

$$\sqrt{1-x^2}y'(x)-y(x)\sqrt{y(x)^2-1}=0$$

✓ **Mathematica** : cpu = 0.0321208 (sec), leaf count = 52

$$\left\{\left\{y(x)\to\sqrt{\tan^2\left(c_1+\sin^{-1}(x)\right)+1}\left(-\cot\left(c_1+\sin^{-1}(x)\right)\right)\right\},\left\{y(x)\to\sqrt{\tan^2\left(c_1+\sin^{-1}(x)\right)+1}\cot\left(c_1+\text{si}\right.\right.\right.$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 16

$$\left\{\arcsin\left(x\right)+\arctan\left(\frac{1}{\sqrt{\left(y\left(x\right)\right)^2-1}}\right)+\_C1=0\right\}$$

2.192 ODE No. 192

$$\sqrt{a^2+x^2}y'(x)-\sqrt{a^2+x^2}+y(x)+x=0$$

✓ **Mathematica** : cpu = 0.0301423 (sec), leaf count = 57

$$\left\{\left\{y(x)\to\frac{c_1}{\sqrt{a^2+x^2}+x}+\frac{a^2\log\left(\sqrt{a^2+x^2}+x\right)}{\sqrt{a^2+x^2}+x}\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 36

$$\left\{y(x)=1\left(a^2\ln\left(x+\sqrt{a^2+x^2}\right)+\_C1\right)\left(x+\sqrt{a^2+x^2}\right)^{-1}\right\}$$

2.193 ODE No. 193

$$-ax(\log(x)+1)+x\log(x)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.00946795 (sec), leaf count = 16

$$\left\{\left\{y(x)\to ax+\frac{c_1}{\log(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 14

$$\left\{y(x)=ax+\frac{\_C1}{\ln\left(x\right)}\right\}$$

2.194 ODE No. 194

$$x \log(x) y'(x) - y(x) \left(2 \log^2(x) + 1\right) - y(x)^2 \log(x) - \log^3(x) = 0$$

✓ **Mathematica** : cpu = 0.0777614 (sec), leaf count = 98

$$\left\{\left\{y(x) \to -\frac{x \left(\frac{c_1 e^{\frac{\log^2(x)}{2}} \log(x)}{x} + \frac{e^{\frac{\log^2(x)}{2}} \log(x)}{x} + \frac{e^{\frac{\log^2(x)}{2}} \log^3(x)}{2x}\right)}{c_1 e^{\frac{\log^2(x)}{2}} + \frac{1}{2} e^{\frac{\log^2(x)}{2}} \log^2(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.024 (sec), leaf count = 23

$$\left\{y(x) = -\frac{\ln(x) \left(\left(\ln(x)\right)^2 + \_C1 + 2\right)}{\left(\ln(x)\right)^2 + \_C1}\right\}$$

2.195 ODE No. 195

$$\sin(x) y'(x) + y(x)^2 \left(-\sin^2(x)\right) + y(x)(\cos(x) - 3\sin(x)) + 4 = 0$$

✓ **Mathematica** : cpu = 0.0590962 (sec), leaf count = 27

$$\left\{\left\{y(x) \to \frac{\csc(x)}{c_1 e^{5x} + \frac{1}{5}} - 4\csc(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.124 (sec), leaf count = 28

$$\left\{y(x) = \frac{-4 \left(\mathrm{e}^x\right)^5 \_C1 - 4}{\sin(x) \left(\left(\mathrm{e}^x\right)^5 \_C1 - 4\right)}\right\}$$

2.196 ODE No. 196

$$\cos(x) y'(x) + y(x) + (\sin(x) + 1)\cos(x) = 0$$

✓ **Mathematica** : cpu = 0.0576438 (sec), leaf count = 53

$$\left\{\left\{y(x) \to c_1 e^{-2\tanh^{-1}\left(\tan\left(\frac{x}{2}\right)\right)} + e^{-2\tanh^{-1}\left(\tan\left(\frac{x}{2}\right)\right)} \left(\sin(x) + 4\log\left(\cos\left(\frac{x}{2}\right) - \sin\left(\frac{x}{2}\right)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.153 (sec), leaf count = 29

$$\left\{y(x) = \frac{\sin(x) + 2\ln(\cos(x)) - 2\ln(\sec(x) + \tan(x)) + \_C1}{\sec(x) + \tan(x)}\right\}$$

2.197 ODE No. 197

$$\cos(x)y'(x) - y(x)^4 - y(x)\sin(x) = 0$$

✓ **Mathematica** : cpu = 0.0433765 (sec), leaf count = 98

$$\left\{\left\{y(x) \to \frac{1}{\sqrt[3]{c_1 \cos^3(x) - \sin(x) - 2\sin(x)\cos^2(x)}}\right\}, \left\{y(x) \to -\frac{\sqrt[3]{-1}}{\sqrt[3]{c_1 \cos^3(x) - \sin(x) - 2\sin(x)\cos^2(x)}}\right\}, \left\{y\right.\right.$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 237

$$\left\{y(x) = \frac{1}{\_C1\ (\sin(x))^4 + 2\cos(x)(\sin(x))^3 - 2\_C1\ (\sin(x))^2 - 3\cos(x)\sin(x) + \_C1} \sqrt[3]{\cos(x)\left(\_C1\ (\sin\right.}\right.$$

2.198 ODE No. 198

$$\sin(x)\cos(x)y'(x) - y(x) - \sin^3(x) = 0$$

✓ **Mathematica** : cpu = 0.0257794 (sec), leaf count = 15

$$\{\{y(x) \to c_1 \tan(x) - \sin(x)\}\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 13

$$\{y(x) = \tan(x)(-\cos(x) + \_C1)\}$$

2.199 ODE No. 199

$$\sin(2x)y'(x) + \sin(2y(x)) = 0$$

✓ **Mathematica** : cpu = 0.187382 (sec), leaf count = 15

$$\{\{y(x) \to \cot^{-1}\left(e^{-2c_1}\tan(x)\right)\}\}$$

✓ **Maple** : cpu = 0.165 (sec), leaf count = 102

$$\left\{y(x) = \frac{1}{2}\arctan\left(2\frac{\_C1\ (2\sin(2x) + \sin(4x))}{-\_C1^2\cos(4x) + \_C1^2 + 4\cos(2x) + \cos(4x) + 3}, \frac{\_C1^2\cos(4x) - \_C1^2 + 4\cos(2x)}{\_C1^2\cos(4x) - \_C1^2 - 4\cos(2x)}\right.\right.$$

2.200 ODE No. 200

$$Ax\left(a\sin^2(x)+c\right)+y'(x)\left(a\sin^2(x)+b\right)+ay(x)\sin(2x)=0$$

✓ **Mathematica** : cpu = 0.0528863 (sec), leaf count = 77

$$\left\{\left\{y(x)\to\frac{\frac{1}{2}aAx^2-\frac{1}{2}aAx\sin(2x)-\frac{1}{4}aA\cos(2x)+Acx^2}{a\cos(2x)-a-2b}+\frac{c_1}{a\cos(2x)-a-2b}\right\}\right\}$$

✓ **Maple** : cpu = 0.062 (sec), leaf count = 53

$$\left\{y(x)=\frac{-A\cos\left(2\,x\right)a-2\,A\sin\left(2\,x\right)ax+2\,x^2(a+2\,c)\,A-8\,\_C1}{4\,a\cos\left(2\,x\right)-4\,a-8\,b}\right\}$$

2.201 ODE No. 201

$$-y(x)f'(x)+2f(x)y'(x)+2f(x)y(x)^2-2f(x)^2=0$$

✓ **Mathematica** : cpu = 0.0803987 (sec), leaf count = 38

$$\left\{\left\{y(x)\to i\sqrt{f(x)}\tan\left(c_1+i\int_1^x-\sqrt{f(K[1])}\,dK[1]\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 23

$$\left\{y(x)=i\tan\left(-i\int\sqrt{f\left(x\right)}\,\mathrm{d}x+\_C1\right)\sqrt{f\left(x\right)}\right\}$$

2.202 ODE No. 202

$$f(x)y'(x)+g(x)\mathrm{tg}(y(x))+h(x)=0$$

✗ **Mathematica** : cpu = 20.5751 (sec), leaf count = 0 , could not solve

```
DSolve[h[x] + g[x]*tg[y[x]] + f[x]*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(f(x)*diff(y(x),x)+g(x)*tg(y(x))+h(x) = 0,y(x))
```

2.203 ODE No. 203

$$x^3 + y(x)y'(x) + y(x) = 0$$

✗ **Mathematica** : cpu = 3.35894 (sec), leaf count = 0 , could not solve

```
DSolve[x^3 + y[x] + y[x]*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(y(x)*diff(y(x),x)+y(x)+x^3 = 0,y(x))
```

2.204 ODE No. 204

$$ay(x) + y(x)y'(x) + x = 0$$

✓ **Mathematica** : cpu = 0.0708056 (sec), leaf count = 70

$$\text{Solve}\left[\frac{1}{2}\log\left(\frac{ay(x)}{x} + \frac{y(x)^2}{x^2} + 1\right) - \frac{a\tan^{-1}\left(\frac{a+\frac{2y(x)}{x}}{\sqrt{4-a^2}}\right)}{\sqrt{4-a^2}} = c_1 - \log(x), y(x)\right]$$

✓ **Maple** : cpu = 0.316 (sec), leaf count = 91

$$\left\{y(x) = RootOf\left(\_Z^2 - \mathrm{e}^{RootOf\left(x^2\left(-\left(\tanh\left(\frac{2\_C1+\_Z+2\ln(x)}{2a}\sqrt{(a-2)(a+2)}\right)\right)^2 a^2+4\left(\tanh\left(1/2\ \frac{\sqrt{(a-2)(a+2)}(2\_C1+\_Z+2\ln(x))}{a}\right.\right.\right.\right.\right.$$

2.205 ODE No. 205

$$\frac{1}{4}\left(a^2-1\right)x + ay(x) + bx^n + y(x)y'(x) = 0$$

✗ **Mathematica** : cpu = 25.8469 (sec), leaf count = 0 , could not solve

```
DSolve[((-1 + a^2)*x)/4 + b*x^n + a*y[x] + y[x]*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(y(x)*diff(y(x),x)+a*y(x)+1/4*(a^2-1)*x+b*x^n = 0,y(x))
```

2.206 ODE No. 206

$$ay(x) - 2a + be^x + y(x)y'(x) = 0$$

✗ **Mathematica** : cpu = 30.2388 (sec), leaf count = 0 , could not solve

```
DSolve[-2*a + b*E^x + a*y[x] + y[x]*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(y(x)*diff(y(x),x)+a*y(x)+b*exp(x)-2*a = 0,y(x))
```

2.207 ODE No. 207

$$y(x)y'(x) + y(x)^2 + 4x(x+1) = 0$$

✓ **Mathematica** : cpu = 0.0130514 (sec), leaf count = 47

$$\left\{\left\{y(x) \to -\sqrt{c_1 e^{-2x} - 4x^2}\right\}, \left\{y(x) \to \sqrt{c_1 e^{-2x} - 4x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 37

$$\left\{y(x) = \sqrt{\mathrm{e}^{-2x}\_C1 - 4x^2}, y(x) = -\sqrt{\mathrm{e}^{-2x}\_C1 - 4x^2}\right\}$$

2.208 ODE No. 208

$$ay(x)^2 - b\cos(c+x) + y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0724679 (sec), leaf count = 118

$$\left\{\left\{y(x) \to -\frac{\sqrt{4a^2c_1e^{-2ax} + 4ab\cos(c+x) + c_1e^{-2ax} + 2b\sin(c+x)}}{\sqrt{4a^2+1}}\right\}, \left\{y(x) \to \frac{\sqrt{4a^2c_1e^{-2ax} + 4ab\cos(c+x}}{\sqrt{4a^2}}\right.\right.$$

✓ **Maple** : cpu = 0.073 (sec), leaf count = 106

$$\left\{y(x) = \frac{1}{4a^2+1}\sqrt{16\left(a^2+1/4\right)^2\_C1\,\mathrm{e}^{-2ax} + 16\left(\cos(x+c)a + 1/2\sin(x+c)\right)\left(a^2+1/4\right)b}, y(x) = -\frac{1}{4a^2+}\right.$$

2.209 ODE No. 209

$$y(x)y'(x) - \sqrt{ay(x)^2 + b} = 0$$

✓ **Mathematica** : cpu = 0.022736 (sec), leaf count = 84

$$\left\{\left\{y(x) \to -\frac{\sqrt{2a^2c_1x + a^2c_1^2 + a^2x^2 - b}}{\sqrt{a}}\right\}, \left\{y(x) \to \frac{\sqrt{2a^2c_1x + a^2c_1^2 + a^2x^2 - b}}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 21

$$\left\{x - \frac{1}{a}\sqrt{a\left(y\left(x\right)\right)^2 + b} + \_C1 = 0\right\}$$

2.210 ODE No. 210

$$y(x)y'(x) + xy(x)^2 - 4x = 0$$

✓ **Mathematica** : cpu = 0.0174381 (sec), leaf count = 47

$$\left\{\left\{y(x) \to -\sqrt{e^{2c_1 - x^2} + 4}\right\}, \left\{y(x) \to \sqrt{e^{2c_1 - x^2} + 4}\right\}\right\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 33

$$\left\{y(x) = \sqrt{\mathrm{e}^{-x^2}\_C1 + 4}, y(x) = -\sqrt{\mathrm{e}^{-x^2}\_C1 + 4}\right\}$$

2.211 ODE No. 211

$$y(x)y'(x) - xe^{\frac{x}{y(x)}} = 0$$

✓ **Mathematica** : cpu = 38.8549 (sec), leaf count = 40

$$\text{Solve}\left[\int_1^{\frac{y(x)}{x}} \frac{K[1]}{K[1]^2 - e^{\frac{1}{K[1]}}}\, dK[1] = c_1 - \log(x), y(x)\right]$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 31

$$\left\{y(x) = RootOf\left(-\int^{\_Z} \frac{\_a}{-\_a^2 + \mathrm{e}^{-a^{-1}}} d\_a + \ln\left(x\right) + \_C1\right) x\right\}$$

2.212 ODE No. 212

$$g(x)f\left(x^2+y(x)^2\right)+y(x)y'(x)+x=0$$

✓ **Mathematica** : cpu = 22.607 (sec), leaf count = 92

$$\text{Solve}\left[\int_1^{y(x)}\left(\frac{K[2]}{f\left(K[2]^2+x^2\right)}-\int_1^x-\frac{2K[1]K[2]f'\left(K[1]^2+K[2]^2\right)}{f\left(K[1]^2+K[2]^2\right)^2}\,dK[1]\right)dK[2]+\int_1^x\left(\frac{K[1]}{f\left(K[1]^2+y(x)^2\right)}+g\right.\right.$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 30

$$\left\{\int_{\_b}^{y(x)}\frac{\_a}{f\left(\_a^2+x^2\right)}\,\mathrm{d}\_a+\int g(x)\,\mathrm{d}x-\_C1=0\right\}$$

2.213 ODE No. 213

$$(y(x)+1)y'(x)-y(x)-x=0$$

✓ **Mathematica** : cpu = 0.101442 (sec), leaf count = 71

$$\text{Solve}\left[\frac{1}{2}\log\left(\frac{x^2-y(x)^2+(x-3)y(x)-x-1}{(x-1)^2}\right)+\log(1-x)=c_1+\frac{\tanh^{-1}\left(\frac{y(x)+2x-1}{\sqrt{5}(y(x)+1)}\right)}{\sqrt{5}},y(x)\right]$$

✓ **Maple** : cpu = 0.713 (sec), leaf count = 66

$$\left\{-\frac{1}{2}\ln\left(\frac{\left(y(x)\right)^2+\left(-x+3\right)y(x)-x^2+x+1}{\left(x-1\right)^2}\right)-\frac{\sqrt{5}}{5}\mathit{Artanh}\left(\frac{\left(-2\,y(x)-3+x\right)\sqrt{5}}{5\,x-5}\right)-\ln\left(x-1\right)-\_C1=0\right.$$

2.214 ODE No. 214

$$(y(x)+x-1)y'(x)-y(x)+2x+3=0$$

✓ **Mathematica** : cpu = 0.110321 (sec), leaf count = 78

$$\text{Solve}\left[2\sqrt{2}\tan^{-1}\left(\frac{-y(x)+2x+3}{\sqrt{2}(y(x)+x-1)}\right)=3c_1+2\log\left(\frac{6x^2+3y(x)^2-10y(x)+8x+11}{(3x+2)^2}\right)+4\log(3x+2),y(x)\right]$$

✓ **Maple** : cpu = 0.161 (sec), leaf count = 48

$$\left\{y(x)=\frac{5}{3}+\frac{\left(-3\,x-2\right)\sqrt{2}\tan\left(\mathit{RootOf}\left(\sqrt{2}\ln\left(2\left(\left(\tan\left(\_Z\right)\right)^2+1\right)\left(3\,x+2\right)^2\right)+2\sqrt{2}\_C1-2\,\_Z\right)\right)}{3}\right\}$$

2.215 ODE No. 215

$$(y(x)+2x-2)y'(x)-y(x)+x+1=0$$

✓ **Mathematica** : cpu = 0.120879 (sec), leaf count = 80

$$\text{Solve}\left[6\sqrt{3}\tan^{-1}\left(\frac{4-3y(x)}{\sqrt{3}(y(x)+2x-2)}\right)=2c_1+3\log\left(\frac{3x^2+3y(x)^2+3(x-3)y(x)-6x+7}{(1-3x)^2}\right)+6\log(3x-1),\right.$$

✓ **Maple** : cpu = 0.184 (sec), leaf count = 51

$$\left\{y(x)=\frac{3}{2}-\frac{x}{2}+\frac{\sqrt{3}(3x-1)}{6}\tan\left(RootOf\left(\sqrt{3}\ln\left(\frac{\left(3\left(\tan\left(\_Z\right)\right)^2+3\right)(3x-1)^2}{4}\right)+2\sqrt{3}\_C1+6\_Z\right)\right)\right.$$

2.216 ODE No. 216

$$(y(x)-2x+1)y'(x)+y(x)+x=0$$

✓ **Mathematica** : cpu = 0.101923 (sec), leaf count = 82

$$\text{Solve}\left[6\sqrt{3}\tan^{-1}\left(\frac{3y(x)+1}{\sqrt{3}(-y(x)+2x-1)}\right)=2c_1+3\log\left(\frac{3x^2+3y(x)^2-3(x-1)y(x)-3x+1}{(1-3x)^2}\right)+6\log(3x-1\right.$$

✓ **Maple** : cpu = 0.174 (sec), leaf count = 51

$$\left\{y(x)=\frac{(-3x+1)\sqrt{3}}{6}\tan\left(RootOf\left(\sqrt{3}\ln\left(\frac{\left(3\left(\tan\left(\_Z\right)\right)^2+3\right)(3x-1)^2}{4}\right)+2\sqrt{3}\_C1+6\_Z\right)\right)+\frac{x}{2}-\right.$$

2.217 ODE No. 217

$$\left(y(x)-x^2\right)y'(x)-x=0$$

✓ **Mathematica** : cpu = 0.0199003 (sec), leaf count = 29

$$\left\{\left\{y(x)\to\frac{1}{2}\left(W\left(-e^{c_1-2x^2-1}\right)+1\right)+x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 23

$$\left\{y(x)=x^2+\frac{lambertW\left(-4\_C1\,\mathrm{e}^{-2x^2-1}\right)}{2}+\frac{1}{2}\right\}$$

2.218 ODE No. 218

$$\left(y(x)-x^2\right)y'(x)+4xy(x)=0$$

✓ **Mathematica** : cpu = 0.10133 (sec), leaf count = 257

$$\left\{\left\{y(x)\to x^2+\frac{1}{-\frac{1}{2x^2}-\frac{\frac{1}{2}-\frac{i}{2}}{\sqrt{2}x^2\sqrt{x^2\sinh\left(\frac{2c_1}{9}\right)+x^2\cosh\left(\frac{2c_1}{9}\right)-i}}}\right\},\left\{y(x)\to x^2+\frac{1}{-\frac{1}{2x^2}+\frac{\frac{1}{2}-\frac{i}{2}}{\sqrt{2}x^2\sqrt{x^2\sinh\left(\frac{2c_1}{9}\right)+x^2\cosh\left(\frac{2c_1}{9}\right)}}}\right\}\right.$$

✓ **Maple** : cpu = 0.203 (sec), leaf count = 57

$$\left\{y(x)=-\frac{\_C1}{2}\sqrt{\_C1^2-4x^2}+\frac{\_C1^2}{2}-x^2,y(x)=\frac{\_C1}{2}\sqrt{\_C1^2-4x^2}+\frac{\_C1^2}{2}-x^2\right\}$$

2.219 ODE No. 219

$$-\mathrm{f0}(x)-\mathrm{f1}(x)y(x)-\mathrm{f2}(x)y(x)^2+(g(x)+y(x))y'(x)=0$$

✗ **Mathematica** : cpu = 300.975 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((y(x)+g(x))*diff(y(x),x)-f2(x)*y(x)^2-f1(x)*y(x)-f0(x) = 0,y(x))
```

2.220 ODE No. 220

$$-x^3+2y(x)y'(x)-xy(x)^2=0$$

✓ **Mathematica** : cpu = 0.01505 (sec), leaf count = 57

$$\left\{\left\{y(x)\to-\sqrt{c_1e^{\frac{x^2}{2}}-x^2-2}\right\},\left\{y(x)\to\sqrt{c_1e^{\frac{x^2}{2}}-x^2-2}\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 43

$$\left\{y(x)=\sqrt{\mathrm{e}^{\frac{x^2}{2}}\_C1-x^2-2},y(x)=-\sqrt{\mathrm{e}^{\frac{x^2}{2}}\_C1-x^2-2}\right\}$$

2.221 ODE No. 221

$$(2y(x)+x+1)y'(x)-2y(x)-x+1=0$$

✓ **Mathematica** : cpu = 0.0191212 (sec), leaf count = 35

$$\left\{\left\{y(x)\to \frac{2}{3}\left(W\left(-e^{c_1+\frac{9x}{4}-1}\right)+1\right)+\frac{1}{2}(-x-1)\right\}\right\}$$

✓ **Maple** : cpu = 0.051 (sec), leaf count = 21

$$\left\{y(x)=-\frac{x}{2}+\frac{2}{3}lambertW\left(\frac{\mathrm{e}^{-\frac{1}{4}}\_C1}{4}\mathrm{e}^{\frac{9x}{4}}\right)+\frac{1}{6}\right\}$$

2.222 ODE No. 222

$$(2y(x)+x+7)y'(x)-y(x)+2x+4=0$$

✓ **Mathematica** : cpu = 0.0591141 (sec), leaf count = 65

$$\text{Solve}\left[5c_1+2\log\left(\frac{4\left(x^2+y(x)^2+4y(x)+6x+13\right)}{5(x+3)^2}\right)+2\tan^{-1}\left(\frac{y(x)-2(x+2)}{2y(x)+x+7}\right)+4\log(x+3)=0,y(x)\right]$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 32

$$\left\{y(x)=-2+(-x-3)\tan\left(RootOf\left(-\_Z+\ln\left(\left(\cos\left(\_Z\right)\right)^{-2}\right)+2\ln\left(x+3\right)+2\_C1\right)\right)\right\}$$

2.223 ODE No. 223

$$(2y(x)-x)y'(x)-y(x)-2x=0$$

✓ **Mathematica** : cpu = 0.0269815 (sec), leaf count = 55

$$\left\{\left\{y(x)\to \frac{1}{2}\left(x-\sqrt{5x^2-4e^{c_1}}\right)\right\},\left\{y(x)\to \frac{1}{2}\left(\sqrt{5x^2-4e^{c_1}}+x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.169 (sec), leaf count = 51

$$\left\{y(x)=\frac{1}{2\_C1}\left(\_C1\,x-\sqrt{5\,\_C1^2x^2+4}\right),y(x)=\frac{1}{2\_C1}\left(\_C1\,x+\sqrt{5\,\_C1^2x^2+4}\right)\right\}$$

2.224 ODE No. 224

$$(2y(x)-6x)y'(x)-y(x)+3x+2=0$$

✓ **Mathematica** : cpu = 0.019939 (sec), leaf count = 29

$$\left\{\left\{y(x)\to 3x-\frac{2}{5}\left(W\left(-e^{c_1+\frac{25x}{4}-1}\right)+1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 35

$$\left\{y(x)=\frac{1}{5}\mathrm{e}^{-lambertW\left(-\frac{\mathrm{e}^{-1}}{2}\mathrm{e}^{\frac{25x}{4}}\mathrm{e}^{-\frac{25\_C1}{4}}\right)+\frac{25x}{4}-1-\frac{25\_C1}{4}}+3x-\frac{2}{5}\right\}$$

2.225 ODE No. 225

$$(4y(x)+2x+3)y'(x)-2y(x)-x-1=0$$

✓ **Mathematica** : cpu = 0.0186956 (sec), leaf count = 33

$$\left\{\left\{y(x)\to \frac{1}{8}\left(W\left(-e^{c_1+8x-1}\right)+1\right)+\frac{1}{4}(-2x-3)\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 20

$$\left\{y(x)=-\frac{x}{2}+\frac{lambertW\left(\mathrm{e}^{5}(\mathrm{e}^{x})^{8}\_C1\right)}{8}-\frac{5}{8}\right\}$$

2.226 ODE No. 226

$$(4y(x)-2x-3)y'(x)+2y(x)-x-1=0$$

✓ **Mathematica** : cpu = 0.0179577 (sec), leaf count = 35

$$\left\{\left\{y(x)\to \frac{1}{8}\left(-W\left(-e^{c_1+8x-1}\right)-1\right)+\frac{1}{4}(2x+3)\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 21

$$\left\{y(x)=\frac{x}{2}-\frac{lambertW\left(-\mathrm{e}^{5}(\mathrm{e}^{x})^{8}\_C1\right)}{8}+\frac{5}{8}\right\}$$

2.227 ODE No. 227

$$(4y(x)-3x-5)y'(x)-3y(x)+7x+2=0$$

✓ **Mathematica** : cpu = 0.0133797 (sec), leaf count = 107

$$\left\{\left\{y(x)\to \frac{1}{4}(3x+5)-\frac{1}{2}i\sqrt{-4c_1-2\left(-\frac{7x^2}{2}-2x\right)-\frac{1}{4}(3x+5)^2}\right\},\left\{y(x)\to \frac{1}{4}(3x+5)+\frac{1}{2}i\sqrt{-4c_1-2\left(-\frac{7}{}\right.}\right.$$

✓ **Maple** : cpu = 0.183 (sec), leaf count = 33

$$\left\{y(x)=\frac{1}{76\_C1}\left(-\sqrt{4-6859\left(x-\frac{7}{19}\right)^2\_C1^2}+(57x+95)\_C1\right)\right\}$$

2.228 ODE No. 228

$$(4y(x)+11x-11)y'(x)-25y(x)-8x+62=0$$

✓ **Mathematica** : cpu = 0.295637 (sec), leaf count = 3357

$$\left\{\left\{y(x)\to \frac{}{4\left(-\frac{}{81(9x-1)\left(81\cosh\left(\frac{3c_1}{8}\right)x^2+81\sinh\left(\frac{3c_1}{8}\right)x^2-18\cosh\left(\frac{3c_1}{8}\right)x-18\sinh\left(\frac{3c_1}{8}\right)x+\cosh\left(\frac{3c_1}{8}\right)+\sinh\left(\frac{3c_1}{8}\right)-1\right)\sqrt[3]{-25828032}}\right.}\right.$$

✓ **Maple** : cpu = 0.329 (sec), leaf count = 271

$$\left\{y(x)=1\left((-76x+28)\sqrt[3]{64-8748\,(9x-1)^2\_C1+108\sqrt{43046721}\sqrt{\_C1\,(x-1/9)^2\left(-\frac{32}{177147}+(x-1/\right.}}\right.\right.$$

2.229 ODE No. 229

$$(12y(x)-5x-8)y'(x)-5y(x)+2x+3=0$$

✓ **Mathematica** : cpu = 0.0131967 (sec), leaf count = 121

$$\left\{\left\{y(x)\to \frac{1}{12}(5x+8)-\frac{i\sqrt{-12c_1-24\left(-\frac{x^2}{12}-\frac{x}{4}\right)-\frac{1}{12}(5x+8)^2}}{2\sqrt{3}}\right\},\left\{y(x)\to \frac{1}{12}(5x+8)+\frac{i\sqrt{-12c_1-24\left(-\right.}\right.\right.$$

✓ **Maple** : cpu = 0.174 (sec), leaf count = 32

$$\left\{y(x)=\frac{1}{12\_C1}\left(-\sqrt{(x+4)^2\_C1^2+24}+(5x+8)\_C1\right)\right\}$$

2.230 ODE No. 230

$$ay(x)y'(x)+by(x)^2+f(x)=0$$

✓ **Mathematica** : cpu = 0.122812 (sec), leaf count = 96

$$\left\{\left\{y(x)\to -e^{-\frac{bx}{a}}\sqrt{2\int_1^x -\frac{f(K[1])e^{\frac{2bK[1]}{a}}}{a}\,dK[1]+c_1}\right\},\left\{y(x)\to e^{-\frac{bx}{a}}\sqrt{2\int_1^x -\frac{f(K[1])e^{\frac{2bK[1]}{a}}}{a}\,dK[1]+c_1}\right\}\right\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 100

$$\left\{y(x)=\frac{1}{a}\sqrt{e^{2\frac{bx}{a}}a\left(\_C1\,a-2\int\left(e^{\frac{bx}{a}}\right)^2 f(x)\,dx\right)}\left(e^{2\frac{bx}{a}}\right)^{-1},y(x)=-\frac{1}{a}\sqrt{e^{2\frac{bx}{a}}a\left(\_C1\,a-2\int\left(e^{\frac{bx}{a}}\right)^2 f(x)\,d\right.}\right.$$

2.231 ODE No. 231

$$y'(x)(ay(x)+bx+c)+\alpha y(x)+\beta x+\gamma=0$$

✓ **Mathematica** : cpu = 2.54782 (sec), leaf count = 252

$$\text{Solve}\left[\frac{(\alpha-b)^2\left(-\log\left(\frac{(ay(x)+bx+c)^2\left(-\frac{(\alpha(bx+c)-a(\beta x+\gamma))\left(a(\alpha-b)y(x)+a(\beta x+\gamma)+b^2(-x)-bc\right)}{(ay(x)+bx+c)^2}+a\beta-\alpha b\right)}{(\alpha(bx+c)-a(\beta x+\gamma))^2}\right)\right)-2\tan^{-1}\left(\frac{\frac{2(a(\beta x+\gamma)-\alpha}{ay(x)+bx}}{(\alpha-b)\sqrt{\frac{4(}{(}}\right.}{2(a\beta-\alpha b)}\right.$$

✓ **Maple** : cpu = 0.215 (sec), leaf count = 178

$$\left\{y(x)=\frac{1}{-a\beta+b\alpha}\left(-b\gamma+\beta\,c+\frac{x(a\beta-b\alpha)+a\gamma-\alpha\,c}{2\,a}\left(\sqrt{4\,a\beta-\alpha^2-2\,b\alpha-b^2}\tan\left(RootOf\left(\sqrt{4\,a\beta-\alpha^2-\right.\right.\right.\right.$$

2.232 ODE No. 232

$$x^2+xy(x)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0104289 (sec), leaf count = 56

$$\left\{\left\{y(x)\to-\frac{\sqrt{2c_1-x^4}}{\sqrt{2}x}\right\},\left\{y(x)\to\frac{\sqrt{2c_1-x^4}}{\sqrt{2}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 39

$$\left\{y(x)=-\frac{1}{2\,x}\sqrt{-2\,x^4+4\_C1},y(x)=\frac{1}{2\,x}\sqrt{-2\,x^4+4\_C1}\right\}$$

2.233 ODE No. 233

$$ax^3\cos(x)+xy(x)y'(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0245538 (sec), leaf count = 38

$$\left\{\left\{y(x)\to-x\sqrt{c_1-2a\sin(x)}\right\},\left\{y(x)\to x\sqrt{c_1-2a\sin(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 30

$$\left\{y(x)=\sqrt{-2\,a\sin\left(x\right)+\_C1}\,x,y(x)=-\sqrt{-2\,a\sin\left(x\right)+\_C1}\,x\right\}$$

2.234 ODE No. 234

$$x^3 - 2x^2 + xy(x)y'(x) + xy(x) - y(x)^2 = 0$$

✗ **Mathematica** : cpu = 29.1916 (sec), leaf count = 0 , could not solve

```
DSolve[-2*x^2 + x^3 + x*y[x] - y[x]^2 + x*y[x]*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x*y(x)*diff(y(x),x)-y(x)^2+x*y(x)+x^3-2*x^2 = 0,y(x))
```

2.235 ODE No. 235

$$(a + xy(x))y'(x) + by(x) = 0$$

✓ **Mathematica** : cpu = 0.0432456 (sec), leaf count = 40

$$\text{Solve}\left[x = c_1 e^{-\frac{y(x)}{b}} - \frac{a e^{-\frac{y(x)}{b}} \text{Ei}\left(\frac{y(x)}{b}\right)}{b}, y(x)\right]$$

✓ **Maple** : cpu = 0.051 (sec), leaf count = 30

$$\left\{ \_C1 + \left(-\mathrm{e}^{\frac{y(x)}{b}} bx + aEi\left(1, -\frac{y(x)}{b}\right)\right)^{-1} = 0 \right\}$$

2.236 ODE No. 236

$$x(y(x) + 4)y'(x) - y(x)^2 - 2y(x) - 2x = 0$$

✓ **Mathematica** : cpu = 0.0174829 (sec), leaf count = 114

$$\left\{ \left\{ y(x) \to \frac{1}{x\left(\frac{1}{x^2+4x} - \frac{e^{-2\left(\frac{\log(x)}{4} + \frac{3}{4}\log(x+4)\right)}}{\sqrt{c_1 - \frac{4}{x+4}}}\right)} - 4 \right\}, \left\{ y(x) \to \frac{1}{x\left(\frac{e^{-2\left(\frac{\log(x)}{4} + \frac{3}{4}\log(x+4)\right)}}{\sqrt{c_1 - \frac{4}{x+4}}} + \frac{1}{x^2+4x}\right)} - 4 \right\} \right\}$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 141

$$\left\{ y(x) = 1\left(-(x+4)^{\frac{3}{2}} \sqrt{\frac{\_C1\ (x+4) - 4}{x+4}} x - 16\sqrt{x} - 4x^{3/2}\right)\left(-(x+4)^{\frac{3}{2}} \sqrt{\frac{\_C1\ (x+4) - 4}{x+4}} + 4\sqrt{x} + x^{\frac{3}{2}}\right)^{-}\right.$$

2.237 ODE No. 237

$$x(a+y(x))y'(x)+by(x)+cx=0$$

✗ **Mathematica** : cpu = 8.42918 (sec), leaf count = 0 , could not solve

```
DSolve[c*x + b*y[x] + x*(a + y[x])*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x*(y(x)+a)*diff(y(x),x)+b*y(x)+c*x = 0,y(x))
```

2.238 ODE No. 238

$$(a+x(y(x)+x))y'(x)-b-y(x)(y(x)+x)=0$$

✓ **Mathematica** : cpu = 0.045073 (sec), leaf count = 192

$$\left\{\left\{y(x)\to \frac{1}{x\left(-\frac{x}{(a^2+ax^2+bx^2)^{3/2}\sqrt{c_1-\frac{1}{(a+b)\left(a^2+ax^2+bx^2\right)}}}-\frac{a}{-a^2-ax^2-bx^2}\right)}-\frac{a+x^2}{x}\right\},\left\{y(x)\to \frac{1}{x\left(\frac{}{(a^2+ax^2+bx^2)^{3/2}}\right.}\right.$$

✓ **Maple** : cpu = 0.08 (sec), leaf count = 91

$$\left\{y(x)=\frac{1}{\_C1\,a^2-1}\left(\_C1\,abx+x-\sqrt{\left(-1+\left(ax^2+bx^2+a^2\right)\_C1\right)(a+b)}\right),y(x)=\frac{1}{\_C1\,a^2-1}\left(\_C1\,abx+\right.\right.$$

2.239 ODE No. 239

$$\left(xy(x)-x^2\right)y'(x)-2x^2-3xy(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0298332 (sec), leaf count = 54

$$\left\{\left\{y(x)\to x-\frac{\sqrt{e^{2c_1}+2x^4}}{x}\right\},\left\{y(x)\to \frac{\sqrt{e^{2c_1}+2x^4}}{x}+x\right\}\right\}$$

✓ **Maple** : cpu = 0.176 (sec), leaf count = 59

$$\left\{y(x)=\frac{1}{\_C1\,x}\left(x^2\_C1-\sqrt{2\,x^4\_C1^2+1}\right),y(x)=\frac{1}{\_C1\,x}\left(x^2\_C1+\sqrt{2\,x^4\_C1^2+1}\right)\right\}$$

2.240 ODE No. 240

$$ax + 2xy(x)y'(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0102593 (sec), leaf count = 41

$$\left\{\left\{y(x) \to -\sqrt{c_1 x - ax\log(x)}\right\}, \left\{y(x) \to \sqrt{c_1 x - ax\log(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 34

$$\left\{y(x) = \sqrt{-ax\ln(x) + \_C1\, x}, y(x) = -\sqrt{-x\left(a\ln(x) - \_C1\right)}\right\}$$

2.241 ODE No. 241

$$ax^2 + 2xy(x)y'(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0105213 (sec), leaf count = 41

$$\left\{\left\{y(x) \to -\sqrt{c_1 x - ax^2}\right\}, \left\{y(x) \to \sqrt{c_1 x - ax^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 33

$$\left\{y(x) = \sqrt{-ax^2 + \_C1\, x}, y(x) = -\sqrt{-ax^2 + \_C1\, x}\right\}$$

2.242 ODE No. 242

$$2xy(x)y'(x) + 2y(x)^2 + 1 = 0$$

✓ **Mathematica** : cpu = 0.015594 (sec), leaf count = 60

$$\left\{\left\{y(x) \to -\frac{\sqrt{e^{4c_1} - x^2}}{\sqrt{2}x}\right\}, \left\{y(x) \to \frac{\sqrt{e^{4c_1} - x^2}}{\sqrt{2}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.015 (sec), leaf count = 39

$$\left\{y(x) = -\frac{1}{2\,x}\sqrt{-2\,x^2 + 4\,\_C1}, y(x) = \frac{1}{2\,x}\sqrt{-2\,x^2 + 4\,\_C1}\right\}$$

2.243 ODE No. 243

$$x(2y(x)+x-1)y'(x)-y(x)(y(x)+2x+1)=0$$

✓ **Mathematica** : cpu = 14.9299 (sec), leaf count = 487

$$\left\{\left\{y(x)\to -\frac{\sqrt[3]{2}x}{\sqrt[3]{-27c_1^2x^2+\sqrt{108c_1^3x^3+\left(27c_1^2x-27c_1^2x^2\right)^2}+27c_1^2x}}+\frac{\sqrt[3]{-27c_1^2x^2+\sqrt{108c_1^3x^3+(27c_1^2x-27c_1^2}}}{3\sqrt[3]{2}c_1}\right.\right.$$

✓ **Maple** : cpu = 0.137 (sec), leaf count = 391

$$\left\{y(x)=\frac{1}{80\_C1}\left(3\left(x\left(\sqrt{5}\sqrt{\frac{80\,(x-1)^2\_C1-x}{\_C1}}+20\,x-20\right)\_C1^2\right)^{2/3}\left(i\sqrt{3}-1\right)\sqrt[3]{5}-3\_C1\left(\left(1+i\sqrt{\right.}\right.\right.\right.$$

2.244 ODE No. 244

$$x(2y(x)-x-1)y'(x)+(-y(x)+2x-1)y(x)=0$$

✓ **Mathematica** : cpu = 14.8962 (sec), leaf count = 484

$$\left\{\left\{y(x)\to -\frac{\sqrt[3]{2}x}{\sqrt[3]{27c_1^2x^2+\sqrt{\left(27c_1^2x^2+27c_1^2x\right)^2-108c_1^3x^3}+27c_1^2x}}-\frac{\sqrt[3]{27c_1^2x^2+\sqrt{\left(27c_1^2x^2+27c_1^2x\right)^2-108c_1^3x}}}{3\sqrt[3]{2}c_1}\right.\right.$$

✓ **Maple** : cpu = 0.12 (sec), leaf count = 391

$$\left\{y(x)=\frac{3}{80\_C1}\left(\left(x\left(\sqrt{5}\sqrt{\frac{80\,(1+x)^2\_C1-x}{\_C1}}-20\,x-20\right)\_C1^2\right)^{\frac{2}{3}}\left(i\sqrt{3}-1\right)\sqrt[3]{5}-\left(\left(1+i\sqrt{3}\right)x5^{\frac{2}{3}}+\right.\right.\right.$$

2.245 ODE No. 245

$$\left(4x^3+2xy(x)\right)y'(x)+112x^2y(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.405662 (sec), leaf count = 1453

$$\left\{\left\{y(x)\to \text{Root}\left[-1521681143169024\#1x^{22}-697437190619136\#1^2x^{20}-145299414712320\#1^3x^{18}-18162426\right.\right.$$

✓ **Maple** : cpu = 0.322 (sec), leaf count = 31

$$\left\{y(x)=\frac{\_C1}{x^{28}\left(RootOf\left(x^{30}\_Z^{360}-24\,x^{30}\_Z^{330}-\_C1\right)\right)^{330}}\right\}$$

2.246 ODE No. 246

$$x(3y(x)+2x)y'(x)+3(y(x)+x)^2=0$$

✓ **Mathematica** : cpu = 0.0321387 (sec), leaf count = 80

$$\left\{\left\{y(x)\to \frac{1}{6}\left(-\frac{\sqrt{2}\sqrt{3e^{4c_1}-x^4}}{x}-4x\right)\right\},\left\{y(x)\to \frac{1}{6}\left(\frac{\sqrt{2}\sqrt{3e^{4c_1}-x^4}}{x}-4x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.168 (sec), leaf count = 63

$$\left\{y(x)=\frac{1}{6\,\_C1\,x}\left(-4\,x^2\_C1-\sqrt{-2\,x^4\_C1^{\,2}+6}\right),y(x)=\frac{1}{6\,\_C1\,x}\left(-4\,x^2\_C1+\sqrt{-2\,x^4\_C1^{\,2}+6}\right)\right\}$$

2.247 ODE No. 247

$$-7x^2+(3x+2)(y(x)-2x-1)y'(x)+xy(x)-y(x)^2-9x-3=0$$

✓ **Mathematica** : cpu = 14.8744 (sec), leaf count = 693

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{\sqrt{\left(-324e^{2c_1}x-216e^{2c_1}+1458x^3+2916x^2+1944x+432\right)^2+4\left(-81x^2-108x-36\right)^3}-324e^{2c_1}}}{6\sqrt[3]{2}}\right.\right.$$

✓ **Maple** : cpu = 0.222 (sec), leaf count = 517

$$\left\{y(x)=-\frac{1}{3}+\frac{3\,x+2}{6}\left(7\left(-1/4\,\sqrt[3]{2\,(3\,x+2)\_C1-27\,(3\,x+2)^3\_C1^{\,3}+2\sqrt{-27\,(3\,x+2)^4\_C1^{\,4}+(3\,x+}\right.\right.\right.$$

2.248 ODE No. 248

$$\left(x^2+6xy(x)+3\right)y'(x)+3y(x)^2+2xy(x)+2x=0$$

✓ **Mathematica** : cpu = 0.0146411 (sec), leaf count = 106

$$\left\{\left\{y(x)\to -\frac{\sqrt{6c_1x-2x^3+\frac{1}{6}\left(x^2+3\right)^2}}{\sqrt{6}x}-\frac{x^2+3}{6x}\right\},\left\{y(x)\to \frac{\sqrt{6c_1x-2x^3+\frac{1}{6}\left(x^2+3\right)^2}}{\sqrt{6}x}-\frac{x^2+3}{6x}\right\}\right\}$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 75

$$\left\{y(x)=\frac{1}{6\,x}\left(-x^2-3-\sqrt{x^4-12\,x^3-12\_C1\,x+6\,x^2+9}\right),y(x)=\frac{1}{6\,x}\left(-x^2-3+\sqrt{x^4-12\,x^3-12\_C1\,x-\right.\right.$$

2.249 ODE No. 249

$$y'(x)\left(axy(x)+bx^n\right)+\alpha y(x)^3+\beta y(x)^2=0$$

✓ **Mathematica** : cpu = 5.0153 (sec), leaf count = 115

$$\text{Solve}\left[\frac{(a(-n)+a+\alpha y(x))y(x)^{\frac{a-an}{\beta}-1}(\alpha y(x)+\beta)^{\frac{a(n-1)}{\beta}}}{a^2(n-1)^2(a(n-1)+\beta)}+\frac{x^{1-n}\exp\left(-\frac{a(n-1)(\log(y(x))-\log(\alpha y(x)+\beta))}{\beta}\right)}{ab(1-n)(n-1)}=c_1,y(x)\right.$$

✓ **Maple** : cpu = 0.209 (sec), leaf count = 232

$$\left\{y(x)=\beta\left(eval\left(RootOf\left(-x^{1-n}\_Z^{\frac{a(n-1)}{\beta}}a^2\beta\,n+\_C1\,a^2bn^2+x^{1-n}\_Z^{\frac{a(n-1)}{\beta}}a^2\beta-x^{1-n}\_Z^{\frac{a(n-1)}{\beta}}a\beta^2-\_Z^{an}\right.\right.\right.\right.$$

2.250 ODE No. 250

$$y'(x)\left(ax+Ax^2+by(x)+Bxy(x)+c\right)+Axy(x)+\alpha x-By(x)^2+\beta y(x)+\gamma=0$$

✗ **Mathematica** : cpu = 301.41 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((B*x*y(x)+A*x^2+a*x+b*y(x)+c)*diff(y(x),x)-B*g(x)^2+A*x*y(x)+alpha*x+beta*y(x)+gamma
```

2.251 ODE No. 251

$$\left(x^2 y(x)-1\right) y'(x)+x y(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.012903 (sec), leaf count = 60

$$\left\{\left\{y(x)\to \frac{1}{x^2}-\frac{\sqrt{c_1 x^2+2x^3+1}}{x^2}\right\},\left\{y(x)\to \frac{\sqrt{c_1 x^2+2x^3+1}}{x^2}+\frac{1}{x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 51

$$\left\{y(x)=\frac{1}{x^2}\left(1-\sqrt{-2\,x^2\_C1+2\,x^3+1}\right),y(x)=\frac{1}{x^2}\left(1+\sqrt{-2\,x^2\_C1+2\,x^3+1}\right)\right\}$$

2.252 ODE No. 252

$$\left(x^2 y(x)-1\right) y'(x)-x y(x)^2+1=0$$

✓ **Mathematica** : cpu = 14.7778 (sec), leaf count = 819

$$\left\{\left\{y(x)\to \frac{6xc_1-x}{6c_1-1}+\frac{\sqrt[3]{-1944c_1^2x^3+648c_1x^3-54x^3+1944c_1^2-648c_1+\sqrt{4\left(54x^2c_1-9x^2\right)^3+\left(-1944c_1^2x^3\right.}}}{3\sqrt[3]{2}\left(6c_1-1\right)}\right.\right.$$

✓ **Maple** : cpu = 0.873 (sec), leaf count = 1338

$$\left\{y(x)=1\left(\left(\left(-\_C1+80\right)x^7-160\,x^4+80\,x\right)\sqrt[3]{4}\sqrt[3]{\left(-80+\left(\_C1-80\right)x^6+160\,x^3\right)^2\_C1\left(-\frac{1}{4}+\sqrt{\frac{-}{-80+(\right.}\right.}\right.\right.$$

2.253 ODE No. 253

$$\left(x^2 y(x)-1\right) y'(x)+8x y(x)^2-8=0$$

✗ **Mathematica** : cpu = 19.0199 (sec), leaf count = 0 , could not solve

```
DSolve[-8 + 8*x*y[x]^2 + (-1 + x^2*y[x])*Derivative[1][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((x^2*y(x)-1)*diff(y(x),x)+8*x*y(x)^2-8 = 0,y(x))
```

2.254 ODE No. 254

$$x^2y(x)^3+x(xy(x)-2)y'(x)+xy(x)^2-2y(x)=0$$

✓ **Mathematica** : cpu = 0.0165904 (sec), leaf count = 99

$$\left\{\left\{y(x)\to -\frac{2x}{\frac{\sqrt{2}\sqrt{-2x(c_1-\log(x))-\frac{x}{2}}}{\sqrt{-\frac{1}{x^3}}}-x^2}\right\},\left\{y(x)\to \frac{2x}{\frac{\sqrt{2}\sqrt{-2x(c_1-\log(x))-\frac{x}{2}}}{\sqrt{-\frac{1}{x^3}}}+x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 59

$$\left\{y(x)=\frac{1}{(-2\ln(x)+2\_C1)x}\left(-1+\sqrt{1-4\ln(x)+4\_C1}\right),y(x)=\frac{1}{(2\ln(x)-2\_C1)x}\left(1+\sqrt{1-4\ln(x)}\right.\right.$$

2.255 ODE No. 255

$$x(xy(x)-3)y'(x)+xy(x)^2-y(x)=0$$

✓ **Mathematica** : cpu = 4.82967 (sec), leaf count = 30

$$\left\{\left\{y(x)\to -\frac{3W\left(e^{\frac{9c_1}{2^{2/3}}-1}x^{2/3}\right)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.226 (sec), leaf count = 74

$$\left\{y(x)=-3\frac{lambertW\left(2/3\sqrt[3]{-1/8\,x^2}\_C1\right)}{x},y(x)=-3\frac{lambertW\left(-1/3\sqrt[3]{-1/8\,x^2}\_C1\left(1+i\sqrt{3}\right)\right)}{x},y(x)=-\right.$$

2.256 ODE No. 256

$$x^2(y(x)-1)y'(x)+(x-1)y(x)=0$$

✓ **Mathematica** : cpu = 0.0202526 (sec), leaf count = 21

$$\left\{\left\{y(x)\to -W\left(x\left(-e^{\frac{1}{x}-c_1}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 31

$$\left\{y(x)=\mathrm{e}^{\frac{\_C1\,x+x\ln(x)-lambertW\left(-x\mathrm{e}^{-C1+x^{-1}}\right)x+1}{x}}\right\}$$

2.257 ODE No. 257

$$x\left(x^4+xy(x)-1\right)y'(x)-y(x)\left(-x^4+xy(x)-1\right)=0$$

✓ **Mathematica** : cpu = 0.362723 (sec), leaf count = 38

$$\text{Solve}\left[\frac{c_1+2xy(x)-2\log\left(\frac{1}{1-xy(x)}\right)-2}{x^2y(x)^2}+\frac{1}{x^4}=0,y(x)\right]$$

✓ **Maple** : cpu = 0.113 (sec), leaf count = 98

$$\left\{y(x)=\frac{-\_C1+\mathrm{e}^{RootOf\left(-2\_Z\,x^4\left(\mathrm{e}^{-\_Z}\right)^2+2\,x^4\left(\mathrm{e}^{-\_Z}\right)^2-2\,\mathrm{e}^{-\_Z}\_C1\,x^4+\left(\mathrm{e}^{-\_Z}\right)^2-2\,\mathrm{e}^{-\_Z}\_C1+\_C1^2\right)}}{x\mathrm{e}^{RootOf\left(-2\_Z\,x^4\left(\mathrm{e}^{-\_Z}\right)^2+2\,x^4\left(\mathrm{e}^{-\_Z}\right)^2-2\,\mathrm{e}^{-\_Z}\_C1\,x^4+\left(\mathrm{e}^{-\_Z}\right)^2-2\,\mathrm{e}^{-\_Z}\_C1+\_C1^2\right)}}\right\}$$

2.258 ODE No. 258

$$-2x^3+2x^2y(x)y'(x)-x^2+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0137141 (sec), leaf count = 43

$$\left\{\left\{y(x)\to-\sqrt{c_1e^{\frac{1}{x}}+x^2}\right\},\left\{y(x)\to\sqrt{c_1e^{\frac{1}{x}}+x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 33

$$\left\{y(x)=\sqrt{\mathrm{e}^{x^{-1}}\_C1+x^2},y(x)=-\sqrt{\mathrm{e}^{x^{-1}}\_C1+x^2}\right\}$$

2.259 ODE No. 259

$$2x^2y(x)y'(x)-e^{x-\frac{1}{x}}x^2-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0198907 (sec), leaf count = 50

$$\left\{\left\{y(x)\to-e^{-\frac{1}{2}/x}\sqrt{c_1+e^x}\right\},\left\{y(x)\to e^{-\frac{1}{2}/x}\sqrt{c_1+e^x}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 51

$$\left\{y(x)=\sqrt{\mathrm{e}^{-x^{-1}}\_C1+\mathrm{e}^{\frac{x^2-1}{x}}},y(x)=-\sqrt{\mathrm{e}^{-x^{-1}}\_C1+\mathrm{e}^{\frac{x^2-1}{x}}}\right\}$$

2.260 ODE No. 260

$$\left(2x^2y(x)+x\right)y'(x)-x^2y(x)^3+2xy(x)^2+y(x)=0$$

✓ **Mathematica** : cpu = 0.0152673 (sec), leaf count = 80

$$\left\{\left\{y(x)\to \frac{x}{\frac{\sqrt{x(c_1-2\log(x))+4x}}{\sqrt{\frac{1}{x^3}}}-2x^2}\right\},\left\{y(x)\to -\frac{x}{\frac{\sqrt{x(c_1-2\log(x))+4x}}{\sqrt{\frac{1}{x^3}}}+2x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 59

$$\left\{y(x)=\frac{1}{(2\ln(x)-2\_C1)\,x}\left(-2+\sqrt{4-2\ln(x)+2\_C1}\right),y(x)=\frac{1}{(-2\ln(x)+2\_C1)\,x}\left(2+\sqrt{4-2\ln(x)}\right.\right.$$

2.261 ODE No. 261

$$\left(2x^2y(x)-x\right)y'(x)-2xy(x)^2-y(x)=0$$

✓ **Mathematica** : cpu = 0.93861 (sec), leaf count = 32

$$\left\{\left\{y(x)\to -\frac{1}{2xW\left(\frac{e^{\frac{9c_1}{2^{2/3}}-1}}{x^2}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.156 (sec), leaf count = 18

$$\left\{y(x)=-\frac{1}{2\,x}\left(lambertW\left(-\frac{\_C1}{2\,x^2}\right)\right)^{-1}\right\}$$

2.262 ODE No. 262

$$2x^3+\left(2x^2y(x)-x^3\right)y'(x)-4xy(x)^2+y(x)^3=0$$

✓ **Mathematica** : cpu = 0.0674234 (sec), leaf count = 101

$$\left\{\left\{y(x)\to \frac{2x^3-\sqrt{e^{4c_1}x^2-3e^{2c_1}x^4}}{e^{2c_1}+x^2}\right\},\left\{y(x)\to \frac{\sqrt{e^{4c_1}x^2-3e^{2c_1}x^4}+2x^3}{e^{2c_1}+x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.317 (sec), leaf count = 65

$$\left\{y(x)=\frac{x}{\_C1\,x^2-1}\left(2\_C1\,x^2-\sqrt{3\_C1\,x^2+1}\right),y(x)=\frac{x}{\_C1\,x^2-1}\left(2\_C1\,x^2+\sqrt{3\_C1\,x^2+1}\right)\right\}$$

2.263 ODE No. 263

$$2x^3+3x^2y(x)^2+y(x)y'(x)+7=0$$

✓ **Mathematica** : cpu = 0.042037 (sec), leaf count = 121

$$\left\{\left\{y(x)\to -\sqrt{c_1e^{-2x^3}+\frac{20\ 2^{2/3}e^{-2x^3}x\Gamma\left(\frac{1}{3},-2x^3\right)}{9\sqrt[3]{-x^3}}-\frac{2x}{3}}\right\},\left\{y(x)\to \sqrt{c_1e^{-2x^3}+\frac{20\ 2^{2/3}e^{-2x^3}x\Gamma\left(\frac{1}{3},-2x^3\right)}{9\sqrt[3]{-x^3}}-\right.\right.$$

✓ **Maple** : cpu = 0.148 (sec), leaf count = 173

$$\left\{y(x)=-\frac{2^{\frac{2}{3}}}{18\,\Gamma\left(2/3\right)}\sqrt{-240\,\Gamma\left(2/3\right)\left(\frac{\left(-\frac{27\,\mathrm{e}^{-2\,x^3}\_C1}{2}+9\,x\right)\Gamma\left(2/3\right)\sqrt[3]{2}\sqrt[3]{-x^3}}{40}+\mathrm{e}^{-2\,x^3}x\left(\pi\sqrt{3}-3/2\,\Gamma\left(1/3,-2\right.\right.\right.\right.$$

2.264 ODE No. 264

$$2x\left(x^3y(x)+1\right)y'(x)+y(x)\left(3x^3y(x)-1\right)=0$$

✓ **Mathematica** : cpu = 0.360136 (sec), leaf count = 680

$$\left\{\left\{y(x)\to \text{Root}\left[81\#1^7e^{\frac{21c_1}{2}}x^{12}+756\#1^6e^{\frac{21c_1}{2}}x^9+2646\#1^5e^{\frac{21c_1}{2}}x^6+4116\#1^4e^{\frac{21c_1}{2}}x^3+2401\#1^3e^{\frac{21c_1}{2}}-x^{3/2}\&\right.\right.\right.$$

✓ **Maple** : cpu = 0.531 (sec), leaf count = 574

$$\left\{y(x)=\frac{-40353607\left(RootOf\left(9\,x^7\_Z^{98}-49\,\_C1\,\_Z^{42}+14\,\_C1\,\_Z^{21}-\_C1\right)\right)^{91}\_C1+756315\left(RootOf\left(9\,x\right.\right.\right.}{3\,x^3\left(RootOf\left(9\,x^7\_Z^{98}-49\,\_C1\,\_Z^{42}+14\,\_C1\,\_Z^{21}-\_C1\right)\right)^7\left(5764801\,\_C1\,\left(RootOf\left(9\,x^7\_\right.\right.\right.}$$

2.265 ODE No. 265

$$2(n+1)^2x^{n-1}\left(x^{n^2}y(x)^2-1\right)+\left(x^{n(n+1)}y(x)-1\right)y'(x)=0$$

✗ **Mathematica** : cpu = 300.037 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((x^(n*(n+1))*y(x)-1)*diff(y(x),x)+2*(n+1)^2*x^(n-1)*(x^(n^2)*y(x)^2-1) = 0,y(x))
```

2.266 ODE No. 266

$$\sqrt{x^2+1}(y(x)-x)y'(x)-a\sqrt{(y(x)^2+1)^3}=0$$

✗ **Mathematica** : cpu = 300.034 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.716 (sec), leaf count = 55

$$\left\{y(x)=\tan\left(RootOf\left(-\arctan(x)+\int^{-\arctan(x)+\_Z}-\frac{1}{2\,a^2+\cos(2\,\_a)-1}\left(\cos(2\,\_a)-1+\sqrt{-2\,a^2(\cos(2\,\_\right.\right.\right.$$

2.267 ODE No. 267

$$y(x)\sin^2(x)y'(x)+y(x)^2\sin(x)\cos(x)-1=0$$

✓ **Mathematica** : cpu = 0.0478581 (sec), leaf count = 36

$$\left\{\left\{y(x)\to-\sqrt{c_1+2x}\csc(x)\right\},\left\{y(x)\to\sqrt{c_1+2x}\csc(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 32

$$\left\{y(x)=\frac{1}{\sin(x)}\sqrt{2\,x+\_C1},y(x)=-\frac{1}{\sin(x)}\sqrt{2\,x+\_C1}\right\}$$

2.268 ODE No. 268

$$f(x)y(x)y'(x)+g(x)y(x)^2+h(x)=0$$

✓ **Mathematica** : cpu = 0.976625 (sec), leaf count = 140

$$\left\{\left\{y(x)\to-e^{\int_1^x-\frac{g(K[1])}{f(K[1])}\,dK[1]}\sqrt{2\int_1^x-\frac{h(K[2])\exp\left(-2\int_1^{K[2]}-\frac{g(K[1])}{f(K[1])}\,dK[1]\right)}{f(K[2])}\,dK[2]+c_1}\right\},\left\{y(x)\to e^{\int_1^x-\frac{g(K[1]}{f(K[1}\right.\right.$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 118

$$\left\{y(x)=1\sqrt{\mathrm{e}^{2\int\frac{g(x)}{f(x)}\,\mathrm{d}x}\left(-2\int\frac{h(x)}{f(x)}\left(\mathrm{e}^{\int\frac{g(x)}{f(x)}\,\mathrm{d}x}\right)^2\mathrm{d}x+\_C1\right)}\left(\mathrm{e}^{2\int\frac{g(x)}{f(x)}\,\mathrm{d}x}\right)^{-1},y(x)=-1\sqrt{\mathrm{e}^{2\int\frac{g(x)}{f(x)}\,\mathrm{d}x}\left(-2\int\frac{h(}{f(}\right.\right.$$

2.269 ODE No. 269

$$-\mathrm{f0}(x) - \mathrm{f1}(x)y(x) - \mathrm{f2}(x)y(x)^2 - \mathrm{f3}(x)y(x)^3 + y'(x)(\mathrm{g0}(x) + \mathrm{g1}(x)y(x)) = 0$$

✗ **Mathematica** : cpu = 320.749 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((g1(x)*y(x)+g0(x))*diff(y(x),x)-f1(x)*y(x)-f2(x)*y(x)^2-f3(x)*y(x)^3-f0(x) = 0,y(x))
```

2.270 ODE No. 270

$$x^2 + \left(y(x)^2 - x\right) y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.021968 (sec), leaf count = 327

$$\left\{\left\{y(x) \to -\frac{3\sqrt[3]{2}x}{\sqrt[3]{\sqrt{\left(81c_1 + 27x^3\right)^2 - 2916x^3} + 81c_1 + 27x^3}} - \frac{\sqrt[3]{\sqrt{\left(81c_1 + 27x^3\right)^2 - 2916x^3} + 81c_1 + 27x^3}}{3\sqrt[3]{2}}\right\}, \left\{\right.$$

✓ **Maple** : cpu = 0.025 (sec), leaf count = 319

$$\left\{y(x) = \frac{1}{2}\left(\left(-4x^3 - 12\_C1 + 4\sqrt{x^6 + (6\_C1 - 4)x^3 + 9\_C1^2}\right)^{\frac{2}{3}} + 4x\right) \frac{1}{\sqrt[3]{-4x^3 - 12\_C1 + 4\sqrt{x^6 + (6\right.}}$$

2.271 ODE No. 271

$$\left(x^2 + y(x)^2\right) y'(x) + 2x(y(x) + 2x) = 0$$

✓ **Mathematica** : cpu = 0.115596 (sec), leaf count = 370

$$\left\{\left\{y(x) \to \frac{\sqrt[3]{\sqrt{-8e^{3c_1}x^3 + e^{6c_1} + 20x^6} + e^{3c_1} - 4x^3}}{\sqrt[3]{2}} - \frac{\sqrt[3]{2}x^2}{\sqrt[3]{\sqrt{-8e^{3c_1}x^3 + e^{6c_1} + 20x^6} + e^{3c_1} - 4x^3}}\right\}, \left\{y(x) \to \right.$$

✓ **Maple** : cpu = 0.185 (sec), leaf count = 352

$$\left\{y(x) = 1\left(\frac{1}{2}\sqrt[3]{4 - 16x^3\_C1^{3/2} + 4\sqrt{20\_C1^3x^6 - 8x^3\_C1^{3/2} + 1}} - 2\frac{\_C1\,x^2}{\sqrt[3]{4 - 16x^3\_C1^{3/2} + 4\sqrt{20\_C1^3x^6}}}\right.\right.$$

2.272 ODE No. 272

$$\left(x^2+y(x)^2\right)y'(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0499943 (sec), leaf count = 42

$$\text{Solve}\left[\log\left(\frac{y(x)}{x}\right)+\frac{2\tan^{-1}\left(\frac{\frac{2y(x)}{x}-1}{\sqrt{3}}\right)}{\sqrt{3}}=c_1-\log(x),y(x)\right]$$

✓ **Maple** : cpu = 0.151 (sec), leaf count = 43

$$\left\{y(x)=\mathrm{e}^{\frac{2\sqrt{3}}{3}RootOf\left(-\sqrt{3}x\mathrm{e}^{-\_C1}+3\tan(\_Z)x\mathrm{e}^{-\_C1}+2\sqrt{3}\mathrm{e}^{2/3\sqrt{3}\_Z}\right)-\_C1}\right\}$$

2.273 ODE No. 273

$$\left(a+x^2+y(x)^2\right)y'(x)+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.0264344 (sec), leaf count = 297

$$\left\{\left\{y(x)\to\frac{\sqrt[3]{\sqrt{2916\left(a+x^2\right)^3+6561c_1^2}+81c_1}}{3\sqrt[3]{2}}-\frac{3\sqrt[3]{2}\left(a+x^2\right)}{\sqrt[3]{\sqrt{2916\left(a+x^2\right)^3+6561c_1^2}+81c_1}}\right\},\left\{y(x)\to\frac{3}{2^{2/3}\sqrt[3]{\sqrt{29}}}\right.$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 401

$$\left\{y(x)=\frac{1}{4}\left(\left(i\left(-12\_C1+4\sqrt{4x^6+12ax^4+12a^2x^2+4a^3+9\_C1^2}\right)^{\frac{2}{3}}+4ix^2+4ia\right)\sqrt{3}-\left(-12\_C1+4\right.\right.\right.$$

2.274 ODE No. 274

$$\left(a+x^2+y(x)^2\right)y'(x)+b+x^2+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.0366443 (sec), leaf count = 411

$$\left\{\left\{y(x)\to\frac{\sqrt[3]{\sqrt{2916\left(a+x^2\right)^3+\left(-81bx+81c_1-27x^3\right)^2}-81bx+81c_1-27x^3}}{3\sqrt[3]{2}}-\frac{}{\sqrt[3]{\sqrt{2916\left(a+x^2\right)^3+(-81b}}}\right.\right.$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 657

$$\left\{ y(x) = \frac{1}{2}\left(\left(-4\,x^3 - 12\,bx - 12\,\_C1 + 4\sqrt{5\,x^6 + (12\,a + 6\,b)\,x^4 + 6\,x^3\,\_C1 + (12\,a^2 + 9\,b^2)\,x^2 + 18\,bx\,\_C1 + \right.\right.\right.$$

2.275 ODE No. 275

$$\left(x^2 + y(x)^2 + x\right) y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0353238 (sec), leaf count = 18

$$\text{Solve}\left[y(x) - \tan^{-1}\left(\frac{x}{y(x)}\right) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.104 (sec), leaf count = 30

$$\left\{ \_C1 + \frac{(ix + y(x))\,\mathrm{e}^{-2\,iy(x)}}{2\,iy\,(x) + 2\,x} = 0 \right\}$$

2.276 ODE No. 276

$$\left(y(x)^2 - x^2\right) y'(x) + 2xy(x) = 0$$

✓ **Mathematica** : cpu = 0.0369275 (sec), leaf count = 61

$$\left\{\left\{y(x) \to \frac{1}{2}\left(e^{c_1} - \sqrt{e^{2c_1} - 4x^2}\right)\right\}, \left\{y(x) \to \frac{1}{2}\left(\sqrt{e^{2c_1} - 4x^2} + e^{c_1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.064 (sec), leaf count = 47

$$\left\{ y(x) = \frac{1}{2\,\_C1}\left(1 + \sqrt{-4\,\_C1^2 x^2 + 1}\right), y(x) = \frac{1}{2\,\_C1}\left(1 - \sqrt{-4\,\_C1^2 x^2 + 1}\right) \right\}$$

2.277 ODE No. 277

$$\left(x^4+y(x)^2\right)y'(x)-4x^3y(x)=0$$

✓ **Mathematica** : cpu = 0.0216785 (sec), leaf count = 53

$$\left\{\left\{y(x)\to\frac{1}{2}\left(c_1-\sqrt{c_1^2+4x^4}\right)\right\},\left\{y(x)\to\frac{1}{2}\left(\sqrt{c_1^2+4x^4}+c_1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.35 (sec), leaf count = 41

$$\left\{y(x)=-\frac{1}{2}\sqrt{4\,x^4+\_C1^2}+\frac{\_C1}{2},y(x)=\frac{1}{2}\sqrt{4\,x^4+\_C1^2}+\frac{\_C1}{2}\right\}$$

2.278 ODE No. 278

$$y'(x)\left(y(x)^2+4\sin(x)\right)-\cos(x)=0$$

✓ **Mathematica** : cpu = 0.0747629 (sec), leaf count = 39

$$\text{Solve}\left[-\frac{1}{32}e^{-4y(x)}\left(8y(x)^2+4y(x)+1\right)-e^{-4y(x)}\sin(x)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 28

$$\left\{\frac{\left(-8\left(y(x)\right)^2-4\,y(x)-32\,\sin\left(x\right)-1\right)\mathrm{e}^{-4\,y(x)}}{32}+\_C1=0\right\}$$

2.279 ODE No. 279

$$\left(y(x)^2+2y(x)+x\right)y'(x)+y(x)^2(y(x)+x)^2+y(x)(y(x)+1)=0$$

✓ **Mathematica** : cpu = 0.796274 (sec), leaf count = 107

$$\left\{\left\{y(x)\to\frac{-\sqrt{\left(-c_1x+x^2-1\right)^2+4\left(x-c_1\right)}+c_1x-x^2+1}{2\left(x-c_1\right)}\right\},\left\{y(x)\to\frac{\sqrt{\left(-c_1x+x^2-1\right)^2+4\left(x-c_1\right)}+c_1\right.\right.$$

✓ **Maple** : cpu = 0.18 (sec), leaf count = 116

$$\left\{y(x)=\frac{1}{-2\_C1+4\,x}\left(-2\,x^2+\_C1\,x+\sqrt{4\,x^4-4\,x^3\_C1+\left(\_C1^2-8\right)x^2+\left(4\_C1+16\right)x-8\_C1+4}+\right.\right.$$

2.280 ODE No. 280

$$(y(x)+x)^2 y'(x) - a^2 = 0$$

✓ **Mathematica** : cpu = 0.0471692 (sec), leaf count = 21

$$\text{Solve}\left[y(x) - a\tan^{-1}\left(\frac{y(x)+x}{a}\right) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 24

$$\{y(x) = aRootOf(\tan(\_Z)\,a - \_Z\,a + \_C1 - x) - \_C1\}$$

2.281 ODE No. 281

$$\left(-x^2 + 2xy(x) + y(x)^2\right) y'(x) + x^2 + 2xy(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0668891 (sec), leaf count = 75

$$\left\{\left\{y(x) \to \frac{1}{2}\left(e^{c_1} - \sqrt{4e^{c_1}x + e^{2c_1} - 4x^2}\right)\right\}, \left\{y(x) \to \frac{1}{2}\left(\sqrt{4e^{c_1}x + e^{2c_1} - 4x^2} + e^{c_1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 55

$$\left\{y(x) = \frac{1}{2\_C1}\left(1 + \sqrt{-4\_C1^2x^2 + 4\_C1\,x + 1}\right), y(x) = \frac{1}{2\_C1}\left(1 - \sqrt{-4\_C1^2x^2 + 4\_C1\,x + 1}\right)\right\}$$

2.282 ODE No. 282

$$(y(x) + 3x - 1)^2 y'(x) - (2y(x) - 1)(4y(x) + 6x - 3) = 0$$

✓ **Mathematica** : cpu = 0.176386 (sec), leaf count = 2129

$$\left\{\left\{y(x) \to \frac{1}{6}(12x + 4e^{c_1} + 1) - \frac{1}{6}\sqrt{36x^2 + 96e^{c_1}x - 12x - 16e^{c_1} + 16e^{2c_1} + 3\ 2^{2/3}\sqrt[3]{-7776e^{c_1}x^5 + 6480e^{c_1}x^4 -}\right.\right.$$

✓ **Maple** : cpu = 0.235 (sec), leaf count = 71

$$\left\{-\ln\left(\frac{-6\,y(x) + 4 - 6\,x}{6\,x - 1}\right) + 3\ln\left(\frac{-6\,y(x) + 3}{6\,x - 1}\right) - 3\ln\left(\frac{-6\,y(x) + 18\,x}{6\,x - 1}\right) - \ln(6\,x - 1) - \_C1 = 0\right\}$$

2.283 ODE No. 283

$$3\left(y(x)^2-x^2\right)y'(x)+2y(x)^3-6x(x+1)y(x)-3e^x=0$$

✓ **Mathematica** : cpu = 0.0577449 (sec), leaf count = 477

$$\left\{\left\{y(x)\to -\frac{e^{-2x}\sqrt[3]{\sqrt{\left(27c_1e^{4x}-27e^{7x}\right)^2-2916e^{12x}x^6}+27c_1e^{4x}-27e^{7x}}}{3\sqrt[3]{2}}-\frac{3\sqrt[3]{2}e^{2x}x^2}{\sqrt[3]{\sqrt{\left(27c_1e^{4x}-27e^{7x}\right)^2-2916e^{12}}}}\right.\right.$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 407

$$\left\{y(x)=\frac{1}{2\,\mathrm{e}^{2x}}\left(4x^2\left(\mathrm{e}^{2x}\right)^2+\left(\left(4\,\mathrm{e}^{3x}-4\_C1+4\sqrt{-4x^6\left(\mathrm{e}^{2x}\right)^2+\left(\mathrm{e}^{3x}\right)^2-2\,\mathrm{e}^{3x}\_C1+\_C1^2}\right)\left(\mathrm{e}^{2x}\right)^2\right)^{\frac{2}{3}}\right)-\right.$$

2.284 ODE No. 284

$$\left(x^2+4y(x)^2\right)y'(x)-xy(x)=0$$

✓ **Mathematica** : cpu = 0.0352367 (sec), leaf count = 59

$$\left\{\left\{y(x)\to -\frac{x}{2\sqrt{W\left(\frac{1}{4}e^{-\frac{c_1}{2}}x^2\right)}}\right\},\left\{y(x)\to \frac{x}{2\sqrt{W\left(\frac{1}{4}e^{-\frac{c_1}{2}}x^2\right)}}\right\}\right\}$$

✓ **Maple** : cpu = 0.151 (sec), leaf count = 21

$$\left\{y(x)=\mathrm{e}^{\frac{1}{2}lambertW\left(\frac{\left(\mathrm{e}^{\_C1}\right)^2x^2}{4}\right)-\_C1}\right\}$$

2.285 ODE No. 285

$$\left(3x^2+2xy(x)+4y(x)^2\right)y'(x)+2x^2+6xy(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0354124 (sec), leaf count = 402

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{\sqrt{\left(432e^{3c_1}+54x^3\right)^2+3881196x^6}+432e^{3c_1}+54x^3}}{12\sqrt[3]{2}}-\frac{33x^2}{2\ 2^{2/3}\sqrt[3]{\sqrt{\left(432e^{3c_1}+54x^3\right)^2+3881196x^6}}}\right.\right.$$

✓ **Maple** : cpu = 0.177 (sec), leaf count = 432

$$\left\{y(x)=\frac{1}{\_C1}\left(\frac{1}{4}\sqrt[3]{x^3\_C1^3+8+2\sqrt{333\_C1^6x^6+4x^3\_C1^3+16}}-\frac{11\_C1^2x^2}{4}\frac{1}{\sqrt[3]{x^3\_C1^3+8+2\sqrt{333\_C1^6x^6+4x^3\_C1^3+16}}}\right.\right.$$

2.286 ODE No. 286

$$(2y(x)-3x+1)^2y'(x)-(3y(x)-2x-4)^2=0$$

✓ **Mathematica** : cpu = 0.201578 (sec), leaf count = 3501

✓ **Maple** : cpu = 1.803 (sec), leaf count = 1337

$$\left\{y(x)=\frac{(5x+3)\left(RootOf\left(\left(115330078125\_C1\,x^9-2283535546875\_C1\,x^8+20095112812500\_C1\,x^7-1031\right.\right.\right.}{5\left(RootOf\left(\left(115330078125\_C1\,x^9-2283535546875\_C1\,x^8+20095112812500\_C1\,x^7-1\right.\right.\right.}$$

2.287 ODE No. 287

$$(2y(x)-4x+1)^2y'(x)-(y(x)-2x)^2=0$$

✓ **Mathematica** : cpu = 0.920473 (sec), leaf count = 77

$$\text{Solve}\left[\frac{y(x)}{2}+\frac{1}{196}\left(14y(x)-\left(8-9\sqrt{2}\right)\log\left(-7y(x)+14x+\sqrt{2}-4\right)-\left(8+9\sqrt{2}\right)\log\left(7y(x)-14x+\sqrt{2}+4\right.\right.\right.$$

✓ **Maple** : cpu = 0.074 (sec), leaf count = 56

$$\left\{-\frac{x}{7}+\frac{4y(x)}{7}-\frac{2\ln\left(7(y(x)-2x)^2+8y(x)-16x+2\right)}{49}-\frac{9\sqrt{2}}{98}Artanh\left(\frac{(7y(x)-14x+4)\sqrt{2}}{2}\right)-\_C1=0\right.$$

2.288 ODE No. 288

$$\left(-3x^2y(x)+6y(x)^2+1\right)y'(x)-3xy(x)^2+x=0$$

✓ **Mathematica** : cpu = 0.0240444 (sec), leaf count = 534

$$\left\{\left\{y(x)\to -\frac{\sqrt[3]{4\sqrt{3}\sqrt{-54c_1x^6+648c_1x^2+432c_1^2-27x^8+207x^4+32}+144c_1-9x^6+108x^2}}{4\ 3^{2/3}}+\frac{}{3\sqrt[3]{3}\sqrt[3]{4\sqrt{3}\sqrt{}}\right.\right.$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 579

$$\left\{y(x)=-\frac{1}{24}\left(-6\,x^2\sqrt[3]{-324\,x^2-432\,\_C1+27\,x^6+12\,\sqrt{-81\,x^8-162\,\_C1\,x^6+621\,x^4+1944\,\_C1\,x^2+1296}\right.\right.$$

2.289 ODE No. 289

$$a+(6y(x)-x)^2y'(x)-6y(x)^2+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.018303 (sec), leaf count = 115

$$\left\{\left\{y(x)\to\frac{1}{6}\left(\sqrt[3]{-18ax+18c_1-x^3}+x\right)\right\},\left\{y(x)\to\frac{x}{6}-\frac{1}{12}\left(1-i\sqrt{3}\right)\sqrt[3]{-18ax+18c_1-x^3}\right\},\left\{y(x)\to\frac{x}{6}-\right.\right.$$

✓ **Maple** : cpu = 0.034 (sec), leaf count = 115

$$\left\{y(x)=\frac{1}{6}\sqrt[3]{-x^3-18\,ax-18\,\_C1}+\frac{x}{6},y(x)=-\frac{1}{12}\sqrt[3]{-x^3-18\,ax-18\,\_C1}-\frac{i}{12}\sqrt{3}\sqrt[3]{-x^3-18\,ax-18\,\_C}\right.$$

2.290 ODE No. 290

$$y'(x)\left(ay(x)^2+2bxy(x)+cx^2\right)+by(x)^2+2cxy(x)+dx^2=0$$

✓ **Mathematica** : cpu = 0.0828373 (sec), leaf count = 831

$$\left\{\left\{y(x)\to-\frac{bx}{a}+\frac{\sqrt[3]{-54b^3x^3+81abcx^3-27a^2dx^3+27a^2e^{3c_1}+\sqrt{4\left(9acx^2-9b^2x^2\right)^3+\left(-54b^3x^3+81abcx^3-\right.}}}{3\sqrt[3]{2}a}\right.\right.$$

✓ **Maple** : cpu = 0.203 (sec), leaf count = 1388

$$\left\{ y(x) = \frac{1}{\_C1}\left(\frac{1}{2\,a}\sqrt[3]{-4\,\_C1^{3}a^{2}dx^{3}+12\,cx^{3}\_C1^{3}ba-8\,b^{3}x^{3}\_C1^{3}+4\,\sqrt{\_C1^{6}a^{2}d^{2}x^{6}-6\,\_C1^{6}abcdx^{6}+4\,\_} \right.\right.$$

2.291 ODE No. 291

$$y'(x)\left(b(\alpha x+\beta y(x))^2-\beta(ax+by(x))\right)-\alpha(ax+by(x))+a(\alpha x+\beta y(x))^2=0$$

✓ **Mathematica** : cpu = 0.526221 (sec), leaf count = 39

$$\text{Solve}\left[\frac{a\beta\left(\log(ax+by(x))+\frac{1}{\alpha x+\beta y(x)}\right)}{a\beta-\alpha b}=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.17 (sec), leaf count = 50

$$\left\{ y(x) = \frac{-ax+\mathrm{e}^{RootOf\left(\_C1\,a\beta\,x-\_C1\,\alpha\,bx-\_Z\,a\beta\,x+\_Z\,\alpha\,bx-\_C1\,\beta\,\mathrm{e}^{-Z}+\mathrm{e}^{-Z}\_Z\,\beta+b\right)}}{b} \right\}$$

2.292 ODE No. 292

$$y'(x)(ay(x)+bx+c)^2+(\alpha y(x)+\beta x+\gamma)^2=0$$

✓ **Mathematica** : cpu = 61.716 (sec), leaf count = 760

$$\text{Solve}\left[(\alpha b-a\beta)\text{RootSum}\left[\#1^3a\beta^3-\#1^3\alpha b\beta^2+2\#1^2a\alpha\beta^2y(x)+\#1^2ab^2\beta y(x)+3\gamma\#1^2a\beta^2-2\#1^2\alpha^2b\beta y(x)-\right.\right.$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 115

$$\left\{ y(x) = \frac{1}{a\beta-b\alpha}\left(\left((bx+c)\,\alpha-a(\beta\,x+\gamma)\right)RootOf\left(\int^{\_Z}\frac{(\_a\,a-b)^2}{\_a^3a^2-2\,\_a^2ab-\_a^2\alpha^2+2\,\_a\,\alpha\,\beta+\_a\,b^2-\beta^2}d \right.\right.\right.$$

2.293 ODE No. 293

$$x\left(y(x)^2-3x\right)y'(x)+2y(x)^3-5xy(x)=0$$

✓ **Mathematica** : cpu = 0.101024 (sec), leaf count = 661

$$\left\{\left\{y(x)\to \text{Root}\left[-\#1^{15}-\frac{25\#1^2e^{\frac{65c_1}{2}}}{x^{26}}+\frac{65e^{\frac{65c_1}{2}}}{x^{25}}\&,1\right]\right\},\left\{y(x)\to \text{Root}\left[-\#1^{15}-\frac{25\#1^2e^{\frac{65c_1}{2}}}{x^{26}}+\frac{65e^{\frac{65c_1}{2}}}{x^{25}}\&,2\right]\right.$$

✓ **Maple** : cpu = 0.373 (sec), leaf count = 35

$$\left\{\ln\left(x\right)-\_C1-\frac{2}{65}\ln\left(\frac{5\left(y(x)\right)^2-13\,x}{x}\right)+\frac{6}{13}\ln\left(y(x)\,\frac{1}{\sqrt{x}}\right)=0\right\}$$

2.294 ODE No. 294

$$x\left(-a+x^2+y(x)^2\right)y'(x)-y(x)\left(a+x^2+y(x)^2\right)=0$$

✓ **Mathematica** : cpu = 0.0350329 (sec), leaf count = 71

$$\left\{\left\{y(x)\to \frac{1}{2}\left(c_1x-\sqrt{-4a+c_1^2x^2+4x^2}\right)\right\},\left\{y(x)\to \frac{1}{2}\left(\sqrt{-4a+c_1^2x^2+4x^2}+c_1x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.108 (sec), leaf count = 112

$$\left\{\left(\left(y(x)\right)^{-2}-\left(-x^2+a\right)^{-1}\right)^{-1}=-x\sqrt{x^2-a}\frac{1}{\sqrt{\_C1+4\,\frac{a}{x^2-a}}}+\frac{x^2}{2}-\frac{a}{2},\left(\left(y(x)\right)^{-2}-\left(-x^2+a\right)^{-1}\right)^{-1}=x\sqrt{x}\right.$$

2.295 ODE No. 295

$$x\left(-x^2+xy(x)+y(x)^2\right)y'(x)+x^2y(x)-y(x)^3+xy(x)^2=0$$

✓ **Mathematica** : cpu = 0.0368645 (sec), leaf count = 31

$$\text{Solve}\left[\frac{x}{y(x)}+\frac{y(x)}{x}+\log\left(\frac{y(x)}{x}\right)=c_1-2\log(x),y(x)\right]$$

✓ **Maple** : cpu = 0.234 (sec), leaf count = 29

$$\left\{y(x)=\mathrm{e}^{RootOf\left(\left(\mathrm{e}^{-Z}\right)^2+2\,\mathrm{e}^{-Z}\ln(x)+2\,\mathrm{e}^{-Z}\_C1+\_Z\,\mathrm{e}^{-Z}+1\right)}x\right\}$$

2.296 ODE No. 296

$$x^4+x\left(x^2y(x)+x^2+y(x)^2\right)y'(x)-2x^2y(x)^2-2y(x)^3=0$$

✓ **Mathematica** : cpu = 0.599654 (sec), leaf count = 102

$$\left\{\left\{y(x)\to -e^{-c_1}x^2-e^{-c_1}\sqrt{-e^{c_1}x^4+e^{2c_1}x^2+x^4}\right\},\left\{y(x)\to e^{-c_1}\sqrt{-e^{c_1}x^4+e^{2c_1}x^2+x^4}-e^{-c_1}x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.779 (sec), leaf count = 135

$$\left\{y(x)=-x\left(-x^3+\_C1\,x+x^2+\sqrt{-\_C1\,x^4+\_C1^2x^2+x^4}\right)\left(\_C1\,x-x^2+\sqrt{-\_C1\,x^4+\_C1^2x^2+x^4}\right)^{-}\right.$$

2.297 ODE No. 297

$$2x\left(5x^2+y(x)^2\right)y'(x)-x^2y(x)+y(x)^3=0$$

✓ **Mathematica** : cpu = 0.0555271 (sec), leaf count = 216

$$\left\{\left\{y(x)\to \text{Root}\left[-\#1^5+\frac{\#1^2e^{3c_1}}{x^{3/2}}+3e^{3c_1}\sqrt{x}\&,1\right]\right\},\left\{y(x)\to \text{Root}\left[-\#1^5+\frac{\#1^2e^{3c_1}}{x^{3/2}}+3e^{3c_1}\sqrt{x}\&,2\right]\right\},\left\{y(x\right.\right.$$

✓ **Maple** : cpu = 0.332 (sec), leaf count = 29

$$\left\{y(x)=\left(RootOf\left(x^9\_C1\,\_Z^{45}-\_Z^{18}-6\,\_Z^9-9\right)\right)^{\frac{9}{2}}x\right\}$$

2.298 ODE No. 298

$$3xy(x)^2y'(x)+y(x)^3-2x=0$$

✓ **Mathematica** : cpu = 0.0101626 (sec), leaf count = 72

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{c_1+x^2}}{\sqrt[3]{x}}\right\},\left\{y(x)\to -\frac{\sqrt[3]{-1}\sqrt[3]{c_1+x^2}}{\sqrt[3]{x}}\right\},\left\{y(x)\to \frac{(-1)^{2/3}\sqrt[3]{c_1+x^2}}{\sqrt[3]{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 73

$$\left\{y(x)=\frac{1}{x}\sqrt[3]{\left(x^2+\_C1\right)x^2},y(x)=-\frac{1+i\sqrt{3}}{2\,x}\sqrt[3]{\left(x^2+\_C1\right)x^2},y(x)=\frac{i\sqrt{3}-1}{2\,x}\sqrt[3]{\left(x^2+\_C1\right)x^2}\right\}$$

2.299 ODE No. 299

$$\left(3xy(x)^2-x^2\right)y'(x)+y(x)^3-2xy(x)=0$$

✓ **Mathematica** : cpu = 0.0215818 (sec), leaf count = 371

$$\left\{\left\{y(x)\to -\frac{\sqrt[3]{\frac{2}{3}}x^2}{\sqrt[3]{9c_1x^2+\sqrt{3}\sqrt{27c_1^2x^4-4x^9}}}-\frac{\sqrt[3]{9c_1x^2+\sqrt{3}\sqrt{27c_1^2x^4-4x^9}}}{\sqrt[3]{2}3^{2/3}x}\right\},\left\{y(x)\to \frac{(1+i\sqrt{3})}{2^{2/3}\sqrt[3]{3}\sqrt[3]{9c_1x^2+\sqrt{3}\sqrt{}}}\right.\right.$$

✓ **Maple** : cpu = 0.183 (sec), leaf count = 276

$$\left\{y(x)=-\frac{12^{\frac{2}{3}}}{144\,x}\left(\left(-12\,ix^3+i\left(\left(12\,\sqrt{-12\,x^5+81\,\_C1^2}+108\,\_C1\right)x^2\right)^{\frac{2}{3}}\right)\sqrt{3}+12\,x^3+\left(\left(12\,\sqrt{-12\,x^5+81}\right.\right.\right.\right.$$

2.300 ODE No. 300

$$6xy(x)^2y'(x)+2y(x)^3+x=0$$

✓ **Mathematica** : cpu = 0.0109453 (sec), leaf count = 99

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{4c_1-x^2}}{2^{2/3}\sqrt[3]{x}}\right\},\left\{y(x)\to -\frac{\sqrt[3]{-1}\sqrt[3]{4c_1-x^2}}{2^{2/3}\sqrt[3]{x}}\right\},\left\{y(x)\to \frac{(-1)^{2/3}\sqrt[3]{4c_1-x^2}}{2^{2/3}\sqrt[3]{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 83

$$\left\{y(x)=\frac{1}{2\,x}\sqrt[3]{-2\,\left(x^2-4\,\_C1\right)x^2},y(x)=-\frac{1+i\sqrt{3}}{4\,x}\sqrt[3]{-2\,\left(x^2-4\,\_C1\right)x^2},y(x)=\frac{i\sqrt{3}-1}{4\,x}\sqrt[3]{-2\,\left(x^2-4\,\_C1\right.}\right.$$

2.301 ODE No. 301

$$\left(x^2+6xy(x)^2\right)y'(x)-y(x)\left(3y(x)^2-x\right)=0$$

✓ **Mathematica** : cpu = 0.0406985 (sec), leaf count = 64

$$\left\{\left\{y(x)\to -\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{3c_1}}{x^3}\right)}}{\sqrt{6}}\right\},\left\{y(x)\to \frac{\sqrt{x}\sqrt{W\left(\frac{6e^{3c_1}}{x^3}\right)}}{\sqrt{6}}\right\}\right\}$$

✓ **Maple** : cpu = 0.206 (sec), leaf count = 25

$$\left\{y(x) = \frac{1}{x} \mathrm{e}^{-\frac{1}{2} lambertW\left(6 \frac{\mathrm{e}^{3} \_C1}{x^{3}}\right)+\frac{3 \_C1}{2}}\right\}$$

2.302 ODE No. 302

$$\left(x^2 y(x)^2 + x\right) y'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.0176637 (sec), leaf count = 70

$$\left\{\left\{y(x) \to \frac{c_1 x - \sqrt{x}\sqrt{c_1^2 x + 4}}{2x}\right\}, \left\{y(x) \to \frac{c_1 x + \sqrt{x}\sqrt{c_1^2 x + 4}}{2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.153 (sec), leaf count = 133

$$\left\{y(x) = -\frac{1}{2 \_C1\, x}\sqrt{-2\, x \_C1\, \left(-2 \_C1 - x + \sqrt{x\left(4 \_C1 + x\right)}\right)}, y(x) = \frac{1}{2 \_C1\, x}\sqrt{-2\, x \_C1\, \left(-2 \_C1 - x -\right.}\right.$$

2.303 ODE No. 303

$$y(x)\left(x^2 y(x)^2 + 1\right) + x(xy(x) - 1)^2 y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0479615 (sec), leaf count = 25

$$\text{Solve}\left[xy(x) - \frac{1}{xy(x)} - 2\log(y(x)) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.204 (sec), leaf count = 34

$$\left\{y(x) = \frac{\mathrm{e}^{RootOf\left(-\mathrm{e}^{2 \_Z} - 2\,\mathrm{e}^{\_Z} \ln(x) + 2\,\mathrm{e}^{\_Z} \_C1 + 2 \_Z\,\mathrm{e}^{\_Z} + 1\right)}}{x}\right\}$$

2.304 ODE No. 304

$$5x^2y(x)^3+\left(10x^3y(x)^2+x^2y(x)+2x\right)y'(x)+xy(x)^2=0$$

✓ **Mathematica** : cpu = 45.1761 (sec), leaf count = 59

$$\text{Solve}\left[-y(x)\left(\frac{\log\left(5x^2y(x)^2+2\right)}{2y(x)}+\frac{\tan^{-1}\left(\sqrt{\frac{5}{2}}xy(x)\right)}{\sqrt{10}y(x)}\right)-\log(y(x))=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.225 (sec), leaf count = 44

$$\left\{y(x)=\frac{\sqrt{10}}{5\,x}\tan\left(RootOf\left(\sqrt{10}\ln\left(\frac{4\left(\left(\tan\left(\_Z\right)\right)^2+1\right)\left(\tan\left(\_Z\right)\right)^2}{5\,x^2}\right)+2\sqrt{10}\_C1+2\,\_Z\right)\right)\right\}$$

2.305 ODE No. 305

$$x^2+\left(y(x)^3-3x\right)y'(x)-3y(x)=0$$

✓ **Mathematica** : cpu = 0.101596 (sec), leaf count = 1277

$$\left\{\left\{y(x)\to-\frac{1}{2}\sqrt{\frac{16\sqrt[3]{2}\left(x^3+3c_1\right)}{\sqrt[3]{104976x^2-\sqrt{11019960576x^4-4\left(144x^3+432c_1\right)^3}}}+\frac{\sqrt[3]{104976x^2-\sqrt{11019960576x^4-4}}}{9\sqrt[3]{2}}}\right.\right.$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 21

$$\left\{\frac{x^3}{3}-3\,xy(x)+\frac{\left(y(x)\right)^4}{4}+\_C1=0\right\}$$

2.306 ODE No. 306

$$\left(y(x)^3 - x^3\right) y'(x) - x^2 y(x) = 0$$

✓ **Mathematica** : cpu = 0.0531372 (sec), leaf count = 201

$$\left\{\left\{y(x) \to \sqrt[3]{x^3 - \sqrt{x^6 - e^{6c_1}}}\right\}, \left\{y(x) \to -\sqrt[3]{-1}\sqrt[3]{x^3 - \sqrt{x^6 - e^{6c_1}}}\right\}, \left\{y(x) \to (-1)^{2/3}\sqrt[3]{x^3 - \sqrt{x^6 - e^{6c_1}}}\right\}, \right.$$

✓ **Maple** : cpu = 0.382 (sec), leaf count = 231

$$\left\{y(x) = x\frac{1}{\sqrt[3]{-\left(x^3\_C1 - \sqrt{\_C1^2 x^6 + 1}\right)x^3\_C1}}, y(x) = x\frac{1}{\sqrt[3]{-\left(x^3\_C1 + \sqrt{\_C1^2 x^6 + 1}\right)x^3\_C1}}, y(x) = 4 - \right.$$

2.307 ODE No. 307

$$y(x)\left(a + x^2 + y(x)^2\right) y'(x) + x\left(-a + x^2 + y(x)^2\right) = 0$$

✓ **Mathematica** : cpu = 0.0278458 (sec), leaf count = 149

$$\left\{\left\{y(x) \to -\sqrt{-\sqrt{a^2 + 4ax^2 + 4c_1} - a - x^2}\right\}, \left\{y(x) \to \sqrt{-\sqrt{a^2 + 4ax^2 + 4c_1} - a - x^2}\right\}, \left\{y(x) \to -\sqrt{\sqrt{a^2 - \right.\right.$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 125

$$\left\{y(x) = \sqrt{-x^2 - a - \sqrt{4\,ax^2 + a^2 - 4\_C1}}, y(x) = \sqrt{-x^2 - a + \sqrt{4\,ax^2 + a^2 - 4\_C1}}, y(x) = -\sqrt{-x^2 - a - \right.$$

2.308 ODE No. 308

$$2y(x)^3 y'(x) + xy(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.00898126 (sec), leaf count = 55

$$\left\{\{y(x) \to 0\}, \left\{y(x) \to -\frac{\sqrt{4c_1 - x^2}}{\sqrt{2}}\right\}, \left\{y(x) \to \frac{\sqrt{4c_1 - x^2}}{\sqrt{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 37

$$\left\{y(x) = 0, y(x) = -\frac{1}{2}\sqrt{-2\,x^2 + 4\_C1}, y(x) = \frac{1}{2}\sqrt{-2\,x^2 + 4\_C1}\right\}$$

2.309 ODE No. 309

$$-2x^3+\left(2y(x)^3+y(x)\right)y'(x)-x=0$$

✓ **Mathematica** : cpu = 0.0148744 (sec), leaf count = 151

$$\left\{\left\{y(x)\to -\frac{\sqrt{-\sqrt{8c_1+4x^4+4x^2+1}-1}}{\sqrt{2}}\right\},\left\{y(x)\to \frac{\sqrt{-\sqrt{8c_1+4x^4+4x^2+1}-1}}{\sqrt{2}}\right\},\left\{y(x)\to -\frac{\sqrt{\sqrt{8c_1+}\right.\right.$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 113

$$\left\{y(x)=-\frac{1}{2}\sqrt{-2-2\sqrt{4\,x^4+4\,x^2+8\,\_C1+1}},y(x)=\frac{1}{2}\sqrt{-2-2\sqrt{4\,x^4+4\,x^2+8\,\_C1+1}},y(x)=-\frac{1}{2}\sqrt{-2}\right.$$

2.310 ODE No. 310

$$x^3+\left(5x^2y(x)+2y(x)^3\right)y'(x)+5xy(x)^2=0$$

✓ **Mathematica** : cpu = 0.0477237 (sec), leaf count = 159

$$\left\{\left\{y(x)\to -\frac{\sqrt{-\sqrt{2e^{4c_1}+23x^4}-5x^2}}{\sqrt{2}}\right\},\left\{y(x)\to \frac{\sqrt{-\sqrt{2e^{4c_1}+23x^4}-5x^2}}{\sqrt{2}}\right\},\left\{y(x)\to -\frac{\sqrt{\sqrt{2e^{4c_1}+23x^4}-}\right.\right.$$

✓ **Maple** : cpu = 0.22 (sec), leaf count = 125

$$\left\{y(x)=-\frac{1}{2}\sqrt{-10\,\_C1\,x^2-2\sqrt{23\,x^4\_C1^2+2}}\frac{1}{\sqrt{\_C1}},y(x)=\frac{1}{2}\sqrt{-10\,\_C1\,x^2-2\sqrt{23\,x^4\_C1^2+2}}\frac{1}{\sqrt{\_C1}},y\right.$$

2.311 ODE No. 311

$$4x^3+9x^2y(x)+\left(3x^3+6x^2y(x)-3xy(x)^2+20y(x)^3\right)y'(x)+6xy(x)^2-y(x)^3=0$$

✓ **Mathematica** : cpu = 0.176528 (sec), leaf count = 2201

$$\left\{\left\{y(x)\to \frac{x}{20}+\frac{1}{2}\sqrt{-\frac{39x^2}{100}+\frac{\sqrt[3]{99x^6+351e^{c_1}x^2+\sqrt{3}\sqrt{-67037x^{12}+185406e^{c_1}x^8-83733e^{2c_1}x^4+32000e^{3c_1}}}}{5\sqrt[3]{2}3^{2/3}}}\right.\right.$$

✓ **Maple** : cpu = 0.191 (sec), leaf count = 50

$$\left\{y(x)=\frac{RootOf\left(x^4\_C1^4+3\,x^3\_C1^3\_Z+3\,\_C1^2\_Z^2x^2-\_C1\,\_Z^3x+5\,\_Z^4-1\right)}{\_C1}\right\}$$

2.312 ODE No. 312

$$(y(x)y'(x)+x)\left(\frac{x^2}{a}+\frac{y(x)^2}{b}\right)+\frac{(a-b)\,(y(x)y'(x)-x)}{a+b}=0$$

✓ **Mathematica** : cpu = 0.251683 (sec), leaf count = 204

$$\left\{\left\{y(x)\to -\frac{\sqrt{b}\sqrt{a^2+2a^2W\left(\frac{c_1(a+b)e^{\frac{bx^2}{2a^2}-\frac{b}{2a}-\frac{x^2}{2b}-\frac{1}{2}}}{2a^3b^2}\right)+ab-ax^2-bx^2}}{\sqrt{a}\sqrt{a+b}}\right\},\left\{y(x)\to \frac{\sqrt{b}\sqrt{a^2+2a^2W\left(\frac{c_1(a+b)e}{\sqrt{}}\right.}}{\sqrt{}}\right.$$

✓ **Maple** : cpu = 1.655 (sec), leaf count = 240

$$\left\{y(x)=\frac{1}{a}\sqrt{\left(e^{\frac{1}{2a^2b}\left(-2\,lambertW\left(1/2\,\frac{(a+b)e^{-1/2}}{a^2b}e^{-1/2\,\frac{x^2}{b}}e^{1/2\,\frac{bx^2}{a^2}}e^{-1/2\,\frac{b}{a}}\left(e^{\frac{-C1}{ab}}\right)^{-1}\right)a^2b+(-x^2-b)a^2+(-b^2-2\_C1)a+b^2x^2\right)}+\right.\right.$$

2.313 ODE No. 313

$$y'(x)\left(3axy(x)^2+2ay(x)^3-bx^3+cx^2\right)-ay(x)^3+2bx^3+3bx^2y(x)+cy(x)^2=0$$

✓ **Mathematica** : cpu = 0.0887803 (sec), leaf count = 537

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{2}(3acx+3ac_1)}{3a\sqrt[3]{\sqrt{\left(27a^2bx^3+27a^2c_1x\right)^2+4\left(3acx+3ac_1\right)^3}+27a^2bx^3+27a^2c_1x}}-\frac{\sqrt[3]{\sqrt{(27a^2bx^3+27a^2c_1x)^2}}}{}\right.\right.$$

✓ **Maple** : cpu = 0.22 (sec), leaf count = 748

$$\left\{y(x)=-\frac{1}{12\,a}\left(\left((12\,icx-12\,i\_C1)\,a+i\left(\left(-108\,bx^3+108\,\_C1\,x+12\sqrt{81\,ab^2x^6-162\,\_C1\,abx^4+12\,c^3x}\right.\right.\right.\right.\right.$$

2.314 ODE No. 314

$$xy(x)^3y'(x) + y(x)^4 - x\sin(x) = 0$$

✓ **Mathematica** : cpu = 0.0452701 (sec), leaf count = 188

$$\left\{\left\{y(x) \to -\frac{\sqrt[4]{c_1 - 4x^4\cos(x) + 16x^3\sin(x) + 48x^2\cos(x) - 96x\sin(x) - 96\cos(x)}}{x}\right\}, \left\{y(x) \to -\frac{i\sqrt[4]{c_1 - 4x^4}}{x}\right.\right.$$

✓ **Maple** : cpu = 0.051 (sec), leaf count = 158

$$\left\{y(x) = \frac{1}{x}\sqrt[4]{(-4x^4 + 48x^2 - 96)\cos(x) + (16x^3 - 96x)\sin(x) + \_C1}, y(x) = \frac{-i}{x}\sqrt[4]{(-4x^4 + 48x^2 - 96)\cos(x}\right.$$

2.315 ODE No. 315

$$\left(2xy(x)^3 - x^4\right)y'(x) + 2x^3y(x) - y(x)^4 = 0$$

✓ **Mathematica** : cpu = 0.113302 (sec), leaf count = 368

$$\left\{\left\{y(x) \to \frac{\sqrt[3]{\frac{2}{3}}e^{c_1}x}{\sqrt[3]{\sqrt{3}\sqrt{27x^6 - 4e^{3c_1}x^3} - 9x^3}} + \frac{\sqrt[3]{\sqrt{3}\sqrt{27x^6 - 4e^{3c_1}x^3} - 9x^3}}{\sqrt[3]{2}3^{2/3}}\right\}, \left\{y(x) \to -\frac{\left(1 + i\sqrt{3}\right)e^{c_1}}{2^{2/3}\sqrt[3]{3}\sqrt[3]{\sqrt{3}\sqrt{27x^6 - 4}}}\right.\right.$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 376

$$\left\{y(x) = \frac{\sqrt[3]{12}}{6\_C1}\left(x\sqrt[3]{12}\_C1 + \left(x\left(-9\_C1\,x^2 + \sqrt{3}\sqrt{\frac{27\_C1^3x^4 - 4x}{\_C1}}\right)\_C1^2\right)^{\frac{2}{3}}\right)\frac{1}{\sqrt[3]{x\left(-9\_C1\,x^2 + \sqrt{3}\right.}}\right.$$

2.316 ODE No. 316

$$\left(2xy(x)^3 + y(x)\right)y'(x) + 2y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0407414 (sec), leaf count = 48

$$\left\{\{y(x) \to 0\}, \text{Solve}\left[x = c_1e^{-\frac{1}{2}y(x)^2} - \frac{1}{4}e^{-\frac{1}{2}y(x)^2}\text{Ei}\left(\frac{y(x)^2}{2}\right), y(x)\right]\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 53

$$\left\{y(x) = 0, y(x) = \sqrt{-2\,RootOf\left(\mathrm{e}^{-Z}Ei\left(1, \_Z\right) + 4\,\mathrm{e}^{-Z}\_C1 - 4x\right)}, y(x) = -\sqrt{-2\,RootOf\left(\mathrm{e}^{-Z}Ei\left(1, \_Z\right) + 4\,\mathrm{e}^{-}\right.}\right.$$

2.317 ODE No. 317

$$\left(x^2+2xy(x)^3+xy(x)\right)y'(x)+y(x)^2-xy(x)=0$$

✓ **Mathematica** : cpu = 0.332684 (sec), leaf count = 23

$$\text{Solve}\left[y(x)^2-\frac{x}{y(x)}+\log(y(x))+\log(x)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.124 (sec), leaf count = 29

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-\left(\mathrm{e}^{-Z}\right)^3-\mathrm{e}^{-Z}\ln(x)+\mathrm{e}^{-Z}\_C1-\_Z\,\mathrm{e}^{-Z}+x\right)}\right\}$$

2.318 ODE No. 318

$$\left(3xy(x)^3-4xy(x)+y(x)\right)y'(x)+\left(y(x)^2-2\right)y(x)^2=0$$

✓ **Mathematica** : cpu = 0.151747 (sec), leaf count = 4284

$$\left\{\{y(x)\to 0\},\left\{y(x)\to -\sqrt{\frac{4\sqrt[3]{2}x^2}{3\sqrt[3]{16x^6+24x^5-27c_1^2x^4+12x^4+2x^3+3\sqrt{3}\sqrt{-32c_1^2x^{10}-48c_1^2x^9+27c_1^4x^8-24c}}}}\right.\right.$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 28

$$\left\{x+(y(x))^{-2}-\frac{\_C1}{(y(x))^2}\frac{1}{\sqrt{(y(x))^2-2}}=0,y(x)=0\right\}$$

2.319 ODE No. 319

$$\left(7xy(x)^3+y(x)-5x\right)y'(x)+y(x)^4-5y(x)=0$$

✓ **Mathematica** : cpu = 0.0251151 (sec), leaf count = 302

$$\left\{\left\{y(x)\to \text{Root}\left[10\#1^7x+2\#1^5-100\#1^4x-25\#1^2+250\#1x-10c_1\&,1\right]\right\},\{y(x)\to \text{Root}\left[10\#1^7x+2\#1^5-\right.\right.$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 35

$$\left\{x+\frac{2(y(x))^5-25(y(x))^2-10\_C1}{10y(x)\left((y(x))^3-5\right)^2}=0\right\}$$

2.320 ODE No. 320

$$\left(x^2 y(x)^3 + x y(x)\right) y'(x) - 1 = 0$$

✓ **Mathematica** : cpu = 0.0596255 (sec), leaf count = 76

$$\left\{\left\{y(x) \to -\frac{\sqrt{2xW\left(c_1 e^{\frac{1}{2x}-1}\right)+2x-1}}{\sqrt{x}}\right\}, \left\{y(x) \to \frac{\sqrt{2xW\left(c_1 e^{\frac{1}{2x}-1}\right)+2x-1}}{\sqrt{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 78

$$\left\{y(x) = \frac{1}{x}\sqrt{2\,x^2 lambertW\left(1/2\_C1\,\mathrm{e}^{-1/2\,\frac{2x-1}{x}}\right)+2\,x^2-x}, y(x) = -\frac{1}{x}\sqrt{2\,x^2 lambertW\left(1/2\_C1\,\mathrm{e}^{-1/2\,\frac{2x-1}{x}}\right)}\right.$$

2.321 ODE No. 321

$$\left(2x^2 y(x)^3 + x^2 y(x)^2 - 2x\right) y'(x) - 2y(x) - 1 = 0$$

✓ **Mathematica** : cpu = 0.183395 (sec), leaf count = 47

$$\text{Solve}\left[\frac{1}{64}\left(-4y(x)^2+4y(x)-2\log(8y(x)+4)+3\right)-\frac{1}{4x(2y(x)+1)} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.173 (sec), leaf count = 42

$$\left\{y(x) = \frac{\mathrm{e}^{RootOf\left(x\left(\mathrm{e}^{\_Z}\right)^3-4x\left(\mathrm{e}^{\_Z}\right)^2+8\_C1\,x\mathrm{e}^{\_Z}+2\_Z\,x\mathrm{e}^{\_Z}+3x\mathrm{e}^{\_Z}+16\right)}}{2}-\frac{1}{2}\right\}$$

2.322 ODE No. 322

$$\left(10x^2 y(x)^3 - 3y(x)^2 - 2\right) y'(x) + 5x y(x)^4 + x = 0$$

✓ **Mathematica** : cpu = 0.211643 (sec), leaf count = 2077

$$\left\{\left\{y(x) \to -\frac{1}{2}\sqrt{\frac{4\sqrt[3]{2}\left(5x^4-10c_1x^2-2\right)}{5x^2\sqrt[3]{2268x^2-216c_1+\sqrt{\left(2160x^2+108\left(x^2-2c_1\right)\right)^2-4\left(60x^4-120c_1x^2-24\right)^3}}}+\frac{\sqrt[3]{2268x^2}}{}\right.\right.$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 29

$$\left\{\frac{5\,x^2(y(x))^4}{2}-(y(x))^3+\frac{x^2}{2}-2\,y(x)+\_C1=0\right\}$$

2.323 ODE No. 323

$$xy'(x)\left(axy(x)^3+c\right)+y(x)\left(bx^3y(x)+c\right)=0$$

✓ **Mathematica** : cpu = 0.0470329 (sec), leaf count = 463

$$\left\{\left\{y(x)\to\frac{\sqrt[3]{54a^2cx^2+\sqrt{2916a^4c^2x^4+108a^3x^3\left(bx^3-2c_1x\right)^3}}}{3\sqrt[3]{2}ax}-\frac{\sqrt[3]{2}\left(bx^3-2c_1x\right)}{\sqrt[3]{54a^2cx^2+\sqrt{2916a^4c^2x^4+108a^3x^3\left(bx^3-\right.}}\right.\right.$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 630

$$\left\{y(x)=-\frac{3^{\frac{2}{3}}}{18\,ax}\left(\left(3\,i\left(bx^2-2\_C1\right)x^2a+i\left(\left(27\,c+3\sqrt{\frac{3\,b^3x^8-18\_C1\,b^2x^6+36\_C1^2bx^4-24\_C1^3x^2+}{a}}\right.\right.\right.\right.\right.$$

2.324 ODE No. 324

$$\left(2x^3y(x)^3-x\right)y'(x)+2x^3y(x)^3-y(x)=0$$

✓ **Mathematica** : cpu = 0.0359007 (sec), leaf count = 723

$$\left\{\left\{y(x)\to-\frac{2x^3-c_1x^2}{6x^2}+\frac{\sqrt[3]{12c_1x^8-6c_1^2x^7+c_1^3x^6+3\sqrt{3}\sqrt{-24c_1x^{12}+12c_1^2x^{11}-2c_1^3x^{10}+16x^{13}+27x^8}-8x}}{6x^2}\right.\right.$$

✓ **Maple** : cpu = 0.137 (sec), leaf count = 815

$$\left\{y(x)=\frac{1}{12\,x}\left(\left(2\_C1\,x-4\,x^2\right)\sqrt[3]{\left(\_C1^3x^2-6\_C1^2x^3+12\_C1\,x^4-8\,x^5+3\,\sqrt{-6\_C1^3x^2+36\_C1^2x^3-}\right.}\right.\right.$$

2.325 ODE No. 325

$$y(x)\left(y(x)^3-2x^3\right)y'(x)+x\left(2y(x)^3-x^3\right)=0$$

✓ **Mathematica** : cpu = 0.054244 (sec), leaf count = 139

$$\text{Solve}\left[\frac{1}{7}\text{RootSum}\left[\#1^4+\#1^3+3\#1^2+\#1+1\&,\frac{8\#1^3\log\left(\frac{y(x)}{x}-\#1\right)+9\#1^2\log\left(\frac{y(x)}{x}-\#1\right)+12\#1\log\left(\frac{y}{}\right.\right.\right.}{4\#1^3+3\#1^2+6\#1+1}$$

✓ **Maple** : cpu = 0.508 (sec), leaf count = 124

$$\left\{\frac{1}{7}\ln\left(\frac{y(x)-x}{x}\right)-\frac{2}{7}\ln\left(\frac{4x^4+4x^3y(x)+12x^2(y(x))^2+4x(y(x))^3+4(y(x))^4}{x^4}\right)-\frac{2\sqrt{3}}{7}\arctan\left(\frac{(x+2y(x)}{3x}\right.\right.$$

2.326 ODE No. 326

$$y(x)y'(x)\left((ay(x)+bx)^3+bx^3\right)+x\left((ay(x)+bx)^3+ay(x)^3\right)=0$$

✓ **Mathematica** : cpu = 4.93203 (sec), leaf count = 13289

✓ **Maple** : cpu = 0.494 (sec), leaf count = 160

$$\left\{y(x)=\frac{x\left(\_C1\,x-bRootOf\left(b^2\_Z^4-2bx\_C1\,\_Z^3+\left(a^2x^2\_C1^2+b^2x^2\_C1^2+\_C1^2x^2-a^2\right)\_Z^2-2bx^3\_\right.\right.\right.}{aRootOf\left(b^2\_Z^4-2bx\_C1\,\_Z^3+\left(a^2x^2\_C1^2+b^2x^2\_C1^2+\_C1^2x^2-a^2\right)\_Z^2-2bx^3\_C1^3\right.}$$

2.327 ODE No. 327

$$\left(2x^2y(x)^3+xy(x)^4+2y(x)+x\right)y'(x)+y(x)^5+y(x)=0$$

✓ **Mathematica** : cpu = 0.403749 (sec), leaf count = 669

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{9c_1^2x^2+3\sqrt{3}\sqrt{-4c_1^3x^6-c_1^4x^4+18c_1^2x^4+4c_1^3x^2+27x^4}+2c_1^3+27x^2}}{3\sqrt[3]{2}x}-\frac{}{3x\sqrt[3]{9c_1^2x^2+3\sqrt{3}\sqrt{-4c_1^3}}}\right.\right.$$

✓ **Maple** : cpu = 0.175 (sec), leaf count = 583

$$\left\{y(x)=\frac{1}{12\_C1\,x}\left(\left(-12\,ix^2\_C1-i\left(108\,\_C1^3x^2+12\,\sqrt{3}\sqrt{27\,\_C1^4x^2+18\,\_C1^2x^2+(4\,x^4-4)\,\_C1-x^2}\right.\right.\right.\right.$$

2.328 ODE No. 328

$$ax^2y(x)^ny'(x)-2xy'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.099213 (sec), leaf count = 42

$$\text{Solve}\left[\frac{n(\log(x)-\log\left(-axy(x)^n+n+2\right))}{n+2}-\frac{2n\log(y(x))}{n+2}=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.193 (sec), leaf count = 33

$$\left\{\frac{\left((y(x))^n\,ax-n-2\right)^n\left((y(x))^n\right)^2}{x^n}-\_C1=0\right\}$$

2.329 ODE No. 329

$$x^ny(x)^m\left(axy'(x)+by(x)\right)+\alpha xy'(x)+\beta y(x)=0$$

✓ **Mathematica** : cpu = 0.331328 (sec), leaf count = 102

$$\text{Solve}\left[\frac{m((a\beta-\alpha b)\log\left(x^ny(x)^m(bm-an)-\alpha n+\beta m\right)+\beta\log(x)(bm-an))}{(bm-an)(\beta m-\alpha n)}+\frac{\alpha m\log(\beta my(x)-\alpha ny(x))}{\beta m-\alpha n}=c\right.$$

✓ **Maple** : cpu = 0.355 (sec), leaf count = 71

$$\left\{\left(x^n(an-bm)\left(y(x)\right)^m-\beta\,m+\alpha\,n\right)^{-a\beta\,m+\alpha\,bm}\left(\left(y(x)\right)^m\right)^{\alpha\,(an-bm)}x^{\beta\,m(an-bm)}-\_C1=0\right\}$$

2.330 ODE No. 330

$$(f(y(x)+x)+1)y'(x)+f(y(x)+x)=0$$

✓ **Mathematica** : cpu = 32.4657 (sec), leaf count = 49

$$\text{Solve}\left[\int_1^{y(x)}\left(-\int_1^x f'(K[1]+K[2])\,dK[1]+f(K[2]+x)+1\right)dK[2]+\int_1^x f(K[1]+y(x))\,dK[1]=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 22

$$\left\{y(x)=-x+RootOf\left(-x+\int^{-Z}1+f(\_a)\,d\_a+\_C1\right)\right\}$$

2.331 ODE No. 331

$$y'(x)\left(\sum_{\nu=1}^{p}y(x)^\nu f(\nu)(x)\right)-\sum_{\nu=1}^{q}y(x)^\nu g(\nu)(x)=0$$

✗ **Mathematica** : cpu = 54.788 (sec), leaf count = 0 , could not solve

```
DSolve[-Sum[y[x]^nu*g[nu][x], {nu, 1, q}] + Sum[y[x]^nu*f[nu][x], {nu, 1, p}]*Derivative[1][
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.332 ODE No. 332

$$x\left(\sqrt{xy(x)}-1\right)y'(x)-y(x)\left(\sqrt{xy(x)}+1\right)=0$$

✓ **Mathematica** : cpu = 0.0833755 (sec), leaf count = 24

$$\text{Solve}\left[\frac{2}{\sqrt{xy(x)}}+\log(y(x))-\log(x)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 33

$$\left\{-1\left(1+\left(\_C1-\ln(x)+\frac{\ln(xy(x))}{2}\right)\sqrt{xy(x)}\right)\frac{1}{\sqrt{xy(x)}}=0\right\}$$

2.333 ODE No. 333

$$-x^{3/2}y(x)^{5/2}+\left(2x^{5/2}y(x)^{3/2}+x^2y(x)-x\right)y'(x)+xy(x)^2-y(x)=0$$

✓ **Mathematica** : cpu = 0.169608 (sec), leaf count = 72

$$\text{Solve}\left[\frac{2\sqrt{xy(x)}\log(y(x))}{\sqrt{x}\sqrt{y(x)}}-\frac{\sqrt{xy(x)}\left(3x^{3/2}y(x)^{3/2}\log(x)+6xy(x)-2\right)}{3x^2y(x)^2}=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.102 (sec), leaf count = 32

$$\left\{\ln\left(y(x)\right)-1\frac{1}{\sqrt{x}}\frac{1}{\sqrt{y\left(x\right)}}+\frac{1}{3}(y(x))^{-\frac{3}{2}}x^{-\frac{3}{2}}-\frac{\ln\left(x\right)}{2}-\_C1=0\right\}$$

2.334 ODE No. 334

$$\left(\sqrt{y(x)+x}+1\right)y'(x)+1=0$$

✓ **Mathematica** : cpu = 0.0365861 (sec), leaf count = 39

$$\left\{\left\{y(x)\to-2\sqrt{c_1+x+1}+c_1+2\right\},\left\{y(x)\to2\sqrt{c_1+x+1}+c_1+2\right\}\right\}$$

✓ **Maple** : cpu = 0.025 (sec), leaf count = 19

$$\left\{-y(x)-2\sqrt{y\left(x\right)+x}-\_C1=0\right\}$$

2.335 ODE No. 335

$$\sqrt{y(x)^2-1}y'(x)-\sqrt{x^2-1}=0$$

✓ **Mathematica** : cpu = 0.179878 (sec), leaf count = 75

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[\frac{1}{2}\#1\sqrt{\#1^2-1}-\frac{1}{2}\log\left(\sqrt{\#1^2-1}+\#1\right)\&\right]\left[c_1+\frac{1}{2}\sqrt{x^2-1}x-\frac{1}{2}\log\left(\sqrt{x^2-1}\right.\right.\right.$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 50

$$\left\{\_C1+x\sqrt{x^2-1}-\ln\left(x+\sqrt{x^2-1}\right)-y(x)\sqrt{\left(y\left(x\right)\right)^2-1}+\ln\left(y(x)+\sqrt{\left(y\left(x\right)\right)^2-1}\right)=0\right\}$$

2.336 ODE No. 336

$$\left(ax+\sqrt{y(x)^2+1}\right)y'(x)+ay(x)+\sqrt{x^2+1}=0$$

✓ **Mathematica** : cpu = 0.0632937 (sec), leaf count = 53

$$\text{Solve}\left[axy(x)+\frac{1}{2}\sqrt{x^2+1}x+\frac{1}{2}\left(y(x)\sqrt{y(x)^2+1}+\sinh^{-1}(y(x))\right)+\frac{1}{2}\sinh^{-1}(x)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 41

$$\left\{\frac{x}{2}\sqrt{x^2+1}+\frac{Arcsinh(x)}{2}+axy(x)+\frac{y(x)}{2}\sqrt{(y\left(x\right))^2+1}+\frac{Arcsinh(y(x))}{2}+\_C1=0\right\}$$

2.337 ODE No. 337

$$\left(\sqrt{x^2+y(x)^2}+x\right)y'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.05922 (sec), leaf count = 52

$$\left\{\left\{y(x)\to -e^{\frac{c_1}{2}}\sqrt{e^{c_1}+2x}\right\},\left\{y(x)\to e^{\frac{c_1}{2}}\sqrt{e^{c_1}+2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.059 (sec), leaf count = 28

$$\left\{-\_C1+\frac{1}{(y\left(x\right))^2}\sqrt{(y\left(x\right))^2+x^2}+\frac{x}{(y\left(x\right))^2}=0\right\}$$

2.338 ODE No. 338

$$y'(x)\left(\sin(\alpha)\left(y(x)^2-x^2\right)-2x\cos(\alpha)y(x)+\sqrt{x^2+y(x)^2}y(x)\right)+\cos(\alpha)\left(y(x)^2-x^2\right)+2x\sin(\alpha)y(x)+x\sqrt{x^2+y}$$

✓ **Mathematica** : cpu = 102.971 (sec), leaf count = 17681

$$\left\{\left\{y(x)\to -\frac{1}{2}e^{c_1}\sin(\alpha)-\frac{1}{2}\sqrt{e^{2c_1}\sin^2(\alpha)+\frac{1}{6}\left(4x^2-4e^{c_1}\cos(\alpha)x-e^{2c_1}-e^{2c_1}\cos(2\alpha)\right)+\frac{1}{2}\left(-4x^2+4e^{c_1}\cos(\right.\right.\right.$$

✓ **Maple** : cpu = 0.744 (sec), leaf count = 129

$$\left\{y(x) = RootOf\left(-\ln(x) + \int^{-Z} \frac{1}{(\_a^2+1)(\cos(2\alpha)\_a^2 + 2\_a\sin(2\alpha) + \_a^2 - \cos(2\alpha) + 1)}\left(-\cos(2\alpha)\_\right.\right.$$

2.339 ODE No. 339

$$\left(x\sqrt{x^2+y(x)^2+1} - y(x)\left(x^2+y(x)^2\right)\right)y'(x) - \sqrt{x^2+y(x)^2+1}y(x) - x\left(x^2+y(x)^2\right) = 0$$

✓ **Mathematica** : cpu = 0.108413 (sec), leaf count = 27

$$\text{Solve}\left[\sqrt{x^2+y(x)^2+1} + \tan^{-1}\left(\frac{x}{y(x)}\right) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.183 (sec), leaf count = 27

$$\left\{\arctan\left(\frac{y(x)}{x}\right) - \sqrt{x^2+(y(x))^2+1} - \_C1 = 0\right\}$$

2.340 ODE No. 340

$$y'(x)\left(\frac{\text{e1}(a+x)}{((a+x)^2+y(x)^2)^{3/2}} + \frac{\text{e2}(x-a)}{((x-a)^2+y(x)^2)^{3/2}}\right) - y(x)\left(\frac{\text{e1}}{((a+x)^2+y(x)^2)^{3/2}} + \frac{\text{e2}}{((x-a)^2+y(x)^2)^{3/2}}\right)$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

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$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

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time expired
```

2.341 ODE No. 341

$$\left(xe^{y(x)} + e^x\right)y'(x) + e^x y(x) + e^{y(x)} = 0$$

✓ **Mathematica** : cpu = 0.0535615 (sec), leaf count = 33

$$\left\{\left\{y(x) \to c_1 e^{-x} - W\left(xe^{c_1 e^{-x} - x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.065 (sec), leaf count = 30

$$\left\{y(x) = -lambertW\left(\frac{x}{\mathrm{e}^x}\left(\mathrm{e}^{\frac{-C1}{\mathrm{e}^x}}\right)^{-1}\right) - \frac{\_C1}{\mathrm{e}^x}\right\}$$

2.342 ODE No. 342

$$x\left(2e^{-xy(x)}+3e^{xy(x)}\right)\left(xy'(x)+y(x)\right)+1=0$$

✓ **Mathematica** : cpu = 0.264993 (sec), leaf count = 163

$$\left\{\left\{y(x)\to -\frac{\cosh^{-1}\left(\frac{1}{24}\left(-5\sqrt{\log^2\left(\frac{c_1}{x}\right)+24}-\log\left(\frac{c_1}{x}\right)\right)\right)}{x}\right\},\left\{y(x)\to \frac{\cosh^{-1}\left(\frac{1}{24}\left(-5\sqrt{\log^2\left(\frac{c_1}{x}\right)+24}-\log\left(\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 17

$$\left\{y(x)=\frac{1}{x}\ln\left(-\frac{\ln(x)}{5}+\frac{\_C1}{5}\right)\right\}$$

2.343 ODE No. 343

$$y'(x)(\log(y(x))+x)-1=0$$

✓ **Mathematica** : cpu = 0.0394093 (sec), leaf count = 35

$$\text{Solve}\left[x=c_1e^{y(x)}+e^{y(x)}\left(\text{Ei}(-y(x))-e^{-y(x)}\log(y(x))\right),y(x)\right]$$

✓ **Maple** : cpu = 0.047 (sec), leaf count = 27

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-\_Z-x-\mathrm{e}^{\mathrm{e}^{-\_Z}}Ei\left(1,\mathrm{e}^{-\_Z}\right)+\_C1\,\mathrm{e}^{\mathrm{e}^{-\_Z}}\right)}\right\}$$

2.344 ODE No. 344

$$y'(x)(\log(y(x))+2x-1)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.02089 (sec), leaf count = 23

$$\left\{\left\{y(x)\to -\frac{W\left(-2c_1e^{-2x}\right)}{2c_1}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 19

$$\left\{y(x)=\mathrm{e}^{-lambertW\left(-2\,\mathrm{e}^{-2\,x}\_C1\right)-2\,x}\right\}$$

2.345 ODE No. 345

$$xy'(x)\left(2x^2y(x)\log(y(x))+1\right)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.0434769 (sec), leaf count = 35

$$\text{Solve}\left[\frac{y(x)}{x^2}+2\left(\frac{1}{2}y(x)^2\log(y(x))-\frac{y(x)^2}{4}\right)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 36

$$\left\{y(x)=\mathrm{e}^{RootOf\left(2\_Z\,x^2\left(\mathrm{e}^{-\_Z}\right)^2-x^2\left(\mathrm{e}^{-\_Z}\right)^2+2\_C1\,x^2+2\mathrm{e}^{-\_Z}\right)}\right\}$$

2.346 ODE No. 346

$$xy'(x)(-ax+y(x)+y(x)\log(xy(x)))-y(x)(ax\log(xy(x))+ax-y(x))=0$$

✓ **Mathematica** : cpu = 0.057926 (sec), leaf count = 24

$$\text{Solve}[ax\log(xy(x))-y(x)\log(xy(x))=c_1,y(x)]$$

✓ **Maple** : cpu = 0.276 (sec), leaf count = 19

$$\left\{(xy(x))^{-ax+y(x)}-\_C1=0\right\}$$

2.347 ODE No. 347

$$(\sin(x)+1)y'(x)\sin(y(x))+\cos(x)(\cos(y(x))-1)=0$$

✓ **Mathematica** : cpu = 0.126318 (sec), leaf count = 32

$$\left\{\{y(x)\to 0\},\left\{y(x)\to 2\sin^{-1}\left(\frac{1}{4}c_1\left(\sin\left(\frac{x}{2}\right)+\cos\left(\frac{x}{2}\right)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.153 (sec), leaf count = 16

$$\{y(x)=\pi-\arccos\left(\sin\left(x\right)\_C1+\_C1-1\right)\}$$

2.348 ODE No. 348

$$y'(x)(x\cos(y(x))+\sin(x))+\sin(y(x))+y(x)\cos(x)=0$$

✓ **Mathematica** : cpu = 0.0496961 (sec), leaf count = 17

$$\text{Solve}[x\sin(y(x))+y(x)\sin(x)=c_1,y(x)]$$

✓ **Maple** : cpu = 0.101 (sec), leaf count = 15

$$\{y(x)\sin(x)+x\sin(y(x))+\_C1=0\}$$

2.349 ODE No. 349

$$xy'(x)\cot\left(\frac{y(x)}{x}\right)+2x\sin\left(\frac{y(x)}{x}\right)-y(x)\cot\left(\frac{y(x)}{x}\right)=0$$

✓ **Mathematica** : cpu = 0.0421346 (sec), leaf count = 15

$$\left\{\left\{y(x)\to x\csc^{-1}\left(2(c_1+\log(x))\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 17

$$\left\{y(x)=\arcsin\left(\left(2\ln(x)+2\_C1\right)^{-1}\right)x\right\}$$

2.350 ODE No. 350

$$y'(x)\cos(y(x))-\sin(y(x))-\cos(x)\sin^2(y(x))=0$$

✓ **Mathematica** : cpu = 0.577675 (sec), leaf count = 53

$$\left\{\left\{y(x)\to\csc^{-1}\left(\frac{1}{2}\left(-2c_1e^{-x}-\sin(x)-\cos(x)\right)\right)\right\},\left\{y(x)\to-\csc^{-1}\left(\frac{1}{2}\left(2c_1e^{-x}+\sin(x)+\cos(x)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 1.077 (sec), leaf count = 226

$$\left\{y(x)=\arctan\left(-2\,\frac{e^{x}}{e^{x}\left(\cos\left(x\right)+\sin\left(x\right)\right)+2\_C1},\frac{\sqrt{16}}{4\_C1^{2}+4\,e^{x}\left(\cos\left(x\right)+\sin\left(x\right)\right)\_C1+\left(e^{x}\right)^{2}\left(2\,\cos\left(x\right)\sin\left(\right.\right.\right.\right.$$

2.351 ODE No. 351

$$y'(x)\cos(y(x)) - \sin^3(y(x)) + x\sin(y(x))\cos^2(y(x)) = 0$$

✓ **Mathematica** : cpu = 0.369557 (sec), leaf count = 61

$$\left\{\left\{y(x) \to -\cot^{-1}\left(\sqrt{e^{x^2}\left(4c_1 - \sqrt{\pi}\text{erf}(x)\right)}\right)\right\}, \left\{y(x) \to \cot^{-1}\left(\sqrt{e^{x^2}\left(4c_1 - \sqrt{\pi}\text{erf}(x)\right)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.504 (sec), leaf count = 55

$$\left\{y(x) = -\arcsin\left(\frac{1}{\sqrt{1 - \sqrt{\pi}Erf\left(x\right)\mathrm{e}^{x^2} - 2\_C1\,\mathrm{e}^{x^2}}}\right), y(x) = \arcsin\left(\frac{1}{\sqrt{1 - \sqrt{\pi}Erf\left(x\right)\mathrm{e}^{x^2} - 2\_C1\,\mathrm{e}^{x^2}}}\right)\right\}$$

2.352 ODE No. 352

$$y'(x)\cos(y(x))(\cos(y(x)) - \sin(\alpha)\sin(x)) + \cos(x)(\cos(x) - \sin(\alpha)\sin(y(x))) = 0$$

✓ **Mathematica** : cpu = 0.134269 (sec), leaf count = 43

$$\text{Solve}\left[4\sin(\alpha)\sin(x)\sin(y(x)) - 4\left(\frac{y(x)}{2} + \frac{1}{4}\sin(2y(x))\right) - 2x - \sin(2x) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.302 (sec), leaf count = 33

$$\left\{\frac{(-2\sin\left(\alpha\right)\sin\left(x\right) + \cos\left(y(x)\right))\sin\left(y(x)\right)}{2} + \frac{\cos\left(x\right)\sin\left(x\right)}{2} + \frac{x}{2} + \_C1 + \frac{y(x)}{2} = 0\right\}$$

2.353 ODE No. 353

$$xy'(x)\cos(y(x)) + \sin(y(x)) = 0$$

✓ **Mathematica** : cpu = 0.0207313 (sec), leaf count = 14

$$\left\{\left\{y(x) \to \sin^{-1}\left(\frac{e^{c_1}}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.06 (sec), leaf count = 12

$$\left\{y(x) = \arcsin\left(\frac{1}{\_C1\,x}\right)\right\}$$

2.354 ODE No. 354

$$y'(x)(x\sin(y(x))-1)+\cos(y(x))=0$$

✓ **Mathematica** : cpu = 0.0664468 (sec), leaf count = 145

$$\left\{\left\{y(x)\to -\cos^{-1}\left(\frac{c_1 x-\sqrt{c_1^2-x^2+1}}{c_1^2+1}\right)\right\},\left\{y(x)\to \cos^{-1}\left(\frac{c_1 x-\sqrt{c_1^2-x^2+1}}{c_1^2+1}\right)\right\},\left\{y(x)\to -\cos^{-1}\left(\frac{\sqrt{}\right.\right.\right.$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 108

$$\left\{y(x)=\arctan\left(\frac{1}{\_C1^2+1}\left(-\_C1\sqrt{\_C1^2-x^2+1}+x\right),\frac{1}{\_C1^2+1}\left(\_C1\,x+\sqrt{\_C1^2-x^2+1}\right)\right),y(x)=a\right.$$

2.355 ODE No. 355

$$y'(x)(x\cos(y(x))+\cos(x))+\sin(y(x))-y(x)\sin(x)=0$$

✓ **Mathematica** : cpu = 0.047638 (sec), leaf count = 17

$$\text{Solve}[x\sin(y(x))+y(x)\cos(x)=c_1,y(x)]$$

✓ **Maple** : cpu = 0.1 (sec), leaf count = 15

$$\{y(x)\cos(x)+x\sin(y(x))+\_C1=0\}$$

2.356 ODE No. 356

$$y'(x)\left(x^2\cos(y(x))+2y(x)\sin(x)\right)+2x\sin(y(x))+y(x)^2\cos(x)=0$$

✓ **Mathematica** : cpu = 0.0648504 (sec), leaf count = 21

$$\text{Solve}\left[x^2\sin(y(x))+y(x)^2\sin(x)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 19

$$\left\{(y(x))^2\sin(x)+x^2\sin(y(x))+\_C1=0\right\}$$

2.357 ODE No. 357

$$x \log(x) y'(x) \sin(y(x)) + \cos(y(x))(1 - x \cos(y(x))) = 0$$

✓ **Mathematica** : cpu = 0.307539 (sec), leaf count = 35

$$\left\{\left\{y(x) \to -\sec^{-1}\left(\frac{x - c_1}{\log(x)}\right)\right\}, \left\{y(x) \to \sec^{-1}\left(\frac{x - c_1}{\log(x)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.58 (sec), leaf count = 13

$$\left\{y(x) = \arccos\left(\frac{\ln(x)}{x + \_C1}\right)\right\}$$

2.358 ODE No. 358

$$\cos(x) y'(x) \sin(y(x)) + \sin(x) \cos(y(x)) = 0$$

✓ **Mathematica** : cpu = 0.044794 (sec), leaf count = 29

$$\left\{\left\{y(x) \to -\cos^{-1}\left(\frac{1}{2} c_1 \sec(x)\right)\right\}, \left\{y(x) \to \cos^{-1}\left(\frac{1}{2} c_1 \sec(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 11

$$\left\{y(x) = \arccos\left(\frac{\_C1}{\cos(x)}\right)\right\}$$

2.359 ODE No. 359

$$3 \sin(x) y'(x) \sin(y(x)) + 5 y(x) \cos^4(x) = 0$$

✓ **Mathematica** : cpu = 0.0585234 (sec), leaf count = 45

$$\left\{\left\{y(x) \to \text{SinIntegral}^{(-1)}\left(c_1 - \frac{5}{3}\left(\frac{5\cos(x)}{4} + \frac{1}{12}\cos(3x) + \log\left(\sin\left(\frac{x}{2}\right)\right) - \log\left(\cos\left(\frac{x}{2}\right)\right)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.051 (sec), leaf count = 28

$$\left\{\frac{\cos(3x)}{12} + \frac{5\cos(x)}{4} + \ln(\csc(x) - \cot(x)) + \frac{3\,Si(y(x))}{5} + \_C1 = 0\right\}$$

2.360 ODE No. 360

$$y'(x)\cos(ay(x)) - b(1 - c\cos(ay(x)))\sqrt{c\cos(ay(x)) + \cos^2(ay(x)) - 1} = 0$$

✓ **Mathematica** : cpu = 53.0075 (sec), leaf count = 6218

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{\sqrt{2}(\cos(a\#1)+1)\sqrt{\frac{2c\cos(a\#1)+\cos(2a\#1)-1}{(\cos(a\#1)+1)^2}}\left(-\frac{\left(\sqrt{-\frac{\sqrt{c^2+4}}{c}-\frac{2}{c}}+\sqrt{\frac{\sqrt{c^2+4}}{c}-\frac{2}{c}}\right)\left(\left(\frac{\sqrt{c-1}}{\sqrt{c+1}}+\sqrt{\right.\right.}{}\right.}{}\right.\right.\right.$$

✓ **Maple** : cpu = 0.2 (sec), leaf count = 48

$$\left\{x + \int^{y(x)} 2\,\frac{\cos(\_a\,a)}{b\,(c\cos(\_a\,a)-1)\,\sqrt{2\,\cos(2\,\_a\,a)-2+4\,c\cos(\_a\,a)}}d\_a + \_C1 = 0\right\}$$

2.361 ODE No. 361

$$y'(x)(-\sin(y(x)) + x\sin(xy(x)) + \cos(y(x)+x)) + y(x)\sin(xy(x)) + \cos(y(x)+x) + \cos(x) = 0$$

✓ **Mathematica** : cpu = 0.208398 (sec), leaf count = 31

$$\text{Solve}[\cos(y(x)) - \cos(xy(x)) + \sin(x)\cos(y(x)) + \cos(x)\sin(y(x)) + \sin(x) = c_1, y(x)]$$

✓ **Maple** : cpu = 0.253 (sec), leaf count = 22

$$\{-\cos(xy(x)) + \sin(y(x)+x) + \sin(x) + \cos(y(x)) + \_C1 = 0\}$$

2.362 ODE No. 362

$$y'(x)\left(x^2 y(x)\sin(xy(x))-4x\right)-y(x)+xy(x)^2\sin(xy(x))=0$$

✓ **Mathematica** : cpu = 0.0684394 (sec), leaf count = 23

$$\text{Solve}[-4\log(y(x))-\cos(xy(x))-\log(x)=c_1,y(x)]$$

✓ **Maple** : cpu = 0.231 (sec), leaf count = 23

$$\left\{y(x)=\frac{1}{x}RootOf\left(-\_Z+\mathrm{e}^{-\frac{\cos(\_Z)}{4}}\_C1\,x^{\frac{3}{4}}\right)\right\}$$

2.363 ODE No. 363

$$(xy'(x)-y(x))\cos^2\left(\frac{y(x)}{x}\right)+x=0$$

✓ **Mathematica** : cpu = 0.0359861 (sec), leaf count = 33

$$\text{Solve}\left[\frac{y(x)}{2x}+\frac{1}{4}\sin\left(\frac{2y(x)}{x}\right)=c_1-\log(x),y(x)\right]$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 35

$$\left\{-\frac{1}{2\,x}\left(\cos\left(\frac{y(x)}{x}\right)\sin\left(\frac{y(x)}{x}\right)x+y(x)\right)-\ln(x)-\_C1=0\right\}$$

2.364 ODE No. 364

$$xy'(x)\left(y(x)\sin\left(\frac{y(x)}{x}\right)-x\cos\left(\frac{y(x)}{x}\right)\right)-y(x)\left(y(x)\sin\left(\frac{y(x)}{x}\right)+x\cos\left(\frac{y(x)}{x}\right)\right)=0$$

✓ **Mathematica** : cpu = 0.0649048 (sec), leaf count = 31

$$\text{Solve}\left[-\log\left(\frac{y(x)}{x}\right)-\log\left(\cos\left(\frac{y(x)}{x}\right)\right)=c_1+2\log(x),y(x)\right]$$

✓ **Maple** : cpu = 0.106 (sec), leaf count = 23

$$\left\{y(x)=\frac{\_C1}{\cos\left(RootOf\left(-\_Z\,x^2\cos\left(\_Z\right)+\_C1\right)\right)x}\right\}$$

2.365 ODE No. 365

$$\left(y(x) f\left(x^2+y(x)^2\right)-x\right) y'(x)+x f\left(x^2+y(x)^2\right)+y(x)=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.304 (sec), leaf count = 42

$$\left\{y(x)=x\left(\tan\left(RootOf\left(-2\_Z-\int^{\frac{x^2\left(\tan(\_Z)\right)^2+1\right)}{\left(\tan(\_Z)\right)^2}}\frac{f(\_a)}{\_a}d\_a+2\_C1\right)\right)\right)^{-1}\right\}$$

2.366 ODE No. 366

$$f\left(ay(x)^2+x^2\right)\left(ay(x)y'(x)+x\right)-xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 201.488 (sec), leaf count = 88

$$\text{Solve}\left[\int_1^{y(x)}\left(-\int_1^x\left(1-2aK[1]K[2]f'\left(aK[2]^2+K[1]^2\right)\right)dK[1]-aK[2]f\left(aK[2]^2+x^2\right)+x\right)dK[2]+\int_1^x(y(x)\right.$$

✓ **Maple** : cpu = 0.071 (sec), leaf count = 45

$$\left\{-ax(y(x))^2\frac{1}{\sqrt{a^2\left(y\left(x\right)\right)^2}}-\int^{-\frac{a(y(x))^2}{2}-\frac{x^2}{2}}f(-2\_a)\,d\_a+\_C1=0\right\}$$

2.367 ODE No. 367

$$f\left(x^c y(x)\right)\left(bxy'(x)-a\right)-x^a y(x)^b\left(cy(x)+xy'(x)\right)=0$$

✗ **Mathematica** : cpu = 13.7233 (sec), leaf count = 0 , could not solve

```
DSolve[-(x^a*y[x]^b*(c*y[x] + x*Derivative[1][y][x])) + f[x^c*y[x]]*(-a + b*x*Derivative[1][
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(f(x^c*y(x))*(b*x*diff(y(x),x)-a)-x^a*y(x)^b*(x*diff(y(x),x)+c*y(x)) = 0,y(x))
```

2.368 ODE No. 368

$$ay(x) + bx^2 + y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.369 ODE No. 369

$$-a^2 + y'(x)^2 + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0492107 (sec), leaf count = 107

$$\left\{\left\{y(x) \to -\frac{a\tan(x-c_1)}{\sqrt{\tan^2(x-c_1)+1}}\right\}, \left\{y(x) \to \frac{a\tan(x-c_1)}{\sqrt{\tan^2(x-c_1)+1}}\right\}, \left\{y(x) \to -\frac{a\tan(c_1+x)}{\sqrt{\tan^2(c_1+x)+1}}\right\}, \left\{y(x) -\right.\right.$$

✓ **Maple** : cpu = 0.728 (sec), leaf count = 68

$$\left\{y(x) = a, y(x) = \tan(-x+\_C1)\sqrt{\frac{a^2}{(\tan(-x+\_C1))^2+1}}, y(x) = -a, y(x) = -\tan(-x+\_C1)\sqrt{\frac{}{(\tan(-x\right.$$

2.370 ODE No. 370

$$-f(x)^2 + y'(x)^2 + y(x)^2 = 0$$

✗ **Mathematica** : cpu = 17.4668 (sec), leaf count = 0 , could not solve

```
DSolve[-f[x]^2 + y[x]^2 + Derivative[1][y][x]^2 == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)^2+y(x)^2-f(x)^2 = 0,y(x))
```

2.371 ODE No. 371

$$y'(x)^2 - y(x)^3 + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0260673 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \tan^2\left(\frac{1}{2}(c_1 - x)\right) + 1\right\}, \left\{y(x) \to \tan^2\left(\frac{1}{2}(c_1 + x)\right) + 1\right\}\right\}$$

✓ **Maple** : cpu = 0.676 (sec), leaf count = 20

$$\left\{y(x) = 1, y(x) = \left(\tan\left(-\frac{x}{2} + \frac{\_C1}{2}\right)\right)^2 + 1\right\}$$

2.372 ODE No. 372

$$ay(x) + b + y'(x)^2 - 4y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.00556673 (sec), leaf count = 27

$$\{\{y(x) \to \wp(x - c_1; a, b)\}, \{y(x) \to \wp(x + c_1; a, b)\}\}$$

✓ **Maple** : cpu = 0.661 (sec), leaf count = 232

$$\left\{y(x) = -\frac{1}{12}\left(\left(i\left(27\,b + 3\sqrt{-3\,a^3 + 81\,b^2}\right)^{\frac{2}{3}} - 3\,ia\right)\sqrt{3} + \left(27\,b + 3\sqrt{-3\,a^3 + 81\,b^2}\right)^{\frac{2}{3}} + 3\,a\right)\frac{1}{\sqrt[3]{27\,b + 3\sqrt{-3}}}\right.$$

2.373 ODE No. 373

$$a^2 y(x)^2\left(\log^2(y(x)) - 1\right) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.100065 (sec), leaf count = 71

$$\left\{\left\{y(x) \to e^{\frac{1}{2}\left(e^{-c_1 + iax} + e^{c_1 - iax}\right)}\right\}, \left\{y(x) \to \exp\left(\frac{1}{2}\left(e^{-c_1 - iax} + e^{c_1 + iax}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.411 (sec), leaf count = 49

$$\left\{y(x) = \left(\mathrm{e}^{-\sin(a(x - \_C1))}\right)^{-1}, y(x) = \mathrm{e}^{-\sin(a(x - \_C1))}, y(x) = \mathrm{e}^{RootOf\left(a^2\left(\mathrm{e}^{-Z}\right)^2\left(\_Z^2 - 1\right)\right)}\right\}$$

2.374 ODE No. 374

$$y'(x)^2 - 2y'(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0646332 (sec), leaf count = 73

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{\sqrt{\#1^2+1}}{\#1} - \frac{1}{\#1} + \sinh^{-1}(\#1)\&\right][c_1 - x]\right\}, \left\{y(x) \to \text{InverseFunction}\left[-\frac{\sqrt{\#1^2}}{\#}\right.\right.$$

✓ **Maple** : cpu = 0.659 (sec), leaf count = 85

$$\left\{x - (y(x))^{-1} - \frac{1}{y(x)}\left((y(x))^2+1\right)^{\frac{3}{2}} + y(x)\sqrt{(y(x))^2+1} + Arcsinh(y(x)) - \_C1 = 0, x - (y(x))^{-1} + \frac{1}{y(x)}\left(\right.\right.$$

2.375 ODE No. 375

$$ay'(x) + bx + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0440014 (sec), leaf count = 71

$$\left\{\left\{y(x) \to \frac{1}{2}\left(-\frac{(a^2-4bx)^{3/2}}{6b} - ax\right) + c_1\right\}, \left\{y(x) \to \frac{1}{2}\left(\frac{(a^2-4bx)^{3/2}}{6b} - ax\right) + c_1\right\}\right\}$$

✓ **Maple** : cpu = 0.654 (sec), leaf count = 49

$$\left\{y(x) = -\frac{ax}{2} - \frac{1}{12b}(a^2-4bx)^{\frac{3}{2}} + \_C1, y(x) = -\frac{ax}{2} + \frac{1}{12b}(a^2-4bx)^{\frac{3}{2}} + \_C1\right\}$$

2.376 ODE No. 376

$$ay'(x) + by(x) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.321728 (sec), leaf count = 110

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{\sqrt{a^2-4\#1b} + a\log\left(\sqrt{a^2-4\#1b} - a\right)}{2b}\&\right]\left[c_1 + \frac{x}{2}\right]\right\}, \left\{y(x) \to \text{InverseFunctio}\right.\right.$$

✓ **Maple** : cpu = 1.237 (sec), leaf count = 219

$$\left\{y(x) = -\frac{1}{4b}\mathrm{e}^{\frac{1}{2a}\left(-2a\,lambertW\left(2\frac{\mathrm{e}^{-1}}{a}\mathrm{e}^{-\frac{C1\,b}{a}}\frac{1}{\sqrt{-b^{-1}}}\left(\mathrm{e}^{\frac{bx}{a}}\right)^{-1}\right) - a\ln\left(-\frac{1}{4b}\right) - 2a + (-2x+2\_C1)b\right)}\left(\mathrm{e}^{\frac{1}{2a}\left(-2a\,lambertW\left(2\frac{\mathrm{e}^{-1}}{a}\mathrm{e}^{-\frac{C}{a}}\right.\right.\right.\right.\right.$$

2.377 ODE No. 377

$$y'(x)^2 + (x-2)y'(x) - y(x) + 1 = 0$$

✓ **Mathematica** : cpu = 0.00546401 (sec), leaf count = 19

$$\{\{y(x) \to c_1 x + c_1^2 - 2c_1 + 1\}\}$$

✓ **Maple** : cpu = 0.641 (sec), leaf count = 24

$$\left\{y(x) = -\frac{x^2}{4} + x, y(x) = 1 + \_C1^2 + (x-2)\,\_C1\right\}$$

2.378 ODE No. 378

$$(a+x)y'(x) + y'(x)^2 - y(x) = 0$$

✓ **Mathematica** : cpu = 0.00560097 (sec), leaf count = 18

$$\{\{y(x) \to ac_1 + c_1 x + c_1^2\}\}$$

✓ **Maple** : cpu = 0.638 (sec), leaf count = 20

$$\left\{y(x) = \_C1\,(\_C1 + a + x), y(x) = -\frac{(x+a)^2}{4}\right\}$$

2.379 ODE No. 379

$$y'(x)^2 - (x+1)y'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.00511811 (sec), leaf count = 18

$$\{\{y(x) \to c_1 x - c_1^2 + c_1\}\}$$

✓ **Maple** : cpu = 0.648 (sec), leaf count = 22

$$\left\{y(x) = \_C1\,(-\_C1 + x + 1), y(x) = \frac{(1+x)^2}{4}\right\}$$

2.380 ODE No. 380

$$y'(x)^2 + 2xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.432854 (sec), leaf count = 1757

$$\left\{\left\{y(x) \to -\frac{x^2}{4} - \frac{1}{4}\sqrt[3]{x^6 - 20\cosh(3c_1)\,x^3 - 20\sinh(3c_1)\,x^3 - 8\cosh(6c_1) - 8\sinh(6c_1) + 8\sqrt{-\cosh(3c_1)\,x^9 -}\right.\right.$$

✓ **Maple** : cpu = 0.654 (sec), leaf count = 619

$$\left\{y(x) = \frac{1}{16}\left(i\sqrt{3}\left(6\_C1 - x^3 + 2\sqrt{-3\,x^3\_C1 + 9\_C1^2}\right)^{\frac{2}{3}} - i\sqrt{3}x^2 - \left(6\_C1 - x^3 + 2\sqrt{-3\,x^3\_C1 + 9\_C}\right.\right.\right.$$

2.381 ODE No. 381

$$y'(x)^2 - 2xy'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.436465 (sec), leaf count = 1757

$$\left\{\left\{y(x) \to \frac{x^2}{4} + \frac{1}{4}\sqrt[3]{x^6 - 20\cosh(3c_1)\,x^3 - 20\sinh(3c_1)\,x^3 - 8\cosh(6c_1) - 8\sinh(6c_1) + 8\sqrt{-\cosh(3c_1)\,x^9 -}\right.\right.$$

✓ **Maple** : cpu = 0.662 (sec), leaf count = 579

$$\left\{y(x) = -\frac{1}{16}\left(i\sqrt{3}\left(-6\_C1 + x^3 + 2\sqrt{-3\,x^3\_C1 + 9\_C1^2}\right)^{\frac{2}{3}} - i\sqrt{3}x^2 - \left(-6\_C1 + x^3 + 2\sqrt{-3\,x^3\_C1 +}\right.\right.\right.$$

2.382 ODE No. 382

$$axy'(x) - bx^2 - c + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.254715 (sec), leaf count = 201

$$\left\{\left\{y(x) \to \frac{1}{2}\left(\frac{1}{2}x\sqrt{a^2x^2 + 4bx^2 + 4c} + \frac{2c\log\left(\sqrt{a^2 + 4b}\sqrt{a^2x^2 + 4bx^2 + 4c} + a^2x + 4bx\right)}{\sqrt{a^2 + 4b}} - \frac{ax^2}{2}\right) + c_1\right\}, \left\{y(\right.\right.$$

✓ **Maple** : cpu = 0.661 (sec), leaf count = 146

$$\left\{y(x) = -\frac{ax^2}{4} - \frac{x}{4}\sqrt{(a^2+4\,b)\,x^2+4\,c} - c\ln\left(\sqrt{a^2+4\,b}x + \sqrt{(a^2+4\,b)\,x^2+4\,c}\right)\frac{1}{\sqrt{a^2+4\,b}} + \_C1, y(x) = -\right.$$

2.383 ODE No. 383

$$axy'(x) + by(x) + cx^2 + y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.384 ODE No. 384

$$(ax+b)y'(x) - ay(x) + c + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 2.06064 (sec), leaf count = 183

$$\left\{\left\{y(x) \to \frac{-2\sqrt{-a^4e^{2c_1}x^2 - 2a^4e^{2c_1}x + a^4\left(-e^{2c_1}\right)} + 2a^3x + a^3 - 2a^2bx - ab^2 - ae^{2c_1} + 4ac}{4a^2}\right\}, \left\{y(x) \to \frac{2\sqrt{-}\right.\right.$$

✓ **Maple** : cpu = 0.025 (sec), leaf count = 50

$$\left\{y(x) = \frac{\_C1^2 + (ax+b)\_C1 + c}{a}, y(x) = \frac{-a^2x^2 - 2\,abx - b^2 + 4\,c}{4\,a}\right\}$$

2.385 ODE No. 385

$$-2x^2y'(x) + y'(x)^2 + 2xy(x) = 0$$

✗ **Mathematica** : cpu = 300.02 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.274 (sec), leaf count = 169

$$\left\{y(x) = \frac{x^4 - \left(RootOf\left(x^{16} - 12\_Z^2x^{12} - 16\_Z^3x^{10} + 30\_Z^4x^8 + 96\_Z^5x^6 + 100\_Z^6x^4 + 48\_Z^7x^2 + 9\_Z\right.\right.\right.}{2\,x}$$

2.386 ODE No. 386

$$ax^3y'(x) - 2ax^2y(x) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.199317 (sec), leaf count = 56

$$\left\{\left\{y(x) \to 2ae^{2c_1}\left(4e^{2c_1} + x^2\right)\right\}, \left\{y(x) \to \frac{e^{2c_1}\left(e^{2c_1} - 2ax^2\right)}{8a}\right\}\right\}$$

✓ **Maple** : cpu = 0.429 (sec), leaf count = 27

$$\left\{y(x) = -\frac{ax^4}{8}, y(x) = \_C1\, x^2 + 2\,\frac{\_C1^{\,2}}{a}\right\}$$

2.387 ODE No. 387

$$y'(x)^2 + e^x\left(y'(x) - y(x)\right) = 0$$

✓ **Mathematica** : cpu = 0.522732 (sec), leaf count = 134

$$\left\{\text{Solve}\left[-\frac{-e^{x/2}\sqrt{4y(x)+e^x} - 4y(x)\log\left(\sqrt{4y(x)+e^x} + e^{x/2}\right) + e^x}{2y(x)} = c_1, y(x)\right], \text{Solve}\left[2\log(y(x)) - \frac{e^{x/2}\sqrt{4y}\right.\right.$$

✓ **Maple** : cpu = 0.676 (sec), leaf count = 115

$$\left\{-\frac{\mathrm{e}^x}{2\,y\left(x\right)} + \ln\left(y(x)\right) + 2\,\mathit{Artanh}\left(\sqrt{\mathrm{e}^{2\,x} + 4\,y\left(x\right)\mathrm{e}^x}\mathrm{e}^{-x}\right) + \frac{1}{2\,y\left(x\right)}\sqrt{\mathrm{e}^{2\,x} + 4\,y\left(x\right)\mathrm{e}^x} - \_C1 = 0, -2\,\mathit{Artanh}\left(\sqrt{\mathrm{e}\right.\right.$$

2.388 ODE No. 388

$$y'(x)^2 - 2y(x)y'(x) - 2x = 0$$

✓ **Mathematica** : cpu = 0.628236 (sec), leaf count = 53

$$\text{Solve}\left[\left\{x = \frac{c_1\text{K\$1177977}}{\sqrt{\text{K\$1177977}^2+1}} + \frac{\text{K\$1177977}\sinh^{-1}(\text{K\$1177977})}{2\sqrt{\text{K\$1177977}^2+1}}, y(x) = \frac{\text{K\$1177977}}{2} - \frac{x}{\text{K\$1177977}}\right\}, \{y(x), \text{K}\right.$$

✓ **Maple** : cpu = 0.087 (sec), leaf count = 223

$$\left\{1\left(\left(-\frac{y(x)}{2} - \frac{1}{2}\sqrt{\left(y\left(x\right)\right)^2 + 2\,x}\right)\mathit{Arcsinh}\left(y(x) + \sqrt{\left(y\left(x\right)\right)^2 + 2\,x}\right) + x\sqrt{2\,\left(y\left(x\right)\right)^2 + 2\,x + 2\,y\left(x\right)\sqrt{\left(y\left(x\right)\right)^2}\right.\right.$$

2.389 ODE No. 389

$$y'(x)^2 - (4y(x)+1)y'(x) + y(x)(4y(x)+1) = 0$$

✓ **Mathematica** : cpu = 0.0460349 (sec), leaf count = 57

$$\left\{\left\{y(x) \to -\frac{1}{4}e^{x-4c_1}\left(2e^{2c_1} - e^x\right)\right\}, \left\{y(x) \to \frac{1}{4}e^{2c_1+x}\left(e^{2c_1+x} - 2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.57 (sec), leaf count = 71

$$\left\{y(x) = -\frac{1}{4}, y(x) = \frac{1}{\_C1}\left(-(\mathrm{e}^x)^2\sqrt{-\frac{\_C1}{(\mathrm{e}^x)^2}} + \_C1\right)\frac{1}{\sqrt{-\frac{\_C1}{(\mathrm{e}^x)^2}}}, y(x) = -\frac{1}{\_C1}\left((\mathrm{e}^x)^2\sqrt{-\frac{\_C1}{(\mathrm{e}^x)^2}} + \_C1\right)\frac{1}{\sqrt{-}}\right.$$

2.390 ODE No. 390

$$ay(x)y'(x) - bx - c + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 2.11155 (sec), leaf count = 142

$$\text{Solve}\left[\left\{x = c_1 e^{b\left(\frac{\log(\text{K\$1178389})}{b} - \frac{\log\left(b - a\text{K\$1178389}^2\right)}{2b}\right)} + e^{b\left(\frac{\log(\text{K\$1178389})}{b} - \frac{\log\left(b - a\text{K\$1178389}^2\right)}{2b}\right)}\left(\frac{\tan^{-1}\left(\frac{\sqrt{a}\text{K\$1178389}}{\sqrt{b - a\text{K\$1178389}^2}}\right)}{\sqrt{a}} - \right.\right.$$

✓ **Maple** : cpu = 0.262 (sec), leaf count = 281

$$\left\{y(x) = 2\frac{\left(-1/4\left(\mathrm{e}^{2\,RootOf\left(\sqrt{a}\_C1\,b\mathrm{e}^{2\_Z} - a\mathrm{e}^{2\_Z}bx + \sqrt{a}\_C1\,b^2 - \mathrm{e}^{2\_Z}\_Z\,b - a\mathrm{e}^{2\_Z}c + ab^2x - \_Z\,b^2 + abc\right)} + b\right)^2 \mathrm{e}^{-2\,RootOf\left(\sqrt{a}\_\right.}\right.}{a^{3/2}\left(\mathrm{e}^{2\,RootOf\left(\sqrt{a}\_C1\right.}\right.}$$

2.391 ODE No. 391

$$y'(x)(ay(x)+bx) + abxy(x) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0075823 (sec), leaf count = 29

$$\left\{\left\{y(x) \to c_1 e^{-ax}\right\}, \left\{y(x) \to c_1 - \frac{bx^2}{2}\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 22

$$\left\{y(x) = \_C1\,\mathrm{e}^{-ax}, y(x) = -\frac{bx^2}{2} + \_C1\right\}$$

2.392 ODE No. 392

$$y(x)^2 \log(ay(x)) - xy(x)y'(x) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.249314 (sec), leaf count = 27

$$\left\{\left\{y(x) \to \frac{e^{\frac{c_1 x}{2} - \frac{c_1^2}{4}}}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.465 (sec), leaf count = 50

$$\left\{y(x) = \frac{1}{a}\mathrm{e}^{\frac{x^2}{4}}, y(x) = \frac{1}{\mathrm{e}^{\_C1^2}\mathrm{e}^{\_C1\,x}a}, y(x) = \frac{\mathrm{e}^{-\_C1\,x}}{\mathrm{e}^{\_C1^2}a}\right\}$$

2.393 ODE No. 393

$$y'(x)^2 + 2y(x)\cot(x)y'(x) - y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0316574 (sec), leaf count = 31

$$\left\{\left\{y(x) \to c_1 \csc^2\left(\frac{x}{2}\right)\right\}, \left\{y(x) \to c_1 \sec^2\left(\frac{x}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 77

$$\left\{y(x) = \frac{\_C1}{\tan(x)}\left(1 + \sqrt{(\tan(x))^2 + 1}\right)\frac{1}{\sqrt{\frac{(\tan(x))^2}{(\tan(x))^2+1}}}, y(x) = \frac{\_C1\left((\tan(x))^2 + 1\right)}{\tan(x)}\sqrt{\frac{(\tan(x))^2}{(\tan(x))^2+1}}\left(1 + \sqrt{(\mathrm{ta}\right.\right.$$

2.394 ODE No. 394

$$-\left(g(x) - f(x)^2\right)e^{-2\int_a^x f(\mathrm{xp})\,d\mathrm{xp}} + 2f(x)y(x)y'(x) + g(x)y(x)^2 + y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 53.9167 (sec), leaf count = 0 , could not solve

```
DSolve[-((-f[x]^2 + g[x])/E^(2*Integrate[f[xp], {xp, a, x}])) + g[x]*y[x]^2 + 2*f[x]*y[x]*De
```

✓ **Maple** : cpu = 5.143 (sec), leaf count = 164

$$\left\{y(x) = -\tan\left(\frac{1}{2\cos(2)+2}\left(\sqrt{2}\int\left(\mathrm{e}^{\int_a^x f(xp)\,\mathrm{d}xp}\right)^2\sqrt{-\frac{(4\cos(2)+\cos(4)+3)\left((f(x))^2 - g(x)\right)}{\left(\mathrm{e}^{\int_a^x f(xp)\,\mathrm{d}xp}\right)^4}}\,\mathrm{d}x - 2\_C1\right.\right.\right.$$

2.395 ODE No. 395

$$2f(x)y(x)y'(x) + g(x)y(x)^2 + h(x) + y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 32.4728 (sec), leaf count = 0 , could not solve

```
DSolve[h[x] + g[x]*y[x]^2 + 2*f[x]*y[x]*Derivative[1][y][x] + Derivative[1][y][x]^2 == 0, y[
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)^2+2*f(x)*y(x)*diff(y(x),x)+g(x)*y(x)^2+h(x) = 0,y(x))
```

2.396 ODE No. 396

$$(y(x) - x)y(x)y'(x) + y'(x)^2 - xy(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.00999144 (sec), leaf count = 29

$$\left\{\left\{y(x) \to \frac{1}{x - c_1}\right\}, \left\{y(x) \to c_1 e^{\frac{x^2}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 20

$$\left\{y(x) = (x + \_C1)^{-1}, y(x) = \mathrm{e}^{\frac{x^2}{2}} \_C1\right\}$$

2.397 ODE No. 397

$$-2x^3y(x)^2y'(x) - 4x^2y(x)^3 + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.440651 (sec), leaf count = 143

$$\left\{\text{Solve}\left[-\frac{x\sqrt{x^4y(x)+4}\,y(x)^{3/2}\sinh^{-1}\left(\frac{1}{2}x^2\sqrt{y(x)}\right)}{2\sqrt{x^2y(x)^3\left(x^4y(x)+4\right)}} - \frac{1}{4}\log(y(x)) = c_1, y(x)\right], \text{Solve}\left[\frac{xy(x)^{3/2}\sqrt{x^4y(x)+4}\,\text{si}}{2\sqrt{x^2y(x)^3\,(x^4}\right.\right.$$

✓ **Maple** : cpu = 0.353 (sec), leaf count = 128

$$\left\{y(x) = \frac{-2\sqrt{2}x^2 - 2\_C1}{2\_C1\,x^4 - \_C1^3}, y(x) = \frac{2\sqrt{2}x^2 - 2\_C1}{2\_C1\,x^4 - \_C1^3}, y(x) = \frac{\left(\sqrt{2}x^2\_C1 - 2\right)\_C1^2}{2\_C1^2x^4 - 4}, y(x) = -4\,x^{-4}, y(x) = -\right.$$

2.398 ODE No. 398

$$y'(x)^2 - 3xy(x)^{2/3}y'(x) + 9y(x)^{5/3} = 0$$

✓ **Mathematica** : cpu = 0.80173 (sec), leaf count = 258

$$\left\{ \text{Solve}\left[-\frac{\left(x^2 - 4\sqrt[3]{y(x)}\right)^{3/2} y(x)^2 \log(y(x))}{6\left(\left(x^2 - 4\sqrt[3]{y(x)}\right) y(x)^{4/3}\right)^{3/2}} + \frac{\sqrt{\left(x^2 - 4\sqrt[3]{y(x)}\right) y(x)^{4/3}} \log\left(\sqrt{x^2 - 4\sqrt[3]{y(x)}} + x\right)}{\sqrt{x^2 - 4\sqrt[3]{y(x)}} y(x)^{2/3}} + \frac{1}{6}\log(y(\right.\right.$$

✓ **Maple** : cpu = 2.454 (sec), leaf count = 138

$$\left\{ \ln(x) + \frac{1}{6}\ln\left(\frac{y(x)}{x^6}\right) - \frac{1}{6}\ln\left(4\sqrt[3]{\frac{y(x)}{x^6}} - 1\right) - 1\sqrt{-4\left(\frac{y(x)}{x^6}\right)^{5/3} + \left(\frac{y(x)}{x^6}\right)^{\frac{4}{3}}}\, Artanh\left(\sqrt{-4\sqrt[3]{\frac{y(x)}{x^6}} + 1}\right)\right.$$

2.399 ODE No. 399

$$2y'(x)^2 + (x-1)y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.00600254 (sec), leaf count = 20

$$\{\{y(x) \to c_1 x + 2c_1^2 - c_1\}\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 22

$$\left\{ y(x) = \_C1\,(2\_C1 + x - 1), y(x) = -\frac{(x-1)^2}{8} \right\}$$

2.400 ODE No. 400

$$-2x^2y'(x) + 2y'(x)^2 + 3xy(x) = 0$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.19 (sec), leaf count = 74

$$\left\{ y(x) = \frac{x^3}{6}, y(x) = \frac{1}{3\_C1}\left(-\sqrt{-6\_C1\,x}x + 3\right), y(x) = \frac{1}{3\_C1}\left(\sqrt{-6\_C1\,x}x + 3\right), y(x) = -\frac{x}{3}\sqrt{-6\_C1\,x} + \right.$$

2.401 ODE No. 401

$$3y'(x)^2 - 2xy'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.333982 (sec), leaf count = 1093

$$\{\{y(x) \to \text{Root}\left[-16e^{6c_1}x^6 + 3\#1^4x^4 + 144e^{6c_1}\#1x^4 - 24\#1^5x^2 - 378e^{6c_1}\#1^2x^2 + 243e^{12c_1} + 48\#1^6 + 216e^{6c_1}\right.$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 580

$$\left\{y(x) = -\frac{1}{48}\left(i\sqrt{3}\left(-54\_C1 + x^3 + 6\sqrt{-3\,x^3\_C1 + 81\,\_C1^2}\right)^{\frac{2}{3}} - i\sqrt{3}x^2 - \left(-54\_C1 + x^3 + 6\sqrt{-3\,x^3\_C1}\right.\right.\right.$$

2.402 ODE No. 402

$$x^2 + 4xy'(x) + 3y'(x)^2 - y(x) = 0$$

✗ **Mathematica** : cpu = 300.003 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.177 (sec), leaf count = 101

$$\left\{y(x) = -\frac{x^2}{3}, y(x) = \frac{-3\,\_C1^2x^2 - 2\sqrt{3}\_C1\,x + 3}{12\,\_C1^2}, y(x) = \frac{-3\,\_C1^2x^2 + 2\sqrt{3}\_C1\,x + 3}{12\,\_C1^2}, y(x) = -\frac{\sqrt{3}\_C1\,x}{6}\right.$$

2.403 ODE No. 403

$$ay'(x)^2 + by'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.296771 (sec), leaf count = 116

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{\sqrt{4\#1a + b^2} + b\log\left(\sqrt{4\#1a + b^2} - b\right)}{2a}\&\right]\left[\frac{x}{2a} + c_1\right]\right\}, \left\{y(x) \to \text{InverseFunctio}\right.\right.$$

✓ **Maple** : cpu = 0.627 (sec), leaf count = 197

$$\left\{y(x) = \frac{1}{4\,a}\mathrm{e}^{-\frac{1}{2\,b}\left(2\,b\,lambertW\left(2\,\frac{\mathrm{e}^{-1}}{b\sqrt{a^{-1}}}\mathrm{e}^{\frac{x}{b}}\left(\mathrm{e}^{-\frac{C1}{b}}\right)^{-1}\right)+b\ln\left(\frac{1}{4\,a}\right)+2\_C1+2\,b-2\,x\right)}\left(\mathrm{e}^{-\frac{1}{2\,b}\left(2\,b\,lambertW\left(2\,\frac{\mathrm{e}^{-1}}{b\sqrt{a^{-1}}}\mathrm{e}^{\frac{x}{b}}\left(\mathrm{e}^{-\frac{C1}{b}}\right)^{-1}\right)\right.\right.\right.\right.$$

2.404 ODE No. 404

$$ay'(x)^2 + bx^2y'(x) + cxy(x) = 0$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.266 (sec), leaf count = 389

$$\left\{ \int_{\_b}^{x} 1 \left(-b\_a^2 - \sqrt{\_a^4 b^2 - 4\,\_a\, acy\,(x)} \right) \left(b\_a^3 + \sqrt{\_a^4 b^2 - 4\,\_a\, acy\,(x)}\,\_a + 6\,ay(x) \right)^{-1} \mathrm{d}\_a + \int^{y(x)} -2\,\frac{}{bx^3}$$

2.405 ODE No. 405

$$ay'(x)^2 + y(x)y'(x) - x = 0$$

✓ **Mathematica** : cpu = 0.96729 (sec), leaf count = 53

$$\text{Solve}\left[\left\{ x = \frac{a\text{K\$1236527}\sin^{-1}(\text{K\$1236527})}{\sqrt{1-\text{K\$1236527}^2}} + \frac{c_1\text{K\$1236527}}{\sqrt{1-\text{K\$1236527}^2}}, y(x) = \frac{x}{\text{K\$1236527}} - a\text{K\$1236527} \right\}, \{y(x), \right.$$

✓ **Maple** : cpu = 0.218 (sec), leaf count = 378

$$\left\{ \_C1 \left(y(x) - \sqrt{4\,ax + (y\,(x))^2} \right) \frac{1}{\sqrt{\frac{1}{a}\left(-y\,(x) + \sqrt{4\,ax + (y\,(x))^2} + 2\,a \right)}} \frac{1}{\sqrt{\frac{1}{a}\left(-y\,(x) + \sqrt{4\,ax + (y\,(x))^2} - 2\,a \right)}} \right.$$

2.406 ODE No. 406

$$ay'(x)^2 - y(x)y'(x) - x = 0$$

✓ **Mathematica** : cpu = 0.805395 (sec), leaf count = 49

$$\text{Solve}\left[\left\{ x = \frac{a\text{K\$1236723}\sinh^{-1}(\text{K\$1236723})}{\sqrt{\text{K\$1236723}^2+1}} + \frac{c_1\text{K\$1236723}}{\sqrt{\text{K\$1236723}^2+1}}, y(x) = a\text{K\$1236723} - \frac{x}{\text{K\$1236723}} \right\}, \{y(x), \right.$$

✓ **Maple** : cpu = 0.079 (sec), leaf count = 262

$$\left\{1\left(-\frac{\sqrt{2}}{2}\left(y(x)+\sqrt{4\,ax+(y\,(x))^2}\right)\,Arcsinh\left(\frac{1}{2\,a}\left(y(x)+\sqrt{4\,ax+(y\,(x))^2}\right)\right)+x\sqrt{\frac{1}{a^2}\left(y\,(x)\,\sqrt{4\,ax+(y\,(x)\right.\right.\right.\right.$$

2.407 ODE No. 407

$$xy'(x)^2-y(x)=0$$

✓ **Mathematica** : cpu = 0.0173002 (sec), leaf count = 51

$$\left\{\left\{y(x)\to\frac{1}{4}\left(-4c_1\sqrt{x}+c_1^2+4x\right)\right\},\left\{y(x)\to\frac{1}{4}\left(4c_1\sqrt{x}+c_1^2+4x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 39

$$\left\{y(x)=0,y(x)=\frac{1}{x}\left(-x+\sqrt{\_C1\,x}\right)^2,y(x)=\frac{1}{x}\left(x+\sqrt{\_C1\,x}\right)^2\right\}$$

2.408 ODE No. 408

$$xy'(x)^2-2y(x)+x=0$$

✓ **Mathematica** : cpu = 0.533863 (sec), leaf count = 166

$$\left\{\text{Solve}\left[\frac{\left(\sqrt{\frac{2y(x)}{x}-1}-1\right)\left(\left(\sqrt{\frac{2y(x)}{x}-1}-1\right)\log\left(\sqrt{\frac{2y(x)}{x}-1}-1\right)-1\right)}{\sqrt{\frac{2y(x)}{x}-1}-\frac{y(x)}{x}}=c_1+\log(x),y(x)\right],\text{Solve}\left[\frac{\left(\sqrt{\frac{2y}{}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 73

$$\left\{y(x)=\left(\frac{1}{2}\left(lambertW\left(\frac{1}{\_C1}\sqrt{\_C1\,x}\right)+1\right)^2\left(lambertW\left(\frac{1}{\_C1}\sqrt{\_C1\,x}\right)\right)^{-2}+\frac{1}{2}\right)x,y(x)=\left(\frac{1}{2}\left(lamber\right.\right.\right.$$

2.409 ODE No. 409

$$xy'(x)^2 - 2y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 30.7643 (sec), leaf count = 66

$$\text{Solve}\left[\left\{x = \frac{y(\text{K\$1237308}) + 2\text{K\$1237308}}{\text{K\$1237308}^2}, y(x) = c_1 e^{2(\log(\text{K\$1237308}) - \log(1 - \text{K\$1237308}))} + e^{2(\log(\text{K\$1237308}) - \log(1 - \text{K\$}}\right.\right.$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 63

$$\left\{y(x) = x\mathrm{e}^{2\,RootOf\left(-x\mathrm{e}^{2\_Z} + 2\,x\mathrm{e}^{\_Z} + 2\,\mathrm{e}^{\_Z} + \_C1 - 2\,\_Z - x\right)} - 2\,\mathrm{e}^{RootOf\left(-x\mathrm{e}^{2\_Z} + 2\,x\mathrm{e}^{\_Z} + 2\,\mathrm{e}^{\_Z} + \_C1 - 2\,\_Z - x\right)}\right\}$$

2.410 ODE No. 410

$$xy'(x)^2 + 4y'(x) - 2y(x) = 0$$

✓ **Mathematica** : cpu = 31.5708 (sec), leaf count = 80

$$\text{Solve}\left[\left\{x = -\frac{2(2\text{K\$1237647} - y(\text{K\$1237647}))}{\text{K\$1237647}^2}, y(x) = c_1 e^{-4\left(\frac{1}{2}\log(2 - \text{K\$1237647}) - \frac{\log(\text{K\$1237647})}{2}\right)} + 4e^{-4\left(\frac{1}{2}\log(2 - \text{K\$123}\right.\right.\right.$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 64

$$\left\{y(x) = \frac{x\mathrm{e}^{2\,RootOf\left(-x\mathrm{e}^{2\_Z} + 4\,x\mathrm{e}^{\_Z} - 4\,\mathrm{e}^{\_Z} + \_C1 + 8\,\_Z - 4\,x\right)}}{2} + 2\,\mathrm{e}^{RootOf\left(-x\mathrm{e}^{2\_Z} + 4\,x\mathrm{e}^{\_Z} - 4\,\mathrm{e}^{\_Z} + \_C1 + 8\,\_Z - 4\,x\right)}\right\}$$

2.411 ODE No. 411

$$xy'(x)^2 + xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.553569 (sec), leaf count = 181

$$\left\{\text{Solve}\left[\frac{\left(\sqrt{\frac{4y(x)}{x} + 1} - 1\right)\left(\left(\sqrt{\frac{4y(x)}{x} + 1} - 1\right)\log\left(\sqrt{\frac{4y(x)}{x} + 1} - 1\right) - 1\right)}{2\left(-\frac{2y(x)}{x} + \sqrt{\frac{4y(x)}{x} + 1} - 1\right)} = c_1 + \frac{\log(x)}{2}, y(x)\right], \text{Solve}\left[\frac{\left(\sqrt{\frac{4}{}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.041 (sec), leaf count = 65

$$\left\{y(x) = \frac{x}{4}\left(1 + 2\,lambertW\left(-1/2\,\frac{1}{\sqrt{\frac{\_C1}{x}}}\right)\right)\left(lambertW\left(-\frac{1}{2}\frac{1}{\sqrt{\frac{\_C1}{x}}}\right)\right)^{-2}, y(x) = \frac{x}{4}\left(1 + 2\,lambertW\left(1/\right.\right.\right.$$

2.412 ODE No. 412

$$a + xy'(x)^2 + y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 27.581 (sec), leaf count = 16145

✓ **Maple** : cpu = 0.04 (sec), leaf count = 146

$$\left\{ -\_C1\, x^2 \left(\frac{1}{x} \left(-y(x) + \sqrt{(y(x))^2 - 4\,ax} \right) \right)^{\frac{3}{2}} \left(-y(x) + \sqrt{(y(x))^2 - 4\,ax} \right)^{-2} + x + \frac{4\,ax^2}{3} \left(-y(x) + \sqrt{(y(x))^2 \right.$$

2.413 ODE No. 413

$$-x^2 + xy'(x)^2 + y(x)y'(x) = 0$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.193 (sec), leaf count = 269

$$\left\{ \int_{\_b}^{x} \frac{1}{\_a} \left(-y(x) - \sqrt{4\,\_a^3 + (y(x))^2} \right) \left(\sqrt{4\,\_a^3 + (y(x))^2} + 4\,y(x) \right)^{-1} \mathrm{d}\_a + \int^{y(x)} 1 \left(-2 + \left(-48\,\_f - 12\,\sqrt{ \right.\right.\right.$$

2.414 ODE No. 414

$$x^3 + xy'(x)^2 + y(x)y'(x) = 0$$

✗ **Mathematica** : cpu = 0 (sec), leaf count = 0 , crash

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Kernel Crash
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✓ **Maple** : cpu = 0.199 (sec), leaf count = 269

$$\left\{ \int_{\_b}^{x} \frac{1}{\_a} \left(-y(x) - \sqrt{-4\,\_a^4 + (y(x))^2} \right) \left(\sqrt{-4\,\_a^4 + (y(x))^2} + 5\,y(x) \right)^{-1} \mathrm{d}\_a + \int^{y(x)} 1 \left(-2 + \left(80\,\_f + 16 \right.\right.\right.$$

2.415 ODE No. 415

$$y(x)y'(x) + xy'(x)^2 - y(x)^4 = 0$$

✓ **Mathematica** : cpu = 0.21431 (sec), leaf count = 133

$$\left\{\left\{y(x) \to -\frac{\sqrt{\tanh^2\left(\frac{1}{2}\left(c_1 - \log(x)\right)\right) - 1}}{2\sqrt{x}}\right\}, \left\{y(x) \to \frac{\sqrt{\tanh^2\left(\frac{1}{2}\left(c_1 - \log(x)\right)\right) - 1}}{2\sqrt{x}}\right\}, \left\{y(x) \to -\frac{\sqrt{\tanh^2\left(\right.\right.\right.}\right.$$

✓ **Maple** : cpu = 0.181 (sec), leaf count = 95

$$\left\{y(x) = -\frac{1}{2}\frac{1}{\sqrt{-x}}, y(x) = \frac{1}{2}\frac{1}{\sqrt{-x}}, y(x) = -\frac{1}{2x}\sqrt{-\left(\tanh\left(-\frac{\ln(x)}{2} + \frac{\_C1}{2}\right)\right)^2 x + x}\left(\tanh\left(-\frac{\ln(x)}{2} + \frac{\_C1}{2}\right)\right.\right.$$

2.416 ODE No. 416

$$xy'(x)^2 + (y(x) - 3x)y'(x) + y(x) = 0$$

✗ **Mathematica** : cpu = 301.91 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.059 (sec), leaf count = 136

$$\left\{-\frac{\_C1}{x}\left(5x - y(x) + \sqrt{9x^2 - 10xy(x) + (y(x))^2}\right)\left(\frac{1}{x}\left(3x - y(x) + \sqrt{9x^2 - 10xy(x) + (y(x))^2}\right)\right)^{-\frac{3}{2}} + x =\right.$$

2.417 ODE No. 417

$$a + xy'(x)^2 - y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.401007 (sec), leaf count = 430

$$\left\{\left\{y(x) \to -\frac{8a^2}{4a - \sinh(c_1) - \cosh(c_1)} - \frac{\sqrt{16a^3\sinh(c_1) + 16a^3\cosh(c_1) - 8a^2x\sinh(c_1) - 8a^2x\cosh(c_1) - 8a\right.}}{}\right.$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 35

$$\left\{y(x) = \frac{x\_C1^2 + a}{\_C1}, y(x) = -2\sqrt{ax}, y(x) = 2\sqrt{ax}\right\}$$

2.418 ODE No. 418

$$ay(x)+xy'(x)^2-y(x)y'(x)=0$$

✓ **Mathematica** : cpu = 0.441013 (sec), leaf count = 165

$$\left\{\text{Solve}\left[-\frac{\sqrt{\frac{y(x)}{x}}\sqrt{\frac{y(x)}{x}-4a}-4a\log\left(\sqrt{\frac{y(x)}{x}-4a}+\sqrt{\frac{y(x)}{x}}\right)+\frac{y(x)}{x}}{4a}=c_1+\frac{\log(x)}{2},y(x)\right],\text{Solve}\left[\frac{y(x)}{4ax}-\frac{\sqrt{\frac{y(x)}{x}}}{x}\right.\right.$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 42

$$\left\{y(x)=0,y(x)=-ax\left(lambertW\left(-\frac{xe}{\_C1\,a}\right)-1\right)^2\left(lambertW\left(-\frac{xe}{\_C1\,a}\right)\right)^{-1}\right\}$$

2.419 ODE No. 419

$$xy'(x)^2+2y(x)y'(x)-x=0$$

✓ **Mathematica** : cpu = 1.47269 (sec), leaf count = 9073

✓ **Maple** : cpu = 0.04 (sec), leaf count = 109

$$\left\{x+\frac{=\_C1}{x}\left(y(x)-\sqrt{(y(x))^2+x^2}\right)\left(\frac{1}{x^2}\left(2x^2+6(y(x))^2-6y(x)\sqrt{(y(x))^2+x^2}\right)\right)^{-\frac{2}{3}}=0,\frac{=\_C1}{x}\left(\sqrt{(y(x))^2}\right.\right.$$

2.420 ODE No. 420

$$a + xy'(x)^2 - 2y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 1.71103 (sec), leaf count = 11757

$$\left\{\left\{y(x) \to -\sqrt{\frac{}{16\sqrt[3]{27a^6x^{12} - 144a^5\cosh(3c_1)\,x^9 - 144a^5\sinh(3c_1)\,x^9 + 272a^4\cosh(6c_1)\,x^6 + 272a^4\sinh(6c_1)}}}\right.\right.$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 689

$$\left\{y(x) = \frac{x}{12\_C1}\left(4\frac{x^2}{\sqrt[3]{-36\,a\_C1^2 + 8\,x^3 + 12\sqrt{a\left(9\,a\_C1^2 - 4\,x^3\right)}\_C1}} + 2\,x + \sqrt[3]{-36\,a\_C1^2 + 8\,x^3 + 12\sqrt{}\right.\right.$$

2.421 ODE No. 421

$$xy'(x)^2 - 2y(x)y'(x) - x = 0$$

✓ **Mathematica** : cpu = 0.0321054 (sec), leaf count = 27

$$\{\{y(x) \to x\sinh(c_1 - \log(x))\}, \{y(x) \to x\sinh(c_1 + \log(x))\}\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 32

$$\left\{y(x) = -ix, y(x) = ix, y(x) = -\frac{\_C1^2 - x^2}{2\_C1}\right\}$$

2.422 ODE No. 422

$$xy'(x)^2 - 2y(x)y'(x) + 4x = 0$$

✓ **Mathematica** : cpu = 0.0466828 (sec), leaf count = 49

$$\left\{\left\{y(x) \to 2\left(2x\sinh^2\left(\frac{1}{2}(c_1 - \log(x))\right) + x\right)\right\}, \left\{y(x) \to 2\left(2x\sinh^2\left(\frac{1}{2}(c_1 + \log(x))\right) + x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 30

$$\left\{y(x) = -2\,x, y(x) = 2\,x, y(x) = \frac{4\_C1^2 + x^2}{2\_C1}\right\}$$

2.423 ODE No. 423

$$xy'(x)^2 - 2y(x)y'(x) + 2y(x) + x = 0$$

✓ **Mathematica** : cpu = 0.0792551 (sec), leaf count = 59

$$\left\{\left\{y(x) \to \frac{1}{2}\left(-2e^{-c_1}x^2 - e^{c_1} + 2x\right)\right\}, \left\{y(x) \to \frac{1}{2}\left(-e^{c_1}x^2 - 2e^{-c_1} + 2x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 44

$$\left\{y(x) = \left(1 - \sqrt{2}\right)x, y(x) = \left(1 + \sqrt{2}\right)x, y(x) = \frac{2\_C1^2 + 2\_C1\,x + x^2}{2\_C1}\right\}$$

2.424 ODE No. 424

$$ay(x)y'(x) + bx + xy'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.408088 (sec), leaf count = 223

$$\left\{\text{Solve}\left[\frac{-2a\tan^{-1}\left(\frac{ay(x)}{x\sqrt{4b-\frac{a^2y(x)^2}{x^2}}}\right) + (a+2)\left(2\tan^{-1}\left(\frac{(a+2)y(x)}{x\sqrt{4b-\frac{a^2y(x)^2}{x^2}}}\right) - i\log\left(\frac{(a+1)y(x)^2}{x^2} + b\right)\right)}{8(a+1)} = c_1 + \frac{1}{2}i\log\right.\right.$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 193

$$\left\{\frac{1}{x}\left(-\_C1\left(ay(x) - \sqrt{a^2\left(y\left(x\right)\right)^2 - 4bx^2}\right)\left(\frac{a}{2x^2}\left(-y(x)\left(a+1\right)\sqrt{a^2\left(y\left(x\right)\right)^2 - 4bx^2} + \left(a^2+a\right)\left(y(x)\right)^2 - 2b\right.\right.\right.\right.$$

2.425 ODE No. 425

$$(x+1)y'(x)^2 - (y(x)+x)y'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.26072 (sec), leaf count = 59

$$\left\{\left\{y(x) \to -\frac{e^{c_1}(e^{c_1} - 2x)}{2\left(e^{c_1}+2\right)}\right\}, \left\{y(x) \to -\frac{2e^{c_1}(2e^{c_1} - x)}{2e^{c_1}+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 45

$$\left\{y(x) = \frac{\_C1\left(\_C1\,x + \_C1 - x\right)}{\_C1 - 1}, y(x) = x + 2 - 2\sqrt{1+x}, y(x) = x + 2 + 2\sqrt{1+x}\right\}$$

2.426 ODE No. 426

$$(3x+1)y'(x)^2-3(y(x)+2)y'(x)+9=0$$

✓ **Mathematica** : cpu = 0.38711 (sec), leaf count = 310

$$\left\{\left\{y(x)\to -\frac{\sqrt{9x^2\sinh(c_1)+9x^2\cosh(c_1)-210x\sinh(c_1)+6x\sinh(2c_1)-210x\cosh(c_1)+6x\cosh(2c_1)+12}}{\sinh(c_1)+\cosh(c_1)}\right.\right.$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 51

$$\left\{y(x)=\frac{9+(3x+1)\_C1^2-6\_C1}{3\_C1},y(x)=-2-2\sqrt{3x+1},y(x)=-2+2\sqrt{3x+1}\right\}$$

2.427 ODE No. 427

$$(3x+5)y'(x)^2-(3y(x)+x)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.626109 (sec), leaf count = 479

$$\left\{\left\{y(x)\to \frac{-\sqrt{5}\sqrt{-144e^{\frac{4c_1}{3}}x^2-360e^{\frac{4c_1}{3}}x+24e^{\frac{8c_1}{3}}x-225e^{\frac{4c_1}{3}}+30e^{\frac{8c_1}{3}}-e^{4c_1}}+6e^{\frac{4c_1}{3}}x+15e^{\frac{4c_1}{3}}-30x-25}{18\left(e^{\frac{4c_1}{3}}+5\right)}\right\}\right.$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 60

$$\left\{y(x)=\frac{(3x+5)\_C1^2-\_C1\,x}{3\_C1-1},y(x)=\frac{x}{3}+\frac{10}{9}-\frac{2}{9}\sqrt{15x+25},y(x)=\frac{x}{3}+\frac{10}{9}+\frac{2}{9}\sqrt{15x+25}\right\}$$

2.428 ODE No. 428

$$y'(x)(-ay(x)+bx+c)+axy'(x)^2-by(x)=0$$

✗ **Mathematica** : cpu = 300.038 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.07 (sec), leaf count = 66

$$\left\{y(x)=\frac{1}{a}\left(-bx+c-2\sqrt{-bcx}\right),y(x)=\frac{1}{a}\left(-bx+c+2\sqrt{-bcx}\right),y(x)=\frac{\_C1\,(\_C1\,ax+bx+c)}{\_C1\,a+b}\right\}$$

2.429 ODE No. 429

$$-y'(x)(ay(x)-a+bx-b)+axy'(x)^2+by(x)=0$$

✗ **Mathematica** : cpu = 300.088 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.069 (sec), leaf count = 72

$$\left\{y(x)=\frac{1}{a}\left(bx+a+b-2\sqrt{bx\,(a+b)}\right),y(x)=\frac{1}{a}\left(bx+a+b+2\sqrt{bx\,(a+b)}\right),y(x)=\frac{\_C1\,(\_C1\,ax-bx+a}{\_C1\,a-b}\right.$$

2.430 ODE No. 430

$$\mathrm{a0}x+y'(x)(\mathrm{a1}x+\mathrm{b1}y(x)+\mathrm{c1})+(\mathrm{a2}x+\mathrm{c2})y'(x)^2+\mathrm{b0}y(x)+\mathrm{c0}=0$$

✓ **Mathematica** : cpu = 270.593 (sec), leaf count = 478

$$\text{Solve}\left[\left\{x=c_1(\mathrm{b0}+\mathrm{b1K\$1749576})\exp\left(\frac{(\mathrm{b1}(\mathrm{b0}-\mathrm{a1})+2\mathrm{a2b0})\tan^{-1}\left(\frac{\mathrm{a1}+2\mathrm{K\$1749576}(\mathrm{a2}+\mathrm{b1})+\mathrm{b0}}{\sqrt{4\mathrm{a0}(\mathrm{a2}+\mathrm{b1})-\mathrm{a1}^2-2\mathrm{a1b0}-\mathrm{b0}^2}}\right)}{(\mathrm{a2}+\mathrm{b1})\sqrt{4\mathrm{a0}(\mathrm{a2}+\mathrm{b1})-\mathrm{a1}^2-2\mathrm{a1b0}-\mathrm{b0}^2}}-\frac{(2\mathrm{a2}+\right.\right.\right.$$

✓ **Maple** : cpu = 1.064 (sec), leaf count = 1602

$$\left\{\frac{1}{2\,a2\,x+2\,c2}\left(-2\left(\_C1-1/2\int\frac{-a1\,x-b1\,y(x)-c1+\sqrt{b1^2(y(x))^2+((2\,b1\,a1-4\,a2\,b0)x-4\,b0\,c2+2\,b1\,c1)y(x)+\left(-4\,a0\,a2+a1^2\right)x^2+(-4\,a0\,c2}{2\,a2\,x+2\,c2}\right.\right.\right.$$

2.431 ODE No. 431

$$x^2y'(x)^2-y(x)^4+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.038275 (sec), leaf count = 111

$$\left\{\left\{y(x)\to\sqrt{\tan^2(c_1-\log(x))+1}(-\cot(c_1-\log(x)))\right\},\left\{y(x)\to\sqrt{\tan^2(c_1-\log(x))+1}\cot(c_1-\log(x))\right\},\right.$$

✓ **Maple** : cpu = 0.149 (sec), leaf count = 62

$$\left\{y(x)=-1,y(x)=1,y(x)=\frac{1}{\tan(-\ln(x)+\_C1)}\sqrt{(\tan(-\ln(x)+\_C1))^2+1},y(x)=-\frac{1}{\tan(-\ln(x)+\_C1}\right.$$

2.432 ODE No. 432

$$\left(a+xy'(x)\right)^2-2ay(x)+x^2=0$$

✓ **Mathematica** : cpu = 1.74377 (sec), leaf count = 64

$$\text{Solve}\left[\left\{y(x)=\frac{a^2+2a\text{K\$1751809}x+\text{K\$1751809}^2x^2+x^2}{2a},x=\frac{c_1}{\sqrt{\text{K\$1751809}^2+1}}-\frac{a\sinh^{-1}(\text{K\$1751809})}{\sqrt{\text{K\$1751809}^2+1}}\right\},\{\right.$$

✓ **Maple** : cpu = 10.948 (sec), leaf count = 242

$$\left\{y(x)=\frac{1}{2\,a\left(\left(RootOf\left(\left(Arcsinh\left(\_Z\right)\right)^2a^2-\_Z^2x^2-2\,Arcsinh\left(\_Z\right)\_C1\,a+\_C1^{\,2}-x^2\right)\right)^2+1\right)}\left(-2\,aRo\right.\right.$$

2.433 ODE No. 433

$$-4a-4x^2+\left(xy'(x)+y(x)+2x\right)^2-4xy(x)=0$$

✓ **Mathematica** : cpu = 0.50641 (sec), leaf count = 22

$$\left\{\left\{y(x)\to\frac{-a-2c_1x+c_1^2}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.235 (sec), leaf count = 34

$$\left\{y(x)=\frac{-x^2-a}{x},y(x)=\_C1+\frac{\_C1^{\,2}-4\,a}{4\,x}\right\}$$

2.434 ODE No. 434

$$x^2y'(x)^2-x^2-2xy(x)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0337824 (sec), leaf count = 27

$$\left\{\left\{y(x)\to x\sinh\left(c_1-\log(x)\right)\right\},\left\{y(x)\to x\sinh\left(c_1+\log(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.004 (sec), leaf count = 7

$$\left\{y(x)=x+\_C1\right\}$$

2.435 ODE No. 435

$$x^2 y'(x)^2 - 2xy(x)y'(x) + y(x)(y(x)+1) - x = 0$$

✓ **Mathematica** : cpu = 0.0382113 (sec), leaf count = 61

$$\left\{\left\{y(x) \to \frac{1}{4}\left(c_1^2 x - 4ic_1\sqrt{x} + 4x - 4\right)\right\}, \left\{y(x) \to \frac{1}{4}\left(c_1^2 x + 4ic_1\sqrt{x} + 4x - 4\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.233 (sec), leaf count = 22

$$\left\{y(x) = x, y(x) = \_C1\sqrt{x} - \frac{x\_C1^2}{4} + x - 1\right\}$$

2.436 ODE No. 436

$$-x^4 + x^2 y'(x)^2 + \left(1 - x^2\right) y(x)^2 - 2xy(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0352345 (sec), leaf count = 26

$$\{\{y(x) \to -x\sinh(x - c_1)\}, \{y(x) \to x\sinh(c_1 + x)\}\}$$

✓ **Maple** : cpu = 1.738 (sec), leaf count = 61

$$\left\{y(x) = -ix, y(x) = ix, y(x) = -\frac{x\left(\left(\mathrm{e}^x\right)^2 - \_C1^2\right)}{2\,\mathrm{e}^x \_C1}, y(x) = \frac{x\left(\left(\mathrm{e}^x\right)^2 \_C1^2 - 1\right)}{2\,\mathrm{e}^x \_C1}\right\}$$

2.437 ODE No. 437

$$-(a + 2xy(x))y'(x) + x^2 y'(x)^2 + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.281889 (sec), leaf count = 47

$$\left\{\left\{y(x) \to \frac{x - 2\sqrt{a}c_1}{4c_1^2}\right\}, \left\{y(x) \to \frac{2\sqrt{a}c_1 + x}{4c_1^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 36

$$\left\{y(x) = -\frac{a}{4\,x}, y(x) = \_C1\,x - \sqrt{\_C1\,a}, y(x) = \_C1\,x + \sqrt{\_C1\,a}\right\}$$

2.438 ODE No. 438

$$x^2 y'(x)^2 + 3xy(x)y'(x) + 2y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.00856304 (sec), leaf count = 21

$$\left\{\left\{y(x) \to \frac{c_1}{x^2}\right\}, \left\{y(x) \to \frac{c_1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 17

$$\left\{y(x) = \frac{\_C1}{x^2}, y(x) = \frac{\_C1}{x}\right\}$$

2.439 ODE No. 439

$$x^2 y'(x)^2 + 3xy(x)y'(x) + 3y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0148699 (sec), leaf count = 49

$$\left\{\left\{y(x) \to c_1 x^{\frac{1}{2}\left(-3-i\sqrt{3}\right)}\right\}, \left\{y(x) \to c_1 x^{\frac{1}{2}i\left(\sqrt{3}+3i\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 33

$$\left\{y(x) = \_C1\, x^{-\frac{i}{2}\sqrt{3}} x^{-\frac{3}{2}}, y(x) = \_C1\, x^{\frac{i}{2}\sqrt{3}} x^{-\frac{3}{2}}\right\}$$

2.440 ODE No. 440

$$x^2 y'(x)^2 + 4xy(x)y'(x) - 5y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.00730007 (sec), leaf count = 19

$$\left\{\left\{y(x) \to \frac{c_1}{x^5}\right\}, \{y(x) \to c_1 x\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 15

$$\left\{y(x) = \frac{\_C1}{x^5}, y(x) = \_C1\, x\right\}$$

2.441 ODE No. 441

$$x^2y'(x)^2-4x(y(x)+2)y'(x)+4y(x)(y(x)+2)=0$$

✓ **Mathematica** : cpu = 0.0733329 (sec), leaf count = 65

$$\left\{\left\{y(x)\to -e^{-c_1}x\left(2\sqrt{2}e^{\frac{c_1}{2}}-x\right)\right\},\left\{y(x)\to e^{\frac{c_1}{2}}x\left(e^{\frac{c_1}{2}}x-2\sqrt{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 1.188 (sec), leaf count = 83

$$\left\{y(x)=-2,y(x)=\frac{1}{\_C1}\left(x^2-2\sqrt{2}\sqrt{\_C1\,x^2}\right),y(x)=\frac{1}{\_C1}\left(2\sqrt{2}\sqrt{\_C1\,x^2}+x^2\right),y(x)=\frac{x\left(-2\sqrt{2}\_C1+x\right.}{\_C1^2}\right.$$

2.442 ODE No. 442

$$x^2y'(x)^2+(1-x)\left(y(x)^2-x^2y(x)\right)+\left(x^3+x^2y(x)-2xy(x)\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.00944779 (sec), leaf count = 28

$$\left\{\left\{y(x)\to c_1e^{-x}x\right\},\left\{y(x)\to c_1x-x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 21

$$\left\{y(x)=\left(-x+\_C1\right)x,y(x)=\_C1\,\mathrm{e}^{-x}x\right\}$$

2.443 ODE No. 443

$$x\left(xy'(x)-y(x)\right)^2-y'(x)=0$$

✓ **Mathematica** : cpu = 0.552065 (sec), leaf count = 1921

$$\left\{\left\{y(x)\to \text{Root}\left[1024x^{12}-576e^{12c_1}\#1^4x^8-2176e^{12c_1}\#1^3x^6+81e^{24c_1}\#1^8x^4-1536e^{12c_1}\#1^2x^4+36e^{24c_1}\#1^7x^2\right.\right.\right.$$

✓ **Maple** : cpu = 1.733 (sec), leaf count = 221

$$\left\{y(x)=-\frac{2}{9\,x^2},y(x)=\frac{\left(RootOf\left(-729\,\_C1\,x^{12}+\_Z^8-12\,\_Z^7+60\,\_Z^6-160\,\_Z^5+240\,\_Z^4-192\,\_Z^3+\right.\right.\right.}{}$$

2.444 ODE No. 444

$$x^2y'(x)^2-(y(x)-2x)y(x)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.147747 (sec), leaf count = 75

$$\left\{\left\{y(x)\to -\frac{\cosh(2c_1)-\sinh(2c_1)}{x\sinh(2c_1)+x\cosh(2c_1)-1}\right\},\left\{y(x)\to -\frac{\cosh(2c_1)-\sinh(2c_1)}{x\sinh(2c_1)+x\cosh(2c_1)+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.877 (sec), leaf count = 120

$$\left\{y(x)=\frac{\_C1^3\sqrt{2}-2\,x\_C1^2}{-2\,\_C1^2+4\,x^2},y(x)=\frac{\_C1^2(\sqrt{2}\_C1+2\,x)}{2\,\_C1^2-4\,x^2},y(x)=4\,x,y(x)=-2\frac{\_C1^2(-\sqrt{2}\_C1+x)}{-2\,\_C1^2+x^2},y(x)\right.$$

2.445 ODE No. 445

$$y'(x)\left(ax^2y(x)^3+b\right)+aby(x)^3+x^2y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.0107936 (sec), leaf count = 49

$$\left\{\left\{y(x)\to -\frac{1}{\sqrt{2ax-2c_1}}\right\},\left\{y(x)\to \frac{1}{\sqrt{2ax-2c_1}}\right\},\left\{y(x)\to \frac{b}{x}+c_1\right\}\right\}$$

✓ **Maple** : cpu = 0.015 (sec), leaf count = 35

$$\left\{y(x)=\frac{1}{\sqrt{2\,ax+\_C1}},y(x)=-\frac{1}{\sqrt{2\,ax+\_C1}},y(x)=\frac{b}{x}+\_C1\right\}$$

2.446 ODE No. 446

$$\left(x^2+1\right)y'(x)^2-2xy(x)y'(x)+y(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.493539 (sec), leaf count = 201

$$\left\{\left\{y(x)\to \frac{e^{2c_1}x-2e^{c_1}-x}{e^{2c_1}+1}\right\},\left\{y(x)\to \frac{e^{2c_1}x+2e^{c_1}-x}{e^{2c_1}+1}\right\},\left\{y(x)\to \frac{-e^{4c_1}x-2\sqrt{-e^{2c_1}+2e^{4c_1}-e^{6c_1}}+x}{2e^{2c_1}-e^{4c_1}-1}\right\},\right.$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 57

$$\left\{y(x)=\sqrt{x^2+1},y(x)=-\sqrt{x^2+1},y(x)=\_C1\,x-\sqrt{-\_C1^2+1},y(x)=\_C1\,x+\sqrt{-\_C1^2+1}\right\}$$

2.447 ODE No. 447

$$\left(x^2-1\right)y'(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.0170938 (sec), leaf count = 41

$$\left\{\left\{y(x)\to c_1-\log\left(\sqrt{x^2-1}+x\right)\right\},\left\{y(x)\to c_1+\log\left(\sqrt{x^2-1}+x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 33

$$\left\{y(x)=-\ln\left(x+\sqrt{x^2-1}\right)+\_C1,y(x)=\ln\left(x+\sqrt{x^2-1}\right)+\_C1\right\}$$

2.448 ODE No. 448

$$\left(x^2-1\right)y'(x)^2-y(x)^2+1=0$$

✓ **Mathematica** : cpu = 0.090217 (sec), leaf count = 109

$$\left\{\left\{y(x)\to\frac{1}{2}\left(e^{-c_1}\sqrt{x^2-1}-e^{c_1}\sqrt{x^2-1}+e^{-c_1}x+e^{c_1}x\right)\right\},\left\{y(x)\to\frac{1}{2}\left(-e^{-c_1}\sqrt{x^2-1}+e^{c_1}\sqrt{x^2-1}+e^{-c_1}x\right.\right.\right.$$

✓ **Maple** : cpu = 266.143 (sec), leaf count = 166

$$\left\{1\sqrt{(-1+y(x))(1+y(x))}\ln\left(y(x)+\sqrt{(y(x))^2-1}\right)\frac{1}{\sqrt{-1+y(x)}}\frac{1}{\sqrt{1+y(x)}}+\int^x\frac{1}{\_a^2-1}\sqrt{(\_a^2-1)\left((y\right.}\right.$$

2.449 ODE No. 449

$$\left(x^2-a^2\right)y'(x)^2+2xy(x)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.011303 (sec), leaf count = 27

$$\left\{\left\{y(x)\to\frac{c_1}{a-x}\right\},\left\{y(x)\to\frac{c_1}{a+x}\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 23

$$\left\{y(x)=\frac{\_C1}{a-x},y(x)=\frac{\_C1}{x+a}\right\}$$

2.450 ODE No. 450

$$\left(x^2-a^2\right)y'(x)^2-x^2-2xy(x)y'(x)=0$$

✓ **Mathematica** : cpu = 0.444352 (sec), leaf count = 26

$$\left\{\left\{y(x)\to\frac{a^2+c_1^2-x^2}{2c_1}\right\}\right\}$$

✓ **Maple** : cpu = 0.455 (sec), leaf count = 51

$$\left\{y(x)=\sqrt{a^2-x^2},y(x)=-\sqrt{a^2-x^2},y(x)=\_C1\,x^2-\_C1\,a^2-\frac{1}{4\_C1}\right\}$$

2.451 ODE No. 451

$$\left(a+x^2\right)y'(x)^2+b-2xy(x)y'(x)+y(x)^2=0$$

✗ **Mathematica** : cpu = 300.751 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.054 (sec), leaf count = 78

$$\left\{y(x)=\frac{1}{a}\sqrt{-ab\left(x^2+a\right)},y(x)=-\frac{1}{a}\sqrt{-ab\left(x^2+a\right)},y(x)=\_C1\,x-\sqrt{-a\_C1^2-b},y(x)=\_C1\,x+\sqrt{-a\_C\right.$$

2.452 ODE No. 452

$$\left(2x^2+1\right)y'(x)^2+\left(x^2+2xy(x)+y(x)^2+2\right)y'(x)+2y(x)^2+1=0$$

✗ **Mathematica** : cpu = 300.752 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 1.744 (sec), leaf count = 37

$$\left\{y(x)=-3\,x-2\,\sqrt{2\,x^2+1},y(x)=-3\,x+2\,\sqrt{2\,x^2+1}\right\}$$

2.453 ODE No. 453

$$\left(a^2-1\right)x^2y'(x)^2+a^2x^2+2xy(x)y'(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.589661 (sec), leaf count = 395

$$\left\{\text{Solve}\left[\frac{a\left(-\log\left(\frac{\left(a^2-1\right)\left(a\sqrt{a^2-\frac{y(x)^2}{x^2}-1}+a^2-\frac{iy(x)}{x}-1\right)}{a^3\left(\frac{y(x)}{x}-i\right)}\right)+\log\left(-\frac{\left(a^2-1\right)\left(a\sqrt{a^2-\frac{y(x)^2}{x^2}-1}+a^2+\frac{iy(x)}{x}-1\right)}{a^3\left(\frac{y(x)}{x}+i\right)}\right)+\log\left(\frac{y(x)^2}{x^2}\right.\right.}{2\left(a^2-1\right)}\right.\right.$$

✓ **Maple** : cpu = 0.742 (sec), leaf count = 229

$$\left\{\frac{1}{2a}\left(-2\_C1\,a+2a\ln(x)+\ln\left(\frac{(y(x))^2+x^2}{x^2}\right)a-2\sqrt{-a^2}\arctan\left(\frac{a^2y(x)}{\sqrt{-a^2}x}\frac{1}{\sqrt{\frac{(y(x))^2+(-a^2+1)x^2}{x^2}}}\right)+2\ln\left(\frac{1}{x}\right.\right.\right.$$

2.454 ODE No. 454

$$ax^2y'(x)^2-(a-1)ax^2-2axy(x)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.155192 (sec), leaf count = 118

$$\left\{\left\{y(x)\to\frac{1}{2}e^{-c_1}x^{1-\frac{\sqrt{a-1}}{\sqrt{a}}}\left(e^{2c_1}-ax^{\frac{2\sqrt{a-1}}{\sqrt{a}}}\right)\right\},\left\{y(x)\to\frac{1}{2}e^{-c_1}x^{1-\frac{\sqrt{a-1}}{\sqrt{a}}}\left(e^{2c_1}x^{\frac{2\sqrt{a-1}}{\sqrt{a}}}-a\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.123 (sec), leaf count = 106

$$\left\{y(x)=\sqrt{-a}x,y(x)=RootOf\left(-\ln(x)-\int^{\_Z}\frac{1}{(a-1)\left(\_a^2+a\right)}\sqrt{(a-1)\left(\_a^2+a\right)}a d\_a+\_C1\right)x,y(x)=\right.$$

2.455 ODE No. 455

$$a + x^3 y'(x)^2 + x^2 y(x) y'(x) = 0$$

✓ **Mathematica** : cpu = 0.397716 (sec), leaf count = 123

$$\left\{\left\{y(x) \to -\frac{e^{-\frac{c_1}{2}}\left(2ae^{c_1} + x\right)}{\sqrt{2}x}\right\}, \left\{y(x) \to \frac{e^{-\frac{c_1}{2}}\left(2ae^{c_1} + x\right)}{\sqrt{2}x}\right\}, \left\{y(x) \to -\frac{e^{-\frac{c_1}{2}}\left(2ax + e^{c_1}\right)}{\sqrt{2}x}\right\}, \left\{y(x) \to \frac{e^{-\frac{c_1}{2}}(2a\right.$$

✓ **Maple** : cpu = 0.18 (sec), leaf count = 66

$$\left\{y(x) = -2\,\frac{\sqrt{ax}}{x}, y(x) = 2\,\frac{\sqrt{ax}}{x}, y(x) = \frac{\_C1^2 + 4\,ax}{2\,\_C1\,x}, y(x) = \frac{x\_C1^2 + 4\,a}{2\,\_C1\,x}\right\}$$

2.456 ODE No. 456

$$2\left(1 - x^2\right) y(x) y'(x) + x\left(x^2 - 1\right) y'(x)^2 + x y(x)^2 - x = 0$$

✓ **Mathematica** : cpu = 0.123379 (sec), leaf count = 79

$$\left\{\left\{y(x) \to x + 2x \sinh^2\left(\frac{1}{2}\left(c_1 - 2i \tan^{-1}\left(\frac{\sqrt{x-1}}{\sqrt{x+1}}\right)\right)\right)\right\}, \left\{y(x) \to x + 2x \sinh^2\left(\frac{1}{2}\left(c_1 + 2i \tan^{-1}\left(\frac{\sqrt{x-1}}{\sqrt{x+1}}\right)\right.\right.\right.$$

✓ **Maple** : cpu = 0.392 (sec), leaf count = 33

$$\left\{y(x) = x, y(x) = -x, y(x) = \sqrt{-\_C1^2 + 1} + \sqrt{x^2 - 1}\,\_C1\right\}$$

2.457 ODE No. 457

$$x^4 y'(x)^2 - x y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.957057 (sec), leaf count = 410

$$\left\{\text{Solve}\left[\frac{x\sqrt{4x^2y(x)+1}\left(\log(x) - \log\left(\sqrt{4x^2y(x)+1}+1\right)\right)}{\sqrt{4x^4y(x)+x^2}} + \frac{x\sqrt{4x^2y(x)+1}\log(y(x)) - x\sqrt{4x^2y(x)+1}\log(\right.\right.$$

✓ **Maple** : cpu = 0.778 (sec), leaf count = 45

$$\left\{y(x) = \frac{i\_C1 - x}{x\_C1^2}, y(x) = \frac{-i\_C1 - x}{x\_C1^2}, y(x) = -\frac{1}{4\,x^2}\right\}$$

2.458 ODE No. 458

$$x^2\left(x^2-a^2\right)y'(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.0639907 (sec), leaf count = 139

$$\left\{\left\{y(x)\to c_1-\frac{ix\sqrt{x^2-a^2}\log\left(\frac{2\left(\sqrt{x^2-a^2}-ia\right)}{x}\right)}{a\sqrt{x^4-a^2x^2}}\right\},\left\{y(x)\to c_1+\frac{ix\sqrt{x^2-a^2}\log\left(\frac{2\left(\sqrt{x^2-a^2}-ia\right)}{x}\right)}{a\sqrt{x^4-a^2x^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 90

$$\left\{y(x)=-1\ln\left(\frac{1}{x}\left(-2\,a^2+2\,\sqrt{-a^2}\sqrt{-a^2+x^2}\right)\right)\frac{1}{\sqrt{-a^2}}+\_C1,y(x)=1\ln\left(\frac{1}{x}\left(-2\,a^2+2\,\sqrt{-a^2}\sqrt{-a^2+x^2}\right)\right.\right.$$

2.459 ODE No. 459

$$-\left(y'(x)-1\right)^2+e^{-2x}y'(x)^2+e^{-2y(x)}=0$$

✓ **Mathematica** : cpu = 2.74372 (sec), leaf count = 272

$$\left\{\left\{y(x)\to\log\left(-\frac{ie^{-c_1}\left(e^x+1\right)\left(e^{2c_1+x}-e^{2c_1}+e^x+1\right)}{\sqrt{8e^x+4e^{2x}+4}}\right)\right\},\left\{y(x)\to\log\left(\frac{ie^{-c_1}\left(e^x+1\right)\left(e^{2c_1+x}-e^{2c_1}+e^x+\right.\right.\right.$$

✓ **Maple** : cpu = 0.614 (sec), leaf count = 65

$$\left\{y(x)=x+\ln\left(\frac{1}{\mathrm{e}^x}\left(-1-\sqrt{\left(\mathrm{e}^x\right)^2-\frac{\left(\mathrm{e}^x\right)^2}{\left(\mathrm{e}^{\_C1}\right)^2}}\right)\right)+\_C1,y(x)=x+\ln\left(\frac{1}{\mathrm{e}^x}\left(-1+\sqrt{\left(\mathrm{e}^x\right)^2-\frac{\left(\mathrm{e}^x\right)^2}{\left(\mathrm{e}^{\_C1}\right)^2}}\right)\right)+\_\right.$$

2.460 ODE No. 460

$$\cos^4(x)\left(y'(x)^2+y(x)^2\right)-a^2=0$$

✗ **Mathematica** : cpu = 56.1227 (sec), leaf count = 0 , could not solve

```
DSolve[-a^2 + Cos[x]^4*(y[x]^2 + Derivative[1][y][x]^2) == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((diff(y(x),x)^2+y(x)^2)*cos(x)^4-a^2 = 0,y(x))
```

2.461 ODE No. 461

$$a(x)y'(x)^2+2b(x)y(x)y'(x)+c(x)y(x)^2+2d(x)y'(x)+2e(x)y(x)+f(x)=0$$

✗ **Mathematica** : cpu = 300.025 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(d0(x)*diff(y(x),x)^2+2*b0(x)*y(x)*diff(y(x),x)+c0(x)*y(x)^2+2*d0(x)*diff(y(x),x)+2*e0
```

2.462 ODE No. 462

$$y(x)y'(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.0167216 (sec), leaf count = 43

$$\left\{\left\{y(x)\to\left(\frac{3}{2}\right)^{2/3}(c_1-x)^{2/3}\right\},\left\{y(x)\to\left(\frac{3}{2}\right)^{2/3}(c_1+x)^{2/3}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 27

$$\left\{x-\frac{2}{3}(y(x))^{\frac{3}{2}}-\_C1=0,x+\frac{2}{3}(y(x))^{\frac{3}{2}}-\_C1=0\right\}$$

2.463 ODE No. 463

$$y(x)y'(x)^2-e^{2x}=0$$

✓ **Mathematica** : cpu = 0.0187577 (sec), leaf count = 47

$$\left\{\left\{y(x)\to\left(\frac{3}{2}\right)^{2/3}(c_1-e^x)^{2/3}\right\},\left\{y(x)\to\left(\frac{3}{2}\right)^{2/3}(c_1+e^x)^{2/3}\right\}\right\}$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 50

$$\left\{-1\sqrt{y(x)\left(\mathrm{e}^x\right)^2}\frac{1}{\sqrt{y(x)}}+\frac{2}{3}(y(x))^{\frac{3}{2}}+\_C1=0,1\sqrt{y(x)\left(\mathrm{e}^x\right)^2}\frac{1}{\sqrt{y(x)}}+\frac{2}{3}(y(x))^{\frac{3}{2}}+\_C1=0\right\}$$

2.464 ODE No. 464

$$y(x)y'(x)^2 + 2xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0625674 (sec), leaf count = 52

$$\left\{\left\{y(x) \to -e^{\frac{c_1}{2}}\sqrt{e^{c_1} - 2x}\right\}, \left\{y(x) \to e^{\frac{c_1}{2}}\sqrt{e^{c_1} - 2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.443 (sec), leaf count = 70

$$\left\{y(x) = \sqrt{\_C1^2 - 2\_C1\,x}, y(x) = \sqrt{\_C1^2 + 2\_C1\,x}, y(x) = -ix, y(x) = ix, y(x) = -\sqrt{\_C1\ (2\,x + \_C1)}, y\right.$$

2.465 ODE No. 465

$$y(x)y'(x)^2 + 2xy'(x) - 9y(x) = 0$$

✗ **Mathematica** : cpu = 300.672 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.07 (sec), leaf count = 210

$$\left\{\right.$$
$$\_C1\,x\left(x + \sqrt{x^2 + 9\ (y\,(x))^2}\right)\left(\frac{1}{y\,(x)}\left(-x - \sqrt{x^2 + 9\ (y\,(x))^2}\right)\right)^{\frac{2}{7}}\left(x\sqrt{x^2 + 9\ (y\,(x))^2} + x^2 + (y(x))^2\right)^{-1} -$$
$$\sqrt[7]{}$$

2.466 ODE No. 466

$$y(x)y'(x)^2 - 2xy'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.253102 (sec), leaf count = 145

$$\left\{\left\{y(x) \to -\sqrt{-2x\sinh(c_1) - 2x\cosh(c_1) - \sinh(2c_1) - \cosh(2c_1)}\right\}, \left\{y(x) \to \sqrt{-2x\sinh(c_1) - 2x\cosh(c_1) -\right.\right.$$

✓ **Maple** : cpu = 0.391 (sec), leaf count = 71

$$\left\{y(x) = x, y(x) = \sqrt{\_C1^2 - 2\,ix\_C1}, y(x) = \sqrt{\_C1^2 + 2\,ix\_C1}, y(x) = -x, y(x) = -\sqrt{\_C1^2 - 2\,ix\_C1}, y(x\right.$$

2.467 ODE No. 467

$$y(x)y'(x)^2 - 4xy'(x) + y(x) = 0$$

✗ **Mathematica** : cpu = 300.226 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.069 (sec), leaf count = 148

$$\left\{ -\frac{\_C1\, x}{y(x)} \frac{1}{\sqrt[3]{\frac{1}{(y(x))^2}\left(8x^2 - 4\,(y(x))^2 - 4x\sqrt{4x^2-(y(x))^2}\right)}} \frac{1}{\sqrt[3]{\frac{1}{y(x)}\left(2x - \sqrt{4x^2-(y(x))^2}\right)}} + x = 0, -\frac{\_C1}{y(x}\right.$$

2.468 ODE No. 468

$$-4a^2xy'(x) + a^2y(x) + y(x)y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 300.368 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.081 (sec), leaf count = 181

$$\left\{ -\frac{\_C1\, x}{ay(x)} \frac{1}{\sqrt[3]{\frac{a}{y(x)}\left(2ax + \sqrt{4a^2x^2-(y(x))^2}\right)}} \frac{1}{\sqrt[3]{\frac{a^2}{(y(x))^2}\left(2a^2x^2 + \sqrt{4a^2x^2-(y(x))^2}ax - (y(x))^2\right)}} + x = 0, -\right.$$

2.469 ODE No. 469

$$axy'(x) + by(x) + y(x)y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.32883 (sec), leaf count = 247

$$\left\{ \text{Solve}\left[\frac{2a\tanh^{-1}\left(\frac{\sqrt{a^2-\frac{4by(x)^2}{x^2}}}{a}\right) - 2(a+2b)\tanh^{-1}\left(\frac{\sqrt{a^2-\frac{4by(x)^2}{x^2}}}{a+2b}\right) + a\log\left(a+b+\frac{y(x)^2}{x^2}\right) + 2b\log\left(a+b+\right.\right.\right.$$
$$\left.\left.\left. 8(a+b) \right.\right.\right.$$

✓ **Maple** : cpu = 0.092 (sec), leaf count = 264

$$\left\{\frac{x}{(y(x))^2}\left(\_C1\left(-\frac{1}{2\,y(x)}\left(ax+\sqrt{a^2x^2-4\,b\,(y(x))^2}\right)\right)^{-\frac{a}{a+b}}\left(ax+\sqrt{a^2x^2-4\,b\,(y(x))^2}\right)\left(\frac{a}{2\,(y(x))^2}\left(ax^2+\right.\right.\right.$$

2.470 ODE No. 470

$$x^3y'(x)-x^2y(x)+y(x)y'(x)^2=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.29 (sec), leaf count = 87

$$\left\{y(x)=-\frac{i}{2}x^2,y(x)=\frac{i}{2}x^2,y(x)=-\frac{1}{4}\sqrt{-4\_C1\,x^2+\_C1^2},y(x)=\frac{1}{4}\sqrt{-4\_C1\,x^2+\_C1^2},y(x)=-2\,\frac{\sqrt{\_C1}}{\_}\right.$$

2.471 ODE No. 471

$$y(x)y'(x)^2-(y(x)-x)y'(x)-x=0$$

✓ **Mathematica** : cpu = 0.00898062 (sec), leaf count = 47

$$\left\{\{y(x)\to c_1+x\},\left\{y(x)\to-\sqrt{2c_1-x^2}\right\},\left\{y(x)\to\sqrt{2c_1-x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.015 (sec), leaf count = 33

$$\left\{y(x)=\sqrt{-x^2+\_C1},y(x)=-\sqrt{-x^2+\_C1},y(x)=x+\_C1\right\}$$

2.472 ODE No. 472

$$(y(x)+x)y'(x)^2+2xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.189126 (sec), leaf count = 127

$$\left\{\left\{y(x)\to\frac{1}{3}\left(-2\sqrt{e^{2c_1}-3e^{c_1}x}-e^{c_1}\right)\right\},\left\{y(x)\to\frac{1}{3}\left(2\sqrt{e^{2c_1}-3e^{c_1}x}-e^{c_1}\right)\right\},\left\{y(x)\to e^{c_1}-2\sqrt{e^{c_1}x+e^{2c_1}}\right\}\right.$$

✓ **Maple** : cpu = 0.475 (sec), leaf count = 121

$$\left\{\ln(x)-Artanh\left(\frac{y(x)+2\,x}{2\,x}\frac{1}{\sqrt{\frac{(y(x))^2+xy(x)+x^2}{x^2}}}\right)+\ln\left(\frac{y(x)}{x}\right)-\_C1=0,\ln(x)+Artanh\left(\frac{y(x)+2\,x}{2\,x}\frac{}{\sqrt{\frac{(y(x)}{}}}\right.\right.$$

2.473 ODE No. 473

$$(y(x)-2x)y'(x)^2-2(x-1)y'(x)+y(x)-2=0$$

✓ **Mathematica** : cpu = 0.378817 (sec), leaf count = 165

$$\left\{\left\{y(x)\to\frac{1}{2}\left(-\sqrt{-4e^{c_1}x+4e^{c_1}-e^{2c_1}}-e^{c_1}+4\right)\right\},\left\{y(x)\to\frac{1}{2}\left(\sqrt{-4e^{c_1}x+4e^{c_1}-e^{2c_1}}-e^{c_1}+4\right)\right\},\{y(x)\to$$

✓ **Maple** : cpu = 0.641 (sec), leaf count = 71

$$\left\{y(x)=2+\_C1-\sqrt{\_C1\ (-\_C1+2x-2)},y(x)=2+\frac{=C1}{2}-\frac{1}{2}\sqrt{\_C1\ (-\_C1+4x-4)},y(x)=(x-1)\right.$$

2.474 ODE No. 474

$$2y(x)y'(x)^2-(4x-5)y'(x)+2y(x)=0$$

✓ **Mathematica** : cpu = 0.236901 (sec), leaf count = 135

$$\left\{\left\{y(x)\to-i\sqrt{2}e^{\frac{c_1}{2}}\sqrt{8e^{c_1}+4x-5}\right\},\left\{y(x)\to i\sqrt{2}e^{\frac{c_1}{2}}\sqrt{8e^{c_1}+4x-5}\right\},\left\{y(x)\to-\frac{1}{4}ie^{\frac{c_1}{2}}\sqrt{e^{c_1}+8x-10}\right\},\{y\right.$$

✓ **Maple** : cpu = 1.041 (sec), leaf count = 152

$$\left\{\ln\left(x-\frac{5}{4}\right)+\frac{1}{2}\ln\left(16\frac{(y(x))^2}{(4x-5)^2}-1\right)+\sqrt{-16\frac{(y(x))^2}{(4x-5)^2}+1}-Artanh\left(\frac{1}{\sqrt{-16\frac{(y(x))^2}{(4x-5)^2}+1}}\right)-\frac{\sqrt{4}}{2}\sqrt{\frac{1}{(4x-\right.$$

2.475 ODE No. 475

$$4y(x)y'(x)^2+2xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0690813 (sec), leaf count = 57

$$\left\{\left\{y(x)\to-\frac{1}{2}e^{2c_1}\sqrt{e^{4c_1}-2x}\right\},\left\{y(x)\to\frac{1}{2}e^{2c_1}\sqrt{e^{4c_1}-2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.454 (sec), leaf count = 67

$$\left\{y(x)=\sqrt{\_C1^2-\_C1\,x},y(x)=\sqrt{\_C1^2+\_C1\,x},y(x)=-\frac{i}{2}x,y(x)=\frac{i}{2}x,y(x)=-\sqrt{\_C1\ (x+\_C1)},y(x)\right.$$

2.476 ODE No. 476

$$4x^3y'(x) - 4x^2y(x) + 9y(x)y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.304 (sec), leaf count = 87

$$\left\{y(x) = -\frac{i}{3}x^2, y(x) = \frac{i}{3}x^2, y(x) = -\frac{1}{6}\sqrt{-4\_C1\,x^2 + \_C1^2}, y(x) = \frac{1}{6}\sqrt{-4\_C1\,x^2 + \_C1^2}, y(x) = -2\,\frac{\sqrt{\_C1}}{\_}\right.$$

2.477 ODE No. 477

$$ay(x)y'(x)^2 + (2x - b)y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.305642 (sec), leaf count = 146

$$\left\{\left\{y(x) \to -\frac{e^{\frac{c_1}{2}}\sqrt{2b + e^{c_1} - 4x}}{2\sqrt{a}}\right\}, \left\{y(x) \to \frac{e^{\frac{c_1}{2}}\sqrt{2b + e^{c_1} - 4x}}{2\sqrt{a}}\right\}, \left\{y(x) \to -\sqrt{2}e^{\frac{c_1}{2}}\sqrt{2ae^{c_1} - b + 2x}\right\}, \left\{y(x) -\right.\right.$$

✓ **Maple** : cpu = 0.517 (sec), leaf count = 622

$$\left\{\int_{\_b}^{x} 1\left(-4\_a + 2\,b - 2\sqrt{4\,a\,(y\,(x))^2 + (b - 2\,\_a)^2}\right)\left((2\,\_a - b)\sqrt{4\,a\,(y\,(x))^2 + (b - 2\,\_a)^2} + 4\,a(y(x))^2 + (b -\right.\right.$$

2.478 ODE No. 478

$$\left(y'(x)^2 + 1\right)(ay(x) + b) - c = 0$$

✓ **Mathematica** : cpu = 0.165914 (sec), leaf count = 141

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{c\tan^{-1}\left(\frac{\sqrt{\#1a+b}}{\sqrt{-\#1a-b+c}}\right) - \sqrt{\#1a+b}\sqrt{-\#1a-b+c}}{a}\&\right][c_1 - x]\right\}, \left\{y(x) \to \text{Inverse}\right.\right.$$

✓ **Maple** : cpu = 0.079 (sec), leaf count = 88

$$\left\{x - \int^{y(x)} (\_a\,a + b)\frac{1}{\sqrt{-(\_a\,a + b)(\_a\,a + b - c)}}d\_a - \_C1 = 0, x - \int^{y(x)} -(\_a\,a + b)\frac{1}{\sqrt{-(\_a\,a + b)(\_a\,a\right.\right.$$

2.479 ODE No. 479

$$\mathrm{a0}x + y'(x)(\mathrm{a1}x + \mathrm{b1}y(x) + \mathrm{c1}) + y'(x)^2(\mathrm{a2}x + \mathrm{b2}y(x) + \mathrm{c2}) + \mathrm{b0}y(x) + \mathrm{c0} = 0$$

✗ **Mathematica** : cpu = 300.033 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.304 (sec), leaf count = 929

$$\left\{ x - \mathrm{e}^{\int \frac{1}{2\,b2\,y(x)+2\,a2\,x+2\,c2}\left(-a1\,x-b1\,y(x)-c1+\sqrt{-4\,a0\,a2\,x^2-4\,a0\,b2\,xy(x)+a1^2x^2+2\,a1\,b1\,xy(x)-4\,a2\,b0\,xy(x)-4\,b0\,b2\,(y(x))^2+b1^2(y(x))^2-4\,a0\,c2\,x+}\right.} \right.$$

2.480 ODE No. 480

$$\left(ay(x) - x^2\right) y'(x)^2 + 2xy(x)y'(x)^2 - y(x)^2 = 0$$

✗ **Mathematica** : cpu = 30.3996 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^2 + 2*x*y[x]*Derivative[1][y][x]^2 + (-x^2 + a*y[x])*Derivative[1][y][x]^2 == 0
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((a*y(x)-x^2)*diff(y(x),x)^2+2*x*y(x)*diff(y(x),x)^2-y(x)^2 = 0,y(x))
```

2.481 ODE No. 481

$$\left(x^2 + y(x)^2\right) y'(x) + xy(x)y'(x)^2 + xy(x) = 0$$

✓ **Mathematica** : cpu = 0.00986825 (sec), leaf count = 49

$$\left\{\left\{y(x) \to \frac{c_1}{x}\right\}, \left\{y(x) \to -\sqrt{2c_1 - x^2}\right\}, \left\{y(x) \to \sqrt{2c_1 - x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 35

$$\left\{y(x) = \sqrt{-x^2 + \_C1}, y(x) = \frac{\_C1}{x}, y(x) = -\sqrt{-x^2 + \_C1}\right\}$$

2.482 ODE No. 482

$$\left(a+x^{22}-y(x)^2\right)y'(x)+xy(x)y'(x)^2-xy(x)=0$$

✗ **Mathematica** : cpu = 63.0395 (sec), leaf count = 0 , could not solve

```
DSolve[-(x*y[x]) + (a + x^22 - y[x]^2)*Derivative[1][y][x] + x*y[x]*Derivative[1][y][x]^2 ==
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x*y(x)*diff(y(x),x)^2+(x^22-y(x)^2+a)*diff(y(x),x)-x*y(x) = 0,y(x))
```

2.483 ODE No. 483

$$\left(2xy(x)-x^2\right)y'(x)^2+2xy(x)y'(x)-y(x)^2+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.162142 (sec), leaf count = 71

$$\left\{\left\{y(x)\to e^{\frac{c_1}{2}}-\sqrt{2e^{\frac{c_1}{2}}x-x^2}\right\},\left\{y(x)\to\sqrt{2e^{\frac{c_1}{2}}x-x^2}+e^{\frac{c_1}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.08 (sec), leaf count = 103

$$\left\{y(x)=0,y(x)=RootOf\left(-2\ln(x)+\int^{\_Z}\frac{1}{\_a\left(\_a^2+1\right)}\left(-2\_a^2+\sqrt{2}\sqrt{\_a\left(\_a-1\right)^2}\right)d\_a+2\_C1\right)x,y(\right.$$

2.484 ODE No. 484

$$\left(2xy(x)-x^2\right)y'(x)^2-6xy(x)y'(x)-y(x)^2+2xy(x)=0$$

✓ **Mathematica** : cpu = 0.152838 (sec), leaf count = 81

$$\left\{\left\{y(x)\to-\sqrt{3x^2-2e^{\frac{c_1}{2}}x}-e^{\frac{c_1}{2}}+2x\right\},\left\{y(x)\to\sqrt{3x^2-2e^{\frac{c_1}{2}}x}-e^{\frac{c_1}{2}}+2x\right\}\right\}$$

✓ **Maple** : cpu = 0.08 (sec), leaf count = 115

$$\left\{y(x)=0,y(x)=RootOf\left(-2\ln(x)+\int^{\_Z}\frac{1}{\_a\left(\_a^2-4\_a+1\right)}\left(-2\_a^2+\sqrt{2}\sqrt{\_a\left(\_a+1\right)^2}+4\_a\right)d\_a\right.$$

2.485 ODE No. 485

$$-y'(x)\left(ay(x)^2+bx^2+c\right)+axy(x)y'(x)^2+bxy(x)=0$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.486 ODE No. 486

$$-a^2+y(x)^2y'(x)^2+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0250952 (sec), leaf count = 117

$$\left\{\left\{y(x)\to -\sqrt{a^2-2c_1x-c_1^2-x^2}\right\},\left\{y(x)\to \sqrt{a^2-2c_1x-c_1^2-x^2}\right\},\left\{y(x)\to -\sqrt{a^2+2c_1x-c_1^2-x^2}\right\},\left\{\right.\right.$$

✓ **Maple** : cpu = 0.098 (sec), leaf count = 54

$$\left\{y(x)=a,y(x)=\sqrt{-\_C1^2+2\_C1\,x+a^2-x^2},y(x)=-a,y(x)=-\sqrt{(a-\_C1+x)\,(a+\_C1-x)}\right\}$$

2.487 ODE No. 487

$$-6x^3y'(x)+4x^2y(x)+y(x)^2y'(x)^2=0$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.417 (sec), leaf count = 100

$$\left\{y(x)=RootOf\left(-\ln(x)+\int^{\_Z}-\frac{3}{4\_a\,(4\_a^3-9)}\left(4\_a^3+3\sqrt{-4\_a^3+9}-9\right)d\_a+\_C1\right)x^{\frac{4}{3}},y(x)=\frac{\sqrt[3]{1}}{2}\right.$$

2.488 ODE No. 488

$$4a^2 - 4ay(x)y'(x) - 4ax + y(x)^2y'(x)^2 + y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.350389 (sec), leaf count = 85

$$\left\{\left\{y(x) \to -\frac{\sqrt{16a^3x - 4a^2x^2 - 4ac_1x - c_1^2}}{2a}\right\}, \left\{y(x) \to \frac{\sqrt{16a^3x - 4a^2x^2 - 4ac_1x - c_1^2}}{2a}\right\}\right\}$$

✓ **Maple** : cpu = 0.434 (sec), leaf count = 111

$$\left\{y(x) = -2\sqrt{ax}, y(x) = 2\sqrt{ax}, y(x) = -\frac{1}{4a}\sqrt{-16a^4 + 32a^3x + (-16x^2 + 8\_C1)a^2 + 8\_C1\,ax - \_C1^2}, y(x\right.$$

2.489 ODE No. 489

$$ay(x)^2 + bx + c + y(x)^2y'(x)^2 + 2xy(x)y'(x) = 0$$

✗ **Mathematica** : cpu = 300.974 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 2.375 (sec), leaf count = 551

$$\left\{y(x) = -\frac{\sqrt{16}}{2a(a+1)}\sqrt{\left((a+1)^2\left(ax - \frac{b}{2} + x\right)^2 aRootOf\left(-b\ln(2ax - b + 2x) + 2\int^{\_Z} -1/4\,\frac{}{(a+1)\_a\ (4\right.\right.}\right.$$

2.490 ODE No. 490

$$a - x^2 - 2xy(x)y'(x) + y(x)^2y'(x)^2 + 2y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.583712 (sec), leaf count = 70

$$\left\{\left\{y(x) \to -\frac{\sqrt{-a + 8c_1x - 4c_1^2 - 2x^2}}{\sqrt{2}}\right\}, \left\{y(x) \to \frac{\sqrt{-a + 8c_1x - 4c_1^2 - 2x^2}}{\sqrt{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.434 (sec), leaf count = 145

$$\left\{y(x) = \sqrt{-2\sqrt{a + 2\_C1}x - \_C1 - x^2 - a}, y(x) = \sqrt{2\sqrt{a + 2\_C1}x - \_C1 - x^2 - a}, y(x) = -\sqrt{-2\sqrt{a +}\right.$$

2.491 ODE No. 491

$$(a-1)b+ax^2+2axy(x)y'(x)+(1-a)y(x)^2+y(x)^2y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.99968 (sec), leaf count = 79

$$\left\{\left\{y(x)\to -\sqrt{-2ac_1x+ac_1^2+b+2c_1x-c_1^2-x^2}\right\},\left\{y(x)\to \sqrt{-2ac_1x+ac_1^2+b+2c_1x-c_1^2-x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.75 (sec), leaf count = 195

$$\left\{y(x)=\sqrt{-ax^2+b},y(x)=\frac{1}{a}\sqrt{\left(-2\,x\sqrt{-a\left(b-\_C1\right)\left(a-1\right)}+\left(-x^2+b\right)a-b+\_C1\right)a},y(x)=\frac{1}{a}\sqrt{\left(2\,x\sqrt{-\right.}\right.$$

2.492 ODE No. 492

$$\left(y(x)^2-a^2\right)y'(x)^2+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.271256 (sec), leaf count = 111

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[\sqrt{a^2-\#1^2}-a\log\left(a\sqrt{a^2-\#1^2}+a^2\right)+a\log(\#1)\&\right][c_1-x]\right\},\left\{y(x)\to \text{Inverse}\right.\right.$$

✓ **Maple** : cpu = 0.421 (sec), leaf count = 122

$$\left\{x-\sqrt{a^2-\left(y\left(x\right)\right)^2}+a^2\ln\left(\frac{1}{y\left(x\right)}\left(2\,a^2+2\,\sqrt{a^2}\sqrt{a^2-\left(y\left(x\right)\right)^2}\right)\right)\frac{1}{\sqrt{a^2}}-\_C1=0,x+\sqrt{a^2-\left(y\left(x\right)\right)^2}-a^2\ln\right.$$

2.493 ODE No. 493

$$\left(a^2-2ax+y(x)^2\right)y'(x)^2+2ay(x)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 8.45994 (sec), leaf count = 553

$$\left\{\text{Solve}\left[\left\{y(x)=\frac{-\sqrt{-a\text{K\$1786906}^2\left(a\text{K\$1786906}^2-2\text{K\$1786906}^2x-2x\right)}-a\text{K\$1786906}}{\text{K\$1786906}^2+1},x=\frac{ac_1^2\text{K\$1786906}\right.\right.\right.$$

✓ **Maple** : cpu = 1.113 (sec), leaf count = 111

$$\left\{[x(\_T)=\frac{1}{2\,a}\left(\left(Artanh\left(\frac{1}{\sqrt{\_T^2+1}}\right)\right)^2\sqrt{\_T^2+1}a^2+\left(-2\,a\_C1\sqrt{\_T^2+1}-2\,a^2\right)Artanh\left(\frac{1}{\sqrt{\_T^2+1}}\right.\right.\right.$$

2.494 ODE No. 494

$$\left(y(x)^2-a^2x^2\right)y'(x)^2+\left(1-a^2\right)x^2+2xy(x)y'(x)=0$$

✗ **Mathematica** : cpu = 301.305 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.173 (sec), leaf count = 161

$$\left\{y(x)=\sqrt{a^2-1}x,y(x)=RootOf\left(-\ln\left(x\right)+\int^{\_Z}\frac{1}{\left(\_a^2+1\right)\left(\_a^2-a^2+1\right)}\left(-\_a^3+\_a\,a^2+\sqrt{\_a^2a^2-a^4+\right.\right.\right.$$

2.495 ODE No. 495

$$\left((1-a)x^2+y(x)^2\right)y'(x)^2+2axy(x)y'(x)+(1-a)y(x)^2+x^2=0$$

✓ **Mathematica** : cpu = 0.108989 (sec), leaf count = 83

$$\left\{\text{Solve}\left[\sqrt{a-1}\tan^{-1}\left(\frac{y(x)}{x}\right)-\frac{1}{2}\log\left(\frac{y(x)^2}{x^2}+1\right)=c_1+\log(x),y(x)\right],\text{Solve}\left[\sqrt{a-1}\tan^{-1}\left(\frac{y(x)}{x}\right)+\frac{1}{2}\log\left(\right.\right.\right.$$

✓ **Maple** : cpu = 0.465 (sec), leaf count = 61

$$\left\{y(x)=\tan\left(RootOf\left(-2\_Z\sqrt{a-1}-\ln\left(\frac{x^2}{\left(\cos\left(\_Z\right)\right)^2}\right)+2\_C1\right)\right)x,y(x)=\tan\left(RootOf\left(2\_Z\sqrt{a-1}-\right.\right.\right.$$

2.496 ODE No. 496

$$\left(y(x)-x\right)^2\left(y'(x)^2+1\right)-a^2\left(y'(x)+1\right)^2=0$$

✓ **Mathematica** : cpu = 95.1373 (sec), leaf count = 65

$$\left\{\left\{y(x)\to c_1-\sqrt{a^2+2c_1x-c_1^2-x^2}\right\},\left\{y(x)\to\sqrt{a^2+2c_1x-c_1^2-x^2}+c_1\right\}\right\}$$

✓ **Maple** : cpu = 0.241 (sec), leaf count = 130

$$\left\{y(x)=x-\sqrt{2}a,y(x)=x+\sqrt{2}a,y(x)=x+RootOf\left(-x+\int^{\_Z}-\frac{1}{2\_a^2-4\,a^2}\left(\_a^2-2\,a^2+\sqrt{-\_a^4+2\_\right.\right.\right.$$

2.497 ODE No. 497

$$-x^2-2xy(x)y'(x)+3y(x)^2y'(x)^2+4y(x)^2=0$$

✓ **Mathematica** : cpu = 0.171784 (sec), leaf count = 203

$$\left\{\left\{y(x)\to -\frac{\sqrt{-4ix\sinh(3c_1)-4ix\cosh(3c_1)+\sinh(6c_1)+\cosh(6c_1)-3x^2}}{\sqrt{3}}\right\},\left\{y(x)\to \frac{\sqrt{-4ix\sinh(3c_1)-}\right.\right.$$

✓ **Maple** : cpu = 0.462 (sec), leaf count = 203

$$\left\{\ln(x)-\frac{1}{2}\sqrt{\frac{x^2-3\left(y(x)\right)^2}{x^2}}+Artanh\left(\frac{1}{2}\sqrt{\frac{x^2-3\left(y(x)\right)^2}{x^2}}\right)+\frac{\sqrt{3}}{6}\sqrt{\frac{\left(\sqrt{3}x-3y(x)\right)\left(\sqrt{3}x+3y(x)\right)}{x^2}}+\frac{1}{2}\ln\left(\right.\right.$$

2.498 ODE No. 498

$$(3y(x)-2)y'(x)^2+4y(x)-4=0$$

✓ **Mathematica** : cpu = 0.100323 (sec), leaf count = 107

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\sqrt{1-\#1}\sqrt{3\#1-2}-\frac{\sin^{-1}\left(\sqrt{3-3\#1}\right)}{\sqrt{3}}\&\right][c_1-2x]\right\},\left\{y(x)\to \text{InverseFunctio}\right.\right.$$

✓ **Maple** : cpu = 0.696 (sec), leaf count = 99

$$\left\{y(x)=1,y(x)=\frac{\sin\left(RootOf\left(-8\sqrt{3}\_C1\,\_Z+8\sqrt{3}x\_Z-(\cos(\_Z))^2+48\,\_C1^2-96\,\_C1\,x+48x^2+\_Z\right.\right.\right.}{6}$$

2.499 ODE No. 499

$$a^2\left(-x^2\right)-2a^2xy(x)y'(x)+\left(1-a^2\right)y(x)^2y'(x)^2+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.287979 (sec), leaf count = 212

$$\left\{\left\{y(x)\to -\frac{\sqrt{a^6\left(-x^2\right)+3a^4x^2+2a^2xe^{a^2c_1-c_1}-2xe^{a^2c_1-c_1}+e^{2a^2c_1-2c_1}-3a^2x^2+x^2}}{\sqrt{a^6-3a^4+3a^2-1}}\right\},\left\{y(x)\to \frac{\sqrt{a^6\left(-x^2\right)}}{\right.\right.$$

✓ **Maple** : cpu = 0.19 (sec), leaf count = 189

$$\left\{y(x)=RootOf\left(-\ln(x)+\int^{\_Z}\frac{\_a}{\left(\_a^2+1\right)\left(\_a^2a^2-\_a^2+a^2\right)}\left(-\_a^2a^2+\_a^2-a^2+\sqrt{\_a^2a^2-\_a^2+a^2}\right)d\right.\right.$$

2.500 ODE No. 500

$$(a-b)y(x)^2y'(x)^2-ab+ay(x)^2-bx^2-2bxy(x)y'(x)=0$$

✓ **Mathematica** : cpu = 1.28871 (sec), leaf count = 100

$$\left\{\left\{y(x)\to -\frac{\sqrt{-ab-2ac_1x+ac_1^2+ax^2+b^2-bx^2}}{\sqrt{b-a}}\right\},\left\{y(x)\to \frac{\sqrt{-ab-2ac_1x+ac_1^2+ax^2+b^2-bx^2}}{\sqrt{b-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.936 (sec), leaf count = 220

$$\left\{y(x)=\frac{1}{b}\sqrt{b\left(2x\sqrt{-ab\left(b-\_C1\right)}+\left(-x^2+\_C1+a\right)b-\_C1\,a\right)},y(x)=\frac{1}{b}\sqrt{\left(-2x\sqrt{-ab\left(b-\_C1\right)}+(-x^2\right.}\right.$$

2.501 ODE No. 501

$$y'(x)^2\left(ay(x)^2+bx+c\right)-by(x)y'(x)+dy(x)^2=0$$

✓ **Mathematica** : cpu = 31.2205 (sec), leaf count = 913

$$\left\{\text{Solve}\left[\left\{y(x)=\frac{b\text{K\$1923803}-\sqrt{-\text{K\$1923803}^2\left(-b^2+4a\text{K\$1923803}^2xb+4dxb+4ac\text{K\$1923803}^2+4cd\right)}}{2\left(a\text{K\$1923803}^2+d\right)},x\right.\right.\right.$$

✓ **Maple** : cpu = 4.984 (sec), leaf count = 215

$$\left\{[x(\_T)=-\frac{1}{4\,bd}\left(\sqrt{\_T^2a+d}\left(\ln\left(\frac{1}{\_T}\left(\sqrt{d}\sqrt{\_T^2a+d}+d\right)\right)\right)^2b^2+\left(\left(2\ln(2)\,b^2+4\sqrt{d}\_C1\,b\right)\sqrt{\_T^2a-\right.\right.\right.\right.$$

2.502 ODE No. 502

$$(ay(x)-bx)^2\left(a^2y'(x)^2+b^2\right)-c^2\left(ay'(x)+b\right)^2=0$$

✓ **Mathematica** : cpu = 1.69317 (sec), leaf count = 100

$$\left\{\left\{y(x)\to \frac{bc_1}{a}-\frac{\sqrt{2b^2c_1x-b^2c_1^2+b^2\left(-x^2\right)+c^2}}{a}\right\},\left\{y(x)\to \frac{\sqrt{2b^2c_1x-b^2c_1^2+b^2\left(-x^2\right)+c^2}}{a}+\frac{bc_1}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.39 (sec), leaf count = 195

$$\left\{y(x)=\frac{bx-\sqrt{2}c}{a},y(x)=\frac{bx+\sqrt{2}c}{a},y(x)=\frac{1}{a}\left(RootOf\left(-x+\int^{-Z}\frac{a}{\left(2\_a^2a^2-4\,c^2\right)b}\left(-\_a^2a^2+2\,c^2+\sqrt{-a^2}\right.\right.\right.\right.$$

2.503 ODE No. 503

$$\mathrm{a0} + y'(x)(\mathrm{a1}x + \mathrm{b1}y(x) + \mathrm{c1}) + y'(x)^2(\mathrm{a2}x + \mathrm{b2}y(x) + \mathrm{c2})^2 + \mathrm{b0}y(x) + \mathrm{c0} = 0$$

✗ **Mathematica** : cpu = 300.047 (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((b2*y(x)+a2*x+c2)^2*diff(y(x),x)^2+(a1*x+b1*y(x)+c1)*diff(y(x),x)+b0*y(x)+a0+c0=0,y(x
```

2.504 ODE No. 504

$$-\left(-a + x^3 + y(x)^3\right) y'(x) + x^2 y(x) + x y(x)^2 y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.824 (sec), leaf count = 247

$$\left\{\int_{\_b}^{y(x)} \_a^2 \frac{1}{\sqrt{x^6 + \left(-2\,\_a^3 - 2\,a\right) x^3 + \left(-\_a^3 + a\right)^2}}\,\mathrm{d}\_a - \frac{\ln(x)}{2} - \_C1 = 0, \int_{\_b}^{y(x)} \_a^2 \frac{1}{\sqrt{x^6 + \left(-2\,\_a^3 - 2\,a\right)}}$$

2.505 ODE No. 505

$$-x^3 + x y(x)^2 y'(x)^2 - 2y(x)^3 y'(x) + 2x y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0128633 (sec), leaf count = 73

$$\left\{\left\{y(x) \to -\sqrt{2c_1 + x^2}\right\}, \left\{y(x) \to \sqrt{2c_1 + x^2}\right\}, \left\{y(x) \to -\sqrt{c_1 x^4 + x^2}\right\}, \left\{y(x) \to \sqrt{c_1 x^4 + x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 52

$$\left\{y(x) = \sqrt{x^2 + \_C1}, y(x) = \sqrt{\_C1\,x^2 + 1}x, y(x) = -\sqrt{x^2 + \_C1}, y(x) = -\sqrt{\_C1\,x^2 + 1}x\right\}$$

2.506 ODE No. 506

$$2x^2(y(x)-x)y(x)^2y'(x)+x^2\left(xy(x)^2-1\right)y'(x)^2-\left(x^2y(x)-1\right)y(x)^2=0$$

✗ **Mathematica** : cpu = 61.4466 (sec), leaf count = 0 , could not solve

```
DSolve[-(y[x]^2*(-1 + x^2*y[x])) + 2*x^2*y[x]^2*(-x + y[x])*Derivative[1][y][x] + x^2*(-
1 + x*y[x]^2)*Derivative[1][y][x]^2 == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x^2*(x*y(x)^2-1)*diff(y(x),x)^2+2*x^2*y(x)^2*(y(x)-x)*diff(y(x),x)-y(x)^2*(x^2*y(x)-
1)=0,y(x))
```

2.507 ODE No. 507

$$\left(y(x)^4-a^2x^2\right)y'(x)^2+2a^2xy(x)y'(x)+y(x)^2\left(y(x)^2-a^2\right)=0$$

✓ **Mathematica** : cpu = 29.2474 (sec), leaf count = 443

$$\left\{\text{Solve}\left[\left\{x=\frac{a^2\text{K\$21962}y(\text{K\$21962})-\sqrt{a^2\text{K\$21962}^2\left(\text{K\$21962}^2+1\right)y(\text{K\$21962})^4}}{a^2\text{K\$21962}^2},y(x)=\frac{1}{4}\left(-\frac{ac_1\sqrt{\text{K\$21}}}{\sqrt[4]{\text{K\$21962}^2}}\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.508 ODE No. 508

$$\left(x^2y(x)^2-x^2+y(x)^4\right)y'(x)^2+2xy(x)y'(x)-y(x)^2=0$$

✗ **Mathematica** : cpu = 55.0064 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^2 + 2*x*y[x]*Derivative[1][y][x] + (-x^2 + x^2*y[x]^2 + y[x]^4)*Derivative[1][y
```

✓ **Maple** : cpu = 1.838 (sec), leaf count = 60

$$\left\{y(x)=-ix,y(x)=ix,y(x)=-Artanh\left(RootOf\left(\left(Artanh(\_Z)\right)^2\_Z^2-2\,Artanh(\_Z)\,\_C1\,\_Z^2+\_C1^2\_Z^2\right.\right.\right.$$

2.509 ODE No. 509

$$9\left(x^2-1\right)y(x)^4y'(x)^2-4x^2-6xy(x)^5y'(x)=0$$

✗ **Mathematica** : cpu = 304.56 (sec), leaf count = 0 , timed out

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```

✓ **Maple** : cpu = 1.46 (sec), leaf count = 212

$$\left\{y(x)=\sqrt[6]{-4\,x^2+4},y(x)=-\sqrt[6]{-4\,x^2+4},y(x)=-\frac{1+i\sqrt{3}}{2}\sqrt[6]{-4\,x^2+4},y(x)=\frac{1+i\sqrt{3}}{2}\sqrt[6]{-4\,x^2+4},y(x)=\right.$$

2.510 ODE No. 510

$$-\left(x^4y(x)^2-1\right)y(x)^2+x^2\left(x^2y(x)^4-1\right)y'(x)^2+2x^3\left(y(x)^2-x^2\right)y(x)^3y'(x)=0$$

✗ **Mathematica** : cpu = 60.1835 (sec), leaf count = 0 , could not solve

```
DSolve[-(y[x]^2*(-1 + x^4*y[x]^2)) + 2*x^3*y[x]^3*(-x^2 + y[x]^2)*Derivative[1][y][x] + x^2*
1 + x^2*y[x]^4)*Derivative[1][y][x]^2 == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x^2*(x^2*y(x)^4-1)*diff(y(x),x)^2+2*x^3*y(x)^3*(y(x)^2-x^2)*diff(y(x),x)-
y(x)^2*(x^4*y(x)^2-1)=0,y(x))
```

2.511 ODE No. 511

$$\left(a^2\sqrt{x^2+y(x)^2}-x^2\right)y'(x)^2+a^2\sqrt{x^2+y(x)^2}+2xy(x)y'(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 1.56976 (sec), leaf count = 229

$$\left\{\text{Solve}\left[\tan^{-1}\left(\frac{x}{y(x)}\right)-\frac{2\sqrt{a^2\left(x^2+y(x)^2\right)\left(\sqrt{x^2+y(x)^2}-a^2\right)}\tan^{-1}\left(\frac{\sqrt{\sqrt{x^2+y(x)^2}-a^2}}{a}\right)}{a\sqrt{x^2+y(x)^2}\sqrt{\sqrt{x^2+y(x)^2}-a^2}}=c_1,y(x)\right],\text{Solve}\right.$$

✓ **Maple** : cpu = 5.059 (sec), leaf count = 199

$$\left\{\arctan\left(\frac{x}{y\left(x\right)}\right)-2\frac{\sqrt{a^2\left(\left(y\left(x\right)\right)^2+x^2\right)\left(-a^2+\sqrt{\left(y\left(x\right)\right)^2+x^2}\right)}}{a\sqrt{\left(y\left(x\right)\right)^2+x^2}\sqrt{-a^2+\sqrt{\left(y\left(x\right)\right)^2+x^2}}}\arctan\left(\frac{\sqrt{-a^2+\sqrt{\left(y\left(x\right)\right)^2+x^2}}}{a}\right)-\_C1\right.$$

2.512 ODE No. 512

$$\left(a\left(x^2+y(x)^2\right)^{3/2}-x^2\right)y'(x)^2+a\left(x^2+y(x)^2\right)^{3/2}+2xy(x)y'(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 4.57686 (sec), leaf count = 725

$$\left\{\text{Solve}\left[\tan^{-1}\left(\frac{x}{y(x)}\right)-\frac{i\sqrt{a}\left(x^2+y(x)^2\right)\sqrt{\sqrt{x^2+y(x)^2}-a\left(x^2+y(x)^2\right)}\left(\sqrt{2}\left(\log\left(\frac{a^{3/2}\left(3i\sqrt{2}a\sqrt{x^2+y(x)^2}+4\sqrt{a}\right.\right.\right.\right.\right.}{4a\sqrt{x}}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 11.819 (sec), leaf count = 135

$$\left\{y(x)=x\left(\tan\left(RootOf\left(-\_Z+\int^{\frac{x^2\left((\tan(\_Z))^2+1\right)}{(\tan(\_Z))^2}}-\frac{1}{(2\_a\,a^2-2)\,\_a^2}(\sqrt{\_a}a+1)\sqrt{-\_a^{\frac{5}{2}}a\,(\sqrt{\_a}a-1)}d\_a\right.\right.\right.\right.$$

2.513 ODE No. 513

$$y'(x)^2\sin(y(x))+2xy'(x)\cos^3(y(x))-\sin(y(x))\cos^4(y(x))=0$$

✗ **Mathematica** : cpu = 300.024 (sec), leaf count = 0 , timed out

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$Aborted
```

✓ **Maple** : cpu = 2.854 (sec), leaf count = 1134

$$\left\{[x(\_T)=\frac{1}{2\_T}\left(\left(\cos\left(\frac{1}{2}\arctan\left(1\left(\_C1^2\_T^2-2\_T\_C1\sqrt[3]{\_C1^3\_T^3+54\_T\_C1+6\sqrt{3}\sqrt{\_C1^2\_}\right.\right.\right.\right.\right.\right.\right.\right.$$

2.514 ODE No. 514

$$y'(x)^2(a\cos(y(x))+b)-c\cos(y(x))+d=0$$

✓ **Mathematica** : cpu = 15.1057 (sec), leaf count = 605

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[\frac{4\sin^2\left(\frac{\#1}{2}\right)\csc(\#1)\sqrt{a\cos(\#1)+b}\sqrt{\frac{\cot^2\left(\frac{\#1}{2}\right)(c-d)}{c+d}}\sqrt{\frac{\csc^2\left(\frac{\#1}{2}\right)(a+b)(d-c\cos(\#1))}{ad+bc}}\left(c(a\right.\right.\right.\right.$$

$$\left.\left.\left.\left.c(a\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.228 (sec), leaf count = 87

$$\left\{x-\int^{y(x)}(a\cos(\_a)+b)\frac{1}{\sqrt{(a\cos(\_a)+b)(c\cos(\_a)-d)}}d\_a-\_C1=0,x-\int^{y(x)}-(a\cos(\_a)+b)\frac{}{\sqrt{(a\right.}$$

2.515 ODE No. 515

$$f\left(x^2+y(x)^2\right)\left(y'(x)^2+1\right)-\left(xy'(x)-y(x)\right)^2=0$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 2.286 (sec), leaf count = 113

$$\left\{y(x)=x\left(\tan\left(RootOf\left(-\_Z+\int^{\frac{x^2\left((\tan(\_Z))^2+1\right)}{(\tan(\_Z))^2}}-\frac{1}{2\_a\left(f\left(\_a\right)-\_a\right)}\sqrt{-\left(f\left(\_a\right)-\_a\right)f\left(\_a\right)}d\_a+\_C1\right.\right.\right.$$

2.516 ODE No. 516

$$\left(x^2+y(x)^2\right)f\left(\frac{x}{\sqrt{x^2+y(x)^2}}\right)\left(y'(x)^2+1\right)-\left(xy'(x)-y(x)\right)^2=0$$

✓ **Mathematica** : cpu = 2.90606 (sec), leaf count = 251

$$\left\{\text{Solve}\left[\int_1^{\frac{y(x)}{x}}\frac{K[1]^2f\left(\frac{1}{\sqrt{K[1]^2+1}}\right)+f\left(\frac{1}{\sqrt{K[1]^2+1}}\right)-1}{(K[1]-i)(K[1]+i)\sqrt{f\left(\frac{1}{\sqrt{K[1]^2+1}}\right)}\left(K[1]\sqrt{f\left(\frac{1}{\sqrt{K[1]^2+1}}\right)}+i\sqrt{f\left(\frac{1}{\sqrt{K[1]^2+1}}\right)-1}\right)}dK[1]=c_1-\right.\right.$$

✓ **Maple** : cpu = 1.141 (sec), leaf count = 72

$$\left\{y(x)=RootOf\left(-\ln(x)+\int^{-Z}-\frac{1}{\_a^2+1}\left(\_a\,f\left(\frac{1}{\sqrt{\_a^2+1}}\right)-\sqrt{-\left(f\left(\frac{1}{\sqrt{\_a^2+1}}\right)\right)^2+f\left(\frac{1}{\sqrt{\_a^2+1}}\right)\right.\right.\right.$$

2.517 ODE No. 517

$$\left(x^2+y(x)^2\right)f\left(\frac{y(x)}{\sqrt{x^2+y(x)^2}}\right)\left(y'(x)^2+1\right)-\left(xy'(x)-y(x)\right)^2=0$$

✓ **Mathematica** : cpu = 3.0065 (sec), leaf count = 281

$$\left\{\text{Solve}\left[\int_1^{\frac{y(x)}{x}}\frac{K[1]^2 f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right)+f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right)-1}{(K[1]-i)(K[1]+i)\sqrt{f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right)}\left(K[1]\sqrt{f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right)}+i\sqrt{f\left(\frac{K[1]}{\sqrt{K[1]^2+1}}\right)-1}\right)}dK[1]=c_1\right.\right.$$

✓ **Maple** : cpu = 1.198 (sec), leaf count = 155

$$\left\{y(x)=RootOf\left(-\ln(x)+\int^{-Z}\frac{1}{\_a^2+1}\left(-\_a\,f\left(\_a\frac{1}{\sqrt{\_a^2+1}}\right)+\sqrt{-\left(f\left(\_a\frac{1}{\sqrt{\_a^2+1}}\right)\right)^2+f\left(\_a\frac{1}{\sqrt{\_}\right.\right.\right.\right.$$

2.518 ODE No. 518

$$y'(x)^3-(y(x)-a)^2(y(x)-b)^2=0$$

✓ **Mathematica** : cpu = 0.776651 (sec), leaf count = 236

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[-\frac{3\sqrt[3]{a-\#1}\left(\frac{\#1-b}{a-b}\right)^{2/3}\,{}_2F_1\left(\frac{1}{3},\frac{2}{3};\frac{4}{3};\frac{a-\#1}{a-b}\right)}{(b-\#1)^{2/3}}\&\right][c_1+x]\right\},\left\{y(x)\to\text{InverseFunctio}\right.\right.$$

✓ **Maple** : cpu = 0.195 (sec), leaf count = 126

$$\left\{x-\int^{y(x)}\frac{1}{\sqrt[3]{(\_a-a)^2(-b+\_a)^2}}d\_a-\_C1=0,x-\int^{y(x)}-2\frac{1}{\left(1+i\sqrt{3}\right)\sqrt[3]{(-\_a+a)^2(b-\_a)^2}}d\_a-\_\right.$$

2.519 ODE No. 519

$$y'(x)^3 - f(x)\left(ay(x)^2 + by(x) + c\right)^2 = 0$$

✓ **Mathematica** : cpu = 1.75358 (sec), leaf count = 473

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{3\left(2\#1a - \sqrt{b^2-4ac} + b\right)\left(\frac{2\#1a+\sqrt{b^2-4ac}+b}{\sqrt{b^2-4ac}}\right)^{2/3}\ {}_2F_1\left(\frac{1}{3},\frac{2}{3};\frac{4}{3};\frac{-b-2a\#1+\sqrt{b^2-4ac}}{2\sqrt{b^2-4ac}}\right)}{2\ 2^{2/3}a(\#1(\#1a+b)+c)^{2/3}}\&\right.\right.\right.$$

✓ **Maple** : cpu = 0.423 (sec), leaf count = 197

$$\left\{\int^{y(x)} \left(\_a^2 a + \_a\, b + c\right)^{-\frac{2}{3}} d\_a + \int^{x} -1\sqrt[3]{f\left(\_a\right)\left(a\left(y\left(x\right)\right)^2 + by\left(x\right) + c\right)^2}\left(a(y(x))^2 + by(x) + c\right)^{-\frac{2}{3}} d\_a + \_\right.$$

2.520 ODE No. 520

$$y'(x)^3 + y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 224.251 (sec), leaf count = 3323

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\frac{\left(243\#1^2 - 27\sqrt{81\#1^2+12}\#1 - 24\sqrt[3]{2}\sqrt[6]{3}\tan^{-1}\left(\frac{1}{\sqrt{3}} - \left(\frac{2}{3}\right)^{2/3}\sqrt[3]{\sqrt{81\#1^2+12} - \right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.178 (sec), leaf count = 245

$$\left\{x - \int^{y(x)} 6\,\frac{\sqrt[3]{108\_a + 12\sqrt{81\_a^2+12}}}{\left(108\_a + 12\sqrt{81\_a^2+12}\right)^{2/3} - 12} d\_a - \_C1 = 0, x - \int^{y(x)} -12\,\frac{}{\left(1+i\sqrt{3}\right)\left(\sqrt[3]{108\_a + 12\sqrt{8}\right.}\right.\right.$$

2.521 ODE No. 521

$$y'(x)^3 + xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.00443687 (sec), leaf count = 14

$$\{\{y(x) \to c_1 x + c_1^3\}\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 33

$$\left\{y(x) = \_C1\left(\_C1^2 + x\right), y(x) = -\frac{2x}{9}\sqrt{-3x}, y(x) = \frac{2x}{9}\sqrt{-3x}\right\}$$

2.522 ODE No. 522

$$y'(x)^3 - (x+5)y'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.0046567 (sec), leaf count = 20

$$\{\{y(x) \to c_1 x - c_1^3 + 5c_1\}\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 44

$$\left\{y(x) = \_C1\left(-\_C1^2 + x + 5\right), y(x) = -\frac{2x+10}{9}\sqrt{3x+15}, y(x) = \frac{2x+10}{9}\sqrt{3x+15}\right\}$$

2.523 ODE No. 523

$$-axy'(x) + x^3 + y'(x)^3 = 0$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.057 (sec), leaf count = 231

$$\left\{y(x) = \int i\left(\left(\frac{i}{12} - \frac{\sqrt{3}}{12}\right)\left(-108x^3 + 12\sqrt{-12a^3x^3 + 81x^6}\right)^{\frac{2}{3}} + \left(\sqrt{3}+i\right)xa\right)\frac{1}{\sqrt[3]{-108x^3 + 12\sqrt{-12a^3x^3 +}}}\right.$$

2.524 ODE No. 524

$$y'(x)^3 - 2y(x)y'(x) + y(x)^2 = 0$$

✗ **Mathematica** : cpu = 0 (sec), leaf count = 0 , crash

```
Kernel Crash
```

✓ **Maple** : cpu = 0.058 (sec), leaf count = 261

$$\left\{x - \int^{y(x)} 6\,\frac{\sqrt[3]{-108\_a^2 + 12\sqrt{3}\sqrt{27\_a^4 - 32\_a^3}}}{\left(-108\_a^2 + 12\sqrt{3}\sqrt{27\_a^4 - 32\_a^3}\right)^{2/3} + 24\_a}\,d\_a - \_C1 = 0, x - \int^{y(x)} 24\,\frac{}{\left(i\sqrt{3} - 1\right)\left((i\sqrt{3}\right.}$$

2.525 ODE No. 525

$$-axy(x)y'(x) + 2ay(x)^2 + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0630733 (sec), leaf count = 135

$$\left\{\left\{y(x) \to c_1 \exp\left(\frac{1}{2}\left(\frac{ax^2}{2} + \frac{1}{2}\sqrt{a}x\sqrt{ax^2 - 8} - 4\log\left(\sqrt{a}\sqrt{ax^2 - 8} + ax\right)\right)\right)\right\}, \left\{y(x) \to c_1 \exp\left(\frac{1}{2}\left(\frac{ax^2}{2} - \frac{1}{2}\sqrt{}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.06 (sec), leaf count = 122

$$\left\{y(x) = \_C1\left(a^2x\frac{1}{\sqrt{a^2}} + \sqrt{a^2x^2 - 8\,a}\right)^{-2\frac{a}{\sqrt{a^2}}} \mathrm{e}^{\frac{x}{4}\left(ax + \sqrt{a^2x^2 - 8\,a}\right)}, y(x) = \_C1\left(a^2x\frac{1}{\sqrt{a^2}} + \sqrt{a^2x^2 - 8\,a}\right)^{2\frac{a}{\sqrt{a^2}}} \mathrm{e}\right.$$

2.526 ODE No. 526

$$-x^3y(x)^3 - \left(x^2 + xy(x) + y(x)^2\right)y'(x)^2 + \left(x^3y(x) + x^2y(x)^2 + xy(x)^3\right)y'(x) + y'(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.00974889 (sec), leaf count = 45

$$\left\{\left\{y(x) \to \frac{1}{-c_1 - x}\right\}, \left\{y(x) \to c_1 e^{\frac{x^2}{2}}\right\}, \left\{y(x) \to c_1 + \frac{x^3}{3}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 32

$$\left\{y(x) = \left(-x + \_C1\right)^{-1}, y(x) = \mathrm{e}^{\frac{x^2}{2}}\_C1, y(x) = \frac{x^3}{3} + \_C1\right\}$$

2.527 ODE No. 527

$$-xy(x)^4y'(x)+y'(x)^3-y(x)^5=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.847 (sec), leaf count = 43

$$\left\{y(x)=\sqrt{\frac{\_C1^{10}}{\left(\_C1^4x-1\right)^2}}\_C1,y(x)=-\frac{3\sqrt{3}}{2}x^{-\frac{3}{2}},y(x)=\frac{3\sqrt{3}}{2}x^{-\frac{3}{2}}\right\}$$

2.528 ODE No. 528

$$abx+ay'(x)^2+by(x)+y'(x)^3=0$$

✗ **Mathematica** : cpu = 300.005 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.072 (sec), leaf count = 86

$$\left\{y(x)=-ax-\frac{\left(\mathrm{e}^{RootOf\left(-2a^2\_Z-3\mathrm{e}^{2\_Z}+8a\mathrm{e}^{\_Z}+2\_C1\,b-5a^2-2bx\right)}-a\right)^2\mathrm{e}^{RootOf\left(-2a^2\_Z-3\mathrm{e}^{2\_Z}+8a\mathrm{e}^{\_Z}+2\_C1\,b-5a^2-\right.}}{b}\right.$$

2.529 ODE No. 529

$$y'(x)^3+xy'(x)^2-y(x)=0$$

✓ **Mathematica** : cpu = 52.8349 (sec), leaf count = 1758

$$\left\{\left\{y(x)\to\frac{1}{2}\left(\frac{4\ 2^{2/3}x^4}{3\left(-16x^3-72x^2-108x+216c_1+\sqrt{4\left(-4x^2-12x-9\right)^3+\left(-16x^3-72x^2-108x+216c_1+5\right.}\right.}\right.\right.$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 1251

$$\left\{y(x)=0,y(x)=1\left((-8\,x-6)\sqrt[3]{-36\,x^2-54\,x+108\,\_C1-8\,x^3+27+6\sqrt{-6\,\left(1+2\,\_C1\right)\left(4\,x^3+18\,x^2-2\right.}}\right.\right.$$

2.530 ODE No. 530

$$y'(x)^3 - y(x)y'(x)^2 + y(x)^2 = 0$$

✗ **Mathematica** : cpu = 0 (sec), leaf count = 0 , crash

```
Kernel Crash
```

✓ **Maple** : cpu = 0.12 (sec), leaf count = 432

$$\left\{ x - \int^{y(x)} 6 \frac{\sqrt[3]{-108\_a^2 + 8\_a^3 + 12\sqrt{-12\_a^5 + 81\_a^4}}}{4\_a^2 + 2\_a \sqrt[3]{-108\_a^2 + 8\_a^3 + 12\sqrt{-12\_a^5 + 81\_a^4}} + \left(-108\_a^2 + 8\_a^3 + 12\sqrt{-12\_a^5}\right.} \right.$$

2.531 ODE No. 531

$$-x^3y(x)^6 - \left(x^2 + y(x)^4 + xy(x)^2\right)y'(x)^2 + \left(x^3y(x)^2 + x^2y(x)^4 + xy(x)^6\right)y'(x) + y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 68.9487 (sec), leaf count = 0 , could not solve

```
DSolve[-(x^3*y[x]^6) + (x^3*y[x]^2 + x^2*y[x]^4 + x*y[x]^6)*Derivative[1][y][x] + Derivative
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)^2-(y(x)^4+x*y(x)^2+x^2)*diff(y(x),x)^2+(x*y(x)^6+x^2*y(x)^4+x^3*y(x)^2)*
x^3*y(x)^6=0,y(x))
```

2.532 ODE No. 532

$$ay'(x)^3 + by'(x)^2 + cy'(x) - d - y(x) = 0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.157 (sec), leaf count = 848

$$\left\{ x - \int^{y(x)} 6 \frac{a\sqrt[3]{12\sqrt{3}\sqrt{27\,(d+\_a)^2a^2}}}{\left(12\sqrt{3}\sqrt{27\,(d+\_a)^2a^2} + 18\,((d+\_a)b + 2/9\,c^2)ca + (-4\,d - 4\,\_a)b^3 - b^2c^2a + (108\,d + 108\_\right.} \right.$$

2.533 ODE No. 533

$$a + xy'(x)^3 - y(x)y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 300.192 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.035 (sec), leaf count = 76

$$\left\{y(x) = \frac{\_C1^3 x + a}{\_C1^2}, y(x) = \frac{3\sqrt[3]{2}}{2}\sqrt[3]{ax^2}, y(x) = -\frac{3\sqrt[3]{2}(1+i\sqrt{3})}{4}\sqrt[3]{ax^2}, y(x) = \frac{3\sqrt[3]{2}(i\sqrt{3}-1)}{4}\sqrt[3]{ax^2}\right\}$$

2.534 ODE No. 534

$$4xy'(x)^3 - 6y(x)y'(x)^2 + 3y(x) - x = 0$$

✗ **Mathematica** : cpu = 300.011 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.074 (sec), leaf count = 84

$$\left\{y(x) = x, y(x) = -\frac{(1+\sqrt{3})\,x}{2}, y(x) = \frac{(\sqrt{3}-1)\,x}{2}, y(x) = \frac{1}{3\_C1}\left(-\sqrt{2}(x+\_C1)\sqrt{\_C1\ (x+\_C1)} - \_C1\right.\right.$$

2.535 ODE No. 535

$$8xy'(x)^3 - 12y(x)y'(x)^2 + 9y(x) = 0$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.056 (sec), leaf count = 51

$$\left\{y(x) = 0, y(x) = -\frac{3\,x}{2}, y(x) = \frac{3\,x}{2}, y(x) = -\frac{1}{3\_C1^2}(\_C1\ (3\_C1 + x))^{\frac{3}{2}}, y(x) = \frac{1}{3\_C1^2}(\_C1\ (3\_C1 + x))^{\frac{3}{2}}\right.$$

2.536 ODE No. 536

$$bx\left(x^2-a^2\right)y'(x)^2+\left(x^2-a^2\right)y'(x)^3+bx+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0254168 (sec), leaf count = 86

$$\left\{\left\{y(x)\to c_1-\frac{bx^2}{2}\right\},\left\{y(x)\to c_1-\tan^{-1}\left(\frac{x\sqrt{a^2-x^2}}{x^2-a^2}\right)\right\},\left\{y(x)\to \tan^{-1}\left(\frac{x\sqrt{a^2-x^2}}{x^2-a^2}\right)+c_1\right\}\right\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 52

$$\left\{y(x)=-\frac{bx^2}{2}+\_C1,y(x)=-\arctan\left(x\frac{1}{\sqrt{a^2-x^2}}\right)+\_C1,y(x)=\arctan\left(x\frac{1}{\sqrt{a^2-x^2}}\right)+\_C1\right\}$$

2.537 ODE No. 537

$$\left(x^6+3xy(x)^2\right)y'(x)-2x^5y(x)+x^3y'(x)^3-3x^2y(x)y'(x)^2-y(x)^3=0$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 598.448 (sec), leaf count = 209

$$\left\{y(x)=RootOf\left(-\ln(x)+\int^{\_Z}-\frac{1}{6\_a}\left(3\sqrt{81\_a^2+12}\_a\,4^{2/3}\left(\frac{3\sqrt{81\_a^2+12}\_a-27\_a^2-4}{\left(27\_a^2+4\right)^2}\right)^{2/3}+27\_\right.\right.\right.$$

2.538 ODE No. 538

$$2\left(xy'(x)+y(x)\right)^3-y(x)y'(x)=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 10.397 (sec), leaf count = 1532

$$\left\{\int_{\_b}^{x}1\left(-6^{\frac{2}{3}}\left(-9\_a^2\left(-1/9\sqrt{3}\sqrt{\frac{27\_a\left(y(x)\right)^2-2y(x)}{\_a}}+y(x)\right)y(x)\right)^{\frac{2}{3}}+6\_a\,y(x)\left(\sqrt[3]{6}\sqrt[3]{-9\_a^2\left(-1/9\right.}\right.\right.\right.$$

2.539 ODE No. 539

$$\sin(x)y'(x)^3 - y'(x)^2\left(y(x)\sin(x) - \cos^2(x)\right) - y'(x)\left(y(x)\cos^2(x) + \sin(x)\right) + y(x)\sin(x) = 0$$

✓ **Mathematica** : cpu = 0.0304389 (sec), leaf count = 45

$$\left\{\{y(x) \to c_1 e^x\}, \{y(x) \to c_1 - \cos(x)\}, \left\{y(x) \to c_1 - \log\left(\sin\left(\frac{x}{2}\right)\right) + \log\left(\cos\left(\frac{x}{2}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 3.576 (sec), leaf count = 32

$$\{y(x) = \_C1\, \mathrm{e}^x, y(x) = -\cos(x) + \_C1, y(x) = -\ln(\csc(x) - \cot(x)) + \_C1\}$$

2.540 ODE No. 540

$$2y(x)y'(x)^3 - y(x)y'(x)^2 + 2xy'(x) - x = 0$$

✓ **Mathematica** : cpu = 0.0220986 (sec), leaf count = 69

$$\left\{\left\{y(x) \to c_1 + \frac{x}{2}\right\}, \left\{y(x) \to \frac{\left(3c_1 - 2ix^{3/2}\right)^{2/3}}{2^{2/3}}\right\}, \left\{y(x) \to \frac{\left(3c_1 + 2ix^{3/2}\right)^{2/3}}{2^{2/3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.35 (sec), leaf count = 109

$$\left\{x + \frac{\_C1\, x}{y(x)}\left(\frac{1}{y(x)}\left(-\sqrt{-xy(x)} + y(x)\right)\right)^{-\frac{2}{3}}\left(\frac{1}{y(x)}\left(-x + \sqrt{-xy(x)} + y(x)\right)\right)^{-\frac{2}{3}} = 0, x + \frac{\_C1\, x}{y(x)}\left(\frac{1}{y(x)}\left(\sqrt{\right.\right.\right.\right.$$

2.541 ODE No. 541

$$y(x)^2y'(x)^3 + 2xy'(x) - y(x) = 0$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 3.656 (sec), leaf count = 103

$$\left\{y(x) = \sqrt{\_C1^3 + 2\_C1\, x}, y(x) = -\frac{2i}{3}\sqrt[4]{2}\sqrt[4]{3}\sqrt[4]{-x^3}, y(x) = \frac{2i}{3}\sqrt[4]{2}\sqrt[4]{3}\sqrt[4]{-x^3}, y(x) = -\sqrt{\_C1^3 + 2\_C1\, x}, y(\right.$$

2.542 ODE No. 542

$$16y(x)^2y'(x)^3+2xy'(x)-y(x)=0$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 3.376 (sec), leaf count = 107

$$\left\{y(x)=\sqrt{16\_C1^3+2\_C1\,x},y(x)=-\frac{i}{3}\sqrt[4]{2}\sqrt[4]{3}\sqrt[4]{-x^3},y(x)=\frac{i}{3}\sqrt[4]{2}\sqrt[4]{3}\sqrt[4]{-x^3},y(x)=-\sqrt{16\_C1^3+2\_C1\,x}\right.$$

2.543 ODE No. 543

$$x\left(x^2+1\right)y'(x)-x^2y(x)+y(x)^3\left(-y'(x)^2\right)+xy(x)^2y'(x)^3=0$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 12.393 (sec), leaf count = 277

$$\left\{y(x)=-\frac{i}{2}\sqrt[4]{-16\,x^4+40\,x^2+2-2\,\sqrt{-\left(8\,x^2-1\right)^3}},y(x)=-\frac{i}{2}\sqrt[4]{-16\,x^4+40\,x^2+2+2\,\sqrt{-\left(8\,x^2-1\right)^3}},y(x)\right.$$

2.544 ODE No. 544

$$x^7y(x)^2y'(x)^3-\left(3x^6y(x)^3-1\right)y'(x)^2+3x^5y(x)^4y'(x)-x^4y(x)^5=0$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 15.838 (sec), leaf count = 4201

$$\left\{\int_{\_b}^{x}\frac{1}{\_a}\left(\left(1-i\sqrt{3}\right)\left(-108\left(y(x)\right)^6\_a^{12}+12\sqrt{3}\sqrt{\frac{27\_a^6\left(y\left(x\right)\right)^3-4}{y\left(x\right)}}\left(y(x)\right)^5\_a^9+72\_a^6\left(y(x)\right)^3-8\right)^{\frac{2}{3}}+\right.\right.$$

2.545 ODE No. 545

$$y'(x)^4 - (y(x)-a)^3 (y(x)-b)^2 = 0$$

✓ **Mathematica** : cpu = 0.732085 (sec), leaf count = 383

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{\sqrt[4]{a-\#1}\sqrt{\frac{\#1-b}{a-b}}B_{\frac{a-\#1}{a-b}}\left(\frac{1}{4},\frac{1}{2}\right)}{\sqrt{b-\#1}\sqrt[4]{\frac{a-\#1}{a-b}}}\&\right]\left[c_1 - \sqrt[4]{-1}x\right]\right\}, \left\{y(x) \to \text{InverseFunction}\left[-\right.\right.\right.$$

✓ **Maple** : cpu = 0.926 (sec), leaf count = 144

$$\left\{x - \int^{y(x)} \frac{1}{\sqrt[4]{(\_a-a)^3 (-b+\_a)^2}} d\_a - \_C1 = 0, x - \int^{y(x)} -i\frac{1}{\sqrt[4]{-(-\_a+a)^3 (b-\_a)^2}} d\_a - \_C1 = 0, x\right.$$

2.546 ODE No. 546

$$y'(x)^4 + 3(x-1)y'(x)^2 - 3(2y(x)-1)y'(x) + 3x = 0$$

✗ **Mathematica** : cpu = 300.006 (sec), leaf count = 0 , timed out

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$Aborted
```

✓ **Maple** : cpu = 2.064 (sec), leaf count = 171

$$\left\{y(x) = 1\left(\left(-6+\_C1^3+(6x-6)\_C1\right)\sqrt{\_C1^2+4x} - 2\_C1^4 + (-14x+6)\_C1^2 + \left(\left(\_C1^2+4x\right)^{\frac{3}{2}}+6\right)\right.\right.$$

2.547 ODE No. 547

$$y'(x)^4 - 4y(x)\left(xy'(x) - 2y(x)\right)^2 = 0$$

✓ **Mathematica** : cpu = 1.34914 (sec), leaf count = 490

$$\left\{\text{Solve}\left[\frac{\sqrt{\left(x^2-4\sqrt{y(x)}\right)y(x)}\log\left(\sqrt{x^2-4\sqrt{y(x)}}+x\right)}{\sqrt{x^2-4\sqrt{y(x)}}\sqrt{y(x)}} - \frac{\sqrt{x^2-4\sqrt{y(x)}}\sqrt{y(x)}\log(y(x))}{4\sqrt{\left(x^2-4\sqrt{y(x)}\right)y(x)}} + \frac{1}{4}\log(y(x)) = c\right.\right.$$

✓ **Maple** : cpu = 3.52 (sec), leaf count = 118

$$\left\{1\left(\sqrt{x^2-4\sqrt{y(x)}}-x\right)^{1\sqrt{x^2y(x)-4(y(x))^{3/2}}\frac{1}{\sqrt{x^2-4\sqrt{y(x)}}}\frac{1}{\sqrt{y(x)}}}\frac{1}{\sqrt{y(x)}}\left(\left(\sqrt{x^2-4\sqrt{y(x)}}+x\right)^{1\sqrt{x^2y(x)-4(y(x))^{3/2}}}\right.\right.$$

2.548 ODE No. 548

$$y'(x)^6-(y(x)-a)^4(y(x)-b)^3=0$$

✓ **Mathematica** : cpu = 1.01739 (sec), leaf count = 569

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\frac{\sqrt[3]{a-\#1}\sqrt{\frac{\#1-b}{a-b}}B_{\frac{a-\#1}{a-b}}\left(\frac{1}{3},\frac{1}{2}\right)}{\sqrt{b-\#1}\sqrt[3]{\frac{a-\#1}{a-b}}}\&\right][c_1-ix]\right\},\left\{y(x)\to \text{InverseFunction}\left[-\frac{\sqrt[3]{a-}\right.\right.\right.$$

✓ **Maple** : cpu = 0.768 (sec), leaf count = 246

$$\left\{x-\int^{y(x)}\frac{1}{\sqrt[6]{(\_a-a)^4(-b+\_a)^3}}d\_a-\_C1=0,x-\int^{y(x)}\frac{-2\,i}{-i+\sqrt{3}}\frac{1}{\sqrt[6]{-(-\_a+a)^4(b-\_a)^3}}d\_a-\_C1\right.$$

2.549 ODE No. 549

$$x^2\left(y'(x)^2+1\right)^3-a^2=0$$

✓ **Mathematica** : cpu = 0.246782 (sec), leaf count = 406

$$\left\{\left\{y(x)\to c_1-\frac{\sqrt[3]{x}\left(2x^{2/3}+\left(1+i\sqrt{3}\right)a^{2/3}\right)\sqrt{\frac{-2x^{2/3}+\left(-1-i\sqrt{3}\right)a^{2/3}}{x^{2/3}}}}{2\sqrt{2}}\right\},\left\{y(x)\to c_1+\frac{\sqrt[3]{x}\sqrt{\frac{-2x^{2/3}+\left(-1-i\sqrt{3}\right)a^{2/3}}{x^{2/3}}}}{2\sqrt{}}\right.\right.$$

✓ **Maple** : cpu = 4.315 (sec), leaf count = 545

$$\left\{y(x)=1\sqrt{-\frac{1}{a^4}\left(a^2x\right)^{\frac{4}{3}}\left(\left(a^2x\right)^{\frac{2}{3}}-a^2\right)}\left(a^2-\left(a^2x\right)^{\frac{2}{3}}\right)\left(a^2x\right)^{-\frac{2}{3}}+\_C1,y(x)=1\sqrt{-\frac{1}{a^4}\left(a^2x\right)^{\frac{4}{3}}\left(\left(a^2x\right)^{\frac{2}{3}}-a^2\right)}\left(\right.\right.$$

2.550 ODE No. 550

$$-ay(x)^s - bx^{\frac{rs}{r-s}} + y'(x)^r = 0$$

✗ **Mathematica** : cpu = 300.024 (sec), leaf count = 0 , timed out

```
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```

✓ **Maple** : cpu = 3.802 (sec), leaf count = 60

$$\left\{(-r+s)\int_{\_b}^{y(x)}\left(x(r-s)\sqrt[r]{\_a\_a^s+bx^{\frac{rs}{r-s}}}-r\_a\right)^{-1}\mathrm{d}\_a+\ln(x)-\_C1=0\right\}$$

2.551 ODE No. 551

$$y'(x)^n - f(x)^n(y(x)-a)^{n+1}(y(x)-b)^{n-1} = 0$$

✓ **Mathematica** : cpu = 0.380168 (sec), leaf count = 84

$$\left\{\left\{y(x)\to\frac{-a(a-b)^n\left(\int_1^x(-1)^{\frac{1}{n}+1}f(K[1])\,dK[1]+c_1\right)^n-bn^n}{-(a-b)^n\left(\int_1^x(-1)^{\frac{1}{n}+1}f(K[1])\,dK[1]+c_1\right)^n-n^n}\right\}\right\}$$

✓ **Maple** : cpu = 1.128 (sec), leaf count = 55

$$\left\{y(x)=1\left(b\left(-\frac{n}{(a-b)\left(\int f(x)\,\mathrm{d}x+\_C1\right)}\right)^n-a\right)\left(-1+\left(-\frac{n}{(a-b)\left(\int f(x)\,\mathrm{d}x+\_C1\right)}\right)^n\right)^{-1}\right\}$$

2.552 ODE No. 552

$$y'(x)^n - f(x)g(y(x)) = 0$$

✓ **Mathematica** : cpu = 0.243341 (sec), leaf count = 39

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[\int_1^{\#1}g(K[1])^{-1/n}\,dK[1]\&\right]\left[\int_1^x f(K[2])^{\frac{1}{n}}\,dK[2]+c_1\right]\right\}\right\}$$

✓ **Maple** : cpu = 1.036 (sec), leaf count = 43

$$\left\{\int^{y(x)}(g(\_a))^{-n^{-1}}\,d\_a+\int^x-\frac{\sqrt[n]{f(\_a)\,g(y(x))}}{\sqrt[n]{g(y(x))}}d\_a+\_C1=0\right\}$$

2.553 ODE No. 553

$$ay'(x)^m + by'(x)^n - y(x) = 0$$

✓ **Mathematica** : cpu = 0.120125 (sec), leaf count = 51

$$\text{Solve}\left[\left\{x = \frac{am\text{K\$708434}^{m-1}}{m-1} + \frac{bn\text{K\$708434}^{n-1}}{n-1} + c_1, y(x) = a\text{K\$708434}^m + b\text{K\$708434}^n\right\}, \{y(x), \text{K\$708434}\}\right]$$

✓ **Maple** : cpu = 0.308 (sec), leaf count = 36

$$\left\{x - \int^{y(x)} (RootOf(-a\_Z^m - b\_Z^n + \_a))^{-1} d\_a - \_C1 = 0, y(x) = 0\right\}$$

2.554 ODE No. 554

$$x^{n-1}y'(x)^n - nxy'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.0757894 (sec), leaf count = 49

$$\text{Solve}\left[\left\{y(x) = \frac{\text{K\$708605}nx^2 - \text{K\$708605}^n x^n}{x}, x = c_1(\text{K\$708605} - \text{K\$708605}n)^{\frac{n}{1-n}}\right\}, \{y(x), \text{K\$708605}\}\right]$$

✓ **Maple** : cpu = 1.642 (sec), leaf count = 32

$$\left\{y(x) = \frac{1}{\_C1}\left(\_C1^2 \sqrt[n]{\frac{x}{\_C1}}n - \left(\_C1^{-1}\right)^{-n}\right)\right\}$$

2.555 ODE No. 555

$$xy'(x) + \sqrt{y'(x)^2 + 1} - y(x) = 0$$

✗ **Mathematica** : cpu = 303.203 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.137 (sec), leaf count = 15

$$\left\{y(x) = \sqrt{\_C1^2 + 1} + \_C1\, x\right\}$$

2.556 ODE No. 556

$$xy'(x)^2+\sqrt{y'(x)^2+1}+y(x)=0$$

✓ **Mathematica** : cpu = 6.42473 (sec), leaf count = 60

$$\text{Solve}\left[\left\{x=\frac{c_1}{(\text{K\$708818}+1)^2}+\frac{-\sqrt{\text{K\$708818}^2+1}-\sinh^{-1}(\text{K\$708818})}{(\text{K\$708818}+1)^2},y(x)=\text{K\$708818}^2(-x)-\sqrt{\text{K\$70881}\right.\right.$$

✓ **Maple** : cpu = 1.483 (sec), leaf count = 581

$$\left\{\_C1\,x^2\left(\sqrt{-4\,xy\left(x\right)+2+2\,\sqrt{4\,x^2-4\,xy\left(x\right)+1}}-2\,x\right)^{-2}+x+2\,\frac{x^2}{\left(\sqrt{-4\,xy\left(x\right)+2+2\,\sqrt{4\,x^2-4\,xy\left(x\right)+}\right.}\right.$$

2.557 ODE No. 557

$$x\left(y'(x)+\sqrt{y'(x)^2+1}\right)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0172032 (sec), leaf count = 39

$$\left\{\left\{y(x)\to-\sqrt{c_1x-x^2}\right\},\left\{y(x)\to\sqrt{c_1x-x^2}\right\}\right\}$$

✓ **Maple** : cpu = 1.015 (sec), leaf count = 74

$$\left\{2\,xy(x)\,\_C1\,\frac{1}{\sqrt{\frac{\left((y(x))^2+x^2\right)^2}{x^2(y(x))^2}}}\left(\sqrt{\frac{x^4+2\,x^2\left(y\left(x\right)\right)^2+\left(y\left(x\right)\right)^4}{x^2\left(y\left(x\right)\right)^2}}y(x)\,x+(y(x))^2-x^2\right)^{-1}+x=0\right\}$$

2.558 ODE No. 558

$$ax\sqrt{y'(x)^2+1}+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.596994 (sec), leaf count = 395

$$\left\{\text{Solve}\left[\frac{a\left(-\log\left(\frac{\left(a^2-1\right)\left(a\sqrt{a^2-\frac{y(x)^2}{x^2}-1}+a^2-\frac{iy(x)}{x}-1\right)}{a^3\left(\frac{y(x)}{x}-i\right)}\right)+\log\left(-\frac{\left(a^2-1\right)\left(a\sqrt{a^2-\frac{y(x)^2}{x^2}-1}+a^2+\frac{iy(x)}{x}-1\right)}{a^3\left(\frac{y(x)}{x}+i\right)}\right)+\log\left(\frac{y(x)^2}{x^2}\right.\right.}{2\left(a^2-1\right)}\right.\right.$$

✓ **Maple** : cpu = 1.734 (sec), leaf count = 223

$$\left\{x-\_C1\,\mathrm{e}^{\frac{1}{a}Arcsinh\left(\frac{1}{\left(a^2-1\right)x}\left(\sqrt{-a^2x^2+x^2+(y(x))^2}a+y(x)\right)\right)}\frac{1}{\sqrt{\frac{1}{(a^2-1)^2x^2}\left(-a^2x^2+a^2\left(y\left(x\right)\right)^2+2\sqrt{-a^2x^2+x^2+(y\right.}}\right.\right.$$

2.559 ODE No. 559

$$-ay(x)y'(x)-ax+y(x)\sqrt{y'(x)^2+1}=0$$

✓ **Mathematica** : cpu = 0.310445 (sec), leaf count = 212

$$\left\{\left\{y(x)\to-\frac{\sqrt{a^6\left(-x^2\right)+3a^4x^2+2a^2xe^{a^2c_1-c_1}-2xe^{a^2c_1-c_1}+e^{2a^2c_1-2c_1}-3a^2x^2+x^2}}{\sqrt{a^6-3a^4+3a^2-1}}\right\},\left\{y(x)\to\frac{\sqrt{a^6\left(-x^2\right)}\right.\right.$$

✓ **Maple** : cpu = 1.228 (sec), leaf count = 215

$$\left\{-\mathrm{e}^{\int\frac{1}{\left(a^2-1\right)y(x)}\left(-a^2x-\sqrt{\left(a^2-1\right)(y(x))^2+a^2x^2}\right)}a\left(a\sqrt{\_a^2+1}-\_a\right)\frac{1}{\sqrt{\_a^2+1}}\left(\_a\,a-\sqrt{\_a^2+1}\right)^{-1}\left(\_a^2a-\sqrt{\_a^2+1}\_a+a\right)^{-1}d\_a\ \_C1+x\right.$$

2.560 ODE No. 560

$$ay(x)\sqrt{y'(x)^2+1}-x^2-2xy(x)y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 21.2957 (sec), leaf count = 110

$$\left\{\left\{y(x)\to -\frac{\sqrt{a^2c_1^2(-x^2)-4a^2c_1x-4a^2+4x^2}}{\sqrt{a^2c_1^2-4}}\right\},\left\{y(x)\to \frac{\sqrt{a^2c_1^2(-x^2)-4a^2c_1x-4a^2+4x^2}}{\sqrt{a^2c_1^2-4}}\right\}\right\}$$

✓ **Maple** : cpu = 2.583 (sec), leaf count = 1120

$$\left\{\int_{\_b}^{x}1\left(2\_a^3-2\_a\left(y(x)\right)^2+\sqrt{a^2\left(\_a^4+2\_a^2\left(y\left(x\right)\right)^2-a^2\left(y\left(x\right)\right)^2+\left(y\left(x\right)\right)^4\right)}\right)\left(-2a^2\_a\left(y(x)\right)^2+2\_a^{5}\right.\right.$$

2.561 ODE No. 561

$$f\left(x^2+y(x)^2\right)\sqrt{y'(x)^2+1}-xy'(x)+y(x)=0$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

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```

✓ **Maple** : cpu = 5.855 (sec), leaf count = 50

$$\left\{y(x)=x\left(\tan\left(RootOf\left(-2\_Z+\int^{\frac{x^2\left(\left(\tan(\_Z)\right)^2+1\right)}{\left(\tan(\_Z)\right)^2}}\frac{f(\_a)}{\_a}\frac{1}{\sqrt{-\left(f\left(\_a\right)\right)^2+\_a}}d\_a+2\_C1\right)\right)\right)^{-1}\right\}$$

2.562 ODE No. 562

$$a\sqrt[3]{y'(x)^3+1}+bxy'(x)-y(x)=0$$

✗ **Mathematica** : cpu = 300.166 (sec), leaf count = 0 , timed out

```
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```

✓ **Maple** : cpu = 1.398 (sec), leaf count = 3306

$$\left\{\left(-\int^{\frac{1}{2b^3x^3+2a^3}}\left(2b^2x^2y(x)\sqrt[3]{-4b^6x^6-8a^3b^3x^3-4b^3x^3\left(y(x)\right)^3+4\sqrt{b^6x^6+2a^3b^3x^3+2b^3x^3\left(y(x)\right)^3+a^6-2\left(y(x)\right)^3a^3+\left(y(x)\right)^6b^3x^3-4a^6-\right.}\right.\right.\right.$$

2.563 ODE No. 563

$$ay(x)+b+xy'(x)+\log\left(y'(x)\right)=0$$

✓ **Mathematica** : cpu = 0.11443 (sec), leaf count = 59

$$\text{Solve}\left[a\left(\frac{(a+1)\log\left(1-aW\left(xe^{-ay(x)-b}\right)\right)}{a^2}+\frac{W\left(xe^{-ay(x)-b}\right)}{a}\right)+ay(x)=c_1,y(x)\right]$$

✓ **Maple** : cpu = 1.438 (sec), leaf count = 66

$$\left\{-\left(\mathrm{e}^{-ay(x)-lambertW\left(x\mathrm{e}^{-ay(x)-b}\right)-b}\right)^{-(a+1)^{-1}}\_C1+x-\frac{\mathrm{e}^{ay(x)+lambertW\left(x\mathrm{e}^{-ay(x)-b}\right)+b}}{a}=0\right\}$$

2.564 ODE No. 564

$$a\left(xy'(x)-y(x)\right)+\log\left(y'(x)\right)=0$$

✓ **Mathematica** : cpu = 0.0420405 (sec), leaf count = 28

$$\left\{\left\{y(x)\to-\frac{e^{-c_1}\left(e^{c_1}c_1-ax\right)}{a}\right\}\right\}$$

✓ **Maple** : cpu = 3.761 (sec), leaf count = 32

$$\left\{y(x)=\frac{1}{a}\left(\ln\left(-\frac{1}{ax}\right)-1\right),y(x)=\_C1\,x+\frac{\ln\left(\_C1\right)}{a}\right\}$$

2.565 ODE No. 565

$$y'(x)+y(x)\log\left(y'(x)\right)-xy(x)-y(x)\log(y(x))=0$$

✓ **Mathematica** : cpu = 0.0113203 (sec), leaf count = 25

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{2}W\left(e^x\right)^2+W\left(e^x\right)}\right\}\right\}$$

✓ **Maple** : cpu = 4.548 (sec), leaf count = 17

$$\left\{y(x)=\_C1\,\mathrm{e}^{\frac{lambertW\left(\mathrm{e}^x\right)\left(lambertW\left(\mathrm{e}^x\right)+2\right)}{2}}\right\}$$

2.566 ODE No. 566

$$y'(x) + \sin\left(y'(x)\right) - x = 0$$

✗ **Mathematica** : cpu = 0.010322 (sec), leaf count = 0 , could not solve

```
DSolve[-x + Sin[Derivative[1][y][x]] + Derivative[1][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.113 (sec), leaf count = 16

$$\left\{y(x) = \int RootOf(\_Z + \sin(\_Z) - x)\, dx + \_C1\right\}$$

2.567 ODE No. 567

$$a\cos\left(y'(x)\right) + by'(x) + x = 0$$

✗ **Mathematica** : cpu = 0.0111219 (sec), leaf count = 0 , could not solve

```
DSolve[x + a*Cos[Derivative[1][y][x]] + b*Derivative[1][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.159 (sec), leaf count = 18

$$\left\{y(x) = \int RootOf(a\cos(\_Z) + \_Z\, b + x)\, dx + \_C1\right\}$$

2.568 ODE No. 568

$$y'(x)^2 \sin\left(y'(x)\right) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0385569 (sec), leaf count = 28

$$\text{Solve}\left[\left\{x = c_1 + \text{K\$746950}\sin(\text{K\$746950}) - \cos(\text{K\$746950}), y(x) = \text{K\$746950}^2\sin(\text{K\$746950})\right\}, \{y(x), \text{K\$7469}\right.$$

✓ **Maple** : cpu = 0.106 (sec), leaf count = 32

$$\left\{x - \int^{y(x)} \left(RootOf\left(\sin(\_Z)\,\_Z^2 - \_a\right)\right)^{-1} d\_a - \_C1 = 0, y(x) = 0\right\}$$

2.569 ODE No. 569

$$\left(y'(x)^2+1\right)\sin^2\left(y(x)-xy'(x)\right)-1=0$$

✓ **Mathematica** : cpu = 0.0425298 (sec), leaf count = 59

$$\left\{\left\{y(x)\to c_1x-\frac{1}{2}\cos^{-1}\left(\frac{c_1^2-1}{c_1^2+1}\right)\right\},\left\{y(x)\to c_1x+\frac{1}{2}\cos^{-1}\left(\frac{c_1^2-1}{c_1^2+1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 2.899 (sec), leaf count = 147

$$\left\{y(x)=\_C1\,x-\arcsin\left(\frac{1}{\sqrt{\_C1^2+1}}\right),y(x)=\_C1\,x+\arcsin\left(\frac{1}{\sqrt{\_C1^2+1}}\right),y(x)=-\sqrt{1-x}\sqrt{x^{-1}}x-a\right.$$

2.570 ODE No. 570

$$\left(y'(x)^2+1\right)\left(ax+\tan^{-1}\left(y'(x)\right)\right)+y'(x)=0$$

✗ **Mathematica** : cpu = 0.10563 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] + (a*x + ArcTan[Derivative[1][y][x]])*(1 + Derivative[1][y][x]^2)
```

✓ **Maple** : cpu = 0.303 (sec), leaf count = 30

$$\left\{y(x)=\int\tan\left(RootOf\left(ax(\tan(\_Z))^2+(\tan(\_Z))^2\_Z+ax+\tan(\_Z)+\_Z\right)\right)\mathrm{d}x+\_C1\right\}$$

2.571 ODE No. 571

$$ax^nf\left(y'(x)\right)+xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.103291 (sec), leaf count = 114

$$\text{Solve}\left[\left\{y(x)=af(\text{K\$747290})x^n+\text{K\$747290}x,x=\left(nf(\text{K\$747290})^{\frac{1}{n}-1}\left(\int_1^{\text{K\$747290}}-\frac{f(K[1])^{\frac{n-1}{n}-1}}{an}\,dK[1]\right)-\right.\right.$$

✓ **Maple** : cpu = 4.12 (sec), leaf count = 169

$$\left\{[y(\_T)=a\left(\left(\frac{1}{f(\_T)\,na}\left((1-n)\int(f(\_T))^{-n^{-1}}\,\mathrm{d}\_T+\_C1\,an\right)\right)^{(n-1)^{-1}}(f(\_T))^{\frac{1}{n(n-1)}}\right)^n f(\_T)+\_T\right.$$

2.572 ODE No. 572

$$f(y'(x))\left(xy'(x)-y(x)\right)^n+y(x)g(y'(x))+xh(y'(x))=0$$

✗ **Mathematica** : cpu = 0.0303417 (sec), leaf count = 0 , could not solve

```
DSolve[x*h[Derivative[1][y][x]] + g[Derivative[1][y][x]]*y[x] + f[Derivative[1][y][x]]*(-
y[x] + x*Derivative[1][y][x])^n == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((x*diff(y(x),x)-y(x))^n*f(diff(y(x),x))+y(x)*g(diff(y(x),x))+x*h(diff(y(x),x))=0,y(x)
```

2.573 ODE No. 573

$$f\left(xy'(x)^2\right)+2xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0193922 (sec), leaf count = 42

$$\left\{\left\{y(x)\to f(c_1)-2\sqrt{c_1}\sqrt{x},y(x)\to f(c_1)+2\sqrt{c_1}\sqrt{x}\right\}\right\}$$

✓ **Maple** : cpu = 3.723 (sec), leaf count = 16

$$\left\{y(x)=f\left(\frac{\_C1^2}{4}\right)+\_C1\sqrt{x}\right\}$$

2.574 ODE No. 574

$$f\left(x-\frac{3}{2}y'(x)^2\right)+y'(x)^3-y(x)=0$$

✓ **Mathematica** : cpu = 0.0148427 (sec), leaf count = 102

$$\left\{\left\{y(x)\to\frac{1}{9}\left(9f(c_1)+2\sqrt{6}x\sqrt{x-c_1}-2\sqrt{6}c_1\sqrt{x-c_1}\right),y(x)\to\frac{1}{9}\left(9f(c_1)-2\sqrt{6}x\sqrt{x-c_1}+2\sqrt{6}c_1\sqrt{x-c_1}\right)\right\}\right.$$

✓ **Maple** : cpu = 0.508 (sec), leaf count = 41

$$\left\{y(x)=f(\_C1)-\frac{2\sqrt{6}}{9}\sqrt{(x-\_C1)^3},y(x)=f(\_C1)+\frac{2\sqrt{6}}{9}\sqrt{(x-\_C1)^3}\right\}$$

2.575 ODE No. 575

$$y'(x)f\left(xy(x)y'(x)-y(x)^2\right)+x^2\left(-y'(x)\right)+xy(x)=0$$

✗ **Mathematica** : cpu = 0.0186969 (sec), leaf count = 0 , could not solve

```
DSolve[x*y[x] - x^2*Derivative[1][y][x] + f[-y[x]^2 + x*y[x]*Derivative[1][y][x]]*Derivative
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)*f(x*y(x)*diff(y(x),x)-y(x)^2)-x^2*diff(y(x),x)+x*y(x)=0,y(x))
```

2.576 ODE No. 576

$$\phi\left(f\left(x,y(x),y'(x)\right),g\left(x,y(x),y'(x)\right)\right)=0$$

✗ **Mathematica** : cpu = 0.00712184 (sec), leaf count = 0 , could not solve

```
DSolve[phi[f[x, y[x], Derivative[1][y][x]], g[x, y[x], Derivative[1][y][x]]] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(phi(f(x,y(x),diff(y(x),x)),g(x,y(x),diff(y(x),x)))=0,y(x))
```

2.577 ODE No. 577

$$y'(x)=F\left(\frac{y(x)}{a+x}\right)$$

✓ **Mathematica** : cpu = 12.0216 (sec), leaf count = 240

$$\text{Solve}\left[\int_1^{y(x)}\left(\frac{1}{-aF\left(\frac{K[2]}{a+x}\right)-xF\left(\frac{K[2]}{a+x}\right)+K[2]}-\int_1^{x}\left(\frac{F'\left(\frac{K[2]}{K[1]+a}\right)}{(K[1]+a)\left(aF\left(\frac{K[2]}{K[1]+a}\right)+K[1]F\left(\frac{K[2]}{K[1]+a}\right)-K[2]\right)}-\right.\right.$$

✓ **Maple** : cpu = 1.804 (sec), leaf count = 28

$$\left\{y(x)=-RootOf\left(\int^{-Z}\left(F(-\_a)+\_a\right)^{-1}d\_a+\ln\left(x+a\right)+\_C1\right)(x+a)\right\}$$

2.578 ODE No. 578

$$y'(x) = F\left(y(x) - x^2\right) + 2x$$

✓ **Mathematica** : cpu = 16.3102 (sec), leaf count = 97

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(K[2]-x^2\right)\int_1^x -\frac{2K[1]F'\left(K[2]-K[1]^2\right)}{F\left(K[2]-K[1]^2\right)^2}\,dK[1]+1}{F\left(K[2]-x^2\right)}\,dK[2] + \int_1^x \left(\frac{2K[1]}{F\left(y(x)-K[1]^2\right)}+1\right)dK[1] = c_1\right.$$

✓ **Maple** : cpu = 6.828 (sec), leaf count = 22

$$\left\{y(x) = x^2 + RootOf\left(-x + \int^{\_Z} \left(F(\_a)\right)^{-1} d\_a + \_C1\right)\right\}$$

2.579 ODE No. 579

$$y'(x) = F\left(\frac{ax^2}{4} + \frac{bx}{2} + y(x)\right) - \frac{ax}{2}$$

✓ **Mathematica** : cpu = 12.6829 (sec), leaf count = 510

$$\text{Solve}\left[\int_1^{y(x)} -\frac{2F\left(K[2]+\frac{ax^2}{4}+\frac{bx}{2}\right)\int_1^x \left(\frac{2aK[1]F'\left(\frac{1}{4}aK[1]^2+\frac{1}{2}bK[1]+K[2]\right)}{\left(2F\left(\frac{1}{4}aK[1]^2+\frac{1}{2}bK[1]+K[2]\right)+b\right)^2} + \frac{2F'\left(\frac{1}{4}aK[1]^2+\frac{1}{2}bK[1]+K[2]\right)}{2F\left(\frac{1}{4}aK[1]^2+\frac{1}{2}bK[1]+K[2]\right)+b} - \frac{4F\left(\frac{1}{4}aK[1]^2+\right.}{(2}\right.\right.$$

✓ **Maple** : cpu = 4.297 (sec), leaf count = 35

$$\left\{y(x) = -\frac{ax^2}{4} - \frac{bx}{2} + RootOf\left(-x + 2\int^{\_Z} \left(2\,F(\_a)+b\right)^{-1} d\_a + \_C1\right)\right\}$$

2.580 ODE No. 580

$$y'(x) = e^{bx} F\left(e^{-bx} y(x)\right)$$

✓ **Mathematica** : cpu = 24.6479 (sec), leaf count = 200

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{1}{bK[2] - e^{bx}F\left(e^{-bx}K[2]\right)} - \int_1^x \left(\frac{F'\left(K[2]e^{-bK[1]}\right)}{e^{bK[1]}F\left(K[2]e^{-bK[1]}\right) - bK[2]} - \frac{e^{bK[1]}F\left(K[2]e^{-bK[1]}\right)\left(F'\left(K[2]\right.\right.\right.\right.\right.$$

$$\left.\left.\left.\left.\left.\left(e^{bK[1]}F\left(K[2]e^{-bK[1]}\right) -\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.504 (sec), leaf count = 31

$$\left\{ y(x) = \frac{RootOf\left(-x + \int^{-Z} (F(\_a) - \_a\, b)^{-1}\, d\_a + \_C1\right)}{\mathrm{e}^{-bx}} \right\}$$

2.581 ODE No. 581

$$y'(x) = \frac{xF\left(\frac{x^2 y(x) + \frac{1}{4}}{x^2}\right) + \frac{1}{2}}{x^3}$$

✓ **Mathematica** : cpu = 39.1376 (sec), leaf count = 141

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(\frac{x^2 K[2] + \frac{1}{4}}{x^2}\right) \int_1^x -\frac{F'\left(\frac{K[2]K[1]^2 + \frac{1}{4}}{K[1]^2}\right)}{2K[1]^3 F\left(\frac{K[2]K[1]^2 + \frac{1}{4}}{K[1]^2}\right)^2} dK[1] + 1}{F\left(\frac{x^2 K[2] + \frac{1}{4}}{x^2}\right)} dK[2] + \int_1^x \left(\frac{1}{2K[1]^3 F\left(\frac{y(x)K[1]^2 + \frac{1}{4}}{K[1]^2}\right)} + \frac{1}{K[1]^2} \right.$$

✓ **Maple** : cpu = 0.37 (sec), leaf count = 32

$$\left\{ y(x) = \frac{4\, RootOf\left(\int^{-Z} (F(\_a))^{-1}\, d\_a x + \_C1\, x + 1\right) x^2 - 1}{4\, x^2} \right\}$$

2.582 ODE No. 582

$$y'(x) = \frac{ax^2 F\left(\frac{axy(x) + 1}{ax}\right) + 1}{ax^2}$$

✓ **Mathematica** : cpu = 16.5308 (sec), leaf count = 139

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(\frac{axK[2] + 1}{ax}\right) \int_1^x \frac{F'\left(\frac{aK[1]K[2] + 1}{aK[1]}\right)}{aK[1]^2 F\left(\frac{aK[1]K[2] + 1}{aK[1]}\right)^2} dK[1] - 1}{F\left(\frac{axK[2] + 1}{ax}\right)} dK[2] + \int_1^x \left(-\frac{1}{aK[1]^2 F\left(\frac{ay(x)K[1] + 1}{aK[1]}\right)} - 1 \right) dK[\right.$$

✓ **Maple** : cpu = 1.818 (sec), leaf count = 30

$$\left\{ y(x) = \frac{RootOf\left(-x + \int^{-Z} (F(\_a))^{-1}\, d\_a + \_C1\right) ax - 1}{ax} \right\}$$

2.583 ODE No. 583

$$y'(x) = -\frac{1}{2}x\left(ax^2 - 2F\left(\frac{ax^4}{8} + y(x)\right)\right)$$

✓ **Mathematica** : cpu = 41.3362 (sec), leaf count = 123

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(K[2] + \frac{ax^4}{8}\right)\int_1^x \frac{aK[1]^3F'\left(\frac{1}{8}aK[1]^4+K[2]\right)}{2F\left(\frac{1}{8}aK[1]^4+K[2]\right)^2}\,dK[1] + 1}{F\left(K[2] + \frac{ax^4}{8}\right)}\,dK[2] + \int_1^x \left(K[1] - \frac{aK[1]^3}{2F\left(\frac{1}{8}aK[1]^4 + y(x)\right)}\right)$$

✓ **Maple** : cpu = 2.022 (sec), leaf count = 31

$$\left\{y(x) = -\frac{ax^4}{8} + RootOf\left(-x^2 + 2\int^{\_Z} (F(\_a))^{-1}\,d\_a + 2\,\_C1\right)\right\}$$

2.584 ODE No. 584

$$y'(x) = \frac{2a}{2aF\left(y(x)^2 - 4ax\right) + y(x)}$$

✓ **Mathematica** : cpu = 18.9935 (sec), leaf count = 112

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{K[2]}{4a^2F\left(K[2]^2 - 4ax\right)} - \frac{2a\int_1^x \frac{K[2]F'\left(K[2]^2-4aK[1]\right)}{aF\left(K[2]^2-4aK[1]\right)^2}\,dK[1] - 1}{2a}\right)dK[2] + \int_1^x -\frac{1}{2aF\left(y(x)^2 - 4aK[1]\right)}$$

✓ **Maple** : cpu = 5.504 (sec), leaf count = 35

$$\left\{\frac{y(x)}{2\,a} + \frac{\int^{(y(x))^2 - 4\,ax} (F(\_a))^{-1}\,d\_a}{8\,a^2} - \_C1 = 0\right\}$$

2.585 ODE No. 585

$$y'(x) = y(x)F(\log(\log(y(x))) - \log(x))$$

✓ **Mathematica** : cpu = 121.002 (sec), leaf count = 202

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{1}{K[2](xF(\log(\log(K[2])) - \log(x)) - \log(K[2]))} - \int_1^x \left(\frac{F(\log(\log(K[2])) - \log(K[1]))\left(\frac{K[1]F'(\log}{K}\right.\right.\right.}{(K[1]F(\log(\log(K[2])) - \log(K[}\right.\right.\right.$$

✓ **Maple** : cpu = 9.802 (sec), leaf count = 122

$$\left\{\int_{\_b}^{x} \frac{F(\ln(\ln(y(x))) - \ln(\_a))}{\_a\, F(\ln(\ln(y(x))) - \ln(\_a)) - \ln(y(x))}\, \mathrm{d}\_a + \int^{y(x)} -\frac{1}{\_f\ (xF(\ln(\ln(\_f))) - \ln(x)) - \ln(\_f))} - \int_{\_b}^{x} \frac{F}{}\right.$$

2.586 ODE No. 586

$$y'(x) = \frac{xF\left(\frac{y(x)}{\sqrt{x^2+1}}\right)}{\sqrt{x^2+1}}$$

✓ **Mathematica** : cpu = 158.944 (sec), leaf count = 972

$$\text{Solve}\left[\int_1^{y(x)} \left(-\frac{\sqrt{x^2+1}F\left(\frac{K[2]}{\sqrt{x^2+1}}\right)}{-x^2F\left(\frac{K[2]}{\sqrt{x^2+1}}\right)^2 - F\left(\frac{K[2]}{\sqrt{x^2+1}}\right)^2 + K[2]^2} - \int_1^x \left(\frac{K[1]\sqrt{K[1]^2+1}\left(\frac{2F\left(\frac{K[2]}{\sqrt{K[1]^2+1}}\right)F'\left(\frac{K[2]}{\sqrt{K[1]^2+1}}\right)K}{\sqrt{K[1]^2+1}}\right.\right.\right.\right.$$
$$\left.\left.\left.\left.\right.\right.\right.\right.$$
$$K[2]\left(K[1]^2F\left(\frac{K[2]}{\sqrt{K[1]^2}}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 1.078 (sec), leaf count = 39

$$\left\{y(x) = RootOf\left(-\ln(x^2+1) + 2\int^{\_Z} (F(\_a) - \_a)^{-1}\, d\_a + 2\,\_C1\right)\sqrt{x^2+1}\right\}$$

2.587 ODE No. 587

$$y'(x) = \frac{1}{2}\sqrt{x}\left(2F\left(y(x) - \frac{x^3}{6}\right) + x^{3/2}\right)$$

✓ **Mathematica** : cpu = 250.009 (sec), leaf count = 120

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(K[2]-\frac{x^3}{6}\right)\int_1^x -\frac{K[1]^2F'\left(K[2]-\frac{K[1]^3}{6}\right)}{2F\left(K[2]-\frac{K[1]^3}{6}\right)^2}dK[1]+1}{F\left(K[2]-\frac{x^3}{6}\right)}dK[2] + \int_1^x \left(\frac{K[1]^2}{2F\left(y(x)-\frac{K[1]^3}{6}\right)} + \sqrt{K[1]}\right) d$$

✓ **Maple** : cpu = 0.594 (sec), leaf count = 29

$$\left\{\int_{\_b}^{y(x)} \left(F\left(\_a - \frac{x^3}{6}\right)\right)^{-1} d\_a - \frac{2}{3}x^{\frac{3}{2}} - \_C1 = 0\right\}$$

2.588 ODE No. 588

$$y'(x) = \frac{F(-(x-y(x))(y(x)+x)) + x}{y(x)}$$

✓ **Mathematica** : cpu = 29.9456 (sec), leaf count = 110

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x -\frac{2K[1]K[2]F'(-(K[1]-K[2])(K[1]+K[2]))}{F(-(K[1]-K[2])(K[1]+K[2]))^2}dK[1] - \frac{K[2]}{F(-(x-K[2])(K[2]+x))}\right) dK[2]$$

✓ **Maple** : cpu = 0.773 (sec), leaf count = 53

$$\left\{y(x) = \sqrt{x^2 + RootOf\left(-2x + \int^{\_Z} (F(\_a))^{-1} d\_a + 2\_C1\right)}, y(x) = -\sqrt{x^2 + RootOf\left(-2x + \int^{\_Z} (F(\_\right.}$$

2.589 ODE No. 589

$$y'(x) = \frac{y(x)^2 F\left(\frac{1-y(x)\log(x)}{y(x)}\right)}{x}$$

✓ **Mathematica** : cpu = 18.9109 (sec), leaf count = 242

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{1}{K[2]^2\left(-F\left(\frac{1-\log(x)K[2]}{K[2]}\right)-1\right)} - \int_1^{x} \left(\frac{\left(-\frac{\log(K[1])}{K[2]} - \frac{1-K[2]\log(K[1])}{K[2]^2}\right)F'\left(\frac{1-K[2]\log(K[1])}{K[2]}\right)}{K[1]\left(F\left(\frac{1-K[2]\log(K[1])}{K[2]}\right)+1\right)} - \frac{\left(-\frac{\log}{}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 1.869 (sec), leaf count = 38

$$\left\{\int_{\_b}^{y(x)} \frac{1}{\_a^2}\left(F\left(\frac{1-\_a\ln(x)}{\_a}\right)+1\right)^{-1} \mathrm{d}\_a - \ln(x) - \_C1 = 0\right\}$$

2.590 ODE No. 590

$$y'(x) = \frac{x}{F\left(x^2+y(x)^2\right)-y(x)}$$

✓ **Mathematica** : cpu = 30.3355 (sec), leaf count = 91

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^{x} \frac{2K[1]K[2]F'\left(K[1]^2+K[2]^2\right)}{F\left(K[1]^2+K[2]^2\right)^2}\,dK[1] - \frac{K[2]}{F\left(K[2]^2+x^2\right)}+1\right)dK[2] + \int_1^{x} -\frac{K[1]}{F\left(K[1]^2+y(x)^2\right.}$$

✓ **Maple** : cpu = 1.005 (sec), leaf count = 28

$$\left\{-y(x) + \frac{\int^{(y(x))^2+x^2}\left(F(\_a)\right)^{-1}d\_a}{2} - \_C1 = 0\right\}$$

2.591 ODE No. 591

$$y'(x) = \frac{xF\left(\frac{ay(x)^2+bx^2}{a}\right)}{\sqrt{a}y(x)}$$

✓ **Mathematica** : cpu = 17.6914 (sec), leaf count = 250

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^{x} \left(\frac{2bK[1]K[2]F'\left(\frac{aK[2]^2+bK[1]^2}{a}\right)}{\sqrt{a}\left(\sqrt{a}F\left(\frac{aK[2]^2+bK[1]^2}{a}\right)+b\right)} - \frac{2bK[1]K[2]F\left(\frac{aK[2]^2+bK[1]^2}{a}\right)F'\left(\frac{aK[2]^2+bK[1]^2}{a}\right)}{\left(\sqrt{a}F\left(\frac{aK[2]^2+bK[1]^2}{a}\right)+b\right)^2}\right)dK[1\right.\right.\right.$$

✓ **Maple** : cpu = 2.249 (sec), leaf count = 108

$$\left\{y(x)=\frac{1}{a}\sqrt{a\left(-bx^2+RootOf\left(\int^{\_Z}\left(b\sqrt{a}+F\left(\_a\right)a\right)^{-1}d\_aba^{\frac{3}{2}}-bx^2+2\_C1\,a\right)a\right)},y(x)=-\frac{1}{a}\sqrt{a\left(-bx\right.}\right.$$

2.592 ODE No. 592

$$y'(x)=\frac{F\left(-\frac{2x^3}{5}+y(x)-2\sqrt{x}\right)+\frac{6x^3}{5}+\sqrt{x}}{x}$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.31 (sec), leaf count = 33

$$\left\{\int_{\_b}^{y(x)}\left(F\left(\_a-\frac{2\,x^3}{5}-2\,\sqrt{x}\right)\right)^{-1}\mathrm{d}\_a-\ln\left(x\right)-\_C1=0\right\}$$

2.593 ODE No. 593

$$y'(x)=\frac{e^xF\left(y(x)^{3/2}-\frac{3e^x}{2}\right)}{\sqrt{y(x)}}$$

✓ **Mathematica** : cpu = 36.6434 (sec), leaf count = 218

$$\text{Solve}\left[\int_1^{y(x)}\left(\frac{\sqrt{K[2]}}{F\left(K[2]^{3/2}-\frac{3e^x}{2}\right)-1}-\int_1^x\left(\frac{3e^{K[1]}\sqrt{K[2]}F\left(K[2]^{3/2}-\frac{3e^{K[1]}}{2}\right)F'\left(K[2]^{3/2}-\frac{3e^{K[1]}}{2}\right)}{2\left(F\left(K[2]^{3/2}-\frac{3e^{K[1]}}{2}\right)-1\right)^2}-\frac{3e^{K[1]}\sqrt{}}{2\left(F\right.}\right.\right.\right.$$

✓ **Maple** : cpu = 0.559 (sec), leaf count = 35

$$\left\{\int_{\_b}^{y(x)}1\sqrt{\_a}\left(F\left(\_a^{\frac{3}{2}}-\frac{3\,\mathrm{e}^x}{2}\right)-1\right)^{-1}\mathrm{d}\_a-\mathrm{e}^x-\_C1=0\right\}$$

2.594 ODE No. 594

$$y'(x) = \frac{xF\left(\frac{y(x)^2-b}{x^2}\right)}{y(x)}$$

✓ **Mathematica** : cpu = 17.8412 (sec), leaf count = 233

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \left(\frac{K[1]F\left(\frac{K[2]^2-b}{K[1]^2}\right)\left(2K[2]F'\left(\frac{K[2]^2-b}{K[1]^2}\right)-2K[2]\right)}{\left(K[1]^2F\left(\frac{K[2]^2-b}{K[1]^2}\right)-K[2]^2+b\right)^2} - \frac{2K[2]F'\left(\frac{K[2]^2-b}{K[1]^2}\right)}{K[1]\left(K[1]^2F\left(\frac{K[2]^2-b}{K[1]^2}\right)-K[2]^2+b\right)}\right)\right.\right.$$

✓ **Maple** : cpu = 1.821 (sec), leaf count = 67

$$\left\{y(x) = \sqrt{RootOf\left(-2\ln(x) + \int^{\_Z} \left(F\left(\_a\right)-\_a\right)^{-1} d\_a + 2\_C1\right)x^2+b}, y(x) = -\sqrt{RootOf\left(-2\ln(x)+\right.}\right.$$

2.595 ODE No. 595

$$y'(x) = \frac{F\left(\frac{xy(x)^2+1}{x}\right)}{x^2y(x)}$$

✓ **Mathematica** : cpu = 18.7222 (sec), leaf count = 201

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{K[2]}{2F\left(\frac{xK[2]^2+1}{x}\right)-1} - \int_1^x \left(\frac{4K[2]F\left(\frac{K[1]K[2]^2+1}{K[1]}\right)F'\left(\frac{K[1]K[2]^2+1}{K[1]}\right)}{K[1]^2\left(2F\left(\frac{K[1]K[2]^2+1}{K[1]}\right)-1\right)^2} - \frac{2K[2]F'\left(\frac{K[1]K[2]^2+1}{K[1]}\right)}{K[1]^2\left(2F\left(\frac{K[1]K[2]^2+1}{K[1]}\right)-1\right.}\right.\right.\right.$$

✓ **Maple** : cpu = 0.37 (sec), leaf count = 72

$$\left\{y(x) = \frac{1}{x}\sqrt{x\left(RootOf\left(\int^{\_Z}\left(-1+2F\left(\_a\right)\right)^{-1}d\_ax + \_C1\,x+1\right)x-1\right)}, y(x) = -\frac{1}{x}\sqrt{x\left(RootOf\left(\int^{\_Z}\right.\right.}\right.$$

2.596 ODE No. 596

$$y'(x) = \frac{F\left(x^2 + y(x) - x\right) - 2x^2 + x}{x}$$

✓ **Mathematica** : cpu = 227.738 (sec), leaf count = 153

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(K[2] + x^2 - x\right) \int_1^x \left(\frac{2K[1]F'\left(K[1]^2 - K[1] + K[2]\right)}{F\left(K[1]^2 - K[1] + K[2]\right)^2} - \frac{F'\left(K[1]^2 - K[1] + K[2]\right)}{F\left(K[1]^2 - K[1] + K[2]\right)^2}\right) dK[1] + 1}{F\left(K[2] + x^2 - x\right)} dK[2] + \int_1^x \left(-\right.\right.$$

✓ **Maple** : cpu = 1.519 (sec), leaf count = 26

$$\left\{y(x) = -x^2 + RootOf\left(-\ln(x) + \int^{\_Z} \left(F(\_a)\right)^{-1} d\_a + \_C1\right) + x\right\}$$

2.597 ODE No. 597

$$y'(x) = \frac{2a}{x^2\left(2aF\left(\frac{xy(x)^2 - 4a}{x}\right) - y(x)\right)}$$

✓ **Mathematica** : cpu = 25.3001 (sec), leaf count = 127

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \frac{2K[2]F'\left(\frac{K[1]K[2]^2 - 4a}{K[1]}\right)}{K[1]^2 F\left(\frac{K[1]K[2]^2 - 4a}{K[1]}\right)^2} dK[1] - \frac{K[2]}{2aF\left(\frac{xK[2]^2 - 4a}{x}\right)} + 1\right) dK[2] + \int_1^x -\frac{1}{K[1]^2 F\left(\frac{y(x)^2 K[1] - 4}{K[1]}\right.}$$

✓ **Maple** : cpu = 1.647 (sec), leaf count = 37

$$\left\{-\frac{y(x)}{2\,a} + \frac{1}{8\,a^2}\int^{(y(x))^2 - 4\,\frac{a}{x}} \left(F(\_a)\right)^{-1} d\_a - \_C1 = 0\right\}$$

2.598 ODE No. 598

$$y'(x) = \frac{F\left(\frac{y(x)}{x}\right) + y(x)}{x - 1}$$

✓ **Mathematica** : cpu = 0.0752431 (sec), leaf count = 36

$$\text{Solve}\left[\int_1^{\frac{y(x)}{x}} \frac{1}{F(K[1]) + K[1]}\, dK[1] = c_1 + \log(1 - x) - \log(x), y(x)\right]$$

✓ **Maple** : cpu = 0.781 (sec), leaf count = 29

$$\left\{y(x) = RootOf\left(-\int^{\_Z} (F(\_a) + \_a)^{-1}\, d\_a + \ln(x - 1) - \ln(x) + \_C1\right) x\right\}$$

2.599 ODE No. 599

$$y'(x) = \frac{F\left(x^2 + y(x)^2\right) - x}{y(x)}$$

✓ **Mathematica** : cpu = 22.0232 (sec), leaf count = 92

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \frac{2K[1]K[2]F'\left(K[1]^2 + K[2]^2\right)}{F\left(K[1]^2 + K[2]^2\right)^2}\, dK[1] - \frac{K[2]}{F\left(K[2]^2 + x^2\right)}\right) dK[2] + \int_1^x \left(1 - \frac{K[1]}{F\left(K[1]^2 + y(x)^2\right.}\right.$$

✓ **Maple** : cpu = 0.423 (sec), leaf count = 57

$$\left\{y(x) = \sqrt{-x^2 + RootOf\left(-2x + \int^{\_Z} \left(F\left(\_a\right)\right)^{-1} d\_a + 2\_C1\right)}, y(x) = -\sqrt{-x^2 + RootOf\left(-2x + \int^{\_Z} (F\right.}\right.$$

2.600 ODE No. 600

$$y'(x) = \frac{y(x)^2 F\left(\frac{1 - 2y(x)\log(x)}{y(x)}\right)}{x}$$

✓ **Mathematica** : cpu = 22.5319 (sec), leaf count = 243

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \left(\frac{2\left(-\frac{2\log(K[1])}{K[2]} - \frac{1 - 2K[2]\log(K[1])}{K[2]^2}\right) F'\left(\frac{1 - 2K[2]\log(K[1])}{K[2]}\right)}{K[1]\left(F\left(\frac{1 - 2K[2]\log(K[1])}{K[2]}\right) + 2\right)} - \frac{2\left(-\frac{2\log(K[1])}{K[2]} - \frac{1 - 2K[2]\log(K[1])}{K[2]^2}\right)}{K[1]\left(F\left(\frac{1-\right.}\right.}\right.$$

✓ **Maple** : cpu = 6.479 (sec), leaf count = 38

$$\left\{\int_{\_b}^{y(x)} \frac{1}{\_a^2}\left(F\left(\frac{-2\_a\ln(x)+1}{\_a}\right)+2\right)^{-1} \mathrm{d}\_a - \ln(x) - \_C1 = 0\right\}$$

2.601 ODE No. 601

$$y'(x) = \frac{xF(-(x-y(x))(y(x)+x))}{y(x)}$$

✓ **Mathematica** : cpu = 32.4683 (sec), leaf count = 187

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{K[2]}{F(-(x-K[2])(K[2]+x))-1} - \int_1^{x} \left(\frac{2K[1]K[2]F(-(K[1]-K[2])(K[1]+K[2]))F'(-(K[1]-K[2])(K[1]+K[2]))}{(F(-(K[1]-K[2])(K[1]+K[2]))-1)}\right.\right.$$

✓ **Maple** : cpu = 0.335 (sec), leaf count = 61

$$\left\{y(x) = \sqrt{x^2 + RootOf\left(-x^2 + \int^{\_Z} (F(\_a)-1)^{-1} d\_a + 2\_C1\right)}, y(x) = -\sqrt{x^2 + RootOf\left(-x^2 + \int^{\_Z} (F\right.}\right.$$

2.602 ODE No. 602

$$y'(x) = \frac{y(x)^2\left(x^2 F\left(\frac{x^2-y(x)}{x^2 y(x)}\right)+2\right)}{x^3}$$

✓ **Mathematica** : cpu = 224.967 (sec), leaf count = 164

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^{x} -\frac{2\left(-\frac{K[1]^2-K[2]}{K[1]^2K[2]^2}-\frac{1}{K[1]^2K[2]}\right)F'\left(\frac{K[1]^2-K[2]}{K[1]^2K[2]}\right)}{K[1]^3 F\left(\frac{K[1]^2-K[2]}{K[1]^2K[2]}\right)^2} dK[1] - \frac{1}{K[2]^2 F\left(\frac{x^2-K[2]}{x^2K[2]}\right)}\right) dK[2] + \int_1^{x} \left(-\right.\right.$$

✓ **Maple** : cpu = 2.294 (sec), leaf count = 33

$$\left\{y(x) = \frac{x^2}{RootOf\left(-\ln(x) - \int^{\_Z} (F(\_a))^{-1} d\_a + \_C1\right)x^2 + 1}\right\}$$

2.603 ODE No. 603

$$y'(x) = \frac{2xF(y(x)+\log(2x+1)) + F(y(x)+\log(2x+1)) - 2}{2x+1}$$

✓ **Mathematica** : cpu = 16.924 (sec), leaf count = 114

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F(K[2]+\log(2x+1))\int_1^x -\frac{2F'(K[2]+\log(2K[1]+1))}{(2K[1]+1)F(K[2]+\log(2K[1]+1))^2}\,dK[1]-1}{F(K[2]+\log(2x+1))}\,dK[2] + \int_1^x \left(\frac{}{(2K[1]+1)F(\log\right.\right.$$

✓ **Maple** : cpu = 1.204 (sec), leaf count = 27

$$\left\{y(x) = -\ln(2x+1) + RootOf\left(-x + \int^{\_Z} (F(\_a))^{-1}\,d\_a + \_C1\right)\right\}$$

2.604 ODE No. 604

$$y'(x) = \frac{2y(x)^3}{2y(x)F\left(\frac{4xy(x)^2+1}{y(x)^2}\right)+1}$$

✓ **Mathematica** : cpu = 23.1867 (sec), leaf count = 140

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \frac{\left(\frac{8K[1]}{K[2]} - \frac{2(4K[1]K[2]^2+1)}{K[2]^3}\right)F'\left(\frac{4K[1]K[2]^2+1}{K[2]^2}\right)}{F\left(\frac{4K[1]K[2]^2+1}{K[2]^2}\right)^2}\,dK[1] + \frac{1}{2K[2]^3F\left(\frac{4xK[2]^2+1}{K[2]^2}\right)} + \frac{1}{K[2]^2}\right)\,dK[2]\right.$$

✓ **Maple** : cpu = 0.512 (sec), leaf count = 30

$$\left\{-\_C1 - (y(x))^{-1} - \frac{\int^{4x+(y(x))^{-2}} (F(\_a))^{-1}\,d\_a}{4} = 0\right\}$$

2.605 ODE No. 605

$$y'(x) = -\frac{y(x)^2\left(2x - F\left(\frac{1-\frac{1}{2}xy(x)}{y(x)}\right)\right)}{4x}$$

✓ **Mathematica** : cpu = 207.679 (sec), leaf count = 142

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \frac{2\left(-\frac{K[1]}{2K[2]} - \frac{1-\frac{1}{2}K[1]K[2]}{K[2]^2}\right)F'\left(\frac{1-\frac{1}{2}K[1]K[2]}{K[2]}\right)}{F\left(\frac{1-\frac{1}{2}K[1]K[2]}{K[2]}\right)^2}\,dK[1] - \frac{4}{K[2]^2F\left(\frac{1-\frac{1}{2}xK[2]}{K[2]}\right)}\right)\,dK[2] + \int_1^x \left(\frac{1}{K\right.\right.$$

✓ **Maple** : cpu = 0.2 (sec), leaf count = 29

$$\left\{y(x) = 2\left(2\,RootOf\left(-\ln(x) - 4\int^{\_Z}(F(\_a))^{-1}\,d\_a + \_C1\right) + x\right)^{-1}\right\}$$

2.606 ODE No. 606

$$y'(x) = -x\left(-F\left(y(x) - \frac{1}{2}e^{-x^2}x^2\right) + e^{-x^2}x^2 - e^{-x^2}\right)$$

✓ **Mathematica** : cpu = 61.6913 (sec), leaf count = 358

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F\left(K[2] - \frac{1}{2}e^{-x^2}x^2\right)\int_1^x\left(\frac{e^{-K[1]^2}K[1]^3F'\left(K[2]-\frac{1}{2}e^{-K[1]^2}K[1]^2\right)}{F\left(K[2]-\frac{1}{2}e^{-K[1]^2}K[1]^2\right)^2} - \frac{e^{-K[1]^2}K[1]\left(e^{K[1]^2}F\left(K[2]-\frac{1}{2}e^{-K[1]^2}K[1]^2\right)\right.}{F\left(K[2]-\frac{1}{2}e^{-K[1]^2}K\right.}\right.}{F\left(K[2] - \frac{1}{2}e^{-x^2}x^2\right)}\right.$$

✓ **Maple** : cpu = 1.879 (sec), leaf count = 34

$$\left\{y(x) = \frac{x^2\mathrm{e}^{-x^2}}{2} + RootOf\left(x^2 - 2\int^{\_Z}(F(\_a))^{-1}\,d\_a + 2\,\_C1\right)\right\}$$

2.607 ODE No. 607

$$y'(x) = \frac{x^3F\left(\frac{y(x)}{x^2}\right) + 2y(x)}{x}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 1.092 (sec), leaf count = 22

$$\left\{y(x) = RootOf\left(-x + \int^{\_Z}(F(\_a))^{-1}\,d\_a + \_C1\right)x^2\right\}$$

2.608 ODE No. 608

$$y'(x)=\frac{\sqrt{y(x)}}{F\left(\frac{x-y(x)}{\sqrt{y(x)}}\right)+\sqrt{y(x)}}$$

✓ **Mathematica** : cpu = 298.102 (sec), leaf count = 271

$$\text{Solve}\left[\int_1^{y(x)}\left(-\int_1^x-\frac{-2\left(-\frac{K[1]-K[2]}{2K[2]^{3/2}}-\frac{1}{\sqrt{K[2]}}\right)\sqrt{K[2]}F'\left(\frac{K[1]-K[2]}{\sqrt{K[2]}}\right)-\frac{F\left(\frac{K[1]-K[2]}{\sqrt{K[2]}}\right)}{\sqrt{K[2]}}-1}{\left(-2\sqrt{K[2]}F\left(\frac{K[1]-K[2]}{\sqrt{K[2]}}\right)+K[1]-K[2]\right)^2}dK[1]-\frac{F\left(\frac{x-K[2]}{\sqrt{K[2]}}\right)}{x\sqrt{K[2]}}+\right.\right.$$

✓ **Maple** : cpu = 2.772 (sec), leaf count = 40

$$\left\{\frac{\ln\left(y(x)\right)}{2}-\int^{x\frac{1}{\sqrt{y(x)}}-\sqrt{y(x)}}\left(2\,F(\_a)-\_a\right)^{-1}d\_a-\_C1=0\right\}$$

2.609 ODE No. 609

$$y'(x)=\frac{F\left(x^3y(x)\right)-3x^2y(x)}{x^3}$$

✓ **Mathematica** : cpu = 49.5264 (sec), leaf count = 114

$$\text{Solve}\left[\int_1^{y(x)}-\frac{F\left(x^3K[2]\right)\int_1^x\left(\frac{3K[1]^5K[2]F'\left(K[1]^3K[2]\right)}{F(K[1]^3K[2])^2}-\frac{3K[1]^2}{F(K[1]^3K[2])}\right)dK[1]+x^3}{F\left(x^3K[2]\right)}dK[2]+\int_1^x\left(1-\frac{3y(x)K[1]^2}{F\left(y(x)K[1]^3\right)}\right.\right.$$

✓ **Maple** : cpu = 0.859 (sec), leaf count = 22

$$\left\{y(x)=\frac{RootOf\left(x-\int^{-Z}\left(F(\_a)\right)^{-1}d\_a+\_C1\right)}{x^3}\right\}$$

2.610 ODE No. 610

$$y'(x) = \frac{x^2 F\left(\frac{y(x)}{x}\right) + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.0585122 (sec), leaf count = 24

$$\text{Solve}\left[\int_1^{\frac{y(x)}{x}} \frac{1}{F(K[1])}\, dK[1] = c_1 + x, y(x)\right]$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 20

$$\left\{y(x) = RootOf\left(x - \int^{\_Z} (F(\_a))^{-1}\, d\_a + \_C1\right) x\right\}$$

2.611 ODE No. 611

$$y'(x) = \frac{F(x(y(x)+x)) - y(x) - 2x}{x}$$

✓ **Mathematica** : cpu = 38.1631 (sec), leaf count = 188

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F(x(K[2]+x)) \int_1^x \left(\frac{2K[1]^2 F'(K[1](K[1]+K[2]))}{F(K[1](K[1]+K[2]))^2} + \frac{K[1](K[2]-F(K[1](K[1]+K[2])))F'(K[1](K[1]+K[2]))}{F(K[1](K[1]+K[2]))^2} - \frac{1-K[}{F}\right.}{F(x(K[2]+x))}$$

✓ **Maple** : cpu = 1.11 (sec), leaf count = 28

$$\left\{y(x) = \frac{-x^2 + RootOf\left(-x + \int^{\_Z} (F(\_a))^{-1}\, d\_a + \_C1\right)}{x}\right\}$$

2.612 ODE No. 612

$$y'(x) = \frac{1}{2} e^{\frac{x^2}{4}} \left(2F\left(e^{-\frac{x^2}{4}} y(x)\right) + e^{-\frac{x^2}{4}} x y(x)\right)$$

✓ **Mathematica** : cpu = 44.808 (sec), leaf count = 196

$$\text{Solve}\left[\int_1^{y(x)} -\frac{e^{-\frac{x^2}{4}} \left(e^{\frac{x^2}{4}} F\left(e^{-\frac{x^2}{4}} K[2]\right) \int_1^x \left(\frac{e^{-\frac{1}{4}K[1]^2} K[1]}{2F\left(e^{-\frac{1}{4}K[1]^2} K[2]\right)} - \frac{e^{-\frac{1}{2}K[1]^2} K[1] K[2] F'\left(e^{-\frac{1}{4}K[1]^2} K[2]\right)}{2F\left(e^{-\frac{1}{4}K[1]^2} K[2]\right)^2}\right) dK[1] + 1\right)}{F\left(e^{-\frac{x^2}{4}} K[2]\right)} d\right.$$

✓ **Maple** : cpu = 3.195 (sec), leaf count = 27

$$\left\{y(x) = RootOf\left(-x + \int^{\_Z} (F(\_a))^{-1}\, d\_a + \_C1\right)\left(\mathrm{e}^{-\frac{x^2}{4}}\right)^{-1}\right\}$$

2.613 ODE No. 613

$$y'(x) = \frac{x^2 F\left(\frac{y(x)-x\log(x)}{x}\right) + y(x) + x}{x}$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.749 (sec), leaf count = 23

$$\left\{y(x) = \left(\ln(x) + RootOf\left(-x + \int^{\_Z} (F(\_a))^{-1}\, d\_a + \_C1\right)\right) x\right\}$$

2.614 ODE No. 614

$$y'(x) = \frac{(a-1)(a+1)x}{a^2 F\left(-\frac{1}{2}a^2x^2 + \frac{x^2}{2} + \frac{y(x)^2}{2}\right) - F\left(-\frac{1}{2}a^2x^2 + \frac{x^2}{2} + \frac{y(x)^2}{2}\right) + y(x)}$$

✓ **Mathematica** : cpu = 68.8272 (sec), leaf count = 174

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^{x} \frac{K[1]K[2]F'\left(-\frac{1}{2}a^2K[1]^2 + \frac{K[1]^2}{2} + \frac{K[2]^2}{2}\right)}{F\left(-\frac{1}{2}a^2K[1]^2 + \frac{K[1]^2}{2} + \frac{K[2]^2}{2}\right)^2}\, dK[1] + \frac{K[2]}{(a-1)(a+1)F\left(\frac{K[2]^2}{2} - \frac{1}{2}a^2x^2 + \frac{x^2}{2}\right)} +$$

✓ **Maple** : cpu = 3.014 (sec), leaf count = 60

$$\left\{\frac{y(x)}{(a-1)(a+1)} + \frac{1}{2a^4 - 4a^2 + 2}\int^{-a^2x^2+x^2+(y(x))^2} \left(F\left(\frac{\_a}{2}\right)\right)^{-1} d\_a - \_C1 = 0\right\}$$

2.615 ODE No. 615

$$y'(x) = \frac{y(x)}{x(y(x)F(xy(x)) - 1)}$$

✓ **Mathematica** : cpu = 15.4434 (sec), leaf count = 74

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \frac{F'(K[1]K[2])}{F(K[1]K[2])^2}\,dK[1] - \frac{1}{K[2]F(xK[2])} + 1\right) dK[2] + \int_1^x -\frac{1}{K[1]F(y(x)K[1])}\,dK[1] = c_1, y(\right.$$

✓ **Maple** : cpu = 1.848 (sec), leaf count = 26

$$\left\{-y(x) + \int^{xy(x)} \frac{1}{F(\_a)\,\_a} d\_a - \_C1 = 0\right\}$$

2.616 ODE No. 616

$$y'(x) = \frac{F(x(xy(x) - 1)) - 2x^3y(x) + x^2}{x^4}$$

✓ **Mathematica** : cpu = 45.11 (sec), leaf count = 174

$$\text{Solve}\left[\int_1^{y(x)} -\frac{F(x(xK[2] - 1)) \int_1^x \left(\frac{2K[2]K[1]^3F'(K[1](K[1]K[2]-1))}{F(K[1](K[1]K[2]-1))^2} - \frac{K[1]^2F'(K[1](K[1]K[2]-1))}{F(K[1](K[1]K[2]-1))^2} - \frac{2K[1]}{F(K[1](K[1]K[2]-1))}\right)}{F(x(xK[2] - 1))}\right.$$

✓ **Maple** : cpu = 1.794 (sec), leaf count = 26

$$\left\{y(x) = \frac{RootOf\left(\int^{-Z} (F(\_a))^{-1}\,d\_ax + \_C1\,x + 1\right) + x}{x^2}\right\}$$

2.617 ODE No. 617

$$y'(x) = \frac{1}{9}e^{-\frac{3x^2}{2}}xy(x)^2F\left(\frac{e^{\frac{3x^2}{2}}(y(x) + 3)}{3y(x)}\right)$$

✓ **Mathematica** : cpu = 257.676 (sec), leaf count = 612

$$\text{Solve}\left[\int_1^{y(x)}\left(-\int_1^x\left(-\frac{K[2]\left(\frac{e^{\frac{3K[1]^2}{2}}}{3K[2]}-\frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]^2}\right)K[1]F'\left(\frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]}\right)}{K[2]F\left(\frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]}\right)-9e^{\frac{3K[1]^2}{2}}K[2]-27e^{\frac{3K[1]^2}{2}}}+\frac{K[2]K[1]F\left(\frac{e^{\frac{3K[1]^2}{2}}(K[2]+3)}{3K[2]}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 1.109 (sec), leaf count = 47

$$\left\{y(x)=-3\,\frac{\mathrm{e}^{3/2\,x^2}}{\mathrm{e}^{3/2\,x^2}-3\,RootOf\left(-x^2-18\int^{-Z}\left(F\left(\_a\right)-27\,\_a\right)^{-1}d\_a+2\,\_C1\right)}\right\}$$

2.618 ODE No. 618

$$y'(x)=\frac{(y(x)+1)(x(y(x)-\log(y(x)+1)-\log(x))+1)}{xy(x)}$$

✓ **Mathematica** : cpu = 0.136872 (sec), leaf count = 25

$$\left\{\left\{y(x)\to -W\left(-\frac{e^{c_1e^x-1}}{x}\right)-1\right\}\right\}$$

✓ **Maple** : cpu = 5.764 (sec), leaf count = 34

$$\left\{y(x)=\frac{1}{x}\left(\mathrm{e}^{-lambertW\left(-\frac{\mathrm{e}^{\mathrm{e}^x\_C1-1}}{x}\right)+\mathrm{e}^x\_C1-1}-x\right)\right\}$$

2.619 ODE No. 619

$$y'(x)=\frac{6y(x)}{-F\left(-\frac{1}{3}y(x)^4-\frac{y(x)^3}{2}-y(x)^2-y(x)+x\right)+8y(x)^4+9y(x)^3+12y(x)^2+6y(x)}$$

✓ **Mathematica** : cpu = 247.316 (sec), leaf count = 327

$$\text{Solve}\left[\int_1^{y(x)}\left(-\frac{F\left(-\frac{1}{3}K[2]^4-\frac{K[2]^3}{2}-K[2]^2-K[2]+x\right)\int_1^x-\frac{6\left(-\frac{4}{3}K[2]^3-\frac{3K[2]^2}{2}-2K[2]-1\right)F'\left(-\frac{1}{3}K[2]^4-\frac{K[2]^3}{2}-K[2]^2-\right.}{F\left(-\frac{1}{3}K[2]^4-\frac{K[2]^3}{2}-K[2]^2-K[2]+K[1]\right)^2}}{F\left(-\frac{1}{3}K[2]^4-\frac{K[2]^3}{2}-K[2]^2-K[2]+x\right)}\right.\right.$$

✓ **Maple** : cpu = 2.099 (sec), leaf count = 81

$$\left\{\int_{\_b}^{y(x)} \frac{1}{\_a}\left(-8\_a^4-9\_a^3-12\_a^2+F\left(-\frac{\_a^4}{3}-\frac{\_a^3}{2}-\_a^2-\_a+x\right)-6\_a\right)\left(F\left(-\frac{\_a^4}{3}-\frac{\_a^3}{2}-\_a^2\right.\right.\right.$$

2.620 ODE No. 620

$$y'(x)=\frac{e^{2F(-(x-y(x))(y(x)+x))}+x^2+2xy(x)+y(x)^2}{-e^{2F(-(x-y(x))(y(x)+x))}+x^2+2xy(x)+y(x)^2}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 5.51 (sec), leaf count = 37

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-\_Z+\int^{\left(\mathrm{e}^{-\_Z}\right)^2-2x\mathrm{e}^{-\_Z}}\left(\mathrm{e}^{2F(\_a)}+\_a\right)^{-1}d\_a+\_C1\right)}-x\right\}$$

2.621 ODE No. 621

$$y'(x)=\frac{1}{y(x)+\sqrt{x}}$$

✓ **Mathematica** : cpu = 0.0847389 (sec), leaf count = 445

$$\left\{\left\{y(x)\to\frac{1}{\text{Root}\left[\#1^6\left(16e^{12c_1}+16x^3\right)-24\#1^4x^2+8\#1^3x^{3/2}+9\#1^2x-6\#1\sqrt{x}+1\&,1\right]}-\sqrt{x}\right\},\left\{y(x)\to\right.\right.$$

✓ **Maple** : cpu = 4.549 (sec), leaf count = 59

$$\left\{y(x)=1\left(\sqrt{x}\left(RootOf\left(\_Z^{18}\_C1-9x\_Z^6-6\sqrt{x}\_Z^3-1\right)\right)^3+1\right)\left(RootOf\left(\_Z^{18}\_C1-9x\_Z^6-6\sqrt{x}\_Z^3\right.\right.\right.$$

2.622 ODE No. 622

$$y'(x) = \frac{1}{y(x) + \sqrt{3x+1} + 2}$$

✓ **Mathematica** : cpu = 0.375107 (sec), leaf count = 134

$$\text{Solve}\left[44c_1 + 6\sqrt{33}\tanh^{-1}\left(\frac{3y(x) + 7\sqrt{3x+1} + 6}{\sqrt{33}\left(y(x) + \sqrt{3x+1} + 2\right)}\right) = 33\left(\log\left(\left(y(x) + \sqrt{3x+1} + 2\right)^2\left(\frac{1}{\left(y(x) + \sqrt{3x+1}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 2.735 (sec), leaf count = 77

$$\left\{\ln\left(\left(3\,y(x)+6\right)\sqrt{3\,x+1} + 3\left(y(x)\right)^2 - 6\,x + 12\,y(x) + 10\right) - 6\,\frac{\sqrt{3\,x+1}}{\sqrt{99\,x+33}}\,Artanh\left(\frac{3\sqrt{3\,x+1} + 6\,y(x) + 12}{\sqrt{99\,x+33}}\right)\right.$$

2.623 ODE No. 623

$$y'(x) = \frac{x^2}{x^{3/2} + y(x)}$$

✓ **Mathematica** : cpu = 0.153733 (sec), leaf count = 77

$$\text{Solve}\left[44c_1 + 6\sqrt{33}\tanh^{-1}\left(\frac{7x^{3/2} + 3y(x)}{\sqrt{33}\left(x^{3/2} + y(x)\right)}\right) = 33\left(\log\left(-\frac{3y(x)}{2x^{3/2}} - \frac{3y(x)^2}{2x^3} + 1\right) + 3\log(x)\right), y(x)\right]$$

✓ **Maple** : cpu = 3.777 (sec), leaf count = 49

$$\left\{\ln\left(3\,x^{3/2}y(x) - 2\,x^3 + 3\left(y(x)\right)^2\right) - \frac{2\sqrt{33}}{11}\,Artanh\left(\frac{\sqrt{33}}{11}\left(x^{\frac{3}{2}} + 2\,y(x)\right)x^{-\frac{3}{2}}\right) - \_C1 = 0\right\}$$

2.624 ODE No. 624

$$y'(x) = \frac{x^{5/3}}{x^{4/3} + y(x)}$$

✓ **Mathematica** : cpu = 48.9042 (sec), leaf count = 9837

✓ **Maple** : cpu = 6.144 (sec), leaf count = 46

$$\left\{y(x) = \frac{1}{2}\left(RootOf\left(\_Z^{192} + 12\,x^{4/3}\_Z^{176} + 48\,x^{8/3}\_Z^{160} + 64\,x^{4}\_Z^{144} - \_C1\right)\right)^{16} + \frac{1}{2}x^{\frac{4}{3}}\right\}$$

2.625 ODE No. 625

$$y'(x) = \frac{1}{2}ix^2\left(-2\sqrt{6y(x) - x^3} + i\right)$$

✓ **Mathematica** : cpu = 0.19656 (sec), leaf count = 76

$$\text{Solve}\left[-y(x) + \frac{1}{12}\left(2i\sqrt{6y(x) - x^3} - \log\left(-x^3 + 6y(x) + 1\right) - 2i\tan^{-1}\left(\sqrt{6y(x) - x^3}\right) - 2x^3 + 12y(x)\right) = c_1, y(\right.$$

✓ **Maple** : cpu = 4.48 (sec), leaf count = 55

$$\left\{-2\,i\sqrt{-x^3 + 6\,y\,(x)} + 2\,i\arctan\left(\sqrt{-x^3 + 6\,y\,(x)}\right) + \ln\left(-x^3 + 6\,y(x) + 1\right) + 2\,x^3 - \_C1 = 0\right\}$$

2.626 ODE No. 626

$$y'(x) = \frac{x}{\sqrt{x^2+1}+y(x)}$$

✓ **Mathematica** : cpu = 0.181083 (sec), leaf count = 104

$$\text{Solve}\left[\frac{1}{2}\left(\log\left(\frac{-\sqrt{x^2+1}y(x)^2-\left(x^2+1\right)y(x)+\left(x^2+1\right)^{3/2}}{\left(x^2+1\right)^{3/2}}\right)+\log\left(x^2+1\right)\right) = c_1 + \frac{\tanh^{-1}\left(\frac{3\sqrt{x^2+1}+y(x)}{\sqrt{5}\left(\sqrt{x^2+1}+y(x)\right.}\right.}{\sqrt{5}}\right.$$

✓ **Maple** : cpu = 7.711 (sec), leaf count = 115

$$\left\{\frac{2}{3}\ln\left(-\frac{1296}{11}\left(y(x)\sqrt{x^2+1}-x^2+(y(x))^2-1\right)\left(y(x)+\sqrt{x^2+1}\right)^{-2}\right)-\frac{4\sqrt{5}}{15}Artanh\left(\sqrt{5}\left(3\sqrt{x^2+1}+y(x)\right.\right.\right.$$

2.627 ODE No. 627

$$y'(x) = \frac{(y(x)\log(x)-1)^2}{x}$$

✓ **Mathematica** : cpu = 0.848785 (sec), leaf count = 25

$$\left\{\left\{y(x)\to\frac{\tan\left(c_1+\log(x)\right)}{\log(x)\tan\left(c_1+\log(x)\right)+1}\right\}\right\}$$

✓ **Maple** : cpu = 14.909 (sec), leaf count = 35

$$\left\{y(x) = \frac{\sin\left(\ln\left(x\right)\right)\_C1+\cos\left(\ln\left(x\right)\right)}{\left(\ln\left(x\right)+\_C1\right)\cos\left(\ln\left(x\right)\right)+\sin\left(\ln\left(x\right)\right)\left(\_C1\ \ln\left(x\right)-1\right)}\right\}$$

2.628 ODE No. 628

$$y'(x) = \frac{1}{3}x\left(3\sqrt{x^2+3y(x)}-2\right)$$

✓ **Mathematica** : cpu = 0.076933 (sec), leaf count = 33

$$\left\{\left\{y(x)\to\frac{1}{48}\left(-54c_1x^2+81c_1^2+9x^4-16x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 10.563 (sec), leaf count = 23

$$\left\{\_C1+\frac{3\,x^2}{4}+\frac{2}{3}-\sqrt{x^2+3\,y\left(x\right)}=0\right\}$$

2.629 ODE No. 629

$$y'(x) = \frac{(2y(x)\log(x) - 1)^2}{x}$$

✓ **Mathematica** : cpu = 0.701542 (sec), leaf count = 47

$$\left\{\left\{y(x) \to \frac{1}{\sqrt{2}\left(\sqrt{2}\log(x) - \tan\left(\frac{1}{2}\left(\sqrt{2}c_1 + 2\sqrt{2}\log(x)\right)\right)\right)}\right\}\right\}$$

✓ **Maple** : cpu = 20.097 (sec), leaf count = 62

$$\left\{y(x) = \frac{\sin\left(\sqrt{2}\ln(x)\right)\_C1 - \cos\left(\sqrt{2}\ln(x)\right)}{\sin\left(\sqrt{2}\ln(x)\right)\left(2\_C1\ \ln(x) + \sqrt{2}\right) + \left(\sqrt{2}\_C1 - 2\ \ln(x)\right)\cos\left(\sqrt{2}\ln(x)\right)}\right\}$$

2.630 ODE No. 630

$$y'(x) = \frac{e^{bx}}{e^{-bx}y(x) + 1}$$

✓ **Mathematica** : cpu = 0.478224 (sec), leaf count = 101

$$\text{Solve}\left[\frac{1}{2}b\left(\log\left(-be^{-2bx}y(x)^2 - be^{-bx}y(x) + 1\right) + 2bx\right) = \frac{b\tan^{-1}\left(\frac{(b+2)\left(-e^{bx}\right) - by(x)}{b\sqrt{-\frac{b+4}{b}}\left(e^{bx} + y(x)\right)}\right)}{\sqrt{-\frac{b+4}{b}}} + c_1, y(x)\right]$$

✓ **Maple** : cpu = 19.011 (sec), leaf count = 98

$$\left\{y(x) = \frac{1}{\mathrm{e}^{-bx}}\mathit{RootOf}\left(-\mathrm{e}^{\mathit{RootOf}\left(\left(\tanh\left(\frac{2\_C1\ b - 2\,bx - \_Z\sqrt{b^2+4\,b}}{2\,b}\right)\right)^2 b + 4\left(\tanh\left(1/2\,\frac{\sqrt{b^2+4\,b}\,(2\_C1\ b - 2\,bx - \_Z)}{b}\right)\right)^2 - 4\,\mathrm{e}^{-Z} - b - 4\right)} -\right.\right.$$

2.631 ODE No. 631

$$y'(x) = \frac{1}{2}x^2\left(2\sqrt{x^3 - 6y(x)} + 1\right)$$

✓ **Mathematica** : cpu = 0.0849332 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{1}{6}\left(-12c_1x^3 - 36c_1^2 - x^6 + x^3\right)\right\}\right\}$$

✓ **Maple** : cpu = 45.07 (sec), leaf count = 23

$$\left\{\_C1 - x^3 - \frac{1}{2} - \sqrt{x^3 - 6\,y\left(x\right)} = 0\right\}$$

2.632 ODE No. 632

$$y'(x) = \frac{e^x}{e^{-x}y(x) + 1}$$

✓ **Mathematica** : cpu = 0.154881 (sec), leaf count = 65

$$\text{Solve}\left[\frac{1}{2}\log\left(-e^{-2x}y(x)^2 - e^{-x}y(x) + 1\right) + x = c_1 + \frac{\tanh^{-1}\left(\frac{y(x)+3e^x}{\sqrt{5}(y(x)+e^x)}\right)}{\sqrt{5}}, y(x)\right]$$

✓ **Maple** : cpu = 11.1 (sec), leaf count = 54

$$\left\{x + \frac{\ln\left(\left(y(x)\right)^2\left(\mathrm{e}^{-x}\right)^2 + y(x)\,\mathrm{e}^{-x} - 1\right)}{2} - \frac{\sqrt{5}}{5}\mathit{Artanh}\left(\frac{2\,y(x)\,\sqrt{5}\mathrm{e}^{-x}}{5} + \frac{\sqrt{5}}{5}\right) - \_C1 = 0\right\}$$

2.633 ODE No. 633

$$y'(x) = \frac{e^{2x/3}}{e^{-2x/3}y(x) + 1}$$

✓ **Mathematica** : cpu = 0.179338 (sec), leaf count = 85

$$\text{Solve}\left[7\left(-9c_1 + 3\log\left(-\frac{2}{3}e^{-4x/3}y(x)^2 - \frac{2}{3}e^{-2x/3}y(x) + 1\right) + 4x\right) = 6\sqrt{7}\tanh^{-1}\left(\frac{y(x) + 4e^{2x/3}}{\sqrt{7}\left(y(x) + e^{2x/3}\right)}\right), y(x)\right]$$

✓ **Maple** : cpu = 14.888 (sec), leaf count = 52

$$\left\{y(x) = 1\mathit{RootOf}\left(-\mathrm{e}^{\mathit{RootOf}\left(343 - 343\left(\tanh\left(1/6\left(4\_C1 - 4\,x - 3\_Z\right)\sqrt{7}\right)\right)^2 + 98\,\mathrm{e}^{-\_Z}\right)} - 3 + 2\_Z + 2\_Z^2\right)\left(\mathrm{e}^{-\frac{2x}{3}}\right)^{-1}\right\}$$

2.634 ODE No. 634

$$y'(x) = \frac{x^5\sqrt{4x^2y(x)+1}+\frac{1}{2}}{x^3}$$

✓ **Mathematica** : cpu = 0.16889 (sec), leaf count = 33

$$\left\{\left\{y(x) \to \frac{-8c_1x^6+16c_1^2x^2+x^{10}-4}{16x^2}\right\}\right\}$$

✓ **Maple** : cpu = 10.351 (sec), leaf count = 26

$$\left\{\_C1 - \frac{1}{x}\sqrt{4\,x^2y\left(x\right)+1}+\frac{x^4}{2} = 0\right\}$$

2.635 ODE No. 635

$$y'(x) = \frac{1}{2}x\left(2\sqrt{x^3-6y(x)}+x\right)$$

✓ **Mathematica** : cpu = 0.112183 (sec), leaf count = 33

$$\left\{\left\{y(x) \to \frac{1}{24}\left(36c_1x^2-36c_1^2-9x^4+4x^3\right)\right\}\right\}$$

✓ **Maple** : cpu = 6.954 (sec), leaf count = 22

$$\left\{\_C1 - \frac{3\,x^2}{2}-\sqrt{x^3-6\,y\left(x\right)} = 0\right\}$$

2.636 ODE No. 636

$$y'(x) = y(x)\left(x^2-\log(y(x))\right)$$

✓ **Mathematica** : cpu = 0.0497345 (sec), leaf count = 24

$$\left\{\left\{y(x) \to e^{-2c_1e^{-x}+x^2-2x+2}\right\}\right\}$$

✓ **Maple** : cpu = 4.838 (sec), leaf count = 19

$$\left\{y(x) = \mathrm{e}^{\frac{-C1}{\mathrm{e}^x}+x^2-2\,x+2}\right\}$$

2.637 ODE No. 637

$$y'(x) = \frac{e^{-x^2} x}{e^{x^2} y(x) + 1}$$

✓ **Mathematica** : cpu = 15.7625 (sec), leaf count = 59

$$\text{Solve}\left[-\frac{1}{4}\log\left(2e^{2x^2}y(x)^2 + 2e^{x^2}y(x) + 1\right) - \frac{1}{2}\tan^{-1}\left(2e^{x^2}y(x) + 1\right) + \frac{x^2}{2} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 27.176 (sec), leaf count = 84

$$\left\{y(x) = -\frac{1}{e^{x^2}}\tan\left(RootOf\left(2x^2 - \ln\left(\frac{81\left(\tan\left(\_Z\right)\right)^2}{10} + \frac{81}{10}\right) + 2\ln\left(9/2\tan\left(\_Z\right) - 9/2\right) + 6\_C1 - 2\_Z\right)\right)\right\}$$

2.638 ODE No. 638

$$y'(x) = y(x)(-(\log(x) - \log(\log(y(x)))))$$

✗ **Mathematica** : cpu = 2.41724 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == -((Log[x] - Log[Log[y[x]]])*y[x]), y[x], x]
```

✓ **Maple** : cpu = 1.461 (sec), leaf count = 35

$$\left\{\int_{\_b}^{y(x)} \frac{1}{\_a\left(x\ln(x) - \ln\left(\ln\left(\_a\right)\right)x + \ln\left(\_a\right)\right)}\,d\_a + \ln(x) - \_C1 = 0\right\}$$

2.639 ODE No. 639

$$y'(x) = y(x)(\log(x) - \log(\log(y(x))))^2$$

✗ **Mathematica** : cpu = 0.306763 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == (Log[x] - Log[Log[y[x]]])^2*y[x], y[x], x]
```

✓ **Maple** : cpu = 1.004 (sec), leaf count = 50

$$\left\{\int_{\_b}^{y(x)} \frac{1}{\_a\left(x\left(\ln(x)\right)^2 - 2\ln(x)\ln\left(\ln\left(\_a\right)\right)x + \left(\ln\left(\ln\left(\_a\right)\right)\right)^2 x - \ln\left(\_a\right)\right)}\,d\_a - \ln(x) - \_C1 = 0\right\}$$

2.640 ODE No. 640

$$y'(x) = \frac{y(x)}{\log(\log(y(x))) - \log(x) + 1}$$

✗ **Mathematica** : cpu = 3.29064 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == y[x]/(1 - Log[x] + Log[Log[y[x]]]), y[x], x]
```

✓ **Maple** : cpu = 0.566 (sec), leaf count = 47

$$\left\{ \int_{\_b}^{y(x)} \frac{-\ln(\ln(\_a)) + \ln(x) - 1}{(\ln(\_a)\ln(x) - \ln(\_a)\ln(\ln(\_a)) - \ln(\_a) + x)\,\_a}\, \mathrm{d}\_a - \_C1 = 0 \right\}$$

2.641 ODE No. 641

$$y'(x) = \frac{x^4\sqrt{4x^2y(x)+1} + \frac{1}{2}}{x^3}$$

✓ **Mathematica** : cpu = 0.160206 (sec), leaf count = 35

$$\left\{ \left\{ y(x) \to \frac{-24c_1x^5 + 36c_1^2x^2 + 4x^8 - 9}{36x^2} \right\} \right\}$$

✓ **Maple** : cpu = 2.438 (sec), leaf count = 26

$$\left\{ \_C1 - \frac{1}{x}\sqrt{4\,x^2y\,(x)+1} + \frac{2\,x^3}{3} = 0 \right\}$$

2.642 ODE No. 642

$$y'(x) = \frac{\left(4ax - y(x)^2\right)^2}{y(x)}$$

✓ **Mathematica** : cpu = 0.124471 (sec), leaf count = 105

$$\left\{ \left\{ y(x) \to -\sqrt{4ax - \sqrt{2}\sqrt{a}\tanh\left(\frac{2\sqrt{2}ax - \sqrt{2}c_1}{\sqrt{a}}\right)} \right\}, \left\{ y(x) \to \sqrt{4ax - \sqrt{2}\sqrt{a}\tanh\left(\frac{2\sqrt{2}ax - \sqrt{2}c_1}{\sqrt{a}}\right)} \right\} \right\}$$

✓ **Maple** : cpu = 1.088 (sec), leaf count = 286

$$\left\{ y(x) = \sqrt{4}\sqrt{\left(\_C1\left(ax - \frac{\sqrt{2}}{4}\sqrt{a}\right)\mathrm{e}^{2x\left(\sqrt{2}\sqrt{a}-2ax\right)} + \mathrm{e}^{-2x\left(\sqrt{2}\sqrt{a}+2ax\right)}\left(ax + \frac{\sqrt{2}}{4}\sqrt{a}\right)\right)\left(\_C1\,\mathrm{e}^{2x\left(\sqrt{2}\sqrt{a}-2ax\right.}\right.} \right.$$

2.643 ODE No. 643

$$y'(x) = \frac{1}{3}x\left(3x\sqrt{x^2+3y(x)}-2\right)$$

✓ **Mathematica** : cpu = 0.105252 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{1}{12}\left(-6c_1x^3+9c_1^2+x^6-4x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.189 (sec), leaf count = 22

$$\left\{\_C1 + \frac{x^3}{2} - \sqrt{x^2+3\,y\left(x\right)} = 0\right\}$$

2.644 ODE No. 644

$$y'(x) = -\frac{1}{2}x^2\left(ax-2\sqrt{a\left(ax^4+8y(x)\right)}\right)$$

✓ **Mathematica** : cpu = 0.252213 (sec), leaf count = 34

$$\left\{\left\{y(x) \to \frac{1}{72}a\left(-96c_1x^3+144c_1^2+16x^6-9x^4\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.666 (sec), leaf count = 27

$$\left\{\_C1 + \frac{4\,ax^3}{3} - \sqrt{a\left(ax^4+8\,y\left(x\right)\right)} = 0\right\}$$

2.645 ODE No. 645

$$y'(x) = y(x)(x-\log(y(x)))$$

✓ **Mathematica** : cpu = 0.0335536 (sec), leaf count = 20

$$\left\{\left\{y(x) \to e^{-e^{c_1-x}+x-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.66 (sec), leaf count = 14

$$\left\{y(x) = \mathrm{e}^{-\frac{\_C1}{\mathrm{e}^x}-1+x}\right\}$$

2.646 ODE No. 646

$$y'(x) = \frac{\sqrt{x^3 - 6y(x)} + \frac{x^3}{2} + \frac{x^2}{2}}{x+1}$$

✓ **Mathematica** : cpu = 0.162161 (sec), leaf count = 35

$$\left\{\left\{y(x) \to \frac{1}{6}\left(18c_1 \log(x+1) - 9c_1^2 + x^3 - 9\log^2(x+1)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.467 (sec), leaf count = 23

$$\left\{\_C1 - 3\ln(1+x) - \sqrt{x^3 - 6\,y(x)} = 0\right\}$$

2.647 ODE No. 647

$$y'(x) = \frac{x\left(ay(x)^2 + bx^2\right)^2}{a^{5/2}y(x)}$$

✓ **Mathematica** : cpu = 0.370658 (sec), leaf count = 115

$$\left\{\left\{y(x) \to -\sqrt{\frac{\sqrt{b}\tan\left(\frac{a^{3/2}bx^2+2c_1}{a^{9/4}\sqrt{b}}\right)}{\sqrt[4]{a}} - \frac{bx^2}{a}}\right\}, \left\{y(x) \to \sqrt{\frac{\sqrt{b}\tan\left(\frac{a^{3/2}bx^2+2c_1}{a^{9/4}\sqrt{b}}\right)}{\sqrt[4]{a}} - \frac{bx^2}{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.461 (sec), leaf count = 460

$$\left\{y(x) = \frac{1}{a}\sqrt{-\left(\_C1\,\mathrm{e}^{\frac{x^2}{2}\left(2\sqrt{-\frac{b}{a^{3/2}}}a^{3/2}+bx^2\right)a^{-\frac{3}{2}}} + \mathrm{e}^{\frac{x^2}{2}\left(-2\sqrt{-\frac{b}{a^{3/2}}}a^{3/2}+bx^2\right)a^{-\frac{3}{2}}}\right)a\left(\left(bx^2 - \sqrt{-ba^{-\frac{3}{2}}}a^{\frac{3}{2}}\right)\mathrm{e}^{\frac{x^2}{2}\left(-2\sqrt{}\right.}\right.}\right.$$

2.648 ODE No. 648

$$y'(x) = -\frac{\sqrt{a}x^3\left(-2\sqrt{ax^4 + 8y(x)} + \sqrt{a}x + \sqrt{a}\right)}{2(x+1)}$$

✓ **Mathematica** : cpu = 0.31188 (sec), leaf count = 128

$$\left\{\left\{y(x) \to \frac{1}{72}\left(-96ac_1x^3 + 144ac_1x^2 - 288ac_1x + 288ac_1\log(x+1) + 144ac_1^2 - 432ac_1 + 16ax^6 - 48ax^5 + 123a\right.\right.\right.$$

✓ **Maple** : cpu = 0.857 (sec), leaf count = 41

$$\left\{\frac{1}{4}\sqrt{ax^4 + 8\,y(x)}\frac{1}{\sqrt{a}} - \frac{x^3}{3} + \frac{x^2}{2} - x + \ln(1+x) - \_C1 = 0\right\}$$

2.649 ODE No. 649

$$y'(x) = x\sqrt{x^2 + 8y(x) - 2x + 1} - \frac{x}{4} + \frac{1}{4}$$

✓ **Mathematica** : cpu = 0.162285 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \frac{1}{8}\left(-16c_1x^2 + 16c_1^2 + 4x^4 - x^2 + 2x - 1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.29 (sec), leaf count = 27

$$\left\{\_C1 + 2\,x^2 + \frac{1}{4} - \sqrt{x^2 - 2\,x + 1 + 8\,y\left(x\right)} = 0\right\}$$

2.650 ODE No. 650

$$y'(x) = x\sqrt{a^2 + 2ax + x^2 + 4y(x)} - \frac{a}{2} - \frac{x}{2}$$

✓ **Mathematica** : cpu = 0.22399 (sec), leaf count = 40

$$\left\{\left\{y(x) \to \frac{1}{4}\left(-a^2 - 2ax - 4c_1x^2 + 4c_1^2 + x^4 - x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.202 (sec), leaf count = 28

$$\left\{\_C1 + x^2 + \frac{1}{2} - \sqrt{x^2 + 2\,ax + a^2 + 4\,y\left(x\right)} = 0\right\}$$

2.651 ODE No. 651

$$y'(x) = \frac{y(x)\left(x^2 + \log(y(x))\right)}{x}$$

✓ **Mathematica** : cpu = 0.0321422 (sec), leaf count = 16

$$\left\{\left\{y(x) \to e^{2c_1x + x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 13

$$\left\{y(x) = \mathrm{e}^{x}\_C1\,\mathrm{e}^{x^2}\right\}$$

2.652 ODE No. 652

$$y'(x) = \frac{x\sqrt{4ax - y(x)^2} + 2a}{y(x)}$$

✓ **Mathematica** : cpu = 1.79794 (sec), leaf count = 101

$$\left\{\left\{y(x) \to -\frac{\sqrt{4096a^5x - 256a^4x^4 + 32a^2e^{c_1}x^2 - e^{2c_1}}}{32a^2}\right\}, \left\{y(x) \to \frac{\sqrt{4096a^5x - 256a^4x^4 + 32a^2e^{c_1}x^2 - e^{2c_1}}}{32a^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.181 (sec), leaf count = 27

$$\left\{-\sqrt{-\left(y\left(x\right)\right)^{2} + 4\,ax} - \frac{x^2}{2} - \_C1 = 0\right\}$$

2.653 ODE No. 653

$$y'(x) = x\sqrt{x^2 + 4y(x) - 4x} - \frac{x}{2} + 1$$

✓ **Mathematica** : cpu = 0.167963 (sec), leaf count = 34

$$\left\{\left\{y(x) \to \frac{1}{4}\left(-4c_1x^2 + 4c_1^2 + x^4 - x^2 + 4x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.162 (sec), leaf count = 24

$$\left\{\_C1 + x^2 + \frac{1}{2} - \sqrt{x^2 - 4\,x + 4\,y\left(x\right)} = 0\right\}$$

2.654 ODE No. 654

$$y'(x) = \frac{\sqrt{x^2 + 3y(x)} - \frac{2x^2}{3} - \frac{2x}{3}}{x + 1}$$

✓ **Mathematica** : cpu = 0.149856 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \frac{1}{12}\left(-18c_1\log(x+1) + 9c_1^2 - 4x^2 + 9\log^2(x+1)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.207 (sec), leaf count = 23

$$\left\{\_C1 + \frac{3\,\ln\left(1 + x\right)}{2} - \sqrt{x^2 + 3\,y\left(x\right)} = 0\right\}$$

2.655 ODE No. 655

$$y'(x) = \frac{e^{-4x/3} y(x)^3}{e^{-2x/3} y(x) + 1}$$

✓ **Mathematica** : cpu = 19.9667 (sec), leaf count = 82

$$\text{Solve}\left[\frac{3}{2}\log(y(x)) + \frac{1}{28}\left(-21\log\left(-3y(x)^2 + 2e^{2x/3}y(x) + 2e^{4x/3}\right) + 6\sqrt{7}\tanh^{-1}\left(\frac{y(x) + 2e^{2x/3}}{\sqrt{7}y(x)}\right) + 28x\right) = c_1\right.$$

✓ **Maple** : cpu = 1.842 (sec), leaf count = 66

$$\left\{x + \frac{3}{2}\ln\left(y(x)\,\mathrm{e}^{-\frac{2x}{3}}\right) - \frac{3}{4}\ln\left(3\,(y(x))^2\left(\mathrm{e}^{-2/3\,x}\right)^2 - 2\,y(x)\,\mathrm{e}^{-2/3\,x} - 2\right) + \frac{3\sqrt{7}}{14}\mathit{Artanh}\left(\frac{3\,y(x)\sqrt{7}}{7}\mathrm{e}^{-\frac{2x}{3}} - \frac{\sqrt{7}}{7}\right.\right.$$

2.656 ODE No. 656

$$y'(x) = \frac{y(x)\left(x^3 + \log(y(x))\right)}{x}$$

✓ **Mathematica** : cpu = 0.0368789 (sec), leaf count = 20

$$\left\{\left\{y(x) \to e^{3c_1 x + \frac{x^3}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 15

$$\left\{y(x) = \mathrm{e}^{\frac{x^3}{2}}\mathrm{e}^{x}\_C1\right\}$$

2.657 ODE No. 657

$$y'(x) = x^2\sqrt{x^2 + 8y(x) - 2x + 1} - \frac{x}{4} + \frac{1}{4}$$

✓ **Mathematica** : cpu = 0.171067 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \frac{1}{72}\left(-96c_1x^3 + 144c_1^2 + 16x^6 - 9x^2 + 18x - 9\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.326 (sec), leaf count = 26

$$\left\{\_C1 + \frac{4\,x^3}{3} - \sqrt{x^2 - 2\,x + 1 + 8\,y\,(x)} = 0\right\}$$

2.658 ODE No. 658

$$y'(x) = \frac{\sqrt{x^2+8y(x)-2x+1} - \frac{x^2}{4} + \frac{1}{4}}{x+1}$$

✓ **Mathematica** : cpu = 0.223253 (sec), leaf count = 45

$$\left\{\left\{y(x) \to \frac{1}{8}\left(-32c_1 \log(4(x+1)) + 16c_1^2 - x^2 + 2x + 16\log^2(4(x+1)) - 1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.279 (sec), leaf count = 28

$$\left\{\_C1 + 4\ln(1+x) - \frac{1}{4} - \sqrt{x^2 - 2x + 1 + 8y(x)} = 0\right\}$$

2.659 ODE No. 659

$$y'(x) = x\sqrt{a^2x^2 + 2abx + 4ay(x) + b^2 - 4c} - \frac{ax}{2} - \frac{b}{2}$$

✓ **Mathematica** : cpu = 0.403828 (sec), leaf count = 60

$$\left\{\left\{y(x) \to \frac{-4a^2c_1x^2 + 4a^2c_1^2 + a^2x^4 - a^2x^2 - 2abx - b^2 + 4c}{4a}\right\}\right\}$$

✓ **Maple** : cpu = 0.441 (sec), leaf count = 41

$$\left\{\_C1 + ax^2 + \frac{a}{2} - \sqrt{a^2x^2 + 2abx + b^2 + 4ay(x) - 4c} = 0\right\}$$

2.660 ODE No. 660

$$y'(x) = x^2\sqrt{a^2 + 2ax + x^2 + 4y(x)} - \frac{a}{2} - \frac{x}{2}$$

✓ **Mathematica** : cpu = 0.242348 (sec), leaf count = 42

$$\left\{\left\{y(x) \to \frac{1}{36}\left(-9a^2 - 18ax - 24c_1x^3 + 36c_1^2 + 4x^6 - 9x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.293 (sec), leaf count = 29

$$\left\{\_C1 + \frac{2x^3}{3} - \sqrt{x^2 + 2ax + a^2 + 4y(x)} = 0\right\}$$

2.661 ODE No. 661

$$y'(x) = x^2\sqrt{a^2x^2+2abx+4ay(x)+b^2-4c} - \frac{ax}{2} - \frac{b}{2}$$

✓ **Mathematica** : cpu = 0.383569 (sec), leaf count = 61

$$\left\{\left\{y(x) \to \frac{-24a^2c_1x^3+36a^2c_1^2+4a^2x^6-9a^2x^2-18abx-9b^2+36c}{36a}\right\}\right\}$$

✓ **Maple** : cpu = 0.214 (sec), leaf count = 39

$$\left\{\_C1 + \frac{2\,ax^3}{3} - \sqrt{a^2x^2+2\,abx+b^2+4\,ay\left(x\right)-4\,c} = 0\right\}$$

2.662 ODE No. 662

$$y'(x) = x^2\sqrt{x^2-4y(x)+2x+1} + \frac{x}{2} + \frac{1}{2}$$

✓ **Mathematica** : cpu = 0.176524 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \frac{1}{36}\left(24c_1x^3-36c_1^2-4x^6+9x^2+18x+9\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.183 (sec), leaf count = 26

$$\left\{\_C1 - \frac{2\,x^3}{3} - \sqrt{x^2+2\,x+1-4\,y\left(x\right)} = 0\right\}$$

2.663 ODE No. 663

$$y'(x) = \frac{x^2\sqrt{4ax-y(x)^2}+2a}{y(x)}$$

✓ **Mathematica** : cpu = 2.17355 (sec), leaf count = 101

$$\left\{\left\{y(x) \to -\frac{\sqrt{147456a^7x-4096a^6x^6+128a^3e^{c_1}x^3-e^{2c_1}}}{192a^3}\right\}, \left\{y(x) \to \frac{\sqrt{147456a^7x-4096a^6x^6+128a^3e^{c_1}x^3-}}{192a^3}\right.\right.$$

✓ **Maple** : cpu = 0.17 (sec), leaf count = 27

$$\left\{-\sqrt{-\left(y\left(x\right)\right)^2+4\,ax} - \frac{x^3}{3} - \_C1 = 0\right\}$$

2.664 ODE No. 664

$$y'(x) = x^2\sqrt{x^2+4y(x)-4x} - \frac{x}{2} + 1$$

✓ **Mathematica** : cpu = 0.175042 (sec), leaf count = 36

$$\left\{\left\{y(x) \to \frac{1}{36}\left(-24c_1x^3 + 36c_1^2 + 4x^6 - 9x^2 + 36x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.164 (sec), leaf count = 25

$$\left\{\_C1 + \frac{2\,x^3}{3} - \sqrt{x^2 - 4\,x + 4\,y\left(x\right)} = 0\right\}$$

2.665 ODE No. 665

$$y'(x) = -\frac{\sqrt{a}\left(-2\sqrt{ax^4+8y(x)} + \sqrt{a}x^4 + \sqrt{a}x^3\right)}{2(x+1)}$$

✓ **Mathematica** : cpu = 0.245619 (sec), leaf count = 41

$$\left\{\left\{y(x) \to \frac{1}{8}\left(-32ac_1\log(x+1) + 16ac_1^2 - ax^4 + 16a\log^2(x+1)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.52 (sec), leaf count = 28

$$\left\{-\frac{1}{4}\sqrt{ax^4+8\,y\left(x\right)}\frac{1}{\sqrt{a}} + \ln\left(1+x\right) - \_C1 = 0\right\}$$

2.666 ODE No. 666

$$y'(x) = y(x)\left(x^3 + x^2 - \log(y(x)) + 1\right)$$

✓ **Mathematica** : cpu = 0.0672097 (sec), leaf count = 29

$$\left\{\left\{y(x) \to e^{-c_1e^{-x}+x^3-2x^2+4x-3}\right\}\right\}$$

✓ **Maple** : cpu = 0.146 (sec), leaf count = 24

$$\left\{y(x) = \mathrm{e}^{-\frac{\_C1}{\mathrm{e}^x}+x^3-2\,x^2+4\,x-3}\right\}$$

2.667 ODE No. 667

$$y'(x) = \frac{e^{-2bx} y(x)^3}{e^{-bx} y(x) + 1}$$

✓ **Mathematica** : cpu = 0.945095 (sec), leaf count = 90

$$\text{Solve}\left[\frac{\log(y(x))}{b} + \frac{1}{2}\left(-\frac{\log\left(y(x)^2 - be^{bx}\left(e^{bx} + y(x)\right)\right)}{b} + \frac{2\tanh^{-1}\left(\frac{\sqrt{\frac{b}{b+4}}\left(2e^{bx} + y(x)\right)}{y(x)}\right)}{\sqrt{b}\sqrt{b+4}} + 2x\right) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.305 (sec), leaf count = 82

$$\left\{bx - bArtanh\left(\left(-2\,y(x)\,\mathrm{e}^{-bx} + b\right)\frac{1}{\sqrt{b^2+4\,b}}\right)\frac{1}{\sqrt{b^2+4\,b}} + \ln\left(y(x)\,\mathrm{e}^{-bx}\right) - \frac{\ln\left(-by(x)\,\mathrm{e}^{-bx} + (y(x))^2\left(\mathrm{e}^{-bx}\right)^2 -\right.}{2}\right.$$

2.668 ODE No. 668

$$y'(x) = \frac{e^{-2x} y(x)^3}{e^{-x} y(x) + 1}$$

✓ **Mathematica** : cpu = 0.509192 (sec), leaf count = 78

$$\text{Solve}\left[\log(y(x)) + y(x)^2\left(\frac{x}{y(x)^2} - \frac{\log\left(-y(x)^2 + e^x y(x) + e^{2x}\right)}{2y(x)^2} + \frac{\tanh^{-1}\left(\frac{y(x)+2e^x}{\sqrt{5}y(x)}\right)}{\sqrt{5}y(x)^2}\right) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 1.044 (sec), leaf count = 58

$$\left\{y(x) = \mathrm{e}^{RootOf\left(2\sqrt{5}Artanh\left(1/5\,\frac{\left(-2\,\mathrm{e}^{-Z}+\mathrm{e}^{x}\right)\sqrt{5}}{\mathrm{e}^{x}}\right)+5\,\ln\left(-\left(\mathrm{e}^{x}\right)^2-\mathrm{e}^{-Z+x}+\left(\mathrm{e}^{-Z}\right)^2\right)+10\_C1-10\_Z-10\,x\right)}\right\}$$

2.669 ODE No. 669

$$y'(x) = \frac{e^x \left(3e^x - 2y(x)^{3/2}\right)^2}{4\sqrt{y(x)}}$$

✓ **Mathematica** : cpu = 0.784893 (sec), leaf count = 264

$$\left\{\left\{y(x) \to \frac{\left(3e^{3c_1+x} + 2e^{3c_1} - 2e^{3e^x} + 3e^{x+3e^x}\right)^{2/3}}{\sqrt[3]{8e^{3c_1+3e^x} + 4e^{6c_1} + 4e^{6e^x}}}\right\}, \left\{y(x) \to -\frac{\sqrt[3]{-1}\left(3e^{3c_1+x} + 2e^{3c_1} - 2e^{3e^x} + 3e^{x+3e^x}\right)^{2/3}}{\sqrt[3]{8e^{3c_1+3e^x} + 4e^{6c_1} + 4e^{6e^x}}}\right\}\right\}$$

✓ **Maple** : cpu = 1.24 (sec), leaf count = 72

$$\left\{\_C1 + 1\mathrm{e}^{-\frac{3\,\mathrm{e}^x}{2} - \frac{9\,\mathrm{e}^{2\,x}}{8}} \left(2\left(y(x)\right)^{3/2}\mathrm{e}^x - 2\,\mathrm{e}^x - 3\,\mathrm{e}^{2\,x}\right)\left(\mathrm{e}^{\frac{3\,\mathrm{e}^x}{2} - \frac{9\,\mathrm{e}^{2\,x}}{8}}\right)^{-1}\left(2\left(y(x)\right)^{3/2}\mathrm{e}^x + 2\,\mathrm{e}^x - 3\,\mathrm{e}^{2\,x}\right)^{-1} = 0\right\}$$

2.670 ODE No. 670

$$y'(x) = \frac{1}{2}ixy(x)\left(-2\sqrt{4\log(a) - x^2 + 4\log(y(x))} + i\right)$$

✓ **Mathematica** : cpu = 0.338578 (sec), leaf count = 99

$$\text{Solve}\left[-\log(y(x)) + \frac{1}{4}\left(-\frac{1}{2}\log\left(4\log(a) - x^2 + 4\log(y(x)) + 1\right) + i\sqrt{4\log(a) - x^2 + 4\log(y(x))} - i\tan^{-1}\left(\sqrt{4\right.\right.\right.$$

✓ **Maple** : cpu = 1.01 (sec), leaf count = 70

$$\left\{-\frac{1}{2}\sqrt{-x^2 + 4\,\ln(a) + 4\,\ln\left(y\left(x\right)\right)} + \frac{1}{2}\arctan\left(\sqrt{-x^2 + 4\,\ln(a) + 4\,\ln\left(y\left(x\right)\right)}\right) - \frac{i}{4}\ln\left(x^2 - 4\,\ln(a) - 4\,\ln(y(x\right.\right.\right.$$

2.671 ODE No. 671

$$y'(x) = \frac{\left(xy(x)^2 + 1\right)^2}{x^4 y(x)}$$

✓ **Mathematica** : cpu = 0.366013 (sec), leaf count = 192

$$\left\{\left\{y(x) \to -\frac{\sqrt{\sqrt{2}e^{\frac{2\sqrt{2}(c_1x+1)}{x}} - \frac{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}}}{x} - \frac{2}{x} - \sqrt{2}}}{\sqrt{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}} + 2}}\right\}, \left\{y(x) \to \frac{\sqrt{\sqrt{2}e^{\frac{2\sqrt{2}(c_1x+1)}{x}} - \frac{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}}}{x} - \frac{2}{x} - \sqrt{2}}}{\sqrt{2e^{\frac{2\sqrt{2}(c_1x+1)}{x}} + 2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.832 (sec), leaf count = 231

$$\left\{y(x)=-\frac{1}{2\,x}\sqrt{-2\,x\left(\_C1\,\mathrm{e}^{\frac{-1-\sqrt{2}x}{x^2}}+\mathrm{e}^{\frac{-1+\sqrt{2}x}{x^2}}\right)\left(\_C1\,\left(\sqrt{2}x+2\right)\mathrm{e}^{\frac{-1-\sqrt{2}x}{x^2}}+\left(2-\sqrt{2}x\right)\mathrm{e}^{\frac{-1+\sqrt{2}x}{x^2}}\right)\left(\_C1\,\mathrm{e}^{\frac{-1-}{x^2}}\right.}\right.$$

2.672 ODE No. 672

$$y'(x)=\frac{x^2\left(\sqrt{4y(x)^3-9x^4}+3x\right)}{y(x)^2}$$

✗ **Mathematica** : cpu = 300.054 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.458 (sec), leaf count = 36

$$\left\{\int_{\_b}^{y(x)}\_a^2\frac{1}{\sqrt{-9\,x^4+4\,\_a^3}}\,\mathrm{d}\_a-\frac{x^3}{3}-\_C1=0\right\}$$

2.673 ODE No. 673

$$y'(x)=\frac{\frac{1}{2}x^2\cos(2y(x))+\frac{x^2}{2}-\frac{1}{2}\sin(2y(x))}{x}$$

✓ **Mathematica** : cpu = 0.0738995 (sec), leaf count = 23

$$\left\{\left\{y(x)\to\tan^{-1}\left(\frac{3c_1+2x^3}{6x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 1.068 (sec), leaf count = 17

$$\left\{y(x)=\arctan\left(\frac{x^3+6\,\_C1}{3\,x}\right)\right\}$$

2.674 ODE No. 674

$$y'(x) = \frac{\sqrt{x^2+4y(x)-4x} - \frac{x^2}{2} + \frac{x}{2} + 1}{x+1}$$

✓ **Mathematica** : cpu = 0.211595 (sec), leaf count = 40

$$\left\{\left\{y(x) \to \frac{1}{4}\left(-8c_1 \log(x+1) + 4c_1^2 - x^2 + 4x + 4\log^2(x+1)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.276 (sec), leaf count = 27

$$\left\{\_C1 + 2\ln(1+x) - 1 - \sqrt{x^2 - 4x + 4y(x)} = 0\right\}$$

2.675 ODE No. 675

$$y'(x) = \frac{ax^4 + ae^x x^3 + ax^3 - x^2 y(x)^2 - e^x x y(x)^2 - x y(x)^2 + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.0495246 (sec), leaf count = 48

$$\left\{\left\{y(x) \to \sqrt{a}x \tanh\left(\frac{1}{6}\sqrt{a}\left(6c_1 + 2x^3 + 3x^2 + 6e^x x - 6e^x\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 37

$$\left\{y(x) = \tanh\left(\frac{(6x-6)\,\mathrm{e}^x + 2x^3 + 3x^2 + 6\_C1}{6}\sqrt{a}\right)x\sqrt{a}\right\}$$

2.676 ODE No. 676

$$y'(x) = \frac{x^6\sqrt{4x^2y(x)+1} + \frac{x}{2} + \frac{1}{2}}{x^3(x+1)}$$

✓ **Mathematica** : cpu = 0.291992 (sec), leaf count = 144

$$\left\{\left\{y(x) \to \frac{-72c_1x^6 + 96c_1x^5 - 144c_1x^4 + 288c_1x^3 + 144c_1^2x^2 - 288c_1x^2\log(x+1) + 9x^{10} - 24x^9 + 52x^8 - 120x\right.\right.$$

✓ **Maple** : cpu = 0.626 (sec), leaf count = 43

$$\left\{\_C1 + 2\ln(1+x) - \frac{1}{x}\sqrt{4x^2y(x)+1} - 2x + x^2 - \frac{2x^3}{3} + \frac{x^4}{2} = 0\right\}$$

2.677 ODE No. 677

$$y'(x) = \frac{ax^4 + ax^3 + ax^3 \log(x+1) - x^2 y(x)^2 - xy(x)^2 + y(x) - xy(x)^2 \log(x+1)}{x}$$

✓ **Mathematica** : cpu = 0.0315925 (sec), leaf count = 80

$$\left\{\left\{y(x) \to \sqrt{a}x \tanh\left(\frac{1}{12}\left(12\sqrt{a}c_1 + 4\sqrt{a}x^3 + 3\sqrt{a}x^2 + 6\sqrt{a}x^2 \log(x+1) + 6\sqrt{a}x - 6\sqrt{a}\log(x+1)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 48

$$\left\{y(x) = \tanh\left(\frac{6\,\ln(1+x)\,x^2 + 4\,x^3 + 3\,x^2 - 6\,\ln(1+x) + 12\,\_C1 + 6\,x + 9}{12}\sqrt{a}\right) x\sqrt{a}\right\}$$

2.678 ODE No. 678

$$y'(x) = \frac{x^2\left(2x\sqrt{x^3 - 6y(x)} + x + 1\right)}{2(x+1)}$$

✓ **Mathematica** : cpu = 0.224884 (sec), leaf count = 101

$$\left\{\left\{y(x) \to \frac{1}{24}\left(24c_1x^3 - 36c_1x^2 + 72c_1x - 72c_1\log(x+1) - 36c_1^2 - 4x^6 + 12x^5 - 33x^4 + 40x^3 + 24x^3\log(x+1)\right.\right.\right.$$

✓ **Maple** : cpu = 0.277 (sec), leaf count = 37

$$\left\{\_C1 - x^3 + \frac{3\,x^2}{2} - 3\,x + 3\,\ln(1+x) - \frac{1}{2} - \sqrt{x^3 - 6\,y(x)} = 0\right\}$$

2.679 ODE No. 679

$$y'(x) = \frac{x^4 + x^3 + x^3\log(x) + 7x^2y(x)^2 + 7xy(x)^2 + y(x) + 7xy(x)^2\log(x)}{x}$$

✓ **Mathematica** : cpu = 0.0294534 (sec), leaf count = 59

$$\left\{\left\{y(x) \to \frac{x\tan\left(\frac{1}{12}\left(12\sqrt{7}c_1 + 4\sqrt{7}x^3 + 3\sqrt{7}x^2 + 6\sqrt{7}x^2\log(x)\right)\right)}{\sqrt{7}}\right\}\right\}$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 37

$$\left\{y(x) = \frac{x\sqrt{7}}{7}\tan\left(\frac{\left(6\,x^2\ln(x) + 4\,x^3 + 3\,x^2 + 12\,\_C1\right)\sqrt{7}}{12}\right)\right\}$$

2.680 ODE No. 680

$$y'(x) = \frac{\sqrt{x^2 - 4y(x) + 2x + 1} + \frac{x^2}{2} + x + \frac{1}{2}}{x + 1}$$

✓ **Mathematica** : cpu = 0.212587 (sec), leaf count = 39

$$\left\{\left\{y(x) \to \frac{1}{4}\left(8c_1 \log(x+1) - 4c_1^2 + x^2 + 2x - 4\log^2(x+1) + 1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.259 (sec), leaf count = 28

$$\left\{\_C1 - 2\ln(1+x) - \frac{1}{2} - \sqrt{x^2 + 2x + 1 - 4y(x)} = 0\right\}$$

2.681 ODE No. 681

$$y'(x) = \frac{ax^2 y(x)^2 + axy(x)^2 \log\left(\frac{1}{x}\right) + bx^4 + bx^3 + bx^3 \log\left(\frac{1}{x}\right) + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.0403152 (sec), leaf count = 84

$$\left\{\left\{y(x) \to \frac{\sqrt{b}x \tan\left(\frac{1}{12}\left(12\sqrt{a}\sqrt{b}c_1 + 4\sqrt{a}\sqrt{b}x^3 + 9\sqrt{a}\sqrt{b}x^2 - 6\sqrt{a}\sqrt{b}x^2\log(x)\right)\right)}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 45

$$\left\{y(x) = \frac{x}{a}\tan\left(\frac{4x^3 + 6x^2\ln\left(x^{-1}\right) + 9x^2 + 12\_C1}{12}\sqrt{ab}\right)\sqrt{ab}\right\}$$

2.682 ODE No. 682

$$y'(x) = \frac{2a}{x\left(-8a^2 + 2axy(x)^2 - xy(x)\right)}$$

✓ **Mathematica** : cpu = 0.0821567 (sec), leaf count = 39

$$\text{Solve}\left[\frac{y(x)^2 e^{-4ay(x)}}{8a} - \frac{e^{-4ay(x)}}{2x} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.395 (sec), leaf count = 28

$$\left\{\_C1 + \frac{-x(y(x))^2 + 4a}{\mathrm{e}^{4ay(x)}x} = 0\right\}$$

2.683 ODE No. 683

$$y'(x) = \frac{y(x)\left(x^4 y(x)\log(x(x+1)) - x^3\log(x(x+1)) - 1\right)}{x}$$

✓ **Mathematica** : cpu = 0.34649 (sec), leaf count = 84

$$\left\{\left\{y(x) \to \frac{e^{\frac{2x^3}{9}+\frac{x}{3}}}{c_1 e^{\frac{x^2}{6}} x \sqrt[3]{x+1}(x(x+1))^{\frac{x^3}{3}} + e^{\frac{x^2}{6}+\frac{1}{18}(4x^2-3x+6)x} x}\right\}\right\}$$

✓ **Maple** : cpu = 0.299 (sec), leaf count = 152

$$\left\{y(x) = \frac{1}{x}(x(1+x))^{-\frac{x^3}{3}} \mathrm{e}^{\frac{2x^3}{9}} \mathrm{e}^{-\frac{x^2}{6}} \mathrm{e}^{\frac{x}{3}} \left(x^{-\frac{x^3}{3}}(1+x)^{-\frac{x^3}{3}} \mathrm{e}^{\frac{x}{6}\left(ix^2\pi\left(csgn(ix(1+x))\right)^3 - ix^2(csgn(ix)+csgn(i+ix))\pi\left(csgn(ix(1+x)\right)\right.\right.\right.$$

2.684 ODE No. 684

$$y'(x) = \frac{x^2\sqrt{x^2+y(x)^2}+y(x)}{x}$$

✓ **Mathematica** : cpu = 0.0231078 (sec), leaf count = 20

$$\left\{\left\{y(x) \to x\sinh\left(\frac{1}{2}\left(2c_1+x^2\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 3.328 (sec), leaf count = 30

$$\left\{\ln\left(\sqrt{(y(x))^2+x^2}+y(x)\right) - \frac{x^2}{2} - \ln(x) - \_C1 = 0\right\}$$

2.685 ODE No. 685

$$y'(x) = \frac{x^3\log((x-1)(x+1)) + y(x) + 7xy(x)^2\log((x-1)(x+1))}{x}$$

✓ **Mathematica** : cpu = 0.0339459 (sec), leaf count = 87

$$\left\{\left\{y(x) \to \frac{x\tan\left(\frac{1}{2}\left(2\sqrt{7}c_1 - \sqrt{7}x^2 + \sqrt{7}x^2\log(x-1) + \sqrt{7}x^2\log(x+1) - \sqrt{7}\log(1-x) - \sqrt{7}\log(x+1)\right)\right)}{\sqrt{7}}\right\}\right\}$$

✓ **Maple** : cpu = 0.116 (sec), leaf count = 48

$$\left\{y(x) = \frac{x\sqrt{7}}{7}\tan\left(\frac{\left(x^2\ln((1+x)(x-1)) - x^2 - \ln((1+x)(x-1)) + 2\_C1 + 1\right)\sqrt{7}}{2}\right)\right\}$$

2.686 ODE No. 686

$$y'(x) = \frac{e^{2x^2} x y(x)^3}{e^{x^2} y(x) + 1}$$

✓ **Mathematica** : cpu = 15.6662 (sec), leaf count = 68

$$\text{Solve}\left[\log(y(x)) - 2y(x)^2 \left(\frac{\log\left(e^{2x^2} y(x)^2 + 2e^{x^2} y(x) + 2\right)}{4y(x)^2} - \frac{\tan^{-1}\left(e^{x^2} y(x) + 1\right)}{2y(x)^2}\right) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 3.229 (sec), leaf count = 85

$$\left\{y(x) = \frac{1}{\mathrm{e}^{x^2}}\left(1 - \tan\left(RootOf\left(-2x^2 - \ln\left(\frac{81\left(\tan\left(\_Z\right)\right)^2}{10} + \frac{81}{10}\right) + 2\ln\left(9/2\tan\left(\_Z\right) - 9/2\right) + 6\_C1 - 2\right.\right.\right.\right.$$

2.687 ODE No. 687

$$y'(x) = \frac{x^3\left(-\log\left(\frac{x+1}{x-1}\right)\right) + y(x) + x y(x)^2 \log\left(\frac{x+1}{x-1}\right)}{x}$$

✓ **Mathematica** : cpu = 0.0571978 (sec), leaf count = 130

$$\left\{\left\{y(x) \to \frac{-x^2(x+1)^{x^2} e^{2c_1+2x} + x(x+1)^{x^2} e^{2c_1+2x} - x^2(x-1)^{x^2} - x(x-1)^{x^2}}{-(x+1)^{x^2} e^{2c_1+2x} + x(x+1)^{x^2} e^{2c_1+2x} - x(x-1)^{x^2} - (x-1)^{x^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.193 (sec), leaf count = 39

$$\left\{y(x) = -\tanh\left(\frac{x^2}{2}\ln\left(\frac{1+x}{x-1}\right) - \frac{1}{2}\ln\left(\frac{1+x}{x-1}\right) + \_C1 + x - 1\right)x\right\}$$

2.688 ODE No. 688

$$y'(x) = \frac{e^{\frac{x+1}{x-1}} x^3 + e^{\frac{x+1}{x-1}} x y(x)^2 + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.103051 (sec), leaf count = 78

$$\left\{\left\{y(x) \to x\tan\left(\frac{1}{2}\left(2c_1 - 8e\text{Ei}\left(\frac{2}{x-1}\right) + e^{\frac{x}{x-1}+\frac{1}{x-1}}x^2 + 2e^{\frac{x}{x-1}+\frac{1}{x-1}}x - 3e^{\frac{2}{x-1}+1}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.086 (sec), leaf count = 42

$$\left\{y(x) = \tan\left(\frac{x^2+2x-3}{2}\mathrm{e}^{\frac{1+x}{x-1}} + 4\,\mathrm{e}Ei\left(1,-2\left(x-1\right)^{-1}\right) + \_C1\right)x\right\}$$

2.689 ODE No. 689

$$y'(x) = \frac{-e^{x+1}x^3 + e^{x+1}xy(x)^2 + xy(x) - y(x)}{(x-1)x}$$

✓ **Mathematica** : cpu = 0.0668967 (sec), leaf count = 60

$$\left\{\left\{y(x) \to -\frac{x\left(e^{2c_1+2e^2\mathrm{Ei}(x-1)+2e^{x+1}}-1\right)}{e^{2c_1+2e^2\mathrm{Ei}(x-1)+2e^{x+1}}+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.168 (sec), leaf count = 25

$$\left\{y(x) = -\tanh\left(\mathrm{e}^{1+x} - \mathrm{e}^2 Ei(1,1-x) + \_C1\right)x\right\}$$

2.690 ODE No. 690

$$y'(x) = \frac{-\frac{x^2}{4} + x^3\sqrt{x^2+8y(x)-2x+1} + \frac{1}{4}}{x+1}$$

✓ **Mathematica** : cpu = 0.284933 (sec), leaf count = 127

$$\left\{\left\{y(x) \to \frac{1}{72}(-96c_1x^3 + 144c_1x^2 - 288c_1x + 288c_1\log(4x+4) + 144c_1^2 - 528c_1 + 16x^6 - 48x^5 + 132x^4 + 32x^3\right.\right.$$

✓ **Maple** : cpu = 0.346 (sec), leaf count = 40

$$\left\{\_C1 + \frac{4x^3}{3} - 2x^2 + 4x - 4\ln(1+x) - \sqrt{x^2-2x+1+8y(x)} = 0\right\}$$

2.691 ODE No. 691

$$y'(x) = \frac{\frac{1}{2}x^3\cos(2y(x)) + \frac{x^3}{2} - \frac{1}{2}\sin(2y(x))}{x}$$

✓ **Mathematica** : cpu = 0.0629376 (sec), leaf count = 21

$$\left\{\left\{y(x) \to \tan^{-1}\left(\frac{2c_1 + x^4}{4x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.727 (sec), leaf count = 17

$$\left\{y(x) = \arctan\left(\frac{x^4 + 8\_C1}{4\,x}\right)\right\}$$

2.692 ODE No. 692

$$y'(x) = \frac{x^3\sqrt{x^2 + y(x)^2} + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.0231577 (sec), leaf count = 20

$$\left\{\left\{y(x) \to x\sinh\left(\frac{1}{3}\left(3c_1 + x^3\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 2.739 (sec), leaf count = 30

$$\left\{\ln\left(\sqrt{\left(y\left(x\right)\right)^2 + x^2} + y(x)\right) - \frac{x^3}{3} - \ln\left(x\right) - \_C1 = 0\right\}$$

2.693 ODE No. 693

$$y'(x) = e^{bx}\left(e^{-3bx}y(x)^3 + e^{-2bx}y(x)^2 + 1\right)$$

✓ **Mathematica** : cpu = 0.16161 (sec), leaf count = 146

$$\text{Solve}\left[-\frac{1}{3}(9b+29)^{2/3}\text{RootSum}\left[\#1^3(9b+29)^{2/3} - 9\#1b - 3\#1 + (9b+29)^{2/3}\&,\ \frac{\log\left(\frac{3e^{-2bx}y(x)+e^{-bx}}{\sqrt[3]{(9b+29)e^{-3bx}}} - \#1\right)}{\#1^2\left(-(9b+29)^{2/3}\right) + 3b + 1}\right.\right.$$

✓ **Maple** : cpu = 0.216 (sec), leaf count = 40

$$\left\{y(x) = \frac{1}{\mathrm{e}^{-bx}}\mathit{RootOf}\left(-x - \int^{\_Z} -\left(\_a^3 + \_a^2 - \_a\,b + 1\right)^{-1} d\_a + \_C1\right)\right\}$$

2.694 ODE No. 694

$$y'(x) = \frac{x^3\sqrt{4x^2y(x)+1} + \frac{x}{2} + \frac{1}{2}}{x^3(x+1)}$$

✓ **Mathematica** : cpu = 0.26913 (sec), leaf count = 66

$$\left\{\left\{y(x) \to \frac{-8c_1x^3 + 4c_1^2x^2 + 8c_1x^2\log(x+1) + 4x^4 - 8x^3\log(x+1) + 4x^2\log^2(x+1) - 1}{4x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.279 (sec), leaf count = 30

$$\left\{-2\ln(1+x) - \frac{1}{x}\sqrt{4x^2y(x)+1} + 2x + \_C1 = 0\right\}$$

2.695 ODE No. 695

$$y'(x) = \frac{x^4 + x^3 + x^2y(x)^2 + xy(x)^2 + y(x)\log(x-1)}{x\log(x-1)}$$

✓ **Mathematica** : cpu = 0.0518886 (sec), leaf count = 34

$$\{\{y(x) \to x\tan(c_1 + 2\text{Ei}(\log(x-1)) + 3\text{Ei}(2\log(x-1)) + \text{Ei}(3\log(x-1)))\}\}$$

✓ **Maple** : cpu = 0.07 (sec), leaf count = 39

$$\{y(x) = \tan(-Ei(1,-3\ln(x-1)) - 3\,Ei(1,-2\ln(x-1)) - 2\,Ei(1,-\ln(x-1)) + \_C1)\,x\}$$

2.696 ODE No. 696

$$y'(x) = \frac{e^{x+1}x^3 + 7e^{x+1}xy(x)^2 + y(x)\log(x-1)}{x\log(x-1)}$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.386 (sec), leaf count = 32

$$\left\{y(x) = \frac{x\sqrt{7}}{7}\tan\left(\left(\mathrm{e}\int\frac{xe^x}{\ln(x-1)}\,\mathrm{d}x + \_C1\right)\sqrt{7}\right)\right\}$$

2.697 ODE No. 697

$$y'(x) = e^{2x/3}\left(e^{-2x}y(x)^3 + e^{-4x/3}y(x)^2 + 1\right)$$

✓ **Mathematica** : cpu = 0.118865 (sec), leaf count = 114

$$\text{Solve}\left[-\frac{35}{3}\text{RootSum}\left[-35\#1^3 + 9\sqrt[3]{35}\#1 - 35\&, \frac{\log\left(\frac{3e^{-4x/3}y(x)+e^{-2x/3}}{\sqrt[3]{35}\sqrt[3]{e^{-2x}}} - \#1\right)}{3\sqrt[3]{35} - 35\#1^2}\&\right]\right] = c_1 + \frac{1}{9}35^{2/3}e^{4x/3}\left(e^{-2x}\right)^{2/3}$$

✓ **Maple** : cpu = 0.152 (sec), leaf count = 40

$$\left\{y(x) = RootOf\left(-x + 3\int^{-Z}\left(3\_a^3 + 3\_a^2 - 2\_a + 3\right)^{-1}d\_a + \_C1\right)\left(\mathrm{e}^{-\frac{2x}{3}}\right)^{-1}\right\}$$

2.698 ODE No. 698

$$y'(x) = e^{x}\left(e^{-3x}y(x)^3 + e^{-2x}y(x)^2 + 1\right)$$

✓ **Mathematica** : cpu = 0.128924 (sec), leaf count = 108

$$\text{Solve}\left[-\frac{19}{3}\text{RootSum}\left[-19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log\left(\frac{3e^{-2x}y(x)+e^{-x}}{\sqrt[3]{38}\sqrt[3]{e^{-3x}}} - \#1\right)}{2\sqrt[3]{38} - 19\#1^2}\&\right]\right] = c_1 + \frac{1}{9}38^{2/3}e^{2x}\left(e^{-3x}\right)^{2/3}x, y(x$$

✓ **Maple** : cpu = 0.174 (sec), leaf count = 34

$$\left\{y(x) = \frac{RootOf\left(-x + \int^{-Z}\left(\_a^3 + \_a^2 - \_a + 1\right)^{-1}d\_a + \_C1\right)}{\mathrm{e}^{-x}}\right\}$$

2.699 ODE No. 699

$$y'(x) = \frac{x\left(3x^2\sqrt{x^2+3y(x)} - 2x - 2\right)}{3(x+1)}$$

✓ **Mathematica** : cpu = 0.22177 (sec), leaf count = 101

$$\left\{\left\{y(x) \to \frac{1}{48}(-24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1\log(x+1) + 36c_1^2 + 4x^6 - 12x^5 + 33x^4 - 36x^3 - 24x^3\log(x+1$$

✓ **Maple** : cpu = 0.393 (sec), leaf count = 36

$$\left\{\_C1 + \frac{x^3}{2} - \frac{3x^2}{4} + \frac{3x}{2} - \frac{3\ln(1+x)}{2} - \sqrt{x^2+3y(x)} = 0\right\}$$

2.700 ODE No. 700

$$y'(x) = \frac{1}{xy(x)\left(xy(x)^2 + x + 1\right)}$$

✓ **Mathematica** : cpu = 0.0618452 (sec), leaf count = 76

$$\left\{\left\{y(x) \to -\frac{\sqrt{2xW\left(c_1 e^{\frac{1}{2x}-\frac{1}{2}}\right)+x-1}}{\sqrt{x}}\right\}, \left\{y(x) \to \frac{\sqrt{2xW\left(c_1 e^{\frac{1}{2x}-\frac{1}{2}}\right)+x-1}}{\sqrt{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.175 (sec), leaf count = 62

$$\left\{y(x) = \frac{1}{x}\sqrt{x\left(2\,lambertW\left(1/2\,\_C1\,\mathrm{e}^{-1/2\,\frac{x-1}{x}}\right)x + x - 1\right)}, y(x) = -\frac{1}{x}\sqrt{x\left(2\,lambertW\left(1/2\,\_C1\,\mathrm{e}^{-1/2\,\frac{x-1}{x}}\right)\right.}\right.$$

2.701 ODE No. 701

$$y'(x) = \frac{x^4 + x^4\log(x) - 2x^2y(x) - 2x^2y(x)\log(x) + y(x)^2 + y(x)^2\log(x) + 2e^x x - 2x - \log(x) - 1}{e^x - 1}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 6.756 (sec), leaf count = 71

$$\left\{y(x) = 1\left(-x^2\left(\mathrm{e}^{\int \frac{\ln(x)+1}{\mathrm{e}^x-1}\,\mathrm{d}x}\right)^2 + x^2\_C1 + \left(\mathrm{e}^{\int \frac{\ln(x)+1}{\mathrm{e}^x-1}\,\mathrm{d}x}\right)^2 + \_C1\right)\left(-\left(\mathrm{e}^{\int \frac{\ln(x)+1}{\mathrm{e}^x-1}\,\mathrm{d}x}\right)^2 + \_C1\right)^{-1}\right\}$$

2.702 ODE No. 702

$$y'(x) = \frac{-x^3 + x^3(-\log(x)) - xy(x)^2 + xy(x) - e^x y(x) - xy(x)^2\log(x)}{x\left(x - e^x\right)}$$

✗ **Mathematica** : cpu = 300.033 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.247 (sec), leaf count = 35

$$\left\{y(x) = \tan\left(\int \frac{x\ln(x)}{\mathrm{e}^x - x}\,\mathrm{d}x + \int \frac{x}{\mathrm{e}^x - x}\,\mathrm{d}x + \_C1\right)x\right\}$$

2.703 ODE No. 703

$$y'(x) = \frac{y(x)\left(x^3 y(x) + x^2 y(x)\log(x) - x^2 - x - x\log(x) + 1\right)}{(x-1)x}$$

✗ **Mathematica** : cpu = 301.051 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.602 (sec), leaf count = 44

$$\left\{y(x) = \frac{\mathrm{e}^{dilog(x)}}{x\mathrm{e}^x\left(x-1\right)}\left(\int -\frac{\mathrm{e}^{dilog(x)}\left(x+\ln\left(x\right)\right)}{\mathrm{e}^x\left(x-1\right)^2}\,\mathrm{d}x + \_C1\right)^{-1}\right\}$$

2.704 ODE No. 704

$$y'(x) = \frac{2ax^3 y(x)^2 + 2bx^5 - y(x) + xy(x)\log(x)}{x(x\log(x) - 1)}$$

✗ **Mathematica** : cpu = 300.022 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.048 (sec), leaf count = 38

$$\left\{y(x) = \frac{x}{a}\tan\left(2\sqrt{ab}\left(\_C1 + \int \frac{x^3}{x\ln\left(x\right) - 1}\,\mathrm{d}x\right)\right)\sqrt{ab}\right\}$$

2.705 ODE No. 705

$$y'(x) = \frac{y(x)\left(x^4 + x^3 + \log(y(x)) + x\right)}{x}$$

✓ **Mathematica** : cpu = 0.0526473 (sec), leaf count = 30

$$\left\{\left\{y(x) \to x^x e^{c_1 x + \frac{x^4}{3} + \frac{x^3}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.159 (sec), leaf count = 24

$$\left\{y(x) = \mathrm{e}^{\frac{x^4}{3}}\mathrm{e}^{\frac{x^3}{2}}\mathrm{e}^{x}\_C1\,x^x\right\}$$

2.706 ODE No. 706

$$y'(x) = -\frac{1}{8}x(y(x)+1)^2(-\log(y(x)-1)+\log(y(x)+1)+2\log(x))$$

✗ **Mathematica** : cpu = 300.067 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.633 (sec), leaf count = 65

$$\left\{\int_{\_b}^{y(x)} \frac{1}{2+2\_a}\left(-\frac{x^2(1+\_a)\ln(\_a-1)}{2}+\frac{x^2(1+\_a)\ln(1+\_a)}{2}+x^2(1+\_a)\ln(x)+4\_a-4\right)^{-1} \mathrm{d}\_a+\right.$$

2.707 ODE No. 707

$$y'(x) = \frac{1}{16}x(y(x)+1)^2(-\log(y(x)-1)+\log(y(x)+1)+2\log(x))^2$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.539 (sec), leaf count = 105

$$\left\{\int_{\_b}^{y(x)} \frac{1}{4+4\_a}\left(\frac{x^2(1+\_a)\left(\ln(1+\_a)\right)^2}{4}+x^2(1+\_a)\left(-\frac{\ln(\_a-1)}{2}+\ln(x)\right)\ln(1+\_a)+\frac{x^2(1+\_a)(\right.\right.$$

2.708 ODE No. 708

$$y'(x) = \frac{(4ax-y(x)^2)^3}{y(x)(4ax-y(x)^2-1)}$$

✓ **Mathematica** : cpu = 0.27662 (sec), leaf count = 89

$$\text{Solve}\left[2a\left(x-\frac{\text{RootSum}\left[-\#1^3+2\#1a-2a\&,\frac{\#1a\log(-\#1+4ax-y(x)^2)-a\log(-\#1+4ax-y(x)^2)}{2a-3\#1^2}\&\right]}{2a}\right)=c_1,y(x)\right]$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

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time expired
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2.709 ODE No. 709

$$y'(x) = \frac{x^3\sqrt{4ax - y(x)^2} + 2ax + 2a}{(x+1)y(x)}$$

✓ **Mathematica** : cpu = 4.27753 (sec), leaf count = 217

$$\left\{\left\{y(x) \to -\frac{1}{6}\sqrt{144ax - 24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1\log(x+1) - 36c_1^2 - 4x^6 + 12x^5 - 33x^4 + 36x^3 + 24x^3}\right.\right.$$

✓ **Maple** : cpu = 0.302 (sec), leaf count = 39

$$\left\{-\sqrt{-(y(x))^2 + 4ax} - \frac{x^3}{3} + \frac{x^2}{2} - x + \ln(1+x) - \_C1 = 0\right\}$$

2.710 ODE No. 710

$$y'(x) = \frac{2x^3 + 4x^2y(x) + 2xy(x)^2 + 2x + e^{\frac{1}{x}} - \log(x)}{\log(x) - e^{\frac{1}{x}}}$$

✗ **Mathematica** : cpu = 300.027 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 2.625 (sec), leaf count = 31

$$\left\{y(x) = -x + \tan\left(2\_C1 - 2\int -\frac{x}{\ln(x) - \mathrm{e}^{x^{-1}}}\,\mathrm{d}x\right)\right\}$$

2.711 ODE No. 711

$$y'(x) = -\frac{y(x)(x\log(y(x)) + \log(y(x)) - 1)}{x+1}$$

✓ **Mathematica** : cpu = 0.0651276 (sec), leaf count = 28

$$\left\{\left\{y(x) \to e^{c_1e^{-x} + e^{-x-1}\mathrm{Ei}(x+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.139 (sec), leaf count = 31

$$\left\{y(x) = 1\mathrm{e}^{\frac{-C1}{\mathrm{e}^x}}\left(\mathrm{e}^{\frac{Ei(1,-1-x)}{\mathrm{e}^x\mathrm{e}}}\right)^{-1}\right\}$$

2.712 ODE No. 712

$$y'(x) = \frac{\frac{x^2}{2} + x^3\sqrt{x^2 - 4y(x) + 2x + 1} + x + \frac{1}{2}}{x+1}$$

✓ **Mathematica** : cpu = 0.258397 (sec), leaf count = 115

$$\left\{\left\{y(x) \to \frac{1}{36}(24c_1x^3 - 36c_1x^2 + 72c_1x - 72c_1\log(x+1) - 36c_1^2 + 132c_1 - 4x^6 + 12x^5 - 33x^4 - 8x^3 + 24x^3\log\right.\right.$$

✓ **Maple** : cpu = 0.335 (sec), leaf count = 38

$$\left\{\_C1 - \frac{2\,x^3}{3} + x^2 - 2\,x + 2\,\ln(1+x) - \sqrt{x^2 + 2\,x + 1 - 4\,y(x)} = 0\right\}$$

2.713 ODE No. 713

$$y'(x) = \frac{-a^2 - aby(x) - ab\sqrt{x} + ab + b^2x + b^2}{a\left(a(-y(x)) - a\sqrt{x} + a + bx + b\right)}$$

✓ **Mathematica** : cpu = 0.120508 (sec), leaf count = 649

$$\left\{\left\{y(x) \to \frac{1}{a^2\text{Root}\left[\#1^6\left(16e^{12c_1} + 16x^3\right) - \frac{24\#1^4x^2}{a^4} + \frac{8\#1^3x^{3/2}}{a^6} + \frac{9\#1^2x}{a^8} - \frac{6\#1\sqrt{x}}{a^{10}} + \frac{1}{a^{12}}\&, 1\right]} - \frac{a\sqrt{x} - a - bx -}{a}\right.\right.$$

✓ **Maple** : cpu = 0.447 (sec), leaf count = 86

$$\left\{y(x) = \frac{1}{2\,a}\left(3\,\tanh\left(RootOf\left(729\,x^3(\tanh(\_Z))^6\,a^6 - 2187\,x^3(\tanh(\_Z))^4\,a^6 + 2187\,x^3(\tanh(\_Z))^2\,a^6 - 729\right.\right.\right.\right.$$

2.714 ODE No. 714

$$y'(x) = -\frac{y(x)\left(x^3y(x) + x^2y(x)\log(x) - x^2 + e^x - x\log(x) - \log\left(\frac{1}{x}\right)\right)}{x\left(e^x - \log\left(\frac{1}{x}\right)\right)}$$

✗ **Mathematica** : cpu = 300.036 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 2.222 (sec), leaf count = 96

$$\left\{y(x) = 1\mathrm{e}^{\int \frac{x\ln(x) + x^2 + \ln\left(x^{-1}\right) - \mathrm{e}^x}{\left(-\ln\left(x^{-1}\right) + \mathrm{e}^x\right)x}\,\mathrm{d}x}\left(\int \frac{x(x + \ln(x))}{-\ln\left(x^{-1}\right) + \mathrm{e}^x}\mathrm{e}^{\int \frac{x\ln(x) + x^2 + \ln\left(x^{-1}\right) - \mathrm{e}^x}{\left(-\ln\left(x^{-1}\right) + \mathrm{e}^x\right)x}\,\mathrm{d}x}\,\mathrm{d}x + \_C1\right)^{-1}\right\}$$

2.715 ODE No. 715

$$y'(x) = \frac{-\frac{x^2}{2} + x^3\sqrt{x^2+4y(x)-4x} + \frac{x}{2} + 1}{x+1}$$

✓ **Mathematica** : cpu = 0.241319 (sec), leaf count = 104

$$\left\{\left\{y(x) \to \frac{1}{36}(-24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1\log(x+1) + 36c_1^2 + 4x^6 - 12x^5 + 33x^4 - 36x^3 - 24x^3\log(x+1$$

✓ **Maple** : cpu = 0.312 (sec), leaf count = 39

$$\left\{\_C1 + \frac{2x^3}{3} - x^2 + 2x - 2\ln(1+x) - \sqrt{x^2-4x+4y(x)} = 0\right\}$$

2.716 ODE No. 716

$$y'(x) = \frac{\sqrt{9x^4 - 4y(x)^3} + 3x^4 + 3x^3}{(x+1)y(x)^2}$$

✓ **Mathematica** : cpu = 4.07658 (sec), leaf count = 133

$$\left\{\left\{y(x) \to \left(-\frac{3}{2}\right)^{2/3}\sqrt[3]{8c_1\log(x+1) - 4c_1^2 + x^4 - 4\log^2(x+1)}\right\}, \left\{y(x) \to \left(\frac{3}{2}\right)^{2/3}\sqrt[3]{8c_1\log(x+1) - 4c_1^2 + x}\right.\right.$$

✓ **Maple** : cpu = 0.361 (sec), leaf count = 37

$$\left\{\int_{\_b}^{y(x)} \frac{\_a^2}{\sqrt{9x^4 - 4\_a^3}}\,d\_a - \ln(1+x) - \_C1 = 0\right\}$$

2.717 ODE No. 717

$$y'(x) = \frac{\sqrt{a^2+2ax+x^2+4y(x)} - \frac{ax}{2} - \frac{a}{2} - \frac{x^2}{2} - \frac{x}{2}}{x+1}$$

✓ **Mathematica** : cpu = 0.302393 (sec), leaf count = 46

$$\left\{\left\{y(x) \to \frac{1}{4}(-a^2 - 2ax - 8c_1\log(x+1) + 4c_1^2 - x^2 + 4\log^2(x+1))\right\}\right\}$$

✓ **Maple** : cpu = 0.381 (sec), leaf count = 33

$$\left\{\_C1 + \frac{a}{2} + 2\ln(1+x) - \sqrt{x^2+2ax+a^2+4y(x)} = 0\right\}$$

2.718 ODE No. 718

$$y'(x) = e^{-x^2} x \left(e^{3x^2} y(x)^3 + e^{2x^2} y(x)^2 + 1 \right)$$

✓ **Mathematica** : cpu = 0.118284 (sec), leaf count = 127

$$\text{Solve}\left[\frac{11}{3} \text{RootSum}\left[11\#1^3 + 15\sqrt[3]{11}\#1 + 11\&, \frac{\log\left(\frac{3e^{2x^2} x y(x) + e^{x^2} x}{\sqrt[3]{11}\sqrt[3]{e^{3x^2} x^3}} - \#1 \right)}{11\#1^2 + 5\sqrt[3]{11}} \& \right] = c_1 + \frac{11^{2/3} e^{x^2} x^3}{18\sqrt[3]{e^{3x^2} x^3}}, y(x) \right]$$

✓ **Maple** : cpu = 0.068 (sec), leaf count = 44

$$\left\{ y(x) = \frac{-11\, RootOf\left(-5\,x^2 + 20250 \int^{-Z} \left(121\,\_a^3 + 3375\,\_a - 3375 \right)^{-1} d\_a + 6\,\_C1 \right) - 15}{45\, \mathrm{e}^{x^2}} \right\}$$

2.719 ODE No. 719

$$y'(x) = \frac{e^{-x} y(x) \left(x^2 y(x) \log(2x) - e^x - x \log(2x) \right)}{x}$$

✓ **Mathematica** : cpu = 0.0882187 (sec), leaf count = 49

$$\left\{ \left\{ y(x) \to \frac{2^{e^{-x}} x^{e^{-x}-1}}{c_1 e^{\text{Ei}(-x)} + 2^{e^{-x}} x^{e^{-x}}} \right\} \right\}$$

✓ **Maple** : cpu = 0.193 (sec), leaf count = 57

$$\left\{ y(x) = -\frac{x^{\mathrm{e}^{-x}} 2^{\mathrm{e}^{-x}} \mathrm{e}^{Ei(1,x)}}{x \left(\int x^{\mathrm{e}^{-x}} 2^{\mathrm{e}^{-x}} \mathrm{e}^{Ei(1,x)} \mathrm{e}^{-x} \left(\ln(2) + \ln(x) \right) \mathrm{d}x + \_C1 \right)} \right\}$$

2.720 ODE No. 720

$$y'(x) = \frac{x^3 \left(\sqrt{9x^4 - 4y(x)^3} + 3x + 3 \right)}{(x+1) y(x)^2}$$

✓ **Mathematica** : cpu = 4.48648 (sec), leaf count = 314

$$\left\{ \left\{ y(x) \to \sqrt[3]{6c_1 x^3 - 9c_1 x^2 + 18c_1 x - 18c_1 \log(x+1) - 9c_1^2 - x^6 + 3x^5 - 6x^4 + 9x^3 + 6x^3 \log(x+1) - 9x^2 - 9x \right.$$

✓ **Maple** : cpu = 0.244 (sec), leaf count = 48

$$\left\{\int_{\_b}^{y(x)} \_a^2 \frac{1}{\sqrt{9\,x^4-4\,\_a^3}}\,\mathrm{d}\_a-\frac{x^3}{3}+\frac{x^2}{2}-x+\ln\left(1+x\right)-\_C1=0\right\}$$

2.721 ODE No. 721

$$y'(x)=\frac{1}{36}\sqrt{x}\left(18x^{3/2}+x^6-12x^3y(x)+36y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.0184284 (sec), leaf count = 27

$$\left\{\left\{y(x)\to\frac{1}{c_1-\frac{2x^{3/2}}{3}}+\frac{x^3}{6}\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 19

$$\left\{y(x)=\frac{x^3}{6}+\left(\_C1-\frac{2}{3}x^{\frac{3}{2}}\right)^{-1}\right\}$$

2.722 ODE No. 722

$$y'(x)=-\frac{y(x)^3}{x(-y(x)+2y(x)\log(x)-1)}$$

✓ **Mathematica** : cpu = 30.1793 (sec), leaf count = 493

$$\text{Solve}\left[-\frac{\sqrt[3]{-2}\left((-2)^{2/3}-\frac{(1-2\log(x))^2\left(-\frac{1}{(2\log(x)-1)^3}\right)^{2/3}(y(x)(5-4\log(x))+2)}{2\sqrt[3]{2}(y(x)(2\log(x)-1)-1)}\right)\left(\frac{y(x)(4\log(x)-5)-2}{\sqrt[3]{2}\sqrt[3]{-\frac{1}{(2\log(x)-1)^3}}(2\log(x)-1)(y(x)(2\log(x)-\right.\right.$$

✓ **Maple** : cpu = 0.372 (sec), leaf count = 70

$$\left\{y(x)=1\mathrm{e}^{RootOf\left(-\mathrm{e}^{\_Z}\ln\left(\frac{\mathrm{e}^{\_Z}+2}{2\,x^4}\right)+3\,\_C1\,\mathrm{e}^{\_Z}+\_Z\,\mathrm{e}^{\_Z}+2\right)}\left(1+\left(2\,\ln\left(x\right)-1\right)\mathrm{e}^{RootOf\left(-\mathrm{e}^{\_Z}\ln\left(\frac{\mathrm{e}^{\_Z}+2}{2\,x^4}\right)+3\,\_C1\,\mathrm{e}^{\_Z}+\_Z\,\mathrm{e}^{\_Z}+2\right)}\right.\right.$$

2.723 ODE No. 723

$$y'(x) = \frac{2a}{32a^3x^2 - 16a^2xy(x)^2 + 2ay(x)^4 + y(x)}$$

✓ **Mathematica** : cpu = 0.0656622 (sec), leaf count = 663

$$\left\{\left\{y(x) \to -\frac{\sqrt[3]{-1024a^6c_1^3 + 9216a^5c_1x - 432a^2 + \sqrt{4\left(-64a^4c_1^2 - 192a^3x\right)^3 + \left(-1024a^6c_1^3 + 9216a^5c_1x - 432a\right.}}}{12\sqrt[3]{2}a}\right.\right.$$

✓ **Maple** : cpu = 0.085 (sec), leaf count = 856

$$\left\{y(x) = -\frac{1}{12\,a}\left(-8\_C1\,a^2\sqrt[3]{\left(64\_C1^3a^4 - 576\_C1\,a^3x + 3\sqrt{-12288\_C1^4a^7x + 24576\_C1^2a^6x^2 - 12288\right.}\right.\right.$$

2.724 ODE No. 724

$$y'(x) = -\frac{y(x)^3}{x(-y(x) + y(x)\log(x) - 1)}$$

✓ **Mathematica** : cpu = 45.6999 (sec), leaf count = 422

$$\text{Solve}\left[-\frac{\sqrt[3]{-2}\left(\frac{1-y(x)(\log(x)-4)}{\sqrt[3]{2}\sqrt[3]{-\frac{1}{(\log(x)-1)^3}}(\log(x)-1)(y(x)(\log(x)-1)-1)} + (-2)^{2/3}\right)\left(\frac{2^{2/3}(y(x)(\log(x)-4)-1)}{\sqrt[3]{-\frac{1}{(\log(x)-1)^3}}(\log(x)-1)(y(x)(\log(x)-1)-1)} + (-\right.\right.$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 18

$$\left\{y(x) = \left(-lambertW\left(\_C1\,\mathrm{e}^{-2}x\right) + \ln(x) - 2\right)^{-1}\right\}$$

2.725 ODE No. 725

$$y'(x) = \frac{x^2 \log(2x) + 2xy(x) \log(2x) + y(x)^2 \log(2x) - \log(x) + \log(2x)}{\log(x)}$$

✓ **Mathematica** : cpu = 0.239754 (sec), leaf count = 19

$$\{\{y(x) \to \tan(c_1 + \log(2)\text{li}(x) + x) - x\}\}$$

✓ **Maple** : cpu = 0.866 (sec), leaf count = 25

$$\{y(x) = -x - \tan(\ln(2)\, Ei(1, -\ln(x)) + \_C1 - x)\}$$

2.726 ODE No. 726

$$y'(x) = \frac{a^2 - aby(x) - ab\sqrt{x} - b^2 x + bc}{a\left(ay(x) + a\sqrt{x} + bx - c\right)}$$

✓ **Mathematica** : cpu = 0.082404 (sec), leaf count = 625

$$\left\{\left\{y(x) \to \frac{1}{a^2 \text{Root}\left[\#1^6 \left(16e^{12c_1} + 16x^3\right) - \frac{24\#1^4 x^2}{a^4} + \frac{8\#1^3 x^{3/2}}{a^6} + \frac{9\#1^2 x}{a^8} - \frac{6\#1\sqrt{x}}{a^{10}} + \frac{1}{a^{12}} \&, 1\right]} - \frac{a\sqrt{x} + bx - c}{a}\right\},\right.$$

✓ **Maple** : cpu = 0.305 (sec), leaf count = 83

$$\left\{y(x) = \frac{1}{2\,a}\left(3 \tanh\left(RootOf\left(-729\,x^3(\tanh(\_Z))^6\,a^6 + 2187\,x^3(\tanh(\_Z))^4\,a^6 - 2187\,x^3(\tanh(\_Z))^2\,a^6 + 7\right.\right.\right.$$

2.727 ODE No. 727

$$y'(x) = \frac{y(x)(y(x) + 2x + 2)}{(x+1)(\log(y(x)) + 2x - 1)}$$

✓ **Mathematica** : cpu = 0.427452 (sec), leaf count = 29

$$\left\{\left\{y(x) \to \frac{W\left(e^{-2x}(c_1 + \log(x+1))\right)}{c_1 + \log(x+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.403 (sec), leaf count = 25

$$\left\{y(x) = \mathrm{e}^{-lambertW\left((\ln(1+x) - \_C1)\mathrm{e}^{-2x}\right) - 2x}\right\}$$

2.728 ODE No. 728

$$y'(x) = \frac{y(x)\left(x^3 + 3y(x)^2\right)}{x\left(6y(x)^2 + x\right)}$$

✓ **Mathematica** : cpu = 0.371134 (sec), leaf count = 72

$$\left\{\left\{y(x) \to -\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1+x^2}}{x}\right)}}{\sqrt{6}}\right\}, \left\{y(x) \to \frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1+x^2}}{x}\right)}}{\sqrt{6}}\right\}\right\}$$

✓ **Maple** : cpu = 0.358 (sec), leaf count = 50

$$\left\{\left((y(x))^{-2} + 6\,x^{-1}\right)^{-1} = \frac{x}{54}\left(\mathrm{e}^{RootOf\left(x^2\mathrm{e}^{-Z} - \mathrm{e}^{-Z}\ln\left(\frac{\left(\mathrm{e}^{-Z}+9\right)x}{2}\right) + 3\_C1\,\mathrm{e}^{-Z} + \_Z\,\mathrm{e}^{-Z} + 9\right)} + 9\right)\right\}$$

2.729 ODE No. 729

$$y'(x) = \frac{(x - y(x))y(x)}{x\left(x - y(x)^3\right)}$$

✓ **Mathematica** : cpu = 0.307507 (sec), leaf count = 327

$$\left\{\left\{y(x) \to \frac{\sqrt[3]{2}(6c_1 - 6\log(x))}{3\sqrt[3]{\sqrt{4\left(6c_1 - 6\log(x)\right)^3 + 2916x^2} + 54x}} - \frac{\sqrt[3]{\sqrt{4\left(6c_1 - 6\log(x)\right)^3 + 2916x^2} + 54x}}{3\sqrt[3]{2}}\right\}, \left\{y(x) \to \frac{(1}{}\right.$$

✓ **Maple** : cpu = 0.108 (sec), leaf count = 404

$$\left\{y(x) = \frac{1}{3}\left(\left(-27\,x + 3\sqrt{24\_C1^3 - 72\_C1^2\ln(x) + 72\_C1\,(\ln(x))^2 - 24\,(\ln(x))^3 + 81\,x^2}\right)^{\frac{2}{3}} + 6\,\ln(x) - 6\right.\right.$$

2.730 ODE No. 730

$$y'(x) = \frac{e^x \left(2y(x)^{3/2} - 3e^x\right)^3}{4\sqrt{y(x)}\left(2y(x)^{3/2} - 3e^x + 2\right)}$$

✗ **Mathematica** : cpu = 48.9197 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == (E^x*(-3*E^x + 2*y[x]^(3/2))^3)/(4*Sqrt[y[x]]*(2 - 3*E^x + 2*y
```

✓ **Maple** : cpu = 2.161 (sec), leaf count = 41

$$\left\{ \mathrm{e}^x - \int^{(y(x))^{\frac{3}{2}} - \frac{3\,\mathrm{e}^x}{2}} \frac{2 + 2\_a}{3\_a^3 - 3\_a - 3} d\_a - \_C1 = 0 \right\}$$

2.731 ODE No. 731

$$y'(x) = \frac{2y(x) + 1}{x\left(2xy(x)^3 + xy(x)^2 - 2\right)}$$

✓ **Mathematica** : cpu = 0.184977 (sec), leaf count = 47

$$\text{Solve}\left[\frac{1}{64}\left(-4y(x)^2 + 4y(x) - 2\log(8y(x) + 4) + 3\right) - \frac{1}{4x(2y(x) + 1)} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.194 (sec), leaf count = 42

$$\left\{ y(x) = \frac{\mathrm{e}^{RootOf\left(x\left(\mathrm{e}^{\_Z}\right)^3 - 4x\left(\mathrm{e}^{\_Z}\right)^2 + 8x\_C1\,\mathrm{e}^{\_Z} + 2\_Z x\mathrm{e}^{\_Z} + 3x\mathrm{e}^{\_Z} + 16\right)}}{2} - \frac{1}{2} \right\}$$

2.732 ODE No. 732

$$y'(x) = \frac{x^3\sqrt{a^2 + 2ax + x^2 + 4y(x)} - \frac{ax}{2} - \frac{a}{2} - \frac{x^2}{2} - \frac{x}{2}}{x + 1}$$

✓ **Mathematica** : cpu = 0.454001 (sec), leaf count = 110

$$\left\{\left\{y(x) \to \frac{1}{36}\left(-9a^2 - 18ax - 24c_1x^3 + 36c_1x^2 - 72c_1x + 72c_1\log(x + 1) + 36c_1^2 + 4x^6 - 12x^5 + 33x^4 - 36x^3 -\right.\right.$$

✓ **Maple** : cpu = 0.405 (sec), leaf count = 43

$$\left\{ \_C1 + \frac{2x^3}{3} - x^2 + 2x - 2\ln(1 + x) - \sqrt{x^2 + 2ax + a^2 + 4y(x)} = 0 \right\}$$

2.733 ODE No. 733

$$y'(x) = \csc(x) \left(x^4 \log(2x) - 2x^2 y(x) \log(2x) + y(x)^2 \log(2x) - \log(2x) + 2x \sin(x)\right)$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = (2*x*sin(x)-ln(2*x)+ln(2*x)*x^4-2*ln(2*x)*x^2*y(x)+ln(2*x)*y(x)^2)/sin
```

2.734 ODE No. 734

$$y'(x) = \frac{y(x) \left(x^3 - x \log(y(x)) - \log(y(x))\right)}{x+1}$$

✓ **Mathematica** : cpu = 0.109047 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \exp\left(-c_1 e^{-x} - e^{-x-1} \text{Ei}(x+1) + x^2 - 3x + 4\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.152 (sec), leaf count = 39

$$\left\{y(x) = \frac{\mathrm{e}^{x^2} \mathrm{e}^4}{\left(\mathrm{e}^x\right)^3} \mathrm{e}^{\frac{\_C1}{\mathrm{e}^x}} \mathrm{e}^{\frac{Ei(1,-1-x)}{\mathrm{e}^x \mathrm{e}}}\right\}$$

2.735 ODE No. 735

$$y'(x) = \frac{(2y(x)\log(x) - 1)^3}{x(-y(x) + 2y(x)\log(x) - 1)}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.069 (sec), leaf count = 78

$$\left\{y(x) = \frac{71\, RootOf\left(-82944 \int^{-Z} \left(5041 \_a^3 - 27648 \_a + 27648\right)^{-1} d\_a - 16 \ln(x) + 3 \_C1\right) - 1}{(142 \ln(x) - 71)\, RootOf\left(-82944 \int^{-Z} (5041 \_a^3 - 27648 \_a + 27648)^{-1} d\_a - 16 \ln(x) + 3 \_C1\right) -}\right.$$

2.736 ODE No. 736

$$y'(x) = \frac{x^4 - 2x^2 y(x) + 2x^2 + y(x)^2 + 2x - 1}{x + 1}$$

✓ **Mathematica** : cpu = 0.0940981 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{(x+1)^2}{c_1 - \frac{x^2}{2} - x} + x^2 + 1\right\}\right\}$$

✓ **Maple** : cpu = 0.2 (sec), leaf count = 43

$$\left\{y(x) = \frac{\_C1\,\left(x^4 + 2\,x^3 - x^2 - 2\,x - 2\right) + x^2 + 1}{1 + \left(x^2 + 2\,x\right)\,\_C1}\right\}$$

2.737 ODE No. 737

$$y'(x) = \frac{x\left(2x^3 - 2xy(x) + x - 1\right)}{x^2 - y(x)}$$

✓ **Mathematica** : cpu = 0.029455 (sec), leaf count = 36

$$\left\{\left\{y(x) \to \frac{1}{2}\left(W\left(-e^{c_1 + \frac{4x^3}{3} - 2x^2 - 1}\right) + 1\right) + x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.083 (sec), leaf count = 29

$$\left\{y(x) = x^2 + \frac{1}{2}\mathit{lambertW}\left(-2\,\frac{\mathrm{e}^{4/3\,x^3}\,\_C1\,\mathrm{e}^{-1}}{\left(\mathrm{e}^{x^2}\right)^2}\right) + \frac{1}{2}\right\}$$

2.738 ODE No. 738

$$y'(x) = \frac{2a}{32a^3 - 16a^2 x y(x)^2 + 2ax^2 y(x)^4 - x^2 y(x)}$$

✓ **Mathematica** : cpu = 0.466549 (sec), leaf count = 1347

$$\left\{\left\{y(x) \to -\frac{4a + e^{c_1}}{12a} + \frac{\sqrt[3]{4608x^2a^4 - 128x^3a^3 + 1152e^{c_1}x^2a^3 - 96e^{c_1}x^3a^2 - 432x^3a^2 - 24e^{2c_1}x^3a - 2e^{3c_1}x^3 +}}{}\right.\right.$$

✓ **Maple** : cpu = 0.904 (sec), leaf count = 1054

$$\left\{ y(x) = \frac{1}{24 \_C1\, ax} \left(-2\, x \sqrt[3]{-216 \_C1^3 a^2 x^3 + 576 \_C1^2 a^3 x^2 + 12\, a \_C1\, x^2 \sqrt{\frac{\left(324 \_C1^4 a^2 + 3 \_C1\right) x^3 + (-}{}} \right.\right.$$

2.739 ODE No. 739

$$y'(x) = \frac{2y(x)+1}{x\left(2xy(x)^2 + xy(x) - 2\right)}$$

✓ **Mathematica** : cpu = 0.120262 (sec), leaf count = 39

$$\text{Solve}\left[\frac{1}{8}(-2y(x) + \log(4y(x)+2) - 1) - \frac{1}{2x(2y(x)+1)} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.18 (sec), leaf count = 35

$$\left\{ y(x) = \frac{\mathrm{e}^{RootOf\left(x\left(\mathrm{e}^{-Z}\right)^2 + 2\, x \_C1\, \mathrm{e}^{-Z} - \_Z\, x \mathrm{e}^{-Z} - x \mathrm{e}^{-Z} + 4\right)}}{2} - \frac{1}{2} \right\}$$

2.740 ODE No. 740

$$y'(x) = \frac{x^4 - 2x^2 y(x)^2 + y(x)^4 + x}{y(x)}$$

✓ **Mathematica** : cpu = 0.0596229 (sec), leaf count = 74

$$\left\{ \left\{ y(x) \to -\frac{\sqrt{2c_1 x^2 + 2x^3 - 1}}{\sqrt{2}\sqrt{c_1 + x}} \right\}, \left\{ y(x) \to \frac{\sqrt{2c_1 x^2 + 2x^3 - 1}}{\sqrt{2}\sqrt{c_1 + x}} \right\} \right\}$$

✓ **Maple** : cpu = 0.104 (sec), leaf count = 72

$$\left\{ y(x) = \frac{\sqrt{2}}{2 \_C1 + 2\, x} \sqrt{(\_C1 + x)\left(2\, x^2 \_C1 + 2\, x^3 - 1\right)}, y(x) = -\frac{\sqrt{2}}{2 \_C1 + 2\, x} \sqrt{(\_C1 + x)\left(2\, x^2 \_C1 + 2\, x^3 - \right.} \right.$$

2.741 ODE No. 741

$$y'(x) = \frac{x\left(ay(x)^2 + bx^2\right)^3}{a^{5/2}y(x)\left(ay(x)^2 + a + bx^2\right)}$$

✓ **Mathematica** : cpu = 2.85958 (sec), leaf count = 175

$$\text{Solve}\left[\frac{1}{2}\left(x^2 - a^{3/2}\text{RootSum}\left[\#1^3b^3 + 3\#1^2ab^2y(x)^2 + \#1a^{3/2}b^2 + 3\#1a^2by(x)^4 + a^{5/2}by(x)^2 + a^{5/2}b + a^3y(x)^6\right.\right.\right.$$

✓ **Maple** : cpu = 1.023 (sec), leaf count = 246

$$\left\{\int_{\_b}^{x} \frac{\left(\_a^2b + a(y(x))^2\right)^3 \_a}{a^3}\left(b\left((y(x))^2 + 1\right)a^{\frac{5}{2}} + a^{\frac{3}{2}}b^2\_a^2 + \left(\_a^2b + a(y(x))^2\right)^3\right)^{-1} \mathrm{d}\_a + \int^{y(x)} 1\left(\left((-\_f^2\right.\right.\right.\right.$$

2.742 ODE No. 742

$$y'(x) = -\frac{(-\cos(y(x)) + x + 1)\cos(y(x))}{(x+1)(x\sin(y(x)) - 1)}$$

✓ **Mathematica** : cpu = 4.2058 (sec), leaf count = 3913

$$\left\{\left\{y(x) \to -\sec^{-1}\left(\frac{c_1x^3}{x^2-1} + \frac{\log(x+1)x^3}{x^2-1} - \frac{c_1^3x^3}{(x^2-1)\left(c_1^2 + 2\log(x+1)c_1 + \log^2(x+1) + 1\right)} - \frac{}{(x^2-1)\left(c_1^2 +\right.}\right.\right.$$

✓ **Maple** : cpu = 1.95 (sec), leaf count = 239

$$\left\{y(x) = \arctan\left(\frac{1}{\_C1^2 - 2\_C1\ \ln(1+x) + (\ln(1+x))^2 + 1}\left((-\ln(1+x) + \_C1)\sqrt{(\ln(1+x))^2 - 2\_C1\ \ln}\right.\right.\right.$$

2.743 ODE No. 743

$$y'(x) = -\frac{i\left(x^4 + 8x^2y(x)^2 + 16y(x)^4 + 8ix\right)}{32y(x)}$$

✗ **Mathematica** : cpu = 46.8911 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-I/32)*((8*I)*x + x^4 + 8*x^2*y[x]^2 + 16*y[x]^4))/y[x], y[x
```

✓ **Maple** : cpu = 0.57 (sec), leaf count = 301

$$\left\{y(x) = -i\sqrt{-i\left(-2\left(-\sqrt{3}+i\right)\_C1\ \mathrm{Ai}^{(1)}\left(1/2\left(-\sqrt{3}+i\right)x\right) + \left(2\sqrt{3}-2i\right)\mathrm{Bi}^{(1)}\left(\frac{\left(-\sqrt{3}+i\right)x}{2}\right) + ix^2\left(A\right.\right.\right.\right.$$

2.744 ODE No. 744

$$y'(x) = \frac{x}{x^4 + 2x^2y(x)^2 + y(x)^4 - y(x)}$$

✓ **Mathematica** : cpu = 0.0427691 (sec), leaf count = 510

$$\left\{\left\{y(x) \to \frac{\sqrt[3]{144c_1x^2 + \sqrt{4\left(12x^2 - 4c_1^2\right)^3 + \left(144c_1x^2 + 16c_1^3 - 108\right)^2} + 16c_1^3 - 108}}{6\sqrt[3]{2}} - \frac{}{3\ 2^{2/3}\sqrt[3]{144c_1x^2 + \sqrt{4\left(\right.}}\right.\right.$$

✓ **Maple** : cpu = 0.243 (sec), leaf count = 621

$$\left\{y(x) = \frac{1}{12}\left(-2\_C1\ \sqrt[3]{-36\,x^2\_C1 - 54 - \_C1^3 + 6\sqrt{48\,x^6 + 24\,x^4\_C1^2 + \left(3\_C1^4 + 108\,\_C1\right)x^2 + 3\_C1}\right.\right.$$

2.745 ODE No. 745

$$y'(x) = \frac{(y(x)\log(x) - 1)^3}{x(-y(x) + y(x)\log(x) - 1)}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.071 (sec), leaf count = 78

$$\left\{y(x) = \frac{47\ RootOf\left(-27783\int^{-Z}\left(2209\_a^3 - 9261\_a + 9261\right)^{-1}d\_a - 7\ln(x) + 3\_C1\right) - 84}{(47\ln(x) - 47)\ RootOf\left(-27783\int^{-Z}(2209\_a^3 - 9261\_a + 9261)^{-1}d\_a - 7\ln(x) + 3\_C1\right) - 84\ \ln}\right.$$

2.746 ODE No. 746

$$y'(x) = -\frac{i\left(x^4 + 2x^2y(x)^2 + y(x)^4 + ix\right)}{y(x)}$$

✗ **Mathematica** : cpu = 45.6394 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-I)*(I*x + x^4 + 2*x^2*y[x]^2 + y[x]^4))/y[x], y[x], x]
```

✓ **Maple** : cpu = 0.489 (sec), leaf count = 243

$$\left\{y(x) = \frac{-i\sqrt{2}}{2\,\mathrm{Ai}\left(-\sqrt[3]{-8\,i}x\right)\_C1 + 2\,\mathrm{Bi}\left(-\sqrt[3]{-8\,i}x\right)}\sqrt{-2\,i\left(\mathrm{Ai}\left(-\sqrt[3]{-8\,i}x\right)\_C1 + \mathrm{Bi}\left(-\sqrt[3]{-8\,i}x\right)\right)\left(-\frac{\_C1\ (-\sqrt{3}}{}\right.}\right.$$

2.747 ODE No. 747

$$y'(x) = -\frac{y(x)\cot(x)\left(x^2 y(x)(-\log(2x)) + x\log(2x) + \tan(x)\right)}{x}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.358 (sec), leaf count = 75

$$\left\{y(x) = 1e^{\int \frac{-x\ln(x)-x\ln(2)-\tan(x)}{x\tan(x)}\,dx}\left(\int -\frac{x(\ln(2)+\ln(x))}{\tan(x)}e^{\int \frac{-x\ln(x)-x\ln(2)-\tan(x)}{x\tan(x)}\,dx}\,dx + \_C1\right)^{-1}\right\}$$

2.748 ODE No. 748

$$y'(x) = \frac{y(x)(y(x)+x)}{x\left(y(x)^3+x\right)}$$

✓ **Mathematica** : cpu = 0.305387 (sec), leaf count = 285

$$\left\{\left\{y(x) \to \frac{2\sqrt[3]{2}(c_1+\log(x))}{\sqrt[3]{\sqrt{2916x^2 - 864\left(c_1+\log(x)\right)^3}+54x}} + \frac{\sqrt[3]{\sqrt{2916x^2 - 864\left(c_1+\log(x)\right)^3}+54x}}{3\sqrt[3]{2}}\right\}, \left\{y(x) \to -\frac{}{\sqrt[3]{}}\right.$$

✓ **Maple** : cpu = 0.107 (sec), leaf count = 404

$$\left\{y(x) = \frac{1}{6}\left(\left(i\left(27x + 3\sqrt{-24\_C1^3 - 72\_C1^2\ln(x) - 72\_C1\,(\ln(x))^2 - 24\,(\ln(x))^3 + 81x^2}\right)^{\frac{2}{3}} - 6i\_C1 -\right.\right.\right.$$

2.749 ODE No. 749

$$y'(x) = \frac{x(x-y(x))^2(y(x)+x)^2}{y(x)}$$

✓ **Mathematica** : cpu = 0.0998584 (sec), leaf count = 126

$$\left\{\left\{y(x) \to -\frac{\sqrt{x^2e^{4c_1+2x^2} - e^{4c_1+2x^2} + x^2 + 1}}{\sqrt{e^{4c_1+2x^2}+1}}\right\}, \left\{y(x) \to \frac{\sqrt{x^2e^{4c_1+2x^2} - e^{4c_1+2x^2} + x^2 + 1}}{\sqrt{e^{4c_1+2x^2}+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 192

$$\left\{y(x)=1\sqrt{\left(\_C1\,\mathrm{e}^{-\frac{x^2\left(x^2-2\right)}{2}}+\mathrm{e}^{-\frac{x^2\left(x^2+2\right)}{2}}\right)\left(\left(x^2+1\right)\mathrm{e}^{-\frac{x^2\left(x^2+2\right)}{2}}+\_C1\ \left(x^2-1\right)\mathrm{e}^{-\frac{x^2\left(x^2-2\right)}{2}}\right)\left(\_C1\,\mathrm{e}^{-\frac{x^2\left(x^2-2\right)}{2}}\right.}\right.$$

2.750 ODE No. 750

$$y'(x)=\frac{y(x)\left(x^2+3y(x)^2\right)}{x\left(6y(x)^2+x\right)}$$

✓ **Mathematica** : cpu = 0.327047 (sec), leaf count = 72

$$\left\{\left\{y(x)\to-\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1+2x}}{x}\right)}}{\sqrt{6}}\right\},\left\{y(x)\to\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1+2x}}{x}\right)}}{\sqrt{6}}\right\}\right\}$$

✓ **Maple** : cpu = 0.265 (sec), leaf count = 49

$$\left\{\left((y(x))^{-2}+6\,x^{-1}\right)^{-1}=\frac{x}{54}\left(\mathrm{e}^{RootOf\left(-\mathrm{e}^{\_Z}\ln\left(\frac{\left(\mathrm{e}^{\_Z}+9\right)x}{2}\right)+3\,\_C1\,\mathrm{e}^{\_Z}+\_Z\,\mathrm{e}^{\_Z}+2\,x\mathrm{e}^{\_Z}+9\right)}+9\right)\right\}$$

2.751 ODE No. 751

$$y'(x)=\frac{y(x)\left(x^4+x\log(y(x))+\log(y(x))\right)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.0728926 (sec), leaf count = 30

$$\left\{\left\{y(x)\to(x+1)^x e^{c_1x+\frac{x^3}{2}-x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.114 (sec), leaf count = 26

$$\left\{y(x)=\frac{(1+x)^x\,\mathrm{e}^{x\_C1}}{\mathrm{e}^{x^2}}\mathrm{e}^{\frac{x^3}{2}}\right\}$$

2.752 ODE No. 752

$$y'(x) = \frac{\cos(y(x))\left(x^3\cos(y(x)) - x - 1\right)}{(x+1)(x\sin(y(x)) - 1)}$$

✗ **Mathematica** : cpu = 31.5869 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == (Cos[y[x]]*(-1 - x + x^3*Cos[y[x]]))/((1 + x)*(-
1 + x*Sin[y[x]])), y[x], x]
```

✓ **Maple** : cpu = 1.624 (sec), leaf count = 723

$$\left\{y(x) = \arctan\left(\frac{1}{36\,(\ln(1+x))^2 + (-24x^3 + 36x^2 - 72\_C1 - 72x)\ln(1+x) + 4x^6 - 12x^5 + 33x^4 + (24\_C}\right.$$

2.753 ODE No. 753

$$y'(x) = \frac{y(x)\log(y(x))\left(x^4\log(y(x)) + x + 1\right)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.100809 (sec), leaf count = 41

$$\left\{\left\{y(x) \to \exp\left(-\frac{12x}{-12c_1 + 3x^4 - 4x^3 + 6x^2 - 12x + 12\log(x+1)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 38

$$\left\{y(x) = \mathrm{e}^{-12\frac{x}{3x^4 - 4x^3 + 6x^2 + 12\ln(1+x) - 12\_C1 - 12x}}\right\}$$

2.754 ODE No. 754

$$y'(x) = \frac{x^3 + xy(x)^2 + xy(x) + y(x)^3}{x^2}$$

✓ **Mathematica** : cpu = 0.0315477 (sec), leaf count = 47

$$\text{Solve}\left[\text{RootSum}\left[\#1^3 + \#1^2 + 1\&, \frac{\log\left(\frac{y(x)}{x} - \#1\right)}{3\#1^2 + 2\#1}\&\right] = c_1 + x, y(x)\right]$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 26

$$\left\{y(x) = \mathit{RootOf}\left(-\int^{\_Z}\left(\_a^3 + \_a^2 + 1\right)^{-1} d\_a + x + \_C1\right)x\right\}$$

2.755 ODE No. 755

$$y'(x) = \frac{y(x)^{3/2}}{x^2 - 2xy(x) + y(x)^2 + y(x)^{3/2}}$$

✓ **Mathematica** : cpu = 0.187475 (sec), leaf count = 2633

$$\left\{\left\{y(x) \to \frac{2}{3}\left(x + e^{c_1} + 2e^{2c_1}\right) - \frac{1}{3}\sqrt[3]{x^3 + 3e^{c_1}x^2 - 12e^{2c_1}x^2 + 3e^{2c_1}x + 12e^{3c_1}x + 48e^{4c_1}x + e^{3c_1} - 30e^{4c_1} - 96e^{5}\right.\right.$$

✓ **Maple** : cpu = 0.165 (sec), leaf count = 44

$$\left\{2\frac{\sqrt{y(x)}}{y(x) - x} + (y(x) - x)^{-1} - 2\frac{x}{\sqrt{y(x)}\,(y(x) - x)} - \_C1 = 0\right\}$$

2.756 ODE No. 756

$$y'(x) = \frac{x^6 + 2x^3y(x) + x^2y(x)^2 + y(x)^3}{x^4}$$

✓ **Mathematica** : cpu = 0.0765612 (sec), leaf count = 95

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{3y(x)}{x^4} + \frac{1}{x^2}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^6}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{1}{9}29^{2/3}\left(\frac{1}{x^6}\right)^{2/3}x^5, y(x)\right]$$

✓ **Maple** : cpu = 0.034 (sec), leaf count = 37

$$\left\{y(x) = \frac{\left(-3 + 29\,RootOf\left(-81\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1}d\_a + x + 3\_C1\right)\right)x^2}{9}\right\}$$

2.757 ODE No. 757

$$y'(x) = \frac{x^3 + 2x^2 - 4xy(x) - 4x - 8}{2x^2 - 8y(x) + 4x - 8}$$

✓ **Mathematica** : cpu = 0.031124 (sec), leaf count = 36

$$\left\{\left\{y(x) \to 2\left(W\left(-e^{c_1 - \frac{x}{4} - 1}\right) + 1\right) + \frac{1}{4}(x^2 + 2x - 4)\right\}\right\}$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 26

$$\left\{y(x) = \frac{x^2}{4} + 2\, lambertW\left(1/2\_C1\, e^{-x/4} e^{-1/2}\right) + \frac{x}{2} + 1\right\}$$

2.758 ODE No. 758

$$y'(x) = \frac{y(x)\left(x^3 y(x) + 2x + 2\right)}{(x+1)(\log(y(x)) + 2x - 1)}$$

✓ **Mathematica** : cpu = 0.929252 (sec), leaf count = 459

$$\left\{\left\{y(x) \to \frac{6W\left(-\frac{1}{6}\sqrt[6]{e^{-12x}\left(6c_1 + 2x^3 - 3x^2 + 6x - 6\log(x+1)\right)^6}\right)}{6c_1 + 2x^3 - 3x^2 + 6x - 6\log(x+1)}\right\}, \left\{y(x) \to \frac{6W\left(\frac{1}{6}\sqrt[6]{e^{-12x}\left(6c_1 + 2x^3 - 3\right.}\right.}{6c_1 + 2x^3 - 3x^2 + 6}\right.$$

✓ **Maple** : cpu = 0.247 (sec), leaf count = 41

$$\left\{y(x) = e^{-lambertW\left(-\frac{\left(-2x^3 + 3x^2 + 6\ln(1+x) + 6\_C1 - 6x\right)e^{-2x}}{6}\right) - 2x}\right\}$$

2.759 ODE No. 759

$$y'(x) = -\frac{ix\left(x^8 + 18x^4 y(x)^2 + 54ix^2 + 81y(x)^4\right)}{243y(x)}$$

✗ **Mathematica** : cpu = 40.7694 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-I/243)*x*((54*I)*x^2 + x^8 + 18*x^4*y[x]^2 + 81*y[x]^4))/y[
```

✓ **Maple** : cpu = 0.704 (sec), leaf count = 315

$$\left\{y(x) = \frac{-\frac{1}{6} - \frac{i}{6}}{x}\sqrt{(1-i)\left(J_{\frac{1}{3}}\left(\left(\frac{2}{27} - \frac{2i}{27}\right)\sqrt{6}x^3\right)\_C1 + Y_{\frac{1}{3}}\left(\left(\frac{2}{27} - \frac{2i}{27}\right)\sqrt{6}x^3\right)\right)\left((-27 - 27i - (1-i)x^6\right.}\right.$$

2.760 ODE No. 760

$$y'(x) = \frac{\left(xy(x)^2+1\right)^3}{x^4 y(x)\left(xy(x)^2+x+1\right)}$$

✓ **Mathematica** : cpu = 1.27325 (sec), leaf count = 112

$$\text{Solve}\left[2\left(\frac{1}{10}\log\left(2x^2y(x)^4+2x^2y(x)^2+x^2+4xy(x)^2+2x+2\right)-\frac{1}{5}\log\left(xy(x)^2-x+1\right)-\frac{1}{10}\tan^{-1}\left(2xy(x)^4+\right.\right.\right.$$

✓ **Maple** : cpu = 1.639 (sec), leaf count = 136

$$\left\{-\frac{(-1+y(x))\left(2\left(y(x)\right)^4+2\left(y(x)\right)^2+1\right)\left(\ln\left(2x^2\left(y(x)\right)^4+\left(2x^2+4x\right)\left(y(x)\right)^2+x^2+2x+2\right)x-\arctan\left(2\right.\right.}{5x\left(2\left(y\right.\right.}\right.$$

2.761 ODE No. 761

$$y'(x) = \frac{-x^3+4x^2-4xy(x)-4x+8}{2x^2+8y(x)-8x+8}$$

✓ **Mathematica** : cpu = 0.0248463 (sec), leaf count = 33

$$\left\{\left\{y(x)\to W\left(-e^{c_1-x-1}\right)+\frac{1}{4}\left(-x^2+4x-4\right)+1\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 18

$$\left\{y(x) = -\frac{x^2}{4}+lambertW\left(\frac{\_C1}{\mathrm{e}^x}\right)+x\right\}$$

2.762 ODE No. 762

$$y'(x) = -\frac{y(x)(x\log(y(x))+\log(y(x))-x)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.0598306 (sec), leaf count = 26

$$\left\{\left\{y(x)\to(x+1)^{-1/x}e^{1-\frac{c_1}{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.112 (sec), leaf count = 22

$$\left\{y(x) = \frac{\mathrm{e}}{\sqrt[x]{1+x}}\mathrm{e}^{-\frac{\_C1}{x}}\right\}$$

2.763 ODE No. 763

$$y'(x) = \frac{y(x)(x\log(y(x)) + \log(y(x)) + x)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.0577452 (sec), leaf count = 22

$$\{\{y(x) \to x^x (x+1)^{-x} e^{c_1 x}\}\}$$

✓ **Maple** : cpu = 0.101 (sec), leaf count = 14

$$\left\{y(x) = \left(\frac{x\_C1}{1+x}\right)^x\right\}$$

2.764 ODE No. 764

$$y'(x) = \frac{y(x)\left(x^4 - x\log(y(x)) - \log(y(x))\right)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.0946113 (sec), leaf count = 50

$$\left\{\left\{y(x) \to (x+1)^{\frac{1}{x}} e^{-\frac{c_1}{x} + \frac{x^3}{4} - \frac{x^2}{3} + \frac{x}{2} - \frac{25}{12x} - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.126 (sec), leaf count = 36

$$\left\{y(x) = \mathrm{e}^{\frac{x^3}{4}} \mathrm{e}^{-\frac{x^2}{3}} \mathrm{e}^{\frac{x}{2}} \sqrt[x]{1+x}\, \mathrm{e}^{\frac{-C1}{x}} \mathrm{e}^{-1}\right\}$$

2.765 ODE No. 765

$$y'(x) = \frac{y(x)\left(xy(x)\log\left(\frac{(x-1)(x+1)}{x}\right) - \log\left(\frac{(x-1)(x+1)}{x}\right) - 1\right)}{x}$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.208 (sec), leaf count = 106

$$\left\{y(x) = \frac{\mathrm{e}^{dilog(1+x)} x^{\ln(1+x)}}{\mathrm{e}^{dilog(x)} x} \mathrm{e}^{-\frac{(\ln(x))^2}{2}} \left(\int -\frac{\mathrm{e}^{dilog(1+x)} x^{\ln(1+x)}}{\mathrm{e}^{dilog(x)} x} \mathrm{e}^{-\frac{(\ln(x))^2}{2}} \ln\left(\frac{(1+x)(x-1)}{x}\right) \left(x^{\ln\left(\frac{(1+x)(x-1)}{x}\right)}\right)^{-1} \mathrm{d}x\right.\right.$$

2.766 ODE No. 766

$$y'(x) = \frac{y(x)\left(x^2 y(x)\log\left(\frac{(x-1)(x+1)}{x}\right) - x\log\left(\frac{(x-1)(x+1)}{x}\right) - \log(x)\right)}{x\log(x)}$$

✗ **Mathematica** : cpu = 300.023 (sec), leaf count = 0 , timed out

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```

✓ **Maple** : cpu = 0.256 (sec), leaf count = 89

$$\left\{y(x) = 1\mathrm{e}^{\int \frac{1}{x\ln(x)}\left(-x\ln\left(\frac{(1+x)(x-1)}{x}\right)-\ln(x)\right)\mathrm{d}x}\left(\int -\frac{x}{\ln(x)}\mathrm{e}^{\int \frac{1}{x\ln(x)}\left(-x\ln\left(\frac{(1+x)(x-1)}{x}\right)-\ln(x)\right)\mathrm{d}x}\ln\left(\frac{(1+x)(x-1)}{x}\right)\mathrm{d}x\right.\right.$$

2.767 ODE No. 767

$$y'(x) = \frac{-x^3 + 2x^2 - 8xy(x) - 8x + 32}{4x^2 + 32y(x) - 8x + 32}$$

✓ **Mathematica** : cpu = 0.0267175 (sec), leaf count = 38

$$\left\{\left\{y(x) \to 4\left(W\left(-e^{c_1 - \frac{x}{16} - 1}\right) + 1\right) + \frac{1}{8}\left(-x^2 + 2x - 8\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 26

$$\left\{y(x) = -\frac{x^2}{8} + 4\,lambertW\left(1/4\_C1\,\mathrm{e}^{-x/16}\mathrm{e}^{-3/4}\right) + \frac{x}{4} + 3\right\}$$

2.768 ODE No. 768

$$y'(x) = \frac{y(x)(y(x)+1)}{x(xy(x) - y(x) - 1)}$$

✓ **Mathematica** : cpu = 0.985909 (sec), leaf count = 66

$$\text{Solve}\left[\frac{2^{2/3}\left(xy(x)\left(-\log\left(\frac{xy(x)}{(x-1)y(x)-1}\right) + \log\left(\frac{y(x)+1}{-xy(x)+y(x)+1}\right) + \log(x) + 1\right) - 1\right)}{9xy(x)} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.11 (sec), leaf count = 26

$$\left\{y(x) = -\left(x\,lambertW\left(\frac{1}{x\mathrm{e}^{x^{-1}}\_C1}\right) + 1\right)^{-1}\right\}$$

2.769 ODE No. 769

$$y'(x) = -\frac{ix\left(x^8 + 8x^4y(x)^2 + 16ix^2 + 16y(x)^4\right)}{32y(x)}$$

✗ **Mathematica** : cpu = 42.6344 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-I/32)*x*((16*I)*x^2 + x^8 + 8*x^4*y[x]^2 + 16*y[x]^4))/y[x]
```

✓ **Maple** : cpu = 0.547 (sec), leaf count = 251

$$\left\{y(x) = -\frac{\sqrt{4}}{2x}\sqrt{\left(-2\ (1/8\,x^6+i)\ \_C1\ J_{1/3}\left((1/3-i/3)\,x^3\right) + \left(-\frac{x^6}{4}-2\,i\right)Y_{\frac{1}{3}}\left(\left(\frac{1}{3}-\frac{i}{3}\right)x^3\right) + (1+i)\,x^3\left(J_{\frac{4}{3}}\right.\right.\right.$$

2.770 ODE No. 770

$$y'(x) = \frac{2y(x)^6}{32x^2y(x)^4 + y(x)^3 + 16xy(x)^2 + 2}$$

✓ **Mathematica** : cpu = 0.126638 (sec), leaf count = 705

$$\left\{\left\{y(x) \to \frac{\sqrt[3]{18432c_1^2x^2 + \sqrt{4\left(192c_1^2x - 12c_1 - 256x^2\right)^3 + \left(18432c_1^2x^2 - 2880c_1x + 8192x^3 + 108\right)^2} - 2880c_1x}}{3\sqrt[3]{2}\,(1-16c_1x)}\right.\right.$$

✓ **Maple** : cpu = 0.132 (sec), leaf count = 1105

$$\left\{y(x) = \frac{1}{96\,x + 6\,\_C1}\left(32\,x\,\_C1\ \sqrt[3]{96\ (\_C1/16 + x)\,\sqrt{3}\sqrt{(4096\,x^3+27)\,\_C1^4 + 576\,x\,\_C1^3 + 2048\,\_C1^2x^2 +}}\right.\right.$$

2.771 ODE No. 771

$$y'(x) = \frac{-a^2x^3 - 2abx^2 - 4axy(x) - 4ax + 8}{2ax^2 + 4bx + 8y(x) + 8}$$

✓ **Mathematica** : cpu = 0.0339719 (sec), leaf count = 46

$$\left\{\left\{y(x) \to \frac{1}{4}(-ax^2 - 2bx - 4) - \frac{2\left(W\left(-e^{-\frac{b^2x}{4}+c_1-1}\right)+1\right)}{b}\right\}\right\}$$

✓ **Maple** : cpu = 0.111 (sec), leaf count = 84

$$\left\{y(x)=\frac{1}{4\,b}\left(-ax^2b-2\,b^2x-4\,b+4\,\mathrm{e}^{1/4\,\frac{1}{a}\left(-4\,lambertW\left(-1/2\,\mathrm{e}^{-1/4\,b^2x}\mathrm{e}^{-1/2\,\frac{-C1\,b^2}{a}}\mathrm{e}^{-b/2}\mathrm{e}^{-1}\right)a+\left(-b^2x-2\,b-4\right)a-2\,\_C1\,b^2\right)}\right)\right\}$$

2.772 ODE No. 772

$$y'(x)=\frac{y(x)\log(y(x))(x\log(y(x))+x+1)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.0631632 (sec), leaf count = 21

$$\left\{\left\{y(x)\to e^{\frac{x}{c_1-x+\log(x+1)}}\right\}\right\}$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 18

$$\left\{y(x)=\mathrm{e}^{\frac{x}{\ln(1+x)+\_C1-x}}\right\}$$

2.773 ODE No. 773

$$y'(x)=\frac{y(x)^2+xy(x)+x}{(x-1)(y(x)+x)}$$

✓ **Mathematica** : cpu = 0.0475909 (sec), leaf count = 61

$$\text{Solve}\left[\frac{1}{2}\log\left(\frac{y(x)^2}{x^2}+\frac{y(x)}{x}+1\right)+\frac{\tan^{-1}\left(\frac{\frac{2y(x)}{x}+1}{\sqrt{3}}\right)}{\sqrt{3}}=c_1+\log(1-x)-\log(x),y(x)\right]$$

✓ **Maple** : cpu = 0.247 (sec), leaf count = 48

$$\left\{y(x)=\frac{\sqrt{3}x}{2}\tan\left(RootOf\left(-\sqrt{3}\ln\left(\frac{3\,x^2\left(\left(\tan\left(\_Z\right)\right)^2+1\right)}{4\,\left(x-1\right)^2}\right)+2\sqrt{3}\_C1-2\,\_Z\right)\right)-\frac{x}{2}\right\}$$

2.774 ODE No. 774

$$y'(x) = \frac{-2ax^2 - x^3 - 4xy(x) - 4x + 8}{4ax + 2x^2 + 8y(x) + 8}$$

✓ **Mathematica** : cpu = 0.0302556 (sec), leaf count = 45

$$\left\{\left\{y(x) \to \frac{1}{4}(-2ax - x^2 - 4) - \frac{2\left(W\left(-e^{-\frac{a^2 x}{4} + c_1 - 1}\right) + 1\right)}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 51

$$\left\{y(x) = \frac{1}{4\,a}\left(-2\,a^2 x - a x^2 - 8\,lambertW\left(-1/2\,\mathrm{e}^{-1/4\,a^2 x}\mathrm{e}^{-a/2}\mathrm{e}^{-1}\mathrm{e}^{1/4\,\_C1\,a^2}\right) - 4\,a - 8\right)\right\}$$

2.775 ODE No. 775

$$y'(x) = \frac{-y(x) + \sqrt{y(x)} + x}{-y(x) + \sqrt{y(x)} + x + 1}$$

✓ **Mathematica** : cpu = 0.0997666 (sec), leaf count = 943

$$\{\{y(x) \to \text{Root}\left[x^6 - 2e^{3c_1}x^3 + e^{6c_1} + \#1^6 + (-6x - 6)\#1^5 + \left(15x^2 + 24x + 9\right)\#1^4 + \left(-20x^3 - 36x^2 - 18x + 2\right.\right.$$

✓ **Maple** : cpu = 0.091 (sec), leaf count = 32

$$\left\{\sqrt{y\left(x\right) - 2\sqrt{y\left(x\right)} - x}\left(y(x) + \sqrt{y\left(x\right)} - x\right) - \_C1 = 0\right\}$$

2.776 ODE No. 776

$$y'(x) = \frac{y(x)\left(x^2 y(x)\log\left(\frac{x^2+1}{x}\right) - x\log\left(\frac{x^2+1}{x}\right) - \log\left(\frac{1}{x}\right)\right)}{x\log\left(\frac{1}{x}\right)}$$

✗ **Mathematica** : cpu = 300.028 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.934 (sec), leaf count = 96

$$\left\{y(x) = 1\mathrm{e}^{\int \frac{1}{x\ln\left(x^{-1}\right)}\left(-\ln\left(\frac{x^2+1}{x}\right)x - \ln\left(x^{-1}\right)\right)\mathrm{d}x}\left(\int -\frac{x}{\ln\left(x^{-1}\right)}\mathrm{e}^{\int \frac{1}{x\ln\left(x^{-1}\right)}\left(-\ln\left(\frac{x^2+1}{x}\right)x - \ln\left(x^{-1}\right)\right)\mathrm{d}x}\ln\left(\frac{x^2+1}{x}\right)\mathrm{d}x + \_\right.\right.$$

2.777 ODE No. 777

$$y'(x) = \frac{y(x)(y(x)+1)}{x\left(xy(x)^4 - y(x) - 1\right)}$$

✓ **Mathematica** : cpu = 0.0910003 (sec), leaf count = 39

$$\text{Solve}\left[-\frac{1}{2}(y(x)+1)^2 + 2(y(x)+1) - \frac{1}{xy(x)} - \log(y(x)+1) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.139 (sec), leaf count = 51

$$\left\{y(x) = \mathrm{e}^{RootOf\left(x\left(\mathrm{e}^{-Z}\right)^3 - 5x\left(\mathrm{e}^{-Z}\right)^2 + 2x\_C1\,\mathrm{e}^{-Z} + 2\_Z x\mathrm{e}^{-Z} + 7x\mathrm{e}^{-Z} - 2x\_C1 - 2\_Z x - 3x + 2\right)} - 1\right\}$$

2.778 ODE No. 778

$$y'(x) = \frac{x^9 y(x)^3 + x^6 y(x)^2 - 3x^2 y(x) + 1}{x^3}$$

✓ **Mathematica** : cpu = 0.0701375 (sec), leaf count = 95

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3x^6 y(x) + x^3}{\sqrt[3]{29}\sqrt[3]{x^9}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{29^{2/3}\left(x^9\right)^{2/3}}{9x^5}, y(x)\right]$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 37

$$\left\{y(x) = \frac{-3 + 29\,RootOf\left(-81\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1} d\_a + x + 3\_C1\right)}{9x^3}\right\}$$

2.779 ODE No. 779

$$y'(x) = \frac{x^3 y(x) + x^3 + xy(x)^2 + y(x)^3}{(x-1)x^3}$$

✓ **Mathematica** : cpu = 0.0322996 (sec), leaf count = 57

$$\text{Solve}\left[-\frac{1}{4}\log\left(\frac{y(x)^2}{x^2} + 1\right) + \frac{1}{2}\log\left(\frac{y(x)}{x} + 1\right) + \frac{1}{2}\tan^{-1}\left(\frac{y(x)}{x}\right) = c_1 + \log(1-x) - \log(x), y(x)\right]$$

✓ **Maple** : cpu = 0.11 (sec), leaf count = 50

$$\left\{-\frac{1}{4}\ln\left(\frac{(y(x))^2 + x^2}{x^2}\right) + \frac{1}{2}\arctan\left(\frac{y(x)}{x}\right) + \frac{1}{2}\ln\left(\frac{y(x)+x}{x}\right) - \ln(x-1) + \ln(x) - \_C1 = 0\right\}$$

2.780 ODE No. 780

$$y'(x) = \frac{x\sqrt{x^2+y(x)^2}+xy(x)+y(x)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.025157 (sec), leaf count = 15

$$\{\{y(x) \to x \sinh(c_1 + \log(x+1))\}\}$$

✓ **Maple** : cpu = 0.408 (sec), leaf count = 27

$$\left\{ \_C1 + \frac{1}{x\left(1+x\right)}\left(\sqrt{\left(y\left(x\right)\right)^2+x^2}+y(x)\right) = 0 \right\}$$

2.781 ODE No. 781

$$y'(x) = \frac{y(x)\left(x^4+x^3+3y(x)^2+x\right)}{x\left(6y(x)^2+x\right)}$$

✓ **Mathematica** : cpu = 0.509127 (sec), leaf count = 82

$$\left\{ \left\{ y(x) \to -\frac{\sqrt{x}\sqrt{W\left(6xe^{2c_1+\frac{2x^3}{3}+x^2}\right)}}{\sqrt{6}} \right\}, \left\{ y(x) \to \frac{\sqrt{x}\sqrt{W\left(6xe^{2c_1+\frac{2x^3}{3}+x^2}\right)}}{\sqrt{6}} \right\} \right\}$$

✓ **Maple** : cpu = 0.29 (sec), leaf count = 61

$$\left\{ \left(\left(y(x)\right)^{-2}+6\,x^{-1}\right)^{-1} = \frac{x}{54}\left(\mathrm{e}^{RootOf\left(2\,x^3\mathrm{e}^{-Z}+3\,x^2\mathrm{e}^{-Z}-3\,\mathrm{e}^{-Z}\ln\left(1/2\,\frac{\mathrm{e}^{-Z}+9}{x}\right)+9\_C1\,\mathrm{e}^{-Z}+3\_Z\,\mathrm{e}^{-Z}+27\right)}+9\right) \right\}$$

2.782 ODE No. 782

$$y'(x) = \frac{y(x)\coth\left(\frac{1}{x}\right)\left(x^2y(x)\log\left(\frac{x^2+1}{x}\right)-x\log\left(\frac{x^2+1}{x}\right)-\tanh\left(\frac{1}{x}\right)\right)}{x}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.546 (sec), leaf count = 96

$$\left\{ y(x) = 1\mathrm{e}^{\int \frac{1}{x\tanh\left(x^{-1}\right)}\left(-\ln\left(\frac{x^2+1}{x}\right)x-\tanh\left(x^{-1}\right)\right)\mathrm{d}x}\left(\int -\frac{x}{\tanh\left(x^{-1}\right)}\mathrm{e}^{\int \frac{1}{x\tanh\left(x^{-1}\right)}\left(-\ln\left(\frac{x^2+1}{x}\right)x-\tanh\left(x^{-1}\right)\right)\mathrm{d}x}\ln\left(\frac{x^2+1}{x}\right.\right.\right.$$

2.783 ODE No. 783

$$y'(x) = -\frac{y(x)\coth(x)\left(x^2 y(x)(-\log(2x)) + x\log(2x) + \tanh(x)\right)}{x}$$

✗ **Mathematica** : cpu = 300.036 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.238 (sec), leaf count = 75

$$\left\{y(x) = 1\mathrm{e}^{\int \frac{-x\ln(x)-x\ln(2)-\tanh(x)}{x\tanh(x)}\,\mathrm{d}x}\left(\int -\frac{x(\ln(2)+\ln(x))}{\tanh(x)}\mathrm{e}^{\int \frac{-x\ln(x)-x\ln(2)-\tanh(x)}{x\tanh(x)}\,\mathrm{d}x}\,\mathrm{d}x + \_C1\right)^{-1}\right\}$$

2.784 ODE No. 784

$$y'(x) = \operatorname{csch}(x)\left(x^2\log(x) + 2xy(x)\log(x) + y(x)^2\log(x) + \log(x) - \sinh(x)\right)$$

✗ **Mathematica** : cpu = 300.116 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 36.043 (sec), leaf count = 24

$$\left\{y(x) = -x - \tan\left(\_C1 - \int \frac{\ln(x)}{\sinh(x)}\,\mathrm{d}x\right)\right\}$$

2.785 ODE No. 785

$$y'(x) = \frac{x^2\sinh(x) + 2xy(x)\sinh(x) + y(x)^2\sinh(x) - \log(x) + \sinh(x)}{\log(x)}$$

✗ **Mathematica** : cpu = 300.031 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 123.082 (sec), leaf count = 24

$$\left\{y(x) = -x - \tan\left(\_C1 - \int \frac{\sinh(x)}{\ln(x)}\,\mathrm{d}x\right)\right\}$$

2.786 ODE No. 786

$$y'(x) = \frac{axy(x)^2 \cosh(x) + bx^3 \cosh(x) + y(x) \log(x)}{x \log(x)}$$

✗ **Mathematica** : cpu = 300.05 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.063 (sec), leaf count = 33

$$\left\{y(x) = \frac{x}{a} \tan\left(\sqrt{ab}\left(\_C1 + \int \frac{x \cosh(x)}{\ln(x)} \, dx\right)\right) \sqrt{ab}\right\}$$

2.787 ODE No. 787

$$y'(x) = \frac{x\left(2x^4 - 2x^2 y(x) + x^2 - x - 1\right)}{(x+1)\left(x^2 - y(x)\right)}$$

✓ **Mathematica** : cpu = 26.7009 (sec), leaf count = 484

$$\text{Solve}\left[\frac{2\ 2^{2/3}\left(2 - \frac{x\left(x^2-x-1\right)\left(2x^2-2y(x)+3\right)}{\sqrt[3]{x^3\left(x^2-x-1\right)^3\left(x^2-y(x)\right)}}\right)\left(\frac{x\left(x^2-x-1\right)\left(2x^2-2y(x)+3\right)}{\sqrt[3]{x^3\left(x^2-x-1\right)^3\left(x^2-y(x)\right)}} + 4\right)\left(\left(1 - \frac{x\left(x^2-x-1\right)\left(2x^2-2y(x)+3\right)}{2\sqrt[3]{x^3\left(x^2-x-1\right)^3\left(x^2-y(x)\right)}}\right)\log\left(\right.\right.}{9\left(-\frac{\left(2x^2-2y(x)+3\right)^3}{\left(x^2-y(x)\right)^3} + \frac{12x(x^2-x-}\right]$$

✓ **Maple** : cpu = 0.619 (sec), leaf count = 191

$$\left\{y(x) = 1\left(4x^2 \mathrm{e}^{RootOf\left(8x^3\mathrm{e}^{-Z} - 24x^2\mathrm{e}^{-Z} - 36x^3 + 6\ln\left(\frac{2\mathrm{e}^{-Z}-9}{(1+x)^4}\right)\mathrm{e}^{-Z} + 18\_C1\,\mathrm{e}^{-Z} - 6\_Z\,\mathrm{e}^{-Z} + 24x\mathrm{e}^{-Z} + 108x^2 - 27\ln\left(\frac{2\mathrm{e}^{-Z}-9}{(1+x)^4}\right) - 81\right.}\right.\right.$$

2.788 ODE No. 788

$$y'(x) = -\frac{y(x)\left(x^2 y(x)(-\coth(x+1)) + \log(x-1) + x\coth(x+1)\right)}{x\log(x-1)}$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.706 (sec), leaf count = 108

$$\left\{ y(x) = 1\left(\mathrm{e}^{-\int \frac{-\ln(x-1)\sinh(1+x)-x\cosh(1+x)}{\sinh(1+x)x\ln(x-1)}\,\mathrm{d}x}\right)^{-1}\left(\_C1 + \int -\frac{x\cosh(1+x)}{\ln(x-1)\sinh(1+x)}\mathrm{e}^{\int \frac{-\ln(x-1)\sinh(1+x)-x\cosh(1+x)}{\sinh(1+x)x\ln(x-1)}\,\mathrm{d}x}\right.\right.$$

2.789 ODE No. 789

$$y'(x) = \frac{x^2\coth(x+1) + 2xy(x)\coth(x+1) + y(x)^2\coth(x+1) - \log(x-1) + \coth(x+1)}{\log(x-1)}$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.790 ODE No. 790

$$y'(x) = \frac{x^4\coth\left(\frac{x+1}{x-1}\right) - 2x^2 y(x)\coth\left(\frac{x+1}{x-1}\right) + y(x)^2\coth\left(\frac{x+1}{x-1}\right) + 2x\log\left(\frac{1}{x-1}\right) - \coth\left(\frac{x+1}{x-1}\right)}{\log\left(\frac{1}{x-1}\right)}$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

```
$Aborted
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = (2*x*ln(1/(x-1))-coth((1+x)/(x-1))+coth((1+x)/(x-1))*y(x)^2-
2*coth((1+x)/(x-1))*x^2*y(x)+coth((1+x)/(x-1))*x^4)/ln(1/(x-1)),y(x))
```

2.791 ODE No. 791

$$y'(x) = \frac{\operatorname{sech}\left(\frac{1}{x-1}\right)\left(x^5 + x^4 - 2x^3 y(x) - 2x^2 y(x) + 2x^2 \cosh\left(\frac{1}{x-1}\right) + x y(x)^2 + y(x)^2 - x - 2x\cosh\left(\frac{1}{x-1}\right) - 1\right)}{x-1}$$

✗ **Mathematica** : cpu = 300.057 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 35.476 (sec), leaf count = 306

$$\left\{ y(x) = 1\left(\left(-x^2+1\right)\left(\mathrm{e}^{\frac{1}{\left(\mathrm{e}^{(x-1)^{-1}}\right)^2+1}\int \frac{\mathrm{e}^{(x-1)^{-1}}(1+x)}{\left(\left(\mathrm{e}^{(x-1)^{-1}}\right)^2+1\right)(x-1)}\,\mathrm{d}x}\right)^4 \left(\mathrm{e}^{\frac{1}{\left(\mathrm{e}^{(x-1)^{-1}}\right)^2+1}\int \frac{\mathrm{e}^{(x-1)^{-1}}(1+x)}{\left(\left(\mathrm{e}^{(x-1)^{-1}}\right)^2+1\right)(x-1)}\,\mathrm{d}x}\mathrm{e}^{2(x-1)^{-1}}\right.\right.$$

2.792 ODE No. 792

$$y'(x) = \frac{y(x)\operatorname{sech}\left(\frac{1}{x+1}\right)\left(x^3 y(x) + x^2 y(x) - x^2 - x - x\cosh\left(\frac{1}{x+1}\right) + \cosh\left(\frac{1}{x+1}\right)\right)}{(x-1)x}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.852 (sec), leaf count = 112

$$\left\{ y(x) = 1\mathrm{e}^{\int \frac{(1-x)\cosh\left((1+x)^{-1}\right)-x^2-x}{x(x-1)\cosh\left((1+x)^{-1}\right)}\,\mathrm{d}x}\left(\int -\frac{x(1+x)}{(x-1)\cosh\left((1+x)^{-1}\right)}\mathrm{e}^{\int \frac{(1-x)\cosh\left((1+x)^{-1}\right)-x^2-x}{x(x-1)\cosh\left((1+x)^{-1}\right)}\,\mathrm{d}x}\,\mathrm{d}x + \_C1\right)^{-1} \right\}$$

2.793 ODE No. 793

$$y'(x) = -\frac{y(x)(xy(x)+1)}{x(xy(x)-y(x)+1)}$$

✓ **Mathematica** : cpu = 15.1537 (sec), leaf count = 399

$$\text{Solve}\left[-\frac{\sqrt[3]{-2}\left(\frac{2^{2/3}((x-1)y(x)-2)}{\sqrt[3]{-\frac{1}{(x-1)^3}}(x-1)((x-1)y(x)+1)} + (-2)^{2/3}\right)\left(\frac{-xy(x)+y(x)+2}{\sqrt[3]{2}\sqrt[3]{-\frac{1}{(x-1)^3}}(x-1)((x-1)y(x)+1)} + (-2)^{2/3}\right)\left(\left(\frac{\sqrt[3]{-1}(-x}{\sqrt[3]{-\frac{1}{(x-1)^3}}(x}\right.\right.\right.$$

✓ **Maple** : cpu = 0.109 (sec), leaf count = 32

$$\left\{ y(x) = -2\,\frac{1}{x}\mathrm{e}^{-lambertW\left(-2\,\frac{(x-1)\left(\mathrm{e}^{-C1}\right)^{3}\mathrm{e}^{-1}}{x}\right)+3\_C1-1} \right\}$$

2.794 ODE No. 794

$$y'(x) = \frac{y(x)}{x\left(x^3y(x)^4 + x^2y(x)^3 + y(x) - 1\right)}$$

✓ **Mathematica** : cpu = 0.0861165 (sec), leaf count = 67

$$\text{Solve}\left[\text{RootSum}\left[\#1^3y(x)^3 + \#1^2y(x)^2 + 1\&, \frac{\#1y(x)\log(x-\#1) + \log(x-\#1)}{3\#1y(x)+2}\&\right] + y(x) - \log(x) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 2.51 (sec), leaf count = 32

$$\left\{ -y(x) + \int^{xy(x)} \frac{1}{\_a\left(\_a^3 + \_a^2 + 1\right)} d\_a - \_C1 = 0 \right\}$$

2.795 ODE No. 795

$$y'(x) = \frac{a^3 + 3a^2x + 3ax^2 + ay(x)^2 + x^3 + y(x)^3 + xy(x)^2}{(a+x)^3}$$

✓ **Mathematica** : cpu = 0.167906 (sec), leaf count = 111

$$\text{Solve}\left[-\frac{19}{3}\text{RootSum}\left[-19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log\left(\frac{\frac{3y(x)}{(a+x)^3} + \frac{1}{(a+x)^2}}{\sqrt[3]{38}\sqrt[3]{\frac{1}{(a+x)^6}}} - \#1\right)}{2\sqrt[3]{38} - 19\#1^2}\&\right] = \frac{1}{9}38^{2/3}\left(\frac{1}{(a+x)^6}\right)^{2/3}(a+x)\right.$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 37

$$\left\{ y(x) = -RootOf\left(-\int^{-Z}\left(\_a^3 - \_a^2 - \_a - 1\right)^{-1} d\_a + \ln(x+a) + \_C1\right)(x+a) \right\}$$

2.796 ODE No. 796

$$y'(x) = \frac{e^{-\frac{3x^2}{2}} x y(x)^3}{3\left(e^{\frac{3x^2}{2}} y(x) + 3e^{\frac{3x^2}{2}} + 3y(x)\right)}$$

✓ **Mathematica** : cpu = 16.1713 (sec), leaf count = 102

$$\text{Solve}\left[\frac{1}{62}\left(-31\log\left(9e^{\frac{3x^2}{2}}(y(x)+3)y(x) + 3e^{3x^2}(y(x)+3)^2 - y(x)^2\right) + 6\sqrt{93}\tanh^{-1}\left(\frac{\sqrt{\frac{3}{31}}\left(2e^{\frac{3x^2}{2}}(y(x)+3) -\right.}{y(x)}\right.\right.\right.$$

✓ **Maple** : cpu = 1.451 (sec), leaf count = 143

$$\left\{y(x) = \mathit{RootOf}\left(\left(\left(7\,\mathrm{e}^{3\,x^2+\mathit{RootOf}\left(\left(\mathrm{e}^{3/2\,x^2}\right)^2\left(42\,\sqrt{93}\tanh\left(\frac{(\_C1-5\_Z)\sqrt{93}}{90}\right)\mathrm{e}^{3\,x^2+\_Z}+217\left(\tanh\left(\frac{(\_C1-5\_Z)\sqrt{93}}{90}\right)\right)^2\mathrm{e}^{3\,x^2+\_Z}+189\right.\right.}\right.\right.\right.\right.$$

2.797 ODE No. 797

$$y'(x) = \frac{y(x)\left(x^3 y(x)\cosh\left(\frac{x+1}{x-1}\right) + x^2 y(x)\cosh\left(\frac{x+1}{x-1}\right) - x^2\cosh\left(\frac{x+1}{x-1}\right) - x\cosh\left(\frac{x+1}{x-1}\right) - 1\right)}{x}$$

✓ **Mathematica** : cpu = 2.0635 (sec), leaf count = 349

$$\left\{\left\{y(x) \to \frac{\exp\left(\frac{(3e^2-1)\text{Chi}\left(\frac{2}{x-1}\right)}{e} + \frac{(1+3e^2)\text{Shi}\left(\frac{2}{x-1}\right)}{e} - \frac{1}{4}ex^2\sinh\left(\frac{2}{x-1}\right) + \frac{x^2\sinh\left(\frac{2}{x-1}\right)}{4e} - \frac{1}{4}ex^2\cosh\left(\frac{2}{x-1}\right) - \frac{x^2\cos}{}\right.}{x\left(c_1\exp\left(\frac{(x-1)\left((-x+e^2(x+\right.}{}\right.\right.}\right.\right.$$

✓ **Maple** : cpu = 0.425 (sec), leaf count = 252

$$\left\{y(x) = \frac{1}{x}\mathrm{e}^{\frac{5\,\mathrm{e}}{4}\mathrm{e}^{2\,(x-1)^{-1}}}\mathrm{e}^{-\frac{\mathrm{e}x^2}{4}\mathrm{e}^{2\,(x-1)^{-1}}}\mathrm{e}^{\frac{\mathrm{e}^{-1}}{4}\mathrm{e}^{-2\,(x-1)^{-1}}}\mathrm{e}^{\mathrm{e}^{-1}\mathit{Ei}\left(1,2\,(x-1)^{-1}\right)}\mathrm{e}^{-\frac{\mathrm{e}^{-1}x^2}{4}\mathrm{e}^{-2\,(x-1)^{-1}}}\left(\mathrm{e}^{\mathrm{e}\mathrm{e}^{2\,(x-1)^{-1}}x}\right)^{-1}\left(\mathrm{e}^{\mathrm{e}\mathit{Ei}\left(1,-\right.}\right.\right.$$

2.798 ODE No. 798

$$y'(x) = \frac{y(x)(y(x)+x+1)}{(x+1)\left(2y(x)^3+y(x)+x\right)}$$

✓ **Mathematica** : cpu = 0.590975 (sec), leaf count = 27

$$\text{Solve}\left[y(x)^2 - \frac{x}{y(x)} + \log(y(x)) - \log(x+1) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.154 (sec), leaf count = 30

$$\left\{y(x) = \mathrm{e}^{RootOf\left(-\left(\mathrm{e}^{-Z}\right)^3+\ln(1+x)\mathrm{e}^{-Z}+\_C1\,\mathrm{e}^{-Z}-\_Z\,\mathrm{e}^{-Z}+x\right)}\right\}$$

2.799 ODE No. 799

$$y'(x) = \frac{y(x)\left(e^{\frac{x+1}{x-1}}x^3y(x) + e^{\frac{x+1}{x-1}}x^2y(x) - e^{\frac{x+1}{x-1}}x^2 - e^{\frac{x+1}{x-1}}x - 1\right)}{x}$$

✓ **Mathematica** : cpu = 0.304315 (sec), leaf count = 70

$$\left\{\left\{y(x) \to \frac{e^{6e\text{Ei}\left(\frac{2}{x-1}\right)}}{x\left(c_1e^{\frac{1}{2}e^{\frac{x}{x-1}+\frac{1}{x-1}}(x^2+4x-5)} + e^{6e\text{Ei}\left(\frac{2}{x-1}\right)}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.43 (sec), leaf count = 147

$$\left\{y(x) = \frac{1}{x}\mathrm{e}^{\frac{5}{2}\mathrm{e}^{\frac{1+x}{x-1}}}\mathrm{e}^{-\frac{x^2}{2}\mathrm{e}^{\frac{1+x}{x-1}}}\left(\mathrm{e}^{e\mathit{Ei}\left(1,-2\,(x-1)^{-1}\right)}\right)^{-6}\left(\mathrm{e}^{x\mathrm{e}^{\frac{1+x}{x-1}}}\right)^{-2}\left(\int -(1+x)\mathrm{e}^{\frac{1+x}{x-1}}\mathrm{e}^{\frac{5}{2}\mathrm{e}^{\frac{1+x}{x-1}}}\mathrm{e}^{-\frac{x^2}{2}\mathrm{e}^{\frac{1+x}{x-1}}}\left(\mathrm{e}^{e\mathit{Ei}\left(1,-2\,(x-1)\right.}\right.\right.\right.$$

2.800 ODE No. 800

$$y'(x) = \frac{-b^3+6b^2x-12bx^2-4by(x)^2+8x^3+8y(x)^3+8xy(x)^2}{(2x-b)^3}$$

✓ **Mathematica** : cpu = 0.188135 (sec), leaf count = 128

$$\text{Solve}\left[-\frac{19}{3}\text{RootSum}\left[-19\#1^3+6\sqrt[3]{38}\#1-19\&, \frac{\log\left(\frac{\frac{4}{(b-2x)^2}-\frac{24y(x)}{(b-2x)^3}}{4\sqrt[3]{38}\sqrt[3]{\frac{1}{(b-2x)^6}}}-\#1\right)}{2\sqrt[3]{38}-19\#1^2}\&\right] = \frac{1}{9}38^{2/3}\left(\frac{1}{(b-2x)^6}\right)^{2/3}(b-$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 41

$$\left\{y(x) = \frac{RootOf\left(-\int^{-Z}\left(\_a^3 - \_a^2 - \_a - 1\right)^{-1} d\_a + \ln\left(-2\,x + b\right) + \_C1\right)\left(-2\,x + b\right)}{2}\right\}$$

2.801 ODE No. 801

$$y'(x) = \frac{1}{2}e^{\frac{x^2}{4}}\left(2e^{-\frac{3x^2}{4}}y(x)^3 + 2e^{-\frac{x^2}{2}}y(x)^2 + e^{-\frac{x^2}{4}}xy(x) + 2\right)$$

✓ **Mathematica** : cpu = 0.106615 (sec), leaf count = 126

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3e^{-\frac{x^2}{2}}y(x) + e^{-\frac{x^2}{4}}}{\sqrt[3]{29}\sqrt[3]{e^{-\frac{3x^2}{4}}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{1}{9}29^{2/3}e^{\frac{x^2}{2}}\left(e^{-\frac{3x^2}{4}}\right)^{2/3}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 63

$$\left\{y(x) = \frac{1}{9}\left(-3\,\mathrm{e}^{-1/4\,x^2}\mathrm{e}^{1/4\,x^2} + 29\,RootOf\left(-81\int^{\_Z}\left(841\,\_a^3 - 27\,\_a + 27\right)^{-1} d\_a + x + 3\,\_C1\right)\right)\left(\mathrm{e}^{\frac{x^2}{4}}\right)^{-1}\right.$$

2.802 ODE No. 802

$$y'(x) = \frac{\_\mathrm{F1}\left(y(x) + \frac{1}{x}\right) + \frac{1}{x}}{x}$$

✓ **Mathematica** : cpu = 0.0774347 (sec), leaf count = 98

$$\text{Solve}\left[\int_1^{y(x)} -\frac{\_\mathrm{F1}\left(K[2] + \frac{1}{x}\right)\left(\int_1^x -\frac{\_\mathrm{F1}'\left(K[2] + \frac{1}{K[1]}\right)}{K[1]^2\left(\_\mathrm{F1}\left(K[2] + \frac{1}{K[1]}\right)\right)^2} dK[1]\right) + 1}{\_\mathrm{F1}\left(K[2] + \frac{1}{x}\right)} dK[2] + \int_1^x \left(\frac{1}{K[1]^2\_\mathrm{F1}\left(\frac{1}{K[1]} + y(x)\right)}\right.\right.$$

✓ **Maple** : cpu = 0.147 (sec), leaf count = 27

$$\left\{y(x) = \frac{RootOf\left(-\ln\left(x\right) + \int^{-Z}\left(\_F1\left(\_a\right)\right)^{-1} d\_a + \_C1\right)x - 1}{x}\right\}$$

2.803 ODE No. 803

$$y'(x) = \frac{\_\mathrm{F1}\left(y(x)^2 - 2\log(x)\right)}{x\sqrt{y(x)^2}}$$

✓ **Mathematica** : cpu = 0.0866959 (sec), leaf count = 634

$$\text{Solve}\left[\int_1^{y(x)} \left(-\int_1^x \left(\frac{2K[2]\left(\_\mathrm{F1}\left(K[2]^2 - 2\log(K[1])\right)\right)^2 \_\mathrm{F1}'\left(K[2]^2 - 2\log(K[1])\right)}{K[1]\left(\_\mathrm{F1}\left(K[2]^2 - 2\log(K[1])\right) - 1\right)^2 \left(\_\mathrm{F1}\left(K[2]^2 - 2\log(K[1])\right) + 1\right)} + \frac{2K[2]\left(\_\mathrm{F1}\right.}{K[1]\left(\_\mathrm{F1}\left(K[2\right.}\right.\right.\right.$$

✓ **Maple** : cpu = 0.598 (sec), leaf count = 65

$$\left\{y(x) = \sqrt{2\ln(x) + 2\,RootOf\left(\ln(x) - \int^{\_Z} \left(\_F1\left(2\_a\right) - 1\right)^{-1} d\_a + \_C1\right)}, y(x) = -\sqrt{2\ln(x) + 2\,RootOf\right.$$

2.804 ODE No. 804

$$y'(x) = \frac{\frac{1}{2}x^4\cos(2y(x)) + \frac{x^4}{2} - \frac{1}{2}x\sin(2y(x)) - \frac{1}{2}\sin(2y(x))}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.484363 (sec), leaf count = 43

$$\left\{\left\{y(x) \to \tan^{-1}\left(\frac{-12c_1 + 3x^4 - 4x^3 + 6x^2 - 12x + 12\log(x+1) - 25}{12x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 1.401 (sec), leaf count = 38

$$\left\{y(x) = \arctan\left(\frac{3\,x^4 - 4\,x^3 + 6\,x^2 + 12\,\ln(1+x) - 12\,\_C1 - 12\,x}{12\,x}\right)\right\}$$

2.805 ODE No. 805

$$y'(x) = \frac{x^4\sqrt{x^2 + y(x)^2} + xy(x) + y(x)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.0348681 (sec), leaf count = 37

$$\left\{\left\{y(x) \to x\sinh\left(\frac{1}{6}\left(6c_1 + 2x^3 - 3x^2 + 6x - 6\log(x+1) + 11\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.68 (sec), leaf count = 42

$$\left\{\ln\left(\sqrt{\left(y\left(x\right)\right)^2 + x^2} + y(x)\right) - \frac{x^3}{3} + \frac{x^2}{2} - x - \ln\left(x\right) + \ln\left(1+x\right) - \_C1 = 0\right\}$$

2.806 ODE No. 806

$$y'(x) = \frac{-\frac{1}{2}x\sin(2y(x)) - \frac{1}{2}\sin(2y(x)) + \frac{1}{2}x\cos(2y(x)) + \frac{x}{2}}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.275673 (sec), leaf count = 23

$$\left\{\left\{y(x) \to \tan^{-1}\left(\frac{-c_1 + x - \log(x+1) + 1}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.802 (sec), leaf count = 22

$$\left\{y(x) = -\arctan\left(\frac{-x + \ln(1+x) - \_C1}{x}\right)\right\}$$

2.807 ODE No. 807

$$y'(x) = -\frac{1}{-e^{y(x)}y(x)\_\mathrm{F1}(y(x) - \log(x)) - x}$$

✗ **Mathematica** : cpu = 1.81117 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == -(-x - E^y[x]*y[x]*_F1[-Log[x] + y[x]])^(-1), y[x], x]
```

✓ **Maple** : cpu = 0.821 (sec), leaf count = 43

$$\left\{\frac{(\ln(x))^2}{2} - y(x)\ln(x) - \int^{y(x)-\ln(x)} \frac{\_F1(\_a)\,\_a + \mathrm{e}^{-\_a}}{\_F1(\_a)} d\_a + \_C1 = 0\right\}$$

2.808 ODE No. 808

$$y'(x) = \frac{(y(x)+1)(2y(x)+1)}{x(2xy(x) - 2y(x) + x - 2)}$$

✓ **Mathematica** : cpu = 1.31948 (sec), leaf count = 149

$$\text{Solve}\left[\frac{2^{2/3}\left(x\log\left(-\frac{6\ 2^{2/3}(y(x)+1)}{2(x-1)y(x)+x-2}\right) - x\log\left(\frac{3\ 2^{2/3}(2xy(x)+x)}{2(x-1)y(x)+x-2}\right) + 2xy(x)\left(\log\left(-\frac{6\ 2^{2/3}(y(x)+1)}{2(x-1)y(x)+x-2}\right) - \log\left(\frac{3\ 2^{2/3}(2xy\right.\right.\right.}{9(2xy(x)+x)}$$

✓ **Maple** : cpu = 0.096 (sec), leaf count = 45

$$\left\{y(x) = 1\left(-x\,lambertW\left(\frac{1}{x\mathrm{e}^{x^{-1}}\_C1}\right) - 2\right)\left(2\,x\,lambertW\left(\frac{1}{x\mathrm{e}^{x^{-1}}\_C1}\right) + 2\right)^{-1}\right\}$$

2.809 ODE No. 809

$$y'(x) = \frac{64x^3 - 240x^2 + 64xy(x)^2 + 64y(x)^3 - 80y(x)^2 + 300x - 125}{(4x-5)^3}$$

✓ **Mathematica** : cpu = 0.167679 (sec), leaf count = 128

$$\text{Solve}\left[-\frac{19}{3}\text{RootSum}\left[-19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log\left(\frac{\frac{192y(x)}{(4x-5)^3} + \frac{16}{(4x-5)^2}}{16\sqrt[3]{38}\sqrt[3]{\frac{1}{(4x-5)^6}}} - \#1\right)}{2\sqrt[3]{38} - 19\#1^2}\&\right] = c_1 + \frac{1}{9}38^{2/3}\left(\frac{1}{(5-4x)^6}\right)^{2/3}\right]$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 41

$$\left\{y(x) = -\frac{RootOf\left(-\int^{-Z}\left(\_a^3 - \_a^2 - \_a - 1\right)^{-1} d\_a + \ln(4x-5) + \_C1\right)(4x-5)}{4}\right\}$$

2.810 ODE No. 810

$$y'(x) = \frac{x^2\log^2(x) + y(x)^2 + y(x) - 2xy(x)\log(x) + x}{x}$$

✓ **Mathematica** : cpu = 0.0157934 (sec), leaf count = 40

$$\left\{\left\{y(x) \to \frac{1}{\frac{c_1}{x} - 1} - \frac{1}{2}x^2\left(\frac{1 - 2x\log(x)}{x^2} - \frac{1}{x^2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 16

$$\left\{y(x) = \left(\ln(x) + (\_C1 - x)^{-1}\right)x\right\}$$

2.811 ODE No. 811

$$y'(x) = \frac{x^4 + x^3e^{y(x)} + xy(x) + e^{y(x)}y(x) - x\log\left(e^{y(x)} + x\right) - e^{y(x)}\log\left(e^{y(x)} + x\right) + x}{x^2}$$

✓ **Mathematica** : cpu = 2.20446 (sec), leaf count = 33

$$\left\{\left\{y(x) \to -\log\left(\frac{e^{-c_1x - \frac{x^3}{2}}}{x} - \frac{1}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 2.608 (sec), leaf count = 32

$$\left\{y(x) = \frac{x^3}{2} + x\_C1 + \ln\left(-x\left(-1 + \mathrm{e}^{\frac{x^3}{2}}\mathrm{e}^{x\_C1}\right)^{-1}\right)\right\}$$

2.812 ODE No. 812

$$y'(x) = x^3\sqrt{x^3 - 6y(x)} + \sqrt{x^3 - 6y(x)} + \frac{x^2}{2} + x^2\sqrt{x^3 - 6y(x)}$$

✓ **Mathematica** : cpu = 0.322621 (sec), leaf count = 70

$$\left\{\left\{y(x) \to \frac{1}{96}\left(72c_1x^4 + 96c_1x^3 + 288c_1x - 144c_1^2 - 9x^8 - 24x^7 - 16x^6 - 72x^5 - 96x^4 + 16x^3 - 144x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.483 (sec), leaf count = 32

$$\left\{-\frac{1}{3}\sqrt{x^3 - 6\,y\left(x\right)} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0\right\}$$

2.813 ODE No. 813

$$y'(x) = \frac{1}{2}\sqrt{a}\left(2\sqrt{ax^4 + 8y(x)} - \sqrt{a}x^3 + 2x^3\sqrt{ax^4 + 8y(x)} + 2x^2\sqrt{ax^4 + 8y(x)}\right)$$

✓ **Mathematica** : cpu = 0.478268 (sec), leaf count = 66

$$\left\{\left\{y(x) \to \frac{1}{72}a\left(-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 87x^4 + 144x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.542 (sec), leaf count = 40

$$\left\{\frac{1}{4}\sqrt{ax^4 + 8\,y\left(x\right)} + \frac{-3\,x^4 - 4\,x^3 - 12\,x}{12}\sqrt{a} - \_C1 = 0\right\}$$

2.814 ODE No. 814

$$y'(x) = \frac{y(x)\left(x^7 y(x)^2 - 3x^3 y(x) - 3\right)}{x\left(x^3 y(x) + 1\right)}$$

✓ **Mathematica** : cpu = 0.0159572 (sec), leaf count = 72

$$\left\{\left\{y(x) \to \frac{x}{\frac{\sqrt{x(c_1-2x)+x}}{\sqrt{\frac{1}{x^7}}} - x^4}\right\}, \left\{y(x) \to -\frac{x}{\frac{\sqrt{x(c_1-2x)+x}}{\sqrt{\frac{1}{x^7}}} + x^4}\right\}\right\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 38

$$\left\{y(x) = \frac{1}{x^3}\left(\sqrt{\_C1 - 2\,x} - 1\right)^{-1}, y(x) = -\frac{1}{x^3}\left(\sqrt{\_C1 - 2\,x} + 1\right)^{-1}\right\}$$

2.815 ODE No. 815

$$y'(x) = \frac{e^{3x^2} x (y(x)+3)^3}{81\left(e^{\frac{3x^2}{2}} y(x) + 3e^{\frac{3x^2}{2}} + 3y(x)\right)}$$

✓ **Mathematica** : cpu = 17.1331 (sec), leaf count = 103

$$\text{Solve}\left[\frac{1}{186}\left(31\log\left(-81e^{\frac{3x^2}{2}}(y(x)+3)y(x) + e^{3x^2}(y(x)+3)^2 - 243y(x)^2\right) - 6\sqrt{93}\tanh^{-1}\left(\frac{2e^{\frac{3x^2}{2}}(y(x)+3) - \right.\right.\right.$$

✓ **Maple** : cpu = 1.298 (sec), leaf count = 168

$$\left\{-10\ln\left(\frac{10\,\mathrm{e}^{3/2\,x^2}(3+y(x))}{27\,\mathrm{e}^{3/2\,x^2} + 9\,\mathrm{e}^{3/2\,x^2} y(x) + 27\,y(x)}\right) + 5\ln\left(\frac{100\,(3+y(x))^2\left(\mathrm{e}^{3/2\,x^2}\right)^2 + \left(-8100\,(y(x))^2 - 24300\,y(\right.\right.\right.$$

2.816 ODE No. 816

$$y'(x) = \frac{x(x-y(x))^3(y(x)+x)^3}{y(x)\left(x^2-y(x)^2-1\right)}$$

✓ **Mathematica** : cpu = 0.144016 (sec), leaf count = 74

$$\text{Solve}\left[\frac{1}{2}\left(\text{RootSum}\left[\#1^3-\#1+1\&,\frac{\#1\log\left(-\#1+x^2-y(x)^2\right)-\log\left(-\#1+x^2-y(x)^2\right)}{3\#1^2-1}\&\right]+x^2\right)=c_1,y(x\right.$$

✓ **Maple** : cpu = 1.025 (sec), leaf count = 190

$$\left\{\int_{\_b}^{x}\frac{(\_a-y(x))^3(\_a+y(x))^3\_a}{\_a^6-3\_a^4(y(x))^2+3\_a^2(y(x))^4-(y(x))^6-\_a^2+(y(x))^2+1}\,\mathrm{d}\_a+\int^{y(x)}-\frac{(-\_f^2+}{-\_f^6+3\_f^4x^2-3\_}\right.$$

2.817 ODE No. 817

$$y'(x) = \frac{\csc(y(x))\left(\frac{1}{2}x^3\log(x)\cos(2y(x))+\frac{1}{2}x^3\log(x)-\cos(y(x))\right)}{x\log(x)}$$

✓ **Mathematica** : cpu = 0.369429 (sec), leaf count = 63

$$\left\{\left\{y(x)\to-\sec^{-1}\left(\frac{-9c_1-x^3+3x^3\log(x)}{9\log(x)}\right)\right\},\left\{y(x)\to\sec^{-1}\left(\frac{-9c_1-x^3+3x^3\log(x)}{9\log(x)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.869 (sec), leaf count = 27

$$\left\{y(x)=\arccos\left(9\,\frac{\ln(x)}{3\,x^3\ln(x)-x^3+9\_C1}\right)\right\}$$

2.818 ODE No. 818

$$y'(x) = \frac{y(x)}{x\left(xy(x)^4+xy(x)^3+xy(x)-1\right)}$$

✓ **Mathematica** : cpu = 0.0474633 (sec), leaf count = 34

$$\text{Solve}\left[\frac{y(x)^3}{3}+\frac{y(x)^2}{2}+\frac{1}{xy(x)}+\log(y(x))=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 34

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-2\,x\left(\mathrm{e}^{-Z}\right)^4-3\,x\left(\mathrm{e}^{-Z}\right)^3+6\,x\_C1\,\mathrm{e}^{-Z}-6\,\_Z\,x\mathrm{e}^{-Z}-6\right)}\right\}$$

2.819 ODE No. 819

$$y'(x) = x^2\sqrt{x^2+3y(x)} + \sqrt{x^2+3y(x)} + x^3\sqrt{x^2+3y(x)} - \frac{2x}{3}$$

✓ **Mathematica** : cpu = 0.227935 (sec), leaf count = 65

$$\left\{\left\{y(x) \to \frac{1}{192}\left(-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4 + 80x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.258 (sec), leaf count = 30

$$\left\{\_C1 + \frac{3\,x^4}{8} + \frac{x^3}{2} + \frac{3\,x}{2} - \sqrt{x^2+3\,y\left(x\right)} = 0\right\}$$

2.820 ODE No. 820

$$y'(x) = \frac{\csc(y(x))\left(\frac{1}{2}x^2\log(x)\cos(2y(x)) + \frac{1}{2}x^2\log(x) - \cos(y(x))\right)}{x\log(x)}$$

✓ **Mathematica** : cpu = 0.329958 (sec), leaf count = 63

$$\left\{\left\{y(x) \to -\sec^{-1}\left(\frac{-4c_1 - x^2 + 2x^2\log(x)}{4\log(x)}\right)\right\}, \left\{y(x) \to \sec^{-1}\left(\frac{-4c_1 - x^2 + 2x^2\log(x)}{4\log(x)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.864 (sec), leaf count = 27

$$\left\{y(x) = \arccos\left(4\,\frac{\ln\left(x\right)}{2\,x^2\ln\left(x\right) - x^2 + 4\,\_C1}\right)\right\}$$

2.821 ODE No. 821

$$y'(x) = \frac{y(x)(xy(x)+1)}{x\left(x^3y(x)^4 - xy(x) - 1\right)}$$

✓ **Mathematica** : cpu = 0.155532 (sec), leaf count = 2093

$$\left\{\left\{\left\{y(x) \to \frac{c_1}{4} - \frac{1}{2}\sqrt{\frac{c_1^2}{4} + \frac{\sqrt[3]{1944c_1^2x^6 + 1458x^5 + \sqrt{\left(1944c_1^2x^6 + 1458x^5\right)^2 - 4\left(54c_1x^4 + 144x^3\right)^3}}}{18\sqrt[3]{2}x^3} + \frac{}{x^3\sqrt[3]{1944}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.173 (sec), leaf count = 25

$$\left\{\frac{1}{2\,x^2\,(y\,(x))^2}+\frac{1}{3\,x^3\,(y\,(x))^3}+y(x)+\_C1=0\right\}$$

2.822 ODE No. 822

$$y'(x)=\frac{1}{4}x\left(-4e^{-x^2}x^2y(x)-4e^{-x^2}x^2+4e^{-x^2}+e^{-2x^2}x^4+4y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.041549 (sec), leaf count = 32

$$\left\{\left\{y(x)\to\frac{1}{c_1-\frac{x^2}{2}}+\frac{1}{2}e^{-x^2}x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.144 (sec), leaf count = 25

$$\left\{y(x)=\frac{x^2\mathrm{e}^{-x^2}}{2}+\left(\_C1-\frac{x^2}{2}\right)^{-1}\right\}$$

2.823 ODE No. 823

$$y'(x)=\frac{y(x)(y(x)+x)}{x\left(y(x)^4+y(x)^3+y(x)+x\right)}$$

✓ **Mathematica** : cpu = 0.402241 (sec), leaf count = 39

$$\text{Solve}\left[\frac{y(x)^3}{3}+\frac{y(x)^2}{2}+\log(y(x))-\frac{y(x)\log(x)+x}{y(x)}=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.145 (sec), leaf count = 38

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-2\left(\mathrm{e}^{-Z}\right)^4-3\left(\mathrm{e}^{-Z}\right)^3+6\,\mathrm{e}^{-Z}\ln(x)+6\_C1\,\mathrm{e}^{-Z}-6\_Z\,\mathrm{e}^{-Z}+6\,x\right)}\right\}$$

2.824 ODE No. 824

$$y'(x) = \frac{y(x)\left(x^3 + x^2 y(x) + y(x)^2\right)}{(x-1)x^2(y(x)+x)}$$

✓ **Mathematica** : cpu = 0.0550056 (sec), leaf count = 68

$$\text{Solve}\left[-\frac{1}{2}\log\left(\frac{y(x)^2}{x^2} + \frac{y(x)}{x} + 1\right) + \log\left(\frac{y(x)}{x}\right) + \frac{\tan^{-1}\left(\frac{\frac{2y(x)}{x}+1}{\sqrt{3}}\right)}{\sqrt{3}} = c_1 + \log(1-x) - \log(x), y(x)\right]$$

✓ **Maple** : cpu = 0.512 (sec), leaf count = 61

$$\left\{-\frac{1}{2}\ln\left(\frac{(y(x))^2 + xy(x) + x^2}{x^2}\right) + \frac{\sqrt{3}}{3}\arctan\left(\frac{(x+2\,y(x))\sqrt{3}}{3\,x}\right) + \ln\left(\frac{y(x)}{x}\right) - \ln(x-1) + \ln(x) - \_C1 = 0\right.$$

2.825 ODE No. 825

$$y'(x) = \frac{x\left(x^2 y(x)^3 + \left(x^2+1\right)^{3/2} y(x)^2 + x^2\left(x^2+1\right)^{3/2} + \left(x^2+1\right)^{3/2} + y(x)^3\right)}{\left(x^2+1\right)^3}$$

✓ **Mathematica** : cpu = 0.206596 (sec), leaf count = 148

$$\text{Solve}\left[-\frac{19}{3}\text{RootSum}\left[-19\#1^3 + 6\sqrt[3]{38}\#1 - 19\&, \frac{\log\left(\frac{\frac{3xy(x)}{\left(x^2+1\right)^2} + \frac{x}{\left(x^2+1\right)^{3/2}}}{\sqrt[3]{38}\sqrt[3]{\frac{x^3}{\left(x^2+1\right)^{9/2}}}} - \#1\right)}{2\sqrt[3]{38} - 19\#1^2}\&\right] = c_1 + \frac{19^{2/3}\left(\frac{x^3}{(x^2+1)^{9/2}}\right)^{2/3}}{9}\right.$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 48

$$\left\{y(x) = \frac{19\,RootOf\left(-1296\int^{-Z}\left(361\_a^3 - 432\_a + 432\right)^{-1}d\_a + 2\ln\left(x^2+1\right) + 3\_C1\right) - 6}{18}\sqrt{x^2+1}\right\}$$

2.826 ODE No. 826

$$y'(x) = \frac{y(x)\left(3xy(x)^2 + 3y(x)^2 + x\right)}{x(x+1)\left(6y(x)^2 + x\right)}$$

✓ **Mathematica** : cpu = 0.592368 (sec), leaf count = 70

$$\left\{\left\{y(x) \to -\frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1}x}{(x+1)^2}\right)}}{\sqrt{6}}\right\}, \left\{y(x) \to \frac{\sqrt{x}\sqrt{W\left(\frac{6e^{2c_1}x}{(x+1)^2}\right)}}{\sqrt{6}}\right\}\right\}$$

✓ **Maple** : cpu = 0.401 (sec), leaf count = 51

$$\left\{\left((y(x))^{-2} + 6\,x^{-1}\right)^{-1} = \frac{x}{54}\left(\mathrm{e}^{RootOf\left(-\mathrm{e}^{-Z}\ln\left(\frac{(1+x)^2\left(\mathrm{e}^{-Z}+9\right)}{2\,x}\right)+3\_C1\,\mathrm{e}^{-Z}+\_Z\,\mathrm{e}^{-Z}+9\right)} + 9\right)\right\}$$

2.827 ODE No. 827

$$y'(x) = \frac{x^2 y(x)\sqrt{x^2 + y(x)^2} + x^3\left(-\sqrt{x^2 + y(x)^2}\right) + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.123833 (sec), leaf count = 111

$$\left\{\left\{y(x) \to \frac{x\left(-2e^{\sqrt{2}c_1 + \frac{\sqrt{2}x^3}{3}} + e^{2\sqrt{2}c_1 + \frac{2\sqrt{2}x^3}{3}} - 1\right)}{2e^{\sqrt{2}c_1 + \frac{\sqrt{2}x^3}{3}} + e^{2\sqrt{2}c_1 + \frac{2\sqrt{2}x^3}{3}} - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.273 (sec), leaf count = 49

$$\left\{\ln\left(2\,\frac{x\left(\sqrt{2\,(y(x))^2 + 2\,x^2} + y(x) + x\right)}{y(x) - x}\right) + \frac{\sqrt{2}x^3}{3} - \ln(x) - \_C1 = 0\right\}$$

2.828 ODE No. 828

$$y'(x) = \frac{(y(x)+1)(2y(x)+1)}{x\left(2xy(x)^4 + xy(x)^3 - 2y(x) - 2\right)}$$

✓ **Mathematica** : cpu = 0.210498 (sec), leaf count = 56

$$\text{Solve}\left[-\frac{1}{8}y(x)^2 + \frac{3y(x)}{8} - \frac{1}{2x(2y(x)+1)} - \frac{1}{2}\log(y(x)+1) + \frac{1}{16}\log(2y(x)+1) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.353 (sec), leaf count = 54

$$\left\{y(x) = \frac{1}{2}\mathrm{e}^{RootOf\left(x\left(\mathrm{e}^{-Z}\right)^3 - 8x\left(\mathrm{e}^{-Z}\right)^2 + 16\ln\left(1/2\,\mathrm{e}^{-Z}+1/2\right)x\mathrm{e}^{-Z} + 8x\_C1\,\mathrm{e}^{-Z} - 2\_Z\,x\mathrm{e}^{-Z} + 7x\mathrm{e}^{-Z} + 16\right)} - \frac{1}{2}\right\}$$

2.829 ODE No. 829

$$y'(x) = \frac{x^6\sqrt{4x^2y(x)+1} + x^5\sqrt{4x^2y(x)+1} + x^3\sqrt{4x^2y(x)+1} + \frac{1}{2}}{x^3}$$

✓ **Mathematica** : cpu = 0.381993 (sec), leaf count = 74

$$\left\{\left\{y(x) \to \frac{-160c_1x^7 - 200c_1x^6 - 400c_1x^4 + 400c_1^2x^2 + 16x^{12} + 40x^{11} + 25x^{10} + 80x^9 + 100x^8 + 100x^6 - 100}{400x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.491 (sec), leaf count = 40

$$\left\{-\_C1 + \frac{1}{x}\left(-4\,x^6 - 5\,x^5 - 10\,x^3 + 10\sqrt{4\,x^2y\,(x)+1}\right) = 0\right\}$$

2.830 ODE No. 830

$$y'(x) = \frac{(x - y(x))y(x)}{x\left(-y(x)^4 - y(x)^3 - y(x) + x\right)}$$

✓ **Mathematica** : cpu = 0.462162 (sec), leaf count = 37

$$\text{Solve}\left[-\frac{1}{3}y(x)^3 - \frac{y(x)^2}{2} - \frac{x}{y(x)} - \log(y(x)) + \log(x) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.153 (sec), leaf count = 38

$$\left\{y(x) = \mathrm{e}^{RootOf\left(2\left(\mathrm{e}^{-Z}\right)^4 + 3\left(\mathrm{e}^{-Z}\right)^3 - 6\,\mathrm{e}^{-Z}\ln(x) + 6\_C1\,\mathrm{e}^{-Z} + 6\_Z\,\mathrm{e}^{-Z} + 6x\right)}\right\}$$

2.831 ODE No. 831

$$y'(x) = \frac{x^3\sqrt{4ax - y(x)^2} + x^2\sqrt{4ax - y(x)^2} + \sqrt{4ax - y(x)^2} + 2a}{y(x)}$$

✓ **Mathematica** : cpu = 4.43295 (sec), leaf count = 145

$$\left\{\left\{y(x) \to -\frac{1}{12}\sqrt{576ax - 72c_1x^4 - 96c_1x^3 - 288c_1x - 144c_1^2 - 9x^8 - 24x^7 - 16x^6 - 72x^5 - 96x^4 - 144x^2}\right\}, \left\{y\right.\right.$$

✓ **Maple** : cpu = 0.376 (sec), leaf count = 35

$$\left\{-\sqrt{-(y(x))^2 + 4ax} - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0\right\}$$

2.832 ODE No. 832

$$y'(x) = \frac{y(x)(y(x) + x + 1)}{(x+1)\left(y(x)^4 + y(x)^3 + y(x)^2 + x\right)}$$

✓ **Mathematica** : cpu = 3.29076 (sec), leaf count = 2497

$$\left\{\left\{y(x) \to -\frac{1}{2}\sqrt{\frac{3\sqrt[3]{2}\left(-8x + 3c_1 + 3\log\right.}{\sqrt[3]{1944\left(c_1 + \log(x+1)\right)^2 + 972\left(c_1 + \log(x+1)\right) + 3726x + \sqrt{\left(1944\left(c_1 + \log(x+1)\right)^2 + 972\right.}}}\right.\right.$$

✓ **Maple** : cpu = 0.214 (sec), leaf count = 31

$$\left\{\ln(1+x) + \frac{x}{y(x)} - \frac{(y(x))^3}{3} - \frac{(y(x))^2}{2} - y(x) + \_C1 = 0\right\}$$

2.833 ODE No. 833

$$y'(x) = \frac{x^4\left(-\sqrt{x^2+y(x)^2}\right) + x^3 y(x)\sqrt{x^2+y(x)^2} + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.116657 (sec), leaf count = 105

$$\left\{\left\{y(x) \to \frac{x\left(-2e^{\sqrt{2}c_1+\frac{x^4}{2\sqrt{2}}} + e^{2\sqrt{2}c_1+\frac{x^4}{\sqrt{2}}} - 1\right)}{2e^{\sqrt{2}c_1+\frac{x^4}{2\sqrt{2}}} + e^{2\sqrt{2}c_1+\frac{x^4}{\sqrt{2}}} - 1}\right\}\right\}$$

✓ **Maple** : cpu = 0.22 (sec), leaf count = 49

$$\left\{\ln\left(2\,\frac{x\left(\sqrt{2\,(y(x))^2+2\,x^2}+y(x)+x\right)}{y(x)-x}\right) + \frac{\sqrt{2}x^4}{4} - \ln(x) - \_C1 = 0\right\}$$

2.834 ODE No. 834

$$y'(x) = \frac{y(x)\left(x^4+3xy(x)^2+3y(x)^2\right)}{x(x+1)\left(6y(x)^2+x\right)}$$

✓ **Mathematica** : cpu = 0.719677 (sec), leaf count = 90

$$\left\{\left\{y(x) \to -\frac{\sqrt{x}\sqrt{W\left(\frac{6(x+1)^2e^{2c_1+x^2-2x-3}}{x}\right)}}{\sqrt{6}}\right\}, \left\{y(x) \to \frac{\sqrt{x}\sqrt{W\left(\frac{6(x+1)^2e^{2c_1+x^2-2x-3}}{x}\right)}}{\sqrt{6}}\right\}\right\}$$

✓ **Maple** : cpu = 0.46 (sec), leaf count = 60

$$\left\{\left((y(x))^{-2}+6\,x^{-1}\right)^{-1} = \frac{x}{54}\left(\mathrm{e}^{RootOf\left(x^2\mathrm{e}^{-Z}-\mathrm{e}^{-Z}\ln\left(\frac{\left(\mathrm{e}^{-Z}+9\right)x}{2\,(1+x)^2}\right)+3\,\_C1\,\mathrm{e}^{-Z}+\_Z\,\mathrm{e}^{-Z}-2\,x\mathrm{e}^{-Z}+9\right)}+9\right)\right\}$$

2.835 ODE No. 835

$$y'(x) = -\frac{1}{x\left(-\sqrt[3]{y(x)^3}\right)\_\mathrm{F1}\left(y(x)^3 - 3\log(x)\right) - x\left(y(x)^3\right)^{2/3}}$$

✗ **Mathematica** : cpu = 2.59547 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == -(-(x*(y[x]^3)^(2/3)) - x*(y[x]^3)^(1/3)*_F1[-3*Log[x] + y[x]^
1), y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = -1/(-(y(x)^3)^(2/3)*x-_F1(y(x)^3-3*ln(x))*(y(x)^3)^(1/3)*x),y(x))
```

2.836 ODE No. 836

$$y'(x) = \frac{(x - y(x))y(x)(y(x) + 1)}{x(xy(x) - y(x) + x)}$$

✓ **Mathematica** : cpu = 11.6586 (sec), leaf count = 379

$$\text{Solve}\left[\frac{1}{9}2^{2/3}\left(\frac{\left(1 - \frac{(x-1)^2\left(\frac{x^6}{(x-1)^3}\right)^{2/3}((x+2)y(x)+x)}{x^4((x-1)y(x)+x)}\right)\left(\frac{\left(\frac{x^6}{(x-1)^3}\right)^{2/3}(x-1)^2((x+2)y(x)+x)}{x^4((x-1)y(x)+x)} + 2\right)\left(\left(1 - \frac{(x-1)^2\left(\frac{x^6}{(x-1)^3}\right)^{2/3}(($$

✓ **Maple** : cpu = 0.261 (sec), leaf count = 73

$$\left\{y(x) = -x\mathrm{e}^{RootOf\left(-\ln\left(\frac{\mathrm{e}^{-Z}}{2}+\frac{9}{2}\right)\mathrm{e}^{-Z}+3\_C1\,\mathrm{e}^{-Z}+\_Z\,\mathrm{e}^{-Z}-x\mathrm{e}^{-Z}+9\right)}\left(-9 + (x-1)\,\mathrm{e}^{RootOf\left(-\ln\left(\frac{\mathrm{e}^{-Z}}{2}+\frac{9}{2}\right)\mathrm{e}^{-Z}+3\_C1\,\mathrm{e}^{-Z}+\_\right.}\right.\right.$$

2.837 ODE No. 837

$$y'(x) = -\frac{1}{-\sqrt[3]{y(x)^3}\log(x)\_\mathrm{F1}\left(3\mathrm{Ei}(-\log(x)) + y(x)^3\right) - \left(y(x)^3\right)^{2/3}\log(x)}$$

✗ **Mathematica** : cpu = 3.13639 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == -(-(Log[x]*(y[x]^3)^(2/3)) - Log[x]*(y[x]^3)^(1/3)*_F1[3*ExpIn
Log[x]] + y[x]^3])^(-1), y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = -1/(-ln(x)*(y(x)^3)^(2/3)-_F1(y(x)^3+3*Ei(1,-ln(x)))*ln(x)*(y(x)^3)^(1
```

2.838 ODE No. 838

$$y'(x) = \frac{\frac{8x^{7/2}}{5} + \frac{4x^6}{25} - \frac{4}{5}x^3 y(x) + \frac{6x^3}{5} - 4\sqrt{x}y(x) + y(x)^2 + 4x + \sqrt{x}}{x}$$

✓ **Mathematica** : cpu = 0.0294032 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{1}{c_1 - \log(x)} + \frac{2}{5}\sqrt{x}\left(x^{5/2} + 5\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 25

$$\left\{y(x) = \frac{2x}{5}\left(x^2 + 5\,\frac{1}{\sqrt{x}}\right) + (\_C1 - \ln(x))^{-1}\right\}$$

2.839 ODE No. 839

$$y'(x) = \frac{e^{\frac{y(x)}{x}}\left(x^2 + xe^{-\frac{y(x)}{x}} + e^{-\frac{y(x)}{x}}y(x)\right)}{x}$$

✓ **Mathematica** : cpu = 0.0733085 (sec), leaf count = 28

$$\left\{\left\{y(x) \to -x\log\left(\frac{e^{2c_1}}{2x} - \frac{x}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.093 (sec), leaf count = 19

$$\left\{y(x) = \ln\left(2\,\frac{x}{-x^2 + \_C1}\right)x\right\}$$

2.840 ODE No. 840

$$y'(x) = \frac{e^{\frac{y(x)}{x}}\left(x^3 + xe^{-\frac{y(x)}{x}} + e^{-\frac{y(x)}{x}}y(x)\right)}{x}$$

✓ **Mathematica** : cpu = 0.085048 (sec), leaf count = 30

$$\left\{\left\{y(x) \to -x\log\left(\frac{e^{3c_1}}{3x} - \frac{x^2}{3}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 19

$$\left\{y(x) = \ln\left(3\,\frac{x}{-x^3 + \_C1}\right)x\right\}$$

2.841 ODE No. 841

$$y'(x) = \frac{-2a^{3/2}bx^2y(x)^2 + 2a^{3/2}cy(x)^2 + a^{5/2}y(x)^4 + \sqrt{a}b^2x^4 - 2\sqrt{a}bcx^2 + \sqrt{a}c^2 + bx^3}{ax^2y(x)}$$

✓ **Mathematica** : cpu = 1.31864 (sec), leaf count = 236

$$\left\{\left\{y(x) \to -\frac{\sqrt{2a^{5/2}bx^2 - 2a^{5/2}c + 4a^3b^2x^3 - 4a^3bcx + a^2x + 4\sqrt{a}b^2c_1x^2 - 4\sqrt{a}bcc_1 + 2bc_1x}}{\sqrt{2}\sqrt{2a^{3/2}bc_1 + a^{7/2} + 2a^4bx}}\right\}, \left\{y(x) \to \frac{\sqrt{2a^{5}}\right.\right.$$

✓ **Maple** : cpu = 0.378 (sec), leaf count = 97

$$\left\{y(x) = \frac{1}{x\_C1 + 1}\sqrt{(x\_C1 + 1)\left((x\_C1 + 1)(bx^2 - c)\sqrt{a} + \frac{x}{2}\right)a^{\frac{3}{2}}a^{-\frac{3}{2}}}, y(x) = -2\frac{\sqrt{(x\_C1 + 1)\left((x\_C1 + \right.}}{a^{3/2}(2x}\right.$$

2.842 ODE No. 842

$$y'(x) = \frac{2x^2y(x)\log^2(x) + x^2y(x)^2\log(x) + x^2\log^3(x) + y(x)}{x\log(x)}$$

✓ **Mathematica** : cpu = 0.120646 (sec), leaf count = 186

$$\left\{\left\{y(x) \to -\frac{c_1e^{\frac{1}{4}x^2(2\log(x)-1)}\left(\frac{x}{2} + \frac{1}{2}x(2\log(x) - 1)\right) + \frac{1}{4}x^2e^{\frac{1}{4}x^2(2\log(x)-1)}(2\log(x) - 1)\left(\frac{x}{2} + \frac{1}{2}x(2\log(x) - 1)\right) + \right.\right.$$
$$\left.\left.x\left(c_1e^{\frac{1}{4}x^2(2\log(x)-1)} + \frac{1}{4}x^2e^{\frac{1}{4}x^2(2\log(x)-1)}(2\log(x) - \right.\right.\right.$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 43

$$\left\{y(x) = -\frac{\ln(x)\left(2x^2\ln(x) - x^2 + 2\_C1 + 4\right)}{2x^2\ln(x) - x^2 + 2\_C1}\right\}$$

2.843 ODE No. 843

$$y'(x) = \frac{2x^3y(x)\log^2(x) + x^3y(x)^2\log(x) + x^3\log^3(x) + y(x)}{x\log(x)}$$

✓ **Mathematica** : cpu = 0.125041 (sec), leaf count = 198

$$\left\{\left\{y(x) \to -\frac{c_1e^{\frac{1}{9}x^3(3\log(x)-1)}\left(\frac{x^2}{3} + \frac{1}{3}x^2(3\log(x) - 1)\right) + \frac{1}{9}x^3e^{\frac{1}{9}x^3(3\log(x)-1)}(3\log(x) - 1)\left(\frac{x^2}{3} + \frac{1}{3}x^2(3\log(x) - \right.\right.$$
$$\left.\left.x^2\left(c_1e^{\frac{1}{9}x^3(3\log(x)-1)} + \frac{1}{9}x^3e^{\frac{1}{9}x^3(3\log(x)-1)}(3\log(x)\right.\right.\right.$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 43

$$\left\{y(x) = -\frac{\ln(x)\left(6x^3\ln(x) - 2x^3 + 9\_C1 + 18\right)}{6x^3\ln(x) - 2x^3 + 9\_C1}\right\}$$

2.844 ODE No. 844

$$y'(x) = \frac{y(x)(y(x)+1)(y(x)+x)}{x(xy(x)+y(x)+x)}$$

✓ **Mathematica** : cpu = 15.8638 (sec), leaf count = 386

$$\text{Solve}\left[\frac{2^{2/3}\left(1-\frac{\left(\frac{x^6}{(x+1)^3}\right)^{2/3}(x+1)^2((x-2)y(x)+x)}{x^4((x+1)y(x)+x)}\right)\left(\frac{\left(\frac{x^6}{(x+1)^3}\right)^{2/3}(x+1)^2((x-2)y(x)+x)}{x^4((x+1)y(x)+x)}+2\right)\left(\left(1-\frac{\left(\frac{x^6}{(x+1)^3}\right)^{2/3}(x+1)^2((x-2\right.}{9\left(\frac{3(}{}\right.}\right.$$

✓ **Maple** : cpu = 0.286 (sec), leaf count = 97

$$\left\{y(x) = -x\mathrm{e}^{RootOf\left(-\ln\left(\frac{\mathrm{e}^{-Z}}{2}+\frac{9}{2}\right)\mathrm{e}^{-Z}+3\_C1\,\mathrm{e}^{-Z}+\_Z\,\mathrm{e}^{-Z}+x\mathrm{e}^{-Z}+9\right)}\left(\mathrm{e}^{RootOf\left(-\ln\left(\frac{\mathrm{e}^{-Z}}{2}+\frac{9}{2}\right)\mathrm{e}^{-Z}+3\_C1\,\mathrm{e}^{-Z}+\_Z\,\mathrm{e}^{-Z}+x\mathrm{e}^{-Z}+9\right)}\right.\right.$$

2.845 ODE No. 845

$$y'(x) = \frac{\sqrt{4y(x)^3-9x^4}+3x^3+x^3\sqrt{4y(x)^3-9x^4}+x^2\sqrt{4y(x)^3-9x^4}}{y(x)^2}$$

✓ **Mathematica** : cpu = 4.95684 (sec), leaf count = 227

$$\left\{\left\{y(x)\to -\frac{1}{2}\sqrt[3]{-\frac{1}{2}\sqrt[3]{72c_1x^4+96c_1x^3+288c_1x+144c_1^2+9x^8+24x^7+16x^6+72x^5+132x^4+144x^2}}\right\},\left\{y(x\right.\right.$$

✓ **Maple** : cpu = 0.301 (sec), leaf count = 44

$$\left\{\int_{\_b}^{y(x)} \_a^2\frac{1}{\sqrt{-9x^4+4\_a^3}}\,\mathrm{d}\_a - \frac{x^4}{4} - \frac{x^3}{3} - x - \_C1 = 0\right\}$$

2.846 ODE No. 846

$$y'(x) = \frac{1}{x^2\left(-\left(\frac{1}{y(x)}+1\right)\right)\_F1\left(x\left(\frac{1}{y(x)}+1\right)\right)+x^2\_F1\left(x\left(\frac{1}{y(x)}+1\right)\right)+x\left(\frac{1}{y(x)}+1\right)-x}$$

✓ **Mathematica** : cpu = 1.38687 (sec), leaf count = 362

$$\text{Solve}\left[\int_1^{y(x)}\left(\frac{x\_F1\left(x\left(\frac{1}{K[2]}+1\right)\right)-1}{xK[2]\_F1\left(x\left(\frac{1}{K[2]}+1\right)\right)+x\_F1\left(x\left(\frac{1}{K[2]}+1\right)\right)-K[2]}-\int_1^x\left(\frac{-\frac{K[1]\_F1'\left(K[1]\left(\frac{1}{K[2]}+1\right)\right)}{K[2]}-\frac{K[1}{}}{K[1]\left(K[2]\_F1\left(K[1]\left(\frac{1}{K[2]}\right.\right.\right.}\right.\right.\right.$$

✓ **Maple** : cpu = 0.221 (sec), leaf count = 40

$$\left\{y(x) = e^{RootOf\left(-\_Z-\int^{\frac{xe^{\_Z}}{e^{\_Z}-1}}\frac{1}{(\_F1(\_a)\_a-1)\_a}d\_a+\_C1\right)}-1\right\}$$

2.847 ODE No. 847

$$y'(x) = x^2\sqrt{x^2-4y(x)+2x+1}+\sqrt{x^2-4y(x)+2x+1}+x^3\sqrt{x^2-4y(x)+2x+1}+\frac{x}{2}+\frac{1}{2}$$

✓ **Mathematica** : cpu = 0.356283 (sec), leaf count = 69

$$\left\{\left\{y(x)\to\frac{1}{144}\left(72c_1x^4+96c_1x^3+288c_1x-144c_1^2-9x^8-24x^7-16x^6-72x^5-96x^4-108x^2+72x+36\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.323 (sec), leaf count = 34

$$\left\{\_C1-\frac{x^4}{2}-\frac{2x^3}{3}-2x-\sqrt{x^2+2x+1-4y(x)}=0\right\}$$

2.848 ODE No. 848

$$y'(x) = \_\mathrm{F1}(y(x) - \log(\sinh(x))) + \coth(x)$$

✓ **Mathematica** : cpu = 0.112138 (sec), leaf count = 154

$$\text{Solve}\left[\int_1^{y(x)} -\frac{\_\mathrm{F1}(K[2] - \log(\sinh(x)))\left(\int_1^x \left(\frac{\_\mathrm{F1}'(K[2]-\log(\sinh(K[1])))(\_\mathrm{F1}(K[2]-\log(\sinh(K[1])))+\coth(K[1]))}{(\_\mathrm{F1}(K[2]-\log(\sinh(K[1]))))^2} - \frac{\_\mathrm{F1}'(K}{\_\mathrm{F1}(K}\right.\right.}{\_\mathrm{F1}(K[2] - \log(\sinh(x)))}$$

✓ **Maple** : cpu = 0.741 (sec), leaf count = 27

$$\left\{\int_{\_b}^{y(x)} (\_F1(\_a - \ln(\sinh(x))))^{-1}\, \mathrm{d}\_a - x - \_C1 = 0\right\}$$

2.849 ODE No. 849

$$y'(x) = x^2\sqrt{x^2 + 4y(x) - 4x} + \sqrt{x^2 + 4y(x) - 4x} + x^3\sqrt{x^2 + 4y(x) - 4x} - \frac{x}{2} + 1$$

✓ **Mathematica** : cpu = 0.318901 (sec), leaf count = 68

$$\left\{\left\{y(x) \to \frac{1}{144}(-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4 + 108x^2 + 144x)\right\}\right\}$$

✓ **Maple** : cpu = 0.302 (sec), leaf count = 33

$$\left\{\_C1 + \frac{x^4}{2} + \frac{2\,x^3}{3} + 2\,x - \sqrt{x^2 - 4\,x + 4\,y\left(x\right)} = 0\right\}$$

2.850 ODE No. 850

$$y'(x) = \_\mathrm{F1}(y(x) - \log(\sin(x)) + \log(\cos(x) + 1)) + \csc(x)$$

✓ **Mathematica** : cpu = 0.196611 (sec), leaf count = 1478

$$\text{Solve}\left[\int_1^{y(x)} -\frac{\sin(x)\left(\left(\int_1^x \left(\frac{(\cot^2(K[1])+\csc(K[1])\cot(K[1])+1)\sin(K[1])(\csc(K[1])+\_\mathrm{F1}(K[2]+\log(\cos(K[1])+1)-\log(\sin(K[1]))))(c}{(-\cot^2(K[1])+\_\mathrm{F1}(K[2]+\log(\cos(K[1])+1)-\log(\sin(K[1])))\cot(K[1}\right.\right.\right.}$$

✓ **Maple** : cpu = 1.39 (sec), leaf count = 32

$$\left\{\int_{\_b}^{y(x)} (\_F1(\_a - \ln(\sin(x)) + \ln(\cos(x) + 1)))^{-1}\, \mathrm{d}\_a - x - \_C1 = 0\right\}$$

2.851 ODE No. 851

$$y'(x) = \frac{a^3x^3 + 3a^2bx^2y(x) + a^2bx^2 + 3ab^2xy(x)^2 + 2ab^2xy(x) + b^3y(x)^3 + b^3y(x)^2 + b^3}{b^3}$$

✓ **Mathematica** : cpu = 0.165319 (sec), leaf count = 145

$$\text{Solve}\left[-\frac{1}{3}(27a+29b)^{2/3}\text{RootSum}\left[\#1^3(27a+29b)^{2/3} - 3\#1b^{2/3} + (27a+29b)^{2/3}\&, \frac{\log\left(\frac{\frac{3ax+b}{b}+3y(x)}{\sqrt[3]{\frac{27a+29b}{b}}} - \#1\right)}{b^{2/3} - \#1^2(27a+29b)^{2/3}}\&\right.\right.$$

✓ **Maple** : cpu = 0.076 (sec), leaf count = 42

$$\left\{y(x) = \frac{RootOf\left(\int^{-Z}\left(\_a^3b + \_a^2b + a + b\right)^{-1}d\_ab - x + \_C1\right)b - ax}{b}\right\}$$

2.852 ODE No. 852

$$y'(x) = \frac{\alpha^3y(x)^3 + \alpha^3y(x)^2 + \alpha^3 + 3\alpha^2\beta xy(x)^2 + 2\alpha^2\beta xy(x) + 3\alpha\beta^2x^2y(x) + \alpha\beta^2x^2 + \beta^3x^3}{\alpha^3}$$

✓ **Mathematica** : cpu = 0.157264 (sec), leaf count = 145

$$\text{Solve}\left[-\frac{1}{3}(29\alpha+27\beta)^{2/3}\text{RootSum}\left[\#1^3(29\alpha+27\beta)^{2/3} - 3\#1\alpha^{2/3} + (29\alpha+27\beta)^{2/3}\&, \frac{\log\left(\frac{\frac{\alpha+3\beta x}{\alpha}+3y(x)}{\sqrt[3]{\frac{29\alpha+27\beta}{\alpha}}} - \#1\right.\right.\right.$$

✓ **Maple** : cpu = 0.079 (sec), leaf count = 42

$$\left\{y(x) = \frac{RootOf\left(\int^{-Z}\left(\_a^3\alpha + \_a^2\alpha + \alpha + \beta\right)^{-1}d\_a\alpha - x + \_C1\right)\alpha - \beta x}{\alpha}\right\}$$

2.853 ODE No. 853

$$y'(x) = \frac{x^3 y(x)^3 + 6x^2 y(x)^2 + 14xy(x) + 2x + 12}{x^2(xy(x) + x + 2)}$$

✓ **Mathematica** : cpu = 0.0184988 (sec), leaf count = 76

$$\left\{\left\{y(x) \to \frac{1}{x^3\left(\frac{1}{x^3} - \frac{1}{x^3\sqrt{c_1 - 2x}}\right)} - \frac{x+2}{x}\right\}, \left\{y(x) \to \frac{1}{x^3\left(\frac{1}{x^3\sqrt{c_1 - 2x}} + \frac{1}{x^3}\right)} - \frac{x+2}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.044 (sec), leaf count = 63

$$\left\{y(x) = \frac{1}{x}\left(-2\sqrt{\_C1 - 2x} - x - 2\right)\left(\sqrt{\_C1 - 2x} + 1\right)^{-1}, y(x) = \frac{1}{x}\left(-2\sqrt{\_C1 - 2x} + x + 2\right)\left(\sqrt{\_C1 - 2}\right.\right.$$

2.854 ODE No. 854

$$y'(x) = \frac{y(x)\left(x^2\log^2(y(x)) + 2x^2\log(x)\log(y(x)) + x^2\log^2(x) + \log(y(x)) + \log(x) - 1\right)}{x}$$

✗ **Mathematica** : cpu = 0.622424 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-1 + Log[x] + x^2*Log[x]^2 + Log[y[x]] + 2*x^2*Log[x]*Log[y[
```

✓ **Maple** : cpu = 0.277 (sec), leaf count = 51

$$\left\{y(x) = 1\left(x^{\frac{x^3}{x^3+3\_C1}}\right)^{-1}\left(x^{\frac{\_C1}{x^3+3\_C1}}\right)^{-3}\left(\mathrm{e}^{\frac{x}{x^3+3\_C1}}\right)^{-3}\right\}$$

2.855 ODE No. 855

$$y'(x) = \frac{y(x)\left(x^3\log^2(y(x)) + 2x^3\log(x)\log(y(x)) + x^3\log^2(x) + \log(y(x)) + \log(x) - 1\right)}{x}$$

✗ **Mathematica** : cpu = 0.675774 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-1 + Log[x] + x^3*Log[x]^2 + Log[y[x]] + 2*x^3*Log[x]*Log[y[
```

✓ **Maple** : cpu = 0.271 (sec), leaf count = 51

$$\left\{y(x) = 1\left(x^{\frac{x^4}{x^4+4\_C1}}\right)^{-1}\left(x^{\frac{\_C1}{x^4+4\_C1}}\right)^{-4}\left(\mathrm{e}^{\frac{x}{x^4+4\_C1}}\right)^{-4}\right\}$$

2.856 ODE No. 856

$$y'(x) = -\frac{x\left(-\_\mathrm{F1}\left(y(x)^2 - 2x\right) - \frac{1}{x}\right)}{\sqrt{y(x)^2}}$$

✓ **Mathematica** : cpu = 0.909467 (sec), leaf count = 100

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{\sqrt{K[2]^2}}{\_\mathrm{F1}\left(K[2]^2 - 2x\right)} - \int_1^x \frac{2K[2]\_\mathrm{F1}'\left(K[2]^2 - 2K[1]\right)}{\left(\_\mathrm{F1}\left(K[2]^2 - 2K[1]\right)\right)^2}\, dK[1]\right) dK[2] + \int_1^x \left(-\frac{1}{\_\mathrm{F1}\left(y(x)^2 - 2K[1]\right.}\right.\right.$$

✓ **Maple** : cpu = 0.359 (sec), leaf count = 65

$$\left\{y(x) = \sqrt{2\,RootOf\left(x^2 - 2\int^{\_Z} \left(\_F1\left(2\,\_a\right)\right)^{-1} d\_a + 4\,\_C1\right) + 2\,x}, y(x) = -\sqrt{2\,RootOf\left(x^2 - 2\int^{\_Z} (\_F\right.}\right.$$

2.857 ODE No. 857

$$y'(x) = x^2\sqrt{x^2 + 8y(x) - 2x + 1} + \sqrt{x^2 + 8y(x) - 2x + 1} + x^3\sqrt{x^2 + 8y(x) - 2x + 1} - \frac{x}{4} + \frac{1}{4}$$

✓ **Mathematica** : cpu = 0.33799 (sec), leaf count = 69

$$\left\{\left\{y(x) \to \frac{1}{72}\left(-72c_1x^4 - 96c_1x^3 - 288c_1x + 144c_1^2 + 9x^8 + 24x^7 + 16x^6 + 72x^5 + 96x^4 + 135x^2 + 18x - 9\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.315 (sec), leaf count = 32

$$\left\{\_C1 + x^4 + \frac{4\,x^3}{3} + 4\,x - \sqrt{x^2 - 2\,x + 1 + 8\,y\left(x\right)} = 0\right\}$$

2.858 ODE No. 858

$$y'(x) = \frac{a^3y(x)^3 + a^3y(x)^2 + a^3 + 3a^2bxy(x)^2 + 2a^2bxy(x) + 3ab^2x^2y(x) + ab^2x^2 + b^3x^3}{a^3}$$

✓ **Mathematica** : cpu = 0.164942 (sec), leaf count = 145

$$\text{Solve}\left[-\frac{1}{3}(29a + 27b)^{2/3}\text{RootSum}\left[\#1^3(29a + 27b)^{2/3} - 3\#1a^{2/3} + (29a + 27b)^{2/3}\&, \frac{\log\left(\frac{\frac{a+3bx}{a} + 3y(x)}{\sqrt[3]{\frac{29a+27b}{a}}} - \#1\right)}{a^{2/3} - \#1^2(29a + 27b)^{2/3}}\right.\right.\&$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 42

$$\left\{ y(x) = \frac{RootOf\left(\int^{-Z} \left(a\_a^3 + a\_a^2 + a + b \right)^{-1} d\_aa - x + \_C1 \right) a - bx}{a} \right\}$$

2.859 ODE No. 859

$$y'(x) = \frac{\_\mathrm{F1}\left(y(x)^2 - 2x\right) + x}{x\sqrt{y(x)^2}}$$

✓ **Mathematica** : cpu = 1.30738 (sec), leaf count = 102

$$\text{Solve}\left[\int_1^{y(x)} \left(\frac{\sqrt{K[2]^2}}{\_\mathrm{F1}\left(K[2]^2 - 2x\right)} - \int_1^x \frac{2K[2]\_\mathrm{F1}'\left(K[2]^2 - 2K[1]\right)}{\left(\_\mathrm{F1}\left(K[2]^2 - 2K[1]\right)\right)^2} dK[1] \right) dK[2] + \int_1^x \left(-\frac{1}{\_\mathrm{F1}\left(y(x)^2 - 2K[1]\right.} \right.$$

✓ **Maple** : cpu = 0.355 (sec), leaf count = 63

$$\left\{ y(x) = \sqrt{2\, RootOf\left(\ln(x) - \int^{\_Z} \left(\_F1\left(2\,\_a\right) \right)^{-1} d\_a + 2\,\_C1 \right) + 2x}, y(x) = -\sqrt{2\, RootOf\left(\ln(x) - \int^{\_Z} \left(\right.\right.\right.\right.$$

2.860 ODE No. 860

$$y'(x) = \frac{\frac{1}{2}x^4\cos(2y(x)) + \frac{x^4}{2} + \frac{1}{2}x^3\cos(2y(x)) + \frac{x^3}{2} - \frac{1}{2}\sin(2y(x)) + \frac{1}{2}x\cos(2y(x)) + \frac{x}{2}}{x}$$

✓ **Mathematica** : cpu = 0.148186 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \to \tan^{-1}\left(\frac{10c_1 + 4x^5 + 5x^4 + 10x^2}{20x} \right) \right\} \right\}$$

✓ **Maple** : cpu = 2.612 (sec), leaf count = 29

$$\left\{ y(x) = \arctan\left(\frac{4\,x^5 + 5\,x^4 + 10\,x^2 + 40\,\_C1}{20\,x} \right) \right\}$$

2.861 ODE No. 861

$$y'(x) = -\frac{e^{-1/x}\left(-\_\mathrm{F1}\left(e^{\frac{1}{x}}y(x)\right) - \frac{e^{\frac{1}{x}}y(x)}{x}\right)}{x}$$

✓ **Mathematica** : cpu = 1.8226 (sec), leaf count = 155

$$\text{Solve}\left[\int_1^{y(x)} -\frac{\_\mathrm{F1}\left(e^{\frac{1}{x}}K[2]\right)\left(\int_1^x\left(\frac{e^{\frac{1}{K[1]}}}{K[1]^2\_\mathrm{F1}\left(e^{\frac{1}{K[1]}}K[2]\right)} - \frac{e^{\frac{2}{K[1]}}K[2]\_\mathrm{F1}'\left(e^{\frac{1}{K[1]}}K[2]\right)}{K[1]^2\left(\_\mathrm{F1}\left(e^{\frac{1}{K[1]}}K[2]\right)\right)^2}\right)dK[1]\right) + e^{\frac{1}{x}}}{\_\mathrm{F1}\left(e^{\frac{1}{x}}K[2]\right)}dK[2] + \int_1^x\right.$$

✓ **Maple** : cpu = 0.205 (sec), leaf count = 26

$$\left\{y(x) = \frac{RootOf\left(-\ln(x) + \int^{-Z}(\_F1(\_a))^{-1}d\_a + \_C1\right)}{\mathrm{e}^{x^{-1}}}\right\}$$

2.862 ODE No. 862

$$y'(x) = -\log(y(x)-1)\left(\frac{\mathrm{Ei}(-\log(y(x)-1))}{x} - \_\mathrm{F1}(x)\right)$$

✗ **Mathematica** : cpu = 1.13121 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == -(Log[-1 + y[x]]*(ExpIntegralEi[-Log[-1 + y[x]]]/x - _F1[x])),
```

✓ **Maple** : cpu = 0.253 (sec), leaf count = 27

$$\left\{y(x) = \mathrm{e}^{RootOf\left(\int^{\frac{-F1(x)}{x}}\mathrm{d}x x + x\_C1 + Ei(1,-\_Z)\right)} + 1\right\}$$

2.863 ODE No. 863

$$y'(x) = \frac{x\sqrt{x^2+y(x)^2} + x^4\sqrt{x^2+y(x)^2} + x^3\sqrt{x^2+y(x)^2} + y(x)}{x}$$

✓ **Mathematica** : cpu = 0.0351088 (sec), leaf count = 30

$$\left\{\left\{y(x) \to x\sinh\left(\frac{1}{12}\left(12c_1 + 3x^4 + 4x^3 + 12x\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 7.155 (sec), leaf count = 38

$$\left\{\ln\left(\sqrt{(y(x))^2+x^2}+y(x)\right)-\frac{x^4}{4}-\frac{x^3}{3}-x-\ln(x)-\_C1=0\right\}$$

2.864 ODE No. 864

$$y'(x)=\frac{e^{\frac{x^2}{4}}y(x)\left(2e^{-\frac{3x^2}{4}}y(x)^2+e^{-\frac{x^2}{2}}xy(x)+e^{-\frac{x^2}{4}}x\right)}{2e^{-\frac{x^2}{4}}y(x)+2}$$

✓ **Mathematica** : cpu = 0.0420508 (sec), leaf count = 137

$$\left\{\left\{y(x)\to\frac{2e^{\frac{x^2}{2}}}{\sqrt{2}\sqrt{2e^{\frac{x^2}{2}}(c_1-2x)+2e^{\frac{x^2}{2}}-2e^{\frac{x^2}{4}}}}\right\},\left\{y(x)\to-\frac{2e^{\frac{x^2}{2}}}{\sqrt{2}\sqrt{2e^{\frac{x^2}{2}}(c_1-2x)+2e^{\frac{x^2}{2}}+2e^{\frac{x^2}{4}}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.12 (sec), leaf count = 162

$$\left\{y(x)=1\left(\mathrm{e}^{\frac{x^2}{2}}\left(\sqrt{\_C1-2x}-1\right)\mathrm{e}^{-\frac{x^2}{4}}-\mathrm{e}^{\frac{x^2}{4}}\sqrt{\_C1-2x}\right)\left(\mathrm{e}^{-\frac{x^2}{4}}\right)^{-1}\left(\mathrm{e}^{-\frac{x^2}{4}}\mathrm{e}^{\frac{x^2}{2}}+\mathrm{e}^{\frac{x^2}{4}}\sqrt{\_C1-2x}\right)^{-1},y(x)\right.$$

2.865 ODE No. 865

$$y'(x)=(1-y(x))\left(-f(x)+\frac{y(x)\log(y(x)-1)}{x(1-y(x))\log(x)}-\frac{\log(y(x)-1)}{x(1-y(x))\log(x)}\right)$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.276 (sec), leaf count = 23

$$\left\{y(x)=\mathrm{e}^{\int\frac{f(x)}{\ln(x)}\,\mathrm{d}x\ln(x)}x^{\_C1}+1\right\}$$

2.866 ODE No. 866

$$y'(x) = x^2\sqrt{a^2+2ax+x^2+4y(x)}+\sqrt{a^2+2ax+x^2+4y(x)}+x^3\sqrt{a^2+2ax+x^2+4y(x)}-\frac{a}{2}-\frac{x}{2}$$

✓ **Mathematica** : cpu = 0.486755 (sec), leaf count = 74

$$\left\{\left\{y(x)\to \frac{1}{144}\left(-36a^2-72ax-72c_1x^4-96c_1x^3-288c_1x+144c_1^2+9x^8+24x^7+16x^6+72x^5+96x^4+108x^{\right.}\right.\right.$$

✓ **Maple** : cpu = 0.565 (sec), leaf count = 37

$$\left\{\_C1+\frac{x^4}{2}+\frac{2\,x^3}{3}+2\,x-\sqrt{x^2+2\,ax+a^2+4\,y\left(x\right)}=0\right\}$$

2.867 ODE No. 867

$$y'(x) = \frac{x^6}{27}+\frac{1}{3}x^4y(x)+\frac{x^4}{9}+x^2y(x)^2+\frac{2}{3}x^2y(x)+y(x)^3+y(x)^2-\frac{2x}{3}+1$$

✓ **Mathematica** : cpu = 0.0630048 (sec), leaf count = 77

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{x^2+3y(x)+1}{\sqrt[3]{29}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]=c_1+\frac{1}{9}29^{2/3}x,y(x)\right]$$

✓ **Maple** : cpu = 0.073 (sec), leaf count = 30

$$\left\{y(x)=-\frac{x^2}{3}+RootOf\left(-x+\int^{\_Z}\left(\_a^3+\_a^2+1\right)^{-1}d\_a+\_C1\right)\right\}$$

2.868 ODE No. 868

$$y'(x) = -x^6+3x^4y(x)+x^4-3x^2y(x)^2-2x^2y(x)+y(x)^3+y(x)^2+2x+1$$

✓ **Mathematica** : cpu = 0.0477884 (sec), leaf count = 79

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{-3x^2+3y(x)+1}{\sqrt[3]{29}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]=c_1+\frac{1}{9}29^{2/3}x,y(x)\right]$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 28

$$\left\{y(x)=x^2+RootOf\left(-x+\int^{\_Z}\left(\_a^3+\_a^2+1\right)^{-1}d\_a+\_C1\right)\right\}$$

2.869 ODE No. 869

$$y'(x) = \frac{2x^5 + 2x^4 - 2x^3 y(x) + x^3 - 2x^2 y(x) + 3x^2 - 2y(x) - x + 1}{x^2 - y(x)}$$

✓ **Mathematica** : cpu = 0.0369618 (sec), leaf count = 42

$$\left\{\left\{y(x) \to \frac{1}{2}\left(W\left(-e^{c_1 + x^4 + \frac{4x^3}{3} - 2x^2 + 4x - 1}\right) + 1\right) + x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.083 (sec), leaf count = 37

$$\left\{y(x) = x^2 + \frac{1}{2}\mathit{lambertW}\left(-2\,\frac{\mathrm{e}^{x^4}\mathrm{e}^{4/3\,x^3}\_C1\,\left(\mathrm{e}^{x}\right)^4\mathrm{e}^{-1}}{\left(\mathrm{e}^{x^2}\right)^2}\right) + \frac{1}{2}\right\}$$

2.870 ODE No. 870

$$y'(x) = \frac{e^{\frac{y(x)}{x}}\left(x^4 + x^3 + xe^{-\frac{y(x)}{x}} + e^{-\frac{y(x)}{x}} y(x) + x\right)}{x}$$

✓ **Mathematica** : cpu = 1.6682 (sec), leaf count = 35

$$\left\{\left\{y(x) \to -x \log\left(\frac{-c_1 - \frac{x^4}{4} - \frac{x^3}{3} - x}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 1.234 (sec), leaf count = 30

$$\left\{y(x) = -\ln\left(-\frac{3\,x^4 + 4\,x^3 + 12\,\_C1 + 12\,x}{12\,x}\right)x\right\}$$

2.871 ODE No. 871

$$y'(x) = \frac{2xy(x)^2 + y(x)^2 + 4xy(x)\log(2x+1) + 2y(x)\log(2x+1) + 2x\log^2(2x+1) + \log^2(2x+1) - 2}{2x+1}$$

✓ **Mathematica** : cpu = 0.023432 (sec), leaf count = 22

$$\left\{\left\{y(x) \to \frac{1}{c_1 - x} - \log(2x+1)\right\}\right\}$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 26

$$\left\{y(x) = \frac{-1 + (\_C1 - x)\ln(2\,x+1)}{-\_C1 + x}\right\}$$

2.872 ODE No. 872

$$y'(x) = \frac{14x^{7/2} + \frac{12x^6}{5} - 6x^3 y(x) - 6x^3 - 5\sqrt{x}y(x) + 10x - 5\sqrt{x} - 5}{x\left(2x^3 - 5y(x) + 10\sqrt{x} - 5\right)}$$

✓ **Mathematica** : cpu = 0.0475679 (sec), leaf count = 215

$$\left\{\left\{y(x) \to \frac{1}{5}\left(2x^3 + 10\sqrt{x} - 5\right) - \frac{\sqrt{-25c_1 x - x\left(2x^3 + 10\sqrt{x} - 5\right)^2 - 50x\left(-\frac{4x^{7/2}}{5} - \frac{2x^6}{25} + \frac{2x^3}{5} - 2x + 2\sqrt{x} + 1\right.}}{5\sqrt{-\frac{1}{x}x}}\right.\right.$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 49

$$\left\{y(x) = \frac{2x^3}{5} + 2\sqrt{x} - \sqrt{\_C1 + 2\ln(x)} - 1, y(x) = \frac{2x^3}{5} + 2\sqrt{x} + \sqrt{\_C1 + 2\ln(x)} - 1\right\}$$

2.873 ODE No. 873

$$y'(x) = \frac{2y(x) + 1}{x\left(2xy(x)^4 + 3xy(x)^3 + xy(x)^2 + 2xy(x) + x - 2\right)}$$

✓ **Mathematica** : cpu = 0.345032 (sec), leaf count = 53

$$\text{Solve}\left[\frac{1}{192}\left(-16y(x)^3 - 12y(x)^2 + 12y(x) - 54\log(4y(x) + 2) + 7\right) - \frac{1}{2x(2y(x) + 1)} = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.29 (sec), leaf count = 50

$$\left\{y(x) = \frac{\mathrm{e}^{RootOf\left(2x\left(\mathrm{e}^{-Z}\right)^4 - 3x\left(\mathrm{e}^{-Z}\right)^3 - 6x\left(\mathrm{e}^{-Z}\right)^2 + 48x\_C1\,\mathrm{e}^{-Z} + 54\_Z x\mathrm{e}^{-Z} + 7x\mathrm{e}^{-Z} + 96\right)}}{2} - \frac{1}{2}\right\}$$

2.874 ODE No. 874

$$y'(x) = \frac{1}{512}x\left(a^3x^{12} + 24a^2x^8y(x) + 8a^2x^8 + 192ax^4y(x)^2 + 128ax^4y(x) - 256ax^2 + 512y(x)^3 + 512y(x)^2 + 512\right.$$

✓ **Mathematica** : cpu = 0.0724654 (sec), leaf count = 101

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{1}{8}\left(3ax^5 + 8x\right) + 3xy(x)}{\sqrt[3]{29}\sqrt[3]{x^3}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{1}{18}29^{2/3}\left(x^3\right)^{2/3}, y(x)\right.$$

✓ **Maple** : cpu = 0.064 (sec), leaf count = 40

$$\left\{y(x)=-\frac{ax^4}{8}-\frac{1}{3}+\frac{29\,RootOf\left(x^2-162\int^{-Z}\left(841\_a^3-27\_a+27\right)^{-1}d\_a+6\_C1\right)}{9}\right\}$$

2.875 ODE No. 875

$$y'(x)=\frac{x^5\left(-\sqrt{x^2+y(x)^2}\right)+x^4y(x)\sqrt{x^2+y(x)^2}+xy(x)+y(x)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.291968 (sec), leaf count = 285

$$\left\{\left\{y(x)\to\frac{x\left(2(x+1)^{\sqrt{2}}\exp\left(\sqrt{2}c_1+\frac{x^4}{2\sqrt{2}}+\frac{x^2}{\sqrt{2}}+\frac{1}{3}\sqrt{2}\left(x^2+3\right)x+\frac{25}{6\sqrt{2}}\right)+(x+1)^{2\sqrt{2}}\left(-e^{2\sqrt{2}c_1+\frac{x^4}{\sqrt{2}}+\sqrt{2}x^2}\right)+\right.\right.}{-2(x+1)^{\sqrt{2}}\exp\left(\sqrt{2}c_1+\frac{x^4}{2\sqrt{2}}+\frac{x^2}{\sqrt{2}}+\frac{1}{3}\sqrt{2}\left(x^2+3\right)x+\frac{25}{6\sqrt{2}}\right)+(x+1)^{2\sqrt{2}}\left(-e^{2\sqrt{2}c_1+\frac{x^4}{\sqrt{2}}+\sqrt{2}x^2}\right)+}$$

✓ **Maple** : cpu = 0.332 (sec), leaf count = 73

$$\left\{\ln\left(2\frac{x\left(\sqrt{2\left(y\left(x\right)\right)^2+2x^2}+y(x)+x\right)}{y\left(x\right)-x}\right)+\sqrt{2}\ln\left(1+x\right)+\frac{\left(3x^4-4x^3+6x^2-12x\right)\sqrt{2}}{12}-\_C1-\ln\left(x\right)=\right.$$

2.876 ODE No. 876

$$y'(x)=-\frac{y(x)^2\left(x^2y(x)-2xy(x)+y(x)-2x\right)}{2x(xy(x)-2y(x)-2)}$$

✓ **Mathematica** : cpu = 0.0194735 (sec), leaf count = 135

$$\left\{\left\{y(x)\to-\frac{4x}{\frac{2\sqrt{-4x\left(c_1-2\left(\frac{x^2}{8}-\frac{x}{2}+\frac{\log(x)}{4}\right)\right)-x(x-2)^2}}{\sqrt{-\frac{1}{x}}}-2(x-2)x}\right\},\left\{y(x)\to\frac{4x}{\frac{2\sqrt{-4x\left(c_1-2\left(\frac{x^2}{8}-\frac{x}{2}+\frac{\log(x)}{4}\right)\right)-x(x-2)^2}}{\sqrt{-\frac{1}{x}}}+2}\right.\right.$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 41

$$\left\{y(x)=-4\left(\sqrt{\_C1-8\ln\left(x\right)}-2x+4\right)^{-1},y(x)=4\left(\sqrt{\_C1-8\ln\left(x\right)}+2x-4\right)^{-1}\right\}$$

2.877 ODE No. 877

$$y'(x) = \frac{x^6 - 3x^4 y(x) + 2x^3 + 3x^2 y(x)^2 - 2xy(x) - y(x)^3 - 2x}{x^2 - y(x) - 1}$$

✓ **Mathematica** : cpu = 0.017231 (sec), leaf count = 49

$$\left\{\left\{y(x) \to \frac{1}{1 - \frac{1}{\sqrt{c_1 - 2x}}} + x^2 - 1\right\}, \left\{y(x) \to \frac{1}{\frac{1}{\sqrt{c_1 - 2x}} + 1} + x^2 - 1\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 73

$$\left\{y(x) = \frac{1}{2x - 2\_C1}\left(-2x^2\_C1 + 2x^3 + \sqrt{2\_C1 - 2x + 1} - 1\right), y(x) = \frac{1}{-2x + 2\_C1}\left(2x^2\_C1 - 2x^3 + \sqrt{}\right.\right.$$

2.878 ODE No. 878

$$y'(x) = \frac{-64a^3x^3 + 48a^2x^2y(x)^2 + 16a^2x^2 - 12axy(x)^4 - 8axy(x)^2 + y(x)^6 + y(x)^4 + 1}{y(x)}$$

✓ **Mathematica** : cpu = 0.28554 (sec), leaf count = 130

$$\text{Solve}\left[2a\left(x - \frac{1}{2}\text{RootSum}\left[64\#1^3a^3 - 48\#1^2a^2y(x)^2 - 16\#1^2a^2 + 12\#1ay(x)^4 + 8\#1ay(x)^2 + 2a - y(x)^6 - y(x\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = (1+y(x)^4-8*a*x*y(x)^2+16*a^2*x^2+y(x)^6-12*y(x)^4*a*x+48*y(x)^2*a^2*x
64*a^3*x^3)/y(x),y(x))
```

2.879 ODE No. 879

$$y'(x) = \frac{x^2\left(-\sqrt{x^2 + y(x)^2}\right) + xy(x)\sqrt{x^2 + y(x)^2} + xy(x) + y(x)}{x(x+1)}$$

✓ **Mathematica** : cpu = 0.159135 (sec), leaf count = 135

$$\left\{\left\{y(x) \to \frac{x\left(-2(x+1)^{\sqrt{2}}e^{\sqrt{2}c_1 + \sqrt{2}x} + e^{2\sqrt{2}c_1 + 2\sqrt{2}x} - (x+1)^{2\sqrt{2}}\right)}{2(x+1)^{\sqrt{2}}e^{\sqrt{2}c_1 + \sqrt{2}x} + e^{2\sqrt{2}c_1 + 2\sqrt{2}x} - (x+1)^{2\sqrt{2}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.282 (sec), leaf count = 55

$$\left\{\ln\left(2\,\frac{x\left(\sqrt{2\,(y(x))^2+2\,x^2}+y(x)+x\right)}{y(x)-x}\right)+\sqrt{2}x-\ln(x)-\sqrt{2}\ln(1+x)-\_C1=0\right\}$$

2.880 ODE No. 880

$$y'(x)=-\frac{2a}{128a^4x^3-96a^3x^2y(x)^2-32a^3x^2+24a^2xy(x)^4+16a^2xy(x)^2-2ay(x)^6-2ay(x)^4-2a-y(x)}$$

✓ **Mathematica** : cpu = 0.137855 (sec), leaf count = 131

$$\text{Solve}\left[\frac{\text{RootSum}\left[-64\#1^3a^3+48\#1^2a^2y(x)^2+16\#1^2a^2-12\#1ay(x)^4-8\#1ay(x)^2+y(x)^6+y(x)^4+1\&,\,\overline{48\#}\right.}{8a^2}\right.$$

✓ **Maple** : cpu = 0.07 (sec), leaf count = 41

$$\left\{\frac{y(x)}{2\,a}+\frac{\int^{(y(x))^2-4\,ax}\left(\_a^3+\_a^2+1\right)^{-1}d\_a}{8\,a^2}-\_C1=0\right\}$$

2.881 ODE No. 881

$$y'(x)=\frac{x^6+9x^4y(x)-6x^3+27x^2y(x)^2-18xy(x)+27y(x)^3-18x}{9x^2+27y(x)+27}$$

✓ **Mathematica** : cpu = 0.0181279 (sec), leaf count = 75

$$\left\{\left\{y(x)\to\frac{1}{27\left(\frac{1}{27}-\frac{1}{\sqrt{c_1-1458x}}\right)}+\frac{1}{3}\left(-x^2-3\right)\right\},\left\{y(x)\to\frac{1}{27\left(\frac{1}{\sqrt{c_1-1458x}}+\frac{1}{27}\right)}+\frac{1}{3}\left(-x^2-3\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 77

$$\left\{y(x)=\frac{1}{-6\,x+6\,\_C1}\left(-2\,x^2\_C1+2\,x^3-3\,\sqrt{2\,\_C1-2\,x+1}+3\right),y(x)=\frac{1}{-6\,x+6\,\_C1}\left(-2\,x^2\_C1+2\,x^3\right.\right.$$

2.882 ODE No. 882

$$y'(x)=-\frac{1}{216}\sqrt{x}\left(-108x^{3/2}+x^9-18x^6y(x)-6x^6+108x^3y(x)^2+72x^3y(x)-216y(x)^3-216y(x)^2-216\right)$$

✓ **Mathematica** : cpu = 0.077347 (sec), leaf count = 119

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{\frac{1}{2}\left(2\sqrt{x}-x^{7/2}\right)+3\sqrt{x}y(x)}{\sqrt[3]{29}\sqrt[3]{x^{3/2}}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]=c_1+\frac{2}{27}29^{2/3}\sqrt{x}\left(x^{3/2}\right.\right.$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 41

$$\left\{y(x)=\frac{x^3}{6}-\frac{1}{3}+\frac{29}{9}RootOf\left(2\,x^{3/2}-243\int^{\_Z}\left(841\,\_a^3-27\,\_a+27\right)^{-1}d\_a+9\,\_C1\right)\right\}$$

2.883 ODE No. 883

$$y'(x)=\frac{x\left(a^3y(x)^6+a^3y(x)^4+a^3+3a^2bx^2y(x)^4+2a^2bx^2y(x)^2+3ab^2x^4y(x)^2+ab^2x^4+b^3x^6\right)}{a^{7/2}y(x)}$$

✓ **Mathematica** : cpu = 1.45749 (sec), leaf count = 164

$$\text{Solve}\left[\frac{x^2}{2}-\frac{1}{2}a^{5/2}\text{RootSum}\left[\#1^3b^3+3\#1^2ab^2y(x)^2+\#1^2ab^2+3\#1a^2by(x)^4+2\#1a^2by(x)^2+a^{5/2}b+a^3y(x)^6\right.\right.$$

✓ **Maple** : cpu = 0.848 (sec), leaf count = 352

$$\left\{\int_{\_b}^{x}\left(b^3\_a^6+3\left(y(x)\right)^2ab^2\_a^4+3\left(y(x)\right)^4a^2b\_a^2+\left(y(x)\right)^6a^3+a\_a^4b^2+2\left(y(x)\right)^2a^2b\_a^2+\left(y(x)\right)^4a^3+a^3\right)\right.$$

2.884 ODE No. 884

$$y'(x)=-\frac{x\left(x^6-3x^4y(x)^2-x^4+3x^2y(x)^4+2x^2y(x)^2-y(x)^6-y(x)^4-1\right)}{y(x)}$$

✓ **Mathematica** : cpu = 0.36532 (sec), leaf count = 71

$$\text{Solve}\left[\frac{1}{4}\left(2\log\left(-x^2+y(x)^2+1\right)-2x^2-\frac{1}{y(x)(y(x)+x)}+\frac{1}{xy(x)-y(x)^2}-2\log(x-y(x))-2\log(y(x)+x)\right)\right.$$

✓ **Maple** : cpu = 0.423 (sec), leaf count = 107

$$\left\{ y(x) = \mathrm{e}^{\mathit{RootOf}\left(-3\,x^{2}\left(\mathrm{e}^{-Z}\right)^{2}+6\,x^{3}\mathrm{e}^{-Z}+3\left(\mathrm{e}^{-Z}\right)^{2}\ln\left(\frac{\left(\mathrm{e}^{-Z}\right)^{2}-2\,x\mathrm{e}^{-Z}+1}{\mathrm{e}^{-Z}-2\,x}\right)-2\_C1\left(\mathrm{e}^{-Z}\right)^{2}-3\_Z\left(\mathrm{e}^{-Z}\right)^{2}-6\,\mathrm{e}^{-Z}\ln\left(\frac{\left(\mathrm{e}^{-Z}\right)^{2}-2\,x\mathrm{e}^{-Z}+1}{\mathrm{e}^{-Z}-2\,x}\right)x\right.}\right.$$

2.885 ODE No. 885

$$y'(x) = -\frac{i\left(x^6+12x^4y(x)^2+4x^4+48x^2y(x)^4+32x^2y(x)^2+64y(x)^6+64y(x)^4+32ix+64\right)}{128y(x)}$$

✗ **Mathematica** : cpu = 40.7513 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-I/128)*(64 + (32*I)*x + 4*x^4 + x^6 + 32*x^2*y[x]^2 + 12*x^
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = -1/128*I*(32*I*x+64+64*y(x)^4+32*x^2*y(x)^2+4*x^4+64*y(x)^6+48*x^2*y(x
```

2.886 ODE No. 886

$$y'(x) = \frac{x^6y(x)^3-3x^5y(x)^2+x^4y(x)^2+3x^4y(x)-4x^3y(x)-x^3+2x^2+1}{x^4}$$

✓ **Mathematica** : cpu = 0.0587644 (sec), leaf count = 82

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{3x^2y(x)-3x+1}{\sqrt[3]{29}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]=c_1-\frac{29^{2/3}}{9x},y(x)\right]$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 42

$$\left\{ y(x) = \frac{9\,x-3+29\,\mathit{RootOf}\left(-81\int^{-Z}\left(841\_a^3-27\_a+27\right)^{-1}d\_ax+3\,x\_C1-1\right)}{9\,x^2} \right\}$$

2.887 ODE No. 887

$$y'(x) = \frac{a^3x^3y(x)^3 + 3a^2x^2y(x)^2 + a^2xy(x) + a^2x + 3axy(x) + a + 1}{a^2x^2(axy(x) + ax + 1)}$$

✓ **Mathematica** : cpu = 0.0255992 (sec), leaf count = 106

$$\left\{\left\{y(x) \to \frac{1}{a^3x^3\left(\frac{1}{a^3x^3} - \frac{1}{x^3\sqrt{c_1 - 2a^6x}}\right)} - \frac{ax+1}{ax}\right\}, \left\{y(x) \to \frac{1}{a^3x^3\left(\frac{1}{x^3\sqrt{c_1 - 2a^6x}} + \frac{1}{a^3x^3}\right)} - \frac{ax+1}{ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 72

$$\left\{y(x) = \frac{1}{ax}\left(-ax - \sqrt{\_C1 - 2\,x} - 1\right)\left(\sqrt{\_C1 - 2\,x} + 1\right)^{-1}, y(x) = \frac{1}{ax}\left(ax - \sqrt{\_C1 - 2\,x} + 1\right)\left(\sqrt{\_C1 - 2\,x}\right.\right.$$

2.888 ODE No. 888

$$y'(x) = \frac{x^4y(x)^3 - 5x^3y(x)^2 + 6x^2y(x) - 2xy(x) - 2x + 1}{x^2\left(x^2y(x) - x + 1\right)}$$

✓ **Mathematica** : cpu = 0.0190239 (sec), leaf count = 78

$$\left\{\left\{y(x) \to \frac{1}{x^4\left(\frac{1}{x^2} - \frac{1}{x^2\sqrt{c_1 + \frac{2}{x}}}\right)} + \frac{x-1}{x^2}\right\}, \left\{y(x) \to \frac{1}{x^4\left(\frac{1}{x^2\sqrt{c_1 + \frac{2}{x}}} + \frac{1}{x^2}\right)} + \frac{x-1}{x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.059 (sec), leaf count = 79

$$\left\{y(x) = \frac{1}{x^2}\left(\sqrt{\frac{\_C1 + 2}{x}}x - x + 1\right)\left(\sqrt{\frac{\_C1 + 2}{x}} - 1\right)^{-1}, y(x) = \frac{1}{x^2}\left(\sqrt{\frac{\_C1 + 2}{x}}x + x - 1\right)\left(\sqrt{\frac{\_C1 -}{x}}\right.\right.$$

2.889 ODE No. 889

$$y'(x) = -\frac{e^x\left(-8y(x)^{9/2} + 36e^x y(x)^3 - 8y(x)^3 + 24e^x y(x)^{3/2} - 54e^{2x}y(x)^{3/2} - 18e^{2x} + 27e^{3x} - 8\right)}{8\sqrt{y(x)}}$$

✗ **Mathematica** : cpu = 300.302 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.447 (sec), leaf count = 49

$$\left\{e^x + \frac{2}{3}\ln\left((y(x))^{\frac{3}{2}} - \frac{3\,e^x}{2}\right) - 4\left(-6\,(y(x))^{3/2} + 9\,e^x\right)^{-1} - \frac{2}{3}\ln\left((y(x))^{\frac{3}{2}} - \frac{3\,e^x}{2} + 1\right) - \_C1 = 0\right\}$$

2.890 ODE No. 890

$$y'(x) = \frac{x}{x^6 + 3x^4y(x)^2 + x^4 + 3x^2y(x)^4 + 2x^2y(x)^2 + y(x)^6 + y(x)^4 - y(x) + 1}$$

✓ **Mathematica** : cpu = 0.138815 (sec), leaf count = 103

$$\text{Solve}\left[y(x) - \frac{1}{2}\text{RootSum}\left[\#1^3 + 3\#1^2y(x)^2 + \#1^2 + 3\#1y(x)^4 + 2\#1y(x)^2 + y(x)^6 + y(x)^4 + 1\&, \frac{}{3\#1^2 + 6\#1}\right.\right.$$

✓ **Maple** : cpu = 1.19 (sec), leaf count = 34

$$\left\{-y(x) + \frac{\int^{(y(x))^2+x^2}\left(\_a^3 + \_a^2 + 1\right)^{-1} d\_a}{2} - \_C1 = 0\right\}$$

2.891 ODE No. 891

$$y'(x) = \frac{y(x)^2\left(x^4y(x) + 2x^2y(x) + 2x^2 - 2y(x)\right)}{x^3\left(x^2y(x) + x^2 - y(x)\right)}$$

✓ **Mathematica** : cpu = 0.0240771 (sec), leaf count = 135

$$\left\{\left\{y(x) \to \frac{x^5}{\frac{\sqrt{x^5\left(c_1 - 2\left(\frac{1}{2x^4} - \frac{1}{x^2} + \log(x)\right)\right) + (x^2-1)^2 x}}{\sqrt{\frac{1}{x^5}}} - x^3\left(x^2-1\right)}\right\}, \left\{y(x) \to -\frac{x^5}{\frac{\sqrt{x^5\left(c_1 - 2\left(\frac{1}{2x^4} - \frac{1}{x^2} + \log(x)\right)\right) + (x^2-1)^2 x}}{\sqrt{\frac{1}{x^5}}} +\right.\right.$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 56

$$\left\{y(x) = x^2\left(\sqrt{\_C1 - 2\ln(x)}x^2 - x^2 + 1\right)^{-1}, y(x) = -x^2\left(\sqrt{\_C1 - 2\ln(x)}x^2 + x^2 - 1\right)^{-1}\right\}$$

2.892 ODE No. 892

$$y'(x) = \frac{e^{-\frac{2}{x^2-y(x)^2-1}} + x^2 + 2xy(x) + y(x)^2}{-e^{-\frac{2}{x^2-y(x)^2-1}} + x^2 + 2xy(x) + y(x)^2}$$

✗ **Mathematica** : cpu = 300.011 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.645 (sec), leaf count = 40

$$\left\{y(x) = \mathrm{e}^{RootOf\left(-\_Z + \int \left(\mathrm{e}^{-\_Z}\right)^2 - 2x\mathrm{e}^{-\_Z}\left(\mathrm{e}^{2(1+\_a)^{-1}} + \_a\right)^{-1} d\_a + \_C1\right)} - x\right\}$$

2.893 ODE No. 893

$$y'(x) = \frac{x^3y(x)^3 + x^3y(x)^2 + x^3 + 6x^2y(x)^2 + 4x^2y(x) + 12xy(x) + 6x + 8}{x^3}$$

✓ **Mathematica** : cpu = 0.0632816 (sec), leaf count = 80

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3y(x)+\frac{x+6}{x}}{\sqrt[3]{29}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{1}{9}29^{2/3}x, y(x)\right]$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 41

$$\left\{y(x) = \frac{29\,RootOf\left(-81\int^{-Z}\left(841\,\_a^3 - 27\,\_a + 27\right)^{-1} d\_a + x + 3\,\_C1\right)x - 3x - 18}{9x}\right\}$$

2.894 ODE No. 894

$$y'(x) = -\frac{i\left(x^6 + 3x^4 y(x)^2 + x^4 + 3x^2 y(x)^4 + 2x^2 y(x)^2 + y(x)^6 + y(x)^4 + ix + 1\right)}{y(x)}$$

✗ **Mathematica** : cpu = 40.6658 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-I)*(1 + I*x + x^4 + x^6 + 2*x^2*y[x]^2 + 3*x^4*y[x]^2 + y[x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = -I*(I*x+1+x^4+2*x^2*y(x)^2+y(x)^4+x^6+3*x^4*y(x)^2+3*x^2*y(x)^4+y(x)^6
```

2.895 ODE No. 895

$$y'(x) = \frac{x\left(a^3x^{12} + 24a^2x^8 y(x) - 32a^2x^6 + 192ax^4 y(x)^2 - 256ax^2 y(x) - 256ax^2 + 512y(x)^3\right)}{64ax^4 + 512y(x) + 512}$$

✓ **Mathematica** : cpu = 0.0253003 (sec), leaf count = 81

$$\left\{\left\{y(x) \to \frac{1}{8}\left(-ax^4 - 8\right) + \frac{1}{512\left(\frac{1}{512} - \frac{1}{\sqrt{c_1 - 262144x^2}}\right)}\right\}, \left\{y(x) \to \frac{1}{8}\left(-ax^4 - 8\right) + \frac{1}{512\left(\frac{1}{\sqrt{c_1 - 262144x^2}} + \frac{1}{512}\right)}\right\}$$

✓ **Maple** : cpu = 0.064 (sec), leaf count = 79

$$\left\{y(x) = 1\left(-8 + \left(-\sqrt{-x^2 + \_C1} - 1\right)ax^4\right)\left(8 + 8\sqrt{-x^2 + \_C1}\right)^{-1}, y(x) = 1\left(8 + \left(-\sqrt{-x^2 + \_C1} + 1\right)ax\right.\right.$$

2.896 ODE No. 896

$$y'(x) = \frac{-x^6 + 3x^4 y(x)^2 + x^4 - 3x^2 y(x)^4 - 2x^2 y(x)^2 + y(x)^6 + y(x)^4 + x + 1}{y(x)}$$

✓ **Mathematica** : cpu = 0.218913 (sec), leaf count = 106

$$\text{Solve}\left[\frac{1}{2}\text{RootSum}\left[-\#1^3 + 3\#1^2 y(x)^2 + \#1^2 - 3\#1 y(x)^4 - 2\#1 y(x)^2 + y(x)^6 + y(x)^4 + 1\&, \frac{\log}{3\#1^2 - 6\#1 y(x)^2}\right.\right.$$

✓ **Maple** : cpu = 0.928 (sec), leaf count = 63

$$\left\{\int_{\_b}^{y(x)} \frac{\_a}{-\_a^6 + 3\,\_a^4 x^2 - 3\,\_a^2 x^4 + x^6 - \_a^4 + 2\,\_a^2 x^2 - x^4 - 1}\,\mathrm{d}\_a + x - \_C1 = 0\right\}$$

2.897 ODE No. 897

$$y'(x) = \frac{\sqrt{x}\left(-108x^{3/2}y(x) + 18x^{9/2} - 108x^{3/2} + x^9 - 18x^6y(x) + 108x^3y(x)^2 - 216y(x)^3\right)}{36x^3 - 216y(x) - 216}$$

✓ **Mathematica** : cpu = 0.0265432 (sec), leaf count = 79

$$\left\{\left\{y(x) \to \frac{1}{6}\left(x^3-6\right) - \frac{1}{216\left(-\frac{1}{\sqrt{c_1-62208x^{3/2}}} - \frac{1}{216}\right)}\right\}, \left\{y(x) \to \frac{1}{6}\left(x^3-6\right) - \frac{1}{216\left(\frac{1}{\sqrt{c_1-62208x^{3/2}}} - \frac{1}{216}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.093 (sec), leaf count = 87

$$\left\{y(x) = 1\left(\sqrt{9\_C1 - 12\,x^{3/2}}x^3 - 3\,x^3 + 18\right)\left(-18 + 6\sqrt{9\_C1 - 12\,x^{3/2}}\right)^{-1}, y(x) = 1\left(\sqrt{9\_C1 - 12\,x^{3/2}}x^3 +\right.\right.$$

2.898 ODE No. 898

$$y'(x) = \frac{4x^6y(x)^3 + 2x^5y(x) + 2x^5 + 3x^4y(x)^2 + \frac{x^3}{2} + \frac{3}{4}x^2y(x) + \frac{1}{16}}{x^6\left(4x^2y(x) + 4x^2 + 1\right)}$$

✓ **Mathematica** : cpu = 0.0224474 (sec), leaf count = 106

$$\left\{\left\{y(x) \to \frac{1}{64x^8\left(\frac{1}{64x^8} - \frac{1}{x^8\sqrt{c_1+\frac{8192}{x}}}\right)} - \frac{4x^2+1}{4x^2}\right\}, \left\{y(x) \to \frac{1}{64x^8\left(\frac{1}{x^8\sqrt{c_1+\frac{8192}{x}}} + \frac{1}{64x^8}\right)} - \frac{4x^2+1}{4x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 87

$$\left\{y(x) = \frac{1}{4\,x^2}\left(-4\,x^2 - \sqrt{\frac{x\_C1+2}{x}} - 1\right)\left(\sqrt{\frac{x\_C1+2}{x}} + 1\right)^{-1}, y(x) = \frac{1}{4\,x^2}\left(4\,x^2 - \sqrt{\frac{x\_C1+2}{x}} + 1\right)\left(\sqrt{\right.\right.$$

2.899 ODE No. 899

$$y'(x) = \frac{x^6 y(x)^3 + x^6 y(x)^2 + x^6 + \frac{x^5}{2} + \frac{3}{4}x^4 y(x)^2 + \frac{1}{2}x^4 y(x) + \frac{3}{16}x^2 y(x) + \frac{x^2}{16} + \frac{1}{64}}{x^8}$$

✓ **Mathematica** : cpu = 0.0692707 (sec), leaf count = 106

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{3y(x)}{x^2} + \frac{4x^2+3}{4x^4}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^6}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 - \frac{1}{9}29^{2/3}\left(\frac{1}{x^6}\right)^{2/3} x^3, y(x)\right]$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 47

$$\left\{y(x) = \frac{116\, RootOf\left(-81\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1} d\_ax + 3\, x\_C1 - 1\right) x^2 - 12\, x^2 - 9}{36\, x^2}\right\}$$

2.900 ODE No. 900

$$y'(x) = \frac{2a\left(4ax - y(x)^2 - 1\right)}{128a^4x^3 - 96a^3x^2y(x)^2 + 24a^2xy(x)^4 - 2ay(x)^6 + 4axy(x) - y(x)^3 - y(x)}$$

✓ **Mathematica** : cpu = 0.0927212 (sec), leaf count = 381

$$\left\{\left\{y(x) \to \text{Root}\left[8\#1^5 a - 16\#1^4 a^2 c_1 - 64\#1^3 a^2 x + \#1^2\left(128a^3 c_1 x - 2\right) + 128\#1 a^3 x^2 - 256a^4 c_1 x^2 + 8ax - 1\&,\right.\right.\right.$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 48

$$\left\{\frac{y(x)}{2\,a} + \left(32\,a^3 x - 8\,a^2 (y(x))^2\right)^{-1} - \frac{1}{16\,a^2\left((y\,(x))^2 - 4\,ax\right)^2} - \_C1 = 0\right\}$$

2.901 ODE No. 901

$$y'(x) = \frac{y(x)\left(-ax\log(y(x)) + x^2 + y(x)\right)}{x(ax - y(x) - y(x)\log(x) - y(x)\log(y(x)))}$$

✓ **Mathematica** : cpu = 0.0901434 (sec), leaf count = 33

$$\text{Solve}\left[ax\log(y(x)) - \frac{x^2}{2} - y(x)\log(x) - y(x)\log(y(x)) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 0.675 (sec), leaf count = 30

$$\left\{y(x) = \mathrm{e}^{RootOf\left(-2\_Z\, ax + 2\,\mathrm{e}^{-\_Z}\ln(x) + 2\_Z\,\mathrm{e}^{-\_Z} + 2\_C1\, a + x^2\right)}\right\}$$

2.902 ODE No. 902

$$y'(x) = \frac{x^6 - 3x^4y(x)^2 + x^3 + 3x^2y(x)^4 - xy(x)^2 - y(x)^6 - x}{y(x)\left(x^2 - y(x)^2 - 1\right)}$$

✓ **Mathematica** : cpu = 0.0989161 (sec), leaf count = 295

$$\left\{\left\{y(x) \to -\frac{1}{2}\sqrt{\frac{4x^3}{x-c_1} - \frac{4c_1x^2}{x-c_1} - \frac{\sqrt{4c_1 - 4x + 1}}{x-c_1} - \frac{1}{x-c_1}}\right\}, \left\{y(x) \to \frac{1}{2}\sqrt{\frac{4x^3}{x-c_1} - \frac{4c_1x^2}{x-c_1} - \frac{\sqrt{4c_1 - 4x +}}{x-c_1}}\right.\right.$$

✓ **Maple** : cpu = 0.297 (sec), leaf count = 183

$$\left\{y(x) = \frac{1}{2\_C1 + 6x}\sqrt{(\_C1 + 3x)\left(4x^2\_C1 + 12x^3 - \sqrt{-12\_C1 - 36x + 9} - 3\right)}, y(x) = \frac{1}{2\_C1 + 6x}\sqrt{(\right.$$

2.903 ODE No. 903

$$y'(x) = \frac{\sin\left(\frac{y(x)}{x}\right)\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\left(2x^2\sin\left(\frac{y(x)}{2x}\right)\cos\left(\frac{y(x)}{2x}\right) + y(x)\right)}{2x}$$

✓ **Mathematica** : cpu = 0.0495524 (sec), leaf count = 19

$$\left\{\left\{y(x) \to 2x\cot^{-1}\left(e^{-c_1 - x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 48

$$\left\{y(x) = \arctan\left(2\frac{\_C1\,\mathrm{e}^x}{\_C1^2\left(\mathrm{e}^x\right)^2 + 1}, \frac{-\_C1^2(\mathrm{e}^x)^2 + 1}{\_C1^2\left(\mathrm{e}^x\right)^2 + 1}\right)x\right\}$$

2.904 ODE No. 904

$$y'(x) = \frac{\sin\left(\frac{y(x)}{x}\right)\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\left(2x^3\sin\left(\frac{y(x)}{2x}\right)\cos\left(\frac{y(x)}{2x}\right)+y(x)\right)}{2x}$$

✓ **Mathematica** : cpu = 0.0511146 (sec), leaf count = 23

$$\left\{\left\{y(x)\to 2x\cot^{-1}\left(e^{-c_1-\frac{x^2}{2}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 64

$$\left\{y(x)=\arctan\left(2\,\frac{\mathrm{e}^{1/2\,x^2}\_C1}{\left(\mathrm{e}^{1/2\,x^2}\right)^2\_C1^{\,2}+1},1\left(-\left(\mathrm{e}^{\frac{x^2}{2}}\right)^2\_C1^{\,2}+1\right)\left(\left(\mathrm{e}^{\frac{x^2}{2}}\right)^2\_C1^{\,2}+1\right)^{-1}\right)x\right\}$$

2.905 ODE No. 905

$$y'(x) = \frac{a^3x^3y(x)^3+a^3x^3y(x)^2+a^3x^3+3a^2x^2y(x)^2+2a^2x^2y(x)+a^2x+3axy(x)+ax+1}{a^3x^3}$$

✓ **Mathematica** : cpu = 0.06236 (sec), leaf count = 85

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{\frac{ax+3}{ax}+3y(x)}{\sqrt[3]{29}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]=c_1+\frac{1}{9}29^{2/3}x,y(x)\right]$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 46

$$\left\{y(x)=\frac{29\,RootOf\left(-81\int^{\_Z}\left(841\_a^3-27\_a+27\right)^{-1}d\_a+x+3\,\_C1\right)ax-3\,ax-9}{9\,ax}\right\}$$

2.906 ODE No. 906

$$y'(x) = \frac{x\left(x^2 + y(x)^2 + 1\right)}{x^6 + 3x^4 y(x)^2 + 3x^2 y(x)^4 - x^2 y(x) + y(x)^6 - y(x)^3 - y(x)}$$

✓ **Mathematica** : cpu = 0.0517286 (sec), leaf count = 326

$$\left\{\left\{y(x) \to \text{Root}\left[4\#1^5 - 4\#1^4 c_1 + 8\#1^3 x^2 + \#1^2\left(2 - 8c_1 x^2\right) + 4\#1 x^4 - 4c_1 x^4 + 2x^2 + 1\&, 1\right]\right\}, \left\{y(x) \to \text{Root}\right.\right.$$

✓ **Maple** : cpu = 0.421 (sec), leaf count = 37

$$\left\{-\left(2x^2 + 2\left(y(x)\right)^2\right)^{-1} - \frac{1}{4\left(\left(y(x)\right)^2 + x^2\right)^2} - y(x) + \_C1 = 0\right\}$$

2.907 ODE No. 907

$$y'(x) = \frac{\frac{3x^2}{2} + x^2\sin(x) - 2x^2\cos(x) + \frac{1}{2}x^2\cos(2x) - 2xy(x) + y(x)^2 + 2xy(x)\cos(x) + x - x\cos(x)}{x}$$

✓ **Mathematica** : cpu = 0.0514381 (sec), leaf count = 22

$$\left\{\left\{y(x) \to \frac{1}{c_1 - \log(x)} - x(\cos(x) - 1)\right\}\right\}$$

✓ **Maple** : cpu = 0.178 (sec), leaf count = 20

$$\left\{y(x) = -(\cos(x) - 1)x + \left(\_C1 - \ln(x)\right)^{-1}\right\}$$

2.908 ODE No. 908

$$y'(x) = \frac{4(a-1)(a+1)x}{a^6x^4 - 3a^4x^4 - 2a^4x^2y(x)^2 + 3a^2x^4 + 4a^2x^2y(x)^2 + a^2y(x)^4 - x^4 - 2x^2y(x)^2 - y(x)^4 + 4y(x)}$$

✓ **Mathematica** : cpu = 1.46748 (sec), leaf count = 1278

$$\left\{\left\{y(x) \to -\frac{c_1}{3\left(1 - a^2\right)} + \frac{\sqrt[3]{18x^2c_1a^6 - 54x^2c_1a^4 - 54a^4 + 54x^2c_1a^2 + 108a^2 - 2c_1^3 - 18x^2c_1 + \sqrt{4\left(3\left(1 - a^2\right)\left(\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.484 (sec), leaf count = 1742

$$\left\{ y(x) = \frac{9^{\frac{2}{3}}}{27\,a^2 - 27}\left(\left(-\_C1\,a^2 + \_C1\right) \sqrt[3]{9} \sqrt[3]{\left(\frac{1}{3}\sqrt{-3\,(a-1)^5\,(a+1)^5\,x^6 + 6\,\_C1^2\,(a-1)^4\,(a+1)^4\,x^4 - 3\,\_} \right.} \right.$$

2.909 ODE No. 909

$$y'(x) = \frac{x^3 y(x)^6 + x^3 y(x)^4 + x^3 + 3x^2 y(x)^4 + 2x^2 y(x)^2 + 3xy(x)^2 + x + 1}{x^5 y(x)}$$

✗ **Mathematica** : cpu = 40.7378 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == (1 + x + x^3 + 3*x*y[x]^2 + 2*x^2*y[x]^2 + 3*x^2*y[x]^4 + x^3*
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x) = (x^3+y(x)^4*x^3+2*x^2*y(x)^2+x+x^3*y(x)^6+3*x^2*y(x)^4+3*x*y(x)^2+1)/x
```

2.910 ODE No. 910

$$y'(x) = \frac{x^6 + 3x^5 y(x) + 3x^4 y(x)^2 + x^4 + x^3 y(x)^3 + 2x^3 y(x) + x^2 y(x)^2 - y(x) - 2x + 1}{x}$$

✓ **Mathematica** : cpu = 0.0613521 (sec), leaf count = 98

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3x^3 + 3x^2 y(x) + x}{\sqrt[3]{29}\sqrt[3]{x^3}} - \#1 \right)}{\sqrt[3]{29} - 29\#1^2}\& \right] = c_1 + \frac{29^{2/3}\left(x^3\right)^{2/3}}{9x}, y(x) \right]$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 42

$$\left\{ y(x) = \frac{-9\,x^2 + 29\,RootOf\left(-81 \int^{-Z} \left(841\,\_a^3 - 27\,\_a + 27\right)^{-1} d\_a + x + 3\,\_C1 \right) - 3}{9\,x} \right\}$$

2.911 ODE No. 911

$$y'(x) = -y(x)\left(-\_\text{F1}(x) - \frac{\log(y(x))}{x} + \cot(x)\log(y(x))\right)$$

✓ **Mathematica** : cpu = 4.2711 (sec), leaf count = 56

$$\text{Solve}\left[\int_1^x \left(\frac{2\log(y(x))\sin(K[1])}{K[1]^2} - \frac{2(\log(y(x))\cos(K[1]) - \sin(K[1])\_\text{F1}(K[1]))}{K[1]}\right) dK[1] - 2\sin(1)\log(y(x)) =$$

✓ **Maple** : cpu = 0.681 (sec), leaf count = 30

$$\left\{y(x) = \mathrm{e}^{\frac{x\_C1}{\sin(x)}}\mathrm{e}^{\frac{x}{\sin(x)}\int \frac{\_F1(x)\sin(x)}{x}\,\mathrm{d}x}\right\}$$

2.912 ODE No. 912

$$y'(x) = \frac{2ax}{-128a^4 + 96a^3xy(x)^2 + 32a^3x - 24a^2x^2y(x)^4 - 16a^2x^2y(x)^2 + 2ax^3y(x)^6 + 2ax^3y(x)^4 + 2ax^3 - x^3y(x)}$$

✓ **Mathematica** : cpu = 1.52603 (sec), leaf count = 205

$$\text{Solve}\left[-\text{RootSum}\left[-\#1^3y(x)^6 - \#1^3y(x)^4 - \#1^3 + 12\#1^2ay(x)^4 + 8\#1^2ay(x)^2 - 48\#1a^2y(x)^2 - 16\#1a^2 + 64\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.913 ODE No. 913

$$y'(x) = \frac{y(x)^3 + y(x) + y(x)^3\left(-\log^3(x)\right) + y(x)^3\log^2(x) + 3y(x)^2\log^2(x) - 2y(x)^2\log(x) - 3y(x)\log(x) + 1}{xy(x)}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 3.729 (sec), leaf count = 43

$$\left\{y(x) = 9\left(9\ln(x) + 56\,RootOf\left(-81\int^{\_Z}\left(3136\,\_a^3 - 27\,\_a + 27\right)^{-1}d\_a - \ln(x) + 3\,\_C1\right) - 3\right)^{-1}\right\}$$

2.914 ODE No. 914

$$y'(x) = \frac{2a\left(-4a + xy(x)^2 + x\right)}{-128a^4 + 96a^3xy(x)^2 - 24a^2x^2y(x)^4 + 2ax^3y(x)^6 + 4ax^2y(x) - x^3y(x)^3 - x^3y(x)}$$

✓ **Mathematica** : cpu = 1.5778 (sec), leaf count = 401

$$\{\{y(x) \to \text{Root}\left[8\#1^5ax^2 - 8\#1^4ac_1x^2 - 64\#1^3a^2x + \#1^2\left(64a^2c_1x + 2x^2\right) + 128\#1a^3 - 128a^3c_1 - 8ax + x^2\&,\right.$$

✓ **Maple** : cpu = 4. (sec), leaf count = 71

$$\left\{\frac{x(y(x))^4 + (-4\,a + x)\,(y(x))^2 - 2\,a}{2\,a\,(y\,(x))^4\left(-x\,(y\,(x))^2 + 4\,a\right)^2} + \frac{8\,a(y(x))^5 + 2\,(y(x))^2 + 1}{16\,a^2\,(y\,(x))^4} + \_C1 = 0\right\}$$

2.915 ODE No. 915

$$y'(x) = \frac{y(x)^3 + y(x) - 8y(x)^3\log^3(x) + 4y(x)^3\log^2(x) + 12y(x)^2\log^2(x) - 4y(x)^2\log(x) - 6y(x)\log(x) + 1}{xy(x)}$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.072 (sec), leaf count = 43

$$\left\{y(x) = 9\left(18\,\ln(x) + 83\,RootOf\left(-81\int^{-Z}\left(6889\,\_a^3 - 27\,\_a + 27\right)^{-1}d\_a - \ln(x) + 3\,\_C1\right) - 3\right)^{-1}\right\}$$

2.916 ODE No. 916

$$y'(x) = \frac{y(x)\left(x^4\log^2(y(x)) + 2x^4\log(x)\log(y(x)) + x^4\log^2(x) + x\log(y(x)) + \log(y(x)) - x + x\log(x) + \log(x)\right.}{x(x+1)}$$

✗ **Mathematica** : cpu = 2.12239 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-1 - x + Log[x] + x*Log[x] + x^4*Log[x]^2 + Log[y[x]] + x*Lo
```

✓ **Maple** : cpu = 1.471 (sec), leaf count = 73

$$\left\{y(x) = \mathrm{e}^{\frac{-12\,\ln(x)\ln(1+x) + \left(-3\,x^4 + 4\,x^3 - 6\,x^2 + 12\,\_C1 + 12\,x\right)\ln(x) - 12\,x}{3\,x^4 - 4\,x^3 + 6\,x^2 + 12\,\ln(1+x) - 12\,\_C1 - 12\,x}}\right\}$$

2.917 ODE No. 917

$$y'(x) = \frac{y(x)\left(x\log^2(y(x)) + 2x\log(x)\log(y(x)) + x\log(y(x)) + \log(y(x)) - x + x\log^2(x) + x\log(x) + \log(x) - 1\right.}{x(x+1)}$$

✗ **Mathematica** : cpu = 1.23633 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-1 - x + Log[x] + x*Log[x] + x*Log[x]^2 + Log[y[x]] + x*Log[
```

✓ **Maple** : cpu = 0.398 (sec), leaf count = 38

$$\left\{y(x) = \mathrm{e}^{\frac{\ln(x)\ln(1+x)+(-x+\_C1)\ln(x)-x}{-\ln(1+x)-\_C1+x}}\right\}$$

2.918 ODE No. 918

$$y'(x) = \frac{2y(x)^8}{128x^3y(x)^6 + 32x^2y(x)^6 + 96x^2y(x)^4 + 2y(x)^6 + y(x)^5 + 16xy(x)^4 + 24xy(x)^2 + 2y(x)^2 + 2}$$

✗ **Mathematica** : cpu = 300.017 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 2.477 (sec), leaf count = 41

$$\left\{x - RootOf\left(\int^{\_Z} \left(64\_a^3 + 16\_a^2 + 1\right)^{-1} d\_a y(x) + \_C1\, y(x) + 1\right) + \frac{1}{4\,(y(x))^2} = 0\right\}$$

2.919 ODE No. 919

$$y'(x) = \frac{\left(-y(x) + \sqrt{y(x)} + x\right) y(x)^{3/2}}{x^3 - 3x^2y(x) + 3xy(x)^2 + xy(x)^{3/2} - y(x)^3 - y(x)^{5/2} + y(x)^2}$$

✗ **Mathematica** : cpu = 300.348 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.316 (sec), leaf count = 82

$$\left\{-\frac{1}{(x - y(x))^3}\left(\left(\_C1\, x^3 - 6x - 1\right)(y(x))^{\frac{5}{2}} + \left(-3x^2\_C1 + 3\right)(y(x))^{\frac{7}{2}} - (y(x))^{\frac{11}{2}}\,\_C1 + 3\,(y(x))^{3/2}x^2 + 3\,(y(\right.\right.$$

2.920 ODE No. 920

$$y'(x) = \frac{2y(x)^6\left(4xy(x)^2+y(x)^2+1\right)}{128x^3y(x)^6+96x^2y(x)^4+4xy(x)^5+y(x)^5+y(x)^3+24xy(x)^2+2}$$

✓ **Mathematica** : cpu = 0.243553 (sec), leaf count = 301

$$\left\{\left\{y(x)\to \text{Root}\left[\#1^5\left(128c_1x^2-8x-1\right)+128\#1^4x^2+\#1^3(64c_1x-2)+64\#1^2x+8\#1c_1+8\&,1\right]\right\},\{y(x)\to\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.921 ODE No. 921

$$y'(x) = -y(x)\left(-\_\text{F1}(x)-\frac{\log(y(x))}{x}+\frac{\log(y(x))}{x\log(x)}\right)$$

✓ **Mathematica** : cpu = 2.78495 (sec), leaf count = 52

$$\text{Solve}\left[\text{ConditionalExpression}\left[\int_1^x\left(\frac{\log(y(x))-\log(y(x))\log(K[1])}{K[1]^2}-\frac{\log(K[1])\_\text{F1}(K[1])}{K[1]}\right)dK[1]=c_1,\Re(x)>\right.\right.$$

✓ **Maple** : cpu = 0.367 (sec), leaf count = 30

$$\left\{y(x)=\mathrm{e}^{\frac{\_C1\,x}{\ln(x)}}\mathrm{e}^{\frac{x}{\ln(x)}\int\frac{\_F1(x)\ln(x)}{x}\,\mathrm{d}x}\right\}$$

2.922 ODE No. 922

$$y'(x) = \frac{y(x)^2}{x^3-3x^2y(x)+x^2\sqrt{y(x)}+3xy(x)^2-2xy(x)^{3/2}-y(x)^3+y(x)^{5/2}+y(x)^2+y(x)^{3/2}}$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.885 (sec), leaf count = 47

$$\left\{\frac{\ln\left(y(x)\right)}{2}-\int^x\frac{1}{\sqrt{y(x)}}-\sqrt{y(x)}\left(2\_a^3+2\_a^2-\_a+2\right)^{-1}d\_a-\_C1=0\right\}$$

2.923 ODE No. 923

$$y'(x) = \frac{x^2 + 2xy(x) + e^{-2(x-y(x))(y(x)+x)} + y(x)^2}{x^2 + 2xy(x) - e^{-2(x-y(x))(y(x)+x)} + y(x)^2}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.526 (sec), leaf count = 36

$$\left\{ y(x) = \mathrm{e}^{RootOf\left(-\_Z + \int \left(\mathrm{e}^{-\_Z}\right)^2 - 2\,\mathrm{e}^{-\_Z} x \left(\mathrm{e}^{2\,\_a} + \_a\right)^{-1} d\_a + \_C1\right)} - x \right\}$$

2.924 ODE No. 924

$$y'(x) = -\frac{y(x)\left(-\_\mathrm{F1}(x) - \frac{\log^2(y(x))}{2x}\right)}{\log(y(x))}$$

✓ **Mathematica** : cpu = 0.880462 (sec), leaf count = 55

$$\text{Solve}\left[\text{ConditionalExpression}\left[\int_1^x \left(-\frac{\_\mathrm{F1}(K[1])}{K[1]} - \frac{\log^2(y(x))}{2K[1]^2}\right) dK[1] + \frac{1}{2}\log^2(y(x)) = c_1, \Re(x) > 0 \vee x \notin \mathbb{R}\right],\right.$$

✓ **Maple** : cpu = 0.144 (sec), leaf count = 46

$$\left\{ y(x) = \mathrm{e}^{\sqrt{2\int \frac{-F1(x)}{x}\,\mathrm{d}x + 2\_C1\,x}}, y(x) = \mathrm{e}^{-\sqrt{2}\sqrt{x\left(\int \frac{-F1(x)}{x}\,\mathrm{d}x + \_C1\right)}} \right\}$$

2.925 ODE No. 925

$$y'(x) = \frac{x^2 + 2xy(x) + e^{2(x-y(x))^2(y(x)+x)^2} + y(x)^2}{x^2 + 2xy(x) - e^{2(x-y(x))^2(y(x)+x)^2} + y(x)^2}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.29 (sec), leaf count = 38

$$\left\{ y(x) = \mathrm{e}^{RootOf\left(-\_Z + \int \left(\mathrm{e}^{-\_Z}\right)^2 - 2\,\mathrm{e}^{-\_Z} x \left(\mathrm{e}^{2\,\_a^2} + \_a\right)^{-1} d\_a + \_C1\right)} - x \right\}$$

2.926 ODE No. 926

$$y'(x) = \frac{\frac{1}{16}x^3y(x)^3 - \frac{1}{2}x^2y(x)^3 - \frac{3}{8}x^2y(x)^2 + xy(x)^3 + xy(x)^2 + \frac{3}{4}xy(x) - \frac{1}{2}}{x(xy(x) - 2y(x) - 2)}$$

✓ **Mathematica** : cpu = 0.0245481 (sec), leaf count = 128

$$\left\{\left\{y(x) \to \frac{1}{16x(x-2)\left(-\frac{e^{2\left(\frac{1}{2}\log(2-x)-\frac{\log(x)}{2}\right)}}{\sqrt{c_1+2048\log(x)}} - \frac{1}{64}\right)} + \frac{2}{x-2}\right\}, \left\{y(x) \to \frac{1}{16x(x-2)\left(\frac{e^{2\left(\frac{1}{2}\log(2-x)-\frac{\log(x)}{2}\right)}}{\sqrt{c_1+2048\log(x)}} - \frac{1}{64}\right)}\right.$$

✓ **Maple** : cpu = 0.116 (sec), leaf count = 67

$$\left\{y(x) = 1\left(2\sqrt{\_C1 + 8\ln(x)} - 8\right)\left(x\sqrt{\_C1 + 8\ln(x)} - 4x + 8\right)^{-1}, y(x) = 1\left(2\sqrt{\_C1 + 8\ln(x)} + 8\right)\left(x\sqrt{\right.}\right.$$

2.927 ODE No. 927

$$y'(x) = -\frac{1}{8}x\Big(12e^{-x^2}x^2y(x)^2 + 8e^{-x^2}x^2y(x) + 8e^{-x^2}x^2 - 8e^{-x^2} + e^{-3x^2}x^6 - 6e^{-2x^2}x^4y(x) - 2e^{-2x^2}x^4 - 8y(x)^3 -$$

✓ **Mathematica** : cpu = 0.120702 (sec), leaf count = 112

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{1}{2}e^{-x^2}x\left(2e^{x^2}-3x^2\right)+3xy(x)}{\sqrt[3]{29}\sqrt[3]{x^3}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{1}{18}29^{2/3}\left(x^3\right)^2\right.$$

✓ **Maple** : cpu = 0.142 (sec), leaf count = 68

$$\left\{y(x) = \frac{58\,RootOf\left(x^2 - 162\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1}d\_a + 6\_C1\right) + \left(9x^2 - 6\,\mathrm{e}^{x^2}\right)\mathrm{e}^{-x^2}}{18\,\mathrm{e}^{-x^2}\mathrm{e}^{x^2}}\right\}$$

2.928 ODE No. 928

$$y'(x) = \frac{e^{\frac{y(x)}{x}}\left(x^2 e^{-\frac{y(x)}{x}} + x e^{-\frac{y(x)}{x}} + x e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} y(x) + x\right)}{x(x+1)}$$

✓ **Mathematica** : cpu = 1.40277 (sec), leaf count = 23

$$\left\{\left\{y(x) \to -x \log\left(-\frac{\log(x+1) - c_1}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.517 (sec), leaf count = 20

$$\left\{y(x) = -\ln\left(\frac{-\ln(1+x) + \_C1}{x}\right) x\right\}$$

2.929 ODE No. 929

$$y'(x) = \frac{-\frac{1}{32}x^3 y(x)^3 + \frac{1}{16}x^2 y(x)^3 + \frac{3}{16}x^2 y(x)^2 - \frac{1}{2}x y(x)^3 + \frac{y(x)^3}{4} - \frac{1}{4}x y(x)^2 - \frac{3}{8}x y(x) + \frac{y(x)}{4} + \frac{1}{4}}{x y(x)}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.06 (sec), leaf count = 42

$$\left\{y(x) = 18\left(58\, RootOf\left(-324\int^{\_Z}\left(841\,\_a^3 - 27\,\_a + 27\right)^{-1} d\_a - \ln(x) + 12\,\_C1\right) + 9x - 6\right)^{-1}\right\}$$

2.930 ODE No. 930

$$y'(x) = \frac{e^{\frac{y(x)}{x}}\left(x^4 + x^2 e^{-\frac{y(x)}{x}} + x e^{-\frac{y(x)}{x}} + x e^{-\frac{y(x)}{x}} y(x) + e^{-\frac{y(x)}{x}} y(x)\right)}{x(x+1)}$$

✓ **Mathematica** : cpu = 1.62408 (sec), leaf count = 39

$$\left\{\left\{y(x) \to -x \log\left(\frac{-c_1 - \frac{x^3}{3} + \frac{x^2}{2} - x + \log(x+1)}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.679 (sec), leaf count = 36

$$\left\{y(x) = -\ln\left(\frac{-2x^3 + 3x^2 + 6\ln(1+x) - 6\,\_C1 - 6x}{6x}\right) x\right\}$$

2.931 ODE No. 931

$$y'(x) = \frac{x^6 + 3x^5 y(x) + 3x^4 y(x)^2 + x^3 y(x)^3 - 2x^3 - 3x^2 y(x) - x y(x)^2 - y(x) - 2x}{x\left(x^2 + x y(x) + 1\right)}$$

✓ **Mathematica** : cpu = 0.0240771 (sec), leaf count = 80

$$\left\{\left\{y(x) \to \frac{1}{x^2\left(\frac{1}{x} - \frac{1}{x\sqrt{c_1 - 2x}}\right)} - \frac{x^2+1}{x}\right\}, \left\{y(x) \to \frac{1}{x^2\left(\frac{1}{x\sqrt{c_1-2x}} + \frac{1}{x}\right)} - \frac{x^2+1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 73

$$\left\{y(x) = \frac{1}{x}\left(-\sqrt{\_C1 - 2x}x^2 - x^2 - 1\right)\left(\sqrt{\_C1 - 2x} + 1\right)^{-1}, y(x) = \frac{1}{x}\left(-\sqrt{\_C1 - 2x}x^2 + x^2 + 1\right)\left(\sqrt{\_C1 -\right.\right.$$

2.932 ODE No. 932

$$y'(x) = \frac{e^{-\frac{3x^2}{2}} x\left(3e^{3x^2} y(x)^3 + e^{\frac{9x^2}{2}} y(x)^3 + 18e^{3x^2} y(x)^2 + 9e^{\frac{9x^2}{2}} y(x)^2 + 27e^{3x^2} y(x) + 27e^{\frac{9x^2}{2}} y(x) + 27e^{\frac{9x^2}{2}} + 27y(\right.}{243y(x)}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.396 (sec), leaf count = 54

$$\left\{y(x) = -369\frac{e^{3/2\,x^2}}{123 + 123\,e^{3/2\,x^2} - 136\,RootOf\left(-41\,x^2 - 50243409\int^{-Z}(9248\,\_a^3 - 1860867\,\_a + 1860867)^{-1}\,d\right.\right.$$

2.933 ODE No. 933

$$y'(x) = \frac{x^3 + x^3\left(-\log^3(x)\right) + x^3\log^2(x) + 3x^2 y(x)\log^2(x) - 2x^2 y(x)\log(x) + x^2 + x y(x)^2 + x y(x) + y(x)^3 - 3x}{x^2}$$

✓ **Mathematica** : cpu = 0.0809593 (sec), leaf count = 99

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{3y(x)}{x^2} + \frac{1-3\log(x)}{x}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{29^{2/3}}{9\sqrt[3]{\frac{1}{x^3}}}, y(x)\right]$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 39

$$\left\{y(x)=\frac{x\left(9\ln(x)-3+29\,RootOf\left(-81\int^{-Z}\left(841\_a^3-27\_a+27\right)^{-1}d\_a+x+3\_C1\right)\right)}{9}\right\}$$

2.934 ODE No. 934

$$y'(x)=-\frac{x^6}{64}-\frac{3x^5}{32}+\frac{3}{16}x^4y(x)-\frac{x^4}{8}+\frac{3}{4}x^3y(x)+\frac{x^3}{8}-\frac{3}{4}x^2y(x)^2+\frac{1}{4}x^2y(x)+\frac{x^2}{4}-\frac{3}{2}xy(x)^2-xy(x)+y(x)^3+y(x)^2+\frac{x}{2}+$$

✓ **Mathematica** : cpu = 0.113474 (sec), leaf count = 102

$$\text{Solve}\left[-\frac{31}{3}\text{RootSum}\left[-31\#1^3+3\,2^{2/3}\sqrt[3]{31}\#1-31\&,\frac{\log\left(\sqrt[3]{\frac{2}{31}}\left(\frac{1}{4}\left(-3x^2-6x+4\right)+3y(x)\right)-\#1\right)}{2^{2/3}\sqrt[3]{31}-31\#1^2}\&\right]=c_1+\right.$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 39

$$\left\{y(x)=\frac{x^2}{4}+\frac{x}{2}+RootOf\left(-x+2\int^{-Z}\left(2\_a^3+2\_a^2+1\right)^{-1}d\_a+\_C1\right)\right\}$$

2.935 ODE No. 935

$$y'(x)=\frac{x^6}{64}-\frac{3x^5}{16}+\frac{3}{16}x^4y(x)+\frac{13x^4}{16}-\frac{3}{2}x^3y(x)-\frac{3x^3}{2}+\frac{3}{4}x^2y(x)^2+\frac{7}{2}x^2y(x)+x^2-3xy(x)^2-2xy(x)+y(x)^3+y(x)^2-\frac{x}{2}$$

✓ **Mathematica** : cpu = 10.1907 (sec), leaf count = 248

$$\text{Solve}\left[\frac{\sqrt[3]{2}\left(\frac{\frac{1}{4}\left(3x^2-12x+4\right)+3y(x)}{\sqrt[3]{2}}+2^{2/3}\right)\left(2^{2/3}-2^{2/3}\left(\frac{1}{4}\left(3x^2-12x+4\right)+3y(x)\right)\right)\left(\left(\frac{1}{4}\left(-3x^2+12x-4\right)-3y(x)+\right.\right.\right.}{9\left(-\left(\frac{1}{4}\left(3x^2-12x+4\right)+\right.\right.}$$

✓ **Maple** : cpu = 0.316 (sec), leaf count = 55

$$\left\{y(x)=\frac{\mathrm{e}^{RootOf\left(\ln\left(\mathrm{e}^{-Z}-4\right)\mathrm{e}^{-Z}+\_C1\,\mathrm{e}^{-Z}-\_Z\,\mathrm{e}^{-Z}+\mathrm{e}^{-Z}x-4\ln\left(\mathrm{e}^{-Z}-4\right)-4\_C1+4\_Z-4x+4\right)}}{4}-1-\frac{x^2}{4}+x\right\}$$

2.936 ODE No. 936

$$y'(x)=\frac{x^6}{512}-\frac{3x^5}{256}+\frac{3}{64}x^4y(x)+\frac{5x^4}{128}-\frac{3}{16}x^3y(x)-\frac{5x^3}{64}+\frac{3}{8}x^2y(x)^2+\frac{7}{16}x^2y(x)+\frac{x^2}{16}-\frac{3}{4}xy(x)^2-\frac{1}{2}xy(x)+y(x)^3+y(x)$$

✓ **Mathematica** : cpu = 0.101505 (sec), leaf count = 99

$$\text{Solve}\left[-\frac{89}{3}\text{RootSum}\left[-89\#1^3+6\sqrt[3]{178}\#1-89\&,\frac{\log\left(\frac{2^{2/3}\left(\frac{1}{8}\left(3x^2-6x+8\right)+3y(x)\right)}{\sqrt[3]{89}}-\#1\right)}{2\sqrt[3]{178}-89\#1^2}\&\right]=c_1+\frac{89^{2/3}x}{18\sqrt[3]{2}},y(x)\right]$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 39

$$\left\{y(x)=-\frac{x^2}{8}+\frac{x}{4}+RootOf\left(-x+4\int^{\_Z}\left(4\_a^3+4\_a^2+3\right)^{-1}d\_a+\_C1\right)\right\}$$

2.937 ODE No. 937

$$y'(x)=\frac{2xy(x)^3+y(x)^3-2y(x)+6xy(x)\log^2(2x+1)+3y(x)\log^2(2x+1)+6xy(x)^2\log(2x+1)+3y(x)^2\log(}{(2x+1)(y(x)+\log(2x+1)+1)}$$

✓ **Mathematica** : cpu = 0.0272439 (sec), leaf count = 124

$$\left\{\left\{y(x)\to\frac{1}{(2x+1)\left(\frac{2x+1}{4x^2+4x+1}-\frac{1}{(2x+1)\sqrt{c_1-2x}}\right)}-\log(2x+1)-1\right\},\left\{y(x)\to\frac{1}{(2x+1)\left(\frac{1}{(2x+1)\sqrt{c_1-2x}}+\frac{2x+1}{4x^2+4x}\right.}\right.$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 79

$$\left\{y(x)=1\left(-\sqrt{\_C1-2x}\ln(2x+1)-\ln(2x+1)-1\right)\left(\sqrt{\_C1-2x}+1\right)^{-1},y(x)=1\left(-\sqrt{\_C1-2x}\ln(2x\right.\right.$$

2.938 ODE No. 938

$$y'(x)=\frac{x^6-3x^5+3x^4y(x)+4x^4-6x^3y(x)-3x^3+3x^2y(x)^2+5x^2y(x)-x^2-3xy(x)^2-2xy(x)+y(x)^3+y(}{x}$$

✓ **Mathematica** : cpu = 0.0651164 (sec), leaf count = 108

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{\frac{3x^2-3x+1}{x}+\frac{3y(x)}{x}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]=c_1+\frac{1}{9}29^{2/3}\left(\frac{1}{x^3}\right)^{2/3}x^2\log(\right.$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 39

$$\left\{y(x) = -x^2 + x - \frac{1}{3} + \frac{29\,RootOf\left(-81\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1}d\_a + \ln(x) + 3\_C1\right)}{9}\right\}$$

2.939 ODE No. 939

$$y'(x) = \frac{x^6 + 6x^5 - 12x^4y(x) + 12x^4 - 48x^3y(x) + 16x^3 + 48x^2y(x)^2 - 48x^2y(x) + 16x^2 + 96xy(x)^2 - 32xy(x) -}{16x^2 - 64y(x) + 32x - 64}$$

✓ **Mathematica** : cpu = 0.403025 (sec), leaf count = 136

$$\text{Solve}\left[\frac{2}{5}\text{RootSum}\left[\#1^4 + 4\#1^3 - 8\#1^2y(x) - 16\#1y(x) - 8\#1 + 16y(x)^2 + 16y(x) + 8\&, \frac{\#1^2(-\log(x - \#1)) -}{}\right.\right.$$

✓ **Maple** : cpu = 0.184 (sec), leaf count = 70

$$\left\{x - \frac{4}{5}\ln\left(y(x) - \frac{x^2}{4} - \frac{x}{2} - 1\right) + \frac{2}{5}\ln\left(2\left(y(x) - 1/4\,x^2 - x/2\right)^2 + 2\,y(x) - \frac{x^2}{2} - x + 1\right) - \frac{2}{5}\arctan\left(-2\,y(x)\right.\right.$$

2.940 ODE No. 940

$$y'(x) = \frac{x^3\log^3(x) - 3x^2y(x)\log^2(x) - x^2 + x^2\log(x) - y(x)^3 - y(x)^2 - 2xy(x) + 3xy(x)^2\log(x) + xy(x)\log(x)}{x(-y(x) - x + x\log(x))}$$

✓ **Mathematica** : cpu = 0.0214292 (sec), leaf count = 80

$$\left\{\left\{y(x) \to -\frac{1}{x\left(-\frac{1}{x^2\sqrt{c_1 - 2x}} - \frac{1}{x^2}\right)} - x + x\log(x)\right\}, \left\{y(x) \to -\frac{1}{x\left(\frac{1}{x^2\sqrt{c_1 - 2x}} - \frac{1}{x^2}\right)} - x + x\log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 63

$$\left\{y(x) = x\left(\sqrt{\_C1 - 2\,x}\ln(x) - \ln(x) + 1\right)\left(\sqrt{\_C1 - 2\,x} - 1\right)^{-1}, y(x) = x\left(\sqrt{\_C1 - 2\,x}\ln(x) + \ln(x) - 1\right)\right.$$

2.941 ODE No. 941

$$y'(x) = \frac{x^6 - 12x^5 + 12x^4 y(x) + 48x^4 - 96x^3 y(x) - 72x^3 + 48x^2 y(x)^2 + 192x^2 y(x) + 32x^2 - 192x y(x)^2 - 32x y(}{16x^2 + 64y(x) - 64x + 64}$$

✓ **Mathematica** : cpu = 0.364561 (sec), leaf count = 53

$$\text{Solve}\left[x - 8\text{RootSum}\left[11776\#1^3 - 40\#1 - 1\&, \#1 \log\left(17664\#1^2 - 1472\#1 + 11x^2 + 44y(x) - 44x - 40\right)\&\right] = c\right.$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 35

$$\left\{y(x) = -\frac{x^2}{4} + x + RootOf\left(-x + \int^{-Z} \frac{\_a + 1}{\_a^3 - \_a - 1} d\_a + \_C1\right)\right\}$$

2.942 ODE No. 942

$$y'(x) = \frac{-\exp\left(\frac{2(x-y(x))^3 (y(x)+x)^3}{x^2 - y(x)^2 - 1}\right) - x^2 - 2xy(x) - y(x)^2}{\exp\left(\frac{2(x-y(x))^3 (y(x)+x)^3}{x^2 - y(x)^2 - 1}\right) - x^2 - 2xy(x) - y(x)^2}$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.63 (sec), leaf count = 43

$$\left\{y(x) = \mathrm{e}^{RootOf\left(-\_Z + \int \left(\mathrm{e}^{-\_Z}\right)^2 - 2\,\mathrm{e}^{-\_Z} x \left(\mathrm{e}^{2\frac{\_a^3}{-\_a+1}} + \_a\right)^{-1} d\_a + \_C1\right)} - x\right\}$$

2.943 ODE No. 943

$$y'(x) = \frac{x^6 - 6x^5 + 24x^4 y(x) + 12x^4 - 96x^3 y(x) - 24x^3 + 192x^2 y(x)^2 + 96x^2 y(x) + 32x^2 - 384x y(x)^2 - 128x y(}{64x^2 + 512y(x) - 128x + 512}$$

✓ **Mathematica** : cpu = 0.407455 (sec), leaf count = 53

$$\text{Solve}\left[x - 16\text{RootSum}\left[6656\#1^3 - 23\#1 - 1\&, \#1 \log\left(79872\#1^2 - 18304\#1 + 181x^2 + 1448y(x) - 362x - 184\right)\right.\right.$$

✓ **Maple** : cpu = 0.057 (sec), leaf count = 40

$$\left\{y(x) = -\frac{x^2}{8} + \frac{x}{4} + RootOf\left(-x + \int^{-Z} 4\frac{\_a + 1}{4\_a^3 - \_a - 1} d\_a + \_C1\right)\right\}$$

2.944 ODE No. 944

$$y'(x)=\frac{a^3x^6+6a^2bx^5+12a^2x^4y(x)-8a^2x^3+12ab^2x^4+48abx^3y(x)-16abx^2+48ax^2y(x)^2-32axy(x)-32a}{16ax^2+32bx+64y(x)+64}$$

✓ **Mathematica** : cpu = 1.72994 (sec), leaf count = 233

$$\text{Solve}\left[x-4\text{RootSum}\left[\#1^6a^3+6\#1^5a^2b+12\#1^4a^2y(x)+12\#1^4ab^2+48\#1^3aby(x)+8\#1^3b^3+8\#1^2ab+48\#\right.\right.$$

✓ **Maple** : cpu = 0.091 (sec), leaf count = 47

$$\left\{y(x)=-\frac{ax^2}{4}-\frac{bx}{2}+RootOf\left(bx+2\int^{-Z}-\frac{b(\_a+1)}{2\_a^3+\_a\,b+b}d\_a+2\_C1\right)\right\}$$

2.945 ODE No. 945

$$y'(x)=\frac{8a^3x^3+12a^2x^4+48a^2x^2y(x)+6ax^5+48ax^3y(x)-16ax^2+96axy(x)^2+x^6+12x^4y(x)-8x^3+48x^2y}{32ax+16x^2+64y(x)+64}$$

✓ **Mathematica** : cpu = 1.2909 (sec), leaf count = 213

$$\text{Solve}\left[x-4\text{RootSum}\left[\#1^6+6\#1^5a+12\#1^4a^2+12\#1^4y(x)+8\#1^3a^3+48\#1^3ay(x)+48\#1^2a^2y(x)+8\#1^2a\right.\right.$$

✓ **Maple** : cpu = 0.08 (sec), leaf count = 41

$$\left\{y(x)=-\frac{x^2}{4}-\frac{ax}{2}+RootOf\left(-x+\int^{-Z}2\,\frac{\_a+1}{2\_a^3+\_a\,a+a}d\_a+\_C1\right)\right\}$$

2.946 ODE No. 946

$$y'(x)=\frac{x\left(12e^{-x^2}x^2y(x)^2+8e^{-x^2}x^2y(x)-8e^{-x^2}y(x)+4e^{-2x^2}x^2+8e^{-x^2}x^2-8e^{-x^2}+e^{-3x^2}x^6-6e^{-2x^2}x^4y(x)\right.}{4e^{-x^2}x^2-8y(x)-8}$$

✓ **Mathematica** : cpu = 0.0821023 (sec), leaf count = 150

$$\left\{\left\{y(x)\to\frac{e^{-3x^2}}{8\left(\frac{1}{8}e^{-3x^2}-\frac{e^{-3x^2}}{\sqrt{c_1-64x^2}}\right)}-\frac{1}{2}e^{-x^2}\left(2e^{x^2}-x^2\right)\right\},\left\{y(x)\to\frac{e^{-3x^2}}{8\left(\frac{e^{-3x^2}}{\sqrt{c_1-64x^2}}+\frac{1}{8}e^{-3x^2}\right)}-\frac{1}{2}e^{-x^2}\left(2e^{x^2}-x\right.\right.\right.$$

✓ **Maple** : cpu = 0.187 (sec), leaf count = 85

$$\left\{y(x)=1\left(-2+x^2\left(1+\sqrt{-x^2+\_C1}\right)\mathrm{e}^{-x^2}\right)\left(2\sqrt{-x^2+\_C1}+2\right)^{-1},y(x)=1\left(2+x^2\left(-1+\sqrt{-x^2+\_C1}\right)\right.\right.$$

2.947 ODE No. 947

$$y'(x)=\frac{x^3\sin(x)+x^2y(x)^2+2x^2y(x)\cos(x)+\frac{x^2}{2}+x^2\cos(x)+\frac{1}{2}x^2\cos(2x)+2xy(x)-2xy(x)\sin(x)+x-x\si}{x^3}$$

✓ **Mathematica** : cpu = 0.107425 (sec), leaf count = 30

$$\left\{\left\{y(x)\to\frac{1}{c_1-\log(x)}-\frac{-\sin(x)+x\cos(x)+1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.39 (sec), leaf count = 44

$$\left\{y(x)=\frac{(\cos(x)\,x-\sin(x)+1)\ln(x)-\cos(x)\,\_C1\,x+\sin(x)\,\_C1+x-\_C1}{x\,(\_C1-\ln(x))}\right\}$$

2.948 ODE No. 948

$$y'(x)=-\frac{216y(x)}{36x^2+4y(x)^8+12y(x)^7+33y(x)^6+60y(x)^5-24xy(x)^4-216y(x)^4-36xy(x)^3-252y(x)^3-72xy(x$$

✓ **Mathematica** : cpu = 0.256433 (sec), leaf count = 39

$$\text{Solve}\left[\frac{36}{y(x)\left(2y(x)^3+3y(x)^2+6y(x)+6\right)-6x}+\log(y(x))=c_1,y(x)\right]$$

✓ **Maple** : cpu = 0.313 (sec), leaf count = 68

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-12\,\_C1\,(\mathrm{e}^{-\_Z})^4-2\,(\mathrm{e}^{-\_Z})^4\_Z-18\,\_C1\,(\mathrm{e}^{-\_Z})^3-3\,(\mathrm{e}^{-\_Z})^3\_Z-36\,\_C1\,(\mathrm{e}^{-\_Z})^2-6\,(\mathrm{e}^{-\_Z})^2\_Z-36\,\_C1\,\mathrm{e}^{-\_Z}-6\,\_Z\,\mathrm{e}^{-\_Z}+36\right.}\right.$$

2.949 ODE No. 949

$$y'(x) = \frac{x^6 - 3x^5 + 3x^4 y(x) + x^4 - 6x^3 y(x) + 2x^3 + 3x^2 y(x)^2 + x^2 y(x) - 3x^2 - 3x y(x)^2 + x y(x) + y(x)^3 + x}{x\left(x^2 + y(x) - x + 1\right)}$$

✓ **Mathematica** : cpu = 0.0215482 (sec), leaf count = 76

$$\left\{\left\{y(x) \to \frac{1}{x\left(\frac{1}{x} - \frac{1}{x\sqrt{c_1 - 2\log(x)}}\right)} - x^2 + x - 1\right\}, \left\{y(x) \to \frac{1}{x\left(\frac{1}{x\sqrt{c_1 - 2\log(x)}} + \frac{1}{x}\right)} - x^2 + x - 1\right\}\right\}$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 81

$$\left\{y(x) = 1\left(\left(-x^2 + x\right)\sqrt{\_C1 - 2\ln(x)} - x^2 + x - 1\right)\left(1 + \sqrt{\_C1 - 2\ln(x)}\right)^{-1}, y(x) = 1\left(\left(-x^2 + x\right)\sqrt{\_C1 -\right.\right.$$

2.950 ODE No. 950

$$y'(x) = \frac{a^3x^6}{64} + \frac{3}{32}a^2bx^5 + \frac{3}{16}a^2x^4y(x) + \frac{a^2x^4}{16} + \frac{3}{16}ab^2x^4 + \frac{3}{4}abx^3y(x) + \frac{1}{4}abx^3 + \frac{3}{4}ax^2y(x)^2 + \frac{1}{2}ax^2y(x) - \frac{ax}{2} + \frac{b^3x^3}{8} +$$

✓ **Mathematica** : cpu = 0.174013 (sec), leaf count = 141

$$\text{Solve}\left[-\frac{1}{3}(27b+58)^{2/3}\text{RootSum}\left[\#1^3(27b+58)^{2/3} - 3\ 2^{2/3}\#1 + (27b+58)^{2/3}\&, \frac{\log\left(\frac{\sqrt[3]{2}\left(\frac{1}{4}\left(3ax^2+6bx+4\right)+3y(x)\right)}{\sqrt[3]{27b+58}}\right.}{2^{2/3} - \#1^2(27b+58)^{2/}\right.\right.$$

✓ **Maple** : cpu = 0.104 (sec), leaf count = 42

$$\left\{y(x) = -\frac{ax^2}{4} - \frac{bx}{2} + RootOf\left(-x + 2\int^{\_Z}\left(2\_a^3 + 2\_a^2 + b + 2\right)^{-1}d\_a + \_C1\right)\right\}$$

2.951 ODE No. 951

$$y'(x) = \frac{a^3x^3}{8} + \frac{3a^2x^4}{16} + \frac{3}{4}a^2x^2y(x) + \frac{a^2x^2}{4} + \frac{3ax^5}{32} + \frac{3}{4}ax^3y(x) + \frac{ax^3}{4} + \frac{3}{2}axy(x)^2 + axy(x) + \frac{x^6}{64} + \frac{3}{16}x^4y(x) + \frac{x^4}{16} + \frac{3}{4}x^2$$

✓ **Mathematica** : cpu = 0.153898 (sec), leaf count = 140

$$\text{Solve}\left[-\frac{1}{3}(27a+58)^{2/3}\text{RootSum}\left[\#1^3(27a+58)^{2/3}-3\,2^{2/3}\#1+(27a+58)^{2/3}\&,\frac{\log\left(\frac{\sqrt[3]{2}\left(\frac{1}{4}(6ax+3x^2+4)+3y(x)\right)}{\sqrt[3]{27a+58}}\right.}{2^{2/3}-\#1^2(27a+58)^{2/}}\right.$$

✓ **Maple** : cpu = 0.084 (sec), leaf count = 41

$$\left\{y(x)=-\frac{x^2}{4}-\frac{ax}{2}+RootOf\left(-x+2\int^{-Z}\left(2\_a^3+2\_a^2+a+2\right)^{-1}d\_a+\_C1\right)\right\}$$

2.952 ODE No. 952

$$y'(x)=\frac{-x^2\sqrt{x^2+y(x)^2}+xy(x)\sqrt{x^2+y(x)^2}+x^5\left(-\sqrt{x^2+y(x)^2}\right)+x^4y(x)\sqrt{x^2+y(x)^2}-x^4\sqrt{x^2+y(x)^2}+}{x}$$

✓ **Mathematica** : cpu = 0.138361 (sec), leaf count = 189

$$\left\{\left\{y(x)\to\frac{x\left(-2e^{\sqrt{2}c_1+\frac{\sqrt{2}x^5}{5}+\frac{x^4}{2\sqrt{2}}+\frac{x^2}{\sqrt{2}}}+e^{2\sqrt{2}c_1+\frac{2\sqrt{2}x^5}{5}+\frac{x^4}{\sqrt{2}}+\sqrt{2}x^2}-1\right)}{2e^{\sqrt{2}c_1+\frac{\sqrt{2}x^5}{5}+\frac{x^4}{2\sqrt{2}}+\frac{x^2}{\sqrt{2}}}+e^{2\sqrt{2}c_1+\frac{2\sqrt{2}x^5}{5}+\frac{x^4}{\sqrt{2}}+\sqrt{2}x^2}-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.67 (sec), leaf count = 62

$$\left\{\ln\left(2\frac{\left(\sqrt{2\left(y(x)\right)^2+2x^2}+y(x)+x\right)x}{y(x)-x}\right)+\frac{\left(4x^5+5x^4+10x^2\right)\sqrt{2}}{20}-\_C1-\ln(x)=0\right\}$$

2.953 ODE No. 953

$$y'(x)=\frac{y(x)\left(x^4\log^2(y(x))+2x^4\log(x)\log(y(x))+x^4\log^2(x)+x^3\log^2(y(x))+2x^3\log(x)\log(y(x))+x^3\log^2(x\right.}{x}$$

✗ **Mathematica** : cpu = 1.48791 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == ((-1 + Log[x] + x*Log[x]^2 + x^3*Log[x]^2 + x^4*Log[x]^2 + Log
```

✓ **Maple** : cpu = 0.454 (sec), leaf count = 145

$$\left\{y(x)=1\left(x^{\frac{x^5}{4x^5+5x^4+10x^2+20\_C1}}\right)^{-4}\left(x^{\frac{x^4}{4x^5+5x^4+10x^2+20\_C1}}\right)^{-5}\left(x^{\frac{x^2}{4x^5+5x^4+10x^2+20\_C1}}\right)^{-10}\left(x^{\frac{\_C1}{4x^5+5x^4+10x^2+20\_C1}}\right)\right.$$

2.954 ODE No. 954

$$y'(x)=\frac{\frac{24}{5}x^{7/2}y(x)-\frac{24x^{13/2}}{25}+\frac{8x^{7/2}}{5}-8x^{3/2}-\frac{8x^9}{125}+\frac{12}{25}x^6y(x)+\frac{4x^6}{25}-\frac{24x^4}{5}-\frac{6}{5}x^3y(x)^2-\frac{4}{5}x^3y(x)+\frac{6x^3}{5}+12xy}{x}$$

✓ **Mathematica** : cpu = 0.0936716 (sec), leaf count = 115

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{\frac{-6x^3-30\sqrt{x}+5}{5x}+\frac{3y(x)}{x}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]\right]=c_1+\frac{1}{9}29^{2/3}\left(\frac{1}{x^3}\right)^{2/3}x^2\,\text{l}$$

✓ **Maple** : cpu = 0.093 (sec), leaf count = 53

$$\left\{y(x)=\frac{1}{45}\left(18\,x^{7/2}+145\,RootOf\left(-81\int^{\_Z}\left(841\,\_a^3-27\,\_a+27\right)^{-1}d\_a+\ln\left(x\right)+3\,\_C1\right)\sqrt{x}-15\sqrt{x}+\right.$$

2.955 ODE No. 955

$$y'(x)=\frac{-24x^{7/2}y(x)+\frac{24x^{13/2}}{5}+14x^{7/2}+40x^{3/2}+\frac{8x^9}{25}-\frac{12}{5}x^6y(x)+\frac{12x^6}{5}+24x^4+6x^3y(x)^2-6x^3y(x)-6x^3-}{x\left(2x^3-5y(x)+10\sqrt{x}-5\right)}$$

✓ **Mathematica** : cpu = 0.0409743 (sec), leaf count = 112

$$\left\{\left\{y(x)\to\frac{1}{5}\left(2x^3+10\sqrt{x}-5\right)-\frac{1}{125x\left(-\frac{1}{x\sqrt{c_1-31250\log(x)}}-\frac{1}{125x}\right)}\right\},\left\{y(x)\to\frac{1}{5}\left(2x^3+10\sqrt{x}-5\right)-\frac{}{125x\left(\frac{}{x}\right.}\right.$$

✓ **Maple** : cpu = 0.116 (sec), leaf count = 101

$$\left\{y(x)=1\left(\left(2\,x^3+10\,\sqrt{x}\right)\sqrt{\_C1-2\,\ln\left(x\right)}-2\,x^3-10\,\sqrt{x}+5\right)\left(5\,\sqrt{\_C1-2\,\ln\left(x\right)}-5\right)^{-1},y(x)=1\left(\left(2\,x^3+\right.\right.\right.$$

2.956 ODE No. 956

$$y'(x)=\frac{y(x)\left(y(x)e^{\frac{2\log^2(x)}{\log(x)+1}}x^{\frac{2}{\log(x)+1}+2}+y(x)e^{\frac{2\log^2(x)}{\log(x)+1}}\log^2(x)x^{\frac{2}{\log(x)+1}+2}+2y(x)e^{\frac{2\log^2(x)}{\log(x)+1}}\log(x)x^{\frac{2}{\log(x)+1}+2}-e^{\frac{2\log^2(}{\log(x)+}\right.}{x(\log(x)+1)}$$

✓ **Mathematica** : cpu = 0.211006 (sec), leaf count = 28

$$\left\{\left\{y(x)\to\frac{1}{\left(c_1e^{\frac{x^4}{4}}+1\right)(\log(x)+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.113 (sec), leaf count = 79

$$\left\{y(x)=\frac{1}{\ln(x)+1}\mathrm{e}^{-\frac{x^4}{4}}\left(x^{-2\frac{\ln(x)}{\ln(x)+1}}(\ln(x)+1)\,\mathrm{e}^{\frac{(-4\ln(x)-4)\ln(\ln(x)+1)-x^4\ln(x)-x^4+8(\ln(x))^2}{4\ln(x)+4}}+\_C1\right)^{-1}\right\}$$

2.957 ODE No. 957

$$y'(x)=\frac{y(x)\left(y(x)e^{\frac{2\log^2(x)}{\log(x)+1}}x^{\frac{2}{\log(x)+1}+3}+y(x)e^{\frac{2\log^2(x)}{\log(x)+1}}\log^2(x)x^{\frac{2}{\log(x)+1}+3}+2y(x)e^{\frac{2\log^2(x)}{\log(x)+1}}\log(x)x^{\frac{2}{\log(x)+1}+3}-e^{\frac{2\log^2(}{\log(x)+}\right.}{x(\log(x)+1)}$$

✓ **Mathematica** : cpu = 0.197583 (sec), leaf count = 28

$$\left\{\left\{y(x)\to\frac{1}{\left(c_1e^{\frac{x^5}{5}}+1\right)(\log(x)+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.057 (sec), leaf count = 79

$$\left\{y(x)=\frac{1}{\ln(x)+1}\mathrm{e}^{-\frac{x^5}{5}}\left(x^{-2\frac{\ln(x)}{\ln(x)+1}}(\ln(x)+1)\,\mathrm{e}^{\frac{(-5\ln(x)-5)\ln(\ln(x)+1)-x^5\ln(x)-x^5+10(\ln(x))^2}{5\ln(x)+5}}+\_C1\right)^{-1}\right\}$$

2.958 ODE No. 958

$$y'(x) = \frac{2xy(x)^3 + y(x)^3 + 2xy(x)^2 + y(x)^2 + 6xy(x)\log^2(2x+1) + 3y(x)\log^2(2x+1) + 6xy(x)^2\log(2x+1) +}{}$$

✓ **Mathematica** : cpu = 0.0631347 (sec), leaf count = 82

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{3y(x)+3\log(2x+1)+1}{\sqrt[3]{29}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right] = c_1 + \frac{1}{9}29^{2/3}x, y(x)\right]$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 40

$$\left\{y(x) = -\ln(2x+1) - \frac{1}{3} + \frac{29\,RootOf\left(-81\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1}d\_a + x + 3\_C1\right)}{9}\right\}$$

2.959 ODE No. 959

$$y'(x) = \frac{\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{x}\right)\left(x^3\sin\left(\frac{y(x)}{2x}\right)\sin\left(\frac{y(x)}{x}\right)\cos\left(\frac{y(x)}{2x}\right) - \frac{1}{2}y(x)\sin\left(\frac{y(x)}{x}\right) + \frac{1}{2}y(x)\sin\left(\frac{y(x)}{2x}\right)\right.}{x}$$

✓ **Mathematica** : cpu = 0.0441831 (sec), leaf count = 20

$$\left\{\left\{y(x) \to x\sin^{-1}\left(e^{c_1+\frac{x^2}{2}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.09 (sec), leaf count = 16

$$\left\{y(x) = \frac{\arccos\left(\mathrm{e}^{x^2}\_C1 + 1\right)x}{2}\right\}$$

2.960 ODE No. 960

$$y'(x) = \frac{\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{x}\right)\left(x^2\sin\left(\frac{y(x)}{2x}\right)\sin\left(\frac{y(x)}{x}\right)\cos\left(\frac{y(x)}{2x}\right) - \frac{1}{2}y(x)\sin\left(\frac{y(x)}{x}\right) + \frac{1}{2}y(x)\sin\left(\frac{y(x)}{2x}\right)\right.}{x}$$

✓ **Mathematica** : cpu = 0.0350675 (sec), leaf count = 14

$$\left\{\left\{y(x) \to x\sin^{-1}\left(e^{c_1+x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 16

$$\left\{y(x) = \frac{\arccos\left(\left(\mathrm{e}^{x}\right)^{2} \_C1 + 1\right) x}{2}\right\}$$

2.961 ODE No. 961

$$y'(x) = \frac{\exp\left(-2x^{6} + 6x^{4}y(x)^{2} + 2x^{4} - 6x^{2}y(x)^{4} - 4x^{2}y(x)^{2} + 2y(x)^{6} + 2y(x)^{4} + 2\right) + x^{2} + 2xy(x) + y(x)^{2}}{-\exp\left(-2x^{6} + 6x^{4}y(x)^{2} + 2x^{4} - 6x^{2}y(x)^{4} - 4x^{2}y(x)^{2} + 2y(x)^{6} + 2y(x)^{4} + 2\right) + x^{2} + 2xy(x) + y(x)^{2}}$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.451 (sec), leaf count = 45

$$\left\{y(x) = \mathrm{e}^{RootOf\left(-\_Z + \int^{\left(\mathrm{e}^{-\_Z}\right)^{2} - 2\,\mathrm{e}^{-\_Z} x} \left(\mathrm{e}^{2\_a^{3} + 2\_a^{2} + 2 + \_a}\right)^{-1} d\_a + \_C1\right)} - x\right\}$$

2.962 ODE No. 962

$$y'(x) = \frac{4(a-1)(a+1)x\left(a^{2}x^{2} - x^{2} -}{a^{8}x^{6} - 4a^{6}x^{6} - 3a^{6}x^{4}y(x)^{2} + 6a^{4}x^{6} + 9a^{4}x^{4}y(x)^{2} + 3a^{4}x^{2}y(x)^{4} - 4a^{2}x^{6} - 9a^{2}x^{4}y(x)^{2} - 6a^{2}x^{2}y(x)^{4} + 4}$$

✓ **Mathematica** : cpu = 5.68876 (sec), leaf count = 1191

$$\left\{\left\{y(x) \to \mathrm{Root}\left[2x^{4}a^{8} - 8x^{4}a^{6} + e^{c_1}x^{4}a^{4} + 11x^{4}a^{4} - 2e^{c_1}x^{4}a^{2} - 6x^{4}a^{2} + 4x^{2}a^{2} + \left(2a^{2} - 2\right)\#1^{5} + e^{c_1}x^{4} + x^{4} +\right.\right.$$

✓ **Maple** : cpu = 1.996 (sec), leaf count = 79

$$\left\{-\frac{y(x)}{(a-1)(a+1)} + 2\frac{1}{(a^{2}-1)^{2}\left(a^{2}x^{2} - x^{2} - (y(x))^{2}\right)^{2}} - 2\frac{1}{(a^{2}-1)^{2}\left(a^{2}x^{2} - x^{2} - (y(x))^{2}\right)} + \_C1 = 0\right\}$$

2.963 ODE No. 963

$$y'(x) = \frac{-\frac{5x^3}{2} + \frac{15}{4}x^3\cos(x) - \frac{3}{2}x^3\cos(2x) + \frac{1}{4}x^3\cos(3x) + \frac{9}{2}x^2y(x) - 6x^2y(x)\cos(x) + \frac{3}{2}x^2y(x)\cos(2x) + \frac{3x^2}{2} +$$

✓ **Mathematica** : cpu = 0.122323 (sec), leaf count = 108

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3 + 3\sqrt[3]{29}\#1 - 29\&, \frac{\log\left(\frac{\frac{3y(x)}{x} + \frac{-3x+3x\cos(x)+1}{x}}{\sqrt[3]{29}\sqrt[3]{\frac{1}{x^3}}} - \#1\right)}{\sqrt[3]{29} - 29\#1^2}\&\right]\right] = c_1 + \frac{1}{9}29^{2/3}\left(\frac{1}{x^3}\right)^{2/3}x^2$$

✓ **Maple** : cpu = 0.26 (sec), leaf count = 39

$$\left\{y(x) = -\cos(x)\,x + x - \frac{1}{3} + \frac{29\,RootOf\left(-81\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1}d\_a + \ln(x) + 3\_C1\right)}{9}\right\}$$

2.964 ODE No. 964

$$y'(x) = -\frac{}{a^8x^6 - 4a^6x^6 - 3a^6x^4y(x)^2 - 2a^6x^4 + 6a^4x^6 + 9a^4x^4y(x)^2 + 6a^4x^4 + 3a^4x^2y(x)^4 + 4a^4x^2y(x)^2 - 4a^2x$$

✓ **Mathematica** : cpu = 5.05745 (sec), leaf count = 264

$$\text{Solve}\left[\frac{y(x)}{(a-1)(a+1)} - \frac{8\text{RootSum}\left[-\#1^3a^6 + 3\#1^3a^4 - 3\#1^3a^2 + \#1^3 + 3\#1^2a^4y(x)^2 + 2\#1^2a^4 - 6\#1^2a^2y(x\right.}{}\right.$$

✓ **Maple** : cpu = 3.314 (sec), leaf count = 80

$$\left\{\frac{y(x)}{(a-1)(a+1)} + 4\frac{1}{a^4 - 2a^2 + 1}\sum_{\_R=RootOf\left(\_Z^3+2\_Z^2+8\right)}\frac{\ln\left(-a^2x^2 + (y(x))^2 + x^2 - \_R\right)}{3\_R^2 + 4\_R} - \_C1 = 0\right\}$$

2.965 ODE No. 965

$$y'(x) = \frac{\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{x}\right)\left(x^4\sin\left(\frac{y(x)}{2x}\right)\sin\left(\frac{y(x)}{x}\right)\cos\left(\frac{y(x)}{2x}\right)+x^3\sin\left(\frac{y(x)}{2x}\right)\sin\left(\frac{y(x)}{x}\right)\cos\left(\frac{y(x)}{2x}\right)-\right.}{}$$

✓ **Mathematica** : cpu = 0.0571286 (sec), leaf count = 29

$$\left\{\left\{y(x)\to x\sin^{-1}\left(xe^{c_1+\frac{x^3}{3}+\frac{x^2}{2}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.126 (sec), leaf count = 25

$$\left\{y(x)=\frac{x}{2}\arccos\left(\mathrm{e}^{\frac{2x^3}{3}}\mathrm{e}^{x^2}\_C1\,x^2+1\right)\right\}$$

2.966 ODE No. 966

$$y'(x) = -\frac{}{216x^3-216x^2y(x)^4-324x^2y(x)^3-648x^2y(x)^2-648x^2y(x)+216x^2-8y(x)^{12}-36y(x)^{11}-126y(x)}$$

✓ **Mathematica** : cpu = 0.444099 (sec), leaf count = 292

$$\text{Solve}\left[72\text{RootSum}\left[-216\#1^3+216\#1^2y(x)^4+324\#1^2y(x)^3+648\#1^2y(x)^2+648\#1^2y(x)-216\#1^2-72\#1y(\right.\right.$$

✓ **Maple** : cpu = 0.829 (sec), leaf count = 50

$$\left\{y(x)=\mathrm{e}^{RootOf\left(-\_Z-6\int^{-1/3\left(\mathrm{e}^{-\_Z}\right)^4-1/2\left(\mathrm{e}^{-\_Z}\right)^3-\left(\mathrm{e}^{-\_Z}\right)^2+x-\mathrm{e}^{-\_Z}}\left(\_a^3+\_a^2+1\right)^{-1}d\_a+\_C1\right)}\right\}$$

2.967 ODE No. 967

$$y'(x) = -\frac{x\left(64x^9-288x^8y(x)-96x^8+432x^7y(x)^2+288x^7y(x)-144x^7-216x^6y(x)^3-216x^6y(x)^2-288x^6y(\right.}{}$$

✓ **Mathematica** : cpu = 0.133491 (sec), leaf count = 151

$$\text{Solve}\left[-\frac{29}{3}\text{RootSum}\left[-29\#1^3+3\sqrt[3]{29}\#1-29\&,\frac{\log\left(\frac{\frac{3xy(x)}{x^2+1}+\frac{-4x^4+2x^3+5x}{2\left(x^2+1\right)^2}}{\sqrt[3]{29}\sqrt[3]{\frac{x^3}{\left(x^2+1\right)^3}}}-\#1\right)}{\sqrt[3]{29}-29\#1^2}\&\right]\right]=c_1+\frac{29^{2/3}\left(\frac{x^3}{\left(x^2+1\right)^3}\right)^{2/3}}{1}$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 91

$$\left\{ y(x) = \frac{58\,RootOf\left(-162\int^{-Z}\left(841\_a^3 - 27\_a + 27\right)^{-1} d\_a + \ln\left(x^2+1\right) + 6\_C1\right) x^2 + 12x^3 - 6x^2 + 58\,R}{18x^2+18} \right.$$

2.968 ODE No. 968

$$y'(x) = \frac{\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{x}\right)\left(x^4\sin\left(\frac{y(x)}{2x}\right)\sin\left(\frac{y(x)}{x}\right)\cos\left(\frac{y(x)}{2x}\right) - \frac{1}{2}xy(x)\sin\left(\frac{y(x)}{x}\right) - \frac{1}{2}y(x)\sin\left(\frac{y(x)}{x}\right)\right.}{}$$

✓ **Mathematica** : cpu = 0.0825083 (sec), leaf count = 30

$$\left\{\left\{y(x) \to x\sin^{-1}\left((x+1)e^{c_1+\frac{x^2}{2}-x-\frac{3}{2}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.158 (sec), leaf count = 29

$$\left\{ y(x) = \frac{x}{2}\arccos\left(\frac{\_C1\,(1+x)^2\,\mathrm{e}^{x^2} + (\mathrm{e}^x)^2}{(\mathrm{e}^x)^2}\right) \right\}$$

2.969 ODE No. 969

$$y'(x) = \frac{\csc\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{2x}\right)\sec\left(\frac{y(x)}{x}\right)\left(-\frac{1}{2}xy(x)\sin\left(\frac{y(x)}{x}\right) - \frac{1}{2}y(x)\sin\left(\frac{y(x)}{x}\right) + x\sin\left(\frac{y(x)}{2x}\right)\sin\left(\frac{y(x)}{x}\right)\cos\left(\frac{y(x)}{2x}\right)\right.}{}$$

✓ **Mathematica** : cpu = 0.0567546 (sec), leaf count = 19

$$\left\{\left\{y(x) \to x\sin^{-1}\left(\frac{e^{c_1}x}{x+1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 26

$$\left\{ y(x) = \frac{x}{2}\arccos\left(\frac{1 + (\_C1+1)\,x^2 + 2x}{(1+x)^2}\right) \right\}$$

2.970 ODE No. 970

$$y'(x) = -\frac{}{216x^3 - 216x^2y(x)^4 - 324x^2y(x)^3 - 648x^2y(x)^2 - 648x^2y(x) - 8y(x)^{12} - 36y(x)^{11} - 126y(x)^{10} - 315}$$

✓ **Mathematica** : cpu = 0.484066 (sec), leaf count = 66

$$\text{Solve}\left[\frac{36\left(2y(x)^4 + 3y(x)^3 + 6y(x)^2 + 6y(x) - 6x - 3\right)}{\left(y(x)\left(2y(x)^3 + 3y(x)^2 + 6y(x) + 6\right) - 6x\right)^2} + \log(y(x)) = c_1, y(x)\right]$$

✓ **Maple** : cpu = 1.079 (sec), leaf count = 181

$$\left\{\frac{1}{6\_C1 - 6\ln\left(y\left(x\right)\right)}\left(-6\sqrt{3\ln\left(y\left(x\right)\right) - 3\_C1 + 9} + \left(2\left(y(x)\right)^4 + 3\left(y(x)\right)^3 + 6\left(y(x)\right)^2 - 6x + 6y(x)\right)\ln\left(y(x\right.\right.\right.$$

2.971 ODE No. 971

$$y'(x) = \frac{(xy(x)+1)^3}{x^5}$$

✓ **Mathematica** : cpu = 0.104104 (sec), leaf count = 157

$$\text{Solve}\left[\frac{1}{3}\log\left(\frac{\frac{3}{x^3} + \frac{3y(x)}{x^2}}{3\sqrt[3]{-\frac{1}{x^6}}} + 1\right) - \frac{1}{6}\log\left(\frac{\left(\frac{3}{x^3} + \frac{3y(x)}{x^2}\right)^2}{9\left(-\frac{1}{x^6}\right)^{2/3}} - \frac{\frac{3}{x^3} + \frac{3y(x)}{x^2}}{3\sqrt[3]{-\frac{1}{x^6}}} + 1\right) + \frac{\tan^{-1}\left(\frac{\frac{2\left(\frac{3}{x^3} + \frac{3y(x)}{x^2}\right)}{3\sqrt[3]{-\frac{1}{x^6}}} - 1}{\sqrt{3}}\right)}{\sqrt{3}} = c_1 - \left(\right.\right.$$

✓ **Maple** : cpu = 0.35 (sec), leaf count = 86

$$\left\{y(x) = \frac{\sqrt{3}}{6x}\left(3\tan\left(\mathit{RootOf}\left(-18x^3\left(-x^{-6}\right)^{2/3} - 6\_Z\sqrt{3} - \ln\left(\frac{\left(\sqrt{3} + \tan\left(\_Z\right)\right)^6}{\left(\left(\tan\left(\_Z\right)\right)^2 + 1\right)^3}\right) + 18\_C1\right)\right)x^3\sqrt[3]{-\right.\right.$$

2.972 ODE No. 972

$$y'(x) = \frac{x\left(-2x^4 + 2x^2 y(x) - x^2 + 1\right)}{y(x) - x^2}$$

✓ **Mathematica** : cpu = 0.0259089 (sec), leaf count = 32

$$\left\{\left\{y(x) \to \frac{1}{2}\left(W\left(-e^{c_1 + x^4 - 2x^2 - 1}\right) + 1\right) + x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.096 (sec), leaf count = 27

$$\left\{y(x) = x^2 + \frac{1}{2}\mathit{lambertW}\left(-2\,\frac{\mathrm{e}^{x^4}\_C1\,\mathrm{e}^{-1}}{\left(\mathrm{e}^{x^2}\right)^2}\right) + \frac{1}{2}\right\}$$

2.973 ODE No. 973

$$y'(x) = e^{-2bx} y(x)\left(e^{bx} y(x) + e^{2bx} + y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.169456 (sec), leaf count = 146

$$\text{Solve}\left[-\frac{1}{3}(9b-7)^{2/3}\text{RootSum}\left[\#1^3(9b-7)^{2/3} - 9\#1 b + 6\#1 + (9b-7)^{2/3}\&, \frac{\log\left(\frac{3e^{-2bx}y(x)+e^{-bx}}{\sqrt[3]{(9b-7)e^{-3bx}}} - \#1\right)}{\#1^2\left(-(9b-7)^{2/3}\right) + 3b - 2}\&\right] =$$

✓ **Maple** : cpu = 0.451 (sec), leaf count = 134

$$\left\{y(x) = -\frac{1}{2}\tan\left(\mathit{RootOf}\left(-\ln\left(\left(4\left(\tan\left(\_Z\right)\right)^2 b - 3\left(\tan\left(\_Z\right)\right)^2 + 4b - 3\right)\left(\tan\left(\_Z\right)\sqrt{-\left(\mathrm{e}^{bx}\right)^2(4b-3)} + \mathrm{e}^{b}\right.\right.\right.\right.$$

2.974 ODE No. 974

$$y'(x) = -x^6 + 3x^4 y(x) - 3x^2 y(x)^2 + y(x)^3 + 2x$$

✓ **Mathematica** : cpu = 0.0107626 (sec), leaf count = 39

$$\left\{\left\{y(x) \to x^2 - \frac{1}{\sqrt{c_1 - 2x}}\right\}, \left\{y(x) \to \frac{1}{\sqrt{c_1 - 2x}} + x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 57

$$\left\{y(x) = 1\left(x^2\sqrt{2\_C1 - 2x} - 1\right)\frac{1}{\sqrt{2\_C1 - 2x}}, y(x) = 1\left(x^2\sqrt{2\_C1 - 2x} + 1\right)\frac{1}{\sqrt{2\_C1 - 2x}}\right\}$$

2.975 ODE No. 975

$$y'(x) = \frac{x^6}{27} + \frac{1}{3}x^4 y(x) + x^2 y(x)^2 + y(x)^3 - \frac{2x}{3}$$

✓ **Mathematica** : cpu = 0.0115763 (sec), leaf count = 47

$$\left\{\left\{y(x) \to -\frac{1}{\sqrt{c_1 - 2x}} - \frac{x^2}{3}\right\}, \left\{y(x) \to \frac{1}{\sqrt{c_1 - 2x}} - \frac{x^2}{3}\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 59

$$\left\{y(x) = -\frac{1}{3}\left(x^2\sqrt{-54\_C1 - 2x} - 3\right)\frac{1}{\sqrt{-54\_C1 - 2x}}, y(x) = -\frac{1}{3}\left(x^2\sqrt{-54\_C1 - 2x} + 3\right)\frac{1}{\sqrt{-54\_C1 - 2}}\right.$$

2.976 ODE No. 976

$$y'(x) = \frac{y(x)\left(x^7 y(x)^2 + x^4 y(x) + x - 3\right)}{x}$$

✓ **Mathematica** : cpu = 0.0799411 (sec), leaf count = 101

$$\text{Solve}\left[-\frac{7}{3}\text{RootSum}\left[-7\#1^3 + 6\sqrt[3]{-7}\#1 - 7\&, \frac{\log\left(\frac{3x^6 y(x) + x^3}{\sqrt[3]{7}\sqrt[3]{-x^9}} - \#1\right)}{2\sqrt[3]{-7} - 7\#1^2}\&\right] = c_1 + \frac{7^{2/3}\left(-x^9\right)^{2/3}}{9x^5}, y(x)\right]$$

✓ **Maple** : cpu = 0.872 (sec), leaf count = 57

$$\left\{y(x) = \frac{1}{2x^3}\left(\sqrt{3}\tan\left(RootOf\left(-\sqrt{3}\ln\left(\frac{9\left(\tan\left(\_Z\right)\right)^2 + 9}{7\left(\sqrt{3} - 3\tan\left(\_Z\right)\right)^2}\right) + 3\sqrt{3}\_C1 - 2\sqrt{3}x - 2\_Z\right)\right) - 1\right)\right\}$$

2.977 ODE No. 977

$$y'(x) = e^{2x^2} x y(x)\left(e^{-x^2} y(x) + e^{-2x^2} + y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.196119 (sec), leaf count = 139

$$\text{Solve}\left[-\frac{25}{3}\text{RootSum}\left[-25\#1^3 + 24\sqrt[3]{-1}5^{2/3}\#1 - 25\&, \frac{\log\left(\frac{3e^{2x^2} x y(x) + e^{x^2} x}{5^{2/3}\sqrt[3]{-e^{3x^2}x^3}} - \#1\right)}{8\sqrt[3]{-1}5^{2/3} - 25\#1^2}\&\right] = c_1 - \frac{5\sqrt[3]{5}e^{x^2}x^3}{18\sqrt[3]{-e^{3x^2}x^3}}, y(\right.$$

✓ **Maple** : cpu = 0.217 (sec), leaf count = 122

$$\left\{y(x)=\frac{1}{2\,\mathrm{e}^{x^2}}\left(\sqrt{11}\tan\left(\mathit{RootOf}\left(-4\sqrt{11}x^2+8\ln\left(-\frac{36\sqrt{11}}{11}+36\tan\left(\_Z\right)\right)\sqrt{11}-4\ln\left(\frac{2592\sqrt{11}\left(\mathrm{e}^{x^2}\right)^2}{25}\right.\right.\right.\right.\right.$$

2.978 ODE No. 978

$$y'(x)=\frac{y(x)\left(x^2+xy(x)+y(x)^2+x\right)}{x^2}$$

✓ **Mathematica** : cpu = 0.0482751 (sec), leaf count = 60

$$\text{Solve}\left[-\frac{1}{2}\log\left(\frac{y(x)^2}{x^2}+\frac{y(x)}{x}+1\right)+\log\left(\frac{y(x)}{x}\right)-\frac{\tan^{-1}\left(\frac{\frac{2y(x)}{x}+1}{\sqrt{3}}\right)}{\sqrt{3}}=c_1+x,y(x)\right]$$

✓ **Maple** : cpu = 0.191 (sec), leaf count = 71

$$\left\{y(x)=-\frac{x}{2}+\frac{\sqrt{3}x}{2}\tan\left(\mathit{RootOf}\left(-\sqrt{3}\ln\left(3\right)-\sqrt{3}\ln\left(\frac{4}{3+3\left(\tan\left(\_Z\right)\right)^2}\right)-2\sqrt{3}\ln\left(-1/6\sqrt{3}+1/2\tan\left(\_Z\right)\right.\right.\right.\right.$$

2.979 ODE No. 979

$$y'(x)=\frac{-x^3+3x^2y(x)-3xy(x)^2+y(x)^3+x}{x}$$

✓ **Mathematica** : cpu = 0.0121091 (sec), leaf count = 37

$$\left\{\left\{y(x)\to x-\frac{1}{\sqrt{c_1-2\log(x)}}\right\},\left\{y(x)\to\frac{1}{\sqrt{c_1-2\log(x)}}+x\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 57

$$\left\{y(x)=1\left(x\sqrt{2\_C1-2\ln\left(x\right)}-1\right)\frac{1}{\sqrt{2\_C1-2\ln\left(x\right)}},y(x)=1\left(x\sqrt{2\_C1-2\ln\left(x\right)}+1\right)\frac{1}{\sqrt{2\_C1-2\ln\left(\right.}}\right.$$

2.980 ODE No. 980

$$y'(x) = \frac{x^3 y(x)^3 + 6x^2 y(x)^2 + 12xy(x) + 2x + 8}{x^3}$$

✓ **Mathematica** : cpu = 0.012631 (sec), leaf count = 43

$$\left\{\left\{y(x) \to -\frac{1}{\sqrt{c_1 - 2x}} - \frac{2}{x}\right\}, \left\{y(x) \to \frac{1}{\sqrt{c_1 - 2x}} - \frac{2}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 35

$$\left\{y(x) = -\frac{1}{\sqrt{\_C1 - 2\,x}} - 2\,x^{-1}, y(x) = \frac{1}{\sqrt{\_C1 - 2\,x}} - 2\,x^{-1}\right\}$$

2.981 ODE No. 981

$$y'(x) = \frac{a^3 x^3 y(x)^3 + 3a^2 x^2 y(x)^2 + a^2 x + 3axy(x) + 1}{a^3 x^3}$$

✓ **Mathematica** : cpu = 0.0167571 (sec), leaf count = 49

$$\left\{\left\{y(x) \to -\frac{1}{ax} - \frac{1}{\sqrt{c_1 - 2x}}\right\}, \left\{y(x) \to \frac{1}{\sqrt{c_1 - 2x}} - \frac{1}{ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 41

$$\left\{y(x) = -\frac{1}{\sqrt{\_C1 - 2\,x}} - \frac{1}{ax}, y(x) = \frac{1}{\sqrt{\_C1 - 2\,x}} - \frac{1}{ax}\right\}$$

2.982 ODE No. 982

$$y'(x) = \frac{1}{2} e^{-\frac{x^2}{2}} y(x) \left(2e^{\frac{x^2}{4}} y(x) + 2e^{\frac{x^2}{2}} + e^{\frac{x^2}{2}} x + 2y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.10736 (sec), leaf count = 132

$$\text{Solve}\left[-\frac{7}{3}\text{RootSum}\left[-7\#1^3 + 6\sqrt[3]{-7}\#1 - 7\&, \frac{\log\left(\frac{3e^{-\frac{x^2}{2}} y(x) + e^{-\frac{x^2}{4}}}{\sqrt[3]{7}\sqrt[3]{-e^{-\frac{3x^2}{4}}}} - \#1\right)}{2\sqrt[3]{-7} - 7\#1^2}\&\right]\right] = c_1 + \frac{1}{9} 7^{2/3} e^{\frac{x^2}{2}} \left(-e^{-\frac{3x^2}{4}}\right)^{2/3} x$$

✓ **Maple** : cpu = 0.548 (sec), leaf count = 145

$$\left\{-\frac{2}{3}\ln\left(-6 + \left(18\,y(x)\,\mathrm{e}^{-1/2\,x^2} + 6\,\mathrm{e}^{-1/4\,x^2}\right)\mathrm{e}^{\frac{x^2}{4}}\right) + \frac{1}{3}\ln\left(36 + \frac{324}{7}\left(y(x)\,\mathrm{e}^{-\frac{x^2}{2}} + \frac{1}{3}\mathrm{e}^{-\frac{x^2}{4}}\right)^2\left(\mathrm{e}^{\frac{x^2}{4}}\right)^2 + \frac{1}{7}\left(108\,y(\right.\right.$$

2.983 ODE No. 983

$$y'(x) = \frac{-x^3 + 3x^2 y(x) + x^2 - 3xy(x)^2 + y(x)^3}{(x-1)(x+1)}$$

✓ **Mathematica** : cpu = 0.255988 (sec), leaf count = 238

$$\text{Solve}\left[\frac{1}{3}\log\left(\frac{\frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1}}{3\sqrt[3]{\frac{1}{(x-1)^3(x+1)^3}}} + 1\right) - \frac{1}{6}\log\left(\frac{\left(\frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1}\right)^2}{9\left(\frac{1}{(x-1)^3(x+1)^3}\right)^{2/3}} - \frac{\frac{3y(x)}{x^2-1} - \frac{3x}{x^2-1}}{3\sqrt[3]{\frac{1}{(x-1)^3(x+1)^3}}} + 1\right) + \frac{\tan^{-1}\left(\frac{\frac{2\left(\frac{3y(x)}{x^2-1} - \frac{3}{x^2 \cdots}\right.}{3\sqrt[3]{\frac{1}{(x-1)^3(x \cdots}}}}{\sqrt{3}}\right.}{\sqrt{3}}\right.$$

✓ **Maple** : cpu = 0.409 (sec), leaf count = 233

$$\left\{ y(x) = \frac{\sqrt{3}}{2}\left(\frac{x^2-1}{3}\left(3\tan\left(\mathit{RootOf}\left(-18\ln(1+x)\left(\frac{1}{(1+x)^3(x-1)^3}\right)^{2/3} x^4 + 18\ln(x-1)\left(\frac{1}{(1+x)^3(x - \cdots}\right.\right.\right.\right.\right.\right.$$

2.984 ODE No. 984

$$y'(x) = \frac{e^{-2x}(x-1)y(x)\left(x^2 y(x)^2 + e^x x y(x) + e^{2x}\right)}{x}$$

✓ **Mathematica** : cpu = 3.02665 (sec), leaf count = 428

$$\text{Solve}\left[\frac{\sqrt[3]{2}\left(\frac{3e^{-2x}x(x-1)y(x)+e^{-x}(x-1)}{\sqrt[3]{2}\sqrt[3]{e^{-3x}(x-1)^3}} + 2^{2/3}\right)\left(2^{2/3} - \frac{2^{2/3}\left(3e^{-2x}x(x-1)y(x)+e^{-x}(x-1)\right)}{\sqrt[3]{e^{-3x}(x-1)^3}}\right)\left(\left(1 - \frac{3e^{-2x}x(x-1)y(x)+e^{-x}(x-1\cdots}{\sqrt[3]{e^{-3x}(x-1)^3}}\right.\right.}{9\left(-\frac{e^{3x}(3e^{-2x}x(x-1)y(x)+e\cdots}{(x-1)^3}\right.}\right.$$

✓ **Maple** : cpu = 0.322 (sec), leaf count = 40

$$\left\{ y(x) = \frac{1}{9x} e^{\mathit{RootOf}\left(-e^{-\_Z}\ln\left(\frac{x\left(e^{-\_Z}+9\right)}{2}\right)+3\_C1\, e^{-\_Z}+\_Z\, e^{-\_Z}+e^{-\_Z}x+9\right)+x} \right\}$$

2.985 ODE No. 985

$$y'(x) = \frac{(xy(x)+1)\left(x^2y(x)^2+x^2y(x)+x^2+2xy(x)+x+1\right)}{x^5}$$

✓ **Mathematica** : cpu = 0.215418 (sec), leaf count = 103

$$\text{Solve}\left[-\frac{17}{3}\text{RootSum}\left[-17\#1^3+3\sqrt[3]{-34}\#1-17\&,\frac{\log\left(\frac{\frac{x+3}{x^3}+\frac{3y(x)}{x^2}}{\sqrt[3]{34}\sqrt[3]{-\frac{1}{x^6}}}-\#1\right)}{\sqrt[3]{-34}-17\#1^2}\&\right]\right] = c_1-\frac{1}{9}34^{2/3}\left(-\frac{1}{x^6}\right)^{2/3}x^3, y(x$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 43

$$\left\{y(x)=\frac{17\,RootOf\left(162\int^{-Z}\left(289\_a^3+54\_a-54\right)^{-1}d\_ax+3\_C1\,x+2\right)x-3x-9}{9x}\right\}$$

2.986 ODE No. 986

$$y'(x) = \frac{-x^3\log^3(x)+3x^2y(x)\log^2(x)+x^2+y(x)^3+xy(x)-3xy(x)^2\log(x)}{x^2}$$

✓ **Mathematica** : cpu = 0.0152769 (sec), leaf count = 44

$$\left\{\left\{y(x)\to x\log(x)-\frac{x}{\sqrt{c_1-2x}}\right\},\left\{y(x)\to\frac{x}{\sqrt{c_1-2x}}+x\log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 36

$$\left\{y(x)=-x\frac{1}{\sqrt{\_C1-2x}}+x\ln(x),y(x)=x\frac{1}{\sqrt{\_C1-2x}}+x\ln(x)\right\}$$

2.987 ODE No. 987

$$y'(x) = \frac{y(x)}{x}-F(x)\left(y(x)^2-ax^2\right)$$

✓ **Mathematica** : cpu = 0.0920166 (sec), leaf count = 40

$$\left\{\left\{y(x)\to\sqrt{a}x\tanh\left(\sqrt{a}\int_1^x K[1]F(K[1])\,dK[1]+\sqrt{a}c_1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 22

$$\left\{y(x)=\tanh\left(\sqrt{a}\left(\_C1+\int F(x)\,x\,dx\right)\right)x\sqrt{a}\right\}$$

2.988 ODE No. 988

$$y'(x) = \frac{y(x)}{x} - F(x)\left(-x^2 - 2xy(x) + y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.317858 (sec), leaf count = 104

$$\left\{\left\{y(x) \to -\frac{x\left(-\exp\left(2\sqrt{2}\left(\int_1^x K[1](-F(K[1]))\,dK[1] + c_1\right)\right) + \sqrt{2}\exp\left(2\sqrt{2}\left(\int_1^x K[1](-F(K[1]))\,dK[1] + c_1\right)\right) -\right.}{\exp\left(2\sqrt{2}\left(\int_1^x K[1](-F(K[1]))\,dK[1] + c_1\right)\right) + 1}\right.$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 29

$$\left\{y(x) = \frac{x\left(\sqrt{2} + 2\tanh\left(\left(\_C1 + \int F(x)\,x\,\mathrm{d}x\right)\sqrt{2}\right)\right)\sqrt{2}}{2}\right\}$$

2.989 ODE No. 989

$$y'(x) = \frac{y(x)}{x} - F(x)\left(-ay(x)^2 - bx^2\right)$$

✓ **Mathematica** : cpu = 0.0994485 (sec), leaf count = 55

$$\left\{\left\{y(x) \to \frac{\sqrt{b}x\tan\left(\sqrt{a}\sqrt{b}\int_1^x K[1]F(K[1])\,dK[1] + \sqrt{a}\sqrt{b}c_1\right)}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 29

$$\left\{y(x) = \frac{x}{a}\tan\left(\sqrt{ab}\left(\_C1 + \int F(x)\,x\,\mathrm{d}x\right)\right)\sqrt{ab}\right\}$$

2.990 ODE No. 990

$$y'(x) = 2x - F(x)\left(-x^4 + 2x^2y(x) - y(x)^2 + 1\right)$$

✓ **Mathematica** : cpu = 0.44447 (sec), leaf count = 49

$$\left\{\left\{y(x) \to \frac{e^{\int_1^x 2F(K[5])\,dK[5]}}{c_1 - \frac{1}{2}e^{\text{Integrate}[2F(K[5]),\{K[5],1,x\},\text{Assumptions}\to\text{True}]}} + x^2 + 1\right\}\right\}$$

✓ **Maple** : cpu = 0.743 (sec), leaf count = 44

$$\left\{y(x) = \frac{-x^2\left(\mathrm{e}^{\int F(x)\,\mathrm{d}x}\right)^2 + \_C1\,x^2 + \left(\mathrm{e}^{\int F(x)\,\mathrm{d}x}\right)^2 + \_C1}{-\left(\mathrm{e}^{\int F(x)\,\mathrm{d}x}\right)^2 + \_C1}\right\}$$

2.991 ODE No. 991

$$y'(x) = \frac{y(x)}{x} - F(x)\left(x^2 + 2xy(x) - y(x)^2\right)$$

✓ **Mathematica** : cpu = 0.240825 (sec), leaf count = 101

$$\left\{\left\{y(x) \to -\frac{x\left(-\exp\left(2\sqrt{2}\left(\int_1^x K[1]F(K[1])\,dK[1] + c_1\right)\right) + \sqrt{2}\exp\left(2\sqrt{2}\left(\int_1^x K[1]F(K[1])\,dK[1] + c_1\right)\right) - 1 - \sqrt{}\right.\right.}{\exp\left(2\sqrt{2}\left(\int_1^x K[1]F(K[1])\,dK[1] + c_1\right)\right) + 1}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 29

$$\left\{y(x) = \frac{x\left(\sqrt{2} - 2\tanh\left(\left(\_C1 + \int F(x)\,x\,\mathrm{d}x\right)\sqrt{2}\right)\right)\sqrt{2}}{2}\right\}$$

2.992 ODE No. 992

$$y'(x) = \frac{y(x)}{x} - F(x)\left(-x^3 - 7xy(x)^2\right)$$

✓ **Mathematica** : cpu = 0.10232 (sec), leaf count = 42

$$\left\{\left\{y(x) \to \frac{x\tan\left(\sqrt{7}\int_1^x K[1]^2F(K[1])\,dK[1] + \sqrt{7}c_1\right)}{\sqrt{7}}\right\}\right\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 25

$$\left\{y(x) = \frac{\tan\left(\left(\int F(x)\,x^2\,\mathrm{d}x + \_C1\right)\sqrt{7}\right)x\sqrt{7}}{7}\right\}$$

2.993 ODE No. 993

$$y'(x) = \frac{y(x)}{x\log(x)} - F(x)\left(-y(x)^2 - 2y(x)\log(x) - \log^2(x)\right)$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

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$Aborted
```

✓ **Maple** : cpu = 0.033 (sec), leaf count = 35

$$\left\{y(x) = -\frac{\ln(x)\left(\int -2\ln(x)\,F(x)\,\mathrm{d}x - \_C1 - 2\right)}{\int -2\ln(x)\,F(x)\,\mathrm{d}x - \_C1}\right\}$$

2.994 ODE No. 994

$$y'(x) = \frac{y(x)}{x\log(x)} - x^3\left(-y(x)^2 - 2y(x)\log(x) - \log^2(x)\right)$$

✓ **Mathematica** : cpu = 0.120508 (sec), leaf count = 198

$$\left\{\left\{y(x) \to -\frac{c_1 e^{\frac{1}{16}x^4(4\log(x)-1)}\left(\frac{x^3}{4} + \frac{1}{4}x^3(4\log(x)-1)\right) + \frac{1}{16}x^4 e^{\frac{1}{16}x^4(4\log(x)-1)}(4\log(x)-1)\left(\frac{x^3}{4} + \frac{1}{4}x^3(4\log(x)\right.\right.}{x^3\left(c_1 e^{\frac{1}{16}x^4(4\log(x)-1)} + \frac{1}{16}x^4 e^{\frac{1}{16}x^4(4\log(x)-1)}(4\lo\right.}$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 43

$$\left\{y(x) = -\frac{\ln(x)\left(4x^4\ln(x) - x^4 + 8\_C1 + 16\right)}{4x^4\ln(x) - x^4 + 8\_C1}\right\}$$

2.995 ODE No. 995

$$y'(x) = (y(x) - e^x)^2 + e^x$$

✓ **Mathematica** : cpu = 0.0170794 (sec), leaf count = 17

$$\left\{\left\{y(x) \to \frac{1}{c_1 - x} + e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.146 (sec), leaf count = 14

$$\left\{y(x) = \mathrm{e}^x + (\_C1 - x)^{-1}\right\}$$

2.996 ODE No. 996

$$y'(x) = \frac{(y(x) - \mathrm{Si}(x))^2 + \sin(x)}{x}$$

✗ **Mathematica** : cpu = 62.2756 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] == (Sin[x] + (-SinIntegral[x] + y[x])^2)/x, y[x], x]
```

✓ **Maple** : cpu = 0.089 (sec), leaf count = 15

$$\left\{y(x) = Si(x) + (\_C1 - \ln(x))^{-1}\right\}$$

2.997 ODE No. 997

$$y'(x) = (y(x) + \cos(x))^2 + \sin(x)$$

✓ **Mathematica** : cpu = 0.0294358 (sec), leaf count = 18

$$\left\{\left\{y(x) \to \frac{1}{c_1 - x} - \cos(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 16

$$\left\{y(x) = -\cos(x) + (\_C1 - x)^{-1}\right\}$$

2.998 ODE No. 998

$$y'(x) = \frac{(-\mathrm{Ci}(x) + y(x) - \log(x))^2 + \cos(x)}{x}$$

✓ **Mathematica** : cpu = 0.430146 (sec), leaf count = 27

$$\left\{\left\{y(x) \to \frac{x^2}{c_1 - \frac{x^2}{2}} + \mathrm{Ci}(x) + \log(x) + 1\right\}\right\}$$

✓ **Maple** : cpu = 0.498 (sec), leaf count = 27

$$\left\{y(x) = \ln(x) + Ci(x) + \frac{-\_C1\, x^2 + 1}{\_C1\, x^2 + 1}\right\}$$

2.999 ODE No. 999

$$y'(x) = \frac{(y(x) - x + \log(x+1))^2 + x}{x+1}$$

✓ **Mathematica** : cpu = 0.0238879 (sec), leaf count = 24

$$\left\{\left\{y(x) \to \frac{1}{c_1 - \log(x+1)} + x - \log(x+1)\right\}\right\}$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 36

$$\left\{y(x) = \frac{-(\ln(1+x))^2 + (x - \_C1)\ln(1+x) + \_C1\, x - 1}{\ln(1+x) + \_C1}\right\}$$

2.1000 ODE No. 1000

$$y'(x) = \frac{x^3 + 2x^2 y(x) - x y(x) - y(x)^2 + x y(x) \log(x)}{x^2 (x + \log(x))}$$

✗ **Mathematica** : cpu = 300.049 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.187 (sec), leaf count = 19

$$\left\{ y(x) = \frac{x(\_C1\ x - 1)}{\_C1\ \ln(x) + 1} \right\}$$

2.1001 ODE No. 1001

$$y''(x) = 0$$

✓ **Mathematica** : cpu = 0.00404361 (sec), leaf count = 12

$$\{\{y(x) \to c_2 x + c_1\}\}$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 9

$$\{y(x) = \_C1\ x + \_C2\}$$

2.1002 ODE No. 1002

$$y''(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.00569952 (sec), leaf count = 16

$$\{\{y(x) \to c_2 \sin(x) + c_1 \cos(x)\}\}$$

✓ **Maple** : cpu = 0.005 (sec), leaf count = 13

$$\{y(x) = \_C1\ \sin(x) + \_C2\ \cos(x)\}$$

2.1003 ODE No. 1003

$$-\sin(nx)+y''(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.112628 (sec), leaf count = 45

$$\left\{\left\{y(x)\to c_2\sin(x)+c_1\cos(x)+\frac{\cos^2(x)(-\sin(nx))-\sin^2(x)\sin(nx)}{n^2-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.078 (sec), leaf count = 26

$$\left\{y(x)=\sin\left(x\right)\_C2+\cos\left(x\right)\_C1-\frac{\sin\left(nx\right)}{n^2-1}\right\}$$

2.1004 ODE No. 1004

$$-a\cos(bx)+y''(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0974877 (sec), leaf count = 47

$$\left\{\left\{y(x)\to\frac{-a\cos^2(x)\cos(bx)-a\sin^2(x)\cos(bx)}{b^2-1}+c_2\sin(x)+c_1\cos(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 27

$$\left\{y(x)=\sin\left(x\right)\_C2+\cos\left(x\right)\_C1-\frac{a\cos\left(bx\right)}{b^2-1}\right\}$$

2.1005 ODE No. 1005

$$-\sin(ax)\sin(bx)+y''(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.522242 (sec), leaf count = 1163

$$\left\{\left\{y(x)\to c_1\cos(x)+c_2\sin(x)+\frac{-\cos(x)\cos((a-b-1)x)a^3+\cos(x)\cos((a-b+1)x)a^3+\cos(x)\cos((a+b\right.\right.$$

✓ **Maple** : cpu = 0.123 (sec), leaf count = 82

$$\left\{y(x)=\sin\left(x\right)\_C2+\cos\left(x\right)\_C1+\frac{-(a+b+1)\left(a+b-1\right)\cos\left(x(a-b)\right)+\cos\left(\left(a+b\right)x\right)\left(a-b+1\right)\left(a-b\right.}{2a^4+\left(-4b^2-4\right)a^2+2b^4-4b^2+2}\right\}$$

2.1006 ODE No. 1006

$$y''(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.00516035 (sec), leaf count = 20

$$\{\{y(x) \to c_1 e^x + c_2 e^{-x}\}\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 15

$$\{y(x) = \_C1\, \mathrm{e}^{x} + \_C2\, \mathrm{e}^{-x}\}$$

2.1007 ODE No. 1007

$$-4e^{x^2}x^2 + y''(x) - 2y(x) = 0$$

✓ **Mathematica** : cpu = 0.0685949 (sec), leaf count = 135

$$\left\{\left\{y(x) \to c_1 e^{\sqrt{2}x} + c_2 e^{-\sqrt{2}x} + \frac{e^{-\sqrt{2}x}\left(-2e^{x\left(x+\sqrt{2}\right)}x + 2e^{\left(x-\sqrt{2}\right)x+2\sqrt{2}x}x + \sqrt{2}e^{x\left(x+\sqrt{2}\right)} + \sqrt{2}e^{\left(x-\sqrt{2}\right)x+2\sqrt{2}x}\right)}{2\sqrt{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 26

$$\left\{y(x) = \mathrm{e}^{\sqrt{2}x}\_C2 + \mathrm{e}^{-\sqrt{2}x}\_C1 + \mathrm{e}^{x^2}\right\}$$

2.1008 ODE No. 1008

$$a^2 y(x) - \cot(ax) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0416175 (sec), leaf count = 48

$$\left\{\left\{y(x) \to -\frac{\sin(ax)\left(\log\left(\cos\left(\frac{ax}{2}\right)\right) - \log\left(\sin\left(\frac{ax}{2}\right)\right)\right)}{a^2} + c_2 \sin(ax) + c_1 \cos(ax)\right\}\right\}$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 41

$$\left\{y(x) = \sin\left(ax\right)\_C2 + \cos\left(ax\right)\_C1 + \frac{\sin\left(ax\right)}{a^2}\ln\left(\frac{1-\cos\left(ax\right)}{\sin\left(ax\right)}\right)\right\}$$

2.1009 ODE No. 1009

$$ly(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.00482309 (sec), leaf count = 28

$$\left\{\left\{y(x) \to c_2 \sin\left(\sqrt{l}x\right) + c_1 \cos\left(\sqrt{l}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 21

$$\left\{y(x) = \_C1 \ \sin\left(\sqrt{l}x\right) + \_C2 \ \cos\left(\sqrt{l}x\right)\right\}$$

2.1010 ODE No. 1010

$$y(x)(ax + b) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.00706392 (sec), leaf count = 46

$$\left\{\left\{y(x) \to c_1 \text{Ai}\left(\frac{-b - ax}{(-a)^{2/3}}\right) + c_2 \text{Bi}\left(\frac{-b - ax}{(-a)^{2/3}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 31

$$\left\{y(x) = \_C1 \ \text{Ai}\left(-(ax + b)a^{-\frac{2}{3}}\right) + \_C2 \ \text{Bi}\left(-(ax + b)a^{-\frac{2}{3}}\right)\right\}$$

2.1011 ODE No. 1011

$$y''(x) - \left(x^2 + 1\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.00791252 (sec), leaf count = 33

$$\left\{\left\{y(x) \to c_1 D_{-1}\left(\sqrt{2}x\right) + c_2 D_0\left(i\sqrt{2}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 17

$$\left\{y(x) = \mathrm{e}^{\frac{x^2}{2}} \left(Erf(x) \_C2 + \_C1\right)\right\}$$

2.1012 ODE No. 1012

$$y''(x) - \left(a + x^2\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.0086488 (sec), leaf count = 47

$$\left\{\left\{y(x) \to c_1 D_{\frac{1}{2}(-a-1)}\left(\sqrt{2}x\right) + c_2 D_{\frac{a-1}{2}}\left(i\sqrt{2}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 29

$$\left\{y(x) = 1\left(\_C2\, W_{-\frac{a}{4},\frac{1}{4}}\left(x^2\right) + \_C1\, M_{-\frac{a}{4},\frac{1}{4}}\left(x^2\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1013 ODE No. 1013

$$y''(x) - \left(a^2x^2 + a\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.0205547 (sec), leaf count = 43

$$\left\{\left\{y(x) \to c_1 D_{-1}\left(\sqrt{2}\sqrt{a}x\right) + c_2 D_0\left(i\sqrt{2}\sqrt{a}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 22

$$\left\{y(x) = \mathrm{e}^{\frac{ax^2}{2}}\left(Erf\left(\sqrt{a}x\right)\_C2 + \_C1\right)\right\}$$

2.1014 ODE No. 1014

$$y''(x) - cx^a y(x) = 0$$

✓ **Mathematica** : cpu = 0.0393652 (sec), leaf count = 170

$$\left\{\left\{y(x) \to (a+2)^{-\frac{1}{a+2}} c_1 c^{\frac{1}{2(a+2)}} x^{\frac{a}{2}+1}{}^{\frac{1}{a+2}} \Gamma\left(1 - \frac{1}{a+2}\right) I_{-\frac{1}{a+2}}\left(\frac{2\sqrt{c}x^{\frac{a+2}{2}}}{a+2}\right) + (-1)^{\frac{1}{a+2}}(a+2)^{-\frac{1}{a+2}} c_2 c^{\frac{1}{2(a+2)}} x^{1-\frac{a}{2}+1}{}^{\frac{1}{a+2}} \Gamma\right.$$

✓ **Maple** : cpu = 0.086 (sec), leaf count = 63

$$\left\{y(x) = \sqrt{x}\left(Y_{(a+2)^{-1}}\left(2\,\frac{\sqrt{-c}x^{a/2+1}}{a+2}\right)\_C2 + J_{(a+2)^{-1}}\left(2\,\frac{\sqrt{-c}x^{a/2+1}}{a+2}\right)\_C1\right)\right\}$$

2.1015 ODE No. 1015

$$y''(x) - y(x)\left(a^2x^{2n} - 1\right) = 0$$

✗ **Mathematica** : cpu = 0.327159 (sec), leaf count = 0 , could not solve

```
DSolve[-((-1 + a^2*x^(2*n))*y[x]) + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + \left(-a^2x^{2\,n} + 1\right)\_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1016 ODE No. 1016

$$y(x)\left(ax^{2c} + bx^{c-1}\right) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.14153 (sec), leaf count = 312

$$\left\{\left\{y(x) \to 2^{\frac{c}{2(c+1)}} c_1 \left(x^{c+1}\right)^{\frac{c}{2(c+1)}} x^{-c/2} e^{-\frac{\sqrt{a}x^{c+1}}{\sqrt{-c^2-2c-1}}} U\left(\frac{\frac{\sqrt{a}cb}{\sqrt{-(c+1)^2}} + \frac{\sqrt{a}b}{\sqrt{-(c+1)^2}} + ac}{2(ca+a)}, \frac{c}{c+1}, \frac{2\sqrt{a}x^{c+1}}{\sqrt{-c^2-2c-1}}\right) + 2^{\overline{2(c}\right.\right.$$

✓ **Maple** : cpu = 0.204 (sec), leaf count = 91

$$\left\{y(x) = x^{-\frac{c}{2}}\left(M_{\frac{-ib}{2\,c+2}\,\frac{1}{\sqrt{a}},(2\,c+2)^{-1}}\left(\frac{2\,ix^{c+1}}{c+1}\sqrt{a}\right)\_C1 + W_{\frac{-ib}{2\,c+2}\,\frac{1}{\sqrt{a}},(2\,c+2)^{-1}}\left(\frac{2\,ix^{c+1}}{c+1}\sqrt{a}\right)\_C2\right)\right\}$$

2.1017 ODE No. 1017

$$\left(e^{2x} - v^2\right)y(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0278048 (sec), leaf count = 46

$$\left\{\left\{y(x) \to c_1\Gamma(1-v)J_{-v}\left(\sqrt{e^{2x}}\right) + c_2\Gamma(v+1)J_v\left(\sqrt{e^{2x}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 17

$$\{y(x) = \_C1\, J_v(\mathrm{e}^x) + \_C2\, Y_v(\mathrm{e}^x)\}$$

2.1018 ODE No. 1018

$$ae^{bx}y(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.022665 (sec), leaf count = 55

$$\left\{\left\{y(x)\to c_1 J_0\left(\frac{2\sqrt{a}\sqrt{e^{bx}}}{b}\right)+2c_2 Y_0\left(\frac{2\sqrt{a}\sqrt{e^{bx}}}{b}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 39

$$\left\{y(x)=\_C1\ J_0\left(2\,\frac{\sqrt{a}\mathrm{e}^{1/2\,bx}}{b}\right)+\_C2\ Y_0\left(2\,\frac{\sqrt{a}\mathrm{e}^{1/2\,bx}}{b}\right)\right\}$$

2.1019 ODE No. 1019

$$y''(x)-y(x)\left(4a^2b^2x^2e^{2bx^2}-1\right)=0$$

✗ **Mathematica** : cpu = 0.749412 (sec), leaf count = 0 , could not solve

```
DSolve[-((-1 + 4*a^2*b^2*E^(2*b*x^2)*x^2)*y[x]) + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\left(-4\,a^2b^2x^2\mathrm{e}^{2\,bx^2}+1\right)\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1020 ODE No. 1020

$$y(x)\left(ae^{2x}+be^{x}+c\right)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.682087 (sec), leaf count = 180

$$\left\{\left\{y(x)\to c_1 e^{i\left(\sqrt{c}\log\left(e^x\right)-\sqrt{a}e^x\right)}U\left(\frac{i\left(b-i\sqrt{a}+2\sqrt{a}\sqrt{c}\right)}{2\sqrt{a}},2i\sqrt{c}+1,2i\sqrt{a}e^x\right)+c_2 e^{i\left(\sqrt{c}\log\left(e^x\right)-\sqrt{a}e^x\right)}L^{2i\sqrt{c}}_{-\frac{i\left(2\sqrt{a}\sqrt{c}-i\sqrt{a}\right.}{2\sqrt{a}}}\right.\right.$$

✓ **Maple** : cpu = 0.186 (sec), leaf count = 58

$$\left\{y(x)=\mathrm{e}^{-\frac{x}{2}}\left(W_{-\frac{i}{2}b\frac{1}{\sqrt{a}},i\sqrt{c}}\left(2\,i\sqrt{a}\mathrm{e}^{x}\right)\_C2+M_{-\frac{i}{2}b\frac{1}{\sqrt{a}},i\sqrt{c}}\left(2\,i\sqrt{a}\mathrm{e}^{x}\right)\_C1\right)\right\}$$

2.1021 ODE No. 1021

$$y(x)\left(a\cos^2(x)+b\right)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0507722 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_1\text{MathieuC}\left[\frac{1}{2}(a+2b),-\frac{a}{4},x\right]+c_2\text{MathieuS}\left[\frac{1}{2}(a+2b),-\frac{a}{4},x\right]\right\}\right\}$$

✓ **Maple** : cpu = 0.214 (sec), leaf count = 39

$$\left\{y(x)=\_C1\ MathieuC\left(-\frac{a}{2}-b,\frac{a}{4},ix\right)+\_C2\ MathieuS\left(-\frac{a}{2}-b,\frac{a}{4},ix\right)\right\}$$

2.1022 ODE No. 1022

$$y(x)(a\cos(2x)+b)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0280746 (sec), leaf count = 28

$$\left\{\left\{y(x)\to c_1\text{MathieuC}\left[b,-\frac{a}{2},x\right]+c_2\text{MathieuS}\left[b,-\frac{a}{2},x\right]\right\}\right\}$$

✓ **Maple** : cpu = 0.201 (sec), leaf count = 21

$$\left\{y(x)=\_C1\ MathieuC\left(b,-\frac{a}{2},x\right)+\_C2\ MathieuS\left(b,-\frac{a}{2},x\right)\right\}$$

2.1023 ODE No. 1023

$$y(x)\left(a\cos^2(x)+b\right)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0158772 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_1\text{MathieuC}\left[\frac{1}{2}(a+2b),-\frac{a}{4},x\right]+c_2\text{MathieuS}\left[\frac{1}{2}(a+2b),-\frac{a}{4},x\right]\right\}\right\}$$

✓ **Maple** : cpu = 0.193 (sec), leaf count = 29

$$\left\{y(x)=\_C1\ MathieuC\left(\frac{a}{2}+b,-\frac{a}{4},x\right)+\_C2\ MathieuS\left(\frac{a}{2}+b,-\frac{a}{4},x\right)\right\}$$

2.1024 ODE No. 1024

$$y''(x) - y(x)\left(2\tan^2(x) + 1\right) = 0$$

✓ **Mathematica** : cpu = 0.165367 (sec), leaf count = 84

$$\left\{\left\{y(x) \to \frac{c_1 \sqrt[4]{1-\cos^2(x)}\sec(x)}{\sqrt[4]{\cos^2(x)-1}} - \frac{c_2 \sqrt[4]{1-\cos^2(x)}\sec(x)\left(\cos(x)\sqrt{1-\cos^2(x)} - \sin^{-1}(\cos(x))\right)}{2\sqrt[4]{\cos^2(x)-1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.139 (sec), leaf count = 30

$$\left\{y(x) = \frac{i\cos(x)\sin(x)\_C2 + \ln(\cos(x) + i\sin(x))\_C2 + \_C1}{\cos(x)}\right\}$$

2.1025 ODE No. 1025

$$y''(x) - y(x)\left(a + (m-1)m\sec^2(x) + (n-1)n\csc^2(x)\right) = 0$$

✓ **Mathematica** : cpu = 0.945808 (sec), leaf count = 615

$$\left\{\left\{y(x) \to \frac{c_2(-1)^{\frac{1}{2}(-2m-1)+1}\cos^2(x)^{\frac{1}{4}(-2m-1)+1}\left(\cos^2(x)-1\right)^{\frac{1}{2}\left(\frac{4am+4\sqrt{-a}n^2+4an-4\sqrt{-a}n+4(-a)^{3/2}+8\sqrt{-a}a+\sqrt{-a}+4mn^2-4}{8a+8n^2-8n+2}\right.}}{}\right.\right.$$

✓ **Maple** : cpu = 0.204 (sec), leaf count = 102

$$\left\{y(x) = (\sin(x))^n\left({}_2\mathrm{F}_1\left(\frac{n}{2} - \frac{m}{2} + \frac{i}{2}\sqrt{a} + \frac{1}{2}, \frac{n}{2} - \frac{m}{2} - \frac{i}{2}\sqrt{a} + \frac{1}{2}; \frac{3}{2} - m; (\cos(x))^2\right)(\cos(x))^{-m+1}\_C2 + (\cos(\right.\right.\right.$$

2.1026 ODE No. 1026

$$y''(x) - y(x)(B + n(n+1)\wp(x; \mathrm{g2}, \mathrm{g3})) = 0$$

✗ **Mathematica** : cpu = 0.183294 (sec), leaf count = 0 , could not solve

```
DSolve[-((B + n*(1 + n)*WeierstrassP[x, {g2, g3}])*y[x]) + Derivative[2][y][x] == 0, y[x], x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + (-n(n+1)\ WeierstrassP(x, g2, g3) - B)\_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1027 ODE No. 1027

$$y(x)\left(a\operatorname{sn}(x|k)^2+b\right)+y''(x)=0$$

✗ **Mathematica** : cpu = 1.30319 (sec), leaf count = 0 , could not solve

```
DSolve[(b + a*JacobiSN[x, k]^2)*y[x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.349 (sec), leaf count = 69

$$\left\{y(x)=\_C1\ HeunG\left(k^{-2},\frac{b}{4\,k^2},-\frac{n}{2},\frac{n}{2}+\frac{1}{2},\frac{1}{2},\frac{1}{2},(JacobiSN(x,k))^2\right)+\_C2\ HeunG\left(k^{-2},\frac{k^2+b+1}{4\,k^2},\frac{n}{2}+1,-\right.\right.$$

2.1028 ODE No. 1028

$$y''(x)-y(x)\left(ap(x)+b+\frac{p^4(x)}{30}+\frac{7p''(x)}{3}\right)=0$$

✗ **Mathematica** : cpu = 0.267845 (sec), leaf count = 0 , could not solve

```
DSolve[-(y[x]*(b + a*p[x] + (p^4)[x]/30 + (7*Derivative[2][p][x])/3)) + Derivative[2][y][x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\left(-\frac{\frac{\mathrm{d}^4}{\mathrm{d}x^4}p(x)}{30}-\frac{7\,\frac{\mathrm{d}^2}{\mathrm{d}x^2}p(x)}{3}-ap(x)-b\right)\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1029 ODE No. 1029

$$y''(x)-y(x)\left(f'(x)+f(x)^2\right)=0$$

✗ **Mathematica** : cpu = 0.11994 (sec), leaf count = 0 , could not solve

```
DSolve[-(y[x]*(f[x]^2 + Derivative[1][f][x])) + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.128 (sec), leaf count = 22

$$\left\{y(x)=\left(\int \mathrm{e}^{\int -2\,f(x)\,\mathrm{d}x}\,\mathrm{d}x+\_C1\right)\mathrm{e}^{\int f(x)\,\mathrm{d}x}\_C2\right\}$$

2.1030 ODE No. 1030

$$y(x)(l+P(x))+y''(x)=0$$

✗ **Mathematica** : cpu = 0.178931 (sec), leaf count = 0 , could not solve

```
DSolve[(l + P[x])*y[x] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{(P(x)+l)\_Y(x)+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1031 ODE No. 1031

$$y''(x)-f(x)y(x)=0$$

✗ **Mathematica** : cpu = 0.128714 (sec), leaf count = 0 , could not solve

```
DSolve[-(f[x]*y[x]) + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{-f(x)\_Y(x)+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1032 ODE No. 1032

$$y(x)\left(\frac{\left(\frac{1}{4}-v^2\right)g'(x)^2}{g(x)}+g'(x)^2+\frac{g^3(x)}{2g'(x)}-\frac{3g''(x)^2}{4g'(x)^2}\right)+y''(x)=0$$

✗ **Mathematica** : cpu = 0.492957 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*((g^3)[x]/(2*Derivative[1][g][x]) + Derivative[1][g][x]^2 + ((1/4 - v^2)*Derivat
```

✓ **Maple** : cpu = 0.112 (sec), leaf count = 48

$$\left\{y(x)=1\left(\_C2\,W_{\frac{i}{2}v^2-\frac{i}{8},\frac{1}{2}}(2\,ig(x))+\_C1\,M_{\frac{i}{2}v^2-\frac{i}{8},\frac{1}{2}}(2\,ig(x))\right)\frac{1}{\sqrt{\frac{\mathrm{d}}{\mathrm{d}x}g\left(x\right)}}\right\}$$

2.1033 ODE No. 1033

$$ae^{-2x}y(x)+y''(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0175565 (sec), leaf count = 37

$$\left\{\left\{y(x)\to c_1\cos\left(\sqrt{a}e^{-x}\right)-c_2\sin\left(\sqrt{a}e^{-x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 27

$$\left\{y(x)=\_C1\ \sin\left(\mathrm{e}^{-x}\sqrt{a}\right)+\_C2\ \cos\left(\mathrm{e}^{-x}\sqrt{a}\right)\right\}$$

2.1034 ODE No. 1034

$$y''(x)-y'(x)+e^{2x}y(x)=0$$

✓ **Mathematica** : cpu = 0.0120144 (sec), leaf count = 20

$$\{\{y(x)\to c_2\sin\left(e^x\right)+c_1\cos\left(e^x\right)\}\}$$

✓ **Maple** : cpu = 0.008 (sec), leaf count = 15

$$\left\{y(x)=\_C1\ \sin\left(\mathrm{e}^{x}\right)+\_C2\ \cos\left(\mathrm{e}^{x}\right)\right\}$$

2.1035 ODE No. 1035

$$ay'(x)+by(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.00584767 (sec), leaf count = 58

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{2}x\left(-\sqrt{a^2-4b}-a\right)}+c_2e^{\frac{1}{2}x\left(\sqrt{a^2-4b}-a\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 41

$$\left\{y(x)=\_C1\ \mathrm{e}^{-\frac{x}{2}\left(a-\sqrt{a^2-4\,b}\right)}+\_C2\ \mathrm{e}^{-\frac{x}{2}\left(a+\sqrt{a^2-4\,b}\right)}\right\}$$

2.1036 ODE No. 1036

$$ay'(x)+by(x)-f(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.486865 (sec), leaf count = 207

$$\left\{\left\{y(x)\to e^{\frac{1}{2}x\left(\sqrt{a^2-4b}-a\right)}\int_1^x\frac{f(K[2])\exp\left(\frac{1}{2}\left(-\sqrt{a^2-4b}-a\right)K[2]+aK[2]\right)}{\sqrt{a^2-4b}}dK[2]+e^{\frac{1}{2}x\left(-\sqrt{a^2-4b}-a\right)}\int_1^x-\frac{f(\right.\right.$$

✓ **Maple** : cpu = 0.093 (sec), leaf count = 124

$$\left\{y(x)=\mathrm{e}^{-\frac{x}{2}\left(a-\sqrt{a^2-4b}\right)}\_C2+\mathrm{e}^{-\frac{x}{2}\left(a+\sqrt{a^2-4b}\right)}\_C1+1\left(\int f(x)\,\mathrm{e}^{-\frac{x}{2}\left(-a+\sqrt{a^2-4b}\right)}\,\mathrm{d}x\mathrm{e}^{x\sqrt{a^2-4b}}-\int f(x)\,\mathrm{e}^{\frac{x}{2}\left(a+\sqrt{a\right.}\right.\right.$$

2.1037 ODE No. 1037

$$ay'(x)+y(x)\left(-\left(b^2x^2+c\right)\right)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0297993 (sec), leaf count = 101

$$\left\{\left\{y(x)\to c_1e^{-\frac{ax}{2}-\frac{bx^2}{2}}H_{\frac{-a^2-4b-4c}{8b}}\left(\sqrt{b}x\right)+c_2e^{-\frac{ax}{2}-\frac{bx^2}{2}}\,{}_1F_1\left(-\frac{-a^2-4b-4c}{16b};\frac{1}{2};bx^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.102 (sec), leaf count = 64

$$\left\{y(x)=\mathrm{e}^{-\frac{x(bx+a)}{2}}x\left(M\left(\frac{a^2+12\,b+4\,c}{16\,b},\frac{3}{2},bx^2\right)\_C1+U\left(\frac{a^2+12\,b+4\,c}{16\,b},\frac{3}{2},bx^2\right)\_C2\right)\right\}$$

2.1038 ODE No. 1038

$$2ay'(x)+f(x)y(x)+y''(x)=0$$

✗ **Mathematica** : cpu = 0.330765 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + 2*a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{f(x)\_Y(x)+2\,a\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1039 ODE No. 1039

$$y''(x) + xy'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.0129129 (sec), leaf count = 47

$$\left\{\left\{y(x) \to \sqrt{\frac{\pi}{2}} c_1 e^{-\frac{x^2}{2}} \text{erfi}\left(\frac{x}{\sqrt{2}}\right) + c_2 e^{-\frac{x^2}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 25

$$\left\{y(x) = \left(Erf\left(\frac{i}{2}\sqrt{2}x\right) \_C1 + \_C2\right) \left(\mathrm{e}^{\frac{x^2}{2}}\right)^{-1}\right\}$$

2.1040 ODE No. 1040

$$y''(x) + xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0306882 (sec), leaf count = 53

$$\left\{\left\{y(x) \to c_1 x - \frac{1}{2} c_2 e^{-\frac{x^2}{2}} \left(\sqrt{2\pi} e^{\frac{x^2}{2}} x \text{erf}\left(\frac{x}{\sqrt{2}}\right) + 2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.042 (sec), leaf count = 33

$$\left\{y(x) = \sqrt{\pi}\sqrt{2}\mathrm{e}^{-\frac{x^2}{2}} \_C2 + x\left(\pi \_C2\ Erf\left(\frac{\sqrt{2}x}{2}\right) + \_C1\right)\right\}$$

2.1041 ODE No. 1041

$$(n+1)y(x) + y''(x) + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0101882 (sec), leaf count = 55

$$\left\{\left\{y(x) \to c_1 e^{-\frac{x^2}{2}} H_n\left(\frac{x}{\sqrt{2}}\right) + c_2 e^{-\frac{x^2}{2}} {}_1F_1\left(-\frac{n}{2}; \frac{1}{2}; \frac{x^2}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 41

$$\left\{y(x) = \mathrm{e}^{-\frac{x^2}{2}} x\left(M\left(-\frac{n}{2} + \frac{1}{2}, \frac{3}{2}, \frac{x^2}{2}\right) \_C1 + U\left(-\frac{n}{2} + \frac{1}{2}, \frac{3}{2}, \frac{x^2}{2}\right) \_C2\right)\right\}$$

2.1042 ODE No. 1042

$$-ny(x)+y''(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.00879695 (sec), leaf count = 61

$$\left\{\left\{y(x)\to c_1 e^{-\frac{x^2}{2}} H_{-n-1}\left(\frac{x}{\sqrt{2}}\right)+c_2 e^{-\frac{x^2}{2}}\,{}_1F_1\left(\frac{n+1}{2};\frac{1}{2};\frac{x^2}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.065 (sec), leaf count = 41

$$\left\{y(x)=\mathrm{e}^{-\frac{x^2}{2}}x\left(U\left(\frac{n}{2}+1,\frac{3}{2},\frac{x^2}{2}\right)\_C2+M\left(\frac{n}{2}+1,\frac{3}{2},\frac{x^2}{2}\right)\_C1\right)\right\}$$

2.1043 ODE No. 1043

$$y''(x)-xy'(x)+2y(x)=0$$

✓ **Mathematica** : cpu = 0.0450429 (sec), leaf count = 69

$$\left\{\left\{y(x)\to \frac{1}{4}c_2\left(\sqrt{2\pi}x^2\operatorname{erfi}\left(\frac{x}{\sqrt{2}}\right)-\sqrt{2\pi}\operatorname{erfi}\left(\frac{x}{\sqrt{2}}\right)-2e^{\frac{x^2}{2}}x\right)+c_1\left(x^2-1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.211 (sec), leaf count = 39

$$\left\{y(x)=-2\,\mathrm{e}^{1/2\,x^2}\_C1\,x+\left(x-1\right)\left(1+x\right)\left(\sqrt{\pi}\sqrt{2}erfi\left(\frac{\sqrt{2}x}{2}\right)\_C1+\_C2\right)\right\}$$

2.1044 ODE No. 1044

$$-ay(x)+y''(x)-xy'(x)=0$$

✓ **Mathematica** : cpu = 0.00964394 (sec), leaf count = 39

$$\left\{\left\{y(x)\to c_1 H_{-a}\left(\frac{x}{\sqrt{2}}\right)+c_2\,{}_1F_1\left(\frac{a}{2};\frac{1}{2};\frac{x^2}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 35

$$\left\{y(x)=x\left(U\left(\frac{1}{2}+\frac{a}{2},\frac{3}{2},\frac{x^2}{2}\right)\_C2+M\left(\frac{1}{2}+\frac{a}{2},\frac{3}{2},\frac{x^2}{2}\right)\_C1\right)\right\}$$

2.1045 ODE No. 1045

$$y''(x) - xy'(x) + (x-1)y(x) = 0$$

✓ **Mathematica** : cpu = 0.0226966 (sec), leaf count = 39

$$\left\{\left\{y(x) \to \sqrt{\frac{\pi}{2}} c_2 e^{x-2} \text{erfi}\left(\frac{x-2}{\sqrt{2}}\right) + c_1 e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.008 (sec), leaf count = 21

$$\left\{y(x) = \mathrm{e}^{x}\left(Erf\left(\frac{i}{2}\sqrt{2}(x-2)\right)\_C1 + \_C2\right)\right\}$$

2.1046 ODE No. 1046

$$ay(x) + y''(x) - 2xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.00771893 (sec), leaf count = 31

$$\left\{\left\{y(x) \to c_1 H_{\frac{a}{2}}(x) + c_2 \, {}_1F_1\left(-\frac{a}{4}; \frac{1}{2}; x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 31

$$\left\{y(x) = x\left(M\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right)\_C1 + U\left(\frac{1}{2} - \frac{a}{4}, \frac{3}{2}, x^2\right)\_C2\right)\right\}$$

2.1047 ODE No. 1047

$$\left(4x^2 + 2\right) y(x) + y''(x) + 4xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0153627 (sec), leaf count = 27

$$\left\{\left\{y(x) \to c_1 e^{-x^2} + c_2 e^{-x^2} x\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 16

$$\left\{y(x) = \mathrm{e}^{-x^2}(\_C2\, x + \_C1)\right\}$$

2.1048 ODE No. 1048

$$\left(2n+3x^2-1\right)y(x)+y''(x)-4xy'(x)=0$$

✓ **Mathematica** : cpu = 0.011479 (sec), leaf count = 45

$$\left\{\left\{y(x)\to c_1e^{\frac{x^2}{2}}H_n(x)+c_2e^{\frac{x^2}{2}}\,{}_1F_1\left(-\frac{n}{2};\frac{1}{2};x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 37

$$\left\{y(x)=\mathrm{e}^{\frac{x^2}{2}}x\left(U\left(-\frac{n}{2}+\frac{1}{2},\frac{3}{2},x^2\right)\_C2+M\left(-\frac{n}{2}+\frac{1}{2},\frac{3}{2},x^2\right)\_C1\right)\right\}$$

2.1049 ODE No. 1049

$$\left(4x^2-1\right)y(x)+y''(x)-4xy'(x)-e^x=0$$

✓ **Mathematica** : cpu = 0.0698578 (sec), leaf count = 109

$$\left\{\left\{y(x)\to c_1e^{x(x-i)}-\frac{1}{2}ic_2e^{(x-i)x+2ix}+\frac{1}{4}\sqrt{\pi}e^{x(x-i)-\frac{i}{2}}\left(e^{2ix}\text{erfi}\left(\left(\frac{1}{2}+\frac{i}{2}\right)-ix\right)-ie^i\text{erf}\left(-x+\left(\frac{1}{2}+\frac{i}{2}\right)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.167 (sec), leaf count = 66

$$\left\{y(x)=\frac{\left(\left(i\cos(x)+\sin(x)\right)\sqrt{\pi}\mathrm{e}^{\frac{i}{2}}Erf\left(x-\frac{1}{2}-\frac{i}{2}\right)-\left(i\cos(x)-\sin(x)\right)\sqrt{\pi}\mathrm{e}^{-\frac{i}{2}}Erf\left(x-\frac{1}{2}+\frac{i}{2}\right)+4\sin(x)\_C\right.}{4}\right.$$

2.1050 ODE No. 1050

$$\left(4x^2-2\right)y(x)+y''(x)-4xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0138127 (sec), leaf count = 23

$$\left\{\left\{y(x)\to c_1e^{x^2}+c_2e^{x^2}x\right\}\right\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 14

$$\left\{y(x)=\mathrm{e}^{x^2}(\_C2\,x+\_C1)\right\}$$

2.1051 ODE No. 1051

$$\left(4x^2-3\right)y(x)-e^{x^2}+y''(x)-4xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0348739 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_1e^{(x-1)x}+\frac{1}{2}c_2e^{(x-1)x+2x}-e^{(x-1)x+x}\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 27

$$\left\{y(x)=\mathrm{e}^{x(1+x)}\_C2+\mathrm{e}^{x(x-1)}\_C1-\mathrm{e}^{x^2}\right\}$$

2.1052 ODE No. 1052

$$axy'(x)+by(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0223949 (sec), leaf count = 78

$$\left\{\left\{y(x)\to c_1e^{-\frac{ax^2}{2}}H_{\frac{b-a}{a}}\left(\frac{\sqrt{a}x}{\sqrt{2}}\right)+c_2e^{-\frac{ax^2}{2}}\,{}_1F_1\left(-\frac{b-a}{2a};\frac{1}{2};\frac{ax^2}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 58

$$\left\{y(x)=\mathrm{e}^{-\frac{ax^2}{2}}x\left(M\left(\frac{2\,a-b}{2\,a},\frac{3}{2},\frac{ax^2}{2}\right)\_C1+U\left(\frac{2\,a-b}{2\,a},\frac{3}{2},\frac{ax^2}{2}\right)\_C2\right)\right\}$$

2.1053 ODE No. 1053

$$a^2x^2y(x)+2axy'(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0303429 (sec), leaf count = 57

$$\left\{\left\{y(x)\to c_1e^{-\frac{ax^2}{2}-\sqrt{a}x}+\frac{c_2e^{\sqrt{a}x-\frac{ax^2}{2}}}{2\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 35

$$\left\{y(x)=\_C1\,\mathrm{e}^{-\frac{x}{2}\left(ax-2\sqrt{a}\right)}+\_C2\,\mathrm{e}^{-\frac{x}{2}\left(ax+2\sqrt{a}\right)}\right\}$$

2.1054 ODE No. 1054

$$(ax+b)y'(x)+y(x)(cx+d)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0481931 (sec), leaf count = 172

$$\left\{\left\{y(x)\to c_1 e^{\frac{cx}{a}-\frac{ax^2}{2}-bx} H_{\frac{-a^3+a^2d-abc+c^2}{a^3}}\left(\frac{ab-2c}{\sqrt{2}a^{3/2}}+\frac{\sqrt{a}x}{\sqrt{2}}\right)+c_2 e^{\frac{cx}{a}-\frac{ax^2}{2}-bx}\,{}_1F_1\left(-\frac{-a^3+da^2-bca+c^2}{2a^3};\frac{1}{2};\left(\frac{ab}{\sqrt{}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 98

$$\left\{y(x)=\mathrm{e}^{-\frac{cx}{a}}\left(U\left(\frac{da^2-abc+c^2}{2\,a^3},\frac{1}{2},-\frac{\left(a^2x+ab-2\,c\right)^2}{2\,a^3}\right)\_C2+M\left(\frac{da^2-abc+c^2}{2\,a^3},\frac{1}{2},-\frac{\left(a^2x+ab-2\,c\right)^2}{2\,a^3}\right.\right.\right.$$

2.1055 ODE No. 1055

$$(ax+b)y'(x)+y(x)\left(\mathrm{a1}x^2+\mathrm{b1}x+\mathrm{c1}\right)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.1568 (sec), leaf count = 421

$$\left\{\left\{y(x)\to c_1\exp\left(\frac{-bx\sqrt{a^2-4\mathrm{a1}}-\frac{1}{2}ax^2\sqrt{a^2-4\mathrm{a1}}-\frac{1}{2}a^2x^2-abx+2\mathrm{a1}x^2+2\mathrm{b1}x}{2\sqrt{a^2-4\mathrm{a1}}}\right)H_{\frac{-a^3-a^2\sqrt{a^2-4\mathrm{a1}}+4\mathrm{a1}\sqrt{a^2-4\mathrm{a}}}{2}}\right.\right.$$

✓ **Maple** : cpu = 0.233 (sec), leaf count = 262

$$\left\{y(x)=\left(\_C2\left(a^2x+ab-4\,a1\,x-2\,b1\right)\,{}_1\mathrm{F}_1\left(\frac{1}{4}\left(3\left(a^2-4\,a1\right)^{3/2}+a^3-2\,a^2c1+\left(2\,b1\,b-4\,a1\right)a+\left(-2\,b^2+\right.\right.\right.\right.\right.$$

2.1056 ODE No. 1056

$$x^2\left(-y'(x)\right)+y''(x)+xy(x)=0$$

✓ **Mathematica** : cpu = 0.0391575 (sec), leaf count = 66

$$\left\{\left\{y(x)\to c_1x-\frac{c_2\left(3e^{\frac{x^3}{3}}\left(-x^3\right)^{2/3}+3^{2/3}x^3\Gamma\left(\frac{2}{3},-\frac{x^3}{3}\right)\right)}{3\left(-x^3\right)^{2/3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.108 (sec), leaf count = 48

$$\left\{y(x)=\frac{1}{x^2}\left(-\mathrm{e}^{\frac{x^3}{3}}\left(-x^3\right)^{\frac{2}{3}}\sqrt[3]{3}\_C2+x^3\left(\_C2\,\Gamma\left(\frac{2}{3}\right)-\_C2\,\Gamma\left(\frac{2}{3},-\frac{x^3}{3}\right)+\_C1\right)\right)\right\}$$

2.1057 ODE No. 1057

$$x^2(-y'(x)) + y''(x) - (x+1)^2 y(x) = 0$$

✓ **Mathematica** : cpu = 0.865006 (sec), leaf count = 55

$$\left\{\left\{y(x) \to c_2 e^{\frac{x^3}{3}+x} \int_1^x e^{-\frac{1}{3}K[1]^3 - 2K[1]}\, dK[1] + c_1 e^{\frac{x^3}{3}+x}\right\}\right\}$$

✓ **Maple** : cpu = 0.132 (sec), leaf count = 50

$$\left\{y(x) = \_C1\ HeunT\left(0, -3, 2\sqrt[3]{3}, \frac{3^{\frac{2}{3}}x}{3}\right) \mathrm{e}^{-x} + \_C2\ HeunT\left(0, 3, 2\sqrt[3]{3}, -\frac{3^{\frac{2}{3}}x}{3}\right) \mathrm{e}^{\frac{x\left(x^2+3\right)}{3}}\right\}$$

2.1058 ODE No. 1058

$$\left(x^4 - 2\right) xy(x) - (x+1)x^2 y'(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.886152 (sec), leaf count = 55

$$\left\{\left\{y(x) \to c_2 e^{\frac{x^3}{3}} \int_1^x e^{\frac{K[1]^4}{4} - \frac{K[1]^3}{3}}\, dK[1] + c_1 e^{\frac{x^3}{3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.117 (sec), leaf count = 29

$$\left\{y(x) = \mathrm{e}^{\frac{x^3}{3}} \left(\int \mathrm{e}^{\frac{x^4}{4} - \frac{x^3}{3}}\, \mathrm{d}x \_C2 + \_C1\right)\right\}$$

2.1059 ODE No. 1059

$$x^4 y'(x) - x^3 y(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0561805 (sec), leaf count = 72

$$\left\{\left\{y(x) \to c_1 x - \frac{c_2 e^{-\frac{x^5}{5}} \left(5\left(x^5\right)^{4/5} - 5^{4/5} e^{\frac{x^5}{5}} x^5 \Gamma\left(\frac{4}{5}, \frac{x^5}{5}\right)\right)}{5\left(x^5\right)^{4/5}}\right\}\right\}$$

✓ **Maple** : cpu = 0.088 (sec), leaf count = 56

$$\left\{y(x) = \frac{1}{x^7}\left(9 \_C2\, \mathrm{e}^{-1/10\, x^5}\left(x^5+4\right) M_{7/5, \frac{9}{10}}\left(1/5\, x^5\right) + x^8\left(x^2 \_C2\, \mathrm{e}^{-\frac{x^5}{10}} M_{\frac{2}{5}, \frac{9}{10}}\left(\frac{x^5}{5}\right) + \_C1\right)\right)\right\}$$

2.1060 ODE No. 1060

$$ax^{q-1}y'(x)+bx^{q-2}y(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0369115 (sec), leaf count = 83

$$\left\{\left\{y(x)\to c_2q^{-1/q}a^{\frac{1}{q}}(x^q)^{\frac{1}{q}}\ {}_1F_1\left(\frac{b}{aq}+\frac{1}{q};1+\frac{1}{q};-\frac{ax^q}{q}\right)+c_1\ {}_1F_1\left(\frac{b}{aq};1-\frac{1}{q};-\frac{ax^q}{q}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 81

$$\left\{y(x)=\mathrm{e}^{-\frac{ax^q}{q}}x\left(M\left(\frac{aq-b}{aq},\ \frac{q+1}{q},\ \frac{ax^q}{q}\right)\_C1+U\left(\frac{aq-b}{aq},\ \frac{q+1}{q},\ \frac{ax^q}{q}\right)\_C2\right)\right\}$$

2.1061 ODE No. 1061

$$-e^{-\frac{x^{3/2}}{3}}x+y''(x)+\sqrt{x}y'(x)+\left(\frac{x}{4}+\frac{1}{4\sqrt{x}}-9\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.094834 (sec), leaf count = 70

$$\left\{\left\{y(x)\to c_1e^{-\frac{1}{3}(\sqrt{x}+9)x}+\frac{1}{6}c_2e^{6x-\frac{1}{3}(\sqrt{x}+9)x}-\frac{1}{9}e^{3x-\frac{1}{3}(\sqrt{x}+9)x}x\right\}\right\}$$

✓ **Maple** : cpu = 0.088 (sec), leaf count = 28

$$\left\{y(x)=-\frac{-9\cosh(3x)\_C1-9\sinh(3x)\_C2+x}{9}\mathrm{e}^{-\frac{1}{3}x^{\frac{3}{2}}}\right\}$$

2.1062 ODE No. 1062

$$\frac{\left(x+\sqrt{x}-8\right)y(x)}{4x^2}+y''(x)-\frac{y'(x)}{\sqrt{x}}=0$$

✓ **Mathematica** : cpu = 0.0288294 (sec), leaf count = 35

$$\left\{\left\{y(x)\to\frac{1}{3}c_2e^{\sqrt{x}}x^2+\frac{c_1e^{\sqrt{x}}}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.024 (sec), leaf count = 19

$$\left\{y(x)=\frac{\_C2\,x^3+\_C1}{x}\mathrm{e}^{\sqrt{x}}\right\}$$

2.1063 ODE No. 1063

$$y''(x) - (2e^x + 1)\, y'(x) + e^{2x} y(x) - e^{3x} = 0$$

✓ **Mathematica** : cpu = 0.0460147 (sec), leaf count = 28

$$\left\{\left\{y(x) \to c_1 e^{e^x} + c_2 e^{x+e^x} + e^x + 2\right\}\right\}$$

✓ **Maple** : cpu = 0.36 (sec), leaf count = 61

$$\left\{y(x) = \left(\_C1 \cosh\left(\frac{x}{2}\right) + \_C2 \sinh\left(\frac{x}{2}\right)\right) \mathrm{e}^{\mathrm{e}^x + \frac{x}{2}} + \mathrm{e}^{\frac{x}{2}} \left(\left(\mathrm{e}^{2x} + \mathrm{e}^x + 1\right) \cosh\left(\frac{x}{2}\right) - 3\left(\mathrm{e}^x + 1/3\,\mathrm{e}^{2x} + 1\right) \sinh(x\right.\right.$$

2.1064 ODE No. 1064

$$a y'(x) + b y(x) + y''(x) + \tan(x) = 0$$

✓ **Mathematica** : cpu = 0.578074 (sec), leaf count = 1400

$$\left\{\left\{y(x) \to e^{\frac{1}{2}\left(-a-\sqrt{a^2-4b}\right)x} c_1 + e^{\frac{1}{2}\left(\sqrt{a^2-4b}-a\right)x} c_2 + \frac{8\left(2\,{}_2F_1\left(1, \frac{1}{4}i\left(\sqrt{a^2-4b}-a\right); \frac{1}{4}i\left(\sqrt{a^2-4b}-a\right)+1; -e^{2ix}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.296 (sec), leaf count = 125

$$\left\{y(x) = \mathrm{e}^{-\frac{x}{2}\left(a-\sqrt{a^2-4b}\right)} \_C2 + \mathrm{e}^{-\frac{x}{2}\left(a+\sqrt{a^2-4b}\right)} \_C1 - 1\left(\int \tan(x)\, \mathrm{e}^{-\frac{x}{2}\left(-a+\sqrt{a^2-4b}\right)}\, \mathrm{d}x \mathrm{e}^{x\sqrt{a^2-4b}} - \int \tan(x)\, \mathrm{e}^{\frac{x}{2}\left(\right.\right.\right.$$

2.1065 ODE No. 1065

$$\left(n^2 - a^2\right) y(x) + 2n \cot(x) y'(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.161478 (sec), leaf count = 114

$$\left\{\left\{y(x) \to c_1 \left(\cos^2(x) - 1\right)^{\frac{1}{4}(1-2n)} P^{\frac{1}{2}(2n-1)}_{\frac{1}{2}\left(2\sqrt{2n^2-a^2}-1\right)}(\cos(x)) + c_2 \left(\cos^2(x) - 1\right)^{\frac{1}{4}(1-2n)} Q^{\frac{1}{2}(2n-1)}_{\frac{1}{2}\left(2\sqrt{2n^2-a^2}-1\right)}(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.237 (sec), leaf count = 60

$$\left\{y(x) = (\sin(x))^{-n+\frac{1}{2}} \left(\mathit{LegendreQ}\left(-\frac{1}{2} + \sqrt{-a^2+2n^2}, n - \frac{1}{2}, \cos(x)\right) \_C2 + \mathit{LegendreP}\left(-\frac{1}{2} + \sqrt{-a^2+2n\right.\right.\right.$$

2.1066 ODE No. 1066

$$y''(x) + \tan(x)y'(x) + y(x)\cos^2(x) = 0$$

✓ **Mathematica** : cpu = 0.035247 (sec), leaf count = 18

$$\{\{y(x) \to c_2 \sin(\sin(x)) + c_1 \cos(\sin(x))\}\}$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 15

$$\{y(x) = \_C1 \sin(\sin(x)) + \_C2 \cos(\sin(x))\}$$

2.1067 ODE No. 1067

$$y''(x) + \tan(x)y'(x) - y(x)\cos^2(x) = 0$$

✓ **Mathematica** : cpu = 0.0334247 (sec), leaf count = 21

$$\{\{y(x) \to c_1 \cosh(\sin(x)) + ic_2 \sinh(\sin(x))\}\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 17

$$\left\{y(x) = \_C1 \, \mathrm{e}^{\sin(x)} + \_C2 \, \mathrm{e}^{-\sin(x)}\right\}$$

2.1068 ODE No. 1068

$$v(v+1)y(x) + y''(x) + \cot(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.151334 (sec), leaf count = 20

$$\{\{y(x) \to c_1 P_v(\cos(x)) + c_2 Q_v(\cos(x))\}\}$$

✓ **Maple** : cpu = 0.223 (sec), leaf count = 45

$$\left\{y(x) = \_C1 \, {}_2\mathrm{F}_1(-\frac{v}{2}, \frac{1}{2} + \frac{v}{2}; \frac{1}{2}; (\cos(x))^2) + \_C2 \cos(x) \, {}_2\mathrm{F}_1(1 + \frac{v}{2}, \frac{1}{2} - \frac{v}{2}; \frac{3}{2}; (\cos(x))^2)\right\}$$

2.1069 ODE No. 1069

$$y''(x) - \cot(x)y'(x) + y(x)\sin^2(x) = 0$$

✓ **Mathematica** : cpu = 0.0364546 (sec), leaf count = 19

$$\{\{y(x) \to c_1 \cos(\cos(x)) - c_2 \sin(\cos(x))\}\}$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 15

$$\{y(x) = \_C1 \ \sin(\cos(x)) + \_C2 \ \cos(\cos(x))\}$$

2.1070 ODE No. 1070

$$a\tan(x)y'(x) + by(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.320237 (sec), leaf count = 143

$$\left\{\left\{y(x) \to c_1 \, {}_2F_1\left(-\frac{a}{4} - \frac{1}{4}\sqrt{a^2+4b}, \frac{1}{4}\sqrt{a^2+4b} - \frac{a}{4}; \frac{1}{2} - \frac{a}{2}; \cos^2(x)\right) + i^{a+1}c_2 \cos^{a+1}(x) \, {}_2F_1\left(\frac{a}{4} - \frac{1}{4}\sqrt{a^2+4b}\right.\right.\right.$$

✓ **Maple** : cpu = 0.174 (sec), leaf count = 60

$$\left\{y(x) = (\cos(x))^{\frac{1}{2}+\frac{a}{2}} \left(LegendreQ\left(\frac{1}{2}\sqrt{a^2+4\,b} - \frac{1}{2}, \frac{1}{2} + \frac{a}{2}, \sin(x)\right) \_C2 + LegendreP\left(\frac{1}{2}\sqrt{a^2+4\,b} - \frac{1}{2}, \frac{1}{2} + \frac{a}{2}\right.\right.\right.$$

2.1071 ODE No. 1071

$$\left(b^2 - a^2\right)y(x) + 2a\cot(ax)y'(x) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0980463 (sec), leaf count = 59

$$\left\{\left\{y(x) \to c_1 e^{-\sqrt{-b^2}x}\csc(ax) + \frac{c_2 e^{\sqrt{-b^2}x}\csc(ax)}{2\sqrt{-b^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.047 (sec), leaf count = 24

$$\left\{y(x) = \frac{\_C2 \ \cos(bx) + \_C1 \ \sin(bx)}{\sin(ax)}\right\}$$

2.1072 ODE No. 1072

$$y(x)\left(-4anp(x)^2+a+bp(x)\right)+ap''(x)y'(x)+y''(x)=0$$

✗ **Mathematica** : cpu = 0.275542 (sec), leaf count = 0 , could not solve

```
DSolve[(a + b*p[x] - 4*a*n*p[x]^2)*y[x] + a*Derivative[1][y][x]*Derivative[2][p][x] + Deriva
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+a\left(\frac{\mathrm{d}^2}{\mathrm{d}x^2}p(x)\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\left(a+bp(x)-4na(p(x))^2\right)\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1073 ODE No. 1073

$$\frac{y'(x)\left(-\wp(x;a,b)\wp'(x;a,b)+\wp(x;a,b)^3-6\wp(x;a,b)^2+\frac{a}{2}\right)}{\wp'(x;a,b)-\wp(x;a,b)^2}+\frac{y(x)\left(\wp(x;a,b)^2(-\wp'(x;a,b))-\left(6\wp(x;a,b)^2-\frac{a}{2}\right)\wp\right.}{\wp(x;a,b)^2+\wp'(x;a,b)}$$

✗ **Mathematica** : cpu = 1.34869 (sec), leaf count = 0 , could not solve

```
DSolve[((-(WeierstrassP[x, {a, b}]*(-a/2 + 6*WeierstrassP[x, {a, b}]^2)) - WeierstrassP[x, {
WeierstrassP[x, {a, b}]^2 + WeierstrassPPrime[x, {a, b}]) + Derivative[2][y][x] == 0, y[x],
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\frac{\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{WeierstrassPPrime\left(x,a,b\right)+\left(WeierstrassP\left(x,a,b\right)\right)^2}\left(11\ WeierstrassP(x,a,b\right.\right.\right.$$

2.1074 ODE No. 1074

$$\frac{k^2\mathrm{cn}(x|k)\mathrm{sn}(x|k)y'(x)}{\mathrm{dn}(x|k)}+n^2y(x)\mathrm{dn}(x|k)^2+y''(x)=0$$

✗ **Mathematica** : cpu = 54.9339 (sec), leaf count = 0 , could not solve

```
DSolve[n^2*JacobiDN[x, k]^2*y[x] + (k^2*JacobiCN[x, k]*JacobiSN[x, k]*Derivative[1][y][x])/J
```

✓ **Maple** : cpu = 0.017 (sec), leaf count = 21

$$\{y(x)=\_C1\ \sin\left(nJacobiAM(x,k)\right)+\_C2\ \cos\left(nJacobiAM(x,k)\right)\}$$

2.1075 ODE No. 1075

$$f(x)y'(x) + g(x)y(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.178737 (sec), leaf count = 0 , could not solve

```
DSolve[g[x]*y[x] + f[x]*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{g(x)\_Y(x) + f(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x) + \frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1076 ODE No. 1076

$$y(x)\left(a + f'(x)\right) + f(x)y'(x) - g(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.19809 (sec), leaf count = 0 , could not solve

```
DSolve[-g[x] + y[x]*(a + Derivative[1][f][x]) + f[x]*Derivative[1][y][x] + Derivative[2][y][
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + f(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x) + \left(\frac{\mathrm{d}}{\mathrm{d}x}f(x) + a\right)\_Y(x) - g(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1077 ODE No. 1077

$$y'(x)(af(x) + b) + y(x)(cf(x) + d) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.304597 (sec), leaf count = 0 , could not solve

```
DSolve[(d + c*f[x])*y[x] + (b + a*f[x])*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + (af(x) + b)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x) + (cf(x) + d)\_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1078 ODE No. 1078

$$y(x)\left(a+\frac{f'(x)}{2}+\frac{f(x)^2}{4}\right)+f(x)y'(x)+y''(x)=0$$

✓ **Mathematica** : cpu = 0.0711954 (sec), leaf count = 73

$$\left\{\left\{y(x)\to c_1\exp\left(-\frac{1}{2}\int_1^x f(K[1])\,dK[1]-\sqrt{-a}x\right)+\frac{c_2e^{\sqrt{-a}x-\frac{1}{2}\int_1^x f(K[1])\,dK[1]}}{2\sqrt{-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 33

$$\left\{y(x)=\mathrm{e}^{-\frac{\int f(x)\,\mathrm{d}x}{2}}\left(\sinh\left(\sqrt{-a}x\right)\_C1+\cosh\left(\sqrt{-a}x\right)\_C2\right)\right\}$$

2.1079 ODE No. 1079

$$by(x)f(x)^{2a}-\frac{af'(x)y'(x)}{f(x)}+y''(x)=0$$

✓ **Mathematica** : cpu = 0.238688 (sec), leaf count = 135

$$\left\{\left\{y(x)\to\frac{1}{2}\left(e^{c_2+\int_1^x -i\sqrt{b}f(K[1])^a\,dK[1]}-2c_1\exp\left(-c_2-\int_1^x -i\sqrt{b}f(K[1])^a\,dK[1]\right)\right)\right\},\left\{y(x)\to\frac{1}{2}\left(e^{c_2+\int_1^x i\sqrt{b}f(K[1]\right.\right.\right.$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 37

$$\left\{y(x)=\_C1\,\mathrm{e}^{\int i(f(x))^a\sqrt{b}\,\mathrm{d}x}+\_C2\,\mathrm{e}^{-\int i(f(x))^a\sqrt{b}\,\mathrm{d}x}\right\}$$

2.1080 ODE No. 1080

$$y(x)\left(a^2+\frac{af'(x)}{f(x)}-b^2f(x)^2\right)-y'(x)\left(2a+\frac{f'(x)}{f(x)}\right)+y''(x)=0$$

✗ **Mathematica** : cpu = 0.307113 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*(a^2 - b^2*f[x]^2 + (a*Derivative[1][f][x])/f[x]) - (2*a + Derivative[1][f][x]/f
```

✓ **Maple** : cpu = 0.329 (sec), leaf count = 74

$$\left\{y(x)=\mathrm{e}^{\int -1\left(\frac{f(x)\left(\mathrm{e}^{\_C1\,b}\right)^2b}{\left(\mathrm{e}^{\int f(x)\,\mathrm{d}x b}\right)^2}+bf(x)-\frac{\left(\mathrm{e}^{\_C1\,b}\right)^2a}{\left(\mathrm{e}^{\int f(x)\,\mathrm{d}x b}\right)^2}+a\right)\left(\frac{\left(\mathrm{e}^{\_C1\,b}\right)^2}{\left(\mathrm{e}^{\int f(x)\,\mathrm{d}x b}\right)^2}-1\right)^{-1}\mathrm{d}x}\_C2\right\}$$

2.1081 ODE No. 1081

$$-\frac{a^2 y(x) f'(x)^2}{b^2+f(x)^2}+\frac{f(x) f^3(x) y'(x)}{b^2+f(x)^2}+y''(x)=0$$

✗ **Mathematica** : cpu = 0.826144 (sec), leaf count = 0 , could not solve

```
DSolve[-((a^2*y[x]*Derivative[1][f][x]^2)/(b^2 + f[x]^2)) + (f[x]*(f^3)[x]*Derivative[1][y][
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\frac{f(x)\left(\frac{\mathrm{d}^3}{\mathrm{d}x^3}f(x)\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{(f(x))^2+b^2}-\frac{\left(\frac{\mathrm{d}}{\mathrm{d}x}f(x)\right)^2 a^2\_Y(x)}{(f(x))^2+b^2}\right\},\{\_Y(x)\}\right)\right\}$$

2.1082 ODE No. 1082

$$y(x)\left(\frac{\left(m^2-v^2\right)g'(x)^2}{g(x)}+g'(x)^2\right)-y'(x)\left(\frac{(2m-1)g'(x)}{g(x)}+\frac{g''(x)}{g'(x)}\right)+y''(x)=0$$

✗ **Mathematica** : cpu = 0.539833 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*(Derivative[1][g][x]^2 + ((m^2 - v^2)*Derivative[1][g][x]^2)/g[x]) - Derivative[
1 + 2*m)*Derivative[1][g][x])/g[x] + Derivative[2][g][x]/Derivative[1][g][x]) + Derivative[2
```

✓ **Maple** : cpu = 0.131 (sec), leaf count = 74

$$\left\{y(x)=(g(x))^{2m}\,\mathrm{e}^{-ig(x)}\left(U\left(\frac{i}{2}m^2-\frac{i}{2}v^2+m+\frac{1}{2},2m+1,2ig(x)\right)\_C2+M\left(\frac{i}{2}m^2-\frac{i}{2}v^2+m+\frac{1}{2},2m+1\right.\right.\right.$$

2.1083 ODE No. 1083

$$-\frac{f'(x)y'(x)}{f(x)}+y(x)\left(-\frac{f''(x)}{2f(x)}+\frac{3f'(x)^2}{4f(x)^2}+\frac{\left(\frac{1}{4}-v^2\right)g'(x)^2}{g(x)^2}+g'(x)^2+\frac{g^3(x)}{2g'(x)}-\frac{3g''(x)^2}{4g'(x)^2}\right)+y''(x)=0$$

✗ **Mathematica** : cpu = 0.826787 (sec), leaf count = 0 , could not solve

```
DSolve[-((Derivative[1][f][x]*Derivative[1][y][x])/f[x]) + y[x]*((3*Derivative[1][f][x]^2)/(
```

✓ **Maple** : cpu = 0.106 (sec), leaf count = 31

$$\left\{y(x)=\sqrt{\frac{f(x)\,g(x)}{\frac{\mathrm{d}}{\mathrm{d}x}g(x)}}\left(J_v(g(x))\_C1+Y_v(g(x))\_C2\right)\right\}$$

2.1084 ODE No. 1084

$$-y'(x)\left(\frac{2f'(x)}{f(x)}-\frac{g'(x)}{g(x)}+\frac{g''(x)}{g'(x)}\right)+y(x)\left(-\frac{f''(x)}{f(x)}+\frac{f'(x)\left(\frac{2f'(x)}{f(x)}-\frac{g'(x)}{g(x)}+\frac{g''(x)}{g'(x)}\right)}{f(x)}-\frac{v^2g'(x)^2}{g(x)^2}+g'(x)^2\right)+y''(x)$$

✗ **Mathematica** : cpu = 0.867474 (sec), leaf count = 0 , could not solve

```
DSolve[-(Derivative[1][y][x]*((2*Derivative[1][f][x])/f[x] - Derivative[1][g][x]/g[x] + Deri
```

✓ **Maple** : cpu = 0.083 (sec), leaf count = 20

$$\{y(x)=f(x)\left(J_v(g(x))\_C1+Y_v(g(x))\_C2\right)\}$$

2.1085 ODE No. 1085

$$-y'(x)\left(\frac{(2v-1)g'(x)}{g(x)}+\frac{g''(x)}{g'(x)}+\frac{2h'(x)}{h(x)}\right)+y(x)\left(g'(x)^2+\frac{h'(x)\left(\frac{(2v-1)g'(x)}{g(x)}+\frac{g''(x)}{g'(x)}+\frac{2h'(x)}{h(x)}\right)}{h(x)}-\frac{h''(x)}{h(x)}\right)+y''(x$$

✗ **Mathematica** : cpu = 0.908022 (sec), leaf count = 0 , could not solve

```
DSolve[-(Derivative[1][y][x]*(((-1 + 2*v)*Derivative[1][g][x])/g[x] + (2*Derivative[1][h][x]
1 + 2*v)*Derivative[1][g][x])/g[x] + (2*Derivative[1][h][x])/h[x] + Derivative[2][g][x]/Deri
```

✓ **Maple** : cpu = 0.079 (sec), leaf count = 24

$$\{y(x)=h(x)\left(g(x)\right)^v\left(J_v(g(x))\_C1+Y_v(g(x))\_C2\right)\}$$

2.1086 ODE No. 1086

$$4y''(x)+9xy(x)=0$$

✓ **Mathematica** : cpu = 0.0060547 (sec), leaf count = 42

$$\left\{\left\{y(x)\to c_1\text{Ai}\left(\sqrt[3]{-1}\left(\frac{3}{2}\right)^{2/3}x\right)+c_2\text{Bi}\left(\sqrt[3]{-1}\left(\frac{3}{2}\right)^{2/3}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.024 (sec), leaf count = 29

$$\left\{y(x)=\_C1\,\text{Ai}\left(-\frac{3^{\frac{2}{3}}\sqrt[3]{2}x}{2}\right)+\_C2\,\text{Bi}\left(-\frac{3^{\frac{2}{3}}\sqrt[3]{2}x}{2}\right)\right\}$$

2.1087 ODE No. 1087

$$4y''(x) - \left(a + x^2\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.00928684 (sec), leaf count = 36

$$\left\{\left\{y(x) \to c_1 D_{\frac{1}{4}(-a-2)}(x) + c_2 D_{\frac{a-2}{4}}(ix)\right\}\right\}$$

✓ **Maple** : cpu = 0.076 (sec), leaf count = 33

$$\left\{y(x) = 1\left(\_C2\, W_{-\frac{a}{8},\frac{1}{4}}\left(\frac{x^2}{2}\right) + \_C1\, M_{-\frac{a}{8},\frac{1}{4}}\left(\frac{x^2}{2}\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1088 ODE No. 1088

$$4y''(x) + 4\tan(x)y'(x) + y(x)\left(-\left(5\tan^2(x) + 2\right)\right) = 0$$

✓ **Mathematica** : cpu = 0.103028 (sec), leaf count = 180

$$\left\{\left\{y(x) \to -\frac{(-1)^{7/8}2^{5/8}c_1}{\sqrt[8]{-8\cos^2(2x) - 16\cos(2x) - 8}} + \frac{3(-1)^{5/8}c_2\left(4\sqrt[4]{-1}2^{3/4}\sinh^{-1}\left(\frac{1}{2}\sqrt[4]{-\frac{1}{2}}\sqrt[4]{-8\cos^2(2x) - 16\cos(2\right.\right.\right.$$
$$\left.\left.\left.8\sqrt[8]{2}\sqrt[8]{\right.\right.\right.$$

✓ **Maple** : cpu = 0.14 (sec), leaf count = 31

$$\left\{y(x) = \left(i\cos(x)\sin(x)\_C2 - \ln\left(\sin(x) + i\cos(x)\right)\_C2 + \_C1\right)\frac{1}{\sqrt{\cos(x)}}\right\}$$

2.1089 ODE No. 1089

$$-y'(x)(ab + c + x) + ay''(x) + y(x)(b(c + x) + d) = 0$$

✓ **Mathematica** : cpu = 0.0464585 (sec), leaf count = 99

$$\left\{\left\{y(x) \to c_1 e^{bx} H_d\left(\frac{x}{\sqrt{2}\sqrt{a}} - \frac{ab - c}{\sqrt{2}\sqrt{a}}\right) + c_2 e^{bx}\, {}_1F_1\left(-\frac{d}{2}; \frac{1}{2}; \left(\frac{x}{\sqrt{2}\sqrt{a}} - \frac{ab - c}{\sqrt{2}\sqrt{a}}\right)^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 58

$$\left\{y(x) = \mathrm{e}^{bx}\left(U\left(-\frac{d}{2}, \frac{1}{2}, \frac{(ab - c - x)^2}{2\,a}\right)\_C2 + M\left(-\frac{d}{2}, \frac{1}{2}, \frac{(ab - c - x)^2}{2\,a}\right)\_C1\right)\right\}$$

2.1090 ODE No. 1090

$$a\left(a^2-2be^{-ax}\right)y'(x)+a^2y''(x)+b^2e^{-2ax}y(x)=0$$

✓ **Mathematica** : cpu = 0.0334109 (sec), leaf count = 50

$$\left\{\left\{y(x)\to c_1e^{-\frac{be^{-ax}}{a^2}}-\frac{bc_2e^{-\frac{be^{-ax}}{a^2}-ax}}{a^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 40

$$\left\{y(x)=\mathrm{e}^{-\frac{a^3x+2\,be^{-ax}}{2\,a^2}}\left(\sinh\left(\frac{ax}{2}\right)\_C1+\cosh\left(\frac{ax}{2}\right)\_C2\right)\right\}$$

2.1091 ODE No. 1091

$$x\left(y''(x)+y(x)\right)-\cos(x)=0$$

✓ **Mathematica** : cpu = 0.0279021 (sec), leaf count = 41

$$\left\{\left\{y(x)\to c_2\sin(x)+c_1\cos(x)+\frac{1}{2}(\mathrm{Ci}(2x)\sin(x)-\mathrm{Si}(2x)\cos(x)+\log(x)\sin(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 35

$$\left\{y(x)=\frac{\sin(x)\,Ci(2\,x)}{2}-\frac{Si(2\,x)\cos(x)}{2}+\frac{(2\,\_C2+\ln(x))\sin(x)}{2}+\cos(x)\,\_C1\right\}$$

2.1092 ODE No. 1092

$$(a+x)y(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.100264 (sec), leaf count = 72

$$\left\{\left\{y(x)\to c_2e^{-ix}x\,{}_1F_1\left(1-\frac{1}{4}i(-2(a-2)-4);2;2ix\right)+c_1e^{-ix}xU\left(1-\frac{1}{4}i(-2(a-2)-4),2,2ix\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 29

$$\left\{y(x)=\_C1\,M_{-\frac{i}{2}a,\,\frac{1}{2}}(2\,ix)+\_C2\,W_{-\frac{i}{2}a,\,\frac{1}{2}}(2\,ix)\right\}$$

2.1093 ODE No. 1093

$$xy''(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.00572768 (sec), leaf count = 13

$$\{\{y(x) \to c_1 \log(x) + c_2\}\}$$

✓ **Maple** : cpu = 0.006 (sec), leaf count = 10

$$\{y(x) = \_C2 \ln(x) + \_C1\}$$

2.1094 ODE No. 1094

$$ay(x) + xy''(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0244594 (sec), leaf count = 41

$$\{\{y(x) \to c_1 J_0\left(2\sqrt{a}\sqrt{x}\right) + 2c_2 Y_0\left(2\sqrt{a}\sqrt{x}\right)\}\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 29

$$\{y(x) = \_C1 \, J_0\left(2\sqrt{a}\sqrt{x}\right) + \_C2 \, Y_0\left(2\sqrt{a}\sqrt{x}\right)\}$$

2.1095 ODE No. 1095

$$lxy(x) + xy''(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.00999432 (sec), leaf count = 30

$$\left\{\left\{y(x) \to c_1 J_0\left(\sqrt{l}x\right) + c_2 Y_0\left(\sqrt{l}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 23

$$\left\{y(x) = \_C1 \, J_0\left(\sqrt{l}x\right) + \_C2 \, Y_0\left(\sqrt{l}x\right)\right\}$$

2.1096 ODE No. 1096

$$(a+x)y(x)+xy''(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0138079 (sec), leaf count = 61

$$\left\{\left\{y(x)\to c_1 e^{-ix}U\left(\frac{1}{2}i(a-i),1,2ix\right)+c_2 e^{-ix}L_{-\frac{1}{2}i(a-i)}(2ix)\right\}\right\}$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 39

$$\left\{y(x)=\mathrm{e}^{-ix}\left(U\left(\frac{1}{2}+\frac{i}{2}a,\,1,\,2\,ix\right)\_C2+M\left(\frac{1}{2}+\frac{i}{2}a,\,1,\,2\,ix\right)\_C1\right)\right\}$$

2.1097 ODE No. 1097

$$ay(x)+xy''(x)-y'(x)=0$$

✓ **Mathematica** : cpu = 0.0281808 (sec), leaf count = 46

$$\{\{y(x)\to 2ac_1xJ_2\left(2\sqrt{a}\sqrt{x}\right)-2ac_2xY_2\left(2\sqrt{a}\sqrt{x}\right)\}\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 31

$$\left\{y(x)=x\left(J_2\left(2\sqrt{a}\sqrt{x}\right)\_C1+Y_2\left(2\sqrt{a}\sqrt{x}\right)\_C2\right)\right\}$$

2.1098 ODE No. 1098

$$-ax^3y(x)+xy''(x)-y'(x)=0$$

✓ **Mathematica** : cpu = 0.0105914 (sec), leaf count = 41

$$\left\{\left\{y(x)\to c_1\cosh\left(\frac{\sqrt{a}x^2}{2}\right)+ic_2\sinh\left(\frac{\sqrt{a}x^2}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 27

$$\left\{y(x)=\_C1\,\sinh\left(\frac{x^2}{2}\sqrt{a}\right)+\_C2\,\cosh\left(\frac{x^2}{2}\sqrt{a}\right)\right\}$$

2.1099 ODE No. 1099

$$x^3\left(e^{x^3}-v^2\right)y(x)+xy''(x)-y'(x)=0$$

✗ **Mathematica** : cpu = 1.04912 (sec), leaf count = 0 , could not solve

```
DSolve[(E^x^3 - v^2)*x^3*y[x] - Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.044 (sec), leaf count = 25

$$\left\{y(x)=\_C1\,J_v\left(\mathrm{e}^{\frac{x^2}{2}}\right)+\_C2\,Y_v\left(\mathrm{e}^{\frac{x^2}{2}}\right)\right\}$$

2.1100 ODE No. 1100

$$xy''(x)+2y'(x)-xy(x)-e^x=0$$

✓ **Mathematica** : cpu = 0.0307061 (sec), leaf count = 44

$$\left\{\left\{y(x)\to\frac{c_1e^{-x}}{x}+\frac{c_2e^x}{2x}+\frac{e^x(2x-1)}{4x}\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 23

$$\left\{y(x)=\frac{\sinh(x)\_C2}{x}+\frac{\cosh(x)\_C1}{x}+\frac{\mathrm{e}^x}{2}\right\}$$

2.1101 ODE No. 1101

$$axy(x)+xy''(x)+2y'(x)=0$$

✓ **Mathematica** : cpu = 0.0279866 (sec), leaf count = 51

$$\left\{\left\{y(x)\to\frac{c_1e^{-\sqrt{-a}x}}{x}+\frac{c_2e^{\sqrt{-a}x}}{2\sqrt{-a}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 29

$$\left\{y(x)=\frac{1}{x}\left(\_C2\,\cosh\left(\sqrt{-a}x\right)+\_C1\,\sinh\left(\sqrt{-a}x\right)\right)\right\}$$

2.1102 ODE No. 1102

$$ax^2y(x)+xy''(x)+2y'(x)=0$$

✓ **Mathematica** : cpu = 0.00765077 (sec), leaf count = 42

$$\left\{\left\{y(x)\to \frac{c_1\text{Ai}\left(-\frac{ax}{(-a)^{2/3}}\right)}{x}+\frac{c_2\text{Bi}\left(-\frac{ax}{(-a)^{2/3}}\right)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 33

$$\left\{y(x)=1\left(\_C2\,Y_{\frac{1}{3}}\left(\frac{2}{3}\sqrt{a}x^{\frac{3}{2}}\right)+\_C1\,J_{\frac{1}{3}}\left(\frac{2}{3}\sqrt{a}x^{\frac{3}{2}}\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1103 ODE No. 1103

$$ay(x)+xy''(x)-2y'(x)=0$$

✓ **Mathematica** : cpu = 0.0288384 (sec), leaf count = 64

$$\left\{\left\{y(x)\to 6a^{3/2}c_1x^{3/2}J_3\left(2\sqrt{a}\sqrt{x}\right)-2ia^{3/2}c_2x^{3/2}Y_3\left(2\sqrt{a}\sqrt{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 33

$$\left\{y(x)=x^{\frac{3}{2}}\left(J_3\left(2\sqrt{a}\sqrt{x}\right)\_C1+Y_3\left(2\sqrt{a}\sqrt{x}\right)\_C2\right)\right\}$$

2.1104 ODE No. 1104

$$ay(x)+vy'(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0377915 (sec), leaf count = 104

$$\left\{\left\{y(x)\to c_2a^{\frac{v-1}{2}-v+1}x^{\frac{v-1}{2}-v+1}\Gamma(2-v)J_{1-v}\left(2\sqrt{a}\sqrt{x}\right)+c_1a^{\frac{1-v}{2}}x^{\frac{1-v}{2}}\Gamma(v)J_{v-1}\left(2\sqrt{a}\sqrt{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 41

$$\left\{y(x)=x^{\frac{1}{2}-\frac{v}{2}}\left(Y_{v-1}\left(2\sqrt{a}\sqrt{x}\right)\_C2+J_{v-1}\left(2\sqrt{a}\sqrt{x}\right)\_C1\right)\right\}$$

2.1105 ODE No. 1105

$$ay'(x)+bxy(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.022863 (sec), leaf count = 64

$$\left\{\left\{y(x)\to c_1 x^{\frac{1-a}{2}} J_{\frac{a-1}{2}}\left(\sqrt{b}x\right)+c_2 x^{\frac{1-a}{2}} Y_{\frac{a-1}{2}}\left(\sqrt{b}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 39

$$\left\{y(x)=x^{-\frac{a}{2}+\frac{1}{2}}\left(Y_{\frac{a}{2}-\frac{1}{2}}\left(\sqrt{b}x\right)\_C2+J_{\frac{a}{2}-\frac{1}{2}}\left(\sqrt{b}x\right)\_C1\right)\right\}$$

2.1106 ODE No. 1106

$$ay'(x)+bx^{\mathrm{a1}}y(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0538687 (sec), leaf count = 441

$$\left\{\left\{y(x)\to c_1\left(\frac{1}{\mathrm{a1}}+1\right)^{\frac{a}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}-\frac{1}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}}\mathrm{a1}^{\frac{a}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}-\frac{1}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}}b^{\frac{1}{2}\left(\frac{1}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}-\frac{a}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}\right)}\left(x^{\mathrm{a1}}\right)^{\frac{1}{2}\left(\frac{1}{\mathrm{a1}}+1\right)\left(\frac{1}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}-\frac{a}{\left(\frac{1}{\mathrm{a1}}+1\right)\mathrm{a1}}\right)}\right.\right.$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 71

$$\left\{y(x)=x^{-\frac{a}{2}+\frac{1}{2}}\left(J_{\frac{a-1}{a1+1}}\left(2\frac{\sqrt{b}x^{a1/2+1/2}}{a1+1}\right)\_C1+Y_{\frac{a-1}{a1+1}}\left(2\frac{\sqrt{b}x^{a1/2+1/2}}{a1+1}\right)\_C2\right)\right\}$$

2.1107 ODE No. 1107

$$ay(x)+(b+x)y'(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0312139 (sec), leaf count = 40

$$\left\{\left\{y(x)\to c_1 e^{-x}U(b-a,b,x)+c_2 e^{-x}L_{a-b}^{b-1}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.074 (sec), leaf count = 30

$$\left\{y(x)=\mathrm{e}^{-x}(U(-a+b,\,b,\,x)\_C2+M(-a+b,\,b,\,x)\_C1)\right\}$$

2.1108 ODE No. 1108

$$(a+b+x)y'(x)+ay(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0361212 (sec), leaf count = 37

$$\left\{\left\{y(x)\to c_1 e^{-x}U(b,a+b,x)+c_2 e^{-x}L_{-b}^{a+b-1}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 26

$$\left\{y(x)=\mathrm{e}^{-x}(M(b,\,a+b,\,x)\_C1+U(b,\,a+b,\,x)\_C2)\right\}$$

2.1109 ODE No. 1109

$$xy''(x)-xy'(x)-y(x)-e^x x(x+1)=0$$

✓ **Mathematica** : cpu = 0.054013 (sec), leaf count = 45

$$\left\{\left\{y(x)\to c_2(-e^x x\mathrm{Ei}(-x)-1)+c_1 e^x x+e^x\left(x^2+x-x\log(-x)-1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 33

$$\left\{y(x)=\mathrm{e}^{x}\left(-\_C1\ Ei(1,x)\,x+x^2+x\_C2-x\ln\left(x\right)+\mathrm{e}^{-x}\_C1-1\right)\right\}$$

2.1110 ODE No. 1110

$$-ay(x)+xy''(x)-xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0439652 (sec), leaf count = 36

$$\left\{\left\{y(x)\to c_2 G_{1,2}^{2,0}\left(-x\left|\begin{array}{c}1-a\\0,1\end{array}\right.\right)+c_1 x\,{}_1F_1(a+1;2;x)\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 23

$$\left\{y(x)=x(M(a+1,\,2,\,x)\_C1+U(a+1,\,2,\,x)\_C2)\right\}$$

2.1111 ODE No. 1111

$$xy''(x) - (x+1)y'(x) + y(x) = 0$$

✓ **Mathematica** : cpu = 0.0187737 (sec), leaf count = 20

$$\{\{y(x) \to c_1 e^x + c_2(-x-1)\}\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 13

$$\{y(x) = \_C2\, \mathrm{e}^{x} + \_C1\, x + \_C1\}$$

2.1112 ODE No. 1112

$$xy''(x) - (x+1)y'(x) - 2(x-1)y(x) = 0$$

✓ **Mathematica** : cpu = 0.0267063 (sec), leaf count = 30

$$\left\{\left\{y(x) \to c_1 e^{2x} - \frac{1}{9}c_2 e^{-x}(3x+1)\right\}\right\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 22

$$\left\{y(x) = \_C1\, \mathrm{e}^{2\,x} + \_C2\, \mathrm{e}^{-x}(3\,x+1)\right\}$$

2.1113 ODE No. 1113

$$-ay(x) + (b-x)y'(x) + xy''(x) = 0$$

✓ **Mathematica** : cpu = 0.0225283 (sec), leaf count = 24

$$\left\{\left\{y(x) \to c_1 U(a,b,x) + c_2 L_{-a}^{b-1}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 17

$$\{y(x) = \_C1\, M(a,\, b,\, x) + \_C2\, U(a,\, b,\, x)\}$$

2.1114 ODE No. 1114

$$xy''(x) - 2(x-1)y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0423672 (sec), leaf count = 39

$$\left\{\left\{y(x) \to c_2 G^{2,0}_{1,2}\left(-2x \middle| \begin{matrix} \frac{1}{2} \\ -1, 0 \end{matrix}\right) + c_1 e^x (I_0(x) - I_1(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 34

$$\{y(x) = \mathrm{e}^x (\_C2\, K_1(-x) - \_C2\, K_0(-x) + \_C1\, (I_0(x) - I_1(x)))\}$$

2.1115 ODE No. 1115

$$xy''(x) - (3x-2)y'(x) - (2x-3)y(x) = 0$$

✓ **Mathematica** : cpu = 0.0650904 (sec), leaf count = 76

$$\left\{\left\{y(x) \to c_2 e^{-\frac{1}{2}\left(\sqrt{17}-3\right)x}\, {}_1F_1\left(1 - \frac{6}{\sqrt{17}}; 2; \sqrt{17}x\right) + c_1 e^{-\frac{1}{2}\left(\sqrt{17}-3\right)x} U\left(1 - \frac{6}{\sqrt{17}}, 2, \sqrt{17}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.091 (sec), leaf count = 47

$$\left\{y(x) = \mathrm{e}^{-\frac{x\left(-3+\sqrt{17}\right)}{2}} \left(U\left(1 - \frac{6\sqrt{17}}{17}, 2, \sqrt{17}x\right) \_C2 + M\left(1 - \frac{6\sqrt{17}}{17}, 2, \sqrt{17}x\right) \_C1\right)\right\}$$

2.1116 ODE No. 1116

$$y'(x)(ax + b + n) + any(x) + xy''(x) = 0$$

✓ **Mathematica** : cpu = 0.052934 (sec), leaf count = 43

$$\left\{\left\{y(x) \to c_1 e^{-ax} U(b, b+n, ax) + c_2 e^{-ax} L^{b+n-1}_{-b}(ax)\right\}\right\}$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 31

$$\{y(x) = \mathrm{e}^{-ax} (U(b,\, b+n,\, ax) \_C2 + M(b,\, b+n,\, ax) \_C1)\}$$

2.1117 ODE No. 1117

$$-(x+1)(a+b)y'(x)+abxy(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0947784 (sec), leaf count = 107

$$\left\{\left\{y(x)\to c_1 U\left(-\frac{-a^2-ba-a+b}{a-b},a+b+2,(a-b)x\right)e^{(a+b+1)\log(x)+bx}+c_2 L^{a+b+1}_{\frac{-a^2-ab-a+b}{a-b}}(x(a-b))e^{(a+b+1)\log(}\right.\right.$$

✓ **Maple** : cpu = 0.11 (sec), leaf count = 82

$$\left\{y(x)=x^{a+b+1}\mathrm{e}^{bx}\left(U\left(\frac{a^2+ab+a-b}{a-b},\,a+b+2,\,x(a-b)\right)\_C2+M\left(\frac{a^2+ab+a-b}{a-b},\,a+b+2,\,x(a-b)\right)\_\right.\right.$$

2.1118 ODE No. 1118

$$y'(x)(x(a+b)+m+n)+y(x)(abx+an+bm)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0961841 (sec), leaf count = 51

$$\{\{y(x)\to c_1 e^{-ax}U(m,m+n,(a-b)x)+c_2 e^{-ax}L^{m+n-1}_{-m}(x(a-b))\}\}$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 39

$$\{y(x)=\mathrm{e}^{-ax}(U(m,\,m+n,\,x(a-b))\_C2+M(m,\,m+n,\,x(a-b))\_C1)\}$$

2.1119 ODE No. 1119

$$y(x)\left(a^2x+2ab\right)-2(ax+b)y'(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.178397 (sec), leaf count = 77

$$\left\{\left\{y(x)\to c_1 e^{ax}x^{b-\frac{1}{2}\sqrt{(2b+1)^2}+\frac{1}{2}}+\frac{c_2 e^{ax}x^{b+\frac{1}{2}\sqrt{(2b+1)^2}+\frac{1}{2}}}{\sqrt{(2b+1)^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.041 (sec), leaf count = 20

$$\left\{y(x)=\mathrm{e}^{ax}\left(x^{2\,b+1}\_C2+\_C1\right)\right\}$$

2.1120 ODE No. 1120

$$(ax+b)y'(x)+y(x)(cx+d)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0645423 (sec), leaf count = 166

$$\left\{\left\{y(x)\to c_1 e^{\frac{1}{2}x\left(-\sqrt{a^2-4c}-a\right)}U\left(-\frac{-ab-\sqrt{a^2-4c}b+2d}{2\sqrt{a^2-4c}},b,\sqrt{a^2-4c}x\right)+c_2 e^{\frac{1}{2}x\left(-\sqrt{a^2-4c}-a\right)}L^{b-1}_{\frac{-b\sqrt{a^2-4c}-ab+2d}{2\sqrt{a^2-4c}}}\left(x\right.\right.\right.$$

✓ **Maple** : cpu = 0.216 (sec), leaf count = 109

$$\left\{y(x)=\mathrm{e}^{-\frac{x}{2}\left(a+\sqrt{a^2-4\,c}\right)}\left(U\left(\frac{1}{2}\left(b\sqrt{a^2-4\,c}+ab-2\,d\right)\frac{1}{\sqrt{a^2-4\,c}},\,b,\,\sqrt{a^2-4\,c}x\right)\_C2+M\left(\frac{1}{2}\left(b\sqrt{a^2-4\,c}+\right.\right.\right.\right.$$

2.1121 ODE No. 1121

$$-\left(x^2-x\right)y'(x)+xy''(x)+(x-1)y(x)=0$$

✓ **Mathematica** : cpu = 9.73639 (sec), leaf count = 40

$$\left\{\left\{y(x)\to c_2 x\int_1^x\frac{e^{\frac{K[1]^2}{2}-K[1]}}{K[1]^2}\,dK[1]+c_1 x\right\}\right\}$$

✓ **Maple** : cpu = 0.024 (sec), leaf count = 23

$$\left\{y(x)=\left(\int\frac{1}{x^2}\mathrm{e}^{\frac{x(x-2)}{2}}\,\mathrm{d}x\_C1+\_C2\right)x\right\}$$

2.1122 ODE No. 1122

$$-\left(x^2-x-2\right)y'(x)+xy''(x)-x(x+3)y(x)=0$$

✓ **Mathematica** : cpu = 9.45095 (sec), leaf count = 56

$$\left\{\left\{y(x)\to c_2 e^{\frac{x^2}{2}}\int_1^x\frac{e^{-\frac{1}{2}K[1]^2-K[1]}}{K[1]^2}\,dK[1]+c_1 e^{\frac{x^2}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.151 (sec), leaf count = 28

$$\left\{y(x)=\mathrm{e}^{\frac{x^2}{2}}\left(\int\frac{1}{x^2}\mathrm{e}^{-\frac{x(x+2)}{2}}\,\mathrm{d}x\_C2+\_C1\right)\right\}$$

2.1123 ODE No. 1123

$$-\left(2ax^2+1\right)y'(x)+bx^3y(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0128066 (sec), leaf count = 91

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{2}\sqrt{b}x^2\left(\frac{a}{\sqrt{b}}-\frac{\sqrt{a^2-b}}{\sqrt{b}}\right)}+c_2e^{\frac{1}{2}\sqrt{b}x^2\left(\frac{\sqrt{a^2-b}}{\sqrt{b}}+\frac{a}{\sqrt{b}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 45

$$\left\{y(x)=\_C1\,\mathrm{e}^{\frac{x^2}{2}\left(\sqrt{a^2-b}+a\right)}+\_C2\,\mathrm{e}^{-\frac{x^2}{2}\left(\sqrt{a^2-b}-a\right)}\right\}$$

2.1124 ODE No. 1124

$$-2\left(x^2-a\right)y'(x)+2nxy(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.065118 (sec), leaf count = 65

$$\left\{\left\{y(x)\to c_1\,{}_1F_1\left(-\frac{n}{2};a+\frac{1}{2};x^2\right)+i^{1-2a}c_2x^{1-2a}\,{}_1F_1\left(-a-\frac{n}{2}+\frac{1}{2};\frac{3}{2}-a;x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.079 (sec), leaf count = 29

$$\left\{y(x)=\_C1\,M\left(-\frac{n}{2},\,\frac{1}{2}+a,\,x^2\right)+\_C2\,U\left(-\frac{n}{2},\,\frac{1}{2}+a,\,x^2\right)\right\}$$

2.1125 ODE No. 1125

$$-4x^5-4x^3y(x)+\left(4x^2-1\right)y'(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.187612 (sec), leaf count = 48

$$\left\{\left\{y(x)\to c_1e^{-\left(1-\sqrt{2}\right)x^2}+c_2e^{-\left(1+\sqrt{2}\right)x^2}-x^2-2\right\}\right\}$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 36

$$\left\{y(x)=\mathrm{e}^{x^2\left(\sqrt{2}-1\right)}\_C2+\mathrm{e}^{-x^2\left(1+\sqrt{2}\right)}\_C1-x^2-2\right\}$$

2.1126 ODE No. 1126

$$\left(a^2x^3+a\right)y(x)+\left(2ax^3-1\right)y'(x)+xy''(x)=0$$

✗ **Mathematica** : cpu = 1.19099 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{\left(a^2x^3+a\right)y(x)+\left(2x^3a-1\right)y'(x)+xy''(x)=0,y(1)=c_1,y'(1)=c_2\right\}\right)(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 19

$$\left\{y(x)=\mathrm{e}^{-\frac{ax^3}{3}}\left(\_C2\,x^2+\_C1\right)\right\}$$

2.1127 ODE No. 1127

$$y(x)\left(a^2x\log^2(x)+a\log(x)+a\right)+(2ax\log(x)+1)y'(x)+xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0414095 (sec), leaf count = 36

$$\left\{\left\{y(x)\to c_1e^{ax}x^{-ax}+c_2e^{ax}x^{-ax}\log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 21

$$\left\{y(x)=x^{-ax}\mathrm{e}^{ax}(\ln(x)\_C2+\_C1)\right\}$$

2.1128 ODE No. 1128

$$(xf(x)+2)y'(x)+f(x)y(x)+xy''(x)=0$$

✗ **Mathematica** : cpu = 0.256098 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + (2 + x*f[x])*Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.223 (sec), leaf count = 32

$$\left\{y(x)=\frac{1}{x}\left(\_C2\int \mathrm{e}^{\int \frac{-xf(x)-2}{x}\,\mathrm{d}x}x^2\,\mathrm{d}x+\_C1\right)\right\}$$

2.1129 ODE No. 1129

$$(x-3)y''(x)-(4x-9)y'(x)+(3x-6)y(x)=0$$

✓ **Mathematica** : cpu = 0.0388676 (sec), leaf count = 42

$$\left\{\left\{y(x)\to \frac{1}{8}c_2e^{3x-9}\left(4x^3-42x^2+150x-183\right)+c_1e^{x-3}\right\}\right\}$$

✓ **Maple** : cpu = 0.034 (sec), leaf count = 30

$$\left\{y(x) = \_C1\,\mathrm{e}^{x}+\_C2\,\mathrm{e}^{3\,x}\left(4\,x^3-42\,x^2+150\,x-183\right)\right\}$$

2.1130 ODE No. 1130

$$ay(x)+2xy''(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0125727 (sec), leaf count = 46

$$\left\{\left\{y(x)\to c_2\sin\left(\sqrt{2}\sqrt{a}\sqrt{x}\right)+c_1\cos\left(\sqrt{2}\sqrt{a}\sqrt{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 31

$$\left\{y(x) = \_C1\,\sin\left(\sqrt{x}\sqrt{2}\sqrt{a}\right)+\_C2\,\cos\left(\sqrt{x}\sqrt{2}\sqrt{a}\right)\right\}$$

2.1131 ODE No. 1131

$$ay(x)+2xy''(x)-(x-1)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0119136 (sec), leaf count = 58

$$\left\{\left\{y(x)\to c_1\sqrt{x}U\left(\frac{1}{2}(1-2a),\frac{3}{2},\frac{x}{2}\right)+c_2\sqrt{x}L^{\frac{1}{2}}_{\frac{1}{2}(2a-1)}\left(\frac{x}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 33

$$\left\{y(x) = \sqrt{x}\left(U\left(-a+\frac{1}{2},\frac{3}{2},\frac{x}{2}\right)\_C2+M\left(-a+\frac{1}{2},\frac{3}{2},\frac{x}{2}\right)\_C1\right)\right\}$$

2.1132 ODE No. 1132

$$ay(x)+2xy''(x)-(2x-1)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0116304 (sec), leaf count = 48

$$\left\{\left\{y(x)\to c_1\sqrt{x}U\left(\frac{1-a}{2},\frac{3}{2},x\right)+c_2\sqrt{x}L^{\frac{1}{2}}_{\frac{a-1}{2}}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 29

$$\left\{y(x)=\sqrt{x}\left(U\left(-\frac{a}{2}+\frac{1}{2},\frac{3}{2},x\right)\_C2+M\left(-\frac{a}{2}+\frac{1}{2},\frac{3}{2},x\right)\_C1\right)\right\}$$

2.1133 ODE No. 1133

$$(2x-1)y''(x)-(3x-4)y'(x)+(x-3)y(x)=0$$

✓ **Mathematica** : cpu = 0.0906932 (sec), leaf count = 92

$$\left\{\left\{y(x)\to 2^{5/8}c_1e^{x-\frac{1}{2}}+\frac{c_2e^{\frac{x}{2}-\frac{1}{2}}\left(\sqrt{2}e^{x/2}\sqrt[4]{2x-1}\Gamma\left(\frac{3}{4},\frac{1}{4}(2x-1)\right)-2\sqrt[4]{e}\right)}{2^{5/8}\sqrt[4]{2x-1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 37

$$\left\{y(x)=1\mathrm{e}^{\frac{x}{2}}\left(U\left(1,\frac{3}{4},\frac{x}{2}-\frac{1}{4}\right)\_C2+M\left(1,\frac{3}{4},\frac{x}{2}-\frac{1}{4}\right)\_C1\right)\frac{1}{\sqrt[4]{2\,x-1}}\right\}$$

2.1134 ODE No. 1134

$$4xy''(x)-(a+x)y(x)=0$$

✓ **Mathematica** : cpu = 0.0945592 (sec), leaf count = 78

$$\left\{\left\{y(x)\to\frac{1}{4}c_2e^{-x/2}x\,{}_1F_1\left(\frac{1}{128}(-32(-a-4i)-128i)+1;2;x\right)+\frac{1}{4}c_1e^{-x/2}xU\left(\frac{1}{128}(-32(-a-4i)-128i)+1\right.\right.\right.$$

✓ **Maple** : cpu = 0.044 (sec), leaf count = 21

$$\left\{y(x)=\_C1\,M_{-\frac{a}{4},\frac{1}{2}}(x)+\_C2\,W_{-\frac{a}{4},\frac{1}{2}}(x)\right\}$$

2.1135 ODE No. 1135

$$4xy''(x) + 2y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0104689 (sec), leaf count = 27

$$\{\{y(x) \to c_1 \cosh\left(\sqrt{x}\right) + ic_2 \sinh\left(\sqrt{x}\right)\}\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 17

$$\{y(x) = \_C1 \sinh\left(\sqrt{x}\right) + \_C2 \cosh\left(\sqrt{x}\right)\}$$

2.1136 ODE No. 1136

$$4xy''(x) + 4y'(x) - (x+2)y(x) = 0$$

✓ **Mathematica** : cpu = 0.0206987 (sec), leaf count = 30

$$\left\{\left\{y(x) \to c_2 e^{x/2} \text{Ei}(-x) + c_1 e^{x/2}\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 16

$$\left\{y(x) = \mathrm{e}^{\frac{x}{2}} (Ei(1,x) \_C2 + \_C1)\right\}$$

2.1137 ODE No. 1137

$$ly(x) + 4xy''(x) - (x+2)y(x) + 4y(x) = 0$$

✓ **Mathematica** : cpu = 0.0972058 (sec), leaf count = 74

$$\left\{\left\{y(x) \to \frac{1}{4} c_2 e^{-x/2} x \, {}_1F_1\left(\frac{1}{128}(-32(l+(2-4i))-128i)+1;2;x\right) + \frac{1}{4} c_1 e^{-x/2} x U\left(\frac{1}{128}(-32(l+(2-4i))-12\right.\right.$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 25

$$\left\{y(x) = \_C1 \, M_{\frac{l}{4}+\frac{1}{2},\frac{1}{2}}(x) + \_C2 \, W_{\frac{l}{4}+\frac{1}{2},\frac{1}{2}}(x)\right\}$$

2.1138 ODE No. 1138

$$y(x)(-(-2m-4n+x))+4my'(x)+4xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0298934 (sec), leaf count = 38

$$\left\{\left\{y(x)\to c_1e^{-x/2}U(-n,m,x)+c_2e^{-x/2}L_n^{m-1}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 26

$$\left\{y(x)=\mathrm{e}^{-\frac{x}{2}}(U(-n,\,m,\,x)\_C2+M(-n,\,m,\,x)\_C1)\right\}$$

2.1139 ODE No. 1139

$$-(a+x)y(x)+16xy''(x)+8y'(x)=0$$

✓ **Mathematica** : cpu = 0.0134904 (sec), leaf count = 74

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{4}(2\log(x)-x)}U\left(\frac{a+6}{8},\frac{3}{2},\frac{x}{2}\right)+c_2e^{\frac{1}{4}(2\log(x)-x)}L^{\frac{1}{2}}_{\frac{1}{8}(-a-6)}\left(\frac{x}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.074 (sec), leaf count = 37

$$\left\{y(x)=\sqrt{x}\mathrm{e}^{-\frac{x}{4}}\left(U\left(\frac{a}{8}+\frac{3}{4},\frac{3}{2},\frac{x}{2}\right)\_C2+M\left(\frac{a}{8}+\frac{3}{4},\frac{3}{2},\frac{x}{2}\right)\_C1\right)\right\}$$

2.1140 ODE No. 1140

$$axy''(x)+by'(x)+cy(x)=0$$

✓ **Mathematica** : cpu = 0.0481928 (sec), leaf count = 190

$$\left\{\left\{y(x)\to c_1a^{\frac{1}{2}\left(\frac{b}{a}-1\right)}c^{\frac{1}{2}\left(1-\frac{b}{a}\right)}x^{\frac{1}{2}\left(1-\frac{b}{a}\right)}\Gamma\left(\frac{b}{a}\right)J_{\frac{b}{a}-1}\left(\frac{2\sqrt{c}\sqrt{x}}{\sqrt{a}}\right)+c_2a^{\frac{1}{2}\left(1-\frac{b}{a}\right)-\frac{a-b}{a}}c^{\frac{a-b}{a}+\frac{1}{2}\left(\frac{b}{a}-1\right)}x^{\frac{a-b}{a}+\frac{1}{2}\left(\frac{b}{a}-1\right)}\Gamma\left(2-\right.\right.\right.$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 66

$$\left\{y(x)=x^{\frac{a-b}{2a}}\left(Y_{\frac{-a+b}{a}}\left(2\sqrt{\frac{c}{a}}\sqrt{x}\right)\_C2+J_{\frac{-a+b}{a}}\left(2\sqrt{\frac{c}{a}}\sqrt{x}\right)\_C1\right)\right\}$$

2.1141 ODE No. 1141

$$(3a+bx)y'(x)+axy''(x)+3by(x)=0$$

✓ **Mathematica** : cpu = 0.129106 (sec), leaf count = 70

$$\left\{\left\{y(x)\to \frac{c_2 e^{-\frac{bx}{a}}\left(b^2x^2\text{Ei}\left(\frac{bx}{a}\right)-ae^{\frac{bx}{a}}(a+bx)\right)}{2a^2x^2}+c_1e^{-\frac{bx}{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 55

$$\left\{y(x)=\frac{1}{x^2}\left(Ei\left(1,-\frac{bx}{a}\right)\mathrm{e}^{-\frac{bx}{a}}\_C2\,b^2x^2+\_C1\,\mathrm{e}^{-\frac{bx}{a}}x^2+a\_C2\,(bx+a)\right)\right\}$$

2.1142 ODE No. 1142

$$cy(x)\sqrt[5]{ax+b}+5(ax+b)y''(x)+8ay'(x)=0$$

✓ **Mathematica** : cpu = 0.0596197 (sec), leaf count = 108

$$\left\{\left\{y(x)\to \frac{3ac_2\sin\left(\frac{\sqrt{5}\sqrt{c}(ax+b)^{3/5}}{3a}\right)}{\sqrt{5}\sqrt{c}(ax+b)^{3/5}}+\frac{6ac_1\cos\left(\frac{\sqrt{5}\sqrt{c}(ax+b)^{3/5}}{3a}\right)}{\sqrt{5}\sqrt{c}(ax+b)^{3/5}}\right\}\right\}$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 53

$$\left\{y(x)=1\left(\_C2\,\cosh\left(\frac{1}{3\,a}(ax+b)^{\frac{3}{5}}\sqrt{-5\,c}\right)+\_C1\,\sinh\left(\frac{1}{3\,a}(ax+b)^{\frac{3}{5}}\sqrt{-5\,c}\right)\right)(ax+b)^{-\frac{3}{5}}\right\}$$

2.1143 ODE No. 1143

$$(a+bx)y'(x)+2axy''(x)+cy(x)=0$$

✓ **Mathematica** : cpu = 0.0460915 (sec), leaf count = 93

$$\left\{\left\{y(x)\to c_1e^{\frac{a\log(x)-bx}{2a}}U\left(-\frac{c-b}{b},\frac{3}{2},\frac{bx}{2a}\right)+c_2e^{\frac{a\log(x)-bx}{2a}}L^{\frac{1}{2}}_{\frac{c-b}{b}}\left(\frac{bx}{2a}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.101 (sec), leaf count = 57

$$\left\{y(x)=\sqrt{x}\mathrm{e}^{-\frac{bx}{2\,a}}\left(U\left(\frac{b-c}{b},\frac{3}{2},\frac{bx}{2\,a}\right)\_C2+M\left(\frac{b-c}{b},\frac{3}{2},\frac{bx}{2\,a}\right)\_C1\right)\right\}$$

2.1144 ODE No. 1144

$$(3a+bx)y'(x)+2axy''(x)+cy(x)=0$$

✓ **Mathematica** : cpu = 0.040256 (sec), leaf count = 88

$$\left\{\left\{y(x)\to c_1 e^{-\frac{bx}{2a}} U\left(-\frac{2c-3b}{2b},\frac{3}{2},\frac{bx}{2a}\right)+c_2 e^{-\frac{bx}{2a}} L^{\frac{1}{2}}_{\frac{2c-3b}{2b}}\left(\frac{bx}{2a}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.083 (sec), leaf count = 60

$$\left\{y(x)=\mathrm{e}^{-\frac{bx}{2a}}\left(U\left(\frac{3b-2c}{2b},\frac{3}{2},\frac{bx}{2a}\right)\_C2+M\left(\frac{3b-2c}{2b},\frac{3}{2},\frac{bx}{2a}\right)\_C1\right)\right\}$$

2.1145 ODE No. 1145

$$y(x)(\mathrm{a0}x+\mathrm{b0})+(\mathrm{a1}x+\mathrm{b1})y'(x)+(\mathrm{a2}x+\mathrm{b2})y''(x)=0$$

✓ **Mathematica** : cpu = 0.372927 (sec), leaf count = 398

$$\left\{\left\{y(x)\to c_1 U\left(-\frac{\mathrm{b2a1}^2-\mathrm{a2b1a1}-\sqrt{\mathrm{a1}^2-4\mathrm{a0a2}}\mathrm{b2a1}+2\mathrm{a2}^2\mathrm{b0}+\mathrm{a2}\sqrt{\mathrm{a1}^2-4\mathrm{a0a2}}\mathrm{b1}-2\mathrm{a0a2b2}-2\mathrm{a2}^2\sqrt{\mathrm{a1}^2}}{2\mathrm{a2}^2\sqrt{\mathrm{a1}^2-4\mathrm{a0a2}}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.2 (sec), leaf count = 248

$$\left\{y(x)=(a2\,x+b2)^{\frac{a1\,b2+a2^2-a2\,b1}{a2^2}}\,\mathrm{e}^{-\frac{x}{2\,a2}\left(\sqrt{-4\,a0\,a2+a1^2}+a1\right)}\left(U\left(\frac{1}{2\,a2^2}\left(\left(a1\,b2+2\,a2^2-a2\,b1\right)\sqrt{-4\,a0\,a2+a\right.\right.\right.\right.$$

2.1146 ODE No. 1146

$$x^2y''(x)-6y(x)=0$$

✓ **Mathematica** : cpu = 0.0231814 (sec), leaf count = 18

$$\left\{\left\{y(x)\to c_1x^3+\frac{c_2}{x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 15

$$\left\{y(x)=\frac{\_C2\,x^5+\_C1}{x^2}\right\}$$

2.1147 ODE No. 1147

$$x^2y''(x) - 12y(x) = 0$$

✓ **Mathematica** : cpu = 0.017944 (sec), leaf count = 18

$$\left\{\left\{y(x) \to c_1x^4 + \frac{c_2}{x^3}\right\}\right\}$$

✓ **Maple** : cpu = 0.008 (sec), leaf count = 15

$$\left\{y(x) = \frac{\_C1\,x^7 + \_C2}{x^3}\right\}$$

2.1148 ODE No. 1148

$$ay(x) + x^2y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0106916 (sec), leaf count = 77

$$\left\{\left\{y(x) \to c_1x^{\frac{1}{2}\left(\frac{1}{\sqrt{a}} - \frac{\sqrt{1-4a}}{\sqrt{a}}\right)\sqrt{a}} + c_2x^{\frac{1}{2}\left(\frac{\sqrt{1-4a}}{\sqrt{a}} + \frac{1}{\sqrt{a}}\right)\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 35

$$\left\{y(x) = \_C1\,x^{\frac{1}{2}+\frac{1}{2}\sqrt{1-4\,a}} + \_C2\,x^{\frac{1}{2}-\frac{1}{2}\sqrt{1-4\,a}}\right\}$$

2.1149 ODE No. 1149

$$y(x)(ax + b) + x^2y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0671639 (sec), leaf count = 212

$$\left\{\left\{y(x) \to c_2a^{\frac{1}{2}(\sqrt{1-4b}+1)-\frac{1}{2}\sqrt{1-4b}}x^{\frac{1}{2}(\sqrt{1-4b}+1)-\frac{1}{2}\sqrt{1-4b}}\Gamma\left(\sqrt{1-4b}+1\right)J_{\sqrt{1-4b}}\left(2\sqrt{a}\sqrt{x}\right) + c_1a^{\frac{1}{2}(1-\sqrt{1-4b})+\frac{1}{2}\sqrt{1-4b}}\right.\right.$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 45

$$\left\{y(x) = \sqrt{x}\left(Y_{\sqrt{1-4\,b}}\left(2\,\sqrt{a}\sqrt{x}\right)\_C2 + J_{\sqrt{1-4\,b}}\left(2\,\sqrt{a}\sqrt{x}\right)\_C1\right)\right\}$$

2.1150 ODE No. 1150

$$x^2 y''(x) + \left(x^2 - 2\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.0105527 (sec), leaf count = 53

$$\left\{\left\{y(x) \to \sqrt{\frac{2}{\pi}} c_2 \left(-\sin(x) - \frac{\cos(x)}{x}\right) + \sqrt{\frac{2}{\pi}} c_1 \left(\frac{\sin(x)}{x} - \cos(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.067 (sec), leaf count = 27

$$\left\{y(x) = \frac{(\_C1\, x + \_C2)\cos(x) + \sin(x)\,(\_C2\, x - \_C1)}{x}\right\}$$

2.1151 ODE No. 1151

$$x^2 y''(x) - \left(a x^2 + 2\right) y(x) = 0$$

✓ **Mathematica** : cpu = 0.0189164 (sec), leaf count = 129

$$\left\{\left\{y(x) \to \frac{\sqrt{\frac{2}{\pi}} c_2 \sqrt{x}\left(i \sinh\left(\sqrt{a}x\right) - \frac{i\cosh\left(\sqrt{a}x\right)}{\sqrt{a}x}\right)}{\sqrt{-i\sqrt{a}x}} + \frac{\sqrt{\frac{2}{\pi}} c_1 \sqrt{x}\left(\frac{\sinh\left(\sqrt{a}x\right)}{\sqrt{a}x} - \cosh\left(\sqrt{a}x\right)\right)}{\sqrt{-i\sqrt{a}x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.09 (sec), leaf count = 43

$$\left\{y(x) = \frac{1}{x}\left(\_C2\,\left(ax + \sqrt{a}\right)\mathrm{e}^{-\sqrt{a}x} - \_C1\,\mathrm{e}^{\sqrt{a}x}\left(ax - \sqrt{a}\right)\right)\right\}$$

2.1152 ODE No. 1152

$$\left(a^2 x^2 - 6\right) y(x) + x^2 y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0192588 (sec), leaf count = 114

$$\left\{\left\{y(x) \to \frac{\sqrt{\frac{2}{\pi}} c_1 \sqrt{x}\left(\frac{3\sin(ax)}{a^2x^2} - \sin(ax) - \frac{3\cos(ax)}{ax}\right)}{\sqrt{ax}} + \frac{\sqrt{\frac{2}{\pi}} c_2 \sqrt{x}\left(-\frac{3\cos(ax)}{a^2x^2} - \frac{3\sin(ax)}{ax} + \cos(ax)\right)}{\sqrt{ax}}\right\}\right\}$$

✓ **Maple** : cpu = 0.243 (sec), leaf count = 53

$$\left\{y(x) = \frac{\left(\_C1\, a^2x^2 + 3\,\_C2\, ax - 3\,\_C1\right)\cos(ax) + \sin(ax)\left(\_C2\, a^2x^2 - 3\,\_C1\, ax - 3\,\_C2\right)}{x^2}\right\}$$

2.1153 ODE No. 1153

$$y(x)\left(ax^2-(v-1)v\right)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0339143 (sec), leaf count = 56

$$\left\{\left\{y(x)\to c_1\sqrt{x}J_{\frac{1}{2}(2v-1)}\left(\sqrt{a}x\right)+c_2\sqrt{x}Y_{\frac{1}{2}(2v-1)}\left(\sqrt{a}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 31

$$\left\{y(x)=\sqrt{x}\left(Y_{v-\frac{1}{2}}\left(\sqrt{a}x\right)\_C2+J_{v-\frac{1}{2}}\left(\sqrt{a}x\right)\_C1\right)\right\}$$

2.1154 ODE No. 1154

$$y(x)\left(ax^2+bx+c\right)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.020756 (sec), leaf count = 88

$$\left\{\left\{y(x)\to c_1M_{-\frac{ib}{2\sqrt{a}},-\frac{1}{2}i\sqrt{4c-1}}\left(2i\sqrt{a}x\right)+c_2W_{-\frac{ib}{2\sqrt{a}},-\frac{1}{2}i\sqrt{4c-1}}\left(2i\sqrt{a}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 57

$$\left\{y(x)=\_C1\,M_{-\frac{i}{2}b\frac{1}{\sqrt{a}},\frac{1}{2}\sqrt{1-4\,c}}\left(2\,i\sqrt{a}x\right)+\_C2\,W_{-\frac{i}{2}b\frac{1}{\sqrt{a}},\frac{1}{2}\sqrt{1-4\,c}}\left(2\,i\sqrt{a}x\right)\right\}$$

2.1155 ODE No. 1155

$$y(x)\left(ax^k-(b-1)b\right)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0519865 (sec), leaf count = 225

$$\left\{\left\{y(x)\to c_1k^{-\frac{2(1-b)}{k}-\frac{2b}{k}+\frac{1}{k}}a^{\frac{1-b}{k}+\frac{1}{2}\left(\frac{2b}{k}-\frac{1}{k}\right)}\left(x^k\right)^{\frac{1-b}{k}+\frac{1}{2}\left(\frac{2b}{k}-\frac{1}{k}\right)}\Gamma\left(-\frac{2b}{k}+\frac{1}{k}+1\right)J_{\frac{1-2b}{k}}\left(\frac{2\sqrt{a}\sqrt{x^k}}{k}\right)+c_2k^{-1/k}a^{\frac{b}{k}+}\right.\right.$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 67

$$\left\{y(x)=\sqrt{x}\left(Y_{\frac{1}{k}\sqrt{(2\,b-1)^2}}\left(2\,\frac{\sqrt{a}x^{k/2}}{k}\right)\_C2+J_{\frac{1}{k}\sqrt{(2\,b-1)^2}}\left(2\,\frac{\sqrt{a}x^{k/2}}{k}\right)\_C1\right)\right\}$$

2.1156 ODE No. 1156

$$x^2 y''(x) + \frac{y(x)}{\log(x)} - e^x x(x\log(x)+2) = 0$$

✗ **Mathematica** : cpu = 0.204687 (sec), leaf count = 0 , could not solve

```
DSolve[-(E^x*x*(2 + x*Log[x])) + y[x]/Log[x] + x^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.136 (sec), leaf count = 71

$$\left\{y(x) = \ln(x)\_C2 - (Ei(1,-\ln(x))\ln(x)+x)\_C1 - \ln(x)\left(-\int \frac{(Ei(1,-\ln(x))\ln(x)+x)\,\mathrm{e}^x(2+x\ln(x))}{x}\right.\right.$$

2.1157 ODE No. 1157

$$ay'(x) + x^2 y''(x) - xy(x) = 0$$

✗ **Mathematica** : cpu = 0.495101 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\{y''(x)x^2 - y(x)x + ay'(x) = 0, y(1) = c_1, y'(1) = c_2\}\right)(x)\}\}$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + \frac{a\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{x^2} - \frac{\_Y(x)}{x}\right\},\{\_Y(x)\}\right)\right\}$$

2.1158 ODE No. 1158

$$-y(x)\left(ab + b^2x^2\right) + ay'(x) + x^2y''(x) = 0$$

✓ **Mathematica** : cpu = 14.3402 (sec), leaf count = 42

$$\left\{\left\{y(x) \to c_2 e^{bx}\int_1^x e^{\frac{a}{K[1]} - 2bK[1]}\,dK[1] + c_1 e^{bx}\right\}\right\}$$

✓ **Maple** : cpu = 0.224 (sec), leaf count = 178

$$\left\{y(x) = \sqrt{x}\left(\mathrm{e}^{bx} HeunD\left(-4\sqrt{2}\sqrt{ab}, -1 - 4\sqrt{2}\sqrt{ab}, 8\sqrt{2}\sqrt{ab}, -4\sqrt{2}\sqrt{ab}+1, 1\left(\sqrt{2}\sqrt{ab}x - a\right)\left(\sqrt{2}\sqrt{ab}x + a\right)\right.\right.\right.$$

2.1159 ODE No. 1159

$$-ax^2 + x^2 y''(x) + xy'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 0.0170874 (sec), leaf count = 44

$$\left\{\left\{y(x) \to \frac{ax^2}{3} + \frac{c_1\left(x^2+1\right)}{2x} + \frac{ic_2\left(x^2-1\right)}{2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 19

$$\left\{y(x) = x\_C2 + \frac{ax^2}{3} + \frac{\_C1}{x}\right\}$$

2.1160 ODE No. 1160

$$ay(x) + x^2 y''(x) + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0103261 (sec), leaf count = 30

$$\left\{\left\{y(x) \to c_2 \sin\left(\sqrt{a}\log(x)\right) + c_1 \cos\left(\sqrt{a}\log(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 23

$$\left\{y(x) = \_C1\ \sin\left(\sqrt{a}\ln\left(x\right)\right) + \_C2\ \cos\left(\sqrt{a}\ln\left(x\right)\right)\right\}$$

2.1161 ODE No. 1161

$$-(a+x)y(x) + x^2 y''(x) + xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0493982 (sec), leaf count = 78

$$\left\{\left\{y(x) \to (-1)^{-\sqrt{a}} c_1 \Gamma\left(1-2\sqrt{a}\right) I_{-2\sqrt{a}}\left(2\sqrt{x}\right) + (-1)^{\sqrt{a}} c_2 \Gamma\left(2\sqrt{a}+1\right) I_{2\sqrt{a}}\left(2\sqrt{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 31

$$\left\{y(x) = \_C1\ I_{2\sqrt{a}}\left(2\sqrt{x}\right) + \_C2\ K_{2\sqrt{a}}\left(2\sqrt{x}\right)\right\}$$

2.1162 ODE No. 1162

$$\left(x^2-v^2\right)y(x)+x^2y''(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0592002 (sec), leaf count = 18

$$\{\{y(x)\to c_1J_v(x)+c_2Y_v(x)\}\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 15

$$\{y(x)=\_C1\,J_v(x)+\_C2\,Y_v(x)\}$$

2.1163 ODE No. 1163

$$-f(x)+\left(x^2-v^2\right)y(x)+x^2y''(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.338569 (sec), leaf count = 70

$$\left\{\left\{y(x)\to J_v(x)\int_1^x-\frac{\pi f(K[1])Y_v(K[1])}{2K[1]}\,dK[1]+Y_v(x)\int_1^x\frac{\pi f(K[2])J_v(K[2])}{2K[2]}\,dK[2]+c_1J_v(x)+c_2Y_v(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 49

$$\left\{y(x)=-\frac{J_v(x)\pi}{2}\int\frac{Y_v(x)f(x)}{x}\,\mathrm{d}x+\frac{Y_v(x)\pi}{2}\int\frac{J_v(x)f(x)}{x}\,\mathrm{d}x+Y_v(x)\_C1+J_v(x)\_C2\right\}$$

2.1164 ODE No. 1164

$$y(x)\left(lx^2-v^2\right)+x^2y''(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.021841 (sec), leaf count = 30

$$\left\{\left\{y(x)\to c_1J_v\left(\sqrt{l}x\right)+c_2Y_v\left(\sqrt{l}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.025 (sec), leaf count = 23

$$\left\{y(x)=\_C1\,J_v\left(\sqrt{l}x\right)+\_C2\,Y_v\left(\sqrt{l}x\right)\right\}$$

2.1165 ODE No. 1165

$$(a+x)y'(x)+x^2y''(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0503245 (sec), leaf count = 37

$$\left\{\left\{y(x)\to \frac{c_1(a+x)}{a+1}-\frac{c_2xe^{a/x}}{a^2(a+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 19

$$\left\{y(x)=(x+a)\_C1+\_C2\,x\mathrm{e}^{\frac{a}{x}}\right\}$$

2.1166 ODE No. 1166

$$-3x^3+x^2y''(x)-xy'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0142971 (sec), leaf count = 23

$$\left\{\left\{y(x)\to c_1x+c_2x\log(x)+\frac{3x^3}{4}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 21

$$\left\{y(x)=\frac{x\left(4\,\ln\left(x\right)\_C1+3\,x^2+4\,\_C2\right)}{4}\right\}$$

2.1167 ODE No. 1167

$$y(x)\left(ax^m+b\right)+x^2y''(x)-xy'(x)=0$$

✓ **Mathematica** : cpu = 0.08278 (sec), leaf count = 326

$$\left\{\left\{y(x)\to c_1m^{-\frac{2(m-i\sqrt{b-1}m)}{m^2}-\frac{2i\sqrt{b-1}}{m}}a^{\frac{m-i\sqrt{b-1}m}{m^2}+\frac{i\sqrt{b-1}}{m}}(x^m)^{\frac{m-i\sqrt{b-1}m}{m^2}+\frac{i\sqrt{b-1}}{m}}\Gamma\left(1-\frac{2i\sqrt{b-1}}{m}\right)J_{-\frac{2i\sqrt{b-1}}{m}}\left(\frac{2\sqrt{a}\sqrt{x^m}}{m}\right.\right.\right.$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 63

$$\left\{y(x)=x\left(Y_{2\,\frac{\sqrt{1-b}}{m}}\left(2\,\frac{\sqrt{a}x^{m/2}}{m}\right)\_C2+J_{2\,\frac{\sqrt{1-b}}{m}}\left(2\,\frac{\sqrt{a}x^{m/2}}{m}\right)\_C1\right)\right\}$$

2.1168 ODE No. 1168

$$x^2 y''(x) + 2xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.00574592 (sec), leaf count = 15

$$\left\{\left\{y(x) \to c_2 - \frac{c_1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.009 (sec), leaf count = 11

$$\left\{y(x) = \_C1 + \frac{\_C2}{x}\right\}$$

2.1169 ODE No. 1169

$$y(x)\left(ax - b^2\right) + x^2 y''(x) + 2xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0717979 (sec), leaf count = 236

$$\left\{\left\{y(x) \to c_1 a^{\frac{1}{2}\left(-\sqrt{4b^2+1}-1\right)+\frac{1}{2}\sqrt{4b^2+1}} x^{\frac{1}{2}\left(-\sqrt{4b^2+1}-1\right)+\frac{1}{2}\sqrt{4b^2+1}} \Gamma\left(1-\sqrt{4b^2+1}\right) J_{-\sqrt{4b^2+1}}\left(2\sqrt{a}\sqrt{x}\right) + c_2 a^{\frac{1}{2}\left(\sqrt{4b^2+\right.}\right.$$

✓ **Maple** : cpu = 0.025 (sec), leaf count = 49

$$\left\{y(x) = 1\left(\_C2\, Y_{\sqrt{4\,b^2+1}}\left(2\,\sqrt{a}\sqrt{x}\right) + \_C1\, J_{\sqrt{4\,b^2+1}}\left(2\,\sqrt{a}\sqrt{x}\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1170 ODE No. 1170

$$y(x)\left(ax^2 + b\right) + x^2 y''(x) + 2xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.023903 (sec), leaf count = 58

$$\left\{\left\{y(x) \to c_1 j_{\frac{1}{2}\left(\sqrt{1-4b}-1\right)}\left(\sqrt{a}x\right) + c_2 y_{\frac{1}{2}\left(\sqrt{1-4b}-1\right)}\left(\sqrt{a}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 43

$$\left\{y(x) = 1\left(\_C2\, Y_{\frac{1}{2}\sqrt{1-4\,b}}\left(\sqrt{a}x\right) + \_C1\, J_{\frac{1}{2}\sqrt{1-4\,b}}\left(\sqrt{a}x\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1171 ODE No. 1171

$$y(x)\left(ax+lx^2-n(n+1)\right)+x^2y''(x)+2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0539711 (sec), leaf count = 142

$$\left\{\left\{y(x)\to c_1e^{n\log(x)-i\sqrt{l}x}U\left(\frac{i\left(a-2i\sqrt{l}n-2i\sqrt{l}\right)}{2\sqrt{l}},2n+2,2i\sqrt{l}x\right)+c_2e^{n\log(x)-i\sqrt{l}x}L^{2n+1}_{-\frac{i\left(a-2i\sqrt{l}n-2i\sqrt{l}\right)}{2\sqrt{l}}}\left(2i\sqrt{l}x\right)\right.\right.$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 49

$$\left\{y(x)=\frac{1}{x}\left(\_C1\,M_{-\frac{i}{2}a\frac{1}{\sqrt{l}},n+\frac{1}{2}}\left(2\,i\sqrt{l}x\right)+\_C2\,W_{-\frac{i}{2}a\frac{1}{\sqrt{l}},n+\frac{1}{2}}\left(2\,i\sqrt{l}x\right)\right)\right\}$$

2.1172 ODE No. 1172

$$ay(x)+x^2y''(x)+2(x-1)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0576688 (sec), leaf count = 158

$$\left\{\left\{y(x)\to 2^{\frac{1}{2}\left(1-\sqrt{1-4a}\right)}c_1\left(\frac{1}{x}\right)^{\frac{1}{2}\left(1-\sqrt{1-4a}\right)}\,{}_1F_1\left(\frac{1}{2}-\frac{1}{2}\sqrt{1-4a};1-\sqrt{1-4a};-\frac{2}{x}\right)+2^{\frac{1}{2}\left(\sqrt{1-4a}+1\right)}c_2\left(\frac{1}{x}\right)^{\frac{1}{2}\left(\sqrt{1-4a}\right.}\right.\right.$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 47

$$\left\{y(x)=\mathrm{e}^{-x^{-1}}\sqrt{x^{-1}}\left(K_{\frac{1}{2}\sqrt{1-4\,a}}(x^{-1})\_C2+I_{\frac{1}{2}\sqrt{1-4\,a}}(x^{-1})\_C1\right)\right\}$$

2.1173 ODE No. 1173

$$2(a+x)y'(x)-(b-1)by(x)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0655256 (sec), leaf count = 74

$$\left\{\left\{y(x)\to(-2)^{1-b}c_1a^{1-b}\left(\frac{1}{x}\right)^{1-b}\,{}_1F_1\left(1-b;2-2b;\frac{2a}{x}\right)+(-2)^bc_2a^b\left(\frac{1}{x}\right)^b\,{}_1F_1\left(b;2b;\frac{2a}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.076 (sec), leaf count = 37

$$\left\{y(x)=1\mathrm{e}^{\frac{a}{x}}\left(K_{b-\frac{1}{2}}\left(\frac{a}{x}\right)\_C2+I_{b-\frac{1}{2}}\left(\frac{a}{x}\right)\_C1\right)\frac{1}{\sqrt{x}}\right\}$$

2.1174 ODE No. 1174

$$x^5(-\log(x)) + x^2y''(x) - 2xy'(x) + 2y(x) = 0$$

✓ **Mathematica** : cpu = 0.0192696 (sec), leaf count = 33

$$\left\{\left\{y(x) \to c_2x^2 + c_1x + \frac{1}{144}\left(12x^5\log(x) - 7x^5\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 25

$$\left\{y(x) = \frac{x^5\ln(x)}{12} - \frac{7x^5}{144} + x^2\_C1 + x\_C2\right\}$$

2.1175 ODE No. 1175

$$-\left(ax^2 + 12a + 4\right)\cos(x) + x^2y''(x) - 2xy'(x) - 4y(x) - x\sin(x) = 0$$

✓ **Mathematica** : cpu = 0.175485 (sec), leaf count = 38

$$\left\{\left\{y(x) \to \frac{-2a\sin(x) - ax\cos(x) - \sin(x)}{x} + c_2x^4 + \frac{c_1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 29

$$\left\{y(x) = \frac{(-2a-1)\sin(x) + x^5\_C2 - ax\cos(x) + \_C1}{x}\right\}$$

2.1176 ODE No. 1176

$$x^2y''(x) + \left(x^2+2\right)y(x) - 2xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0182895 (sec), leaf count = 33

$$\left\{\left\{y(x) \to c_1e^{-ix}x - \frac{1}{2}ic_2e^{ix}x\right\}\right\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 15

$$\{y(x) = x(\cos(x)\_C2 + \sin(x)\_C1)\}$$

2.1177 ODE No. 1177

$$x^2y''(x)+\left(x^2+2\right)y'(x)+x^2(-\sec(x))-2xy'(x)=0$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.071 (sec), leaf count = 34

$$\left\{y(x)=\left(-\cos\left(x\right)\int\frac{\sin\left(x\right)}{\cos\left(x\right)x}\,\mathrm{d}x+\cos\left(x\right)\_C1+\sin\left(x\right)\left(\_C2+\ln\left(x\right)\right)\right)x\right\}$$

2.1178 ODE No. 1178

$$x^3(-\sec(x))+x^2y''(x)+\left(x^2+2\right)y(x)-2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0585209 (sec), leaf count = 74

$$\left\{\left\{y(x)\to c_1e^{-ix}x-\frac{1}{2}ic_2e^{ix}x+\frac{1}{2}e^{-ix}x\left(e^{2ix}\log\left(1+e^{-2ix}\right)+\log\left(1+e^{2ix}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 23

$$\left\{y(x)=\left(\cos\left(x\right)\ln\left(\cos\left(x\right)\right)+\cos\left(x\right)\_C1+\sin\left(x\right)\left(x+\_C2\right)\right)x\right\}$$

2.1179 ODE No. 1179

$$\left(a^2x^2+2\right)y(x)+x^2y''(x)-2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0415951 (sec), leaf count = 53

$$\left\{\left\{y(x)\to c_1xe^{-\sqrt{-a^2}x}+\frac{c_2xe^{\sqrt{-a^2}x}}{2\sqrt{-a^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 19

$$\left\{y(x)=x(\cos\left(ax\right)\_C2+\sin\left(ax\right)\_C1)\right\}$$

2.1180 ODE No. 1180

$$-f(x)+\left(-v^2+x^2+1\right)y(x)+x^2y''(x)+3xy'(x)=0$$

✓ **Mathematica** : cpu = 0.21898 (sec), leaf count = 73

$$\left\{\left\{y(x)\to \frac{J_v(x)\int_1^x -\frac{1}{2}\pi f(K[1])Y_v(K[1])\,dK[1]+Y_v(x)\int_1^x \frac{1}{2}\pi f(K[2])J_v(K[2])\,dK[2]}{x}+\frac{c_1J_v(x)}{x}+\frac{c_2Y_v(x)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.047 (sec), leaf count = 49

$$\left\{y(x)=\frac{-J_v(x)\pi\int Y_v(x)f(x)\,\mathrm{d}x+Y_v(x)\pi\int J_v(x)f(x)\,\mathrm{d}x+2\,Y_v(x)\_C1+2\,J_v(x)\_C2}{2\,x}\right\}$$

2.1181 ODE No. 1181

$$x^2y''(x)+(3x-1)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0290249 (sec), leaf count = 37

$$\left\{\left\{y(x)\to \frac{c_1e^{-1/x}}{x}-\frac{c_2e^{-1/x}\mathrm{Ei}\left(\frac{1}{x}\right)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 25

$$\left\{y(x)=\frac{1}{x\mathrm{e}^{x^{-1}}}\left(\_C1\,Ei\left(1,-x^{-1}\right)+\_C2\right)\right\}$$

2.1182 ODE No. 1182

$$x^2y''(x)-3xy'(x)+4y(x)-5x=0$$

✓ **Mathematica** : cpu = 0.0172515 (sec), leaf count = 24

$$\left\{\left\{y(x)\to c_1x^2+2c_2x^2\log(x)+5x\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 20

$$\left\{y(x)=x^2\_C2+x^2\ln(x)\_C1+5\,x\right\}$$

2.1183 ODE No. 1183

$$x^2 y''(x) + x^2(-\log(x)) - 3xy'(x) - 5y(x) = 0$$

✓ **Mathematica** : cpu = 0.0278269 (sec), leaf count = 27

$$\left\{\left\{y(x) \to c_1 x^5 + \frac{c_2}{x} - \frac{1}{9}x^2 \log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 22

$$\left\{y(x) = x^5 \_C2 + \frac{\_C1}{x} - \frac{x^2 \ln(x)}{9}\right\}$$

2.1184 ODE No. 1184

$$-x^4 + x^2 y''(x) + x^2 - 4xy'(x) + 6y(x) = 0$$

✓ **Mathematica** : cpu = 0.0199038 (sec), leaf count = 38

$$\left\{\left\{y(x) \to c_2 x^3 + c_1 x^2 + \frac{1}{2}\left(x^4 + 2x^2 + 2x^2 \log(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 25

$$\left\{y(x) = \frac{x^2\left(2\,x\_C1 + x^2 + 2\,\ln(x) + 2\,\_C2 + 2\right)}{2}\right\}$$

2.1185 ODE No. 1185

$$-\left(2x^3 - 4\right) y(x) + x^2 y''(x) + 5xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0396823 (sec), leaf count = 67

$$\left\{\left\{y(x) \to \frac{3\sqrt[3]{6}c_2 K_0\left(\frac{2}{3}\sqrt{2}x^{3/2}\right)}{x^2} - \frac{3\sqrt[3]{-3}c_1 I_0\left(\frac{2}{3}\sqrt{2}x^{3/2}\right)}{2^{2/3}x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 33

$$\left\{y(x) = \frac{1}{x^2}\left(\_C2\, K_0\left(\frac{2\sqrt{2}}{3}x^{\frac{3}{2}}\right) + \_C1\, I_0\left(\frac{2\sqrt{2}}{3}x^{\frac{3}{2}}\right)\right)\right\}$$

2.1186 ODE No. 1186

$$x^3(-\sin(x)) + x^2 y''(x) - 5xy'(x) + 8y(x) = 0$$

✓ **Mathematica** : cpu = 0.0345453 (sec), leaf count = 42

$$\left\{\left\{y(x) \to c_2 x^4 + c_1 x^2 + \frac{1}{2}\left(x^4 \text{Ci}(x) - x^3 \sin(x) + x^2 \cos(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.024 (sec), leaf count = 36

$$\left\{y(x) = \frac{x^4 Ci(x)}{2} - \frac{\sin(x) x^3}{2} + \frac{x^2\left(2\_C1\, x^2 + 2\_C2 + \cos(x)\right)}{2}\right\}$$

2.1187 ODE No. 1187

$$axy'(x) + by(x) + x^2 y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0131173 (sec), leaf count = 99

$$\left\{\left\{y(x) \to c_1 x^{\frac{1}{2}\sqrt{b}\left(-\frac{\sqrt{a^2-2a-4b+1}}{\sqrt{b}}-\frac{a-1}{\sqrt{b}}\right)} + c_2 x^{\frac{1}{2}\sqrt{b}\left(\frac{\sqrt{a^2-2a-4b+1}}{\sqrt{b}}-\frac{a-1}{\sqrt{b}}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.012 (sec), leaf count = 53

$$\left\{y(x) = \_C1\, x^{-\frac{a}{2}+\frac{1}{2}+\frac{1}{2}\sqrt{a^2-2a-4b+1}} + \_C2\, x^{-\frac{a}{2}+\frac{1}{2}-\frac{1}{2}\sqrt{a^2-2a-4b+1}}\right\}$$

2.1188 ODE No. 1188

$$(ax+b)y'(x) + cy(x) + x^2 y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0901639 (sec), leaf count = 266

$$\left\{\left\{y(x) \to c_1 i^{-\sqrt{a^2-2a-4c+1}+a-1} b^{\frac{1}{2}\left(-\sqrt{a^2-2a-4c+1}+a-1\right)} \left(\frac{1}{x}\right)^{\frac{1}{2}\left(-\sqrt{a^2-2a-4c+1}+a-1\right)} {}_1F_1\left(\frac{a}{2} - \frac{1}{2}\sqrt{a^2-2a-4c+\right.\right.\right.$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 114

$$\left\{y(x) = x^{-\frac{1}{2}\sqrt{a^2-2a-4c+1}-\frac{a}{2}+\frac{1}{2}}\left(U\left(-\frac{1}{2}+\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{a}{2}, 1+\sqrt{a^2-2a-4c+1}, \frac{b}{x}\right)\_C2 + M\left(-\right.\right.\right.$$

2.1189 ODE No. 1189

$$axy'(x)+y(x)\left(bx^m+c\right)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0728327 (sec), leaf count = 445

$$\left\{\left\{y(x)\to c_1m^{-\frac{-\sqrt{a^2-2a-4c+1}-a+1}{m}-\frac{\sqrt{a^2-2a-4c+1}}{m}}b^{\frac{-\sqrt{a^2-2a-4c+1}-a+1}{2m}+\frac{\sqrt{a^2-2a-4c+1}}{2m}}\left(x^m\right)^{\frac{-\sqrt{a^2-2a-4c+1}-a+1}{2m}+\frac{\sqrt{a^2-2a-4c+1}}{2m}}\mathrm{I}\right.\right.$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 79

$$\left\{y(x)=x^{-\frac{a}{2}+\frac{1}{2}}\left(Y_{\frac{1}{m}\sqrt{a^2-2\,a-4\,c+1}}\left(2\,\frac{\sqrt{b}x^{m/2}}{m}\right)\_C2+J_{\frac{1}{m}\sqrt{a^2-2\,a-4\,c+1}}\left(2\,\frac{\sqrt{b}x^{m/2}}{m}\right)\_C1\right)\right\}$$

2.1190 ODE No. 1190

$$y(x)(ax+b)+x^2y''(x)+x^2y'(x)=0$$

✓ **Mathematica** : cpu = 0.0313688 (sec), leaf count = 122

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{2}\left(\left(\sqrt{1-4b}+1\right)\log(x)-2x\right)}U\left(\frac{1}{2}\left(-2a+\sqrt{1-4b}+1\right),\sqrt{1-4b}+1,x\right)+c_2e^{\frac{1}{2}\left(\left(\sqrt{1-4b}+1\right)\log(x)-2x\right)}L_{\frac{1}{2}(2a}^{\sqrt{1-}}\right.\right.$$

✓ **Maple** : cpu = 0.09 (sec), leaf count = 38

$$\left\{y(x)=\mathrm{e}^{-\frac{x}{2}}\left(W_{a,\,\frac{1}{2}\sqrt{1-4\,b}}(x)\_C2+M_{a,\,\frac{1}{2}\sqrt{1-4\,b}}(x)\_C1\right)\right\}$$

2.1191 ODE No. 1191

$$x^2y''(x)+x^2y'(x)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.0103975 (sec), leaf count = 110

$$\left\{\left\{y(x)\to\frac{2c_2e^{\frac{1}{2}(\log(x)-x)}\left(i\sinh\left(\frac{x}{2}\right)-\frac{2i\cosh\left(\frac{x}{2}\right)}{x}\right)}{\sqrt{\pi}\sqrt{-ix}}+\frac{2c_1e^{\frac{1}{2}(\log(x)-x)}\left(\frac{2\sinh\left(\frac{x}{2}\right)}{x}-\cosh\left(\frac{x}{2}\right)\right)}{\sqrt{\pi}\sqrt{-ix}}\right\}\right\}$$

✓ **Maple** : cpu = 0.015 (sec), leaf count = 23

$$\left\{y(x)=\frac{\_C2\,(x+2)\,\mathrm{e}^{-x}+\_C1\,(x-2)}{x}\right\}$$

2.1192 ODE No. 1192

$$x^2y''(x) + \left(x^2-1\right)y'(x) - y(x) = 0$$

✓ **Mathematica** : cpu = 11.0874 (sec), leaf count = 39

$$\left\{\left\{y(x) \to c_2 e^{-x}\int_1^x e^{K[1]-\frac{1}{K[1]}}\,dK[1] + c_1 e^{-x}\right\}\right\}$$

✓ **Maple** : cpu = 0.132 (sec), leaf count = 51

$$\left\{y(x) = \sqrt{x}\left(HeunD\left(-4,3,-8,5,\frac{x-1}{1+x}\right)\mathrm{e}^{-x^{-1}}\_C2 + \mathrm{e}^{-x}HeunD\left(4,3,-8,5,\frac{x-1}{1+x}\right)\_C1\right)\right\}$$

2.1193 ODE No. 1193

$$x^2y''(x) + (x+1)xy'(x) + (x-9)y(x) = 0$$

✓ **Mathematica** : cpu = 0.048803 (sec), leaf count = 44

$$\left\{\left\{y(x) \to \frac{c_1((x-8)x+20)}{x^3} - \frac{c_2 e^{-x}\left(x^3+9x^2+36x+60\right)}{x^3}\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 38

$$\left\{y(x) = \frac{\_C2\left(x^3+9\,x^2+36\,x+60\right)\mathrm{e}^{-x} + \_C1\left(x^2-8\,x+20\right)}{x^3}\right\}$$

2.1194 ODE No. 1194

$$x^2y''(x) + (x+1)xy'(x) + (3x-1)y(x) = 0$$

✓ **Mathematica** : cpu = 0.0521584 (sec), leaf count = 65

$$\left\{\left\{y(x) \to c_1 e^{-x}(x-3)x - \frac{c_2 e^{-x}\left(x^3(-\mathrm{Ei}(x)) + 3x^2\mathrm{Ei}(x) + e^x x^2 - 2e^x x - e^x\right)}{6x}\right\}\right\}$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 48

$$\left\{y(x) = \frac{x^2\_C2\,\mathrm{e}^{-x}(x-3)\,Ei(1,-x) + \_C1\,x^2(x-3)\,\mathrm{e}^{-x} + \_C2\left(x^2-2\,x-1\right)}{x}\right\}$$

2.1195 ODE No. 1195

$$x^2y''(x)+(x+3)xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0287872 (sec), leaf count = 80

$$\left\{\left\{y(x)\to c_1U\left(2+\sqrt{2},1+2\sqrt{2},x\right)e^{\left(\sqrt{2}-1\right)\log(x)-x}+c_2L_{-2-\sqrt{2}}^{2\sqrt{2}}(x)e^{\left(\sqrt{2}-1\right)\log(x)-x}\right\}\right\}$$

✓ **Maple** : cpu = 0.12 (sec), leaf count = 93

$$\left\{y(x)=-1\left(-\_C1\left(\sqrt{2}+x+1\right)I_{-\frac{1}{2}+\sqrt{2}}\left(\frac{x}{2}\right)-\_C1\left(x-\sqrt{2}+1\right)I_{\frac{1}{2}+\sqrt{2}}\left(\frac{x}{2}\right)+\left(\left(-\sqrt{2}-x-1\right)K_{-\frac{1}{2}+\sqrt{2}}\left(\frac{x}{2}\right)\right.\right.\right.$$

2.1196 ODE No. 1196

$$x^2y''(x)-(x-1)xy'(x)+(x-1)y(x)=0$$

✓ **Mathematica** : cpu = 0.0255963 (sec), leaf count = 37

$$\left\{\left\{y(x)\to\frac{c_2\left(x^2\mathrm{Ei}(x)-e^xx-e^x\right)}{2x}+c_1x\right\}\right\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 31

$$\left\{y(x)=\frac{Ei(1,-x)\_C2\,x^2+\_C2\,(1+x)\,\mathrm{e}^x+\_C1\,x^2}{x}\right\}$$

2.1197 ODE No. 1197

$$-(a+x)y(x)+x^2y''(x)-\left(x^2-2x\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.019317 (sec), leaf count = 78

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{2}(x-\log(x))}J_{\frac{1}{2}\sqrt{4a+1}}\left(-\frac{ix}{2}\right)+c_2e^{\frac{1}{2}(x-\log(x))}Y_{\frac{1}{2}\sqrt{4a+1}}\left(-\frac{ix}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.041 (sec), leaf count = 43

$$\left\{y(x)=1\mathrm{e}^{\frac{x}{2}}\left(K_{\frac{1}{2}\sqrt{4\,a+1}}\left(\frac{x}{2}\right)\_C2+I_{\frac{1}{2}\sqrt{4\,a+1}}\left(\frac{x}{2}\right)\_C1\right)\frac{1}{\sqrt{x}}\right\}$$

2.1198 ODE No. 1198

$$x^2y''(x) - \left(x^2 - 2x\right)y'(x) - (3x+2)y(x) = 0$$

✓ **Mathematica** : cpu = 0.029599 (sec), leaf count = 41

$$\left\{\left\{y(x) \to c_1 e^x x - \frac{c_2\left(e^x x^3 \text{Ei}(-x) + x^2 - x + 2\right)}{6x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 37

$$\left\{y(x) = \frac{\mathrm{e}^x Ei(1,x)\_C2\, x^3 + \_C1\, x^3 \mathrm{e}^x - \_C2\left(x^2 - x + 2\right)}{x^2}\right\}$$

2.1199 ODE No. 1199

$$x^2y''(x) - (x+4)xy'(x) + 4y(x) = 0$$

✓ **Mathematica** : cpu = 0.0133269 (sec), leaf count = 41

$$\left\{\left\{y(x) \to c_2 e^x x^4 - \frac{1}{6}c_1 x\left(e^x x^3 \text{Ei}(-x) + x^2 - x + 2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 35

$$\left\{y(x) = \left(\mathrm{e}^x Ei(1,x)\_C2\, x^3 + \_C1\, x^3 \mathrm{e}^x - \_C2\left(x^2 - x + 2\right)\right) x\right\}$$

2.1200 ODE No. 1200

$$-(v-1)vy(x) + x^2y''(x) + 2x^2y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0221104 (sec), leaf count = 62

$$\left\{\left\{y(x) \to c_1 e^{-x}\sqrt{x}J_{\frac{1}{2}(2v-1)}(-ix) + c_2 e^{-x}\sqrt{x}Y_{\frac{1}{2}(2v-1)}(-ix)\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 27

$$\left\{y(x) = \sqrt{x}\mathrm{e}^{-x}\left(K_{v-\frac{1}{2}}(x)\_C2 + I_{v-\frac{1}{2}}(x)\_C1\right)\right\}$$

2.1201 ODE No. 1201

$$x^2y''(x)+(2x+1)xy'(x)-4y(x)=0$$

✓ **Mathematica** : cpu = 0.055067 (sec), leaf count = 44

$$\left\{\left\{y(x)\to \frac{c_1e^{-2x}(2x+3)}{2x^2}+\frac{c_2\left(2x^2-4x+3\right)}{4x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 34

$$\left\{y(x)=\frac{\_C1\left(2x^2-4x+3\right)}{x^2}+\frac{\_C2\,\mathrm{e}^{-2x}(2x+3)}{x^2}\right\}$$

2.1202 ODE No. 1202

$$x^2y''(x)-2(x+1)xy'(x)+2(x+1)y(x)=0$$

✓ **Mathematica** : cpu = 0.0154628 (sec), leaf count = 22

$$\left\{\left\{y(x)\to c_1x+\frac{1}{2}c_2e^{2x}x\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 14

$$\left\{y(x)=x\left(\mathrm{e}^{2x}\_C2+\_C1\right)\right\}$$

2.1203 ODE No. 1203

$$ax^2y'(x)+x^2y''(x)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.022529 (sec), leaf count = 124

$$\left\{\left\{y(x)\to \frac{2c_2e^{\frac{1}{2}(\log(x)-ax)}\left(i\sinh\left(\frac{ax}{2}\right)-\frac{2i\cosh\left(\frac{ax}{2}\right)}{ax}\right)}{\sqrt{\pi}\sqrt{-iax}}+\frac{2c_1e^{\frac{1}{2}(\log(x)-ax)}\left(\frac{2\sinh\left(\frac{ax}{2}\right)}{ax}-\cosh\left(\frac{ax}{2}\right)\right)}{\sqrt{\pi}\sqrt{-iax}}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 28

$$\left\{y(x)=\frac{\_C2\,(ax+2)\,\mathrm{e}^{-ax}+\_C1\,(ax-2)}{x}\right\}$$

2.1204 ODE No. 1204

$$x^2(a+2b)y'(x)+y(x)\left(bx^2(a+b)-2\right)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.020851 (sec), leaf count = 132

$$\left\{\left\{y(x)\to \frac{2c_2e^{\frac{1}{2}(-ax-2bx+\log(x))}\left(i\sinh\left(\frac{ax}{2}\right)-\frac{2i\cosh\left(\frac{ax}{2}\right)}{ax}\right)}{\sqrt{\pi}\sqrt{-iax}}+\frac{2c_1e^{\frac{1}{2}(-ax-2bx+\log(x))}\left(\frac{2\sinh\left(\frac{ax}{2}\right)}{ax}-\cosh\left(\frac{ax}{2}\right)\right)}{\sqrt{\pi}\sqrt{-iax}}\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 35

$$\left\{y(x)=\frac{\_C2\,(ax+2)\,\mathrm{e}^{-(a+b)x}+\_C1\,\mathrm{e}^{-bx}(ax-2)}{x}\right\}$$

2.1205 ODE No. 1205

$$ax^2y'(x)+f(x)y(x)+x^2y''(x)=0$$

✗ **Mathematica** : cpu = 0.210026 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + a*x^2*Derivative[1][y][x] + x^2*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{f(x)\_Y(x)}{x^2}+a\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1206 ODE No. 1206

$$y(x)\left(abx+cx^2+d\right)+x(2ax+b)y'(x)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.115223 (sec), leaf count = 120

$$\left\{\left\{y(x)\to c_1e^{\frac{1}{2}(-2ax-(b-1)\log(x))}J_{\frac{1}{2}\sqrt{b^2-2b-4d+1}}\left(-i\sqrt{a^2-c}x\right)+c_2e^{\frac{1}{2}(-2ax-(b-1)\log(x))}Y_{\frac{1}{2}\sqrt{b^2-2b-4d+1}}\left(-i\sqrt{a^2-c}\right.\right.\right.$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 76

$$\left\{y(x)=\mathrm{e}^{-ax}x^{-\frac{b}{2}+\frac{1}{2}}\left(Y_{\frac{1}{2}\sqrt{b^2-2\,b-4\,d+1}}\left(\sqrt{-a^2+c}x\right)\_C2+J_{\frac{1}{2}\sqrt{b^2-2\,b-4\,d+1}}\left(\sqrt{-a^2+c}x\right)\_C1\right)\right\}$$

2.1207 ODE No. 1207

$$x(ax+b)y'(x)+y(x)\left(\text{a1}x^2+\text{b1}x+\text{c1}\right)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.123812 (sec), leaf count = 294

$$\left\{\left\{y(x)\to c_1U\left(-\frac{-ab+2\text{b1}-\sqrt{a^2-4\text{a1}}-\sqrt{a^2-4\text{a1}}\sqrt{b^2-2b-4\text{c1}+1}}{2\sqrt{a^2-4\text{a1}}},\sqrt{b^2-2b-4\text{c1}+1}+1,\sqrt{a^2-4\text{a1}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.221 (sec), leaf count = 110

$$\left\{y(x)=\mathrm{e}^{-\frac{ax}{2}}x^{-\frac{b}{2}}\left(W_{-\frac{ab-2\,b1}{2}\frac{1}{\sqrt{a^2-4\,a1}},\frac{1}{2}\sqrt{b^2-2\,b-4\,c1+1}}\left(\sqrt{a^2-4\,a1}\,x\right)\_C2+M_{-\frac{ab-2\,b1}{2}\frac{1}{\sqrt{a^2-4\,a1}},\frac{1}{2}\sqrt{b^2-2\,b-4\,c1+1}}\left(\sqrt{}\right.\right.\right.$$

2.1208 ODE No. 1208

$$x^3y'(x)+x^2y''(x)+\left(x^2-2\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0402662 (sec), leaf count = 59

$$\left\{\left\{y(x)\to\frac{c_2e^{-\frac{x^2}{2}}\left(\sqrt{2\pi}e^{\frac{x^2}{2}}\operatorname{erf}\left(\frac{x}{\sqrt{2}}\right)-2x\right)}{2x}+\frac{c_1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 35

$$\left\{y(x)=\frac{1}{x}\left(\sqrt{\pi}\sqrt{2}Erf\left(\frac{\sqrt{2}x}{2}\right)\_C2-2\,\mathrm{e}^{-1/2\,x^2}\_C2\,x+\_C1\right)\right\}$$

2.1209 ODE No. 1209

$$x^2y''(x)+\left(x^2+2\right)xy'(x)+\left(x^2-2\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0226077 (sec), leaf count = 67

$$\left\{\left\{y(x)\to\frac{c_1e^{-\frac{x^2}{2}}\left(e^{\frac{x^2}{2}}x-\sqrt{\frac{\pi}{2}}\operatorname{erfi}\left(\frac{x}{\sqrt{2}}\right)\right)}{x^2}+\frac{c_2e^{-\frac{x^2}{2}}}{x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 41

$$\left\{y(x)=\frac{1}{x^2}\left(\left(-Erf\left(\frac{i}{2}\sqrt{2}x\right)\pi\_C2+\_C1\right)\mathrm{e}^{-\frac{x^2}{2}}+i\sqrt{\pi}\sqrt{2}\_C2\,x\right)\right\}$$

2.1210 ODE No. 1210

$$y(x)\left(a((-1)^n-1)+2nx^2\right)-2x\left(x^2-a\right)y'(x)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.270471 (sec), leaf count = 252

$$\left\{\left\{y(x)\to c_1(-1)^{\frac{1}{4}\left(-\sqrt{4a^2-4a(-1)^n+1}-2a+1\right)}x^{\frac{1}{2}\left(-\sqrt{4a^2-4a(-1)^n+1}-2a+1\right)}\,{}_1F_1\left(-\frac{a}{2}-\frac{n}{2}-\frac{1}{4}\sqrt{4a^2-4(-1)^na+1}+\right.\right.$$

✓ **Maple** : cpu = 0.679 (sec), leaf count = 81

$$\left\{y(x)=\mathrm{e}^{\frac{x^2}{2}}x^{-\frac{1}{2}-a}\left(M_{\frac{n}{2}+\frac{a}{2}+\frac{1}{4},\frac{1}{4}\sqrt{1-4(-1)^na+4a^2}}\left(x^2\right)\_C1+W_{\frac{n}{2}+\frac{a}{2}+\frac{1}{4},\frac{1}{4}\sqrt{1-4(-1)^na+4a^2}}\left(x^2\right)\_C2\right)\right\}$$

2.1211 ODE No. 1211

$$4x^3y'(x)+x^2y''(x)+\left(4x^4+2x^2+1\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0582652 (sec), leaf count = 68

$$\left\{\left\{y(x)\to c_1e^{-x^2}x^{\frac{1}{2}-\frac{i\sqrt{3}}{2}}-\frac{ic_2e^{-x^2}x^{\frac{1}{2}+\frac{i\sqrt{3}}{2}}}{\sqrt{3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 36

$$\left\{y(x)=\mathrm{e}^{-x^2}\left(x^{\frac{1}{2}-\frac{i}{2}\sqrt{3}}\_C2+x^{\frac{1}{2}+\frac{i}{2}\sqrt{3}}\_C1\right)\right\}$$

2.1212 ODE No. 1212

$$x\left(ax^2+b\right)y'(x)+f(x)y(x)+x^2y''(x)=0$$

✗ **Mathematica** : cpu = 0.380713 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + x*(b + a*x^2)*Derivative[1][y][x] + x^2*Derivative[2][y][x] == 0, y[x], x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{f(x)\_Y(x)}{x^2}+\frac{\left(ax^2+b\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{x}+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1213 ODE No. 1213

$$\left(x^3+1\right) x y'(x)+x^2 y''(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0819452 (sec), leaf count = 54

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{3} c_1\, {}_1F_1\left(-\frac{1}{3};\frac{1}{3};-\frac{x^3}{3}\right)}{x}+\frac{c_2 x\, {}_1F_1\left(\frac{1}{3};\frac{5}{3};-\frac{x^3}{3}\right)}{\sqrt[3]{3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 53

$$\left\{y(x)=x^{\frac{3}{2}} \mathrm{e}^{-\frac{x^3}{6}} \left(\_C1\, I_{-\frac{1}{6}}\left(\frac{x^3}{6}\right)+\_C1\, I_{\frac{5}{6}}\left(\frac{x^3}{6}\right)-\_C2\left(K_{\frac{1}{6}}\left(\frac{x^3}{6}\right)-K_{\frac{5}{6}}\left(\frac{x^3}{6}\right)\right)\right)\right\}$$

2.1214 ODE No. 1214

$$y(x)\left(-a^2+x^2(2a+2n+1)+a(-1)^n-x^4\right)+x^2 y''(x)=0$$

✓ **Mathematica** : cpu = 0.294634 (sec), leaf count = 260

$$\left\{\left\{y(x)\to \frac{c_1 e^{-\frac{x^2}{2}} 2^{\frac{1}{4}\left(\sqrt{4a^2-4a(-1)^n+1}+2\right)} \left(x^2\right)^{\frac{1}{4}\left(\sqrt{4a^2-4a(-1)^n+1}+2\right)} U\left(\frac{1}{4}\left(-2a-2n+\sqrt{4a^2-4(-1)^n a+1}+1\right)\right.\right.\right.$$
$$\left.\left.\left.\frac{}{\sqrt{x}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.62 (sec), leaf count = 71

$$\left\{y(x)=1\left(\_C1\, M_{\frac{n}{2}+\frac{a}{2}+\frac{1}{4},\frac{1}{4}\sqrt{1-4\,(-1)^n a+4\,a^2}}\left(x^2\right)+\_C2\, W_{\frac{n}{2}+\frac{a}{2}+\frac{1}{4},\frac{1}{4}\sqrt{1-4\,(-1)^n a+4\,a^2}}\left(x^2\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1215 ODE No. 1215

$$x y'(x)\left(a x^n+b\right)+y(x)\left(\mathrm{a1} x^{2n}+\mathrm{b1} x^n+\mathrm{c1}\right)+x^2 y''(x)=0$$

✓ **Mathematica** : cpu = 0.163448 (sec), leaf count = 664

$$\left\{\left\{y(x)\to c_1 x^{\frac{1-n}{2}} 2^{\frac{\sqrt{b^2n^2-2bn^2-4c1n^2+n^2}+n^2}{2n^2}} \left(x^n\right)^{\frac{\sqrt{b^2n^2-2bn^2-4c1n^2+n^2}+n^2}{2n^2}} \exp\left(\frac{1}{2}\left(-\frac{a x^n}{n}-b\log(x)\right)-\frac{\sqrt{a^2-4\mathrm{a1}}x^n}{2n}\right.\right.\right.$$
$$\left.\left.\left.\right.\right.\right.$$

✓ **Maple** : cpu = 0.176 (sec), leaf count = 148

$$\left\{y(x)=\mathrm{e}^{-\frac{a x^{n}}{2\,n}}x^{-\frac{b}{2}-\frac{n}{2}+\frac{1}{2}}\left(W_{-\frac{(b+n-1)a-2\,b1}{2\,n}\frac{1}{\sqrt{a^{2}-4\,a1}},\frac{1}{2\,n}\sqrt{b^{2}-2\,b-4\,c1+1}}\left(\frac{x^{n}}{n}\sqrt{a^{2}-4\,a1}\right)\_C2+M_{-\frac{(b+n-1)a-2\,b1}{2\,n}\frac{1}{\sqrt{a^{2}-4}}}\right.\right.$$

2.1216 ODE No. 1216

$$xy'(x)\left(ax^{\mathrm{a1}}+b\right)+y(x)\left(Ax^{2\mathrm{a1}}+Bx^{\mathrm{a1}}+Cx^{\mathrm{b1}}+\mathrm{DD}\right)+x^{2}y''(x)=0$$

✗ **Mathematica** : cpu = 1.47117 (sec), leaf count = 0 , could not solve

```
DSolve[(DD + B*x^a1 + A*x^(2*a1) + C*x^b1)*y[x] + x*(b + a*x^a1)*Derivative[1][y][x] + x^2*D
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^{2}}{\mathrm{d}x^{2}}\_Y(x)+\frac{\left(ax^{a1}+b\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{x}+\frac{\left(Ax^{2\,a1}+Bx^{a1}+Cx^{b1}+DD\right)\_Y(x)}{x^{2}}\right\},\{\_Y(x)\}\right)\right.$$

2.1217 ODE No. 1217

$$-y(x)(a+x\tan(x))+x^{2}y''(x)-\left(2x^{2}\tan(x)-x\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.147032 (sec), leaf count = 30

$$\left\{\left\{y(x)\to c_1\sec(x)J_{\sqrt{a}}(x)+c_2\sec(x)Y_{\sqrt{a}}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 24

$$\left\{y(x)=\frac{1}{\cos\left(x\right)}\left(\_C1\,J_{\sqrt{a}}(x)+\_C2\,Y_{\sqrt{a}}(x)\right)\right\}$$

2.1218 ODE No. 1218

$$y(x)(a+x\cot(x))+x^{2}y''(x)+\left(2x^{2}\cot(x)+x\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.150699 (sec), leaf count = 38

$$\left\{\left\{y(x)\to c_1\csc(x)J_{i\sqrt{a}}(x)+c_2\csc(x)Y_{i\sqrt{a}}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 30

$$\left\{y(x)=\frac{1}{\sin\left(x\right)}\left(\_C2\,Y_{i\sqrt{a}}(x)+\_C1\,J_{i\sqrt{a}}(x)\right)\right\}$$

2.1219 ODE No. 1219

$$y(x)\left(ax^2+bx+c+xf'(x)+f(x)^2-f(x)\right)+2xf(x)y'(x)+x^2y''(x)=0$$

✗ **Mathematica** : cpu = 300.03 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.082 (sec), leaf count = 69

$$\left\{y(x)=\mathrm{e}^{-\int\frac{f(x)}{x}\,\mathrm{d}x}\left(W_{-\frac{i}{2}b\frac{1}{\sqrt{a}},\frac{1}{2}\sqrt{1-4\,c}}\left(2\,i\sqrt{a}x\right)\_C2+M_{-\frac{i}{2}b\frac{1}{\sqrt{a}},\frac{1}{2}\sqrt{1-4\,c}}\left(2\,i\sqrt{a}x\right)\_C1\right)\right\}$$

2.1220 ODE No. 1220

$$y(x)\left(x^2\left(a+f'(x)+f(x)^2\right)-(v-1)v\right)+2x^2f(x)y'(x)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 193.071 (sec), leaf count = 96

$$\left\{\left\{y(x)\to c_1J_{\frac{1}{2}(2v-1)}\left(\sqrt{a}x\right)\exp\left(\int_1^x\frac{1-2K[1]f(K[1])}{2K[1]}\,dK[1]\right)+c_2Y_{\frac{1}{2}(2v-1)}\left(\sqrt{a}x\right)\exp\left(\int_1^x\frac{1-2K[1]f(K[1])}{2K[1]}\right.\right.\right.$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 40

$$\left\{y(x)=\sqrt{x}\mathrm{e}^{-\frac{\int2\,f(x)\,\mathrm{d}x}{2}}\left(Y_{v-\frac{1}{2}}\left(\sqrt{a}x\right)\_C2+J_{v-\frac{1}{2}}\left(\sqrt{a}x\right)\_C1\right)\right\}$$

2.1221 ODE No. 1221

$$y(x)\left(x^2\left(-f'(x)+f(x)^2+1\right)-xf(x)-v^2\right)+\left(x-2x^2f(x)\right)y'(x)+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0594613 (sec), leaf count = 40

$$\left\{\left\{y(x)\to c_1J_v(x)e^{\int_1^x f(K[1])\,dK[1]}+c_2Y_v(x)e^{\int_1^x f(K[1])\,dK[1]}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 35

$$\left\{y(x)=\sqrt{x}\mathrm{e}^{-\frac{1}{2}\int\frac{-2\,xf(x)+1}{x}\,\mathrm{d}x}\left(Y_v(x)\_C2+J_v(x)\_C1\right)\right\}$$

2.1222 ODE No. 1222

$$\left(x^2+1\right) y''(x)+xy'(x)+2y(x)=0$$

✓ **Mathematica** : cpu = 0.0215486 (sec), leaf count = 30

$$\left\{\left\{y(x)\to c_2 \sin\left(\sqrt{2}\sinh^{-1}(x)\right)+c_1 \cos\left(\sqrt{2}\sinh^{-1}(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 23

$$\left\{y(x)=\_C1 \sin\left(\sqrt{2}Arcsinh(x)\right)+\_C2 \cos\left(\sqrt{2}Arcsinh(x)\right)\right\}$$

2.1223 ODE No. 1223

$$\left(x^2+1\right) y''(x)+xy'(x)-9y(x)=0$$

✓ **Mathematica** : cpu = 0.0199141 (sec), leaf count = 25

$$\left\{\left\{y(x)\to c_1 \cosh\left(3\sinh^{-1}(x)\right)+ic_2 \sinh\left(3\sinh^{-1}(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 39

$$\left\{y(x)=\_C1 \sin\left(3\arctan\left(\frac{x}{\sqrt{-x^2-1}}\right)\right)+\_C2 \cos\left(3\arctan\left(\frac{x}{\sqrt{-x^2-1}}\right)\right)\right\}$$

2.1224 ODE No. 1224

$$ay(x)+\left(x^2+1\right) y''(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0196082 (sec), leaf count = 30

$$\left\{\left\{y(x)\to c_2 \sin\left(\sqrt{a}\sinh^{-1}(x)\right)+c_1 \cos\left(\sqrt{a}\sinh^{-1}(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 23

$$\left\{y(x)=\_C1 \sin\left(\sqrt{a}Arcsinh(x)\right)+\_C2 \cos\left(\sqrt{a}Arcsinh(x)\right)\right\}$$

2.1225 ODE No. 1225

$$\left(x^2+1\right) y''(x)-xy'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0315563 (sec), leaf count = 29

$$\left\{\left\{y(x)\to c_2\left(x \sinh ^{-1}(x)-\sqrt{x^2+1}\right)+c_1 x\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 23

$$\left\{y(x) = -\sqrt{x^2+1}\_C2+x(\_C2\ Arcsinh(x)+\_C1)\right\}$$

2.1226 ODE No. 1226

$$-(v-1)vy(x)+\left(x^2+1\right) y''(x)+2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0194911 (sec), leaf count = 30

$$\{\{y(x)\to c_1 P_{v-1}(ix)+c_2 Q_{v-1}(ix)\}\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 25

$$\{y(x) = \_C1\ LegendreP(v-1,ix)+\_C2\ LegendreQ(v-1,ix)\}$$

2.1227 ODE No. 1227

$$\left(x^2+1\right) y''(x)-2xy'(x)+2y(x)=0$$

✓ **Mathematica** : cpu = 0.0344758 (sec), leaf count = 21

$$\left\{\left\{y(x)\to c_2 x-c_1(x-i)^2\right\}\right\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 16

$$\left\{y(x) = \_C2\ x^2+\_C1\ x-\_C2\right\}$$

2.1228 ODE No. 1228

$$ay(x)+\left(x^2+1\right)y''(x)+3xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0162343 (sec), leaf count = 82

$$\left\{\left\{y(x)\to \frac{c_1 P^{\frac{1}{2}}_{\frac{1}{2}\left(2\sqrt{1-a}-1\right)}(ix)}{\sqrt[4]{x^2+1}}+\frac{c_2 Q^{\frac{1}{2}}_{\frac{1}{2}\left(2\sqrt{1-a}-1\right)}(ix)}{\sqrt[4]{x^2+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.086 (sec), leaf count = 53

$$\left\{y(x)=1\left(\_C2\left(x+\sqrt{x^2+1}\right)^{-\sqrt{1-a}}+\_C1\left(x+\sqrt{x^2+1}\right)^{\sqrt{1-a}}\right)\frac{1}{\sqrt{x^2+1}}\right\}$$

2.1229 ODE No. 1229

$$\left(x^2+1\right)y''(x)+4xy'(x)+2y(x)+2x-2\cos(x)=0$$

✓ **Mathematica** : cpu = 0.0448439 (sec), leaf count = 48

$$\left\{\left\{y(x)\to \frac{c_1}{x^2+1}+\frac{c_2 x}{x^2+1}+\frac{-x^3-6\cos(x)}{3\left(x^2+1\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 31

$$\left\{y(x)=\frac{-x^3+3\_C1\,x-6\,\cos\left(x\right)+3\_C2}{3\,x^2+3}\right\}$$

2.1230 ODE No. 1230

$$axy'(x)+(a-2)y(x)+\left(x^2+1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.0265473 (sec), leaf count = 82

$$\left\{\left\{y(x)\to c_1\left(x^2+1\right)^{\frac{2-a}{4}}P^{\frac{a-2}{2}}_{\frac{a-4}{2}}(ix)+c_2\left(x^2+1\right)^{\frac{2-a}{4}}Q^{\frac{a-2}{2}}_{\frac{a-4}{2}}(ix)\right\}\right\}$$

✓ **Maple** : cpu = 0.106 (sec), leaf count = 36

$$\left\{y(x)=\_C1\left(x^2+1\right)^{1-\frac{a}{2}}+\_C2\,{}_2\mathrm{F}_1(1,\frac{a}{2}-\frac{1}{2};\frac{3}{2};-x^2)x\right\}$$

2.1231 ODE No. 1231

$$\left(x^2-1\right)y''(x)-v(v+1)y(x)=0$$

✓ **Mathematica** : cpu = 0.0781431 (sec), leaf count = 58

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(-\frac{v}{2}-\frac{1}{2},\frac{v}{2};\frac{1}{2};x^2\right)+ic_2x\,{}_2F_1\left(\frac{v}{2}+\frac{1}{2},-\frac{v}{2};\frac{3}{2};x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 52

$$\left\{y(x)=-(x-1)\,(1+x)\left({}_2\mathrm{F}_1(1-\frac{v}{2},\frac{3}{2}+\frac{v}{2};\frac{3}{2};x^2)\_C2\,x+\_C1\,{}_2\mathrm{F}_1(1+\frac{v}{2},\frac{1}{2}-\frac{v}{2};\frac{1}{2};x^2)\right)\right\}$$

2.1232 ODE No. 1232

$$\frac{nxP_n(x)-nP_{n-1}(x)}{x^2-1}-n(n+1)y(x)+\left(x^2-1\right)y''(x)=0$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.19 (sec), leaf count = 409

$$\left\{y(x)=3\,(1+x)\left(-{}_2\mathrm{F}_1(n/2+1,-n/2+1/2;\,1/2;\,x^2)(n+1)\int 1/3\,\frac{}{(1+x)^3\,(x-1)^3\,(({}_2\mathrm{F}_1(n/2+1,-n/2+1}\right.\right.$$

2.1233 ODE No. 1233

$$\frac{nxQ_n(x)-nQ_{n-1}(x)}{x^2-1}-n(n+1)y(x)+\left(x^2-1\right)y''(x)=0$$

✗ **Mathematica** : cpu = 299.997 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.154 (sec), leaf count = 409

$$\left\{y(x)=3\,(1+x)\left(-{}_2\mathrm{F}_1(n/2+1,-n/2+1/2;\,1/2;\,x^2)(n+1)\int 1/3\,\frac{}{(1+x)^3\,(({}_2\mathrm{F}_1(n/2+1,-n/2+1/2;\,1/2;}\right.\right.$$

2.1234 ODE No. 1234

$$\left(x^2-1\right)y''(x)+xy'(x)+2=0$$

✓ **Mathematica** : cpu = 0.0290854 (sec), leaf count = 38

$$\left\{\left\{y(x)\to \log\left(\sqrt{x^2-1}+x\right)\left(c_1-\log\left(\sqrt{x^2-1}+x\right)\right)+c_2\right\}\right\}$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.1235 ODE No. 1235

$$ay(x)+\left(x^2-1\right)y''(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0287277 (sec), leaf count = 50

$$\left\{\left\{y(x)\to c_2\sin\left(\sqrt{a}\log\left(\sqrt{x^2-1}+x\right)\right)+c_1\cos\left(\sqrt{a}\log\left(\sqrt{x^2-1}+x\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 45

$$\left\{y(x)=1\left(\_C1\left(\left(x+\sqrt{x^2-1}\right)^{i\sqrt{a}}\right)^2+\_C2\right)\left(\left(x+\sqrt{x^2-1}\right)^{i\sqrt{a}}\right)^{-1}\right\}$$

2.1236 ODE No. 1236

$$f(x)y(x)+\left(x^2-1\right)y''(x)+xy'(x)=0$$

✗ **Mathematica** : cpu = 0.363588 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + x*Derivative[1][y][x] + (-1 + x^2)*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{f(x)\_Y(x)}{x^2-1}+\frac{x\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{x^2-1}+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1237 ODE No. 1237

$$\left(x^2-1\right)y''(x)+2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0111895 (sec), leaf count = 30

$$\left\{\left\{y(x)\to c_1\left(\frac{1}{2}\log(1-x)-\frac{1}{2}\log(x+1)\right)+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 20

$$\left\{y(x)=\_C1-\frac{\left(\ln\left(1+x\right)-\ln\left(x-1\right)\right)\_C2}{2}\right\}$$

2.1238 ODE No. 1238

$$-a+\left(x^2-1\right)y''(x)+2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0188073 (sec), leaf count = 36

$$\left\{\left\{y(x)\to\frac{1}{2}(a+c_1)\log(1-x)+\frac{1}{2}(a-c_1)\log(x+1)+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 26

$$\left\{y(x)=\frac{\left(a-\_C1\right)\ln\left(1+x\right)}{2}+\frac{\left(a+\_C1\right)\ln\left(x-1\right)}{2}+\_C2\right\}$$

2.1239 ODE No. 1239

$$-ly(x)+\left(x^2-1\right)y''(x)+2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0144366 (sec), leaf count = 46

$$\left\{\left\{y(x)\to c_1P_{\frac{1}{2}\left(\sqrt{4l+1}-1\right)}(x)+c_2Q_{\frac{1}{2}\left(\sqrt{4l+1}-1\right)}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 35

$$\left\{y(x)=\_C1\ LegendreP\left(\frac{1}{2}\sqrt{1+4\,l}-\frac{1}{2},x\right)+\_C2\ LegendreQ\left(\frac{1}{2}\sqrt{1+4\,l}-\frac{1}{2},x\right)\right\}$$

2.1240 ODE No. 1240

$$-v(v+1)y(x)+\left(x^2-1\right)y''(x)+2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0184882 (sec), leaf count = 18

$$\{\{y(x)\to c_1P_v(x)+c_2Q_v(x)\}\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 15

$$\{y(x)=\_C1\ LegendreP(v,x)+\_C2\ LegendreQ(v,x)\}$$

2.1241 ODE No. 1241

$$-(v-1)(v+2)y(x)+\left(x^2-1\right)y''(x)-2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0159146 (sec), leaf count = 30

$$\left\{\left\{y(x)\to c_1\left(x^2-1\right)P_v^2(x)+c_2\left(x^2-1\right)Q_v^2(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 24

$$\{y(x)=(1+x)\,(x-1)\,(\_C2\ LegendreQ(v,2,x)+\_C1\ LegendreP(v,2,x))\}$$

2.1242 ODE No. 1242

$$\left(x^2-1\right)y''(x)-\left(x^2-x\right)y(x)-(3x+1)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0772488 (sec), leaf count = 68

$$\left\{\left\{y(x)\to c_1e^{-x}(x+1)^2-c_2e^{-x-2}\left(x^2(-\text{Ei}(2(x+1)))-2x\text{Ei}(2(x+1))-\text{Ei}(2(x+1))+2e^{2x+2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.077 (sec), leaf count = 41

$$\left\{y(x)=\_C2\,\mathrm{e}^{-x-2}(1+x)^2\,Ei(1,-2\,x-2)+\_C1\,\mathrm{e}^{-x}(1+x)^2+2\,\mathrm{e}^{x}\_C2\right\}$$

2.1243 ODE No. 1243

$$\left(x^2-1\right)y''(x)+\left(x^2+1\right)y(x)+4xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0305097 (sec), leaf count = 45

$$\left\{\left\{y(x)\to \frac{c_1e^{-ix}}{x^2-1}-\frac{ic_2e^{ix}}{2\left(x^2-1\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 21

$$\left\{y(x)=\frac{\_C2\,\cos(x)+\_C1\,\sin(x)}{x^2-1}\right\}$$

2.1244 ODE No. 1244

$$-(v-n)(n+v+1)y(x)+2(n+1)xy'(x)+\left(x^2-1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.0312827 (sec), leaf count = 42

$$\left\{\left\{y(x)\to c_1\left(x^2-1\right)^{-n/2}P_v^n(x)+c_2\left(x^2-1\right)^{-n/2}Q_v^n(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.071 (sec), leaf count = 27

$$\left\{y(x)=\left(x^2-1\right)^{-\frac{n}{2}}\left(LegendreP(v,n,x)\_C1+LegendreQ(v,n,x)\_C2\right)\right\}$$

2.1245 ODE No. 1245

$$-(-n+v+1)(n+v)y(x)-2(n-1)xy'(x)+\left(x^2-1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.0222196 (sec), leaf count = 42

$$\left\{\left\{y(x)\to c_1\left(x^2-1\right)^{n/2}P_v^n(x)+c_2\left(x^2-1\right)^{n/2}Q_v^n(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 27

$$\left\{y(x)=\left(x^2-1\right)^{\frac{n}{2}}\left(LegendreP(v,n,x)\_C1+LegendreQ(v,n,x)\_C2\right)\right\}$$

2.1246 ODE No. 1246

$$-2(v-1)xy'(x)-2vy(x)+\left(x^2-1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.0208296 (sec), leaf count = 42

$$\left\{\left\{y(x)\to c_1\left(x^2-1\right)^{v/2}P_v^v(x)+c_2\left(x^2-1\right)^{v/2}Q_v^v(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.158 (sec), leaf count = 28

$$\left\{y(x)=\left(x^2-1\right)^v\left({}_2\mathrm{F}_1(\frac{1}{2},v+1;\frac{3}{2};x^2)\_C2\,x+\_C1\right)\right\}$$

2.1247 ODE No. 1247

$$2axy'(x)+(a-1)ay(x)+\left(x^2-1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.216496 (sec), leaf count = 97

$$\left\{\left\{y(x)\to c_1\sqrt{1-x^2}\left(x^2-1\right)^{-a/2}e^{-\sqrt{(a-1)^2}\tanh^{-1}(x)}+\frac{c_2\sqrt{1-x^2}\left(x^2-1\right)^{-a/2}e^{\sqrt{(a-1)^2}\tanh^{-1}(x)}}{2\sqrt{(a-1)^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 27

$$\left\{y(x)=\_C1\,(1+x)^{1-a}+\_C2\,(x-1)^{1-a}\right\}$$

2.1248 ODE No. 1248

$$axy'(x)+y(x)\left(bx^2+cx+d\right)+\left(x^2-1\right)y''(x)=0$$

✗ **Mathematica** : cpu = 2.10198 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{\left(bx^2+cx+d\right)y(x)+xay'(x)+\left(x^2-1\right)y''(x)=0,y(0)=c_1,y'(0)=c_2\right\}\right)\right.$$

✓ **Maple** : cpu = 0.221 (sec), leaf count = 134

$$\left\{y(x)=\mathrm{e}^{\sqrt{-b}x}\left(x^2-1\right)^{-\frac{a}{4}}\left(\left(\frac{1}{2}+\frac{x}{2}\right)^{1-\frac{a}{4}}\left(-\frac{1}{2}+\frac{x}{2}\right)^{\frac{a}{4}}HeunC\left(4\sqrt{-b},1-\frac{a}{2},\frac{a}{2}-1,2\,c,d-c-\frac{a^2}{8}+b+\frac{1}{2},\frac{1}{2}\right.\right.\right.$$

2.1249 ODE No. 1249

$$(ax+b)y'(x)+cy(x)+\left(x^2-1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.175824 (sec), leaf count = 193

$$\left\{\left\{y(x)\to c_2 2^{\frac{1}{2}(a+b-2)}(x-1)^{\frac{1}{2}(-a-b+2)}\,{}_2F_1\left(-\frac{b}{2}-\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{1}{2},-\frac{b}{2}+\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{1}{2};-\right.\right.$$

✓ **Maple** : cpu = 0.078 (sec), leaf count = 134

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(-\frac{1}{2}-\frac{1}{2}\sqrt{a^2-2\,a-4\,c+1}+\frac{a}{2},-\frac{1}{2}+\frac{1}{2}\sqrt{a^2-2\,a-4\,c+1}+\frac{a}{2};\frac{a}{2}-\frac{b}{2};\frac{1}{2}+\frac{x}{2})+\_C2\left(\frac{1}{2}\right.\right.$$

2.1250 ODE No. 1250

$$\left(x^2-a^2\right)y''(x)+8xy'(x)+12y(x)=0$$

✓ **Mathematica** : cpu = 0.0523503 (sec), leaf count = 41

$$\left\{\left\{y(x)\to \frac{c_2\left(a^2+3x^2\right)}{3(a-x)^3(a+x)^3}+\frac{c_1}{(a+x)^3}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 41

$$\left\{y(x)=\frac{3\_C2\,a^2x+\_C2\,x^3+\_C1\,a^2+3\_C1\,x^2}{\left(a-x\right)^3\left(x+a\right)^3}\right\}$$

2.1251 ODE No. 1251

$$x(x+1)y''(x)-(x-1)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0369061 (sec), leaf count = 25

$$\{\{y(x)\to c_1(x-1)+c_2(x\log(x)-\log(x)-4)\}\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 20

$$\{y(x)=\_C2\,(x-1)\ln(x)-4\,\_C2+\_C1\,(x-1)\}$$

2.1252 ODE No. 1252

$$(ax+b)y'(x)+cy(x)+x(x+1)y''(x)=0$$

✓ **Mathematica** : cpu = 0.153241 (sec), leaf count = 151

$$\left\{\left\{y(x)\to c_2x^{1-b}\,{}_2F_1\left(\frac{a}{2}-b-\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{1}{2},\frac{a}{2}-b+\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{1}{2};2-b;-x\right)+c_1\,{}_2F_1\right.\right.$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 124

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(-\frac{1}{2}-\frac{1}{2}\sqrt{a^2-2\,a-4\,c+1}+\frac{a}{2},-\frac{1}{2}+\frac{1}{2}\sqrt{a^2-2\,a-4\,c+1}+\frac{a}{2};\,a-b;\,1+x)+\_C2\,(1+x\right.$$

2.1253 ODE No. 1253

$$x(x+1)y''(x)+(3x+2)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0265108 (sec), leaf count = 34

$$\left\{\left\{y(x)\to\frac{\sqrt{2}c_1}{x}+\frac{c_2\log(2x+2)}{\sqrt{2}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 16

$$\left\{y(x)=\frac{\ln(1+x)\_C1+\_C2}{x}\right\}$$

2.1254 ODE No. 1254

$$\left(x^2+x-2\right)y''(x)+\left(x^2-x\right)y'(x)-\left(6x^2+7x\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0905623 (sec), leaf count = 69

$$\left\{\left\{y(x)\to\frac{1}{5}c_2e^{-3x-5}\left(195e^{5x}x\mathrm{Ei}(5-5x)-195e^{5x}\mathrm{Ei}(5-5x)+e^5x+44e^5\right)-c_1e^{2x}(x-1)\right\}\right\}$$

✓ **Maple** : cpu = 0.084 (sec), leaf count = 42

$$\left\{y(x)=-195\,\_C2\,\mathrm{e}^{2\,x-5}(x-1)\,Ei(1,5\,x-5)+\_C2\,(x+44)\,\mathrm{e}^{-3\,x}+\_C1\,\mathrm{e}^{2\,x}(x-1)\right\}$$

2.1255 ODE No. 1255

$$ay'(x)+(x-1)xy''(x)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.212632 (sec), leaf count = 118

$$\left\{\left\{y(x)\to \frac{c_1\left(a^2+2ax-a+2x^2-2x\right)}{a^2+3a+4}+\frac{c_2x^{a+1}\left(a^2+2ax-a+2x^2-2x\right)(1-x)^{1-a}}{(a-1)a(a+1)\left(a^2+3a+4\right)\left(a^2+a(2x-1)+2(x-1)x\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 42

$$\left\{y(x)=\left(a^2+a(2\,x-1)+2\,x^2-2\,x\right)\_C1+\frac{\_C2\,x^a x(x-1)}{(x-1)^a}\right\}$$

2.1256 ODE No. 1256

$$-v(v+1)y(x)+(x-1)xy''(x)+(2x-1)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0241033 (sec), leaf count = 26

$$\{\{y(x)\to c_1P_v(2x-1)+c_2Q_v(2x-1)\}\}$$

✓ **Maple** : cpu = 0.113 (sec), leaf count = 51

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(-v,-v;\,-2\,v;\,x^{-1})x^v+\_C2\,{}_2\mathrm{F}_1(v+1,v+1;\,2+2\,v;\,x^{-1})x^{-v-1}\right\}$$

2.1257 ODE No. 1257

$$((a+1)x+b)y'(x)+(x-1)xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0499031 (sec), leaf count = 33

$$\left\{\left\{y(x)\to \frac{c_1x^{b+1}\,{}_2F_1(b+1,a+b+1;b+2;x)}{b+1}+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.23 (sec), leaf count = 27

$$\left\{y(x)=\_C1+{}_2\mathrm{F}_1(b+1,a+b+1;\,b+2;\,x)x^{b+1}\_C2\right\}$$

2.1258 ODE No. 1258

$$(ax+b)y'(x)+cy(x)+(x-1)xy''(x)=0$$

✓ **Mathematica** : cpu = 0.166451 (sec), leaf count = 146

$$\left\{\left\{y(x)\to (-1)^{b+1}c_2x^{b+1}\,{}_2F_1\left(\frac{a}{2}+b-\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{1}{2},\frac{a}{2}+b+\frac{1}{2}\sqrt{a^2-2a-4c+1}+\frac{1}{2};b+2;x\right)+\right.\right.$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 110

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(-\frac{1}{2}-\frac{1}{2}\sqrt{a^2-2\,a-4\,c+1}+\frac{a}{2},-\frac{1}{2}+\frac{1}{2}\sqrt{a^2-2\,a-4\,c+1}+\frac{a}{2};\,-b;\,x)+\_C2\,x^{b+1}{}_2\mathrm{F}_1(\frac{1}{2}-\right.$$

2.1259 ODE No. 1259

$$((a+1)x+b)y'(x)-ly(x)+(x-1)xy''(x)=0$$

✓ **Mathematica** : cpu = 0.144298 (sec), leaf count = 120

$$\left\{\left\{y(x)\to (-1)^{b+1}c_2x^{b+1}\,{}_2F_1\left(\frac{a}{2}+b-\frac{1}{2}\sqrt{a^2+4l}+1,\frac{a}{2}+b+\frac{1}{2}\sqrt{a^2+4l}+1;b+2;x\right)+c_1\,{}_2F_1\left(\frac{a}{2}-\frac{1}{2}\sqrt{a^2-\right.\right.\right.$$

✓ **Maple** : cpu = 0.059 (sec), leaf count = 92

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(\frac{a}{2}-\frac{1}{2}\sqrt{a^2+4\,l},\frac{a}{2}+\frac{1}{2}\sqrt{a^2+4\,l};\,-b;\,x)+\_C2\,x^{b+1}{}_2\mathrm{F}_1(\frac{a}{2}-\frac{1}{2}\sqrt{a^2+4\,l}+b+1,\frac{a}{2}+\frac{1}{2}\sqrt{a^{2}}\right.$$

2.1260 ODE No. 1260

$$y'(x)(x(\mathrm{a1}+\mathrm{b1}+1)-\mathrm{d1})+\mathrm{a1b1d1}+(x-1)xy''(x)=0$$

✓ **Mathematica** : cpu = 0.170673 (sec), leaf count = 65

$$\left\{\left\{y(x)\to \mathrm{a1b1}x\Gamma(\mathrm{d1}+1)\,{}_3\tilde{F}_2(1,\mathrm{a1}+\mathrm{b1}+1,1;\mathrm{d1}+1,2;x)-\frac{c_1x^{1-\mathrm{d1}}\,{}_2F_1(1-\mathrm{d1},\mathrm{a1}+\mathrm{b1}-\mathrm{d1}+1;2-\mathrm{d1};x)}{\mathrm{d1}-1}\right.\right.$$

✓ **Maple** : cpu = 0.566 (sec), leaf count = 76

$$\left\{y(x)=\int\left(-(signum(x-1))^{a1+b1-d1}\,(-signum(x-1))^{-a1-b1+d1}\,a1\,b1\,{}_2\mathrm{F}_1(d1,-a1-b1+d1;\,1+d1;\,x)-\right.\right.$$

2.1261 ODE No. 1261

$$y(x)(2lx(-n+p-1)+2lp+m)+2\left(x(-2l+n+1)-lx^2+n+1\right)y'(x)+x(x+2)y''(x)=0$$

✗ **Mathematica** : cpu = 2.67882 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\{(-2xl-2xnl+2xpl+2pl+m)y(x)+2\left(-lx^2-2lx+nx+x+n+1\right)y'(x\right)$$

✓ **Maple** : cpu = 0.234 (sec), leaf count = 105

$$\left\{y(x)=(x+2)^{-\frac{n}{2}-\frac{1}{2}}\left(-\frac{x}{2}-1\right)^{\frac{n}{2}+\frac{1}{2}}\left(x^{-n}HeunC\left(4\,l,-n,n,-4\,pl,\frac{(4\,n+4\,p+4)\,l}{2}-\frac{n^2}{2}+m-n,-\frac{x}{2}\right)\_C2\right.\right.$$

2.1262 ODE No. 1262

$$\left(x^2+x-1\right)y'(x)+(x+1)^2y''(x)-(x+2)y(x)=0$$

✓ **Mathematica** : cpu = 41.0851 (sec), leaf count = 87

$$\left\{\left\{y(x)\to c_2e^{-x}\int_1^x(K[1]+1)^{\frac{K[1]}{K[1]+1}+\frac{1}{K[1]+1}}\exp\left(-\frac{K[1]^2}{K[1]+1}-\frac{K[1]}{K[1]+1}+2K[1]-\frac{1}{K[1]+1}\right)dK[1]+c_1e^{-x}\right\}\right.$$

✓ **Maple** : cpu = 0.263 (sec), leaf count = 53

$$\left\{y(x)=(1+x)\left(\_C1\,\mathrm{e}^{-x}HeunD\left(4,4,-8,12,\frac{x}{x+2}\right)+\_C2\,HeunD\left(-4,4,-8,12,\frac{x}{x+2}\right)\mathrm{e}^{\frac{x-1}{2\,x+2}}\right)\right\}$$

2.1263 ODE No. 1263

$$-(20x+30)\left(x^2+3x\right)^{7/3}+x(x+3)y''(x)+(3x-1)y'(x)+y(x)=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.086 (sec), leaf count = 52

$$\left\{y(x)=1\left(\_C2+\int\frac{1}{x^2+3\,x}\left(\_C1+3\left(x^2+3\,x\right)^{7/3}x(x+3)\right)(x+3)^{\frac{7}{3}}x^{-\frac{4}{3}}\,\mathrm{d}x\right)x^{\frac{4}{3}}(x+3)^{-\frac{7}{3}}\right\}$$

2.1264 ODE No. 1264

$$\left(x^2+3x+4\right)y''(x)+\left(x^2+x+1\right)y'(x)-(2x+3)y(x)=0$$

✓ **Mathematica** : cpu = 0.0635523 (sec), leaf count = 23

$$\left\{\left\{y(x)\to c_2\left(x^2+x+3\right)+c_1e^{-x}\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 19

$$\left\{y(x)=\_C1\,\mathrm{e}^{-x}+\_C2\,\left(x^2+x+3\right)\right\}$$

2.1265 ODE No. 1265

$$(x-2)(x-1)y''(x)-(2x-3)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0436648 (sec), leaf count = 64

$$\left\{\left\{y(x)\to c_1\left(x^2-3x+2\right)P^2_{\frac{1}{2}\left(-1+\sqrt{5}\right)}(2x-3)+c_2\left(x^2-3x+2\right)Q^2_{\frac{1}{2}\left(-1+\sqrt{5}\right)}(2x-3)\right\}\right\}$$

✓ **Maple** : cpu = 0.131 (sec), leaf count = 93

$$\left\{y(x)=(x-2)^2\left(\_C1\,{}_2\mathrm{F}_1(\frac{1}{2}-\frac{\sqrt{5}}{2},\frac{5}{2}-\frac{\sqrt{5}}{2};-\sqrt{5}+1;(x-1)^{-1})(x-1)^{\frac{\sqrt{5}}{2}-\frac{1}{2}}+\_C2\,{}_2\mathrm{F}_1(\frac{1}{2}+\frac{\sqrt{5}}{2},\frac{5}{2}+\frac{\sqrt{5}}{2};\right.\right.$$

2.1266 ODE No. 1266

$$(x-2)^2y''(x)-(x-2)y'(x)-3y(x)=0$$

✓ **Mathematica** : cpu = 0.0295027 (sec), leaf count = 22

$$\left\{\left\{y(x)\to c_1(x-2)^3+\frac{c_2}{x-2}\right\}\right\}$$

✓ **Maple** : cpu = 0.009 (sec), leaf count = 19

$$\left\{y(x)=\frac{\_C1+\_C2\,(x-2)^4}{x-2}\right\}$$

2.1267 ODE No. 1267

$$-\left(l+2x^2-5x\right)y'(x)+2x^2y''(x)-(4x-1)y(x)=0$$

✗ **Mathematica** : cpu = 300.106 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.072 (sec), leaf count = 41

$$\left\{y(x)=\mathrm{e}^{x}\left(\_C1\int\frac{1}{2\,\mathrm{e}^{x}}\mathrm{e}^{\frac{l}{2x}}x^{-\frac{3}{2}}\,\mathrm{d}x+\_C2\right)\frac{1}{\sqrt{x}}\left(\mathrm{e}^{\frac{l}{2x}}\right)^{-1}\right\}$$

2.1268 ODE No. 1268

$$y(x)(ax+b)+2(x-1)xy''(x)+(2x-1)y'(x)=0$$

✗ **Mathematica** : cpu = 1.46146 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\{(xa+b)y(x)+(2x-1)y'(x)+2(x-1)xy''(x)=0,y(2)=c_1,y'(2)=c_2\}\right)($$

✓ **Maple** : cpu = 0.111 (sec), leaf count = 39

$$\left\{y(x)=\_C1\,\mathit{MathieuC}\left(-a-2\,b,\frac{a}{2},\arccos\left(\sqrt{x}\right)\right)+\_C2\,\mathit{MathieuS}\left(-a-2\,b,\frac{a}{2},\arccos\left(\sqrt{x}\right)\right)\right\}$$

2.1269 ODE No. 1269

$$((2v+5)x-2v-3)y'(x)+(v+1)y(x)+2(x-1)xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0858634 (sec), leaf count = 60

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(\frac{1}{2},v+1;v+\frac{3}{2};x\right)+c_2i^{-2v-1}x^{\frac{1}{2}(-2v-1)}\,{}_2F_1\left(\frac{1}{2},-v;\frac{1}{2}-v;x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 40

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(\frac{1}{2},v+1;\,\frac{3}{2}+v;\,x)+\_C2\,x^{-\frac{1}{2}-v}{}_2\mathrm{F}_1(\frac{1}{2},-v;\,\frac{1}{2}-v;\,x)\right\}$$

2.1270 ODE No. 1270

$$\left(2x^2+6x+4\right)y''(x)+\left(10x^2+21x+8\right)y'(x)+\left(12x^2+17x+8\right)y(x)=0$$

✗ **Mathematica** : cpu = 300.006 (sec), leaf count = 0 , timed out

```
$Aborted
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✓ **Maple** : cpu = 0.185 (sec), leaf count = 46

$$\left\{y(x)=\mathrm{e}^{-2x}(x+2)^4\left(\_C2\,(1+x)^{\frac{5}{2}}\,HeunC\left(-1,\frac{5}{2},4,-\frac{7}{4},\frac{7}{2},-1-x\right)+\_C1\,HeunC\left(-1,-\frac{5}{2},4,-\frac{7}{4},\frac{7}{2},-1-\right.\right.$$

2.1271 ODE No. 1271

$$4x^2y''(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0126099 (sec), leaf count = 27

$$\left\{\left\{y(x)\to c_1\sqrt{x}+\frac{1}{2}c_2\sqrt{x}\log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 14

$$\left\{y(x)=\sqrt{x}(\ln(x)\_C2+\_C1)\right\}$$

2.1272 ODE No. 1272

$$\left(4a^2x^2+1\right)y(x)+4x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0129343 (sec), leaf count = 32

$$\left\{\left\{y(x)\to c_1\sqrt{x}J_0(ax)+c_2\sqrt{x}Y_0(ax)\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 23

$$\left\{y(x)=\sqrt{x}(Y_0(ax)\_C2+J_0(ax)\_C1)\right\}$$

2.1273 ODE No. 1273

$$4x^2y''(x) - y(x)\left(-4kx + 4m^2 + x^2 - 1\right) = 0$$

✓ **Mathematica** : cpu = 0.018158 (sec), leaf count = 20

$$\{\{y(x) \to c_1 M_{k,m}(x) + c_2 W_{k,m}(x)\}\}$$

✓ **Maple** : cpu = 0.074 (sec), leaf count = 17

$$\{y(x) = \_C1\, M_{k,\,m}(x) + \_C2\, W_{k,\,m}(x)\}$$

2.1274 ODE No. 1274

$$\left(x - v^2\right) y(x) + 4x^2y''(x) + 4xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.042685 (sec), leaf count = 38

$$\left\{\left\{y(x) \to c_1\Gamma(1-v)J_{-v}\left(\sqrt{x}\right) + c_2\Gamma(v+1)J_v\left(\sqrt{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 19

$$\left\{y(x) = \_C1\, J_v\left(\sqrt{x}\right) + \_C2\, Y_v\left(\sqrt{x}\right)\right\}$$

2.1275 ODE No. 1275

$$y(x)\left(2x(2l - m + 1) - m^2 - x^2 + 1\right) + 4x^2y''(x) + 4xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.0364367 (sec), leaf count = 120

$$\left\{\left\{y(x) \to c_1 e^{\frac{1}{2}\left(\sqrt{m^2-1}\log(x)-x\right)} U\left(\frac{1}{2}\left(-2l + m + \sqrt{m^2-1}\right), \sqrt{m^2-1}+1, x\right) + c_2 e^{\frac{1}{2}\left(\sqrt{m^2-1}\log(x)-x\right)} L_{\frac{1}{2}\left(2l-\sqrt{r}\right.}^{\sqrt{m^2-1}}\right.$$

✓ **Maple** : cpu = 0.159 (sec), leaf count = 53

$$\left\{y(x) = 1\left(\_C2\, W_{l-\frac{m}{2}+\frac{1}{2},\,\frac{1}{2}\sqrt{m-1}\sqrt{m+1}}(x) + \_C1\, M_{l-\frac{m}{2}+\frac{1}{2},\,\frac{1}{2}\sqrt{m-1}\sqrt{m+1}}(x)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1276 ODE No. 1276

$$-4e^x\sqrt{x^3}+4x^2y''(x)-\left(4x^2+1\right)y(x)+4xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0594133 (sec), leaf count = 55

$$\left\{\left\{y(x)\to\frac{c_1e^{-x}}{\sqrt{x}}+\frac{c_2e^x}{2\sqrt{x}}+\frac{e^x\sqrt{x^3}(2x-1)}{4x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 31

$$\left\{y(x)=\sinh\left(x\right)\_C2\frac{1}{\sqrt{x}}+\cosh\left(x\right)\_C1\frac{1}{\sqrt{x}}+\frac{\mathrm{e}^x}{2\,x}\sqrt{x^3}\right\}$$

2.1277 ODE No. 1277

$$-\left(ax^2+1\right)y(x)+4x^2y''(x)+4xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0267687 (sec), leaf count = 51

$$\left\{\left\{y(x)\to\frac{c_1e^{-\frac{\sqrt{a}x}{2}}}{\sqrt{x}}+\frac{c_2e^{\frac{\sqrt{a}x}{2}}}{\sqrt{a}\sqrt{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 27

$$\left\{y(x)=1\left(\_C2\,\cosh\left(\frac{x}{2}\sqrt{a}\right)+\_C1\,\sinh\left(\frac{x}{2}\sqrt{a}\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1278 ODE No. 1278

$$f(x)y(x)+4x^2y''(x)+4xy'(x)=0$$

✗ **Mathematica** : cpu = 0.253691 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + 4*x*Derivative[1][y][x] + 4*x^2*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{f(x)\_Y(x)}{4\,x^2}+\frac{\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{x}+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1279 ODE No. 1279

$$4x^2y''(x)+5xy'(x)-y(x)-\log(x)=0$$

✓ **Mathematica** : cpu = 0.171547 (sec), leaf count = 74

$$\left\{\left\{y(x)\to c_1x^{\frac{1}{2}\left(\frac{\sqrt{17}}{4}-\frac{1}{4}\right)}+c_2x^{\frac{1}{2}\left(-\frac{1}{4}-\frac{\sqrt{17}}{4}\right)}-\frac{256(\log(x)+1)}{\left(\sqrt{17}-1\right)^2\left(1+\sqrt{17}\right)^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.167 (sec), leaf count = 32

$$\left\{y(x)=x^{-\frac{1}{8}+\frac{\sqrt{17}}{8}}\_C2+x^{-\frac{1}{8}-\frac{\sqrt{17}}{8}}\_C1-\ln(x)-1\right\}$$

2.1280 ODE No. 1280

$$4x^2y''(x)-\left(4x^2+12x+3\right)y(x)+8xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0385345 (sec), leaf count = 52

$$\left\{\left\{y(x)\to\frac{c_2e^{-x}\left(4e^{2x}x^2\text{Ei}(-2x)+2x-1\right)}{2x^{3/2}}+c_1e^x\sqrt{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 40

$$\left\{y(x)=(4\,\mathrm{e}^{x}Ei(1,2\,x)\_C2\,x^2+(-2\,x+1)\_C2\,\mathrm{e}^{-x}+\_C1\,x^2\mathrm{e}^{x})x^{-\frac{3}{2}}\right\}$$

2.1281 ODE No. 1281

$$4x^2y''(x)+\left(4x^2-4x-1\right)y(x)-4(2x-1)xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0201112 (sec), leaf count = 28

$$\left\{\left\{y(x)\to\frac{c_1e^x}{\sqrt{x}}+c_2e^x\sqrt{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 15

$$\left\{y(x)=\mathrm{e}^{x}(x\_C2+\_C1)\,\frac{1}{\sqrt{x}}\right\}$$

2.1282 ODE No. 1282

$$4x^3y'(x)+4x^2y''(x)+\left(x^2-4\right)\left(x^2+6\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0231702 (sec), leaf count = 39

$$\left\{\left\{y(x)\to \frac{c_1e^{-\frac{x^2}{4}}}{x^2}+\frac{1}{5}c_2e^{-\frac{x^2}{4}}x^3\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 21

$$\left\{y(x)=\frac{\_C2\,x^5+\_C1}{x^2}\mathrm{e}^{-\frac{x^2}{4}}\right\}$$

2.1283 ODE No. 1283

$$4x^2y''(x)+4x^2\log(x)y'(x)+y(x)\left(x^2\log^2(x)+2x-8\right)-4\sqrt{e^xx^{-x}}x^2=0$$

✓ **Mathematica** : cpu = 0.105657 (sec), leaf count = 90

$$\left\{\left\{y(x)\to c_1e^{x/2}x^{-\frac{x}{2}-1}+\frac{1}{3}c_2e^{x/2}x^{2-\frac{x}{2}}+\frac{1}{9}\left(3x^2\sqrt{e^xx^{-x}}\log(x)-x^2\sqrt{e^xx^{-x}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.138 (sec), leaf count = 48

$$\left\{y(x)=\frac{x^2}{3}\left(\ln\left(x\right)-\frac{1}{3}\right)\sqrt{x^{-x}\mathrm{e}^x}+\mathrm{e}^{\frac{x}{2}}\left(\_C1\,x^{-\frac{x}{2}+2}+\_C2\,x^{-\frac{x}{2}-1}\right)\right\}$$

2.1284 ODE No. 1284

$$(2x+1)^2y''(x)-2(2x+1)y'(x)-12y(x)-3x-1=0$$

✓ **Mathematica** : cpu = 0.0448237 (sec), leaf count = 47

$$\left\{\left\{y(x)\to c_1(2x+1)^3+\frac{c_2}{2x+1}+\frac{-72x^2-56x-7}{192(2x+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 41

$$\left\{y(x)=\frac{\_C1}{2\,x+1}+\left(2\,x+1\right)^3\_C2+\frac{-72\,x^2-56\,x-7}{384\,x+192}\right\}$$

2.1285 ODE No. 1285

$$((4a+2)x-a)y'(x)+(a-1)ay(x)+x(4x-1)y''(x)=0$$

✓ **Mathematica** : cpu = 0.317964 (sec), leaf count = 134

$$\left\{\left\{y(x)\to \frac{2c_1\sqrt[4]{4x-1}x^{\frac{1}{2}-\frac{a}{2}}e^{\sqrt{-(a-1)^2}\tan^{-1}\left(\sqrt{4x-1}\right)}}{\sqrt[4]{1-4x}}-\frac{c_2\sqrt[4]{4x-1}x^{\frac{1}{2}-\frac{a}{2}}e^{-\sqrt{-(a-1)^2}\tan^{-1}\left(\sqrt{4x-1}\right)}}{2\sqrt{-(a-1)^2}\sqrt[4]{1-4x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.102 (sec), leaf count = 52

$$\left\{y(x)=\_C1\ {}_2\mathrm{F}_1(\frac{a}{2},\frac{a}{2}-\frac{1}{2};\ a;\ 4\,x)+\_C2\ x^{1-a}{}_2\mathrm{F}_1(1-\frac{a}{2},-\frac{a}{2}+\frac{1}{2};\ -a+2;\ 4\,x)\right\}$$

2.1286 ODE No. 1286

$$(3x-1)^2y''(x)+3(3x-1)y'(x)-9y(x)-\log^2(3x-1)=0$$

✓ **Mathematica** : cpu = 0.102968 (sec), leaf count = 101

$$\left\{\left\{y(x)\to \frac{c_1\left((1-3x)^2+1\right)}{2(1-3x)}+\frac{ic_2\left((1-3x)^2-1\right)}{2(1-3x)}+\frac{-6x-3x\log^2(3x-1)+\log^2(3x-1)+\log(3x-1)-\log}{9(3x-1)}\right.\right.$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 32

$$\left\{y(x)=\frac{\_C1}{3\,x-1}+(3\,x-1)\,\_C2-\frac{\left(\ln\left(3\,x-1\right)\right)^2}{9}-\frac{2}{9}\right\}$$

2.1287 ODE No. 1287

$$9(x-1)xy''(x)+3(2x-1)y'(x)-20y(x)=0$$

✓ **Mathematica** : cpu = 0.019086 (sec), leaf count = 83

$$\left\{\left\{y(x)\to c_2\sqrt[3]{1-x}\sqrt[3]{x}Q_1^{\frac{2}{3}}(2x-1)-\frac{c_1(2-2x)^{2/3}\sqrt[3]{1-x}x^{2/3}(6x-5)}{3\ 2^{2/3}(x-1)\Gamma\left(\frac{4}{3}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 27

$$\left\{y(x)=\_C1\ (6\,x-5)\,x^{\frac{2}{3}}+\_C2\ (6\,x-1)\,(x-1)^{\frac{2}{3}}\right\}$$

2.1288 ODE No. 1288

$$16x^2y''(x)+(4x+3)y(x)=0$$

✓ **Mathematica** : cpu = 0.0358623 (sec), leaf count = 47

$$\left\{\left\{y(x)\to c_1e^{i\sqrt{x}}\sqrt[4]{x}+ic_2e^{-i\sqrt{x}}\sqrt[4]{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 21

$$\left\{y(x)=\sqrt[4]{x}\left(\cos\left(\sqrt{x}\right)\_C2+\sin\left(\sqrt{x}\right)\_C1\right)\right\}$$

2.1289 ODE No. 1289

$$16x^2y''(x)+32xy'(x)-(4x+5)y(x)=0$$

✓ **Mathematica** : cpu = 0.0786807 (sec), leaf count = 53

$$\left\{\left\{y(x)\to\frac{c_2e^{-\sqrt{x}}\left(\sqrt{x}+1\right)}{x^{5/4}}-\frac{c_1e^{\sqrt{x}}\left(\sqrt{x}-1\right)}{x^{5/4}}\right\}\right\}$$

✓ **Maple** : cpu = 0.085 (sec), leaf count = 33

$$\left\{y(x)=1\left(\_C2\left(\sqrt{x}+1\right)\mathrm{e}^{-\sqrt{x}}+\_C1\,\mathrm{e}^{\sqrt{x}}\left(\sqrt{x}-1\right)\right)x^{-\frac{5}{4}}\right\}$$

2.1290 ODE No. 1290

$$\left(27x^2+4\right)y''(x)+27xy'(x)-3y(x)=0$$

✓ **Mathematica** : cpu = 0.164912 (sec), leaf count = 103

$$\left\{\left\{y(x)\to c_1\cosh\left(\frac{\sqrt{-27x^2-4}\tan^{-1}\left(\frac{3x}{\sqrt{-9x^2-\frac{4}{3}}}\right)}{3\sqrt{27x^2+4}}\right)+ic_2\sinh\left(\frac{\sqrt{-27x^2-4}\tan^{-1}\left(\frac{3x}{\sqrt{-9x^2-\frac{4}{3}}}\right)}{3\sqrt{27x^2+4}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 47

$$\left\{y(x)=\_C1\,\sin\left(\frac{1}{3}\arctan\left(3\,\frac{\sqrt{3}x}{\sqrt{-27\,x^2-4}}\right)\right)+\_C2\,\cos\left(\frac{1}{3}\arctan\left(3\,\frac{\sqrt{3}x}{\sqrt{-27\,x^2-4}}\right)\right)\right\}$$

2.1291 ODE No. 1291

$$48(x-1)xy''(x)+(152x-40)y'(x)+53y(x)=0$$

✓ **Mathematica** : cpu = 0.0725476 (sec), leaf count = 92

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(\frac{13}{12}-\frac{\sqrt{\frac{5}{2}}}{6},\frac{13}{12}+\frac{\sqrt{\frac{5}{2}}}{6};\frac{5}{6};x\right)+\sqrt[6]{-1}c_2\sqrt[6]{x}\,{}_2F_1\left(\frac{5}{4}-\frac{\sqrt{\frac{5}{2}}}{6},\frac{5}{4}+\frac{\sqrt{\frac{5}{2}}}{6};\frac{7}{6};x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 62

$$\left\{y(x)=\_C1\ {}_2\mathrm{F}_1(\frac{13}{12}-\frac{\sqrt{5}\sqrt{2}}{12},\frac{13}{12}+\frac{\sqrt{5}\sqrt{2}}{12};\frac{5}{6};x)+\_C2\ \sqrt[6]{x}{}_2\mathrm{F}_1(\frac{5}{4}-\frac{\sqrt{5}\sqrt{2}}{12},\frac{5}{4}+\frac{\sqrt{5}\sqrt{2}}{12};\frac{7}{6};x)\right\}$$

2.1292 ODE No. 1292

$$50(x-1)xy''(x)+25(2x-1)y'(x)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.0401798 (sec), leaf count = 53

$$\left\{\left\{y(x)\to c_1\cosh\left(\frac{2}{5}\log\left(\sqrt{x-1}+\sqrt{x}\right)\right)+ic_2\sinh\left(\frac{2}{5}\log\left(\sqrt{x-1}+\sqrt{x}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.06 (sec), leaf count = 31

$$\left\{y(x)=1\left(\_C1\left(\sqrt{x}+\sqrt{x-1}\right)^{\frac{4}{5}}+\_C2\right)\left(\sqrt{x}+\sqrt{x-1}\right)^{-\frac{2}{5}}\right\}$$

2.1293 ODE No. 1293

$$144(x-1)xy''(x)+(120x-48)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.324136 (sec), leaf count = 44

$$\left\{\left\{y(x)\to(-1)^{2/3}c_2x^{2/3}\,{}_2F_1\left(\frac{7}{12},\frac{7}{12};\frac{5}{3};x\right)+c_1\,{}_2F_1\left(-\frac{1}{12},-\frac{1}{12};\frac{1}{3};x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.073 (sec), leaf count = 33

$$\left\{y(x)=\sqrt[3]{x}\left(LegendreP\left(-\frac{1}{2},\frac{2}{3},\sqrt{1-x}\right)\_C1+LegendreQ\left(-\frac{1}{2},\frac{2}{3},\sqrt{1-x}\right)\_C2\right)\right\}$$

2.1294 ODE No. 1294

$$144(x-1)xy''(x)+(168x-96)y'(x)+y(x)=0$$

✓ **Mathematica** : cpu = 0.0659441 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(\frac{1}{12},\frac{1}{12};\frac{2}{3};x\right)+\sqrt[3]{-1}c_2\sqrt[3]{x}\,{}_2F_1\left(\frac{5}{12},\frac{5}{12};\frac{4}{3};x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 33

$$\left\{y(x)=\sqrt[6]{x}\left(LegendreP\left(-\frac{1}{2},\frac{1}{3},\sqrt{1-x}\right)\_C1+LegendreQ\left(-\frac{1}{2},\frac{1}{3},\sqrt{1-x}\right)\_C2\right)\right\}$$

2.1295 ODE No. 1295

$$ax^2y''(x)+bxy'(x)+y(x)\left(cx^2+dx+f\right)=0$$

✓ **Mathematica** : cpu = 0.256552 (sec), leaf count = 310

$$\left\{\left\{y(x)\to c_1U\left(-\frac{-\sqrt{c}a-id\sqrt{a}-\sqrt{c}\sqrt{a^2-2ba-4fa+b^2}}{2a\sqrt{c}},\frac{\sqrt{a^2-2ba-4fa+b^2}}{a}+1,\frac{2i\sqrt{c}x}{\sqrt{a}}\right)\exp\left(\frac{\log(x)\right.\right.\right.$$

✓ **Maple** : cpu = 0.302 (sec), leaf count = 106

$$\left\{y(x)=x^{-\frac{b}{2a}}\left(M_{-\frac{i}{2}d\frac{1}{\sqrt{c}}\frac{1}{\sqrt{a}},\frac{1}{2a}\sqrt{a^2+(-2b-4f)a+b^2}}\left(2ix\sqrt{c}\frac{1}{\sqrt{a}}\right)\_C1+W_{-\frac{i}{2}d\frac{1}{\sqrt{c}}\frac{1}{\sqrt{a}},\frac{1}{2a}\sqrt{a^2+(-2b-4f)a+b^2}}\left(2ix\sqrt{c}\frac{1}{\sqrt{}}\right.\right.\right.$$

2.1296 ODE No. 1296

$$y(x)\left(\mathrm{a0}x^2+\mathrm{b0}x+\mathrm{c0}\right)+\left(\mathrm{a1}x^2+\mathrm{b1}x\right)y'(x)+\mathrm{a2}x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.531119 (sec), leaf count = 356

$$\left\{\left\{y(x)\to c_1U\left(-\frac{2\mathrm{b0a2}-\sqrt{\mathrm{a1}^2-4\mathrm{a0a2}}\mathrm{a2}-\mathrm{a1b1}-\sqrt{\mathrm{a1}^2-4\mathrm{a0a2}}\sqrt{\mathrm{a2}^2-2\mathrm{b1a2}-4\mathrm{c0a2}+\mathrm{b1}^2}}{2\mathrm{a2}\sqrt{\mathrm{a1}^2-4\mathrm{a0a2}}},\frac{\sqrt{\mathrm{a2}^2-2\mathrm{b1}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.347 (sec), leaf count = 150

$$\left\{y(x)=x^{-\frac{b1}{2\,a2}}\mathrm{e}^{-\frac{a1\,x}{2\,a2}}\left(M_{-\frac{a1\,b1-2\,a2\,b0}{2\,a2}\frac{1}{\sqrt{-4\,a0\,a2+a1^2}},\frac{1}{2\,a2}\sqrt{a2^2+(-2\,b1-4\,c0)a2+b1^2}}\left(\frac{x}{a2}\sqrt{-4\,a0\,a2+a1^2}\right)\_C1+W_{-\frac{a}{}}\right.\right.\right.$$

2.1297 ODE No. 1297

$$\left(ax^2+1\right)y''(x)+axy'(x)+by(x)=0$$

✓ **Mathematica** : cpu = 0.0340842 (sec), leaf count = 52

$$\left\{\left\{y(x)\to c_2\sin\left(\frac{\sqrt{b}\sinh^{-1}\left(\sqrt{a}x\right)}{\sqrt{a}}\right)+c_1\cos\left(\frac{\sqrt{b}\sinh^{-1}\left(\sqrt{a}x\right)}{\sqrt{a}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 63

$$\left\{y(x)=1\left(\_C1\left(\left(\sqrt{a}x+\sqrt{ax^2+1}\right)^{i\sqrt{b}\frac{1}{\sqrt{a}}}\right)^2+\_C2\right)\left(\left(\sqrt{a}x+\sqrt{ax^2+1}\right)^{i\sqrt{b}\frac{1}{\sqrt{a}}}\right)^{-1}\right\}$$

2.1298 ODE No. 1298

$$\left(ax^2+1\right)y''(x)+bxy'(x)+cy(x)=0$$

✓ **Mathematica** : cpu = 0.0781883 (sec), leaf count = 162

$$\left\{\left\{y(x)\to c_1\left(ax^2+1\right)^{\frac{2a-b}{4a}}P^{\frac{b-2a}{2a}}_{\frac{\sqrt{a^2-2ba-4ca+b^2}-a}{2a}}\left(i\sqrt{a}x\right)+c_2\left(ax^2+1\right)^{\frac{2a-b}{4a}}Q^{\frac{b-2a}{2a}}_{\frac{\sqrt{a^2-2ba-4ca+b^2}-a}{2a}}\left(i\sqrt{a}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.125 (sec), leaf count = 124

$$\left\{y(x)=\left(ax^2+1\right)^{\frac{2a-b}{4a}}\left(LegendreP\left(\frac{1}{2a}\left(\sqrt{a^2+\left(-2b-4c\right)a+b^2}-a\right),\frac{2a-b}{2a},\sqrt{-a}x\right)\_C1+LegendreQ\left(\frac{2}{2}\right.\right.\right.$$

2.1299 ODE No. 1299

$$\left(a^2x^2-1\right)y''(x)+2a^2xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0143755 (sec), leaf count = 19

$$\left\{\left\{y(x)\to c_2-\frac{c_1\tanh^{-1}(ax)}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 27

$$\left\{y(x)=\_C1-\frac{\left(\ln\left(ax+1\right)-\ln\left(ax-1\right)\right)\_C2}{2a}\right\}$$

2.1300 ODE No. 1300

$$\left(a^2x^2-1\right)y''(x)+2a^2xy'(x)-2a^2y(x)=0$$

✓ **Mathematica** : cpu = 0.0155044 (sec), leaf count = 41

$$\left\{\left\{y(x)\to ac_1x+c_2\left(ax\left(\frac{1}{2}\log(ax+1)-\frac{1}{2}\log(1-ax)\right)-1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 31

$$\left\{y(x)=-\frac{\_C2\,a\ln\left(ax+1\right)x}{2}+\frac{\_C2\,a\ln\left(ax-1\right)x}{2}+\_C1\,x+\_C2\right\}$$

2.1301 ODE No. 1301

$$\left(ax^2+bx\right)y''(x)-2ay(x)+2by'(x)=0$$

✓ **Mathematica** : cpu = 0.034249 (sec), leaf count = 31

$$\left\{\left\{y(x)\to \frac{c_2(ax+b)^3}{3ax}+\frac{c_1}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.023 (sec), leaf count = 19

$$\left\{y(x)=\frac{\_C1+\_C2\left(ax+b\right)^3}{x}\right\}$$

2.1302 ODE No. 1302

$$\mathrm{A0}y(x)(ax+b)+\mathrm{A1}(ax+b)y'(x)+\mathrm{A2}(ax+b)^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0840161 (sec), leaf count = 243

$$\left\{\left\{y(x)\to c_1\left(\frac{2b}{a}+2x\right)^{\frac{\mathrm{A1}}{2a\mathrm{A2}}}(2a\mathrm{A2}x+2\mathrm{A2}b)^{-\frac{\mathrm{A1}}{2a\mathrm{A2}}}\left(-\frac{\mathrm{A0}\left(\frac{b}{a}+x\right)}{a\mathrm{A2}}\right)^{\frac{1}{2}-\frac{\mathrm{A1}}{2a\mathrm{A2}}}I_{\frac{\mathrm{A1}}{a\mathrm{A2}}-1}\left(2\sqrt{-\frac{\mathrm{A0}\left(\frac{b}{a}+x\right)}{a\mathrm{A2}}}\right)+c_2(-1\right.\right.$$

✓ **Maple** : cpu = 0.061 (sec), leaf count = 98

$$\left\{y(x)=(ax+b)^{-\frac{-aA2+A1}{2\,aA2}}\left(J_{\frac{aA2-A1}{aA2}}\left(2\sqrt{A0}\sqrt{\frac{ax+b}{a^2A2}}\right)\_C1+Y_{\frac{aA2-A1}{aA2}}\left(2\sqrt{A0}\sqrt{\frac{ax+b}{a^2A2}}\right)\_C2\right)\right\}$$

2.1303 ODE No. 1303

$$y''(x)\left(ax^2+bx+c\right)+(dx+f)y'(x)+gy(x)=0$$

✗ **Mathematica** : cpu = 14.6264 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{gy(x)+(xd+f)y'(x)+\left(ax^2+bx+c\right)y''(x)=0,y(0)=c_1,y'(0)=c_2\right\}\right)(x\right.\right.$$

✓ **Maple** : cpu = 0.225 (sec), leaf count = 501

$$\left\{y(x)=\_C1\ {}_2\mathrm{F}_1\left(-\frac{1}{2\,a}\left(a-d+\sqrt{a^2+\left(-2\,d-4\,g\right)a+d^2}\right),\frac{1}{2\,a}\left(-a+d+\sqrt{a^2+\left(-2\,d-4\,g\right)a+d^2}\right);\ \frac{1}{2\,a^2}\left(\right.\right.\right.$$

2.1304 ODE No. 1304

$$x^3y''(x)+xy'(x)-(2x+3)y(x)=0$$

✓ **Mathematica** : cpu = 0.0342787 (sec), leaf count = 50

$$\left\{\left\{y(x)\to \frac{c_2\left(e^{\frac{1}{x}}\text{Ei}\left(-\frac{1}{x}\right)+2x^3-x^2+x\right)}{6x}+\frac{c_1e^{\frac{1}{x}}}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 38

$$\left\{y(x)=\frac{1}{x}\left(Ei\left(1,x^{-1}\right)\mathrm{e}^{x^{-1}}\_C2+\_C1\,\mathrm{e}^{x^{-1}}-2\left(x^2-x/2+1/2\right)x\_C2\right)\right\}$$

2.1305 ODE No. 1305

$$x^3y''(x)+2xy'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.0723223 (sec), leaf count = 47

$$\left\{\left\{y(x)\to c_2G_{1,2}^{2,0}\left(-\frac{2}{x}\middle|\begin{array}{c}\frac{1}{2}\\-1,0\end{array}\right)+c_1e^{\frac{1}{x}}\left(I_0\left(\frac{1}{x}\right)-I_1\left(\frac{1}{x}\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 44

$$\left\{y(x)=\mathrm{e}^{x^{-1}}\left(-\_C2\,K_1\left(-x^{-1}\right)+\_C2\,K_0\left(-x^{-1}\right)+\_C1\,\left(I_0\left(x^{-1}\right)-I_1\left(x^{-1}\right)\right)\right)\right\}$$

2.1306 ODE No. 1306

$$y(x)\left(ax^2+a+bx\right)+x^3y''(x)+x^2y'(x)=0$$

✗ **Mathematica** : cpu = 1.00491 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{y''(x)x^3+y'(x)x^2+\left(ax^2+bx+a\right)y(x)=0,y(1)=c_1,y'(1)=c_2\right\}\right)(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.158 (sec), leaf count = 69

$$\left\{y(x)=HeunD\left(0,8\,a+4\,b,0,8\,a-4\,b,\frac{1+x}{x-1}\right)\left(\int\frac{1}{x}\left(HeunD\left(0,8\,a+4\,b,0,8\,a-4\,b,\frac{1+x}{x-1}\right)\right)^{-2}\mathrm{d}x\_C2+\_\right.\right.$$

2.1307 ODE No. 1307

$$x^3y''(x)+(x+1)xy'(x)-2y(x)=0$$

✓ **Mathematica** : cpu = 0.085608 (sec), leaf count = 54

$$\left\{\left\{y(x)\to \frac{c_1e^{\frac{1}{x}}(x+1)}{x}-\frac{c_2\left(e^{\frac{1}{x}}x\text{Ei}\left(-\frac{1}{x}\right)+e^{\frac{1}{x}}\text{Ei}\left(-\frac{1}{x}\right)+x\right)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 36

$$\left\{y(x)=\frac{\_C2\,\mathrm{e}^{x^{-1}}(1+x)\,Ei\left(1,x^{-1}\right)+\_C1\,(1+x)\,\mathrm{e}^{x^{-1}}-\_C2\,x}{x}\right\}$$

2.1308 ODE No. 1308

$$x^3y''(x)-x^2y'(x)+xy(x)-\log^3(x)=0$$

✓ **Mathematica** : cpu = 0.0216775 (sec), leaf count = 41

$$\left\{\left\{y(x)\to c_1x+c_2x\log(x)+\frac{2\log^3(x)+6\log^2(x)+9\log(x)+6}{8x}\right\}\right\}$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 40

$$\left\{y(x)=\frac{2\left(\ln\left(x\right)\right)^3+6\left(\ln\left(x\right)\right)^2+\left(8\_C1\,x^2+9\right)\ln\left(x\right)+8\_C2\,x^2+6}{8\,x}\right\}$$

2.1309 ODE No. 1309

$$x^3 y''(x) - \left(x^2 - 1\right) y'(x) + x y(x) = 0$$

✓ **Mathematica** : cpu = 0.0831518 (sec), leaf count = 84

$$\left\{\left\{y(x) \to c_2 G_{1,2}^{2,0}\left(-\frac{1}{2x^2}\middle| \begin{matrix} 1 \\ -\frac{1}{2}, -\frac{1}{2} \end{matrix}\right) + \sqrt{2} c_1 e^{\frac{1}{4x^2}} x \left(\left(1 - \frac{1}{2x^2}\right) I_0\left(\frac{1}{4x^2}\right) + \frac{I_1\left(\frac{1}{4x^2}\right)}{2x^2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.094 (sec), leaf count = 85

$$\left\{y(x) = \frac{\_C1}{x} \mathrm{e}^{\frac{1}{4\,x^2}} \left(2\,x^2 I_0(1/4\,x^{-2}) + I_1\left(\frac{1}{4\,x^2}\right) - I_0\left(\frac{1}{4\,x^2}\right)\right) + \frac{\_C2}{x} \mathrm{e}^{\frac{1}{4\,x^2}} \left(2\,K_0(-1/4\,x^{-2}) x^2 + K_1\left(-\frac{1}{4\,x^2}\right)\right.\right.$$

2.1310 ODE No. 1310

$$x^3 y''(x) + 3x^2 y'(x) + x y(x) - 1 = 0$$

✓ **Mathematica** : cpu = 0.0133391 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{c_1}{x} + \frac{c_2 \log(x)}{x} + \frac{\log^2(x)}{2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 20

$$\left\{y(x) = \frac{1}{x}\left(\frac{(\ln(x))^2}{2} + \_C1\ \ln(x) + \_C2\right)\right\}$$

2.1311 ODE No. 1311

$$-v(v+1)x y(x) + x\left(x^2+1\right) y''(x) + \left(2x^2+1\right) y'(x) = 0$$

✓ **Mathematica** : cpu = 0.134065 (sec), leaf count = 63

$$\left\{\left\{y(x) \to c_2 G_{2,2}^{2,0}\left(-x^2\middle| \begin{matrix} \frac{1-v}{2}, \frac{v+2}{2} \\ 0, 0 \end{matrix}\right) + c_1\, {}_2F_1\left(\frac{v}{2} + \frac{1}{2}, -\frac{v}{2}; 1; -x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.15 (sec), leaf count = 52

$$\left\{y(x) = \_C1\ {}_2\mathrm{F}_1(-\frac{v}{2}, \frac{1}{2} + \frac{v}{2}; \frac{1}{2}; x^2+1) + \_C2\ \sqrt{x^2+1}\,{}_2\mathrm{F}_1(1 + \frac{v}{2}, \frac{1}{2} - \frac{v}{2}; \frac{3}{2}; x^2+1)\right\}$$

2.1312 ODE No. 1312

$$x\left(x^2+1\right)y''(x)+2\left(x^2-1\right)y'(x)-2xy(x)=0$$

✓ **Mathematica** : cpu = 0.0245618 (sec), leaf count = 32

$$\left\{\left\{y(x)\to \frac{c_1}{x^2+1}+\frac{c_2x^3}{3\left(x^2+1\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 19

$$\left\{y(x)=\frac{\_C2\,x^3+\_C1}{x^2+1}\right\}$$

2.1313 ODE No. 1313

$$x(-(v-n))(n+v+1)y(x)+\left(2(n+1)x^2+2n+1\right)y'(x)+x\left(x^2+1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.210615 (sec), leaf count = 87

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(\frac{n}{2}-\frac{v}{2},\frac{n}{2}+\frac{v}{2}+\frac{1}{2};n+1;-x^2\right)+c_2x^{-2n}\,{}_2F_1\left(-\frac{n}{2}-\frac{v}{2},-\frac{n}{2}+\frac{v}{2}+\frac{1}{2};1-n;-x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 35

$$\left\{y(x)=x^{-n}\left(LegendreQ\left(v,n,\sqrt{x^2+1}\right)\_C2+LegendreP\left(v,n,\sqrt{x^2+1}\right)\_C1\right)\right\}$$

2.1314 ODE No. 1314

$$x(n-v-1)(n+v)y(x)-\left(2(n-1)x^2+2n-1\right)y'(x)+x\left(x^2+1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.188528 (sec), leaf count = 87

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(-\frac{n}{2}-\frac{v}{2},-\frac{n}{2}+\frac{v}{2}+\frac{1}{2};1-n;-x^2\right)+c_2x^{2n}\,{}_2F_1\left(\frac{n}{2}-\frac{v}{2},\frac{n}{2}+\frac{v}{2}+\frac{1}{2};n+1;-x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.083 (sec), leaf count = 33

$$\left\{y(x)=x^{n}\left(LegendreQ\left(v,n,\sqrt{x^2+1}\right)\_C2+LegendreP\left(v,n,\sqrt{x^2+1}\right)\_C1\right)\right\}$$

2.1315 ODE No. 1315

$$ax^3y(x)+\left(x^2-1\right)xy''(x)+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0280829 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_2\sin\left(\sqrt{a}\sqrt{x^2-1}\right)+c_1\cos\left(\sqrt{a}\sqrt{x^2-1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 45

$$\left\{y(x)=\_C1\ \sin\left(\left(1+x\right)\left(x-1\right)\sqrt{a}\frac{1}{\sqrt{x^2-1}}\right)+\_C2\ \cos\left(\left(1+x\right)\left(x-1\right)\sqrt{a}\frac{1}{\sqrt{x^2-1}}\right)\right\}$$

2.1316 ODE No. 1316

$$x\left(x^2-1\right)y''(x)+\left(x^2-1\right)y'(x)-xy(x)=0$$

✓ **Mathematica** : cpu = 0.0944366 (sec), leaf count = 38

$$\left\{\left\{y(x)\to c_2G_{2,2}^{2,0}\left(x^2\middle|\begin{array}{c}\frac{1}{2},\frac{3}{2}\\0,0\end{array}\right)+\frac{2c_1E\left(x^2\right)}{\pi}\right\}\right\}$$

✓ **Maple** : cpu = 0.041 (sec), leaf count = 18

$$\{y(x)=\_C1\ EllipticE(x)+\_C2\ (EllipticCE(x)-EllipticCK(x))\}$$

2.1317 ODE No. 1317

$$x\left(x^2-1\right)y''(x)+\left(3x^2-1\right)y'(x)+xy(x)=0$$

✓ **Mathematica** : cpu = 0.127403 (sec), leaf count = 38

$$\left\{\left\{y(x)\to c_2G_{2,2}^{2,0}\left(x^2\middle|\begin{array}{c}\frac{1}{2},\frac{1}{2}\\0,0\end{array}\right)+\frac{2c_1K\left(x^2\right)}{\pi}\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 13

$$\{y(x)=\_C1\ EllipticK(x)+\_C2\ EllipticCK(x)\}$$

2.1318 ODE No. 1318

$$\left(ax^2+b\right)y'(x)+cxy(x)+x\left(x^2-1\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.296062 (sec), leaf count = 172

$$\left\{\left\{y(x)\to c_1\,{}_2F_1\left(\frac{a}{4}-\frac{1}{4}\sqrt{a^2-2a-4c+1}-\frac{1}{4},\frac{a}{4}+\frac{1}{4}\sqrt{a^2-2a-4c+1}-\frac{1}{4};\frac{1}{2}-\frac{b}{2};x^2\right)+i^{b+1}c_2x^{b+1}\,{}_2F_1\left(\frac{a}{4}\right.\right.\right.$$

✓ **Maple** : cpu = 0.141 (sec), leaf count = 122

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_1(-\frac{1}{4}+\frac{a}{4}+\frac{1}{4}\sqrt{a^2-2\,a-4\,c+1},-\frac{1}{4}+\frac{a}{4}-\frac{1}{4}\sqrt{a^2-2\,a-4\,c+1};\,-\frac{b}{2}+\frac{1}{2};\,x^2)+\_C2\,x^{b+1}{}_2\right.$$

2.1319 ODE No. 1319

$$x\left(x^2+2\right)y''(x)-y'(x)-6xy(x)=0$$

✓ **Mathematica** : cpu = 0.10006 (sec), leaf count = 118

$$\left\{\left\{y(x)\to\frac{c_2\left(-2\sqrt[4]{2}x^2\,{}_2F_1\left(\frac{1}{4},\frac{3}{4};\frac{5}{4};-\frac{x^2}{2}\right)-\sqrt[4]{2}x^4\,{}_2F_1\left(\frac{1}{4},\frac{3}{4};\frac{5}{4};-\frac{x^2}{2}\right)-\sqrt[4]{x^2+2}x^2-\sqrt[4]{x^2+2}\right)}{3\sqrt[4]{x^2+2}}+c_1\left(x^2+2\right)^{3/4}\right.\right.$$

✓ **Maple** : cpu = 0.116 (sec), leaf count = 31

$$\left\{y(x)=\left(x^2+2\right)^{\frac{3}{4}}\left(x^{\frac{3}{2}}\_C1+{}_2\mathrm{F}_1(-\frac{3}{4},\frac{7}{4};\,\frac{1}{4};\,-\frac{x^2}{2})\_C2\right)\right\}$$

2.1320 ODE No. 1320

$$x\left(x^2-2\right)y''(x)+\left(x^2+4x+2\right)y(x)-\left(x^3+3x^2-2x-2\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0692582 (sec), leaf count = 21

$$\left\{\left\{y(x)\to c_1e^xx^2+c_2(x-1)\right\}\right\}$$

✓ **Maple** : cpu = 0.047 (sec), leaf count = 17

$$\left\{y(x)=\_C1\,(x-1)+\_C2\,\mathrm{e}^x x^2\right\}$$

2.1321 ODE No. 1321

$$(x+1)x^2y''(x)-(2x+1)xy'(x)+(2x+1)y(x)=0$$

✓ **Mathematica** : cpu = 0.0282112 (sec), leaf count = 18

$$\{\{y(x)\to c_1x+c_2x(x+\log(x))\}\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 15

$$\{y(x)=x(\_C2\ \ln(x)+\_C2\ x+\_C1)\}$$

2.1322 ODE No. 1322

$$(x+1)x^2y''(x)+2(3x+2)xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0326516 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_1\left(-\frac{1}{3x^3}+\frac{1}{x^2}-\frac{3}{x}-\frac{1}{x+1}-4\log(x)+4\log(x+1)\right)+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 44

$$\left\{y(x)=\_C1+\left(-4\ \ln(x)+4\ \ln(1+x)-\frac{12\,x^3+6\,x^2-2\,x+1}{3\,x^3\,(1+x)}\right)\_C2\right\}$$

2.1323 ODE No. 1323

$$y''(x)=\frac{2(x+1)y(x)}{(x-1)x}-\frac{2(x-2)y'(x)}{(x-1)x}$$

✗ **Mathematica** : cpu = 0.747315 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x)\to \text{DifferentialRoot}\{\{y,x\},\{(-2x-2)y(x)+(2x-4)y'(x)+(x-1)xy''(x)=0,y(2)=c_1,y'(2)=c_2\}\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 17

$$\left\{y(x)=\frac{\_C1+\_C2\ (x-1)^3}{x^2}\right\}$$

2.1324 ODE No. 1324

$$y''(x) = \frac{(5x-4)y'(x)}{(x-1)x} - \frac{(9x-6)y(x)}{(x-1)x^2}$$

✓ **Mathematica** : cpu = 0.0302777 (sec), leaf count = 25

$$\{\{y(x) \to c_1 x^3 - c_2 x^2 (x \log(x) + 1)\}\}$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 18

$$\{y(x) = x^2(\ln(x)\_C2\, x + \_C1\, x + \_C2)\}$$

2.1325 ODE No. 1325

$$y''(x) = -\frac{y(x)(abx - \alpha\beta)}{(x-1)x^2} - \frac{y'(x)(x(a+b+1)+\alpha+\beta-1)}{(x-1)x}$$

✓ **Mathematica** : cpu = 0.266776 (sec), leaf count = 52

$$\left\{\left\{y(x) \to (-1)^{\alpha} c_1 x^{\alpha}\, {}_2F_1(a+\alpha, \alpha+b; \alpha-\beta+1; x) + (-1)^{\beta} c_2 x^{\beta}\, {}_2F_1(a+\beta, b+\beta; -\alpha+\beta+1; x)\right\}\right\}$$

✓ **Maple** : cpu = 0.137 (sec), leaf count = 86

$$\left\{y(x) = (x-1)^{1-a-\alpha-b-\beta}\left({}_2\mathrm{F}_1(1-\alpha-b, 1-a-\alpha;\, 1+\beta-\alpha;\, x) x^{\beta} \_C2 + {}_2\mathrm{F}_1(1-b-\beta, 1-a-\beta;\, 1-\beta+\right.\right.$$

2.1326 ODE No. 1326

$$y''(x) = -\frac{y'(x)}{x+1} - \frac{y(x)}{x(x+1)^2}$$

✓ **Mathematica** : cpu = 0.0255861 (sec), leaf count = 29

$$\left\{\left\{y(x) \to \frac{c_1 x}{x+1} + \frac{c_2(x\log(x)-1)}{x+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 22

$$\left\{y(x) = \frac{\ln(x)\_C2\, x + \_C1\, x - \_C2}{1+x}\right\}$$

2.1327 ODE No. 1327

$$y''(x) = \frac{2y'(x)}{(x-2)x} - \frac{y(x)}{(x-2)x^2}$$

✓ **Mathematica** : cpu = 0.169255 (sec), leaf count = 104

$$\left\{\left\{y(x) \to \left(-\frac{1}{2}\right)^{-\frac{1}{\sqrt{2}}} c_1 x^{-\frac{1}{\sqrt{2}}} {}_2F_1\left(-\frac{1}{\sqrt{2}}, -1-\frac{1}{\sqrt{2}}; 1-\sqrt{2}; \frac{x}{2}\right) + \left(-\frac{1}{2}\right)^{\frac{1}{\sqrt{2}}} c_2 x^{\frac{1}{\sqrt{2}}} {}_2F_1\left(\frac{1}{\sqrt{2}}, -1+\frac{1}{\sqrt{2}}; 1+\sqrt{2};\right.\right.$$

✓ **Maple** : cpu = 0.127 (sec), leaf count = 81

$$\left\{y(x) = (x-2)^2 \left(\_C1\ {}_2\mathrm{F}_1(2-\frac{\sqrt{2}}{2}, 1-\frac{\sqrt{2}}{2};\ 1-\sqrt{2};\ \frac{x}{2}) x^{-\frac{\sqrt{2}}{2}} + \_C2\ {}_2\mathrm{F}_1(2+\frac{\sqrt{2}}{2}, 1+\frac{\sqrt{2}}{2};\ 1+\sqrt{2};\ \frac{x}{2}) x^{\frac{\sqrt{2}}{2}}\right)\right.$$

2.1328 ODE No. 1328

$$y''(x) = \frac{2y(x)}{(x-1)^2 x}$$

✓ **Mathematica** : cpu = 0.0230374 (sec), leaf count = 36

$$\left\{\left\{y(x) \to \frac{c_2\left(-x^2 + 2x\log(x) + 1\right)}{x-1} - \frac{c_1 x}{x-1}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 27

$$\left\{y(x) = \frac{2\ln(x)\ \_C2\ x - \_C2\ x^2 + \_C1\ x + \_C2}{x-1}\right\}$$

2.1329 ODE No. 1329

$$y''(x) = -\frac{y'(x)\left(-x(a(\delta+\text{gamma1})+\alpha+\beta-\delta+1)+a\text{gamma1}+x^2(\alpha+\beta+1)\right)}{(x-1)x(x-a)} - \frac{y(x)(\alpha\beta x - q)}{(x-1)x(x-a)}$$

✗ **Mathematica** : cpu = 6.56692 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x) \to \text{DifferentialRoot}\{\{y, x\}, \{(x\alpha\beta - q)y(x) + (\alpha x^2 + \beta x^2 + x^2 - \alpha x - \beta x - a\delta x + \delta x - a\text{gamma1}x - x$$

✓ **Maple** : cpu = 0.377 (sec), leaf count = 64

$$\{y(x) = \_C1\ HeunG(a, q, \alpha, \beta, \gamma 1, \delta, x) + \_C2\ x^{1-\gamma 1} HeunG(a, q-(-1+\gamma 1)(\delta(a-1)+\alpha+\beta-\gamma 1+1), \beta+$$

2.1330 ODE No. 1330

$$y''(x) = -\frac{y'(x)\left(Ax^2+Bx+C\right)}{(x-a)(x-b)(x-c)} - \frac{(\mathrm{DD}x+e)y(x)}{(x-a)(x-b)(x-c)}$$

✗ **Mathematica** : cpu = 187.149 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\left\{(x\mathrm{DD}+e)y(x)+\left(Ax^2+Bx+C\right)y'(x)-(a-x)(b-x)(c-x)y''(x)=0,y\right.\right.$$

✓ **Maple** : cpu = 1.211 (sec), leaf count = 1147

$$\left\{y(x) = \_C1\ HeunG\left(\frac{a-c}{a-b},\frac{DD\,a+E}{a-b},\frac{A}{2}-\frac{1}{2}+\frac{1}{2}\sqrt{A^2-2\,A-4\,DD+1},1\left(\left(A(b-c)\,a-Abc-Bc-C\right)\sqrt{A}\right.\right.\right.$$

2.1331 ODE No. 1331

$$y''(x) = \frac{(x-4)y'(x)}{2(x-2)x} - \frac{(x-3)y(x)}{2(x-2)x^2}$$

✓ **Mathematica** : cpu = 0.0460137 (sec), leaf count = 55

$$\left\{\left\{y(x) \to \frac{c_1\sqrt[4]{x-2}\sqrt{x}}{\sqrt[4]{2-x}} + \frac{2c_2(x-2)^{3/4}\sqrt{x}}{\sqrt[4]{2-x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 19

$$\left\{y(x) = \_C1\ \sqrt{x} + \_C2\ \sqrt{x\,(x-2)}\right\}$$

2.1332 ODE No. 1332

$$y''(x) = \frac{y'(x)}{x+1} - \frac{(3x+1)y(x)}{4x^2(x+1)}$$

✓ **Mathematica** : cpu = 0.0257016 (sec), leaf count = 26

$$\{\{y(x) \to c_1\sqrt{x} + c_2\sqrt{x}(x+\log(x))\}\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 17

$$\{y(x) = \sqrt{x}(\_C2\ \ln(x) + \_C2\,x + \_C1)\}$$

2.1333 ODE No. 1333

$$y''(x) = \frac{v(v+1)y(x)}{4x^2} - \frac{(3x-1)y'(x)}{2(x-1)x}$$

✓ **Mathematica** : cpu = 0.116175 (sec), leaf count = 70

$$\left\{\left\{y(x) \to c_1 i^{-v} x^{-v/2}\, {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2}-v; x\right) + c_2 i^{v+1} x^{\frac{v+1}{2}}\, {}_2F_1\left(\frac{1}{2}, v+1; v+\frac{3}{2}; x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.078 (sec), leaf count = 45

$$\left\{y(x) = \_C1\, x^{-\frac{v}{2}} {}_2\mathrm{F}_1(\tfrac{1}{2}, -v;\ \tfrac{1}{2}-v;\ x) + \_C2\, x^{\frac{1}{2}+\frac{v}{2}} {}_2\mathrm{F}_1(\tfrac{1}{2}, v+1;\ \tfrac{3}{2}+v;\ x)\right\}$$

2.1334 ODE No. 1334

$$y''(x) = -\frac{y(x)\left(x(a^2-b^2)+c^2\right)}{4(x-1)x^2} - \frac{((a+1)x-1)y'(x)}{(x-1)x}$$

✓ **Mathematica** : cpu = 0.203329 (sec), leaf count = 114

$$\left\{\left\{y(x) \to i^{-c} c_1 x^{-c/2}\, {}_2F_1\left(\frac{a}{2}-\frac{b}{2}-\frac{c}{2}, \frac{a}{2}+\frac{b}{2}-\frac{c}{2}; 1-c; x\right) + i^{c} c_2 x^{c/2}\, {}_2F_1\left(\frac{a}{2}-\frac{b}{2}+\frac{c}{2}, \frac{a}{2}+\frac{b}{2}+\frac{c}{2}; c+1; x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.1 (sec), leaf count = 89

$$\left\{y(x) = (x-1)^{1-a}\left(x^{-\frac{c}{2}} {}_2\mathrm{F}_1(-\frac{a}{2}-\frac{b}{2}-\frac{c}{2}+1, -\frac{a}{2}+\frac{b}{2}-\frac{c}{2}+1;\ 1-c;\ x)\_C2 + x^{\frac{c}{2}} {}_2\mathrm{F}_1(-\frac{a}{2}-\frac{b}{2}+\frac{c}{2}+1, -\frac{a}{2}-\right.$$

2.1335 ODE No. 1335

$$y''(x) = -\frac{y(x)(ax+b)}{4(x-1)^2 x} - \frac{(3x-1)y'(x)}{2(x-1)x}$$

✓ **Mathematica** : cpu = 0.324224 (sec), leaf count = 893

$$\left\{\left\{y(x) \to e^{\frac{1}{4}(-2\log(1-x)-\log(x))} \sqrt[4]{x} c_1\, {}_2F_1\left(\frac{1}{4}\left(\sqrt{-8a-4b-4\sqrt{4a^2+4ba-a-b}+1}+1\right), \frac{\left(-8a-4b-4\sqrt{4a}\right.\right.\right.$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 57

$$\left\{y(x) = \_C1\ \mathit{LegendreP}\left(\frac{1}{2}\sqrt{1-4\,a}-\frac{1}{2}, \sqrt{-a-b}, \sqrt{x}\right) + \_C2\ \mathit{LegendreQ}\left(\frac{1}{2}\sqrt{1-4\,a}-\frac{1}{2}, \sqrt{-a-b}, \sqrt{x}\right)\right\}$$

2.1336 ODE No. 1336

$$y''(x) = -\frac{(1-3x)y(x)}{(x-1)(2x-1)^2}$$

✓ **Mathematica** : cpu = 0.0557889 (sec), leaf count = 70

$$\{\{y(x) \to c_2\sqrt{1-2x}(2x\log(2(x-1)+1) - 2\log(2(x-1)+1) - 2x\log(x-1) + 2\log(x-1) - 1) - c_1\sqrt{1-2x}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 44

$$\{y(x) = (2\_C2\,(x-1)\ln(2x-1) - 2\_C2\,(x-1)\ln(x-1) + \_C1\,x - \_C1 - \_C2)\sqrt{2x-1}\}$$

2.1337 ODE No. 1337

$$y''(x) = -\frac{(a+2b+3x)y'(x)}{2(a+x)(b+x)} - \frac{(a-b)y(x)}{4(a+x)^2(b+x)}$$

✓ **Mathematica** : cpu = 0.0877964 (sec), leaf count = 62

$$\left\{\left\{y(x) \to \frac{c_1}{\sqrt{\frac{b+x}{a-b}+1}} + \frac{c_2\sqrt{b+x}}{\sqrt{a-b}\sqrt{\frac{b+x}{a-b}+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 27

$$\left\{y(x) = 1\left(\sqrt{x+b}\_C1 + \_C2\right)\frac{1}{\sqrt{\frac{x+a}{a-b}}}\right\}$$

2.1338 ODE No. 1338

$$y''(x) = \frac{y(x)}{3(x-2)x^2} + \frac{(6x-1)y'(x)}{3(x-2)x}$$

✓ **Mathematica** : cpu = 0.0694496 (sec), leaf count = 40

$$\left\{\left\{y(x) \to \frac{3}{935}c_2x\left(18x^2 - 102x + 187\right) + c_1\sqrt[6]{x}(2-x)^{17/6}\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 27

$$\left\{y(x) = \_C2\,\sqrt[6]{x}(x-2)^{\frac{17}{6}} + 18\,\_C1\,x\left(x^2 - \frac{17x}{3} + \frac{187}{18}\right)\right\}$$

2.1339 ODE No. 1339

$$y''(x) = -\frac{y'(x)\left(a(b+2)x^2 + x(c-d+1)\right)}{x^2(ax+1)} - \frac{y(x)(abx-cd)}{x^2(ax+1)}$$

✓ **Mathematica** : cpu = 0.276933 (sec), leaf count = 66

$$\left\{\left\{y(x) \to c_1 a^{-c} x^{-c}\, {}_2F_1(1-c, b-c; -c-d+1; -ax) + c_2 a^d x^d\, {}_2F_1(d+1, b+d; c+d+1; -ax)\right\}\right\}$$

✓ **Maple** : cpu = 0.142 (sec), leaf count = 76

$$\left\{y(x) = (ax+1)^{-b+c-d}\left(x^{-c}{}_2\mathrm{F}_1(-d, 1-b-d;\ 1-d-c;\ -ax)\_C2 + x^d{}_2\mathrm{F}_1(c, 1-b+c;\ 1+d+c;\ -ax)\_C1\right.\right.$$

2.1340 ODE No. 1340

$$y''(x) = \frac{2(ax+2b)y'(x)}{x(ax+b)} - \frac{y(x)(2ax+6b)}{x^2(ax+b)}$$

✓ **Mathematica** : cpu = 0.0373982 (sec), leaf count = 32

$$\left\{\left\{y(x) \to \frac{c_2 x^3}{ax+b} + \frac{c_1 x^2}{ax+b}\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 20

$$\left\{y(x) = \frac{x^2(\_C2\, x + \_C1)}{ax+b}\right\}$$

2.1341 ODE No. 1341

$$y''(x) = -\frac{y(x)(avx-b)}{x^2(ax+b)} - \frac{(2ax+b)y'(x)}{x(ax+b)} + Ax$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

`$Aborted`

✓ **Maple** : cpu = 0.182 (sec), leaf count = 201

$$\left\{y(x) = \frac{1}{a^2(v+6)(v+2)(v+12)}\left(x^{-\frac{1}{2}+\frac{1}{2}\sqrt{1-4v}} a^2 \_C2\,(v+6)(v+2)(v+12)\, {}_2\mathrm{F}_1(-\frac{1}{2} - \frac{1}{2}\sqrt{1-4v}, \frac{3}{2} - \frac{1}{2}\sqrt{1}\right.\right.$$

2.1342 ODE No. 1342

$$y''(x) = -\frac{a y(x)}{x^4}$$

✓ **Mathematica** : cpu = 0.0444679 (sec), leaf count = 51

$$\left\{\left\{y(x) \to c_1 x e^{\frac{\sqrt{-a}}{x}} + \frac{c_2 x e^{-\frac{\sqrt{-a}}{x}}}{2\sqrt{-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 31

$$\left\{y(x) = x\left(\cosh\left(\frac{1}{x}\sqrt{-a}\right)\_C2 + \sinh\left(\frac{1}{x}\sqrt{-a}\right)\_C1\right)\right\}$$

2.1343 ODE No. 1343

$$y''(x) = -\frac{y(x)\left((1-a)ax^2 - b(b+x)\right)}{x^4}$$

✗ **Mathematica** : cpu = 0.664013 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y, x\}, \left\{y''(x)x^4 + \left(-a^2x^2 + ax^2 - bx - b^2\right)y(x) = 0, y(1) = c_1, y'(1) = c_2\right\}\right)(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.108 (sec), leaf count = 58

$$\left\{y(x) = I_{a+1}\left(\frac{b}{x}\right)\_C1\, b - K_{a+1}\left(\frac{b}{x}\right)\_C2\, b + 2\left(\_C1\, I_a\left(\frac{b}{x}\right) + \_C2\, K_a\left(\frac{b}{x}\right)\right)(ax + b/2)\right\}$$

2.1344 ODE No. 1344

$$y''(x) = -\frac{\left(e^{2/x} - v^2\right)y(x)}{x^4}$$

✓ **Mathematica** : cpu = 0.565205 (sec), leaf count = 173

$$\left\{\left\{y(x) \to \frac{c_1 2^{v+\frac{v+1}{2}}\left(e^{2/x}\right)^{\frac{v+1}{2}-\frac{1}{2}}\left(-e^{2/x}\right)^{\frac{1}{2}(-v-1)+\frac{1}{2}} I_v\left(\sqrt{-e^{2/x}}\right)}{\log\left(e^{2/x}\right)} + \frac{c_2(-1)^{-v}2^{v+\frac{v+1}{2}}\left(e^{2/x}\right)^{\frac{v+1}{2}-\frac{1}{2}}\left(-e^{2/x}\right)^{\frac{1}{2}(-v-1}}{\log\left(e^{2/x}\right)}\right.\right.$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 23

$$\left\{y(x) = x\left(Y_v\left(\mathrm{e}^{x^{-1}}\right)\_C2 + J_v\left(\mathrm{e}^{x^{-1}}\right)\_C1\right)\right\}$$

2.1345 ODE No. 1345

$$y''(x) = \frac{2y(x)}{x^4} - \frac{y'(x)}{x^3}$$

✓ **Mathematica** : cpu = 0.0295769 (sec), leaf count = 52

$$\left\{\left\{y(x) \to c_1 e^{\frac{1}{2x^2}} x - \sqrt{\frac{\pi}{2}} c_2 e^{\frac{1}{2x^2}} x \text{erf}\left(\frac{1}{\sqrt{2}x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.049 (sec), leaf count = 25

$$\left\{y(x) = x \mathrm{e}^{\frac{1}{2\,x^2}} \left(Erf\left(\frac{\sqrt{2}}{2\,x}\right) \_C2 + \_C1\right)\right\}$$

2.1346 ODE No. 1346

$$y''(x) = \frac{(a+b)y'(x)}{x^2} - \frac{y(x)(x(a+b)+ab)}{x^4}$$

✓ **Mathematica** : cpu = 0.325209 (sec), leaf count = 87

$$\left\{\left\{y(x) \to c_1 x e^{-\frac{-\sqrt{(a-b)^2}+a+b}{2x}} + \frac{c_2 x e^{-\frac{\sqrt{(a-b)^2}}{2x} - \frac{a}{2x} - \frac{b}{2x}}}{\sqrt{(a-b)^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 25

$$\left\{y(x) = x\left(\mathrm{e}^{-\frac{a}{x}} \_C1 + \mathrm{e}^{-\frac{b}{x}} \_C2\right)\right\}$$

2.1347 ODE No. 1347

$$y''(x) = -\frac{y(x)}{x^4} - \frac{y'(x)}{x}$$

✓ **Mathematica** : cpu = 0.0859104 (sec), leaf count = 31

$$\left\{\left\{y(x) \to c_2 J_0\left(\frac{1}{x}\right) + \frac{c_1 K_0\left(\frac{i}{x}\right)}{\sqrt{\pi}}\right\}\right\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 19

$$\left\{y(x) = \_C1\, J_0\left(x^{-1}\right) + \_C2\, Y_0\left(x^{-1}\right)\right\}$$

2.1348 ODE No. 1348

$$y''(x) = -\frac{y(x)\left(a\left(x^4+1\right)+bx^2\right)}{x^4} - \frac{y'(x)}{x}$$

✗ **Mathematica** : cpu = 1.30295 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\left\{y''(x)x^4+y'(x)x^3+\left(ax^4+bx^2+a\right)y(x)=0,y(1)=c_1,y'(1)=c_2\right\}\right)(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.207 (sec), leaf count = 73

$$\left\{y(x) = HeunD\left(0,2\,a+b,0,2\,a-b,\frac{x^2+1}{x^2-1}\right)\left(\int\frac{1}{x}\left(HeunD\left(0,2\,a+b,0,2\,a-b,\frac{x^2+1}{x^2-1}\right)\right)^{-2}\mathrm{d}x\_C2+\_C1\right)\right\}$$

2.1349 ODE No. 1349

$$y''(x) = -\frac{y(x)}{x^4} - \frac{\left(x^2+1\right)y'(x)}{x^3}$$

✓ **Mathematica** : cpu = 0.0970816 (sec), leaf count = 76

$$\left\{\left\{y(x) \to c_2 G^{2,0}_{1,2}\left(-\frac{1}{2x^2}\middle|\begin{matrix}\frac{3}{2}\\0,0\end{matrix}\right) + c_1 e^{\frac{1}{4x^2}}\left(\left(1-\frac{1}{2x^2}\right)I_0\left(\frac{1}{4x^2}\right)+\frac{I_1\left(\frac{1}{4x^2}\right)}{2x^2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 85

$$\left\{y(x) = \frac{\_C1}{x^2}\mathrm{e}^{\frac{1}{4\,x^2}}\left(2\,x^2 I_0\left(1/4\,x^{-2}\right)+I_1\left(\frac{1}{4\,x^2}\right)-I_0\left(\frac{1}{4\,x^2}\right)\right)+\frac{\_C2}{x^2}\mathrm{e}^{\frac{1}{4\,x^2}}\left(2\,K_0\left(-1/4\,x^{-2}\right)x^2+K_1\left(-\frac{1}{4\,x^2}\right)\right.\right.$$

2.1350 ODE No. 1350

$$y''(x) = -\frac{a^2 y(x)}{x^4} - \frac{2y'(x)}{x}$$

✓ **Mathematica** : cpu = 0.0105236 (sec), leaf count = 25

$$\left\{\left\{y(x) \to c_1 \cos\left(\frac{a}{x}\right) - c_2 \sin\left(\frac{a}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.008 (sec), leaf count = 21

$$\left\{y(x) = \_C1\ \sin\left(\frac{a}{x}\right) + \_C2\ \cos\left(\frac{a}{x}\right)\right\}$$

2.1351 ODE No. 1351

$$y''(x) = \frac{y(x)}{x^4} - \frac{\left(2x^2+1\right)y'(x)}{x^3}$$

✓ **Mathematica** : cpu = 0.0278903 (sec), leaf count = 50

$$\left\{\left\{y(x) \to c_1 e^{\frac{1}{2x^2}} - \sqrt{\frac{\pi}{2}} c_2 e^{\frac{1}{2x^2}} \operatorname{erf}\left(\frac{1}{\sqrt{2}x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 24

$$\left\{y(x) = \mathrm{e}^{\frac{1}{2\,x^2}}\left(Erf\left(\frac{\sqrt{2}}{2\,x}\right)\_C2 + \_C1\right)\right\}$$

2.1352 ODE No. 1352

$$y''(x) = -\frac{2(a+x)y'(x)}{x^2} - \frac{by(x)}{x^4}$$

✓ **Mathematica** : cpu = 0.0146453 (sec), leaf count = 89

$$\left\{\left\{y(x) \to c_1 e^{-\frac{\sqrt{b}\left(-\frac{\sqrt{a^2-b}}{\sqrt{b}}-\frac{a}{\sqrt{b}}\right)}{x}} + c_2 e^{-\frac{\sqrt{b}\left(\frac{\sqrt{a^2-b}}{\sqrt{b}}-\frac{a}{\sqrt{b}}\right)}{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 43

$$\left\{y(x) = \_C1\,\mathrm{e}^{\frac{1}{x}\left(a-\sqrt{a^2-b}\right)} + \_C2\,\mathrm{e}^{\frac{1}{x}\left(\sqrt{a^2-b}+a\right)}\right\}$$

2.1353 ODE No. 1353

$$y''(x) = \frac{\left(2x^2-1\right)y'(x)}{x^3} - \frac{y(x)}{x^4}$$

✓ **Mathematica** : cpu = 0.10829 (sec), leaf count = 119

$$\left\{\left\{y(x) \to c_1\left(x^3+2x-\frac{1}{x}\right) - \frac{c_2\left(\sqrt{2\pi}x^4\operatorname{erfi}\left(\frac{1}{\sqrt{2}x}\right) + 2\sqrt{2\pi}x^2\operatorname{erfi}\left(\frac{1}{\sqrt{2}x}\right) - \sqrt{2\pi}\operatorname{erfi}\left(\frac{1}{\sqrt{2}x}\right) + 2e^{\frac{1}{2x^2}}x - 2e^{\frac{1}{2x^2}}x^3\right)}{16x}\right\}\right\}$$

✓ **Maple** : cpu = 0.211 (sec), leaf count = 66

$$\left\{y(x) = \frac{1}{x}\left(\_C1\,\sqrt{2}\sqrt{\pi}\left(x^4+2\,x^2-1\right)erfi\left(\frac{\sqrt{2}}{2\,x}\right) + \left(-2\,\_C1\,x^3+2\,\_C1\,x\right)\mathrm{e}^{\frac{1}{2\,x^2}} + \_C2\left(x^4+2\,x^2-1\right)\right)\right\}$$

2.1354 ODE No. 1354

$$y''(x) = \frac{\left(2x^2-1\right)y'(x)}{x^3} - \frac{2y(x)}{x^4}$$

✓ **Mathematica** : cpu = 0.0717694 (sec), leaf count = 108

$$\left\{\left\{y(x) \to \frac{c_2\left(-5\sqrt{2\pi}x^2\text{erfi}\left(\frac{1}{\sqrt{2}x}\right)+\sqrt{2\pi}\text{erfi}\left(\frac{1}{\sqrt{2}x}\right)-2e^{\frac{1}{2x^2}}x+4e^{\frac{1}{2x^2}}x^5+8e^{\frac{1}{2x^2}}x^3\right)}{12x^2}+c_1\left(1-\frac{1}{5x^2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.256 (sec), leaf count = 33

$$\left\{y(x) = \frac{1}{x^2}\left(\_C2\,{}_1\mathrm{F}_1(-\frac{5}{2};-\frac{1}{2};\frac{1}{2\,x^2})x^5+5\,\_C1\,x^2-\_C1\right)\right\}$$

2.1355 ODE No. 1355

$$y''(x) = \frac{xy(x)}{x^3+1} - \frac{\left(x^3-1\right)y'(x)}{x\left(x^3+1\right)}$$

✓ **Mathematica** : cpu = 0.129546 (sec), leaf count = 59

$$\left\{\left\{y(x) \to \frac{1}{2}c_2\left(2x^2-x^2\sqrt[3]{x^3+1}\,{}_2F_1\left(\frac{1}{3},\frac{2}{3};\frac{5}{3};-x^3\right)\right)+c_1\sqrt[3]{x^3+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.142 (sec), leaf count = 30

$$\left\{y(x) = \sqrt[3]{x^3+1}\left({}_2\mathrm{F}_1(\frac{2}{3},\frac{4}{3};\frac{5}{3};-x^3)\_C1\,x^2+\_C2\right)\right\}$$

2.1356 ODE No. 1356

$$y''(x) = -\frac{y(x)\left(-n^2-v(v+1)x^2\right)}{x^2\left(x^2+1\right)} - \frac{\left(2x^2+1\right)y'(x)}{x\left(x^2+1\right)}$$

✓ **Mathematica** : cpu = 0.303275 (sec), leaf count = 90

$$\left\{\left\{y(x) \to c_1x^{-n}\,{}_2F_1\left(-\frac{n}{2}-\frac{v}{2},-\frac{n}{2}+\frac{v}{2}+\frac{1}{2};1-n;-x^2\right)+c_2x^n\,{}_2F_1\left(\frac{n}{2}-\frac{v}{2},\frac{n}{2}+\frac{v}{2}+\frac{1}{2};n+1;-x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.084 (sec), leaf count = 29

$$\left\{y(x) = \_C1\ LegendreP\left(v,n,\sqrt{x^2+1}\right)+\_C2\ LegendreQ\left(v,n,\sqrt{x^2+1}\right)\right\}$$

2.1357 ODE No. 1357

$$y''(x) = -\frac{\left(ax^2+a-1\right)y'(x)}{x\left(x^2+1\right)} - \frac{y(x)\left(bx^2+c\right)}{x^2\left(x^2+1\right)}$$

✓ **Mathematica** : cpu = 0.66683 (sec), leaf count = 288

$$\left\{\left\{y(x) \to c_1 x^{\frac{1}{2}\left(-\sqrt{a^2-4a-4c+4}-a+2\right)}\, {}_2F_1\left(-\frac{1}{4}\sqrt{a^2-2a-4b+1}-\frac{1}{4}\sqrt{a^2-4a-4c+4}+\frac{1}{4},\frac{1}{4}\sqrt{a^2-2a-4b+\right.\right.$$

✓ **Maple** : cpu = 0.128 (sec), leaf count = 97

$$\left\{y(x) = x^{1-\frac{a}{2}}\left(LegendreP\left(-\frac{1}{2}+\frac{1}{2}\sqrt{a^2-2\,a-4\,b+1},\frac{1}{2}\sqrt{a^2-4\,a-4\,c+4},\sqrt{x^2+1}\right)\_C1 + LegendreQ\left(-\right.\right.\right.$$

2.1358 ODE No. 1358

$$y''(x) = \frac{\left(x^2-2\right)y'(x)}{x\left(x^2-1\right)} - \frac{\left(x^2-2\right)y(x)}{x^2\left(x^2-1\right)}$$

✓ **Mathematica** : cpu = 0.0662808 (sec), leaf count = 66

$$\left\{\left\{y(x) \to \frac{c_1 x \sqrt[4]{x^2-1}}{\sqrt[4]{1-x^2}} + \frac{c_2 x \sqrt[4]{x^2-1}\log\left(\sqrt{x^2-1}+x\right)}{\sqrt[4]{1-x^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 20

$$\left\{y(x) = x\left(\ln\left(x+\sqrt{x^2-1}\right)\_C2 + \_C1\right)\right\}$$

2.1359 ODE No. 1359

$$y''(x) = -\frac{v(v+1)y(x)}{x^2\left(x^2-1\right)} - \frac{2xy'(x)}{x^2-1}$$

✓ **Mathematica** : cpu = 0.104714 (sec), leaf count = 86

$$\left\{\left\{y(x) \to c_1 i^{-v} x^{-v}\, {}_2F_1\left(\frac{1}{2}-\frac{v}{2},-\frac{v}{2};\frac{1}{2}-v;x^2\right) + c_2 i^{v+1} x^{v+1}\, {}_2F_1\left(\frac{v}{2}+\frac{1}{2},\frac{v}{2}+1;v+\frac{3}{2};x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.098 (sec), leaf count = 57

$$\left\{y(x) = \_C1\, {}_2\mathrm{F}_1(-\frac{v}{2},\frac{1}{2}-\frac{v}{2};\,\frac{1}{2}-v;\,x^2)x^{-v} + \_C2\, {}_2\mathrm{F}_1(1+\frac{v}{2},\frac{1}{2}+\frac{v}{2};\,\frac{3}{2}+v;\,x^2)x^{v+1}\right\}$$

2.1360 ODE No. 1360

$$y''(x) = \frac{v(v+1)y(x)}{x^2} - \frac{2xy'(x)}{x^2-1}$$

✓ **Mathematica** : cpu = 0.0967066 (sec), leaf count = 68

$$\left\{\left\{y(x) \to c_1 i^{-v} x^{-v}\, {}_2F_1\left(\frac{1}{2}, -v; \frac{1}{2}-v; x^2\right) + c_2 i^{v+1} x^{v+1}\, {}_2F_1\left(\frac{1}{2}, v+1; v+\frac{3}{2}; x^2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.079 (sec), leaf count = 47

$$\left\{y(x) = \_C1\ {}_2\mathrm{F}_1(\frac{1}{2}, -v;\ \frac{1}{2}-v;\ x^2)x^{-v} + \_C2\ {}_2\mathrm{F}_1(\frac{1}{2}, v+1;\ \frac{3}{2}+v;\ x^2)x^{v+1}\right\}$$

2.1361 ODE No. 1361

$$y''(x) = \frac{2xy'(x)}{x^2-1} - \frac{\left(a(a+1) - a(a+3)x^2\right)y(x)}{x^2\left(x^2-1\right)}$$

✓ **Mathematica** : cpu = 0.484862 (sec), leaf count = 38

$$\left\{\left\{y(x) \to c_1 x^{-a} + c_2\left(-2ax^2 + 2a - x^2 + 3\right)x^{a+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 33

$$\left\{y(x) = \_C1\ x^{-a} + \_C2\ x^{a+1}\left(2\,ax^2 + x^2 - 2\,a - 3\right)\right\}$$

2.1362 ODE No. 1362

$$y''(x) = \frac{2xy'(x)}{x^2-1} - \frac{y(x)\left(\left(x^2-1\right)x^2(a-n)(a+n+1) + 2ax^2 + n(n+1)\left(x^2-1\right)\right)}{x^2\left(x^2-1\right)}$$

✗ **Mathematica** : cpu = 13.8857 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y, x\}, \left\{-2y'(x)x^3 + \left(a^2x^4 - n^2x^4 + ax^4 - nx^4 - a^2x^2 + 2n^2x^2 + ax^2 + 2nx^2 - n^2\right.\right.\right.$$

✓ **Maple** : cpu = 0.252 (sec), leaf count = 109

$$\left\{y(x) = \_C1\ HeunC\left(0, -n - \frac{1}{2}, -2, -\frac{a^2}{4} + \frac{n^2}{4} - \frac{a}{4} + \frac{n}{4}, -\frac{n^2}{4} - \frac{n}{4} + \frac{3}{4} + \frac{a^2}{4} - \frac{a}{4}, x^2\right)x^{-n} + \_C2\ HeunC\left(0,\right.\right.$$

2.1363 ODE No. 1363

$$y''(x) = -\frac{\left(ax^2+a-2\right)y'(x)}{x\left(x^2-1\right)} - \frac{by(x)}{x^2}$$

✓ **Mathematica** : cpu = 0.802791 (sec), leaf count = 236

$$\left\{\left\{y(x)\to c_1(-1)^{\frac{1}{4}\left(-\sqrt{a^2-2a-4b+1}+a-1\right)}x^{\frac{1}{2}\left(-\sqrt{a^2-2a-4b+1}+a-1\right)}\,{}_2F_1\left(\frac{a}{2}-\frac{1}{2},\frac{a}{2}-\frac{1}{2}\sqrt{a^2-2a-4b+1}-\frac{1}{2};1-\frac{1}{2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.153 (sec), leaf count = 161

$$\left\{y(x)=\left(x^2-1\right)^{-a+2}\left({}_2\mathrm{F}_1(-\frac{a}{2}+\frac{3}{2},-\frac{a}{2}+\frac{3}{2}+\frac{1}{2}\sqrt{a^2-2\,a-4\,b+1};\,1+\frac{1}{2}\sqrt{a^2-2\,a-4\,b+1};\,x^2)x^{\frac{a}{2}-\frac{1}{2}+\frac{1}{2}\sqrt{a}}\right.\right.$$

2.1364 ODE No. 1364

$$y''(x) = \frac{y'(x)\left(2(a-1)x^2-2a+2bc\left(x^2-1\right)x^c\right)}{x\left(x^2-1\right)} - \frac{y(x)\left(bc(2a-c-1)x^{c+2}-bc(2a-c+1)x^c+x^2((a-1)a-\right.}{x^2\left(x^2-1\right)}$$

✓ **Mathematica** : cpu = 0.169577 (sec), leaf count = 42

$$\left\{\left\{y(x)\to c_1P_v(x)e^{a\log(x)+bx^c}+c_2Q_v(x)e^{a\log(x)+bx^c}\right\}\right\}$$

✓ **Maple** : cpu = 0.114 (sec), leaf count = 25

$$\left\{y(x)=x^a\mathrm{e}^{bx^c}\left(\mathit{LegendreQ}(v,x)\_C2+\mathit{LegendreP}(v,x)\_C1\right)\right\}$$

2.1365 ODE No. 1365

$$y''(x) = -\frac{ay(x)}{\left(x^2+1\right)^2}$$

✓ **Mathematica** : cpu = 0.0964144 (sec), leaf count = 72

$$\left\{\left\{y(x)\to c_1\sqrt{x^2+1}e^{i\sqrt{a+1}\tan^{-1}(x)}+\frac{ic_2\sqrt{x^2+1}e^{-i\sqrt{a+1}\tan^{-1}(x)}}{2\sqrt{a+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.064 (sec), leaf count = 59

$$\left\{y(x)=\sqrt{x^2+1}\left(\left(\frac{x+i}{-x+i}\right)^{-\frac{1}{2}\sqrt{a+1}}\_C2+\left(\frac{x+i}{-x+i}\right)^{\frac{1}{2}\sqrt{a+1}}\_C1\right)\right\}$$

2.1366 ODE No. 1366

$$y''(x) = -\frac{2xy'(x)}{x^2+1} - \frac{y(x)}{(x^2+1)^2}$$

✓ **Mathematica** : cpu = 0.0239382 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{c_1}{\sqrt{x^2+1}} + \frac{c_2 x}{\sqrt{x^2+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.01 (sec), leaf count = 17

$$\left\{y(x) = (\_C1\, x + \_C2)\frac{1}{\sqrt{x^2+1}}\right\}$$

2.1367 ODE No. 1367

$$y''(x) = -\frac{y(x)\left(a^2\left(x^2+1\right)^2 + m^2 - n(n+1)\left(x^2+1\right)\right)}{\left(x^2+1\right)^2} - \frac{2xy'(x)}{x^2+1}$$

✗ **Mathematica** : cpu = 2.30339 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y,x\}, \left\{y''(x)\left(x^2+1\right)^2 + 2xy'(x)\left(x^2+1\right) + \left(a^2x^4 + 2a^2x^2 - n^2x^2 - nx^2 + a^2 + n\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.26 (sec), leaf count = 88

$$\left\{y(x) = \left(x^2+1\right)^{\frac{m}{2}}\left(HeunC\left(0, \frac{1}{2}, m, -\frac{a^2}{4}, \frac{1}{4} + \frac{a^2}{4} + \frac{m^2}{4} - \frac{n^2}{4} - \frac{n}{4}, -x^2\right)\_C2\, x + HeunC\left(0, -\frac{1}{2}, m, -\frac{a^2}{4}, \frac{1}{4}\right.\right.\right.$$

2.1368 ODE No. 1368

$$y''(x) = -\frac{axy'(x)}{x^2+1} - \frac{by(x)}{(x^2+1)^2}$$

✓ **Mathematica** : cpu = 0.0278288 (sec), leaf count = 106

$$\left\{\left\{y(x) \to c_1\left(x^2+1\right)^{\frac{2-a}{4}} P^{\frac{1}{2}\sqrt{a^2-4a+4b+4}}_{\frac{a-2}{2}}(ix) + c_2\left(x^2+1\right)^{\frac{2-a}{4}} Q^{\frac{1}{2}\sqrt{a^2-4a+4b+4}}_{\frac{a-2}{2}}(ix)\right\}\right\}$$

✓ **Maple** : cpu = 0.078 (sec), leaf count = 71

$$\left\{y(x) = \left(x^2+1\right)^{\frac{1}{2}-\frac{a}{4}}\left(LegendreQ\left(\frac{a}{2}-1, \frac{1}{2}\sqrt{a^2-4\,a+4\,b+4}, ix\right)\_C2 + LegendreP\left(\frac{a}{2}-1, \frac{1}{2}\sqrt{a^2-4\,a+4}\right.\right.\right.$$

2.1369 ODE No. 1369

$$y''(x) = -\frac{a y(x)}{(x^2-1)^2}$$

✓ **Mathematica** : cpu = 0.104289 (sec), leaf count = 75

$$\left\{\left\{y(x) \to c_1 \sqrt{1-x^2} e^{-\sqrt{1-a}\tanh^{-1}(x)} + \frac{c_2 \sqrt{1-x^2} e^{\sqrt{1-a}\tanh^{-1}(x)}}{2\sqrt{1-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.055 (sec), leaf count = 55

$$\left\{y(x) = \sqrt{x^2-1}\left(\left(\frac{x-1}{1+x}\right)^{-\frac{1}{2}\sqrt{1-a}} \_C2 + \left(\frac{x-1}{1+x}\right)^{\frac{1}{2}\sqrt{1-a}} \_C1\right)\right\}$$

2.1370 ODE No. 1370

$$y''(x) = \frac{a^2 y(x)}{(x^2-1)^2} - \frac{2x y'(x)}{x^2-1}$$

✓ **Mathematica** : cpu = 0.030629 (sec), leaf count = 53

$$\left\{\left\{y(x) \to c_1 \cosh\left(\frac{1}{2}a(\log(1-x)-\log(x+1))\right) + i c_2 \sinh\left(\frac{1}{2}a(\log(1-x)-\log(x+1))\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 19

$$\{y(x) = \_C1 \sinh(a\,Artanh(x)) + \_C2 \cosh(a\,Artanh(x))\}$$

2.1371 ODE No. 1371

$$y''(x) = -\frac{y(x)\left(-a^2-\lambda(x^2-1)\right)}{(x^2-1)^2} - \frac{2x y'(x)}{x^2-1}$$

✓ **Mathematica** : cpu = 0.0226317 (sec), leaf count = 48

$$\left\{\left\{y(x) \to c_1 P^a_{\frac{1}{2}\left(\sqrt{4\lambda+1}-1\right)}(x) + c_2 Q^a_{\frac{1}{2}\left(\sqrt{4\lambda+1}-1\right)}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 37

$$\left\{y(x) = \_C1\ LegendreP\left(\frac{1}{2}\sqrt{1+4\lambda}-\frac{1}{2}, a, x\right) + \_C2\ LegendreQ\left(\frac{1}{2}\sqrt{1+4\lambda}-\frac{1}{2}, a, x\right)\right\}$$

2.1372 ODE No. 1372

$$y''(x) = -\frac{y(x)\left(\left(x^2-1\right)\left(ax^2+bx+c\right)-k^2\right)}{\left(x^2-1\right)^2} - \frac{2xy'(x)}{x^2-1}$$

✗ **Mathematica** : cpu = 4.06564 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\left\{\left(ax^4+bx^3-ax^2+cx^2-bx-k^2-c\right)y(x)+\left(2x^3-2x\right)y'(x)+\left(x^4-2x^2\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.297 (sec), leaf count = 110

$$\left\{y(x) = \mathrm{e}^{\sqrt{-a}x}\left(HeunC\left(4\sqrt{-a},-k,k,2\,b,\frac{k^2}{2}+a-b+c,\frac{1}{2}+\frac{x}{2}\right)\sqrt{2\,x-2}(1+x)^{-\frac{k}{2}}\left(x-1\right)^{\frac{k}{2}-\frac{1}{2}}\_C2+Heun\right.\right.$$

2.1373 ODE No. 1373

$$y''(x) = -\frac{y(x)\left(-a^2\left(x^2-1\right)^2-m^2-n(n+1)\left(x^2-1\right)\right)}{\left(x^2-1\right)^2} - \frac{2xy'(x)}{x^2-1}$$

✗ **Mathematica** : cpu = 2.35807 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\left\{\left(-a^2x^4+2a^2x^2-n^2x^2-nx^2-a^2-m^2+n^2+n\right)y(x)+\left(2x^3-2x\right)y'(x)\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.244 (sec), leaf count = 84

$$\left\{y(x) = \left(x^2-1\right)^{\frac{m}{2}}\left(HeunC\left(0,\frac{1}{2},m,-\frac{a^2}{4},\frac{1}{4}+\frac{a^2}{4}+\frac{m^2}{4}-\frac{n^2}{4}-\frac{n}{4},x^2\right)\_C2\,x+HeunC\left(0,-\frac{1}{2},m,-\frac{a^2}{4},\frac{1}{4}+\right.\right.\right.$$

2.1374 ODE No. 1374

$$y''(x) = \frac{2(2a-1)xy'(x)}{x^2-1} - \frac{y(x)\left(x^2(2a(2a-1)-v(v+1))+2a+v(v+1)\right)}{\left(x^2-1\right)^2}$$

✓ **Mathematica** : cpu = 0.0394215 (sec), leaf count = 32

$$\left\{\left\{y(x) \to c_1\left(x^2-1\right)^a P_v(x)+c_2\left(x^2-1\right)^a Q_v(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 23

$$\left\{y(x) = \left(x^2-1\right)^a\left(LegendreQ(v,x)\_C2+LegendreP(v,x)\_C1\right)\right\}$$

2.1375 ODE No. 1375

$$y''(x) = -\frac{y(x)\left(4ax^2(a-n) - \left(x^2-1\right)\left(2a+(v-n)(n+v+1)\right)\right)}{\left(x^2-1\right)^2} - \frac{2x(-2a+n+1)y'(x)}{x^2-1}$$

✓ **Mathematica** : cpu = 0.0533663 (sec), leaf count = 54

$$\left\{\left\{y(x) \to c_1\left(x^2-1\right)^{\frac{1}{2}(2a-n)} P_v^n(x) + c_2\left(x^2-1\right)^{\frac{1}{2}(2a-n)} Q_v^n(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 29

$$\left\{y(x) = \left(x^2-1\right)^{a-\frac{n}{2}} \left(LegendreQ(v,n,x)\_C2 + LegendreP(v,n,x)\_C1\right)\right\}$$

2.1376 ODE No. 1376

$$y''(x) = -\frac{by(x)}{x^2\left(a+x^2\right)} - \frac{\left(a+2x^2\right)y'(x)}{x\left(a+x^2\right)}$$

✓ **Mathematica** : cpu = 0.0993698 (sec), leaf count = 82

$$\left\{\left\{y(x) \to c_2 \sin\left(\frac{\sqrt{b}\left(\log(x) - \log\left(\sqrt{a}\sqrt{a+x^2}+a\right)\right)}{\sqrt{a}}\right) + c_1 \cos\left(\frac{\sqrt{b}\left(\log(x) - \log\left(\sqrt{a}\sqrt{a+x^2}+a\right)\right)}{\sqrt{a}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.031 (sec), leaf count = 73

$$\left\{y(x) = 1\left(\_C2\left(\left(\frac{1}{x}\left(2a+2\sqrt{a}\sqrt{x^2+a}\right)\right)^{i\sqrt{b}\frac{1}{\sqrt{a}}}\right)^2 + \_C1\right)\left(\left(\frac{1}{x}\left(2a+2\sqrt{a}\sqrt{x^2+a}\right)\right)^{i\sqrt{b}\frac{1}{\sqrt{a}}}\right)^{-1}\right\}$$

2.1377 ODE No. 1377

$$y''(x) = -\frac{b^2 y(x)}{\left(a^2+x^2\right)^2}$$

✓ **Mathematica** : cpu = 0.236639 (sec), leaf count = 109

$$\left\{\left\{y(x) \to c_1\sqrt{a^2+x^2}e^{i\sqrt{\frac{b^2}{a^2}+1}\tan^{-1}\left(\frac{x}{a}\right)} + \frac{ic_2\sqrt{a^2+x^2}e^{-i\sqrt{\frac{a^2+b^2}{a^2}}\tan^{-1}\left(\frac{x}{a}\right)}}{2a\sqrt{\frac{a^2+b^2}{a^2}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.132 (sec), leaf count = 83

$$\left\{y(x) = \sqrt{a^2+x^2}\left(\left(\frac{ix-a}{ix+a}\right)^{\frac{1}{2a}\sqrt{a^2+b^2}}\_C1 + \left(\frac{ix-a}{ix+a}\right)^{-\frac{1}{2a}\sqrt{a^2+b^2}}\_C2\right)\right\}$$

2.1378 ODE No. 1378

$$y''(x) = -\frac{2\left(x^2-1\right)y'(x)}{(x-1)^2 x} - \frac{\left(-2x^2+2x+2\right)y(x)}{(x-1)^2 x^2}$$

✓ **Mathematica** : cpu = 0.0541499 (sec), leaf count = 65

$$\left\{\left\{y(x) \to \frac{c_1 x^2}{1-x} + \frac{c_2 x\left(2x^2\log(1-x) - 2x^2\log(x) + 2x - 2x\log(1-x) + 2x\log(x) - 1\right)}{(x-1)^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 48

$$\left\{y(x) = \frac{x}{(x-1)^2}\left(-\_C2\, x(x-1)\ln(x-1) + \_C2\, x(x-1)\ln(x) + \_C1\, x^2 + (-\_C1 - \_C2)\, x + \frac{-\_C2}{2}\right)\right\}$$

2.1379 ODE No. 1379

$$y''(x) = \frac{12y(x)}{(x+1)^2\left(x^2+2x+3\right)}$$

✓ **Mathematica** : cpu = 0.0821452 (sec), leaf count = 99

$$\left\{\left\{y(x) \to \frac{c_2\left(2x^3+4x^2-3\sqrt{2}x^2\tan^{-1}\left(\frac{x+1}{\sqrt{2}}\right)+8x-6\sqrt{2}x\tan^{-1}\left(\frac{x+1}{\sqrt{2}}\right)-9\sqrt{2}\tan^{-1}\left(\frac{x+1}{\sqrt{2}}\right)+2\right)}{2(x+1)^2} + c_1\left(\frac{2}{(x+\right.\right.\right.$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 59

$$\left\{y(x) = \frac{1}{(1+x)^2}\left(-3\_C2\left(x^2+2x+3\right)\arctan\left(1/2\,(1+x)\sqrt{2}\right) + \_C2\left(x^3+2x^2+4x+1\right)\sqrt{2} + \_C1\,(x^2 -\right.\right.$$

2.1380 ODE No. 1380

$$y''(x) = -\frac{by(x)}{x^2(x-a)^2}$$

✓ **Mathematica** : cpu = 0.304902 (sec), leaf count = 132

$$\left\{\left\{y(x) \to \frac{c_2(x-a)^{\frac{1}{2}\sqrt{\frac{a^2-4b}{a^2}}+\frac{1}{2}} x^{\frac{1}{2}-\frac{1}{2}\sqrt{\frac{a^2-4b}{a^2}}}}{a\sqrt{\frac{a^2-4b}{a^2}}} + c_1(x-a)^{\frac{1}{2}-\frac{1}{2}\sqrt{1-\frac{4b}{a^2}}} x^{\frac{1}{2}\sqrt{1-\frac{4b}{a^2}}+\frac{1}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 67

$$\left\{y(x) = \sqrt{x\left(a-x\right)}\left(\left(\frac{x}{a-x}\right)^{\frac{1}{2a}\sqrt{a^2-4b}}\_C2 + \left(\frac{a-x}{x}\right)^{\frac{1}{2a}\sqrt{a^2-4b}}\_C1\right)\right\}$$

2.1381 ODE No. 1381

$$y''(x) = c - \frac{by(x)}{x^2(x-a)^2}$$

✓ **Mathematica** : cpu = 0.716324 (sec), leaf count = 589

$$\left\{\left\{y(x) \to -\frac{2cx^2(a-x)\left(1-\frac{x}{a}\right)^{-\frac{1}{2}\sqrt{\frac{a^2-4b}{a^2}}}\left(\sqrt{\frac{a^2-4b}{a^2}}\left(1-\frac{x}{a}\right)^{\sqrt{\frac{a^2-4b}{a^2}}}\,{}_2F_1\left(\frac{1}{2}\sqrt{1-\frac{4b}{a^2}}-\frac{1}{2},\frac{1}{2}\sqrt{1-\frac{4b}{a^2}}+\frac{3}{2};\frac{1}{2}\sqrt{1-\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.177 (sec), leaf count = 175

$$\left\{y(x) = 1\sqrt{x\left(a-x\right)}\left(\left(\_C2\sqrt{a^2-4b} - \int\sqrt{x\left(a-x\right)}\left(\frac{a-x}{x}\right)^{-\frac{1}{2a}\sqrt{a^2-4b}}\,\mathrm{d}xc\right)\left(\frac{a-x}{x}\right)^{\frac{1}{2a}\sqrt{a^2-4b}} + \left(\int\sqrt{\right.\right.\right.$$

2.1382 ODE No. 1382

$$y''(x) = \frac{cy(x)}{(x-a)^2(x-b)^2}$$

✓ **Mathematica** : cpu = 0.704154 (sec), leaf count = 154

$$\left\{\left\{y(x) \to c_1(x-a)^{\frac{1}{2}\left(\sqrt{\frac{4c}{(a-b)^2}+1}+1\right)}(x-b)^{\frac{1}{2}\left(1-\sqrt{\frac{4c}{(a-b)^2}+1}\right)} - \frac{c_2(x-a)^{\frac{1}{2}-\frac{1}{2}\sqrt{\frac{4c}{(a-b)^2}+1}}(x-b)^{\frac{1}{2}\sqrt{\frac{4c}{(a-b)^2}+1}+\frac{1}{2}}}{(a-b)\sqrt{\frac{4c}{(a-b)^2}+1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.121 (sec), leaf count = 104

$$\left\{y(x) = \sqrt{(a-x)\left(b-x\right)}\left(\left(\frac{a-x}{b-x}\right)^{\frac{1}{2a-2b}\sqrt{a^2-2ab+b^2+4c}}\_C1 + \left(\frac{a-x}{b-x}\right)^{-\frac{1}{2a-2b}\sqrt{a^2-2ab+b^2+4c}}\_C2\right)\right\}$$

2.1383 ODE No. 1383

$$y''(x) = -\frac{y'(x)\left((x-a)^2(\alpha+\beta+1)(x-b)+(x-a)(-\alpha-\beta+1)(x-b)^2\right)}{(x-a)^2(x-b)^2} - \frac{\alpha\beta(a-b)^2 y(x)}{(x-a)^2(x-b)^2}$$

✓ **Mathematica** : cpu = 0.141092 (sec), leaf count = 50

$$\left\{\left\{y(x) \to c_1 e^{\alpha(\log(x-a)-\log(x-b))} + c_2 e^{\beta(\log(x-a)-\log(x-b))}\right\}\right\}$$

✓ **Maple** : cpu = 0.052 (sec), leaf count = 39

$$\left\{y(x) = \_C1 \left(\frac{a-x}{b-x}\right)^{\beta} + \_C2 \left(\frac{a-x}{b-x}\right)^{\alpha}\right\}$$

2.1384 ODE No. 1384

$$y''(x) = -\frac{y(x)\left(-\left(a^2-1\right)x^2+2(a+3)bx-b^2\right)}{4x^2}$$

✓ **Mathematica** : cpu = 0.033921 (sec), leaf count = 110

$$\left\{\left\{y(x) \to c_1 M_{\frac{(a+3)b}{2\sqrt{a^2-1}},\frac{\sqrt{b\left(b^2+1\right)}}{2\sqrt{b}}}\left(\sqrt{a^2-1}x\right) + c_2 W_{\frac{(a+3)b}{2\sqrt{a^2-1}},\frac{\sqrt{b\left(b^2+1\right)}}{2\sqrt{b}}}\left(\sqrt{a^2-1}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.27 (sec), leaf count = 73

$$\left\{y(x) = \_C1\, M_{\frac{b(a+3)}{2},\frac{1}{\sqrt{a^2-1}},\frac{1}{2}\sqrt{b^2+1}}\left(\sqrt{a^2-1}x\right) + \_C2\, W_{\frac{b(a+3)}{2},\frac{1}{\sqrt{a^2-1}},\frac{1}{2}\sqrt{b^2+1}}\left(\sqrt{a^2-1}x\right)\right\}$$

2.1385 ODE No. 1385

$$y''(x) = -\frac{\left(ax^2+a-3\right)y(x)}{4\left(x^2+1\right)^2}$$

✓ **Mathematica** : cpu = 0.0200789 (sec), leaf count = 78

$$\left\{\left\{y(x) \to c_1\sqrt{x^2+1}P^{\frac{1}{2}}_{\frac{1}{2}(\sqrt{1-a}-1)}(ix) + c_2\sqrt{x^2+1}Q^{\frac{1}{2}}_{\frac{1}{2}(\sqrt{1-a}-1)}(ix)\right\}\right\}$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 55

$$\left\{y(x) = \sqrt[4]{x^2+1}\left(\left(x+\sqrt{x^2+1}\right)^{-\frac{1}{2}\sqrt{1-a}}\_C2 + \left(x+\sqrt{x^2+1}\right)^{\frac{1}{2}\sqrt{1-a}}\_C1\right)\right\}$$

2.1386 ODE No. 1386

$$y''(x) = \frac{18y(x)}{(2x+1)^2\left(x^2+x+1\right)}$$

✓ **Mathematica** : cpu = 0.0926537 (sec), leaf count = 108

$$\left\{\left\{y(x) \to \frac{c_1\left(x^2+x+1\right)}{(2x+1)^2} + \frac{c_2\left(16x^3+24x^2-12\sqrt{3}x^2\tan^{-1}\left(\frac{2x+1}{\sqrt{3}}\right)+30x-12\sqrt{3}x\tan^{-1}\left(\frac{2x+1}{\sqrt{3}}\right)-12\sqrt{3}\tan\right.\right.}{(2x+1)^2}$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 58

$$\left\{y(x) = \frac{1}{(2\,x+1)^2}\left(36\,\_C2\left(x^2+x+1\right)\arctan\left(1/3\left(2\,x+1\right)\sqrt{3}\right)-16\left(x^3+x^2+\frac{11\,x}{8}+3/16\right)\_C2\,\sqrt{3}+\_\right.\right.$$

2.1387 ODE No. 1387

$$y''(x) = \frac{3y(x)}{4\left(x^2+x+1\right)^2}$$

✓ **Mathematica** : cpu = 0.0405344 (sec), leaf count = 50

$$\left\{\left\{y(x) \to c_1\sqrt{x^2+x+1} + \frac{2c_2\sqrt{x^2+x+1}\tan^{-1}\left(\frac{2x+1}{\sqrt{3}}\right)}{\sqrt{3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 28

$$\left\{y(x) = \sqrt{x^2+x+1}\left(\arctan\left(\frac{\left(2\,x+1\right)\sqrt{3}}{3}\right)\_C2+\_C1\right)\right\}$$

2.1388 ODE No. 1388

$$y''(x) = -\frac{y(x)\left(v(v+1)(x-1)-a^2x\right)}{4(x-1)^2x^2} - \frac{(3x-1)y'(x)}{2(x-1)x}$$

✓ **Mathematica** : cpu = 0.30513 (sec), leaf count = 235

$$\left\{\left\{y(x) \to c_2(-1)^{\frac{1}{2}(-2v-3)+1}x^{\frac{1}{4}(-2v-3)+1}e^{\frac{1}{4}(-2\log(1-x)-\log(x))}(x-1)^{\frac{1}{2}\left(\frac{1}{2}(a+v+1)+\frac{1}{2}(a+v+2)+\frac{1}{2}(-2v-3)+1\right)}\,{}_2F_1\left(\frac{1}{2}(-2\right.\right.$$

✓ **Maple** : cpu = 0.083 (sec), leaf count = 76

$$\left\{y(x) = (x-1)^{-\frac{a}{2}} \left(x^{-\frac{v}{2}} {}_2\mathrm{F}_1(-\frac{v}{2}-\frac{a}{2},\frac{1}{2}-\frac{v}{2}-\frac{a}{2};\frac{1}{2}-v;x)\_C1 + x^{\frac{1}{2}+\frac{v}{2}} {}_2\mathrm{F}_1(1+\frac{v}{2}-\frac{a}{2},\frac{1}{2}+\frac{v}{2}-\frac{a}{2};\frac{3}{2}+v;x)\_\right.\right.$$

2.1389 ODE No. 1389

$$y''(x) = -\frac{y(x)\left(-4n^2x - v(v+1)(x-1)^2\right)}{4(x-1)^2x^2} - \frac{(3x-1)y'(x)}{2(x-1)x}$$

✓ **Mathematica** : cpu = 0.385188 (sec), leaf count = 217

$$\left\{\left\{y(x) \to c_2(-1)^{\frac{1}{2}(-2v-3)+1} x^{\frac{1}{4}(-2v-3)+1} e^{\frac{1}{4}(-2\log(1-x)-\log(x))} (x-1)^{\frac{1}{2}\left(n+\frac{1}{2}(2n+1)+\frac{1}{2}(-2v-3)+v+2\right)} {}_2F_1\left(\frac{1}{2}(2n+1)+\right.\right.\right.$$

✓ **Maple** : cpu = 0.081 (sec), leaf count = 68

$$\left\{y(x) = (x-1)^{-n}\left(x^{-\frac{v}{2}} {}_2\mathrm{F}_1(-v-n,-n+\frac{1}{2};\frac{1}{2}-v;x)\_C1 + x^{\frac{1}{2}+\frac{v}{2}} {}_2\mathrm{F}_1(v-n+1,-n+\frac{1}{2};\frac{3}{2}+v;x)\_C2\right)\right\}$$

2.1390 ODE No. 1390

$$y''(x) = -\frac{3y(x)}{16(x-1)^2x^2}$$

✓ **Mathematica** : cpu = 0.0423058 (sec), leaf count = 51

$$\left\{\left\{y(x) \to \frac{2c_2(1-x)^{3/4}x^{5/4}}{\sqrt{-(x-1)x}} + c_1(1-x)^{3/4}\sqrt[4]{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 25

$$\left\{y(x) = \_C1\, x^{\frac{3}{4}}\sqrt[4]{x-1} + \_C2\, \sqrt[4]{x}(x-1)^{\frac{3}{4}}\right\}$$

2.1391 ODE No. 1391

$$y''(x) = \frac{\left(7ax^2+5\right)y'(x)}{x\left(ax^2+1\right)} - \frac{\left(15ax^2+5\right)y(x)}{x^2\left(ax^2+1\right)}$$

✓ **Mathematica** : cpu = 0.058589 (sec), leaf count = 27

$$\left\{\left\{y(x) \to c_1 x^5 - \frac{1}{4}c_2 x\left(2ax^2+1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 20

$$\left\{y(x) = \_C1\, x^5 + 2\,\_C2\, ax^3 + \_C2\, x\right\}$$

2.1392 ODE No. 1392

$$y''(x) = -\frac{bxy'(x)}{a\left(x^2-1\right)} - \frac{y(x)\left(cx^2+dx+e\right)}{a\left(x^2-1\right)^2}$$

✓ **Mathematica** : cpu = 92.8445 (sec), leaf count = 1763961

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✓ **Maple** : cpu = 0.237 (sec), leaf count = 561

$$\left\{y(x) = \left(-\frac{1}{2}+\frac{x}{2}\right)^{\frac{1}{4a}\left(2a+\sqrt{4a^2+(-4b-4c-4d-4e)a+b^2}\right)}\left(x^2-1\right)^{-\frac{b}{4a}}\left(\,{}_2\mathrm{F}_1\left(-\frac{1}{4a}\left(-\sqrt{4a^2+(-4b-4c-4d-4\right.\right.\right.\right.$$

2.1393 ODE No. 1393

$$y''(x) = -\frac{y(x)\left(bx^2+cx+d\right)}{a(x-1)^2x^2}$$

✓ **Mathematica** : cpu = 19.0999 (sec), leaf count = 413606

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✓ **Maple** : cpu = 0.161 (sec), leaf count = 272

$$\left\{y(x) = (x-1)^{-\frac{1}{2}\left(\sqrt{a-4b-4c-4d}-\sqrt{a}\right)\frac{1}{\sqrt{a}}}\left(\,{}_2\mathrm{F}_1\left(-\frac{1}{2}\left(\sqrt{a-4b-4c-4d}-\sqrt{a}-\sqrt{a-4d}+\sqrt{a-4b}\right)\frac{1}{\sqrt{a}},\frac{1}{2}\left(-\right.\right.\right.\right.$$

2.1394 ODE No. 1394

$$y''(x) = -\frac{cy(x)}{x^2(ax+b)^2} - \frac{2y'(x)}{x}$$

✓ **Mathematica** : cpu = 0.0510327 (sec), leaf count = 115

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✓ **Maple** : cpu = 0.12 (sec), leaf count = 79

$$\left\{ y(x) = \sqrt{\frac{ax+b}{x}} \left(\left(\frac{x}{ax+b} \right)^{-\frac{a}{2b}\sqrt{\frac{b^2-4c}{a^2}}} \_C2 + \left(\frac{x}{ax+b} \right)^{\frac{a}{2b}\sqrt{\frac{b^2-4c}{a^2}}} \_C1 \right) \right\}$$

2.1395 ODE No. 1395

$$y''(x) = -\frac{y(x)}{(ax+b)^4}$$

✓ **Mathematica** : cpu = 0.16149 (sec), leaf count = 78

too large to display

✓ **Maple** : cpu = 0.06 (sec), leaf count = 39

too large to display

2.1396 ODE No. 1396

$$y''(x) = -\frac{Ay(x)}{\left(ax^2+bx+c\right)^2}$$

✓ **Mathematica** : cpu = 1.42529 (sec), leaf count = 211

$$\left\{ \left\{ y(x) \to \frac{c_2\sqrt{ax^2+bx+c}\exp\left(-\frac{\sqrt{4ac-b^2}\sqrt{1-\frac{4A}{b^2-4ac}}\tan^{-1}\left(\frac{2ax+b}{\sqrt{4ac-b^2}}\right)}{\sqrt{b^2-4ac}} \right)}{\sqrt{b^2-4ac}\sqrt{1-\frac{4A}{b^2-4ac}}} + c_1\sqrt{x(ax+b)+c}\exp\left(\frac{\sqrt{4ac-b^2}\sqrt{1}\right.\right.\right.$$

✓ **Maple** : cpu = 0.161 (sec), leaf count = 178

$$\left\{y(x)=\sqrt{a x^2+b x+c}\left(\left(1\left(i\sqrt{4\,ca-b^2}-2\,ax-b\right)\left(2\,ax+b+i\sqrt{4\,ca-b^2}\right)^{-1}\right)^{-\frac{a}{2}\sqrt{\frac{-4\,ca+b^2-4\,A}{a^2}}\frac{1}{\sqrt{-4\,ca+b^2}}}\_C\right.\right.$$

2.1397 ODE No. 1397

$$y''(x)=\frac{y(x)}{x^5}-\frac{y'(x)}{x^4}$$

✓ **Mathematica** : cpu = 0.0282503 (sec), leaf count = 38

$$\left\{\left\{y(x)\to\frac{c_2\Gamma\left(\frac{1}{3},-\frac{1}{3x^3}\right)}{3^{2/3}\sqrt[3]{-\frac{1}{x^3}}}+c_1x\right\}\right\}$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 27

$$\left\{y(x)=x\left(-\sqrt{3}\Gamma\left(\frac{2}{3}\right)\Gamma\left(\frac{1}{3},-\frac{1}{3\,x^3}\right)\_C2+2\,\pi\,\_C2+\_C1\right)\right\}$$

2.1398 ODE No. 1398

$$y''(x)=-\frac{\left(-(2v+1)^2+x^2-1\right)y(x)}{\left(x^2-1\right)^2}-\frac{\left(3x^2-1\right)y'(x)}{x\left(x^2-1\right)}$$

✗ **Mathematica** : cpu = 1.47543 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x)\to\text{DifferentialRoot}\left(\{y,x\},\left\{x\left(x^2-4v^2-4v-2\right)y(x)+\left(3x^4-4x^2+1\right)y'(x)+\left(x^5-2x^3+x\right)y''(x)=\right.\right.$$

✓ **Maple** : cpu = 0.189 (sec), leaf count = 69

$$\left\{y(x)=\_C1\left(x^2-1\right)^{-v-\frac{1}{2}}{}_2\mathrm{F}_1(-v,-v;\,-2\,v;\,-x^2+1)+\_C2\left(x^2-1\right)^{v+\frac{1}{2}}{}_2\mathrm{F}_1(v+1,v+1;\,2+2\,v;\,-x^2+1)\right.$$

2.1399 ODE No. 1399

$$y''(x) = \frac{(3x+1)y'(x)}{(x-1)(x+1)} - \frac{36(x+1)^2 y(x)}{(x-1)^2(3x+5)^2}$$

✓ **Mathematica** : cpu = 0.0541528 (sec), leaf count = 72

$$\left\{\left\{y(x) \to c_1 e^{\frac{1}{2}(3\log(1-x)+\log(3x+5))} + \frac{1}{2}c_2 e^{\frac{1}{2}(3\log(1-x)+\log(3x+5))}(3\log(1-x)+\log(3x+5))\right\}\right\}$$

✓ **Maple** : cpu = 0.085 (sec), leaf count = 34

$$\left\{y(x) = (x-1)^{\frac{3}{2}}\sqrt{3x+5}(\_C2\ \ln(3x+5) + 3\_C2\ \ln(x-1) + \_C1)\right\}$$

2.1400 ODE No. 1400

$$y''(x) = \frac{y'(x)}{x} - \frac{a y(x)}{x^6}$$

✓ **Mathematica** : cpu = 0.0512103 (sec), leaf count = 60

$$\left\{\left\{y(x) \to c_1 x^2 e^{\frac{\sqrt{-a}}{2x^2}} + \frac{c_2 x^2 e^{-\frac{\sqrt{-a}}{2x^2}}}{2\sqrt{-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 35

$$\left\{y(x) = x^2\left(\cosh\left(\frac{1}{2x^2}\sqrt{-a}\right)\_C2 + \sinh\left(\frac{1}{2x^2}\sqrt{-a}\right)\_C1\right)\right\}$$

2.1401 ODE No. 1401

$$y''(x) = -\frac{(a+3x^2)\,y'(x)}{x^3} - \frac{b y(x)}{x^6}$$

✓ **Mathematica** : cpu = 0.0144821 (sec), leaf count = 93

$$\left\{\left\{y(x) \to c_1 e^{-\frac{\sqrt{b}\left(-\frac{\sqrt{a^2-4b}}{\sqrt{b}}-\frac{a}{\sqrt{b}}\right)}{4x^2}} + c_2 e^{-\frac{\sqrt{b}\left(\frac{\sqrt{a^2-4b}}{\sqrt{b}}-\frac{a}{\sqrt{b}}\right)}{4x^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.054 (sec), leaf count = 45

$$\left\{y(x) = \_C1\ \mathrm{e}^{-\frac{1}{4x^2}\left(-a+\sqrt{a^2-4b}\right)} + \_C2\ \mathrm{e}^{\frac{1}{4x^2}\left(a+\sqrt{a^2-4b}\right)}\right\}$$

2.1402 ODE No. 1402

$$y''(x) = -\frac{y(x)\left(4a(a+1)x^4 - 2a\left(x^2-1\right)x^2 + \left(x^2-1\right)^2\left(x^2-v^2\right)\right)}{x^2\left(x^2-1\right)^2} - \frac{\left((1-4a)x^2-1\right)y'(x)}{x\left(x^2-1\right)}$$

✗ **Mathematica** : cpu = 4.5375 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x) \to \text{DifferentialRoot}\{\{y,x\},\{\left(x^6+4a^2x^4-v^2x^4+2ax^4-2x^4+2v^2x^2+2ax^2+x^2-v^2\right)y(x)+\left(-4ax^5\right.$$

✓ **Maple** : cpu = 0.305 (sec), leaf count = 58

$$\left\{y(x) = \left(x^2-1\right)^a\left(x^2-1\right)\left(\_C1\, x^v\, HeunC\left(0,v,1,\frac{1}{4},\frac{a}{2}+\frac{1}{4},x^2\right) + \_C2\, x^{-v}\, HeunC\left(0,-v,1,\frac{1}{4},\frac{a}{2}+\frac{1}{4},x^2\right)\right)\right.$$

2.1403 ODE No. 1403

$$y''(x) = -y'(x)\left(\frac{-\text{a1}-\text{b1}+1}{x-\text{c1}} + \frac{-\text{a2}-\text{b2}+1}{x-\text{c2}} + \frac{-\text{a3}-\text{b3}+1}{x-\text{c3}}\right) - \frac{y(x)\left(\frac{\text{a1b1(c1-c2)(c1-c3)}}{x-\text{c1}} + \frac{\text{a2b2(c2-c1)(c2-c3)}}{x-\text{c2}}\right.}{(x-\text{c1})(x-\text{c2})(x-\text{c3})}$$

✗ **Mathematica** : cpu = 97.9766 (sec), leaf count = 0 , DifferentialRoot result

$$\{\{y(x) \to \text{DifferentialRoot}\{\{y,x\},\{(\text{c1}-x)^2(\text{c2}-x)^2y''(x)(\text{c3}-x)^2+(\text{c1}-x)(\text{c2}-x)\left(\text{a1}x^2+\text{a2}x^2+\text{a3}x^2+\right.$$

✓ **Maple** : cpu = 1.052 (sec), leaf count = 298

$$\left\{y(x) = (x-c2)^{a2}(x-c3)^{b3}\left(HeunG\left(\frac{c1-c3}{c1-c2}, \frac{((-2\,a1-a3-b2+2)\,c1+(a1+a3-1)\,c2+c3\,(a1+b\right.\right.\right.$$

2.1404 ODE No. 1404

$$y''(x) = -\frac{\left(1-2x^2\right)y(x)}{4x^6} - \frac{\left(2x^2+1\right)y'(x)}{x^3}$$

✓ **Mathematica** : cpu = 0.0237603 (sec), leaf count = 33

$$\left\{\left\{y(x) \to \frac{c_1 e^{\frac{1}{4x^2}}}{x} + c_2 e^{\frac{1}{4x^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 19

$$\left\{y(x) = \frac{\_C1\, x + \_C2}{x} \mathrm{e}^{\frac{1}{4x^2}}\right\}$$

2.1405 ODE No. 1405

$$y''(x) = \frac{\left(2x^2+1\right)y'(x)}{x^3} - \frac{\left(ax^4+10x^2+1\right)y(x)}{4x^6}$$

✓ **Mathematica** : cpu = 0.0751635 (sec), leaf count = 77

$$\left\{\left\{y(x) \to c_1 e^{-\frac{1}{4x^2}} x^{\frac{3}{2}-\frac{\sqrt{9-a}}{2}} + \frac{c_2 e^{-\frac{1}{4x^2}} x^{\frac{\sqrt{9-a}}{2}+\frac{3}{2}}}{\sqrt{9-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.074 (sec), leaf count = 42

$$\left\{y(x) = \mathrm{e}^{-\frac{1}{4x^2}}\left(x^{\frac{3}{2}-\frac{1}{2}\sqrt{-a+9}}\_C2 + x^{\frac{3}{2}+\frac{1}{2}\sqrt{-a+9}}\_C1\right)\right\}$$

2.1406 ODE No. 1406

$$y''(x) = -\frac{27xy(x)}{16\left(x^3-1\right)^2}$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

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$Aborted
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✓ **Maple** : cpu = 0.158 (sec), leaf count = 44

$$\left\{y(x) = \sqrt{x}\sqrt[4]{x^3-1}\left(LegendreQ\left(-\frac{1}{6},\frac{1}{3},\sqrt{-x^3+1}\right)\_C2 + LegendreP\left(-\frac{1}{6},\frac{1}{3},\sqrt{-x^3+1}\right)\_C1\right)\right\}$$

2.1407 ODE No. 1407

$$y''(x) = -y'(x)\left(\frac{\mathrm{b1}(-\mathrm{al1}-\mathrm{bl1}+1)}{\mathrm{b1}x-\mathrm{a1}} + \frac{\mathrm{b2}(-\mathrm{al2}-\mathrm{bl2}+1)}{\mathrm{b2}x-\mathrm{a2}} + \frac{\mathrm{b3}(-\mathrm{al3}-\mathrm{bl3}+1)}{\mathrm{b3}x-\mathrm{a3}}\right) - \frac{y(x)\left(\frac{\mathrm{al1bl1(a1b2-a2b1)(a3b1-}}{\mathrm{b1}x-\mathrm{a1}}\right.$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

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```

✓ **Maple** : cpu = 2.766 (sec), leaf count = 2597

$$\left\{y(x) = (b3\,x-a3)^{\frac{1}{2}\left((al3+bl3)\sqrt{(2\,al1+2\,al2+2\,al3+2\,bl1+2\,bl2+2\,bl3-4)\sqrt{al3^2+6\,al3\,bl3+bl3^2}+2\,bl3^2+(2\,al1+2\,al2+8\,al3+2\,bl1-}\right.}\right.$$

2.1408 ODE No. 1408

$$y''(x) = -\frac{y(x)\left(Ax^2+B\right)}{x\left(x^2-\text{a1}\right)\left(x^2-\text{a2}\right)\left(x^2-\text{a3}\right)} - \frac{y'(x)\left(x^2\left(\left(x^2-\text{a1}\right)\left(x^2-\text{a2}\right)+\left(x^2-\text{a1}\right)\left(x^2-\text{a3}\right)+\left(x^2-\text{a2}\right)\left(x^2\right.\right.\right.}{x\left(x^2-\text{a1}\right)\left(x^2-\text{a2}\right)\left(x^2-\text{a3}\right.}$$

✗ **Mathematica** : cpu = 60.8376 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\left\{\left(Ax^2+B\right)y(x)+\left(2x^6-\text{a1}x^4-\text{a2}x^4-\text{a3}x^4+\text{a1a2a3}\right)y'(x)-x\left(\text{a1}-x^2\right)\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + \frac{\left(x^2\left(\left(x^2-a1\right)\left(x^2-a2\right)+\left(x^2-a2\right)\left(x^2-a3\right)+\left(x^2-a3\right)\left(x^2-a1\right)\right)-\left(x^2\right.\right.\right.\right.}{\left(x^2-a1\right)\left(x^2-a2\right)x\left(x^2-a3\right)}\right.$$

2.1409 ODE No. 1409

$$y''(x) = -b^2x^{-2a}y(x) - \frac{ay'(x)}{x}$$

✓ **Mathematica** : cpu = 0.0246101 (sec), leaf count = 43

$$\left\{\left\{y(x) \to c_1 \cos\left(\frac{bx^{1-a}}{a-1}\right) - c_2 \sin\left(\frac{bx^{1-a}}{a-1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.016 (sec), leaf count = 39

$$\left\{y(x) = \_C1\ \sin\left(\frac{x^{1-a}b}{a-1}\right) + \_C2\ \cos\left(\frac{x^{1-a}b}{a-1}\right)\right\}$$

2.1410 ODE No. 1410

$$y''(x) = -\frac{y'(x)\left(apx^b+q\right)}{x\left(ax^b-1\right)} - \frac{y(x)\left(arx^b+s\right)}{x^2\left(ax^b-1\right)}$$

✓ **Mathematica** : cpu = 0.133329 (sec), leaf count = 481

$$\left\{\left\{y(x) \to c_1 i^{\frac{-\sqrt{q^2+2q+4s+1}+q+1}{b}} a^{\frac{-\sqrt{q^2+2q+4s+1}+q+1}{2b}} \left(x^b\right)^{\frac{-\sqrt{q^2+2q+4s+1}+q+1}{2b}}\ {}_2F_1\left(\frac{p}{2b}+\frac{q}{2b}-\frac{\sqrt{p^2-2p-4r+1}}{2b}-\frac{\sqrt{}\right.\right.\right.$$

✓ **Maple** : cpu = 0.296 (sec), leaf count = 253

$$\left\{y(x) = \_C1\ {}_2\mathrm{F}_1\left(\frac{1}{2\,b}\left(p+q+\sqrt{q^2+2\,q+4\,s+1}+\sqrt{p^2-2\,p-4\,r+1}\right),\frac{1}{2\,b}\left(p+q+\sqrt{q^2+2\,q+4\,s+1}-\sqrt{}\right.\right.\right.$$

2.1411 ODE No. 1411

$$y''(x) = \frac{y(x)}{e^x + 1}$$

✓ **Mathematica** : cpu = 0.332477 (sec), leaf count = 42

$$\left\{\left\{y(x) \to c_1\left(e^{-x}+1\right) + c_2 e^{-x}\left(e^x \log\left(e^x+1\right) + \log\left(e^x+1\right) + 1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 27

$$\left\{y(x) = \frac{\_C1\,\left(\mathrm{e}^x+1\right)\ln\left(\mathrm{e}^x+1\right) + \_C2\,\mathrm{e}^x + \_C1 + \_C2}{\mathrm{e}^x}\right\}$$

2.1412 ODE No. 1412

$$y''(x) = \frac{y'(x)}{x\log(x)} + y(x)\log^2(x)$$

✓ **Mathematica** : cpu = 0.0165661 (sec), leaf count = 29

$$\{\{y(x) \to c_1 \cosh(x(\log(x)-1)) + ic_2 \sinh(x(\log(x)-1))\}\}$$

✓ **Maple** : cpu = 0.009 (sec), leaf count = 23

$$\{y(x) = \_C1\ \sinh\left(x(\ln(x)-1)\right) + \_C2\ \cosh\left(x(\ln(x)-1)\right)\}$$

2.1413 ODE No. 1413

$$y''(x) = \frac{y'(x)}{x(\log(x)-1)} - \frac{y(x)}{x^2(\log(x)-1)}$$

✗ **Mathematica** : cpu = 0.344401 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -(y[x]/(x^2*(-1 + Log[x]))) + Derivative[1][y][x]/(x*(-
1 + Log[x])), y[x], x]
```

✓ **Maple** : cpu = 0.05 (sec), leaf count = 12

$$\{y(x) = \_C1\ x + \_C2\ \ln(x)\}$$

2.1414 ODE No. 1414

$$y''(x) = y(x)\left(-\operatorname{csch}^2(x)\right)\left(-a^2\sinh^2(x) - (n-1)n\right)$$

✓ **Mathematica** : cpu = 1.13699 (sec), leaf count = 231

$$\left\{\left\{y(x) \to \frac{c_2(-1)^{\frac{1}{2}(-2n-1)+1}\tanh^2(x)^{\frac{1}{4}(-2n-1)+1}\left(\tanh^2(x)-1\right)^{\frac{1}{2}\left(\frac{a+n}{2}+\frac{1}{2}(a+n+1)+\frac{1}{2}(-2n-1)+1\right)-\frac{1}{2}}\,{}_2F_1\left(\frac{1}{2}(-2n-1\right.}{\sqrt{\tanh(x)}}\right.\right.$$

✓ **Maple** : cpu = 0.267 (sec), leaf count = 97

$$\left\{y(x) = \_C1\,(\sinh(x))^n\,{}_2\mathrm{F}_1(-\frac{a}{2}+\frac{n}{2},\frac{a}{2}+\frac{n}{2};\,\frac{1}{2};\,\frac{\cosh(2x)}{2}+\frac{1}{2}) + \_C2\,(\sinh(x))^n\,(2\cosh(2x)+2)^{\frac{3}{4}}\,{}_2\mathrm{F}_1(\frac{1}{2}+\right.$$

2.1415 ODE No. 1415

$$y''(x) = -\left(n^2-a^2\right)y(x) - 2n\coth(x)y'(x)$$

✓ **Mathematica** : cpu = 0.847334 (sec), leaf count = 273

$$\left\{\left\{y(x) \to \frac{c_2(-1)^{\frac{1}{2}(-2n-1)+1}\tanh^2(x)^{\frac{1}{4}(-2n-1)+1}\left(\tanh^2(x)-1\right)^{\frac{1}{2}\left(\frac{a+n}{2}+\frac{1}{2}(a+n+1)+\frac{1}{2}(-2n-1)+1\right)}\,{}_2F_1\left(\frac{1}{2}(-2n-1)-\right.\right.\right.$$

✓ **Maple** : cpu = 0.145 (sec), leaf count = 36

$$\left\{y(x) = (\sinh(x))^{-n+\frac{1}{2}}\left(\mathit{LegendreQ}\left(a-\frac{1}{2},n-\frac{1}{2},\cosh(x)\right)\_C2 + \mathit{LegendreP}\left(a-\frac{1}{2},n-\frac{1}{2},\cosh(x)\right)\_C1\right)\right.$$

2.1416 ODE No. 1416

$$y''(x) = -(v-n)(n+v+1)y(x) - (2n+1)\cot(x)y'(x)$$

✓ **Mathematica** : cpu = 0.205072 (sec), leaf count = 46

$$\left\{\left\{y(x) \to c_1\left(\cos^2(x)-1\right)^{-n/2}P_v^n(\cos(x)) + c_2\left(\cos^2(x)-1\right)^{-n/2}Q_v^n(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.183 (sec), leaf count = 26

$$\left\{y(x) = (\sin(x))^{-n}\left(\mathit{LegendreP}(v,n,\cos(x))\,\_C1 + \mathit{LegendreQ}(v,n,\cos(x))\,\_C2\right)\right\}$$

2.1417 ODE No. 1417

$$y''(x) = -\csc(x)y'(x)\left(\sin^2(x) - \cos(x)\right) - y(x)\sin^2(x)$$

✓ **Mathematica** : cpu = 0.140058 (sec), leaf count = 52

$$\left\{\left\{y(x) \to c_1 e^{\frac{\cos(x)}{2}} \cos\left(\frac{1}{2}\sqrt{3}\cos(x)\right) + c_2 e^{\frac{\cos(x)}{2}} \sin\left(\frac{1}{2}\sqrt{3}\cos(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.148 (sec), leaf count = 31

$$\left\{y(x) = \mathrm{e}^{\frac{\cos(x)}{2}}\left(\sin\left(\frac{\sqrt{3}\cos(x)}{2}\right)\_C1 + \cos\left(\frac{\sqrt{3}\cos(x)}{2}\right)\_C2\right)\right\}$$

2.1418 ODE No. 1418

$$y''(x) = \frac{y(x)\sin(x)}{x\cos(x) - \sin(x)} - \frac{x\sin(x)y'(x)}{x\cos(x) - \sin(x)}$$

✗ **Mathematica** : cpu = 1.26035 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == (Sin[x]*y[x])/(x*Cos[x] - Sin[x]) - (x*Sin[x]*Derivative[1][y]
```

✓ **Maple** : cpu = 15.536 (sec), leaf count = 59

$$\left\{y(x) = \sin(x)\left(\int \mathrm{e}^{\int \frac{-2(\cos(x))^3 x + 3(\cos(x))^2 \sin(x) - \sin(x)}{\cos(x)(\cos(x)x - \sin(x))\sin(x)}\,\mathrm{d}x} \cos(x)\,\mathrm{d}x\_C2 + \_C1\right)\right\}$$

2.1419 ODE No. 1419

$$y''(x) = -\frac{\sec(x)y'(x)\left(x^2\sin(x) - 2x\cos(x)\right)}{x^2} - \frac{y(x)\sec(x)(2x\cos(x) - x\sin(x))}{x^2}$$

✗ **Mathematica** : cpu = 1.16478 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -((Sec[x]*(2*x*Cos[x] - x*Sin[x])*y[x])/x^2) - (Sec[x]*(-
2*x*Cos[x] + x^2*Sin[x])*Derivative[1][y][x])/x^2, y[x], x]
```

✓ **Maple** : cpu = 0.239 (sec), leaf count = 12

$$\{y(x) = x(\sin(x)\_C2 + \_C1)\}$$

2.1420 ODE No. 1420

$$\cos^2(x)y''(x) - y(x)\left(a\cos^2(x) + (n-1)n\right) = 0$$

✓ **Mathematica** : cpu = 0.440619 (sec), leaf count = 134

$$\left\{\left\{y(x) \to c_1 i^{1-n}\cos^{1-n}(x)\,{}_2F_1\left(-\frac{n}{2} - \frac{i\sqrt{a}}{2} + \frac{1}{2}, -\frac{n}{2} + \frac{i\sqrt{a}}{2} + \frac{1}{2}; \frac{3}{2} - n; \cos^2(x)\right) + c_2 i^n \cos^n(x)\,{}_2F_1\left(\frac{n}{2} - \frac{i\sqrt{a}}{2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.325 (sec), leaf count = 123

$$\left\{y(x) = \_C1\ \sin(2\,x)\,(\cos(x))^{-n}\,{}_2\mathrm{F}_1(1 + \frac{i}{2}\sqrt{a} - \frac{n}{2}, 1 - \frac{i}{2}\sqrt{a} - \frac{n}{2};\ \frac{3}{2} - n;\ \frac{\cos(2\,x)}{2} + \frac{1}{2}) + \_C2\ (\cos(x))^{n}\ (-2\right.$$

2.1421 ODE No. 1421

$$y''(x) = -a^2 n y(x)\sec^2(ax)\left((n-1)\sin^2(ax) + \cos^2(ax)\right) - a(n-1)\sin(2ax)\sec^2(ax)y'(x)$$

✓ **Mathematica** : cpu = 0.248482 (sec), leaf count = 67

$$\left\{\left\{y(x) \to c_1 e^{-\sqrt{-a^2}x}\cos^{n-1}(ax) + \frac{c_2 e^{\sqrt{-a^2}x}\cos^{n-1}(ax)}{2\sqrt{-a^2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.076 (sec), leaf count = 27

$$\left\{y(x) = \_C1\ (\cos(ax))^{n} + \_C2\ \sin(ax)\,(\cos(ax))^{n-1}\right\}$$

2.1422 ODE No. 1422

$$y''(x) = 2y(x)\csc^2(x)$$

✓ **Mathematica** : cpu = 0.0867199 (sec), leaf count = 64

$$\left\{\left\{y(x) \to \frac{c_1\cos(x)}{\sqrt{\cos^2(x)-1}} + \frac{c_2\left(\cos(x)\log\left(\sqrt{\cos^2(x)-1} + \cos(x)\right) - \sqrt{\cos^2(x)-1}\right)}{\sqrt{\cos^2(x)-1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.254 (sec), leaf count = 50

$$\left\{y(x) = \frac{-i\ln(\cos(2\,x) + i\sin(2\,x))\sin(2\,x)\_C2 + \_C1\ \sin(2\,x) + 2\_C2\,(\cos(2\,x) - 1)}{\cos(2\,x) - 1}\right\}$$

2.1423 ODE No. 1423

$$y''(x) = -a y(x) \csc^2(x)$$

✓ **Mathematica** : cpu = 0.0715893 (sec), leaf count = 70

$$\left\{\left\{y(x) \to c_1 \sqrt[4]{\cos^2(x)-1} P^{\frac{1}{2}\sqrt{1-4a}}_{-\frac{1}{2}}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x)-1} Q^{\frac{1}{2}\sqrt{1-4a}}_{-\frac{1}{2}}(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.28 (sec), leaf count = 132

$$\left\{y(x) = 1 \sqrt[4]{2\cos(2x)+2}\left(\frac{\cos(2x)}{2} - \frac{1}{2}\right)^{\frac{1}{4}\sqrt{1-4a}} \sqrt{-2\cos(2x)+2}\left({}_2\mathrm{F}_1\left(\frac{1}{4}\sqrt{1-4a}+\frac{3}{4}, \frac{1}{4}\sqrt{1-4a}+\frac{3}{4}; \frac{3}{2};\right.\right.\right.$$

2.1424 ODE No. 1424

$$\sin^2(x) y''(x) - y(x)\left(a\sin^2(x) + (n-1)n\right) = 0$$

✓ **Mathematica** : cpu = 0.173365 (sec), leaf count = 90

$$\left\{\left\{y(x) \to c_1 \sqrt[4]{\cos^2(x)-1} P^{\frac{1}{2}(2n-1)}_{\frac{1}{2}i(2\sqrt{a}+i)}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x)-1} Q^{\frac{1}{2}(2n-1)}_{\frac{1}{2}i(2\sqrt{a}+i)}(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.289 (sec), leaf count = 120

$$\left\{y(x) = 1\left(\frac{\cos(2x)}{2} - \frac{1}{2}\right)^{\frac{n}{2}} \left({}_2\mathrm{F}_1\left(\frac{1}{2}+\frac{i}{2}\sqrt{a}+\frac{n}{2}, \frac{1}{2}-\frac{i}{2}\sqrt{a}+\frac{n}{2}; \frac{3}{2}; \frac{\cos(2x)}{2}+\frac{1}{2}\right)(2\cos(2x)+2)^{\frac{3}{4}} \sqrt[4]{-2\cos(2\right.\right.\right.$$

2.1425 ODE No. 1425

$$y''(x) = y(x)\csc^2(x)\left(-\left(-a^2\cos^2(x) - (3-2a)\cos(x) + 3a - 3\right)\right)$$

✓ **Mathematica** : cpu = 0.760992 (sec), leaf count = 236

$$\left\{\left\{y(x) \to \frac{c_2\sqrt{1-\cos(x)}\left(-\frac{(2a-1)(\cos(x)+1)}{-2a\cos(x)+\cos(x)+2}\right)^{a+\frac{1}{2}}(-2a\cos(x)+\cos(x)+2)\left(1-\cos^2(x)\right)^{-a}\left(\frac{(2a-1)(\cos(x)-1)}{(2a-1)\cos(x)-2}\right.\right.\right.}{2}$$

✓ **Maple** : cpu = 0.47 (sec), leaf count = 91

$$\left\{y(x) = 1\left(\_C2\,{}_2\mathrm{F}_1\left(a-\frac{1}{2}, -\frac{1}{2}-a; \frac{3}{2}-a; \frac{\cos(x)}{2}+\frac{1}{2}\right)(\cos(x)+1)^{-\frac{1}{4}-\frac{a}{2}}\sqrt{2\cos(x)+2}(\cos(x)-1)^{\frac{a}{2}-\frac{1}{4}} + 2\right.\right.$$

2.1426 ODE No. 1426

$$\sin^2(x)y''(x) - y(x)\left(a^2\cos^2(x) + \frac{b^2}{(2a-3)^2} + 3a + b\cos(x) + 2\right) = 0$$

✓ **Mathematica** : cpu = 6.08872 (sec), leaf count = 4128

$$\left\{\left\{y(x) \to c_1(\cos(x)+1)^{\frac{1}{2}\left(-\frac{8a^2}{-16a^2+48a-36}+\frac{24a}{-16a^2+48a-36}+a-\frac{-32a^2+96a+\sqrt{\left(32a^2-96a+72\right)^2-4\left(-16a^2+48a-36\right)\left(16a^4+16ba^2-88a^2-\right.}}{2\left(-16a^2+48a-36\right)}\right.}\right.\right.$$

✓ **Maple** : cpu = 0.643 (sec), leaf count = 549

$$\left\{y(x) = 1\left(\frac{\cos(x)}{2}-\frac{1}{2}\right)^{\frac{1}{8a-12}\left(4a-6+\sqrt{4b^2+16(a-3/2)^2b+16a^4-72a^2+81}\right)}\left({}_2\mathrm{F}_1\left(\frac{1}{8a-12}\left(8a^2-\sqrt{4b^2-16\ (a-3/\right.\right.\right.\right.$$

2.1427 ODE No. 1427

$$y''(x) = y(x)\left(-\csc^2(x)\right)\left(-\left(a^2b^2-(a+1)^2\right)\sin^2(x) - a(a+1)b\sin(2x) - (a-1)a\right)$$

✗ **Mathematica** : cpu = 200.887 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -(Csc[x]^2*(-((-1 + a)*a) - (-(1 + a)^2 + a^2*b^2)*Sin[x]^2 -
```

✓ **Maple** : cpu = 1.68 (sec), leaf count = 179

$$\left\{y(x) = 1e^{\int \frac{1}{\sin(2x)(b\sin(2x)+\cos(2x)+1)}\left(2b((a+1)\cos(2x)+a+1/2)\sin(2x)-\left(\left(ab^2-a-2\right)\cos(2x)-ab^2-a+1\right)(\cos(2x)+1)\right)dx}\left(\int -2e^{-}\right.\right.$$

2.1428 ODE No. 1428

$$y''(x) = y(x)\left(-\csc^2(x)\right)\left(a\cos^2(x) + b\sin^2(x) + c\right)$$

✓ **Mathematica** : cpu = 0.404768 (sec), leaf count = 104

$$\left\{\left\{y(x) \to c_1 \sqrt[4]{\cos^2(x)-1}\, P^{\frac{1}{2}\sqrt{-4a-4c+1}}_{\frac{1}{2}(2\sqrt{b-a}-1)}(\cos(x)) + c_2 \sqrt[4]{\cos^2(x)-1}\, Q^{\frac{1}{2}\sqrt{-4a-4c+1}}_{\frac{1}{2}(2\sqrt{b-a}-1)}(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.323 (sec), leaf count = 183

$$\left\{y(x) = 1\sqrt[4]{2\cos(2x)+2}\left(\frac{\cos(2x)}{2} - \frac{1}{2}\right)^{\frac{1}{4}\sqrt{-4a+1-4c}}\sqrt{-2\cos(2x)+2}\left({}_2\mathrm{F}_1\left(\frac{1}{4}\sqrt{-4a+1-4c} + \frac{1}{2}\sqrt{-a+b}\right.\right.\right.$$

2.1429 ODE No. 1429

$$y''(x) = y(x)\csc^2(x) - \cot(x)y'(x)$$

✓ **Mathematica** : cpu = 0.0584828 (sec), leaf count = 51

$$\left\{\left\{y(x) \to c_1 \cosh\left(\log\left(\cos\left(\frac{x}{2}\right)\right) - \log\left(\sin\left(\frac{x}{2}\right)\right)\right) - ic_2 \sinh\left(\log\left(\cos\left(\frac{x}{2}\right)\right) - \log\left(\sin\left(\frac{x}{2}\right)\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 25

$$\left\{y(x) = \frac{\sin(x)\_C1}{\cos(x)-1} + \frac{(\cos(x)-1)\_C2}{\sin(x)}\right\}$$

2.1430 ODE No. 1430

$$y''(x) = y(x)\csc^2(x)\left(-\left(v(v+1)\sin^2(x) - n^2\right)\right) - \cot(x)y'(x)$$

✓ **Mathematica** : cpu = 0.474691 (sec), leaf count = 22

$$\{\{y(x) \to c_1 P_v^n(\cos(x)) + c_2 Q_v^n(\cos(x))\}\}$$

✓ **Maple** : cpu = 0.366 (sec), leaf count = 101

$$\left\{y(x) = 1\left(\frac{\cos(2x)}{2} - \frac{1}{2}\right)^{\frac{n}{2}}\left(\sin(2x)\,{}_2\mathrm{F}_1\left(1 + \frac{v}{2} + \frac{n}{2}, \frac{1}{2} - \frac{v}{2} + \frac{n}{2}; \frac{3}{2}; \frac{\cos(2x)}{2} + \frac{1}{2}\right)\_C1 + {}_2\mathrm{F}_1\left(-\frac{v}{2} + \frac{n}{2}, \frac{1}{2} + \frac{v}{2}\right.\right.\right.$$

2.1431 ODE No. 1431

$$y''(x) = \cot(2x)y'(x) - 2y(x)$$

✓ **Mathematica** : cpu = 0.221263 (sec), leaf count = 80

$$\left\{\left\{y(x) \to c_1\left(\cos^2(x) - \frac{1}{2}\right) - \frac{2}{3}c_2\cos^{\frac{3}{2}}(x)\left(2\cos^2(x)\,{}_2F_1\left(\frac{1}{4},\frac{3}{4};\frac{7}{4};\cos^2(x)\right) - {}_2F_1\left(\frac{1}{4},\frac{3}{4};\frac{7}{4};\cos^2(x)\right) + 3(1 - c\right.\right.$$

✓ **Maple** : cpu = 0.233 (sec), leaf count = 30

$$\left\{y(x) = (\sin(2\,x))^{\frac{3}{4}}\left(LegendreQ\left(\frac{1}{4},\frac{3}{4},\cos(2\,x)\right)\_C2 + LegendreP\left(\frac{1}{4},\frac{3}{4},\cos(2\,x)\right)\_C1\right)\right\}$$

2.1432 ODE No. 1432

$$y''(x) = -\cot(x)y'(x) - \frac{1}{4}y(x)\left(-17\sin^2(x) - 1\right)\csc^2(x)$$

✓ **Mathematica** : cpu = 0.0973101 (sec), leaf count = 37

$$\left\{\left\{y(x) \to \frac{c_1 e^{-2x}}{\sqrt{\sin(x)}} + \frac{c_2 e^{2x}}{4\sqrt{\sin(x)}}\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 22

$$\left\{y(x) = (\_C2\,\cosh(2\,x) + \_C1\,\sinh(2\,x))\frac{1}{\sqrt{\sin(x)}}\right\}$$

2.1433 ODE No. 1433

$$y''(x) = -\frac{y(x)\sec^2(x)\left(2x^2 + x^2\sin^2(x) - 24\cos^2(x)\right)}{4x^2} - \tan(x)y'(x) + \sqrt{\cos(x)}$$

✓ **Mathematica** : cpu = 0.257467 (sec), leaf count = 46

$$\left\{\left\{y(x) \to \frac{1}{5}c_2 x^3\sqrt{\cos(x)} + \frac{c_1\sqrt{\cos(x)}}{x^2} - \frac{1}{4}x^2\sqrt{\cos(x)}\right\}\right\}$$

✓ **Maple** : cpu = 0.116 (sec), leaf count = 28

$$\left\{y(x) = \frac{4\,x^5\_C1 - x^4 + 4\,\_C2}{4\,x^2}\sqrt{\cos(x)}\right\}$$

2.1434 ODE No. 1434

$$y''(x) = -\frac{b\cot(x)y'(x)}{a} - \frac{y(x)\csc^2(x)\left(c\cos^2(x)+d\cos(x)+e\right)}{a}$$

✓ **Mathematica** : cpu = 107.712 (sec), leaf count = 1596424

too large to display

✓ **Maple** : cpu = 0.68 (sec), leaf count = 517

$$\left\{y(x) = (\sin(x))^{-\frac{a+b}{2a}}\left(\frac{\cos(x)}{2}-\frac{1}{2}\right)^{\frac{1}{4a}\left(2a+\sqrt{a^2+(-2b-4c-4d-4e)a+b^2}\right)}\left({}_2\mathrm{F}_1(\frac{1}{4a}\left(\sqrt{a^2+(-2b-4c-4d-4e)}\right.\right.\right.$$

2.1435 ODE No. 1435

$$y''(x) = -4y(x)\sin(3x)\csc^3(x)$$

✓ **Mathematica** : cpu = 0.14272 (sec), leaf count = 70

$$\left\{\left\{y(x)\to c_1\sqrt[4]{\cos^2(x)-1}P^{\frac{i\sqrt{47}}{2}}_{-\frac{1}{2}+4i}(\cos(x))+c_2\sqrt[4]{\cos^2(x)-1}Q^{\frac{i\sqrt{47}}{2}}_{-\frac{1}{2}+4i}(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.171 (sec), leaf count = 38

$$\left\{y(x) = \sqrt{\sin(x)}\left(LegendreQ\left(-\frac{1}{2}+4i,\frac{i}{2}\sqrt{47},\cos(x)\right)\_C2+LegendreP\left(-\frac{1}{2}+4i,\frac{i}{2}\sqrt{47},\cos(x)\right)\_C1\right)\right\}$$

2.1436 ODE No. 1436

$$y''(x) = -\frac{1}{4}y(x)\csc^2(x)\left(-4n^2+4v(v+1)\sin^2(x)-\cos^2(x)+2\right)$$

✓ **Mathematica** : cpu = 0.540458 (sec), leaf count = 42

$$\left\{\left\{y(x)\to c_1\sqrt[4]{\cos^2(x)-1}P_v^n(\cos(x))+c_2\sqrt[4]{\cos^2(x)-1}Q_v^n(\cos(x))\right\}\right\}$$

✓ **Maple** : cpu = 0.281 (sec), leaf count = 113

$$\left\{y(x) = 1\sqrt{-2\cos(2x)+2}\sqrt[4]{2\cos(2x)+2}\left(\frac{\cos(2x)}{2}-\frac{1}{2}\right)^{\frac{n}{2}}\left({}_2\mathrm{F}_1(1+\frac{v}{2}+\frac{n}{2},\frac{1}{2}-\frac{v}{2}+\frac{n}{2};\frac{3}{2};\frac{\cos(2x)}{2}+\frac{1}{2})\right.\right.$$

2.1437 ODE No. 1437

$$y''(x) = \left(3\sin^2(x)+1\right)\csc(x)\sec(x)y'(x) + y(x)\tan^2(x)$$

✓ **Mathematica** : cpu = 0.281029 (sec), leaf count = 44

$$\left\{\left\{y(x) \to c_1 \cos^{\frac{\sqrt{13}}{2}-\frac{3}{2}}(x) + c_2 \cos^{-\frac{3}{2}-\frac{\sqrt{13}}{2}}(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.177 (sec), leaf count = 29

$$\left\{y(x) = \_C1\,(\cos(x))^{-\frac{3}{2}+\frac{\sqrt{13}}{2}} + \_C2\,(\cos(x))^{-\frac{3}{2}-\frac{\sqrt{13}}{2}}\right\}$$

2.1438 ODE No. 1438

$$y''(x) = y(x)\left(-\csc^2(x)\right)\sec^2(x)\left(-a\sin^2(x)\cos^2(x) - (m-1)m\sin^2(x) - (n-1)n\cos^2(x)\right)$$

✓ **Mathematica** : cpu = 0.938034 (sec), leaf count = 615

$$\left\{\left\{y(x) \to \frac{c_2(-1)^{\frac{1}{2}(-2m-1)+1}\cos^2(x)^{\frac{1}{4}(-2m-1)+1}\left(\cos^2(x)-1\right)^{\frac{1}{2}\left(\frac{4am+4\sqrt{-a}n^2+4an-4\sqrt{-a}n+4(-a)^{3/2}+8\sqrt{-a}a+\sqrt{-a}+4mn^2-4}{8a+8n^2-8n+2}\right.}\right.\right.$$

✓ **Maple** : cpu = 0.181 (sec), leaf count = 102

$$\left\{y(x) = (\sin(x))^n\left((\cos(x))^{-m+1}\,{}_2\mathrm{F}_1\left(\frac{n}{2}-\frac{m}{2}+\frac{i}{2}\sqrt{a}+\frac{1}{2},\frac{n}{2}-\frac{m}{2}-\frac{i}{2}\sqrt{a}+\frac{1}{2};\frac{3}{2}-m;(\cos(x))^2\right)\_C2 + (\cos(\right.\right.\right.$$

2.1439 ODE No. 1439

$$y''(x) = \frac{\phi'(x)y'(x)}{\phi(x)-\phi(a)} - \frac{y(x)\left(\phi''(a) - n(n+1)(\phi(x)-\phi(a))^2\right)}{\phi(x)-\phi(a)}$$

✗ **Mathematica** : cpu = 0.803159 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == (Derivative[1][phi][x]*Derivative[1][y][x])/(-phi[a] + phi[x])
(n*(1 + n)*(-phi[a] + phi[x])^2) + Derivative[2][phi][a]))/(-phi[a] + phi[x]), y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) - \frac{\left(\frac{\mathrm{d}}{\mathrm{d}x}\phi(x)\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{\phi(x)-\phi(a)} + \frac{\left(-n(n+1)(\phi(x)-\phi(a))^2 + \frac{\mathrm{d}^2}{\mathrm{d}a^2}\phi(a)\right)\_Y(x)}{\phi(x)-\phi(a)}\right\}, \{\_Y\right.\right.$$

2.1440 ODE No. 1440

$$y''(x) = -\frac{y'(x)\left(-\phi''(x) - \phi(x)\phi'(x) + \phi(x^3)\right)}{\phi'(x) + \phi(x)^2} - \frac{y(x)\left(-\phi(x)\phi''(x) + \phi(x)^2\left(-\phi'(x)\right) + \phi'(x)^2\right)}{\phi'(x) + \phi(x)^2}$$

✗ **Mathematica** : cpu = 0.864044 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -((Derivative[1][y][x]*(phi[x^3] - phi[x]*Derivative[1][phi][x
(phi[x]^2*Derivative[1][phi][x]) + Derivative[1][phi][x]^2 - phi[x]*Derivative[2][phi][x]))/
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\left(\left(\frac{\mathrm{d}}{\mathrm{d}x}\phi(x)\right)^2 - (\phi(x))^2\frac{\mathrm{d}}{\mathrm{d}x}\phi(x) - \phi(x)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\phi(x)\right)\_Y(x)}{\frac{\mathrm{d}}{\mathrm{d}x}\phi(x) + (\phi(x))^2} + \frac{\left(\phi(x^3) - \phi(x)\frac{\mathrm{d}}{\mathrm{d}x}\phi(x) - \frac{\mathrm{d}^2}{\mathrm{d}x^2}\phi(x)\right)}{\frac{\mathrm{d}}{\mathrm{d}x}\phi(x) + (\phi(x))^2}\right.\right.$$

2.1441 ODE No. 1441

$$y''(x) = -\frac{y'(x)(-\mathrm{cn}(x|k)\mathrm{dn}(x|k) - 2\mathrm{sn}(x|k))}{\mathrm{sn}(x|k)^2 - \mathrm{sn}(a|k)^2} - \frac{y(x)\left(6k^2\mathrm{sn}(a|k)^4 - 4\left(k^2+1\right)\mathrm{sn}(a|k)^2 + 2\right)}{\mathrm{sn}(x|k)^2 - \mathrm{sn}(a|k)^2} - \frac{1}{\mathrm{sn}(x|k)^2 - \mathrm{sn}(a|k)}$$

✗ **Mathematica** : cpu = 1.55144 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -(-JacobiSN[a, k]^2 + JacobiSN[x, k]^2)^(-1) - ((2 - 4*(1 + k^
JacobiSN[a, k]^2 + JacobiSN[x, k]^2) - ((-(JacobiCN[x, k]*JacobiDN[x, k]) - 2*JacobiSN[x, k]
JacobiSN[a, k]^2 + JacobiSN[x, k]^2), y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) - 2\frac{JacobiSN(x,k)\,JacobiCN(x,k)\,JacobiDN(x,k)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{\left(JacobiSN(x,k)\right)^2 - JacobiSN(a,k)} - \frac{\left(-2 + 4\left(k^2+1\right.\right.\right.\right.$$

2.1442 ODE No. 1442

$$y''(x) = \frac{y(x)}{f(x)} - \frac{xy'(x)}{f(x)}$$

✗ **Mathematica** : cpu = 0.220951 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == y[x]/f[x] - (x*Derivative[1][y][x])/f[x], y[x], x]
```

✓ **Maple** : cpu = 0.07 (sec), leaf count = 30

$$\left\{y(x) = x\left(\int \mathrm{e}^{\int \frac{1}{x}\left(-2-\frac{x^2}{f(x)}\right)\mathrm{d}x}\mathrm{d}x\_C1 + \_C2\right)\right\}$$

2.1443 ODE No. 1443

$$y''(x) = -\frac{f'(x)y'(x)}{2f(x)} - \frac{g(x)y(x)}{f(x)}$$

✗ **Mathematica** : cpu = 0.271059 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -((g[x]*y[x])/f[x]) - (Derivative[1][f][x]*Derivative[1][y][x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{g(x)\_Y(x)}{f(x)} + \frac{\left(\frac{\mathrm{d}}{\mathrm{d}x}f(x)\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{2f(x)} + \frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1444 ODE No. 1444

$$y''(x) = -by(x)f(x)^{2a} - \frac{af'(x)y'(x)}{f(x)}$$

✗ **Mathematica** : cpu = 1.48694 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -(b*f[x]^(2*a)*y[x]) - (a*Derivative[1][f][x]*Derivative[1][y]
```

✓ **Maple** : cpu = 0.015 (sec), leaf count = 37

$$\left\{y(x) = \_C1\, \mathrm{e}^{\int i(f(x))^a\sqrt{b}\,\mathrm{d}x} + \_C2\, \mathrm{e}^{-\int i(f(x))^a\sqrt{b}\,\mathrm{d}x}\right\}$$

2.1445 ODE No. 1445

$$y''(x) = -\frac{y'(x)\left(2f(x)g(x)g'(x)^2 - \left(g(x)^2-1\right)\left(2f'(x)g'(x) + f(x)g''(x)\right)\right)}{f(x)\left(g(x)^2-1\right)g'(x)} - \frac{y(x)\left(\left(g(x)^2-1\right)\left(f'(x)\left(2f'(x)g'(x\right.\right.}$$

✗ **Mathematica** : cpu = 1.3343 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[2][y][x] == -((Derivative[1][y][x]*(2*f[x]*g[x]*Derivative[1][g][x]^2 - (-
1 + g[x]^2)*(2*Derivative[1][f][x]*Derivative[1][g][x] + f[x]*Derivative[2][g][x])))/(f[x]*(
1 + g[x]^2)*Derivative[1][g][x])) - (y[x]*(-(f[x]*Derivative[1][g][x]^2*(2*g[x]*Derivative[1
1 + g[x]^2)*(-(f[x]*Derivative[1][g][x]*Derivative[2][f][x]) + Derivative[1][f][x]*(2*Deriva
1 + g[x]^2)*Derivative[1][g][x]), y[x], x]
```

✓ **Maple** : cpu = 0.279 (sec), leaf count = 20

$$\{y(x) = f(x)\left(LegendreP(v, g(x))\_C1 + LegendreQ(v, g(x))\_C2\right)\}$$

2.1446 ODE No. 1446

$$y''(x) = -\frac{(x-1)y(x)}{x^4} - \frac{y'(x)}{x}$$

✓ **Mathematica** : cpu = 0.0233401 (sec), leaf count = 33

$$\left\{\left\{y(x) \to c_1 e^{-1/x} - c_2 e^{-1/x} \text{Ei}\left(\frac{2}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 22

$$\left\{y(x) = \mathrm{e}^{-x^{-1}} \left(Ei\left(1, -2\,x^{-1}\right) \_C2 + \_C1\right)\right\}$$

2.1447 ODE No. 1447

$$y''(x) = -\frac{(-x-1)y(x)}{x^4} - \frac{y'(x)}{x}$$

✓ **Mathematica** : cpu = 0.0207867 (sec), leaf count = 29

$$\left\{\left\{y(x) \to c_1 e^{\frac{1}{x}} - c_2 e^{\frac{1}{x}} \text{Ei}\left(-\frac{2}{x}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.06 (sec), leaf count = 20

$$\left\{y(x) = \mathrm{e}^{x^{-1}} \left(Ei\left(1, 2\,x^{-1}\right) \_C2 + \_C1\right)\right\}$$

2.1448 ODE No. 1448

$$y''(x) = -\frac{b^2 y(x)}{\left(x^2 - a^2\right)^2}$$

✓ **Mathematica** : cpu = 0.32539 (sec), leaf count = 149

$$\left\{\left\{y(x) \to c_1 (x-a)^{\frac{1}{2}\sqrt{1-\frac{b^2}{a^2}}+\frac{1}{2}} (a+x)^{\frac{1}{2}-\frac{1}{2}\sqrt{1-\frac{b^2}{a^2}}} - \frac{c_2 (x-a)^{\frac{1}{2}-\frac{1}{2}\sqrt{\frac{a^2-b^2}{a^2}}} (a+x)^{\frac{1}{2}\sqrt{\frac{a^2-b^2}{a^2}}+\frac{1}{2}}}{2a\sqrt{\frac{a^2-b^2}{a^2}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.103 (sec), leaf count = 77

$$\left\{y(x) = \sqrt{(a-x)(x+a)}\left(\left(\frac{a-x}{x+a}\right)^{-\frac{1}{2a}\sqrt{a^2-b^2}} \_C2 + \left(\frac{a-x}{x+a}\right)^{\frac{1}{2a}\sqrt{a^2-b^2}} \_C1\right)\right\}$$

2.1449 ODE No. 1449

$$y^{(3)}(x) - \lambda y(x) = 0$$

✓ **Mathematica** : cpu = 0.0156852 (sec), leaf count = 53

$$\left\{\left\{y(x) \to c_1 e^{(-1)^{2/3}\sqrt[3]{\lambda}x} + c_2 e^{-\sqrt[3]{-1}\sqrt[3]{\lambda}x} + c_3 e^{\sqrt[3]{\lambda}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 47

$$\left\{y(x) = \_C1\, \mathrm{e}^{-\frac{\left(i\sqrt{3}+1\right)x}{2}\sqrt[3]{\lambda}} + \_C2\, \mathrm{e}^{\frac{\left(i\sqrt{3}-1\right)x}{2}\sqrt[3]{\lambda}} + \_C3\, \mathrm{e}^{\sqrt[3]{\lambda}x}\right\}$$

2.1450 ODE No. 1450

$$ax^3 y(x) - bx + y^{(3)}(x) = 0$$

✗ **Mathematica** : cpu = 300.007 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.233 (sec), leaf count = 1616

$$\left\{y(x) = \int -11211200\, bx^3 \left(\left(-5/8\, x^6 {}_0\mathrm{F}_2\left(\,;\frac{13}{6},7/3;-\frac{x^6 a}{216}\right)a + 35\, {}_0\mathrm{F}_2\left(\,;7/6,4/3;-\frac{x^6 a}{216}\right)\right) {}_0\mathrm{F}_2\left(\,;5/6,7/6;-\frac{x^6}{21}\right.\right.\right.$$

2.1451 ODE No. 1451

$$y^{(3)}(x) - ax^b y(x) = 0$$

✓ **Mathematica** : cpu = 0.0231792 (sec), leaf count = 168

$$\left\{\left\{y(x) \to (-1)^{\frac{1}{b+3}}(b+3)^{-\frac{3}{b+3}} c_2 x a^{\frac{1}{b+3}}\, {}_0F_2\left(;1-\frac{1}{b+3},1+\frac{1}{b+3};\frac{ax^{b+3}}{(b+3)^3}\right) + (-1)^{\frac{2}{b+3}}(b+3)^{-\frac{6}{b+3}} c_3 x^2 a^{\frac{2}{b+3}}\, {}_0F_2\right.\right.$$

✓ **Maple** : cpu = 0.092 (sec), leaf count = 114

$$\left\{y(x) = \_C1\, {}_0\mathrm{F}_2\left(\,;\frac{b+1}{b+3},\frac{b+2}{b+3};\frac{x^{b+3}a}{(b+3)^3}\right) + \_C2\, x\, {}_0\mathrm{F}_2\left(\,;\frac{b+2}{b+3},\frac{b+4}{b+3};\frac{x^{b+3}a}{(b+3)^3}\right) + \_C3\, x^2\, {}_0\mathrm{F}_2\left(\,;\frac{b+4}{b+3},\frac{b+5}{b+3}\right.\right.$$

2.1452 ODE No. 1452

$$y^{(3)}(x)+3y'(x)-4y(x)=0$$

✓ **Mathematica** : cpu = 0.00803571 (sec), leaf count = 54

$$\left\{\left\{y(x)\to c_3e^x+c_1e^{-x/2}\sin\left(\frac{\sqrt{15}x}{2}\right)+c_2e^{-x/2}\cos\left(\frac{\sqrt{15}x}{2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.008 (sec), leaf count = 35

$$\left\{y(x)=\_C1\,\mathrm{e}^{x}+\_C2\,\mathrm{e}^{-\frac{x}{2}}\sin\left(\frac{\sqrt{15}x}{2}\right)+\_C3\,\mathrm{e}^{-\frac{x}{2}}\cos\left(\frac{\sqrt{15}x}{2}\right)\right\}$$

2.1453 ODE No. 1453

$$a^2(-y'(x))-e^{2ax}\sin^2(x)+y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.628851 (sec), leaf count = 128

$$\left\{\left\{y(x)\to\frac{e^{-ax}\left(-9\left(a^2-4\right)a^4e^{3ax}\cos(2x)-3\left(11a^2-4\right)a^3e^{3ax}\sin(2x)+\left(9a^6+49a^4+56a^2+16\right)\left(12a^2c_1e^{2ax}\right.\right.\right.}{12a^3\left(9a^6+49a^4+56a^2+16\right)}$$

✓ **Maple** : cpu = 0.138 (sec), leaf count = 122

$$\left\{y(x)=\frac{1}{108\,a^9+588\,a^7+672\,a^5+192\,a^3}\left(\left(\left(-9\,a^6+36\,a^4\right)\cos\left(2\,x\right)+\left(-33\,a^5+12\,a^3\right)\sin\left(2\,x\right)+9\,a^6+49\,a^4\right.\right.\right.$$

2.1454 ODE No. 1454

$$2axy'(x)+ay(x)+y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.0103991 (sec), leaf count = 79

$$\left\{\left\{y(x)\to c_1\mathrm{Ai}\left(\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}x\right)^2+c_3\mathrm{Bi}\left(\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}x\right)^2+c_2\mathrm{Ai}\left(\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}x\right)\mathrm{Bi}\left(\sqrt[3]{-\frac{1}{2}}\sqrt[3]{a}x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 55

$$\left\{y(x)=\_C1\left(\mathrm{Ai}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right)\right)^2+\_C2\left(\mathrm{Bi}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right)\right)^2+\_C3\,\mathrm{Ai}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right)\mathrm{Bi}\left(-\frac{2^{\frac{2}{3}}x}{2}\sqrt[3]{a}\right)\right\}$$

2.1455 ODE No. 1455

$$x(a+b-1)y'(x)-aby(x)+x^2(-y''(x))+y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.0286544 (sec), leaf count = 127

$$\left\{\left\{y(x)\to \sqrt[3]{-\frac{1}{3}}c_2 x\,{}_2F_2\left(\frac{1}{3}-\frac{a}{3},\frac{1}{3}-\frac{b}{3};\frac{2}{3},\frac{4}{3};\frac{x^3}{3}\right)+c_1\,{}_2F_2\left(-\frac{a}{3},-\frac{b}{3};\frac{1}{3},\frac{2}{3};\frac{x^3}{3}\right)+\left(-\frac{1}{3}\right)^{2/3}c_3x^2\,{}_2F_2\left(\frac{2}{3}-\frac{a}{3},\frac{2}{3}\right.\right.\right.$$

✓ **Maple** : cpu = 0.145 (sec), leaf count = 71

$$\left\{y(x)=\_C1\,{}_2\mathrm{F}_2(-\frac{a}{3},-\frac{b}{3};\,\frac{1}{3},\frac{2}{3};\,\frac{x^3}{3})+\_C2\,x{}_2\mathrm{F}_2(\frac{1}{3}-\frac{b}{3},\frac{1}{3}-\frac{a}{3};\,\frac{2}{3},\frac{4}{3};\,\frac{x^3}{3})+\_C3\,x^2{}_2\mathrm{F}_2(-\frac{a}{3}+\frac{2}{3},-\frac{b}{3}+\frac{2}{3};\,\frac{4}{3},\right.$$

2.1456 ODE No. 1456

$$x^{2c-2}y'(x)+(c-1)x^{2c-3}y(x)+y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.0356006 (sec), leaf count = 183

$$\left\{\left\{y(x)\to c_1\,{}_1F_2\left(\frac{1}{2}-\frac{1}{2c};1-\frac{1}{c},1-\frac{1}{2c};-\frac{x^{2c}}{4c^2}\right)+4^{-1/c}c_3c^{-2/c}\left(x^{2c}\right)^{\frac{1}{c}}\,{}_1F_2\left(\frac{1}{2}+\frac{1}{2c};1+\frac{1}{2c},1+\frac{1}{c};-\frac{x^{2c}}{4c^2}\right)+2^{-}\right.\right.$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 73

$$\left\{y(x)=x\left(\left(J_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right)\right)^2\_C1+J_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right)Y_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right)\_C3+\left(Y_{\frac{1}{2c}}\left(\frac{x^c}{2c}\right)\right)^2\_C2\right)\right\}$$

2.1457 ODE No. 1457

$$-3y'(x)(a+2\wp(x;\mathrm{g2},\mathrm{g3}))+by(x)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0520064 (sec), leaf count = 0 , could not solve

```
DSolve[b*y[x] - 3*(a + 2*WeierstrassP[x, {g2, g3}])*Derivative[1][y][x] + Derivative[3][y][x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+(-6\,WeierstrassP(x,g2,g3)-3\,a)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+b\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1458 ODE No. 1458

$$\frac{1}{2}y(x)\left(\left(1-n^2\right)\wp'(x;\mathrm{g2},\mathrm{g3})-a\right)+\left(1-n^2\right)y'(x)\wp(x;\mathrm{g2},\mathrm{g3})+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0198475 (sec), leaf count = 0 , could not solve

```
DSolve[((-a + (1 - n^2)*WeierstrassPPrime[x, {g2, g3}])*y[x])/2 + (1 - n^2)*WeierstrassP[x,
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+\left(-n^2\,WeierstrassP(x,g2,g3)+WeierstrassP(x,g2,g3)\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\left(-\frac{Weie\right.\right.\right.$$

2.1459 ODE No. 1459

$$-y'(x)(a+4n(n+1)\wp(x;\mathrm{g2},\mathrm{g3}))-2n(n+1)y(x)\wp'(x;\mathrm{g2},\mathrm{g3})+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.02018 (sec), leaf count = 0 , could not solve

```
DSolve[-2*n*(1 + n)*WeierstrassPPrime[x, {g2, g3}]*y[x] - (a + 4*n*(1 + n)*WeierstrassP[x, {
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=\left(DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\left(-n^2\,WeierstrassP(x,g2,g3)-n\,WeierstrassP(x,g2,g3)-\frac{a}{4}\right)\_Y(x)\right\},\{\_\right.\right.\right.$$

2.1460 ODE No. 1460

$$y'(x)(a+A\wp(x;\mathrm{g2},\mathrm{g3}))+By(x)\wp'(x;\mathrm{g2},\mathrm{g3})+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0145912 (sec), leaf count = 0 , could not solve

```
DSolve[B*WeierstrassPPrime[x, {g2, g3}]*y[x] + (a + A*WeierstrassP[x, {g2, g3}])*Derivative[
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+\left(A\,WeierstrassP(x,g2,g3)+a\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+B\,WeierstrassPPrime(x,g2,g3)\_\right.\right.\right.$$

2.1461 ODE No. 1461

$$-y'(x)\left(a+3k^2\mathrm{sn}(z|x)^2\right)+y(x)\left(b+c\mathrm{sn}(z|x)^2-3k^2\mathrm{cn}(z|x)\mathrm{dn}(z|x)\mathrm{sn}(z|x)\right)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0303813 (sec), leaf count = 0 , could not solve

```
DSolve[(b - 3*k^2*JacobiCN[z, x]*JacobiDN[z, x]*JacobiSN[z, x] + c*JacobiSN[z, x]^2)*y[x] -
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+\left(-3\,k^2(JacobiSN(z,x))^2-a\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\left(b+c(JacobiSN(z,x))^2-3\,k^2Jaco\right.\right.\right.$$

2.1462 ODE No. 1462

$$-y'(x)\left(a+6k^2\sin^2(x)\right)+by(x)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0229674 (sec), leaf count = 0 , could not solve

```
DSolve[b*y[x] - (a + 6*k^2*Sin[x]^2)*Derivative[1][y][x] + Derivative[3][y][x] == 0, y[x], x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+\left(-6\,k^2(\sin(x))^2-a\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+b\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1463 ODE No. 1463

$$y(x)f'(x)+2f(x)y'(x)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0657541 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*Derivative[1][f][x] + 2*f[x]*Derivative[1][y][x] + Derivative[3][y][x] == 0, y[x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=\left(DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\frac{f(x)\_Y(x)}{2}\right\},\{\_Y(x)\}\right)\right)^2\right\}$$

2.1464 ODE No. 1464

$$y^{(3)}(x) - 2y''(x) - 3y'(x) + 10y(x) = 0$$

✓ **Mathematica** : cpu = 0.00642556 (sec), leaf count = 34

$$\{\{y(x) \to c_3 e^{-2x} + c_1 e^{2x} \sin(x) + c_2 e^{2x} \cos(x)\}\}$$

✓ **Maple** : cpu = 0.006 (sec), leaf count = 27

$$\{y(x) = \_C1\, \mathrm{e}^{-2x} + \_C2\, \mathrm{e}^{2x} \sin(x) + \_C3\, \mathrm{e}^{2x} \cos(x)\}$$

2.1465 ODE No. 1465

$$-a^2 y'(x) + 2a^2 y(x) + y^{(3)}(x) - 2y''(x) - \sinh(x) = 0$$

✓ **Mathematica** : cpu = 0.0877506 (sec), leaf count = 95

$$\left\{\left\{y(x) \to \frac{e^{-x}\left(3a^2 e^{2x} - a^2 - 3e^{2x} - 12e^x \sinh(x) - 6e^x \cosh(x) + 1\right)}{6(a-2)(a+2)\left(a^2-1\right)} + c_1 e^{-ax} + c_3 e^{ax} + c_2 e^{2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.077 (sec), leaf count = 214

$$\left\{y(x) = \frac{1}{12\,a^5 - 60\,a^3 + 48\,a}\left(-3\,(a+1)\left((a-2)\,\mathrm{e}^{-ax} + \mathrm{e}^{ax}(a+2)\right)\cosh\left((a-1)\,x\right) + 3\left((a-2)\,\mathrm{e}^{-ax} + \mathrm{e}^{ax}(a+\right.\right.$$

2.1466 ODE No. 1466

$$a^3(-y(x)) + 3a^2 y'(x) - 3ay''(x) - e^{ax} + y^{(3)}(x) = 0$$

✓ **Mathematica** : cpu = 0.0173517 (sec), leaf count = 46

$$\left\{\left\{y(x) \to c_3 x^2 e^{ax} + c_2 x e^{ax} + c_1 e^{ax} + \frac{1}{6}x^3 e^{ax}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 27

$$\left\{y(x) = \frac{\mathrm{e}^{ax}\left(6\,\_C3\,x^2 + x^3 + 6\,\_C2\,x + 6\,\_C1\right)}{6}\right\}$$

2.1467 ODE No. 1467

$$\mathrm{a0}y(x)+\mathrm{a1}y'(x)+\mathrm{a2}y''(x)+y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.00658875 (sec), leaf count = 84

$$\left\{\left\{y(x)\to c_1e^{x\text{Root}\left[\#1^3+\#1^2\mathrm{a2}+\#1\mathrm{a1}+\mathrm{a0}\&,1\right]}+c_2e^{x\text{Root}\left[\#1^3+\#1^2\mathrm{a2}+\#1\mathrm{a1}+\mathrm{a0}\&,2\right]}+c_3e^{x\text{Root}\left[\#1^3+\#1^2\mathrm{a2}+\#1\mathrm{a1}+\mathrm{a0}\&,3\right]}\right\}\right\}$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 590

$$\left\{y(x)=\_C1\,\mathrm{e}^{-x\left(\left(\frac{i}{12}\sqrt{3}+\frac{1}{12}\right)\left(36\,a1\,a2-108\,a0-8\,a2^3+12\sqrt{12\,a0\,a2^3-3\,a1^2a2^2-54\,a1\,a2\,a0+12\,a1^3+81\,a0^2}\right)^{\frac{2}{3}}+\frac{a2}{3}\sqrt[3]{36\,a1\,a2-10}\right.}\right.$$

2.1468 ODE No. 1468

$$2\left(2a+4x^2-1\right)y'(x)-8axy(x)+y^{(3)}(x)-6xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0864793 (sec), leaf count = 57

$$\left\{\left\{y(x)\to c_2H_{\frac{a}{2}}(x)\,{}_1F_1\left(-\frac{a}{4};\frac{1}{2};x^2\right)+c_1H_{\frac{a}{2}}(x)^2+c_3\,{}_1F_1\left(-\frac{a}{4};\frac{1}{2};x^2\right)^2\right\}\right\}$$

✓ **Maple** : cpu = 0.082 (sec), leaf count = 59

$$\left\{y(x)=x^2\left(\left(U\left(\frac{1}{2}-\frac{a}{4},\frac{3}{2},x^2\right)\right)^2\_C2+U\left(\frac{1}{2}-\frac{a}{4},\frac{3}{2},x^2\right)M\left(\frac{1}{2}-\frac{a}{4},\frac{3}{2},x^2\right)\_C3+\left(M\left(\frac{1}{2}-\frac{a}{4},\frac{3}{2},x^2\right)\right)\right.\right.$$

2.1469 ODE No. 1469

$$a^3x^3y(x)+3a^2x^2y'(x)+3axy''(x)+y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.0352527 (sec), leaf count = 72

$$\left\{\left\{y(x)\to c_1e^{-\frac{ax^2}{2}}+c_2e^{-\frac{ax^2}{2}-\sqrt{3}\sqrt{a}x}+c_3e^{\sqrt{3}\sqrt{a}x-\frac{ax^2}{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 37

$$\left\{y(x)=\mathrm{e}^{-\frac{ax^2}{2}}\left(\_C1+\_C2\,\mathrm{e}^{\sqrt{3}\sqrt{a}x}+\_C3\,\mathrm{e}^{-\sqrt{3}\sqrt{a}x}\right)\right\}$$

2.1470 ODE No. 1470

$$y^{(3)}(x) - \sin(x)y''(x) - 2\cos(x)y'(x) + y(x)\sin(x) - \log(x) = 0$$

✗ **Mathematica** : cpu = 300.028 (sec), leaf count = 0 , timed out

```
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```

✓ **Maple** : cpu = 0.087 (sec), leaf count = 36

$$\left\{y(x) = \left(\_C3 + \int \left(2\_C1\, x + \_C2 + \frac{x^2 \ln(x)}{2} - \frac{3x^2}{4}\right) \mathrm{e}^{\cos(x)}\, \mathrm{d}x\right) \mathrm{e}^{-\cos(x)}\right\}$$

2.1471 ODE No. 1471

$$f(x)y''(x) + f(x)y(x) + y^{(3)}(x) + y'(x) = 0$$

✗ **Mathematica** : cpu = 0.0813647 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + Derivative[1][y][x] + f[x]*Derivative[2][y][x] + Derivative[3][y][x] == 0
```

✓ **Maple** : cpu = 0.204 (sec), leaf count = 36

$$\left\{y(x) = \mathrm{e}^{ix}\left(\int \mathrm{e}^{-2ix}\left(\int \_C3\, \mathrm{e}^{\int i - f(x)\,\mathrm{d}x}\,\mathrm{d}x + \_C2\right)\,\mathrm{d}x + \_C1\right)\right\}$$

2.1472 ODE No. 1472

$$f(x)\left(x^2y''(x) - 2xy'(x) + 2y(x)\right) + y^{(3)}(x) = 0$$

✗ **Mathematica** : cpu = 0.0785566 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*(2*y[x] - 2*x*Derivative[1][y][x] + x^2*Derivative[2][y][x]) + Derivative[3][y][
```

✓ **Maple** : cpu = 0.285 (sec), leaf count = 33

$$\left\{y(x) = \left(\int \_C1 + \_C2 \int \mathrm{e}^{-\int x^2 f(x) + 3x^{-1}\,\mathrm{d}x}\,\mathrm{d}x\,\mathrm{d}x + \_C3\right)x\right\}$$

2.1473 ODE No. 1473

$$y(x)\left(f(x)g(x)+g'(x)\right)+f(x)y''(x)+g(x)y'(x)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0135224 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*(f[x]*g[x] + Derivative[1][g][x]) + g[x]*Derivative[1][y][x] + f[x]*Derivative[2
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+f(x)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+g(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\left(f(x)\,g(x)+\frac{\mathrm{d}}{\mathrm{d}x}g(x)\right)\_Y(x)\right\},\{\_Y(x)\}\right.$$

2.1474 ODE No. 1474

$$y'(x)\left(f'(x)+2f(x)^2+4g(x)\right)+y(x)\left(4f(x)g(x)+2g'(x)\right)+3f(x)y''(x)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0159485 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*(4*f[x]*g[x] + 2*Derivative[1][g][x]) + (2*f[x]^2 + 4*g[x] + Derivative[1][f][x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=\left(DESol\left(\left\{\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+f(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+g(x)\_Y(x)\right\},\{\_Y(x)\}\right)\right)^2\right\}$$

2.1475 ODE No. 1475

$$4y^{(3)}(x)-8y''(x)-11y'(x)-3y(x)+18e^x=0$$

✓ **Mathematica** : cpu = 0.0282029 (sec), leaf count = 38

$$\left\{\left\{y(x)\to c_1e^{-x/2}+c_2e^{-x/2}x+c_3e^{3x}+e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.021 (sec), leaf count = 23

$$\left\{y(x)=(\_C3\,x+\_C2)\,\mathrm{e}^{-\frac{x}{2}}+\_C1\,\mathrm{e}^{3\,x}+\mathrm{e}^x\right\}$$

2.1476 ODE No. 1476

$$-36n^2y'(x)\wp(x;\mathrm{g2},\mathrm{g3}) - 2(n+3)(4n-3)ny(x)\phi'(x) + 27y^{(3)}(x) = 0$$

✗ **Mathematica** : cpu = 0.125944 (sec), leaf count = 0 , could not solve

```
DSolve[-2*n*(3 + n)*(-3 + 4*n)*y[x]*Derivative[1][phi][x] - 36*n^2*WeierstrassP[x, {g2, g3}]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{27\,\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x) - 36\,n^2\,WeierstrassP(x,g2,g3)\,\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x) + (-8\,WeierstrassPPrime(x,g2,g3)\right.\right.$$

2.1477 ODE No. 1477

$$xy^{(3)}(x) + 3y''(x) + xy(x) = 0$$

✓ **Mathematica** : cpu = 0.177838 (sec), leaf count = 48

$$\left\{\left\{y(x) \to \frac{c_1e^{-x}}{x} + \frac{c_2e^{\sqrt[3]{-1}x}}{x} + \frac{c_3e^{-(-1)^{2/3}x}}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 41

$$\left\{y(x) = \frac{1}{x}\left(\_C1\,\mathrm{e}^{-x} + \_C2\,\mathrm{e}^{\frac{x}{2}}\sin\left(\frac{\sqrt{3}x}{2}\right) + \_C3\,\mathrm{e}^{\frac{x}{2}}\cos\left(\frac{\sqrt{3}x}{2}\right)\right)\right\}$$

2.1478 ODE No. 1478

$$-ax^2y(x) + xy^{(3)}(x) + 3y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0340103 (sec), leaf count = 104

$$\left\{\left\{y(x) \to -\frac{2(-1)^{3/4}\sqrt{2}c_1\,{}_0F_2\left(;\frac{1}{2},\frac{3}{4};\frac{ax^4}{64}\right)}{\sqrt[4]{a}x} + c_2\,{}_0F_2\left(;\frac{3}{4},\frac{5}{4};\frac{ax^4}{64}\right) + \frac{\sqrt[4]{-1}\sqrt[4]{a}c_3x\,{}_0F_2\left(;\frac{5}{4},\frac{3}{2};\frac{ax^4}{64}\right)}{2\sqrt{2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.127 (sec), leaf count = 48

$$\left\{y(x) = \_C1\,{}_0\mathrm{F}_2(\ ;\frac{3}{4},\frac{5}{4};\ \frac{ax^4}{64}) + \frac{\_C2}{x}\,{}_0\mathrm{F}_2(\ ;\frac{1}{2},\frac{3}{4};\ \frac{ax^4}{64}) + \_C3\,x\,{}_0\mathrm{F}_2(\ ;\frac{5}{4},\frac{3}{2};\ \frac{ax^4}{64})\right\}$$

2.1479 ODE No. 1479

$$(a+b)y''(x) - ay(x) + xy^{(3)}(x) - xy'(x) = 0$$

✓ **Mathematica** : cpu = 0.149072 (sec), leaf count = 153

$$\left\{\left\{y(x) \to \frac{1}{2} i c_2 x\, {}_1F_2\left(\frac{a}{2}+\frac{1}{2}; \frac{3}{2}, \frac{a}{2}+\frac{b}{2}+\frac{1}{2}; \frac{x^2}{4}\right) + c_1\, {}_1F_2\left(\frac{a}{2}; \frac{1}{2}, \frac{a}{2}+\frac{b}{2}; \frac{x^2}{4}\right) + c_3\left(\frac{i}{2}\right)^{-a-b+2} x^{-a-b+2}\, {}_1F_2\left(1-\right.\right.\right.$$

✓ **Maple** : cpu = 0.244 (sec), leaf count = 92

$$\left\{y(x) = \_C1\ {}_1\mathrm{F}_2\left(\frac{a}{2}; \frac{1}{2}, \frac{a}{2}+\frac{b}{2}; \frac{x^2}{4}\right) + \_C2\ x\, {}_1\mathrm{F}_2\left(\frac{1}{2}+\frac{a}{2}; \frac{3}{2}, \frac{a}{2}+\frac{b}{2}+\frac{1}{2}; \frac{x^2}{4}\right) + \_C3\ x^{-a-b+2}\, {}_1\mathrm{F}_2\left(1-\frac{b}{2}; 2-\frac{a}{2}-\right.\right.$$

2.1480 ODE No. 1480

$$-(2v+x)y''(x) - (-2v+x-1)y'(x) + xy^{(3)}(x) + (x-1)y(x) = 0$$

✓ **Mathematica** : cpu = 0.220617 (sec), leaf count = 93

$$\left\{\left\{y(x) \to \frac{c_3 e^x x^{2v+2} \Gamma\left(v+\frac{3}{2}\right)\, {}_1\tilde{F}_1\left(v+\frac{3}{2}; 2v+3; -2x\right)}{\Gamma\left(\frac{1}{2}-v\right)} + c_2 2^{-2v-2} e^x G_{2,3}^{2,1}\left(2x \middle| \begin{array}{c} 1, v+\frac{3}{2} \\ 1, 2(v+1), 0 \end{array}\right) + c_1 e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.267 (sec), leaf count = 35

$$\left\{y(x) = \_C1\ \mathrm{e}^x + \_C2\ x^{v+1} I_{-v-1}(x) + \_C3\ x^{v+1} K_{v+1}(x)\right\}$$

2.1481 ODE No. 1481

$$-f(x) + \left(x^2-3\right) y''(x) + xy^{(3)}(x) + 4xy'(x) + 2y(x) = 0$$

✓ **Mathematica** : cpu = 0.997118 (sec), leaf count = 431

$$\left\{\left\{y(x) \to -\frac{1}{240} e^{-\frac{x^2}{2}} \left(-240x^5 \left(\int_1^x \left(\frac{1}{15}\sqrt{\frac{\pi}{2}} K[1] \mathrm{erfi}\left(\frac{K[1]}{\sqrt{2}}\right) f(K[1]) - \frac{1}{240}\left(15\mathrm{Ei}\left(\frac{K[1]^2}{2}\right) + 16 e^{\frac{K[1]^2}{2}}\right) f(K\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 44

$$\left\{y(x) = \left(\_C3 + \int \frac{2\_C1\ x + \_C2 - \iint -f(x)\, \mathrm{d}x\, \mathrm{d}x}{x^6} \mathrm{e}^{\frac{x^2}{2}}\, \mathrm{d}x\right) \mathrm{e}^{-\frac{x^2}{2}} x^5\right\}$$

2.1482 ODE No. 1482

$$axy(x) - b + 2xy^{(3)}(x) + 3y''(x) = 0$$

✗ **Mathematica** : cpu = 300.029 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.328 (sec), leaf count = 1616

$$\left\{y(x) = -\int 2802800\,bx\left(\left(-5/8\,{}_0\mathrm{F}_2(\ ;\ \frac{13}{6}, 7/3;\ -\frac{ax^3}{54})ax^3 + \frac{35}{4}{}_0\mathrm{F}_2(\ ;\ 7/6, 4/3;\ -\frac{ax^3}{54})\right){}_0\mathrm{F}_2(\ ;\ 5/6, 7/6;\ -\frac{ax^3}{54}\right.\right.$$

2.1483 ODE No. 1483

$$-4(\nu + x - 1)y''(x) + (6\nu + 2x - 5)y'(x) + (1 - 2\nu)y(x) + 2xy^{(3)}(x) = 0$$

✓ **Mathematica** : cpu = 0.155751 (sec), leaf count = 112

$$\left\{\left\{y(x) \to \frac{c_3 e^x x\Gamma\left(\frac{5}{2} - 3\nu\right)\left(\frac{2\,{}_1\tilde{F}_1\left(\frac{3}{2} - 3\nu; 1 - 2\nu; -x\right)}{3(2\nu - 1)x} + \frac{2}{3x\Gamma(2 - 2\nu)}\right)}{\Gamma\left(\frac{3}{2} - \nu\right)} + c_2 e^x G^{2,1}_{2,3}\left(x \,\middle|\, \begin{matrix} 1, 3\nu - \frac{1}{2} \\ 1, 2\nu, 0 \end{matrix}\right) + c_1 e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.273 (sec), leaf count = 37

$$\left\{y(x) = \_C1\,\mathrm{e}^x + \_C2\,\mathrm{e}^{\frac{x}{2}} x^\nu I_\nu\left(\frac{x}{2}\right) + \_C3\,\mathrm{e}^{\frac{x}{2}} x^\nu K_\nu\left(\frac{x}{2}\right)\right\}$$

2.1484 ODE No. 1484

$$6y'(x)(ak + bx) + 3(2ax + k)y''(x) + y(x)(3bk + 2cx) + 2xy^{(3)}(x) = 0$$

✗ **Mathematica** : cpu = 63.2972 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y, x\}, \left\{(2xc + 3bk)y(x) + (6xb + 6ak)y'(x) + (6xa + 3k)y''(x) + 2xy^{(3)}(x) = 0, y(1\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{(3\,bk + 2\,cx)\_Y(x) + (6\,ak + 6\,bx)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x) + (6\,ax + 3\,k)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x) + 2\,x\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)\right\}, \{\right.\right.$$

2.1485 ODE No. 1485

$$(x-2)xy^{(3)}(x)-(x-2)xy''(x)-2y'(x)+2y(x)=0$$

✓ **Mathematica** : cpu = 0.118571 (sec), leaf count = 66

$$\left\{\left\{y(x)\to -\frac{c_3\left(4e^x\text{Ei}(2-x)-e^2\left(x^2\log(2-x)-x^2\log(x)+2x+2\right)\right)}{4e^2}+c_1x^2+c_2e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.379 (sec), leaf count = 51

$$\left\{y(x)=\_C3\ Ei(1,x-2)\,\mathrm{e}^{x-2}+\frac{\_C3\ x^2\ln(x-2)}{4}+\_C2\,\mathrm{e}^{x}-\frac{\_C3\ \ln(x)\,x^2}{4}+\frac{(2\,x+2)\,\_C3}{4}+\_C1\ x^2\right\}$$

2.1486 ODE No. 1486

$$(2x-1)y^{(3)}(x)-8xy'(x)+8y(x)=0$$

✓ **Mathematica** : cpu = 0.169653 (sec), leaf count = 65

$$\left\{\left\{y(x)\to \frac{1}{4}c_3x\left(\frac{e^{2x-2}\text{Ei}(2-4x)}{x}-\frac{2\text{Ei}(1-2x)}{e}-\frac{e^{-2x}}{x}\right)+c_1x-c_2e^{2x}\right\}\right\}$$

✓ **Maple** : cpu = 0.25 (sec), leaf count = 51

$$\left\{y(x)=\_C1\ x+\_C2\,\mathrm{e}^{2\,x}-\frac{\_C3\ \left(2\,x\mathrm{e}^{-1}Ei(1,2\,x-1)-Ei(1,4\,x-2)\,\mathrm{e}^{2\,x-2}-\mathrm{e}^{-2\,x}\right)}{4}\right\}$$

2.1487 ODE No. 1487

$$(2x-1)y^{(3)}(x)+(x+4)y''(x)+2y'(x)=0$$

✗ **Mathematica** : cpu = 299.995 (sec), leaf count = 0 , timed out

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✓ **Maple** : cpu = 0.086 (sec), leaf count = 38

$$\left\{y(x)=1\left(\_C3+\int(2\,\_C1\ x+\_C2)\mathrm{e}^{\frac{x}{2}}(2\,x-1)^{-\frac{3}{4}}\,\mathrm{d}x\right)\mathrm{e}^{-\frac{x}{2}}\frac{1}{\sqrt[4]{2\,x-1}}\right\}$$

2.1488 ODE No. 1488

$$ax^2y(x)+x^2y^{(3)}(x)-6y'(x)=0$$

✓ **Mathematica** : cpu = 0.562456 (sec), leaf count = 102

$$\left\{\left\{y(x)\to \frac{c_1e^{-\sqrt[3]{a}x}\left(\sqrt[3]{a}x+2\right)}{x}+\frac{c_2e^{\sqrt[3]{-1}\sqrt[3]{a}x}\left(\sqrt[3]{a}x+2(-1)^{2/3}\right)}{x}+\frac{c_3e^{-(-1)^{2/3}\sqrt[3]{a}x}\left(\sqrt[3]{a}x-2\sqrt[3]{-1}\right)}{x}\right\}\right\}$$

✓ **Maple** : cpu = 0.553 (sec), leaf count = 132

$$\left\{y(x)=\frac{1}{x}\left(-\_C2\left(\left(-i-\sqrt{3}\right)\left(-a^4\right)^{\frac{2}{3}}+ia^3x\right)\mathrm{e}^{\frac{-\frac{i}{2}\left(\sqrt{3}-i\right)x}{a}\sqrt[3]{-a^4}}+\_C3\left(\left(\sqrt{3}-i\right)\left(-a^4\right)^{\frac{2}{3}}+ia^3x\right)\mathrm{e}^{\frac{\frac{i}{2}\left(\sqrt{3}+i\right)x}{a}\sqrt[3]{}}\right.\right.$$

2.1489 ODE No. 1489

$$x^2y^{(3)}(x)+(x+1)y''(x)-y(x)=0$$

✗ **Mathematica** : cpu = 0.806194 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{y^{(3)}(x)x^2-y(x)+(x+1)y''(x)=0,y(1)=c_1,y'(1)=c_2,y''(1)=c_3\right\}\right)(x)\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{-\_Y(x)+(1+x)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+x^2\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1490 ODE No. 1490

$$x^2y^{(3)}(x)+\left(x^2+1\right)y'(x)-xy''(x)=0$$

✓ **Mathematica** : cpu = 0.0190034 (sec), leaf count = 33

$$\left\{\left\{y(x)\to \frac{1}{2}c_1x^2\,{}_0\tilde{F}_1\left(;2;-\frac{x^2}{4}\right)+c_2xY_1(x)+c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.064 (sec), leaf count = 18

$$\{y(x)=\_C1+\_C2\,xJ_1(x)+\_C3\,xY_1(x)\}$$

2.1491 ODE No. 1491

$$\left(-4a^2\nu^2+4a^2x^{2a}+1\right)y'(x)+x^2y^{(3)}(x)+3xy''(x)=4a^3x^{2a-1}y(x)$$

✓ **Mathematica** : cpu = 0.0458602 (sec), leaf count = 102

$$\left\{\left\{y(x)\to c_2\left(x^{2a}\right)^{-\nu}\,{}_1F_2\left(-\nu-\frac{1}{2};1-2\nu,1-\nu;-x^{2a}\right)+c_3\left(x^{2a}\right)^{\nu}\,{}_1F_2\left(\nu-\frac{1}{2};\nu+1,2\nu+1;-x^{2a}\right)+c_1\,{}_1F_2\left(\right.\right.\right.$$

✓ **Maple** : cpu = 0.09 (sec), leaf count = 88

$$\left\{y(x)=\_C1\,{}_1\mathrm{F}_2(-\frac{1}{2};\,\nu+1,-\nu+1;\,-x^{2\,a})+\_C2\,x^{-2\,a\nu}{}_1\mathrm{F}_2(-\frac{1}{2}-\nu;\,1-2\,\nu,-\nu+1;\,-x^{2\,a})+\_C3\,x^{2\,a\nu}{}_1\mathrm{F}_2(\right.$$

2.1492 ODE No. 1492

$$\left(4x(n-m)+m(2m-1)+2x^2\right)y'(x)-2n(-2m+2x+1)y(x)-3x(x-m)y''(x)+x^2y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.414113 (sec), leaf count = 43

$$\left\{\left\{y(x)\to c_2U(-n,m,x)L_n^{m-1}(x)+c_1U(-n,m,x)^2+c_3L_n^{m-1}(x)^2\right\}\right\}$$

✓ **Maple** : cpu = 0.114 (sec), leaf count = 39

$$\left\{y(x)=\_C1\,\left(M(-n,\,m,\,x)\right)^2+\_C2\,\left(U(-n,\,m,\,x)\right)^2+\_C3\,M(-n,\,m,\,x)U(-n,\,m,\,x)\right\}$$

2.1493 ODE No. 1493

$$-f(x)+x^2y^{(3)}(x)+\left(x^2+2\right)y'(x)+4xy''(x)+3xy(x)=0$$

✓ **Mathematica** : cpu = 7.45654 (sec), leaf count = 2582

$$\left\{\left\{y(x)\to J_0(x)c_1+2Y_0(x)c_2+\frac{2c_3\,{}_1F_2\left(1;\frac{1}{2},\frac{1}{2};-\frac{x^2}{4}\right)}{x}+\frac{xJ_0(x)\int_1^x\left(\frac{-16J_1(K[1])Y_0(K[1])^2f(K[1])\,{}_1F_2(3;\frac{5}{2},\frac{5}{2};-\frac{1}{4}K[1]^2)}{\right.}\right.\right.$$

✓ **Maple** : cpu = 0.323 (sec), leaf count = 1033

$$\left\{y(x)=\frac{1}{x}\left(-\int-18\,\frac{}{\left(\left(-18\,x^2J_0\left(x\right)-72\,xJ_1\left(x\right)+54\,J_0\left(x\right)\right){}_1\mathrm{F}_2(1;\,1/2,1/2;\,-1/4\,x^2)+8\,\left(9/4\,J_0\left(x\right)\left(x^2+9\right)\right.\right.\right.\right.\right.$$

2.1494 ODE No. 1494

$$x^2 y^{(3)}(x) + 5xy''(x) + 4y'(x) - \log(x) = 0$$

✓ **Mathematica** : cpu = 0.0289878 (sec), leaf count = 43

$$\left\{\left\{y(x) \to -\frac{c_1}{x} - \frac{2c_2}{x} - \frac{2c_2 \log(x)}{x} + c_3 - \frac{x}{2} + \frac{1}{4}x\log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.022 (sec), leaf count = 32

$$\left\{y(x) = \frac{\left(x^2 + 4\_C2\right)\ln(x) - 2x^2 + 4\_C1\,x + 4\_C3}{4x}\right\}$$

2.1495 ODE No. 1495

$$x^2 y^{(3)}(x) + 6xy''(x) + 6y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0186556 (sec), leaf count = 24

$$\left\{\left\{y(x) \to -\frac{c_2}{2x^2} - \frac{c_1}{x} + c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 16

$$\left\{y(x) = \_C1 + \frac{\_C2}{x^2} + \frac{\_C3}{x}\right\}$$

2.1496 ODE No. 1496

$$ax^2 y(x) + x^2 y^{(3)}(x) + 6xy''(x) + 6y'(x) = 0$$

✓ **Mathematica** : cpu = 0.274145 (sec), leaf count = 63

$$\left\{\left\{y(x) \to \frac{c_1 e^{-\sqrt[3]{a}x}}{x^2} + \frac{c_2 e^{\sqrt[3]{-1}\sqrt[3]{a}x}}{x^2} + \frac{c_3 e^{-(-1)^{2/3}\sqrt[3]{a}x}}{x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.028 (sec), leaf count = 57

$$\left\{y(x) = \frac{1}{x^2}\left(\_C1\,\mathrm{e}^{\frac{\left(i\sqrt{3}-1\right)x}{2}\sqrt[3]{-a}} + \_C2\,\mathrm{e}^{-\frac{\left(i\sqrt{3}+1\right)x}{2}\sqrt[3]{-a}} + \_C3\,\mathrm{e}^{\sqrt[3]{-a}x}\right)\right\}$$

2.1497 ODE No. 1497

$$-3x(p+q)y''(x)+3p(3q+1)y'(x)+x^2y^{(3)}(x)+x^2(-y(x))=0$$

✓ **Mathematica** : cpu = 0.489725 (sec), leaf count = 135

$$\left\{\left\{y(x)\to c_1\,{}_0F_2\left(;\frac{2}{3}-p,\frac{1}{3}-q;\frac{x^3}{27}\right)+c_2(-1)^{\frac{1}{3}(3p+1)}3^{-3p-1}x^{3p+1}\,{}_0F_2\left(;p+\frac{4}{3},p-q+\frac{2}{3};\frac{x^3}{27}\right)+c_3(-1)^{\frac{1}{3}(3q+2)}\right.\right.$$

✓ **Maple** : cpu = 0.277 (sec), leaf count = 77

$$\left\{y(x)=\_C1\,{}_0\mathrm{F}_2(\ ;-p+\frac{2}{3},-q+\frac{1}{3};\ \frac{x^3}{27})+\_C2\,x^{1+3p}{}_0\mathrm{F}_2(\ ;p+\frac{4}{3},\frac{2}{3}-q+p;\ \frac{x^3}{27})+\_C3\,x^{2+3q}{}_0\mathrm{F}_2(\ ;q+\frac{5}{3},\right.$$

2.1498 ODE No. 1498

$$\left(ax^2+6n\right)y'(x)-2axy(x)-2(n+1)xy''(x)+x^2y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 8.46035 (sec), leaf count = 584

$$\left\{\left\{y(x)\to -\frac{\pi c_3 2^{-n-\frac{3}{2}}x\left(\sqrt{a}x\right)^{-n-\frac{1}{2}}\left(-a^{3/2}2^{2n}x^3\sec(\pi n)\Gamma\left(\frac{3}{2}-n\right)\Gamma\left(n+\frac{3}{2}\right)J_{\frac{1}{2}(2n+1)}\left(\sqrt{a}x\right)\ {}_1\tilde{F}_2\left(\frac{3}{2}-n;\frac{1}{2}-n,\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.267 (sec), leaf count = 53

$$\left\{y(x)=\_C1\,x^{n+\frac{1}{2}}J_{-n-\frac{1}{2}}\left(\sqrt{a}x\right)+\_C2\,x^{n+\frac{1}{2}}Y_{-n-\frac{1}{2}}\left(\sqrt{a}x\right)+\_C3\,\left(ax^2+4\,n-2\right)\right\}$$

2.1499 ODE No. 1499

$$-\left(\nu^2+x^2-\frac{1}{4}\right)y'(x)+\left(\nu^2+x^2-2x-\frac{1}{4}\right)y(x)+x^2y^{(3)}(x)-\left(x^2-2x\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.238095 (sec), leaf count = 97

$$\left\{\left\{y(x)\to \frac{c_3e^xx^{\nu+\frac{1}{2}}\Gamma\left(\nu+\frac{1}{2}\right)\ {}_1\tilde{F}_1\left(\nu+\frac{1}{2};2\nu+1;-2x\right)}{\Gamma\left(\frac{3}{2}-\nu\right)}+c_2 2^{-\nu-\frac{1}{2}}e^xG^{2,1}_{2,3}\left(2x\left|\begin{array}{c}1,0\\ \frac{1}{2}-\nu,\nu+\frac{1}{2},0\end{array}\right.\right)+c_1e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.277 (sec), leaf count = 25

$$\left\{y(x)=\_C1\,\mathrm{e}^x+\_C2\,\sqrt{x}I_\nu(x)+\_C3\,\sqrt{x}K_\nu(x)\right\}$$

2.1500 ODE No. 1500

$$\nu(2x+1)y'(x)-\nu(x+1)y(x)-x(v+x)y''(x)+x^2y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 47.5441 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{y^{(3)}(x)x^2-(x+v)y''(x)x-(x+1)\nu y(x)+(2x\nu+\nu)y'(x)=0,y(1)=c_1,\right.\right.\right.$$

✓ **Maple** : cpu = 0.227 (sec), leaf count = 55

$$\left\{y(x)=\_C1\,\mathrm{e}^{x}+\_C2\,x^{\frac{\nu}{2}+\frac{1}{2}}J_{-\nu-1}\left(2\sqrt{\nu}\sqrt{x}\right)+\_C3\,x^{\frac{\nu}{2}+\frac{1}{2}}Y_{-\nu-1}\left(2\sqrt{\nu}\sqrt{x}\right)\right\}$$

2.1501 ODE No. 1501

$$\left(-\nu^2+x^2-2x+\frac{1}{4}\right)y'(x)+\left(\nu^2-\frac{1}{4}\right)y(x)+x^2y^{(3)}(x)-2\left(x^2-x\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.203404 (sec), leaf count = 86

$$\left\{\left\{y(x)\to \frac{c_3e^xx^{\nu+\frac{1}{2}}\Gamma\left(\nu+\frac{1}{2}\right)\,{}_1\tilde{F}_1\left(\nu+\frac{1}{2};2\nu+1;-x\right)}{\Gamma\left(\frac{3}{2}-\nu\right)}+c_2e^xG^{2,1}_{2,3}\left(x\left|\begin{array}{c}1,0\\ \frac{1}{2}-\nu,\nu+\frac{1}{2},0\end{array}\right.\right)+c_1e^x\right\}\right\}$$

✓ **Maple** : cpu = 0.246 (sec), leaf count = 37

$$\left\{y(x)=\_C1\,\mathrm{e}^{x}+\_C2\,\mathrm{e}^{\frac{x}{2}}\sqrt{x}I_{\nu}\left(\frac{x}{2}\right)+\_C3\,\mathrm{e}^{\frac{x}{2}}\sqrt{x}K_{\nu}\left(\frac{x}{2}\right)\right\}$$

2.1502 ODE No. 1502

$$-\left(x^4-6x\right)y''(x)-\left(2x^3-6\right)y'(x)+x^2y^{(3)}(x)+2x^2y(x)=0$$

✓ **Mathematica** : cpu = 0.0602725 (sec), leaf count = 98

$$\left\{\left\{y(x)\to \frac{c_2\Gamma\left(\frac{1}{3}\right)\,{}_2F_2\left(-\frac{2}{3},\frac{1}{3};\frac{2}{3},\frac{4}{3};\frac{x^3}{3}\right)}{3x\Gamma\left(\frac{4}{3}\right)}+\frac{\sqrt[3]{-\frac{1}{3}}c_3\Gamma\left(\frac{2}{3}\right)\,{}_2F_2\left(-\frac{1}{3},\frac{2}{3};\frac{4}{3},\frac{5}{3};\frac{x^3}{3}\right)}{3\Gamma\left(\frac{5}{3}\right)}+\frac{c_1}{x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.49 (sec), leaf count = 103

$$\left\{y(x)=\frac{1}{x^2}\left(\_C3\int \mathrm{e}^{\frac{x^3}{6}}\sqrt{x}\left(K_{\frac{5}{6}}\left(-\frac{x^3}{6}\right)x^3-K_{\frac{1}{6}}\left(-\frac{x^3}{6}\right)x^3+2\,K_{1/6}(-1/6\,x^3)\right)\,\mathrm{d}x+\_C2\int \mathrm{e}^{\frac{x^3}{6}}\sqrt{x}\left(I_{\frac{1}{6}}\left(-\frac{x^3}{6}\right.\right.\right.\right.$$

2.1503 ODE No. 1503

$$\left(x^2+1\right) y^{(3)}(x)+\frac{1}{x^2}+8xy''(x)+10y'(x)-2\log(x)-3=0$$

✓ **Mathematica** : cpu = 0.120344 (sec), leaf count = 62

$$\left\{\left\{y(x)\to c_3-\frac{100(3c_2-1)\,x^3+900c_2x+225c_1+36x^5-60\left(3x^4+10x^2+15\right)x\log(x)}{900\left(x^2+1\right)^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 67

$$\left\{y(x)=\frac{\left(45\,x^5+150\,x^3+225\,x\right)\ln\left(x\right)-9\,x^5+225\,\_C1\,x^4+\left(225\,\_C2-50\right)x^3+450\,\_C1\,x^2+(675\,\_C2-\right.}{225\,\left(x^2+1\right)^2}$$

2.1504 ODE No. 1504

$$\left(x^2+2\right) y^{(3)}(x)+\left(x^2+2\right) y'(x)-2xy''(x)-2xy(x)=0$$

✓ **Mathematica** : cpu = 0.114022 (sec), leaf count = 43

$$\left\{\left\{y(x)\to\frac{c_1x^2}{2}+\frac{1}{2}ic_2e^{-ix}-\frac{1}{4}c_3e^{ix}\right\}\right\}$$

✓ **Maple** : cpu = 0.216 (sec), leaf count = 18

$$\left\{y(x)=\_C1\,x^2+\_C2\,\cos\left(x\right)+\_C3\,\sin\left(x\right)\right\}$$

2.1505 ODE No. 1505

$$(2ax+b)y'(x)+ay(x)+2(x-1)xy^{(3)}(x)+3(2x-1)y''(x)=0$$

✗ **Mathematica** : cpu = 62.1685 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to\text{DifferentialRoot}\left(\{y,x\},\left\{ay(x)+(2xa+b)y'(x)+(6x-3)y''(x)+2(x-1)xy^{(3)}(x)=0,y(2)=c_1,y\right.\right.\right.$$

✓ **Maple** : cpu = 0.157 (sec), leaf count = 79

$$\left\{y(x)=\_C1\left(MathieuC\left(-\frac{a}{2}-\frac{b}{2}+1,\frac{a}{4},\arccos\left(\sqrt{x}\right)\right)\right)^2+\_C2\left(MathieuS\left(-\frac{a}{2}-\frac{b}{2}+1,\frac{a}{4},\arccos\left(\sqrt{x}\right)\right)\right.\right.$$

2.1506 ODE No. 1506

$$4x^2y^{(3)}(x)+\left(x^2+14x-1\right)y''(x)+4(x+1)y'(x)+2y(x)=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.06 (sec), leaf count = 43

$$\left\{y(x)=\left(\_C3+\int\frac{2\_C1\,x+\_C2}{4}\mathrm{e}^{\frac{x}{4}}\mathrm{e}^{\frac{1}{4x}}x^{-\frac{5}{2}}\,\mathrm{d}x\right)\mathrm{e}^{-\frac{x}{4}}\sqrt{x}\mathrm{e}^{-\frac{1}{4x}}\right\}$$

2.1507 ODE No. 1507

$$xy^{(3)}(x)(ax+b)+(\alpha x+\beta)y''(x)-f(x)+xy'(x)+y(x)=0$$

✗ **Mathematica** : cpu = 2.48951 (sec), leaf count = 0 , could not solve

```
DSolve[-f[x] + y[x] + x*Derivative[1][y][x] + (beta + alpha*x)*Derivative[2][y][x] + x*(b +
```

✓ **Maple** : cpu = 0.651 (sec), leaf count = 1210

$$\left\{y(x)=(ax+b)^{\frac{(2b+\beta)a-\alpha b}{ab}}\left(HeunC\left(0,\frac{2b-\beta}{b},\frac{(2b+\beta)a-\alpha b}{ab},-\frac{b}{a^2},\frac{(4a-\alpha)b^2-\alpha\beta b+a\beta^2}{2ab^2},-\frac{ax}{b}\right)\left(\int-\right.\right.\right.$$

2.1508 ODE No. 1508

$$y(x)\left(ax^3+\nu^2-1\right)+\left(1-\nu^2\right)xy'(x)+x^3y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.841726 (sec), leaf count = 143

$$\left\{\left\{y(x)\to c_2 3^{\nu-1}a^{\frac{1-\nu}{3}}x^{1-\nu}\,{}_0F_2\left(;1-\frac{2\nu}{3},1-\frac{\nu}{3};-\frac{ax^3}{27}\right)+c_3 3^{-\nu-1}a^{\frac{\nu+1}{3}}x^{\nu+1}\,{}_0F_2\left(;\frac{\nu}{3}+1,\frac{2\nu}{3}+1;-\frac{ax^3}{27}\right)+\frac{1}{3}\sqrt[3]{}\right.\right.$$

✓ **Maple** : cpu = 0.153 (sec), leaf count = 81

$$\left\{y(x)=\_C1\,x\,{}_0\mathrm{F}_2(\ ;-\frac{\nu}{3}+1,\frac{\nu}{3}+1;-\frac{ax^3}{27})+\_C2\,x^{-\nu+1}\,{}_0\mathrm{F}_2(\ ;1-\frac{2\nu}{3},-\frac{\nu}{3}+1;-\frac{ax^3}{27})+\_C3\,x^{\nu+1}\,{}_0\mathrm{F}_2(\ ;\frac{2}{3}\right.\right.$$

2.1509 ODE No. 1509

$$\left(\left(1-4\nu^2\right)x+4x^3\right)y'(x)+\left(4\nu^2-1\right)y(x)+x^3y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.0105946 (sec), leaf count = 34

$$\left\{\left\{y(x)\to c_1xJ_\nu(x)^2+c_3xY_\nu(x)^2+c_2xJ_\nu(x)Y_\nu(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.057 (sec), leaf count = 29

$$\left\{y(x)=x\left(\left(J_\nu(x)\right)^2\_C1+J_\nu(x)Y_\nu(x)\_C3+\left(Y_\nu(x)\right)^2\_C2\right)\right\}$$

2.1510 ODE No. 1510

$$y(x)\left(a(\nu-1)x^{2\nu}+bx^{3\nu}+\nu^2-1\right)+x\left(ax^{2\nu}-\nu^2+1\right)y'(x)+x^3y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0862793 (sec), leaf count = 0 , could not solve

```
DSolve[(-1 + nu^2 + a*(-1 + nu)*x^(2*nu) + b*x^(3*nu))*y[x] + x*(1 - nu^2 + a*x^(2*nu))*Deri
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{x^3\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+\left(x^{2\,\nu}ax-\nu^2x+x\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\left(x^{2\,\nu}a\nu-ax^{2\,\nu}+bx^{3\,\nu}+\nu^2-1\right)\_Y(x)\right\},\{\right.$$

2.1511 ODE No. 1511

$$x^3y^{(3)}(x)+(x+8)x^3-6(x-1)x^3\log(x)+3x^2y''(x)-2xy'(x)+2y(x)=0$$

✓ **Mathematica** : cpu = 0.0383809 (sec), leaf count = 51

$$\left\{\left\{y(x)\to\frac{c_1}{x^2}+c_2x+c_3x\log(x)+\frac{1}{450}\left(-50x^4+50x^4\log(x)-18x^3-135x^3\log(x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 49

$$\left\{y(x)=\frac{\left(50\,x^6-135\,x^5+450\,\_C3\,x^3\right)\ln(x)-50\,x^6-18\,x^5+450\,\_C1\,x^3+450\,\_C2}{450\,x^2}\right\}$$

2.1512 ODE No. 1512

$$\left(1-a^2\right) xy'(x)+x^3y^{(3)}(x)+3x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0389815 (sec), leaf count = 29

$$\left\{\left\{y(x)\to -\frac{c_1x^{-a}}{a}+\frac{c_2x^a}{a}+c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 18

$$\left\{y(x)=\_C1+\_C2\,x^{-a}+\_C3\,x^a\right\}$$

2.1513 ODE No. 1513

$$x^3y^{(3)}(x)-4x^2y''(x)+\left(x^2+8\right)xy'(x)-2\left(x^2+4\right)y(x)=0$$

✓ **Mathematica** : cpu = 0.0803549 (sec), leaf count = 25

$$\left\{\left\{y(x)\to c_1x^2-c_2x\sin(x)+c_3x\cos(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.226 (sec), leaf count = 18

$$\{y(x)=x(\cos(x)\,\_C3+\sin(x)\,\_C2+\_C1\,x)\}$$

2.1514 ODE No. 1514

$$\left(ax^3-12\right)y(x)+x^3y^{(3)}(x)+6x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.742234 (sec), leaf count = 102

$$\left\{\left\{y(x)\to \frac{c_1e^{-\sqrt[3]{a}x}\left(\sqrt[3]{a}x+2\right)}{x^3}+\frac{c_2e^{\sqrt[3]{-1}\sqrt[3]{a}x}\left(\sqrt[3]{a}x+2(-1)^{2/3}\right)}{x^3}+\frac{c_3e^{-(-1)^{2/3}\sqrt[3]{a}x}\left(\sqrt[3]{a}x-2\sqrt[3]{-1}\right)}{x^3}\right\}\right\}$$

✓ **Maple** : cpu = 0.546 (sec), leaf count = 132

$$\left\{y(x)=\frac{1}{x^3}\left(-\_C2\left(\left(-i-\sqrt{3}\right)\left(-a^4\right)^{\frac{2}{3}}+ia^3x\right)\mathrm{e}^{\frac{-\frac{i}{2}\left(\sqrt{3}-i\right)x}{a}\sqrt[3]{-a^4}}+\_C3\left(\left(\sqrt{3}-i\right)\left(-a^4\right)^{\frac{2}{3}}+ia^3x\right)\mathrm{e}^{\frac{\frac{i}{2}\left(\sqrt{3}+i\right)x}{a}}\right.\right.$$

2.1515 ODE No. 1515

$$y(x)\left(a\left(4c^2\nu^2-a^2\right)+4b^2c^2(c-a)x^{2c}\right)+y'(x)\left(3(a-1)ax+4b^2c^2x^{2c+1}-4c^2\nu^2+1\right)+3(1-a)x^2y''(x)+x^3y^{(3)}(x)$$

✗ **Mathematica** : cpu = 0.215204 (sec), leaf count = 0 , could not solve

```
DSolve[(a*(-a^2 + 4*c^2*nu^2) + 4*b^2*c^2*(-a + c)*x^(2*c))*y[x] + (1 - 4*c^2*nu^2 + 3*(-
1 + a)*a*x + 4*b^2*c^2*x^(1 + 2*c))*Derivative[1][y][x] + 3*(1 - a)*x^2*Derivative[2][y][x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.1516 ODE No. 1516

$$x^3y^{(3)}(x)+(x+3)x^2y''(x)+5(x-6)xy'(x)+(4x+30)y(x)=0$$

✗ **Mathematica** : cpu = 301.564 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.477 (sec), leaf count = 188

$$\left\{y(x)=\frac{\_C3\,\mathrm{e}^{-x}\left(x^8+28\,x^7+450\,x^6+5100\,x^5+42900\,x^4+267120\,x^3+1179360\,x^2+3326400\,x+4536000\right)}{\right.$$

2.1517 ODE No. 1517

$$x^3y^{(3)}(x)-2x^3+x^2y''(x)+2xy'(x)-y(x)+\log(x)=0$$

✓ **Mathematica** : cpu = 0.403684 (sec), leaf count = 30686

Too large to display

✓ **Maple** : cpu = 0.519 (sec), leaf count = 866

$$\left\{y(x)=-\int-\frac{\left(x\frac{\left(11-3\sqrt{69}\right)\left(44+12\sqrt{69}\right)^{\frac{2}{3}}}{1200}+\frac{\sqrt[3]{44+12\sqrt{69}}}{12}+\frac{2}{3}\right)^2\sqrt[3]{44+12\sqrt{69}}\left(3\sqrt{69}\sqrt[3]{44+12\sqrt{69}}-11\sqrt[3]{44+12\sqrt{69}}\right.}{13800\,x^3}\right.$$

2.1518 ODE No. 1518

$$x\left(x^2+1\right)y^{(3)}(x)+3\left(2x^2+1\right)y''(x)-12y(x)=0$$

✓ **Mathematica** : cpu = 0.244444 (sec), leaf count = 106

$$\left\{\left\{y(x)\to \frac{1}{3}c_1\left(2x^2+1\right)+\frac{1}{3}c_2x\sqrt{x^2+1}+\frac{c_3\left(2x^2+1\right)\left(3x^2+3\sqrt{x^2+1}x^2\log(x)-3\sqrt{x^2+1}x^2\log\left(\sqrt{x^2+1}+\right.\right.\right.\right.}{6\left(2x^3+x\right)}$$

✓ **Maple** : cpu = 0.474 (sec), leaf count = 60

$$\left\{y(x)=\frac{1}{x}\left(3\,Artanh\left(\frac{1}{\sqrt{x^2+1}}\right)\sqrt{x^2+1}\_C2\,x^2+\_C1\,x^2\sqrt{x^2+1}+2\_C3\,x^3-3\_C2\,x^2+\_C3\,x-\_C2\right)\right.$$

2.1519 ODE No. 1519

$$(x+3)x^2y^{(3)}(x)-3(x+2)xy''(x)+6(x+1)y'(x)-6y(x)=0$$

✓ **Mathematica** : cpu = 0.0309243 (sec), leaf count = 65

$$\left\{\left\{y(x)\to \frac{1}{4}c_1\left(x^3-3x^2+3x+3\right)+\frac{1}{2}c_2\left(-x^3+3x^2-x-1\right)+\frac{1}{8}c_3\left(3x^3-5x^2+x+1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 19

$$\left\{y(x)=\_C2\,x^3+\_C1\,x^2+\_C3\,x+\_C3\right\}$$

2.1520 ODE No. 1520

$$y''(x)\left(-6x(\mathrm{a1}+\mathrm{a2}+\mathrm{a3})+3\mathrm{a1a2}+3\mathrm{a1a3}+3\mathrm{a2a3}+9x^2\right)+2(x-\mathrm{a1})(x-\mathrm{a2})(x-\mathrm{a3})y^{(3)}(x)-2\left(b+\left(n^2+n-3\right)\right.$$

✗ **Mathematica** : cpu = 73.0389 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{-n(n+1)y(x)-2\left(xn^2+xn-3x+b\right)y'(x)+3\left(3x^2-2\mathrm{a1}x-2\mathrm{a2}x-2\mathrm{a3}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.596 (sec), leaf count = 288

$$\left\{y(x)=-\_C2\,(x-a1)\left(HeunG\left(\frac{-a3+a1}{-a2+a1},\frac{\left(-n^2-n+3\right)a1-b}{-4\,a2+4\,a1},\frac{n}{2}+1,-\frac{n}{2}+\frac{1}{2},\frac{3}{2},\frac{1}{2},\frac{-x+a1}{-a2+a1}\right)\right)^2+\_\right.$$

2.1521 ODE No. 1521

$$(x+1)x^3y^{(3)}(x)-(4x+2)x^2y''(x)+(10x+4)xy'(x)-4(3x+1)y(x)=0$$

✓ **Mathematica** : cpu = 0.0686794 (sec), leaf count = 35

$$\left\{\left\{y(x)\to c_1x^2+c_3x^2\left(x+\frac{1}{x}+\log^2(x)\right)+c_2x^2\log(x)\right\}\right\}$$

✓ **Maple** : cpu = 0.454 (sec), leaf count = 28

$$\left\{y(x)=x\left(\left(\ln(x)\right)^2\_C3\,x+\_C2\,x\ln(x)+\_C3\,x^2+\_C1\,x+\_C3\right)\right\}$$

2.1522 ODE No. 1522

$$4x^4y^{(3)}(x)-4x^3y''(x)+4x^2y'(x)-1=0$$

✓ **Mathematica** : cpu = 0.0206776 (sec), leaf count = 44

$$\left\{\left\{y(x)\to\frac{c_1x^2}{2}-\frac{c_2x^2}{4}+\frac{1}{2}c_2x^2\log(x)+c_3-\frac{1}{36x}\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 34

$$\left\{y(x)=\frac{18\,x^3\_C1\,\ln(x)-1+(-9\,\_C1+18\,\_C2)\,x^3+36\,\_C3\,x}{36\,x}\right\}$$

2.1523 ODE No. 1523

$$-\left(4x^2+2\right)x^2y''(x)+\left(10x^2+4\right)xy'(x)-4\left(3x^2+1\right)y(x)+\left(x^2+1\right)x^3y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.123681 (sec), leaf count = 74

$$\left\{\left\{y(x)\to c_1\left(-x^3+3x^2-x\right)+\frac{1}{2}c_2\left(x^3-2x^2+x\right)-\frac{c_3x\left(-x^3+3x^2-x\right)\left(\log(x)+1\right)}{2\left(x^2-3x+1\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.469 (sec), leaf count = 23

$$\left\{y(x)=\left(\ln(x)\,\_C2\,x+\_C3\,x^2+(\_C1+\_C2)\,x+\_C3\right)x\right\}$$

2.1524 ODE No. 1524

$$x^6 y^{(3)}(x) + x^2 y''(x) - 2y(x) = 0$$

✓ **Mathematica** : cpu = 0.154576 (sec), leaf count = 96

$$\left\{\left\{y(x) \to -\frac{\left(-\frac{1}{3}\right)^{2/3} c_2 x \Gamma\left(\frac{1}{3}\right)\ {}_2F_2\left(-\frac{2}{3}, \frac{1}{3}; \frac{2}{3}, \frac{4}{3}; \frac{1}{3x^3}\right)}{3\Gamma\left(\frac{4}{3}\right)} + \frac{c_3 \Gamma\left(\frac{2}{3}\right)\ {}_2F_2\left(-\frac{1}{3}, \frac{2}{3}; \frac{4}{3}, \frac{5}{3}; \frac{1}{3x^3}\right)}{9\Gamma\left(\frac{5}{3}\right)} + c_1 x^2\right\}\right\}$$

✓ **Maple** : cpu = 0.536 (sec), leaf count = 98

$$\left\{y(x) = x^2\left(\int 1 e^{\frac{1}{6x^3}}\left(2x^3 I_{1/6}(-1/6\,x^{-3}) - I_{\frac{1}{6}}\left(-\frac{1}{6x^3}\right) - I_{-\frac{5}{6}}\left(-\frac{1}{6x^3}\right)\right) x^{-\frac{11}{2}}\, dx\_C3 + \int 1 e^{\frac{1}{6x^3}}\left(2x^3 K_{1/6}(-\right.\right.$$

2.1525 ODE No. 1525

$$a y(x) + x^6 y^{(3)}(x) + 6x^5 y''(x) = 0$$

✓ **Mathematica** : cpu = 0.448263 (sec), leaf count = 102

$$\left\{\left\{y(x) \to c_1 e^{\frac{\sqrt[3]{a}}{x}}\left(2x - \sqrt[3]{a}\right) + c_2 e^{\frac{(-1)^{2/3}\sqrt[3]{a}}{x}}\left(x - \frac{1}{2}(-1)^{2/3}\sqrt[3]{a}\right) + c_3 e^{-\frac{\sqrt[3]{-1}\sqrt[3]{a}}{x}}\left(\frac{1}{2}\sqrt[3]{-1}\sqrt[3]{a} + x\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.502 (sec), leaf count = 133

$$\left\{y(x) = 4\_C3\left(\left(-i/4 + 1/4\sqrt{3}\right)\sqrt[3]{-a^4} + ixa\right) e^{\frac{i/2\sqrt[3]{-a^4}\left(\sqrt{3}-i\right)}{ax}} - 4\_C2\left(\left(-i/4 - 1/4\sqrt{3}\right)\sqrt[3]{-a^4} + ixa\right) e^{\frac{-i/2}{}}\right.$$

2.1526 ODE No. 1526

$$\left(x^4 + 2x^2 + 2x + 1\right) x^2 y^{(3)}(x) - \left(2x^6 + 3x^4 - 6x^2 - 6x - 1\right) y''(x) + \left(x^6 - 6x^3 - 15x^2 - 12x - 2\right) y'(x) + \left(x^4 + 4x^3\right.$$

✗ **Mathematica** : cpu = 300.064 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.238 (sec), leaf count = 19

$$\left\{y(x) = \_C2\, e^{x^{-1}} + e^x(\_C3\, x + \_C1)\right\}$$

2.1527 ODE No. 1527

$$(x-a)^3(x-b)^3y^{(3)}(x)-cy(x)=0$$

✗ **Mathematica** : cpu = 135.376 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{(a-x)^3(b-x)^3y^{(3)}(x)-cy(x)=0,y(0)=c_1,y'(0)=c_2,y''(0)=c_3\right\}\right)(x)\right.$$

✓ **Maple** : cpu = 0.598 (sec), leaf count = 437

$$\left\{y(x)=(x-b)^{2\,\frac{a}{a-b}}(x-a)^{-2\,\frac{b}{a-b}}\left((b-x)^{-\frac{RootOf\left(\_Z^3+(-3a-3b)\_Z^2+\left(2a^2+8ab+2b^2\right)\_Z-4ba^2-4ab^2-c,index=3\right)}{a-b}}(a-x)^{\frac{RootO}{}}\right.\right.$$

2.1528 ODE No. 1528

$$y^{(3)}(x)\sin(x)+(2\cos(x)+1)y''(x)-\sin(x)y'(x)-\cos(x)=0$$

✓ **Mathematica** : cpu = 0.625234 (sec), leaf count = 72

$$\left\{\left\{y(x)\to\frac{\sin\left(\frac{x}{2}\right)\left(\sqrt{2}\left(c_2x\sin\left(\frac{x}{2}\right)+\cos\left(\frac{x}{2}\right)\left(c_2\log(2(\cos(x)+1))+2c_1\right)\right)-2\cos\left(\frac{x}{2}\right)\sin^{-1}(\cos(x))\right)}{\cos(x)-1}+c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.199 (sec), leaf count = 71

$$\left\{y(x)=\frac{1}{(\cos(x)-1)\sin(x)}\left(\ln\left(\frac{1-\cos(x)}{\sin(x)}\right)(\sin(x))^2\_C1-\ln(\sin(x))(\sin(x))^2\_C1+(\sin(x))^2\_C3+(\right.\right.$$

2.1529 ODE No. 1529

$$y^{(3)}(x)(x+\sin(x))+3(\cos(x)+1)y''(x)-3\sin(x)y'(x)-y(x)\cos(x)+\sin(x)=0$$

✗ **Mathematica** : cpu = 0.0780807 (sec), leaf count = 0 , could not solve

```
DSolve[Sin[x] - Cos[x]*y[x] - 3*Sin[x]*Derivative[1][y][x] + 3*(1 + Cos[x])*Derivative[2][y]
```

✓ **Maple** : cpu = 0.087 (sec), leaf count = 25

$$\left\{y(x)=\frac{\_C3+\_C1\,x^2+\_C2\,x-\cos(x)}{\sin(x)+x}\right\}$$

2.1530 ODE No. 1530

$$y'(x)\left(4\nu(\nu+1)\sin^2(x)+\cos(2x)\right)+2\nu(\nu+1)y(x)\sin(2x)+y^{(3)}(x)\sin^2(x)+3\sin(x)\cos(x)y''(x)=0$$

✗ **Mathematica** : cpu = 0.172382 (sec), leaf count = 0 , could not solve

```
DSolve[2*nu*(1 + nu)*Sin[2*x]*y[x] + (Cos[2*x] + 4*nu*(1 + nu)*Sin[x]^2)*Derivative[1][y][x]
```

✓ **Maple** : cpu = 0.252 (sec), leaf count = 113

$$\left\{y(x)=\_C1\left({}_2\mathrm{F}_1(-\frac{\nu}{2},\frac{\nu}{2}+\frac{1}{2};\frac{1}{2};\frac{\cos(2x)}{2}+\frac{1}{2})\right)^2+\_C2\left(\cos(2x)+1\right)\left({}_2\mathrm{F}_1(1+\frac{\nu}{2},\frac{1}{2}-\frac{\nu}{2};\frac{3}{2};\frac{\cos(2x)}{2}+\frac{1}{2}\right.\right.$$

2.1531 ODE No. 1531

$$A(x)\left(f(x)y''(x)+g(x)y'(x)+h(x)y(x)\right)+f'(x)y''(x)+f(x)y^{(3)}(x)+g'(x)y'(x)+g(x)y''(x)+y(x)h'(x)+h(x)y'(x)$$

✗ **Mathematica** : cpu = 0.032515 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*Derivative[1][h][x] + h[x]*Derivative[1][y][x] + Derivative[1][g][x]*Derivative[
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{f(x)\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)+\left(\frac{\mathrm{d}}{\mathrm{d}x}f(x)+g(x)+A(x)\,f(x)\right)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\left(\frac{\mathrm{d}}{\mathrm{d}x}g(x)+h(x)+A(x)\,g(x)\right.\right.\right.$$

2.1532 ODE No. 1532

$$ny(x)+y^{(3)}(x)+xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0179158 (sec), leaf count = 103

$$\left\{\left\{y(x)\to\frac{c_2x\,{}_1F_2\left(\frac{n}{3}+\frac{1}{3};\frac{2}{3},\frac{4}{3};-\frac{x^3}{9}\right)}{3^{2/3}}+c_1\,{}_1F_2\left(\frac{n}{3};\frac{1}{3},\frac{2}{3};-\frac{x^3}{9}\right)+\frac{c_3x^2\,{}_1F_2\left(\frac{n}{3}+\frac{2}{3};\frac{4}{3},\frac{5}{3};-\frac{x^3}{9}\right)}{3\sqrt[3]{3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.102 (sec), leaf count = 58

$$\left\{y(x)=\_C1\,{}_1\mathrm{F}_2(\frac{n}{3};\frac{1}{3},\frac{2}{3};-\frac{x^3}{9})+\_C2\,x\,{}_1\mathrm{F}_2(\frac{1}{3}+\frac{n}{3};\frac{2}{3},\frac{4}{3};-\frac{x^3}{9})+\_C3\,x^2\,{}_1\mathrm{F}_2(\frac{2}{3}+\frac{n}{3};\frac{4}{3},\frac{5}{3};-\frac{x^3}{9})\right\}$$

2.1533 ODE No. 1533

$$-ny(x)+y^{(3)}(x)-xy'(x)=0$$

✓ **Mathematica** : cpu = 0.0193477 (sec), leaf count = 113

$$\left\{\left\{y(x)\to \frac{\sqrt[3]{-1}c_2x\,{}_1F_2\left(\frac{n}{3}+\frac{1}{3};\frac{2}{3},\frac{4}{3};\frac{x^3}{9}\right)}{3^{2/3}}+c_1\,{}_1F_2\left(\frac{n}{3};\frac{1}{3},\frac{2}{3};\frac{x^3}{9}\right)+\frac{(-1)^{2/3}c_3x^2\,{}_1F_2\left(\frac{n}{3}+\frac{2}{3};\frac{4}{3},\frac{5}{3};\frac{x^3}{9}\right)}{3\sqrt[3]{3}}\right\}\right\}$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 58

$$\left\{y(x)=\_C1\,{}_1\mathrm{F}_2(\frac{n}{3};\,\frac{1}{3},\frac{2}{3};\,\frac{x^3}{9})+\_C2\,x\,{}_1\mathrm{F}_2(\frac{1}{3}+\frac{n}{3};\,\frac{2}{3},\frac{4}{3};\,\frac{x^3}{9})+\_C3\,x^2\,{}_1\mathrm{F}_2(\frac{2}{3}+\frac{n}{3};\,\frac{4}{3},\frac{5}{3};\,\frac{x^3}{9})\right\}$$

2.1534 ODE No. 1534

$$y^{(4)}(x)=0$$

✓ **Mathematica** : cpu = 0.00509411 (sec), leaf count = 24

$$\{\{y(x)\to c_4x^3+c_3x^2+c_2x+c_1\}\}$$

✓ **Maple** : cpu = 0.009 (sec), leaf count = 21

$$\left\{y(x)=\frac{\_C1\,x^3}{6}+\frac{\_C2\,x^2}{2}+\_C3\,x+\_C4\right\}$$

2.1535 ODE No. 1535

$$-f(x)+y^{(4)}(x)+4y(x)=0$$

✓ **Mathematica** : cpu = 1.35743 (sec), leaf count = 219

$$\left\{\left\{y(x)\to e^{-x}\left(\cos(x)\int_1^x\frac{1}{8}e^{K[1]}f(K[1])(\cos(K[1])-\sin(K[1]))\left(\sin^2(K[1])+\cos^2(K[1])\right)\,dK[1]+e^{2x}\cos(x)\int\right.\right.\right.$$

✓ **Maple** : cpu = 0.019 (sec), leaf count = 36

$$\left\{y(x)=\frac{f}{4}+\_C1\,\mathrm{e}^{x}\cos\left(x\right)+\_C2\,\mathrm{e}^{x}\sin\left(x\right)+\_C3\,\mathrm{e}^{-x}\cos\left(x\right)+\_C4\,\mathrm{e}^{-x}\sin\left(x\right)\right\}$$

2.1536 ODE No. 1536

$$\lambda y(x) + y^{(4)}(x) = 0$$

✓ **Mathematica** : cpu = 0.00614654 (sec), leaf count = 76

$$\left\{\left\{y(x) \to c_1 e^{(-1)^{3/4}\sqrt[4]{\lambda}x} + c_2 e^{-\sqrt[4]{-1}\sqrt[4]{\lambda}x} + c_3 e^{-(-1)^{3/4}\sqrt[4]{\lambda}x} + c_4 e^{\sqrt[4]{-1}\sqrt[4]{\lambda}x}\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 50

$$\left\{y(x) = \_C1\, \mathrm{e}^{-i\sqrt[4]{-\lambda}x} + \_C2\, \mathrm{e}^{i\sqrt[4]{-\lambda}x} + \_C3\, \mathrm{e}^{-\sqrt[4]{-\lambda}x} + \_C4\, \mathrm{e}^{\sqrt[4]{-\lambda}x}\right\}$$

2.1537 ODE No. 1537

$$-16e^{x^2}x^4 + y^{(4)}(x) - 12y''(x) + 12y(x) = 0$$

✓ **Mathematica** : cpu = 0.948894 (sec), leaf count = 1722

$$\left\{\left\{y(x) \to \frac{1}{12}e^{-\left(\sqrt{2\left(3-\sqrt{6}\right)}-x\right)x-\sqrt{2\left(3+\sqrt{6}\right)}x-\sqrt{2\left(3-\sqrt{6}\right)}x}\left(-2\sqrt{3+\sqrt{6}}e^{\sqrt{2\left(3+\sqrt{6}\right)}x+2\sqrt{2\left(3-\sqrt{6}\right)}x}x^3+2\sqrt{3+\sqrt{6}}\right.\right.$$

✓ **Maple** : cpu = 0.147 (sec), leaf count = 67

$$\left\{y(x) = \mathrm{e}^{x^2} + \_C1\, \mathrm{e}^{\sqrt{6-2\sqrt{6}}x} + \_C2\, \mathrm{e}^{\sqrt{6+2\sqrt{6}}x} + \_C3\, \mathrm{e}^{-\sqrt{6-2\sqrt{6}}x} + \_C4\, \mathrm{e}^{-\sqrt{6+2\sqrt{6}}x}\right\}$$

2.1538 ODE No. 1538

$$a^4 y(x) + 2a^2 y''(x) - \cosh(ax) + y^{(4)}(x) = 0$$

✓ **Mathematica** : cpu = 0.261199 (sec), leaf count = 66

$$\left\{\left\{y(x) \to \frac{\cos^2(ax)\cosh(ax) + \sin^2(ax)\cosh(ax)}{4a^4} + c_3\sin(ax) + c_4 x\sin(ax) + c_1\cos(ax) + c_2 x\cos(ax)\right\}\right\}$$

✓ **Maple** : cpu = 0.523 (sec), leaf count = 51

$$\left\{y(x) = \frac{\mathrm{e}^{-ax} + (8\,\_C3\,x + 8\,\_C1)\,a^4\cos(ax) + (8\,\_C4\,x + 8\,\_C2)\,a^4\sin(ax) + \mathrm{e}^{ax}}{8\,a^4}\right\}$$

2.1539 ODE No. 1539

$$a^4\lambda y(x)+a^2(\lambda+1)y''(x)+y^{(4)}(x)=0$$

✓ **Mathematica** : cpu = 0.00794484 (sec), leaf count = 44

$$\left\{\left\{y(x)\to c_2\sin\left(a\sqrt{\lambda}x\right)+c_1\cos\left(a\sqrt{\lambda}x\right)+c_4\sin(ax)+c_3\cos(ax)\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 35

$$\left\{y(x)=\_C1\ \sin(ax)+\_C2\ \cos(ax)+\_C3\ \sin\left(a\sqrt{\lambda}x\right)+\_C4\ \cos\left(a\sqrt{\lambda}x\right)\right\}$$

2.1540 ODE No. 1540

$$a(bx-1)y''(x)+aby'(x)+\lambda y(x)+y^{(4)}(x)=0$$

✗ **Mathematica** : cpu = 0.402449 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{\lambda y(x)+aby'(x)+a(xb-1)y''(x)+y^{(4)}(x)=0,y(0)=c_1,y'(0)=c_2,y''(0)\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\lambda\_Y(x)+ab\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+a(bx-1)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\frac{\mathrm{d}^4}{\mathrm{d}x^4}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1541 ODE No. 1541

$$y''(x)\left(ax^2+b\lambda+c\right)+y(x)\left(ax^2+\beta\lambda+\gamma\right)+y^{(4)}(x)=0$$

✗ **Mathematica** : cpu = 80.2199 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{\left(ax^2+\beta\lambda+\gamma\right)y(x)+\left(ax^2+c+b\lambda\right)y''(x)+y^{(4)}(x)=0,y(0)=c_1,y'(0)=\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\left(ax^2+\beta\,\lambda+\gamma\right)\_Y(x)+\left(ax^2+b\lambda+c\right)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+\frac{\mathrm{d}^4}{\mathrm{d}x^4}\_Y(x)\right\},\{\_Y(x)\}\right)\right\}$$

2.1542 ODE No. 1542

$$ay''(x)\wp(x;\mathrm{g2},\mathrm{g3})+by'(x)\wp'(x;\mathrm{g2},\mathrm{g3})+y(x)\left(c\left(6\wp(x;\mathrm{g2},\mathrm{g3})^2-\frac{\mathrm{g2}}{2}\right)+d\right)+y^{(4)}(x)=0$$

✗ **Mathematica** : cpu = 0.0289977 (sec), leaf count = 0 , could not solve

```
DSolve[(d + c*(-g2/2 + 6*WeierstrassP[x, {g2, g3}]^2))*y[x] + b*WeierstrassPPrime[x, {g2, g3
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^4}{\mathrm{d}x^4}\_Y(x)+a\,WeierstrassP(x,g2,g3)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+b\,WeierstrassPPrime(x,g2,g3)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(\right.\right.$$

2.1543 ODE No. 1543

$$-y''(x)\left(a+12k^2\mathrm{sn}(z|x)^2\right)+y(x)\left(\alpha\mathrm{sn}(z|x)^2+\beta\right)+by'(x)+y^{(4)}(x)=0$$

✗ **Mathematica** : cpu = 0.0954414 (sec), leaf count = 0 , could not solve

```
DSolve[(beta + alpha*JacobiSN[z, x]^2)*y[x] + b*Derivative[1][y][x] - (a + 12*k^2*JacobiSN[z
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=DESol\left(\left\{\frac{\mathrm{d}^4}{\mathrm{d}x^4}\_Y(x)+\left(-12\,k^2(JacobiSN(z,x))^2-a\right)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)+b\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\left(\alpha\,(JacobiSN(z,x)\right.\right.\right.$$

2.1544 ODE No. 1544

$$y(x)\left(3f''(x)+3f(x)^2\right)+10f'(x)y'(x)+10f(x)y''(x)+y^{(4)}(x)=0$$

✗ **Mathematica** : cpu = 0.0153156 (sec), leaf count = 0 , could not solve

```
DSolve[10*Derivative[1][f][x]*Derivative[1][y][x] + y[x]*(3*f[x]^2 + 3*Derivative[2][f][x])
```

✓ **Maple** : cpu = 0.017 (sec), leaf count = 41

$$\left\{y(x)=\sum_{\_a=1}^{4}\mathrm{e}^{RootOf\left(\_Z^4+10\,f\_Z^2+10\,df\,\_Z+3\,f^2+3\,ddf,index=\_a\right)x}\_C\_a\right\}$$

2.1545 ODE No. 1545

$$y^{(4)}(x)+2y^{(3)}(x)-3y''(x)-4y'(x)+4y(x)-32\sin(2x)+24\cos(2x)=0$$

✓ **Mathematica** : cpu = 0.177229 (sec), leaf count = 40

$$\{\{y(x)\to c_1e^{-2x}+c_2e^{-2x}x+c_3e^x+c_4e^xx+\sin(2x)\}\}$$

✓ **Maple** : cpu = 0.137 (sec), leaf count = 27

$$\{y(x) = (\_C4\,x+\_C2)\,\mathrm{e}^{-2\,x}+\sin(2\,x)+(\_C3\,x+\_C1)\,\mathrm{e}^{x}\}$$

2.1546 ODE No. 1546

$$a^4x^4y(x)+4a^3x^3y'(x)+6a^2x^2y''(x)+4axy^{(3)}(x)+y^{(4)}(x)=0$$

✓ **Mathematica** : cpu = 0.709805 (sec), leaf count = 301

$$\left\{\left\{y(x)\to \frac{2\left(\sqrt{6}-3\right)\sqrt{-\left(\sqrt{6}-3\right)a}c_3\exp\left(-\frac{ax^2}{2}-\sqrt{-\left(\sqrt{6}-3\right)a}x-\frac{\left(-3+\sqrt{3}+\sqrt{6}\right)ax}{\sqrt{-\left(\sqrt{6}-3\right)a}}\right)}{\left(-3-\sqrt{3}+\sqrt{6}\right)\left(-3+\sqrt{3}+\sqrt{6}\right)a}+\frac{2\left(\sqrt{6}-3\right)\sqrt{-(\sqrt{}}\right.\right.$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 73

$$\left\{y(x) = \mathrm{e}^{-\frac{ax^2}{2}}\left(\_C2\,\mathrm{e}^{\sqrt{-a\left(\sqrt{6}-3\right)}x}+\_C4\,\mathrm{e}^{\sqrt{\left(3+\sqrt{6}\right)a}x}+\_C1\,\mathrm{e}^{-\sqrt{-a\left(\sqrt{6}-3\right)}x}+\_C3\,\mathrm{e}^{-\sqrt{\left(3+\sqrt{6}\right)a}x}\right)\right\}$$

2.1547 ODE No. 1547

$$3y(x)\left(2g(x)f'(x)+5f(x)g'(x)+6f(x)^2g(x)+g''(x)+3g(x)^2\right)+y''(x)\left(4f'(x)+11f(x)^2+10g(x)\right)+y'(x)\left(f''(x\right.$$

✗ **Mathematica** : cpu = 0.0344829 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x]*(6*f[x]^3 + 30*f[x]*g[x] + 7*f[x]*Derivative[1][f][x] + 10*Deriva
```

✓ **Maple** : cpu = 0.023 (sec), leaf count = 87

$$\left\{y(x) = \sum_{\_a=1}^{4}\mathrm{e}^{RootOf\left(\_Z^4+6\,f\_Z^3+\left(11\,f^2+4\,df+10\,g\right)\_Z^2+\left(6\,f^3+7\,df\,f+30\,fg+ddf+10\,dg\right)\_Z+18\,f^2g+6\,df\,g+15\,dg\,f+9\,g^2+3\,ddg,in\right.}\right.$$

2.1548 ODE No. 1548

$$4y^{(4)}(x) - 12y^{(3)}(x) + 11y''(x) - 3y'(x) - 4\cos(x) = 0$$

✓ **Mathematica** : cpu = 0.0945294 (sec), leaf count = 50

$$\left\{\left\{y(x) \to 2c_1 e^{x/2} + \frac{2}{3}c_2 e^{3x/2} + c_3 e^x + c_4 + \frac{18\sin(x)}{65} - \frac{14\cos(x)}{65}\right\}\right\}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 32

$$\left\{y(x) = -\frac{14\cos(x)}{65} + \frac{18\sin(x)}{65} + \_C1\, \mathrm{e}^x + 2\_C2\, \mathrm{e}^{x/2} + \frac{2\_C3}{3}\mathrm{e}^{\frac{3x}{2}} + \_C4\right\}$$

2.1549 ODE No. 1549

$$xy^{(4)}(x) + 5y^{(3)}(x) - 24 = 0$$

✓ **Mathematica** : cpu = 0.0133231 (sec), leaf count = 34

$$\left\{\left\{y(x) \to c_4 x^2 - \frac{c_1}{24x^2} + c_3 x + c_2 + \frac{4x^3}{5}\right\}\right\}$$

✓ **Maple** : cpu = 0.02 (sec), leaf count = 26

$$\left\{y(x) = -\frac{\_C1}{24\,x^2} + \frac{4\,x^3}{5} + \frac{\_C2\,x^2}{2} + \_C3\,x + \_C4\right\}$$

2.1550 ODE No. 1550

$$12x^3y''(x) - \left(6x^2+1\right)y^{(3)}(x) - \left(9x^2-7\right)x^2y'(x) + 2\left(x^2-3\right)x^3y(x) + xy^{(4)}(x) = 0$$

✓ **Mathematica** : cpu = 4.92622 (sec), leaf count = 262

$$\left\{\left\{y(x) \to c_3 e^{\frac{x^2}{2}} \int_1^x \frac{e^{\frac{K[1]^2}{2}} K[1]\left(\int \frac{U\left(\frac{1}{20}\left(-5-9\sqrt{5}\right),-\frac{1}{2},\frac{1}{2}\sqrt{5}K[1]^2\right)\exp\left(\frac{1}{2}\left(-\frac{1}{2}K[1]^2-2\log(K[1])\right)-\frac{1}{4}\sqrt{5}K[1]^2\right)}{\sqrt{K[1]}\sqrt[4]{K[1]^2}}\,dK[1]\right)}{\sqrt[4]{2}}\,dK[1\right.\right.\right.$$

✓ **Maple** : cpu = 0.789 (sec), leaf count = 157

$$\left\{y(x) = -\mathrm{e}^{x^2}\int 1M_{\frac{9\sqrt{5}}{20},\frac{3}{4}}\left(\frac{\sqrt{5}x^2}{2}\right)\mathrm{e}^{-\frac{x^2}{4}}x^{-\frac{3}{2}}\,\mathrm{d}x\_C3 - \mathrm{e}^{x^2}\int 1W_{\frac{9\sqrt{5}}{20},\frac{3}{4}}\left(\frac{\sqrt{5}x^2}{2}\right)\mathrm{e}^{-\frac{x^2}{4}}x^{-\frac{3}{2}}\,\mathrm{d}x\_C4 + \int 1M_{\frac{9\sqrt{5}}{20},\frac{3}{4}}\right.$$

2.1551 ODE No. 1551

$$-2\left(\nu^2x^2+6\right)y''(x)+\nu^2\left(\nu^2x^2+4\right)y(x)+x^2y^{(4)}(x)=0$$

✓ **Mathematica** : cpu = 0.44186 (sec), leaf count = 110

$$\left\{\left\{y(x)\to\frac{c_3(1-x)e^{-\nu x}\left(\nu^2x^2+\nu^2x+\nu^2+6\nu x+6\nu+15\right)}{x}+\frac{c_4(1-x)e^{\nu x}\left(\nu^2x^2+\nu^2x+\nu^2-6\nu x-6\nu+15\right)}{x}\right.\right.$$

✓ **Maple** : cpu = 0.265 (sec), leaf count = 62

$$\left\{y(x)=\frac{\left(\_C4\,\nu^2x^3+6\,\_C4\,\nu\,x^2+15\,\_C4\,x+\_C2\right)\mathrm{e}^{-x\nu}+\mathrm{e}^{x\nu}\left(\_C3\,\nu^2x^3-6\,\_C3\,\nu\,x^2+15\,\_C3\,x+\_C1\right)}{x}\right.$$

2.1552 ODE No. 1552

$$ay(x)-bx^2+x^2y^{(4)}(x)+2xy^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.076 (sec), leaf count = 89

$$\left\{y(x)=\frac{bx^2}{a}+\_C1\,\sqrt{x}J_1\left(2\sqrt[4]{-a}\sqrt{x}\right)+\_C2\,\sqrt{x}Y_1\left(2\sqrt[4]{-a}\sqrt{x}\right)+\_C3\,\sqrt{x}J_1\left(2\sqrt{-\sqrt{-a}}\sqrt{x}\right)+\_C4\,\sqrt{x}Y_1\left(2\right.\right.$$

2.1553 ODE No. 1553

$$x^2y^{(4)}(x)+4xy^{(3)}(x)+2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0243049 (sec), leaf count = 29

$$\{\{y(x)\to c_1(-x)+c_4x+c_1x\log(x)-c_2\log(x)+c_3\}\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 17

$$\{y(x)=(\_C2\,x+\_C4)\ln(x)+\_C1\,x+\_C3\}$$

2.1554 ODE No. 1554

$$x^2 y^{(4)}(x) + 6x y^{(3)}(x) + 6y''(x) = 0$$

✓ **Mathematica** : cpu = 0.023734 (sec), leaf count = 29

$$\left\{\left\{y(x) \to c_4 x + \frac{1}{2}\left(\frac{c_2}{x} - 2c_1 \log(x)\right) + c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 18

$$\left\{y(x) = \_C1 + \_C2\ \ln(x) + \_C3\ x + \frac{\_C4}{x}\right\}$$

2.1555 ODE No. 1555

$$\lambda^2(-y(x)) + x^2 y^{(4)}(x) + 6x y^{(3)}(x) + 6y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0694051 (sec), leaf count = 156

$$\left\{\left\{y(x) \to c_4 G^{2,0}_{0,4}\left(\frac{\lambda^2 x^2}{16}\middle|\ -\tfrac{1}{2}, \tfrac{1}{2}, 0, 0\ \right) + c_2 G^{2,0}_{0,4}\left(\frac{\lambda^2 x^2}{16}\middle|\ 0, 0, -\tfrac{1}{2}, \tfrac{1}{2}\ \right) + \frac{c_1\left(J_1\left(2\sqrt{\lambda}\sqrt{x}\right) + I_1\left(2\sqrt{\lambda}\sqrt{x}\right)\right)}{2\sqrt{\lambda}\sqrt{x}} - \frac{ic_3}{}\right.\right.$$

✓ **Maple** : cpu = 0.181 (sec), leaf count = 61

$$\left\{y(x) = 1\left(\_C1\ J_1\left(2\sqrt{\lambda}\sqrt{x}\right) + \_C2\ Y_1\left(2\sqrt{\lambda}\sqrt{x}\right) + \_C4\ Y_1\left(2\sqrt{-\lambda}\sqrt{x}\right) + \_C3\ J_1\left(2\sqrt{-\lambda}\sqrt{x}\right)\right)\frac{1}{\sqrt{x}}\right\}$$

2.1556 ODE No. 1556

$$x^2 y^{(4)}(x) + 8x y^{(3)}(x) + 12y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0232544 (sec), leaf count = 30

$$\left\{\left\{y(x) \to \frac{1}{6}\left(\frac{c_1}{x^2} + \frac{3c_2}{x}\right) + c_4 x + c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.014 (sec), leaf count = 19

$$\left\{y(x) = \_C1 + \frac{\_C2}{x^2} + \_C3\ x + \frac{\_C4}{x}\right\}$$

2.1557 ODE No. 1557

$$\lambda^2(-y(x)) + x^2 y^{(4)}(x) + 8xy^{(3)}(x) + 12y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0728599 (sec), leaf count = 146

$$\left\{\left\{y(x) \to c_4 G_{0,4}^{2,0}\left(\frac{\lambda^2 x^2}{16}\middle| \begin{array}{c} -1,0,-\frac{1}{2},\frac{1}{2} \end{array}\right) + c_2 G_{0,4}^{2,0}\left(\frac{\lambda^2 x^2}{16}\middle| \begin{array}{c} -\frac{1}{2},\frac{1}{2},-1,0 \end{array}\right) - \frac{3ic_1\left(I_2\left(2\sqrt{\lambda}\sqrt{x}\right) - J_2\left(2\sqrt{\lambda}\sqrt{x}\right)\right)}{4\lambda x}\right.\right.$$

✓ **Maple** : cpu = 0.142 (sec), leaf count = 61

$$\left\{y(x) = \frac{1}{x}\left(\_C2\, Y_2\left(2\sqrt{\lambda}\sqrt{x}\right) + \_C3\, J_2\left(2\sqrt{-\lambda}\sqrt{x}\right) + \_C4\, Y_2\left(2\sqrt{-\lambda}\sqrt{x}\right) + \_C1\, J_2\left(2\sqrt{\lambda}\sqrt{x}\right)\right)\right\}$$

2.1558 ODE No. 1558

$$-\frac{1}{16}b^4 y(x) + x(2n - 2\nu + 4)y^{(3)}(x) + (n - \nu + 1)(n - \nu + 2)y''(x) + x^2 y^{(4)}(x) = 0$$

✓ **Mathematica** : cpu = 0.167481 (sec), leaf count = 319

$$\left\{\left\{y(x) \to c_4 i^{-n+\nu+1} 2^{3n-3\nu-3} b^{2(-n+\nu+1)+n-\nu-2} x^{\frac{1}{2}(n-\nu-2)-n+\nu+1}\Gamma(-n+\nu+2)\left(I_{\nu-n}\left(b\sqrt{x}\right) - J_{\nu-n}\left(b\sqrt{x}\right)\right) + c_3\right.\right.$$

✓ **Maple** : cpu = 0.194 (sec), leaf count = 67

$$\left\{y(x) = x^{-\frac{n}{2}+\frac{\nu}{2}}\left(K_{n-\nu}\left(b\sqrt{x}\right)\_C3 + Y_{n-\nu}\left(b\sqrt{x}\right)\_C4 + J_{n-\nu}\left(b\sqrt{x}\right)\_C2 + I_{n-\nu}\left(b\sqrt{x}\right)\_C1\right)\right\}$$

2.1559 ODE No. 1559

$$a^4\left(-x^3\right)y(x) + x^3 y^{(4)}(x) + 2x^2 y^{(3)}(x) - xy''(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.300403 (sec), leaf count = 100

$$\left\{\left\{y(x) \to c_4 G_{0,4}^{2,0}\left(\frac{a^4 x^4}{256}\middle| \begin{array}{c} 0,0,\frac{1}{2},\frac{1}{2} \end{array}\right) + c_2 G_{0,4}^{2,0}\left(\frac{a^4 x^4}{256}\middle| \begin{array}{c} \frac{1}{2},\frac{1}{2},0,0 \end{array}\right) + \frac{1}{8}ic_1(I_0(ax) - J_0(ax)) + \frac{1}{2}c_3(J_0(ax) + I_0(a\right.\right.$$

✓ **Maple** : cpu = 0.185 (sec), leaf count = 33

$$\{y(x) = \_C1\, I_0(ax) + \_C2\, J_0(ax) + \_C3\, K_0(ax) + \_C4\, Y_0(ax)\}$$

2.1560 ODE No. 1560

$$x^3 y^{(4)}(x) + 6x^2 y^{(3)}(x) + 6x y''(x) = 0$$

✓ **Mathematica** : cpu = 0.0215508 (sec), leaf count = 29

$$\left\{\left\{y(x) \to c_4 x + \frac{1}{2}\left(\frac{c_2}{x} - 2c_1 \log(x)\right) + c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 18

$$\left\{y(x) = \_C1 + \_C2\ \ln(x) + \_C3\ x + \frac{\_C4}{x}\right\}$$

2.1561 ODE No. 1561

$$y(x)\left(ax^4 + (n-2)n(n+1)(n+3)\right) - 2n(n+1)x^2 y''(x) + 4n(n+1)x y'(x) + x^4 y^{(4)}(x) = 0$$

✓ **Mathematica** : cpu = 3.96073 (sec), leaf count = 400

$$\left\{\left\{y(x) \to c_1\left(-2^{n-\frac{5}{2}}\right)\sqrt{x}a^{\frac{2-n}{4}+\frac{1}{4}(n-\frac{3}{2})}\Gamma\left(\frac{3}{2}-n\right)\left(\cos\left(\frac{3}{4}\pi\left(\frac{3}{2}-n\right)\right)\text{ber}_{-n-\frac{1}{2}}\left(\sqrt[4]{a}x\right) + \sin\left(\frac{3}{4}\pi\left(\frac{3}{2}-n\right)\right)\text{be}\right.\right.\right.$$

✓ **Maple** : cpu = 0.285 (sec), leaf count = 69

$$\left\{y(x) = \sqrt{x}\left(Y_{n+\frac{1}{2}}\left(\sqrt[4]{-a}x\right)\_C2 + J_{n+\frac{1}{2}}\left(\sqrt[4]{-a}x\right)\_C1 + Y_{n+\frac{1}{2}}\left(\sqrt{-\sqrt{-a}}x\right)\_C4 + J_{n+\frac{1}{2}}\left(\sqrt{-\sqrt{-a}}x\right)\_C3\right)\right\}$$

2.1562 ODE No. 1562

$$-\left(4n^2-1\right)x^2 y''(x) + \left(4n^2-1\right)x y'(x) + x^4 y^{(4)}(x) - 4x^4 y(x) + 4x^3 y^{(3)}(x) = 0$$

✓ **Mathematica** : cpu = 1.11848 (sec), leaf count = 140

$$\left\{\left\{y(x) \to c_1\,{}_0F_3\left(;\frac{1}{2},1-\frac{n}{2},\frac{n}{2}+1;\frac{x^4}{64}\right) + \frac{1}{8}ic_2x^2\,{}_0F_3\left(;\frac{3}{2},\frac{3}{2}-\frac{n}{2},\frac{n}{2}+\frac{3}{2};\frac{x^4}{64}\right) + c_3\left(\frac{i}{2}\right)^{-n}\Gamma(1-n)^2\left(\text{ber}_{-n}(x\right.\right.\right.$$

✓ **Maple** : cpu = 0.408 (sec), leaf count = 77

$$\left\{y(x) = \left(Y_n\left(\left(\frac{1}{2}-\frac{i}{2}\right)\sqrt{2}x\right)\_C3 + \_C1\ J_n\left(\left(\frac{1}{2}-\frac{i}{2}\right)\sqrt{2}x\right)\right)J_n\left(\left(\frac{1}{2}+\frac{i}{2}\right)\sqrt{2}x\right) + Y_n\left(\left(\frac{1}{2}+\frac{i}{2}\right)\sqrt{2}x\right)\left(\right.\right.$$

2.1563 ODE No. 1563

$$\left(4n^2-4x^4-1\right)y(x)-\left(4n^2-1\right)x^2y''(x)-\left(4n^2-1\right)xy'(x)+x^4y^{(4)}(x)+4x^3y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 1.87275 (sec), leaf count = 232

$$\left\{\left\{y(x)\to \frac{\sqrt[4]{-1}c_2x\,{}_0F_3\left(;\frac{3}{2},1-\frac{n}{2},\frac{n}{2}+1;\frac{x^4}{64}\right)}{2\sqrt{2}}-\frac{2(-1)^{3/4}\sqrt{2}c_1\,{}_0F_3\left(;\frac{1}{2},\frac{1}{2}-\frac{n}{2},\frac{n}{2}+\frac{1}{2};\frac{x^4}{64}\right)}{x}+c_3(-1)^{\frac{1}{4}(1-2n)}2^{2n+}\right.\right.$$

✓ **Maple** : cpu = 0.283 (sec), leaf count = 87

$$\left\{y(x)=\frac{1}{x}\left(\_C4\,{}_0\mathrm{F}_3(\ ;\frac{1}{2},-\frac{n}{2}+\frac{1}{2},\frac{n}{2}+\frac{1}{2};\frac{x^4}{64})+x^2\left(\_C3\,{}_0\mathrm{F}_3(\ ;\frac{3}{2},-\frac{n}{2}+1,\frac{n}{2}+1;\frac{x^4}{64})+\_C2\,(\mathrm{bei}_{-n}(x))^2+\right.\right.\right.$$

2.1564 ODE No. 1564

$$-\left(12n^2+4x^4-3\right)y(x)-\left(4n^2+3\right)x^2y''(x)+\left(12n^2-3\right)xy'(x)+x^4y^{(4)}(x)+4x^3y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 1.37124 (sec), leaf count = 230

$$\left\{\left\{y(x)\to \frac{\sqrt[4]{-1}c_1x\,{}_0F_3\left(;\frac{1}{2},\frac{3}{2}-\frac{n}{2},\frac{n}{2}+\frac{3}{2};\frac{x^4}{64}\right)}{2\sqrt{2}}+c_3(-1)^{\frac{1}{4}(-2n-1)}2^{2n+\frac{1}{2}(2n+1)+1}x^{-2n-1}\,{}_0F_3\left(;1-n,\frac{1}{2}-\frac{n}{2},-\frac{n}{2};\right.\right.\right.$$

✓ **Maple** : cpu = 0.263 (sec), leaf count = 88

$$\left\{y(x)=\frac{1}{x}\left(\_C4\,x^2{}_0\mathrm{F}_3(\ ;\frac{1}{2},\frac{3}{2}-\frac{n}{2},\frac{n}{2}+\frac{3}{2};\frac{x^4}{64})+\_C3\,x^4{}_0\mathrm{F}_3(\ ;\frac{3}{2},-\frac{n}{2}+2,\frac{n}{2}+2;\frac{x^4}{64})+\_C2\,(\mathrm{bei}_{-n}(x))^2+(\right.\right.\right.$$

2.1565 ODE No. 1565

$$\left(x\left(-\rho^2-\sigma^2+1\right)+16x^3\right)y'(x)+y(x)\left(\rho^2\sigma^2+8x^2\right)+\left(x^2\left(-\rho^2-\sigma^2+7\right)+4x^4\right)y''(x)+x^4y^{(4)}(x)+6x^3y^{(3)}(x)=0$$

✓ **Mathematica** : cpu = 0.5619 (sec), leaf count = 242

$$\left\{\left\{y(x)\to c_1x^{-\rho}\,{}_2F_3\left(\frac{1}{2}-\frac{\rho}{2},1-\frac{\rho}{2};1-\rho,-\frac{\rho}{2}-\frac{\sigma}{2}+1,-\frac{\rho}{2}+\frac{\sigma}{2}+1;-x^2\right)+c_3x^{-\sigma}\,{}_2F_3\left(\frac{1}{2}-\frac{\sigma}{2},1-\frac{\sigma}{2};1-\sigma,-\right.\right.\right.$$

✓ **Maple** : cpu = 0.437 (sec), leaf count = 71

$$\left\{y(x)=\left(Y_{\frac{\rho}{2}+\frac{\sigma}{2}}(x)\_C3+\_C1\,J_{\frac{\rho}{2}+\frac{\sigma}{2}}(x)\right)J_{-\frac{\sigma}{2}+\frac{\rho}{2}}(x)+Y_{-\frac{\sigma}{2}+\frac{\rho}{2}}(x)\left(Y_{\frac{\rho}{2}+\frac{\sigma}{2}}(x)\_C4+\_C2\,J_{\frac{\rho}{2}+\frac{\sigma}{2}}(x)\right)\right\}$$

2.1566 ODE No. 1566

$$\left(x\left(-2\mu^2-2\nu^2+1\right)+16x^3\right)y'(x)+y(x)\left(\left(\mu^2-\nu^2\right)^2+8x^2\right)+\left(x^2\left(-2\mu^2-2\nu^2+7\right)+4x^4\right)y''(x)+x^4y^{(4)}(x)+6x$$

✓ **Mathematica** : cpu = 0.665816 (sec), leaf count = 238

$$\left\{\left\{y(x)\to c_1x^{-\mu-\nu}\,{}_2F_3\left(-\frac{\mu}{2}-\frac{\nu}{2}+\frac{1}{2},-\frac{\mu}{2}-\frac{\nu}{2}+1;1-\mu,1-\nu,-\mu-\nu+1;-x^2\right)+c_2x^{\mu-\nu}\,{}_2F_3\left(\frac{\mu}{2}-\frac{\nu}{2}+\frac{1}{2},\frac{\mu}{2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.399 (sec), leaf count = 35

$$\{y(x)=(Y_\mu(x)\_C2+\_C1\,J_\mu(x))\,J_\nu(x)+Y_\nu(x)(Y_\mu(x)\_C4+\_C3\,J_\mu(x))\}$$

2.1567 ODE No. 1567

$$x^4y^{(4)}(x)+8x^3y^{(3)}(x)+12x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.023328 (sec), leaf count = 30

$$\left\{\left\{y(x)\to\frac{1}{6}\left(\frac{c_1}{x^2}+\frac{3c_2}{x}\right)+c_4x+c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 19

$$\left\{y(x)=\_C1+\frac{\_C2}{x^2}+\_C3\,x+\frac{\_C4}{x}\right\}$$

2.1568 ODE No. 1568

$$ay(x)+x^4y^{(4)}(x)+8x^3y^{(3)}(x)+12x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0128687 (sec), leaf count = 122

$$\left\{\left\{y(x)\to c_1x^{\frac{1}{2}\left(-\sqrt{5-4\sqrt{1-a}}-1\right)}+c_2x^{\frac{1}{2}\left(\sqrt{5-4\sqrt{1-a}}-1\right)}+c_3x^{\frac{1}{2}\left(-\sqrt{4\sqrt{1-a}+5}-1\right)}+c_4x^{\frac{1}{2}\left(\sqrt{4\sqrt{1-a}+5}-1\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 89

$$\left\{y(x)=\_C1\,x^{-\frac{1}{2}-\frac{1}{2}\sqrt{5-4\sqrt{1-a}}}+\_C2\,x^{-\frac{1}{2}+\frac{1}{2}\sqrt{5-4\sqrt{1-a}}}+\_C3\,x^{-\frac{1}{2}-\frac{1}{2}\sqrt{5+4\sqrt{1-a}}}+\_C4\,x^{-\frac{1}{2}+\frac{1}{2}\sqrt{5+4\sqrt{1-a}}}\right\}$$

2.1569 ODE No. 1569

$$xy'(x)\left((2a-1)\text{C0}+4b^2\text{B0}c^2x^{2c}\right)+(6-4a)x^3y^{(3)}(x)+x^2y''(x)\left(\text{A0}+4b^2c^2x^{2c}\right)+y(x)\left(4b^2c^2\text{D0}x^{2c}+\text{E0}\right)+x^4y^{(4)}($$

✗ **Mathematica** : cpu = 301.247 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.55 (sec), leaf count = 63

$$\{y(x)=((J_\mu(x^cb)\_C2+Y_\mu(x^cb)\_C3)\,J_\nu(x^cb)+Y_\nu(x^cb)(\_C4\,Y_\mu(x^cb)+\_C1\,J_\mu(x^cb)))\,x^a\}$$

2.1570 ODE No. 1570

$$y(x)\left(\left(a^2-c^2\nu^2\right)\left(a^2+4ac-c^2\nu^2+4c^2\right)-b^4c^4x^{4c}\right)+x^2\left(2a^2+4(a+c-1)^2+4(a-1)(c-1)-2c^2\nu^2-1\right)y''($$

✓ **Mathematica** : cpu = 0.154848 (sec), leaf count = 470

$$\left\{\left\{y(x)\to c_1\Gamma(1-\nu)(-1)^{\frac{a-c\nu}{4c}}2^{-\frac{2(a-c\nu)}{c}-\nu-1}b^{\frac{a-c\nu}{c}+\nu}\left(x^{4c}\right)^{\frac{a-c\nu}{4c}+\frac{\nu}{4}}\left(J_{-\nu}\left(b\sqrt[4]{x^{4c}}\right)+I_{-\nu}\left(b\sqrt[4]{x^{4c}}\right)\right)+c_2\Gamma(2-\nu)(-\right.\right.$$

✓ **Maple** : cpu = 0.102 (sec), leaf count = 49

$$\{y(x)=x^a(Y_\nu(x^cb)\_C2+Y_\nu(ibx^c)\_C4+J_\nu(ibx^c)\_C3+J_\nu(x^cb)\_C1)\}$$

2.1571 ODE No. 1571

$$-\frac{1}{16}b^4x^{2/v}y(x)+\nu^4x^4y^{(4)}(x)+\nu^3(4\nu-2)x^3y^{(3)}(x)+(\nu-1)\nu^2(2\nu-1)x^2y''(x)=0$$

✓ **Mathematica** : cpu = 0.0957742 (sec), leaf count = 390

$$\left\{\left\{y(x)\to c_1\,{}_0F_3\left(;1-\frac{v}{2},1-\frac{v}{2\nu},-\frac{v}{2\nu}-\frac{v}{2}+1;\frac{b^4v^4x^{2/v}}{256\nu^4}\right)+c_2\left(\frac{i}{16}\right)^v v^{2v}b^{2v}\nu^{-2v}\left(x^{2/v}\right)^{v/2}\,{}_0F_3\left(;\frac{v}{2}+1,1-\right.\right.\right.$$

✓ **Maple** : cpu = 0.204 (sec), leaf count = 143

$$\left\{y(x)=\sqrt{x}\left(J_{(\lfloor\nu^{-1}\rfloor)^{-1}}\left(\frac{1}{\lfloor\nu^{-1}\rfloor}\sqrt{\frac{b^2}{\nu^2}}x^{\frac{\lfloor\nu^{-1}\rfloor}{2}}\right)\_C1+Y_{(\lfloor\nu^{-1}\rfloor)^{-1}}\left(\frac{1}{\lfloor\nu^{-1}\rfloor}\sqrt{\frac{b^2}{\nu^2}}x^{\frac{\lfloor\nu^{-1}\rfloor}{2}}\right)\_C2+Y_{(\lfloor\nu^{-1}\rfloor)^{-1}}\left(\frac{1}{\lfloor\nu^{-1}\rfloor}\sqrt{\right.\right.\right.$$

2.1572 ODE No. 1572

$$\left(-2\left(x^2-1\right)\left(\mu(\mu+1)+\nu(\nu+1)\right)+24x^3-8\right)y''(x)-6x(\mu(\mu+1)+\nu(\nu+1)-2)y'(x)+\left((\mu(\mu+1)-\nu(\nu+1))^2-\right.$$

✗ **Mathematica** : cpu = 92.9487 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x)\to \text{DifferentialRoot}\left(\{y,x\},\left\{(\mu-\nu-1)(\mu-\nu+1)(\mu+\nu)(\mu+\nu+2)y(x)-6x\left(\mu^2+\mu+\nu^2+\nu-2\right)y\right.\right.\right.$$

✓ **Maple** : cpu = 0.464 (sec), leaf count = 35

$$\{y(x)=(LegendreQ(\mu,x)\_C2+\_C1\ LegendreP(\mu,x))\ LegendreP(\nu,x)+LegendreQ(\nu,x)\ (LegendreQ(\mu,x)\_$$

2.1573 ODE No. 1573

$$-\frac{1}{x^5}+(2x+e^x)\,y^{(4)}(x)+4(e^x+2)\,y^{(3)}(x)+6e^xy''(x)+4e^xy'(x)+e^xy(x)=0$$

✗ **Mathematica** : cpu = 0.0577964 (sec), leaf count = 0 , could not solve

```
DSolve[-x^(-5) + E^x*y[x] + 4*E^x*Derivative[1][y][x] + 6*E^x*Derivative[2][y][x] + 4*(2 + E
```

✓ **Maple** : cpu = 0.049 (sec), leaf count = 41

$$\left\{y(x)=\frac{24\_C1\,x^4+24\_C2\,x^3+24\_C3\,x^2+24\_C4\,x+1}{(24\,\mathrm{e}^x+48\,x)\,x}\right\}$$

2.1574 ODE No. 1574

$$y(x)\left(a^4\sin^4(x)-3\right)+y^{(4)}(x)\sin^4(x)+2y^{(3)}(x)\sin^3(x)\cos(x)+\left(\sin^2(x)-3\right)\sin^2(x)y''(x)+\left(2\sin^2(x)+3\right)\sin(x)\,c$$

✗ **Mathematica** : cpu = 0.207812 (sec), leaf count = 0 , could not solve

```
DSolve[(-3 + a^4*Sin[x]^4)*y[x] + Cos[x]*Sin[x]*(3 + 2*Sin[x]^2)*Derivative[1][y][x] + Sin[x
3 + Sin[x]^2)*Derivative[2][y][x] + 2*Cos[x]*Sin[x]^3*Derivative[3][y][x] + Sin[x]^4*Derivat
```

✓ **Maple** : cpu = 0.886 (sec), leaf count = 252

$$\left\{y(x)=\sin(x)\left({}_2\mathrm{F}_1\left(\frac{3}{4}-\frac{1}{4}\sqrt{-4\sqrt{-(a-1)(a+1)(a^2+1)}+5},\frac{3}{4}+\frac{1}{4}\sqrt{-4\sqrt{-(a-1)(a+1)(a^2+1)}+5};\right.\right.\right.$$

2.1575 ODE No. 1575

$$-f(x)+y^{(4)}(x)\sin^6(x)+4y^{(3)}(x)\sin^5(x)\cos(x)-6\sin^6(x)y''(x)-4\sin^5(x)\cos(x)y'(x)+y(x)\sin^6(x)=0$$

✗ **Mathematica** : cpu = 0.0662696 (sec), leaf count = 0 , could not solve

```
DSolve[-f[x] + Sin[x]^6*y[x] - 4*Cos[x]*Sin[x]^5*Derivative[1][y][x] - 6*Sin[x]^6*Derivative
```

✓ **Maple** : cpu = 0.5 (sec), leaf count = 719

$$\left\{y(x)=\frac{1}{48\left(\mathrm{e}^{2ix}-1\right)^4(\sin(x))^5}\left(12(\sin(x))^4 x\left(x^2+\frac{20}{3}\right)f\left(\mathrm{e}^{2ix}-3/2\,\mathrm{e}^{4ix}+\mathrm{e}^{6ix}-1/4\,\mathrm{e}^{8ix}-1/4\right)\ln\left(1-\mathrm{e}^{}\right.\right.\right.$$

2.1576 ODE No. 1576

$$2f'(x)\left(y^{(3)}(x)-a^2y'(x)\right)+f(x)\left(a^4y(x)-2a^2y''(x)+y^{(4)}(x)\right)=0$$

✗ **Mathematica** : cpu = 0.236966 (sec), leaf count = 0 , could not solve

```
DSolve[2*Derivative[1][f][x]*(-(a^2*Derivative[1][y][x]) + Derivative[3][y][x]) + f[x]*(a^4*
```

✓ **Maple** : cpu = 0.027 (sec), leaf count = 67

$$\left\{y(x)=\_C1\,\mathrm{e}^{ax}+\_C2\,\mathrm{e}^{-ax}+\_C3\,\mathrm{e}^{\frac{x}{f}\left(-df+\sqrt{a^2f^2+df^2}\right)}+\_C4\,\mathrm{e}^{-\frac{x}{f}\left(df+\sqrt{a^2f^2+df^2}\right)}\right\}$$

2.1577 ODE No. 1577

$$f''(x)y''(x)+2y^{(3)}(x)f'(x)+f(x)y^{(4)}(x)=0$$

✓ **Mathematica** : cpu = 1.08673 (sec), leaf count = 44

$$\left\{\left\{y(x)\to\int_1^x\left(\int_1^{K[2]}\left(\frac{c_1}{f(K[1])}+\frac{c_2K[1]}{f(K[1])}\right)dK[1]\right)dK[2]+c_4x+c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.007 (sec), leaf count = 21

$$\left\{y(x)=\frac{\_C1\,x^3}{6}+\frac{\_C2\,x^2}{2}+\_C3\,x+\_C4\right\}$$

2.1578 ODE No. 1578

$$a^4 y(x) - \lambda(ax-b)\left(y''(x) - a^2 y(x)\right) - 2a^2 y''(x) + y^{(4)}(x) = 0$$

✓ **Mathematica** : cpu = 289.847 (sec), leaf count = 139

$$\left\{\left\{y(x) \to c_3 e^{-ax}\int_1^x 2ae^{2aK[1]}\int e^{-aK[1]}\text{Ai}\left(\frac{a^2+\lambda K[1]a-b\lambda}{(a\lambda)^{2/3}}\right)dK[1]\,dK[1] + c_4 e^{-ax}\int_1^x 2ae^{2aK[2]}\int e^{-aK[2]}\text{B}\right.\right.$$

✓ **Maple** : cpu = 1.366 (sec), leaf count = 89

$$\left\{y(x) = \mathrm{e}^{ax}\left(\int \mathrm{e}^{-2\,ax}\left(\int \mathrm{e}^{ax}\left(\mathrm{Bi}\left(-\frac{\lambda\,(ax-b)+a^2}{a\lambda}\sqrt[3]{-a\lambda}\right)\_C4 + \mathrm{Ai}\left(-\frac{\lambda\,(ax-b)+a^2}{a\lambda}\sqrt[3]{-a\lambda}\right)\_C3\right)\,\mathrm{d}x + \_\right.\right.\right.$$

2.1579 ODE No. 1579

$$-ax - b\sin(x) - c\cos(x) + y^{(n)}(x) + 2y^{(3)}(x) + y'(x) = 0$$

✓ **Mathematica** : cpu = 0.677678 (sec), leaf count = 104

$$\left\{\left\{y(x) \to \frac{ax^2}{2} + \frac{1}{8}b\left(x^2-2\right)\cos(x) - \frac{3}{8}bx\sin(x) - \frac{5}{16}b\cos(x) - \frac{1}{8}c\left(x^2-2\right)\sin(x) + c_2 x\sin(x) + \frac{9}{16}c\sin(x) + c\right.\right.$$

✓ **Maple** : cpu = 0.414 (sec), leaf count = 69

$$\left\{y(x) = \frac{\left(bx^2 + \left(-4\,c - 8\,\_C4\right)x - 6\,b - 8\,\_C2 + 8\,\_C3\right)\cos(x)}{8} + \frac{\left(-cx^2 + \left(-4\,b + 8\,\_C3\right)x + 6\,c + 8\,\_C1 +\right.}{8}\right.$$

2.1580 ODE No. 1580

$$y^{(6)}(x) + y(x) - \sin\left(\frac{x}{2}\right)\sin\left(\frac{3x}{2}\right) = 0$$

✓ **Mathematica** : cpu = 0.985331 (sec), leaf count = 234

$$\left\{\left\{y(x) \to c_4 e^{-\frac{\sqrt{3}x}{2}}\sin\left(\frac{x}{2}\right) + c_6 e^{\frac{\sqrt{3}x}{2}}\sin\left(\frac{x}{2}\right) + c_5\sin(x) + c_1 e^{\frac{\sqrt{3}x}{2}}\cos\left(\frac{x}{2}\right) + c_3 e^{-\frac{\sqrt{3}x}{2}}\cos\left(\frac{x}{2}\right) + c_2\cos(x) + \frac{1}{504}\right.\right.$$

✓ **Maple** : cpu = 0.803 (sec), leaf count = 147

$$\left\{y(x) = \frac{1}{504}\left(504\,\_C3\,\cos(x/2) + 504\,\_C4\,\sin(x/2)\right)\mathrm{e}^{-\frac{\sqrt{3}x}{2}} + \frac{1}{504}\left(504\,\_C5\,\cos(x/2) + 504\,\_C6\,\sin(x/2)\right)\mathrm{e}^{\frac{\sqrt{}}{}}\right.$$

2.1581 ODE No. 1581

$$-axy(x) - b + y^{(5)}(x) = 0$$

✗ **Mathematica** : cpu = 0.180434 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \text{DifferentialRoot}\left(\{y,x\},\left\{-b - xay(x) + y^{(5)}(x) = 0, y(0) = c_1, y'(0) = c_2, y''(0) = c_3, y^{(3)}(0) = c_4, y^{(}\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(diff(diff(diff(y(x),x),x),x),x),x)-a*x*y(x)-b=0,y(x))
```

2.1582 ODE No. 1582

$$a\nu x^{\nu-1}y(x) + ax^{\nu}y'(x) + y^{(5)}(x) = 0$$

✓ **Mathematica** : cpu = 0.647854 (sec), leaf count = 787

$$\left\{\left\{y(x) \to c_5\left(\frac{4}{\nu}+1\right)^{-\frac{16}{\nu+4}} \nu^{-\frac{16}{\nu+4}} a^{\frac{4}{\nu+4}} (x^{\nu})^{\frac{4\left(\frac{4}{\nu}+1\right)}{\nu+4}} \, {}_1F_4\left(\frac{4}{\nu\left(1+\frac{4}{\nu}\right)} + \frac{1}{1+\frac{4}{\nu}}; 1 + \frac{1}{\left(1+\frac{4}{\nu}\right)\nu}, 1 + \frac{2}{\left(1+\frac{4}{\nu}\right)\nu}, 1 + \frac{}{(1}\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = DESol\left(\left\{\frac{\mathrm{d}^5}{\mathrm{d}x^5}\_Y(x) + ax^{\nu}\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x) + a\nu\, x^{\nu-1}\_Y(x)\right\}, \{\_Y(x)\}\right)\right\}$$

2.1583 ODE No. 1583

$$ay^{(4)}(x) - f(x) + y^{(5)}(x) = 0$$

✗ **Mathematica** : cpu = 300.036 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.03 (sec), leaf count = 40

$$\left\{y(x) = \frac{\mathrm{e}^{-ax}\_C1}{a^4} + \frac{fx^4}{24\,a} + \frac{\_C2\,x^3}{6} + \frac{\_C3\,x^2}{2} + \_C4\,x + \_C5\right\}$$

2.1584 ODE No. 1584

$$axy(x) - 5my^{(4)}(x) + xy^{(5)}(x) = 0$$

✓ **Mathematica** : cpu = 2.90613 (sec), leaf count = 216

$$\left\{\left\{y(x) \to c_5 5^{-5m-4} a^{\frac{1}{5}(5m+4)} x^{5m+4}\, {}_0F_4\left(;m+\frac{6}{5},m+\frac{7}{5},m+\frac{8}{5},m+\frac{9}{5};-\frac{ax^5}{3125}\right) + \frac{1}{125}a^{3/5}c_4 x^3\, {}_0F_4\left(;\frac{6}{5},\frac{7}{5},\frac{8}{5},\right.\right.$$

✓ **Maple** : cpu = 0.274 (sec), leaf count = 118

$$\left\{y(x) = \_C1\, {}_0\mathrm{F}_4(\,;\frac{2}{5},\frac{3}{5},\frac{4}{5},\frac{1}{5}-m;-\frac{x^5 a}{3125}) + \_C2\, x\, {}_0\mathrm{F}_4(\,;\frac{3}{5},\frac{4}{5},\frac{6}{5},\frac{2}{5}-m;-\frac{x^5 a}{3125}) + \_C3\, x^2\, {}_0\mathrm{F}_4(\,;\frac{4}{5},\frac{6}{5},\frac{7}{5},\frac{3}{5}\right.$$

2.1585 ODE No. 1585

$$xy(x)\left(ay'(x) + by''(x) + cy^{(3)}(x) + ey^{(4)}(x)\right) = 0$$

✓ **Mathematica** : cpu = 0.228104 (sec), leaf count = 214

$$\left\{\{y(x) \to 0\}, \left\{y(x) \to \frac{c_1 e^{x\mathrm{Root}\left[\#1^3+\frac{\#1^2 c}{e}+\frac{\#1 b}{e}+\frac{a}{e}\&,1\right]}}{\mathrm{Root}\left[\#1^3+\frac{\#1^2 c}{e}+\frac{\#1 b}{e}+\frac{a}{e}\&,1\right]} + \frac{c_2 e^{x\mathrm{Root}\left[\#1^3+\frac{\#1^2 c}{e}+\frac{\#1 b}{e}+\frac{a}{e}\&,2\right]}}{\mathrm{Root}\left[\#1^3+\frac{\#1^2 c}{e}+\frac{\#1 b}{e}+\frac{a}{e}\&,2\right]} + \frac{c_3 e^{x\mathrm{Root}\left[\#\right.}}{\mathrm{Root}\left[\#1^3+\right.}\right.\right.$$

✓ **Maple** : cpu = 0.032 (sec), leaf count = 679

$$\left\{y(x) = 0, y(x) = \_C4\, \mathrm{e}^{\frac{x}{6e}\left(\left(12\sqrt{3}\sqrt{27a^2e^2+(-18abc+4b^3)e+4c^3a-b^2c^2}e-108ae^2+36bce-8c^3\right)^{\frac{2}{3}}-2c\sqrt[3]{12\sqrt{3}\sqrt{27a^2e^2+(-18abc}\right.}\right.$$

2.1586 ODE No. 1586

$$-y^{(4)}(x)(x(aA(5)-A(4))+A(5))-y^{(3)}(x)(x(aA(4)-A(3))+A(4))-(x(aA(3)-A(2))+A(3))y''(x)-(x(aA(2)-A(1$$

✗ **Mathematica** : cpu = 44.9874 (sec), leaf count = 0 , DifferentialRoot result

$$\left\{\left\{y(x) \to \mathrm{DifferentialRoot}\left(\{y,x\},\left\{xA(0)-xaA(1)-A(1)+(xA(1)-xaA(2)-A(2))y'(x)+(xA(2)-xaA(\right.\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x) = \int DESol\left(\left\{-\frac{(axA_2 - xA_1 + A_2)\_Y(x)}{x} - \frac{(axA_3 - xA_2 + A_3)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)}{x} - \frac{(axA_4 - xA_3 + A_4)\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_\right.\right.\right.$$

2.1587 ODE No. 1587

$$x^5 y^{(10)}(x) - a y(x) = 0$$

✓ **Mathematica** : cpu = 0.377199 (sec), leaf count = 492

$$\left\{\left\{y(x) \to \frac{(-1)^{4/5} a^{9/5} c_1 x^9 \, {}_0F_9\left(;\frac{6}{5},\frac{7}{5},\frac{8}{5},\frac{9}{5},2,\frac{11}{5},\frac{12}{5},\frac{13}{5},\frac{14}{5};\frac{a x^5}{9765625}\right)}{3814697265625} + \frac{(-1)^{3/5} a^{8/5} c_3 x^8 \, {}_0F_9\left(;\frac{4}{5},\frac{6}{5},\frac{7}{5},\frac{8}{5},\frac{9}{5},2,\frac{11}{5},\right.}{152587890625}\right.$$

✓ **Maple** : cpu = 0.556 (sec), leaf count = 174

$$\left\{y(x) = x^{\frac{5}{2}}\left(\_C3\, I_5\left(2\,\mathrm{e}^{i/5\pi} a^{1/10}\sqrt{x}\right) + \_C6\, I_5\left(2\,\mathrm{e}^{4/5\,i\pi} a^{1/10}\sqrt{x}\right) + \_C2\, Y_5\left(2\,i a^{\frac{1}{10}}\sqrt{x}\right) + \_C10\, Y_5\left(2\,i\mathrm{e}^{\frac{4\,i}{5}\pi} a^{\frac{1}{10}}\right.\right.\right.$$

2.1588 ODE No. 1588

$$x^{10} y^{(5)}(x) - a y(x) = 0$$

✓ **Mathematica** : cpu = 6.22292 (sec), leaf count = 114

$$\left\{\left\{y(x) \to c_1 x^4 e^{-\frac{\sqrt[5]{a}}{x}} + c_2 x^4 e^{\frac{\sqrt[5]{-1}\,\sqrt[5]{a}}{x}} + c_3 x^4 e^{-\frac{(-1)^{2/5}\,\sqrt[5]{a}}{x}} + c_4 x^4 e^{\frac{(-1)^{3/5}\,\sqrt[5]{a}}{x}} + c_5 x^4 e^{-\frac{(-1)^{4/5}\,\sqrt[5]{a}}{x}}\right\}\right\}$$

✓ **Maple** : cpu = 0.151 (sec), leaf count = 90

$$\left\{y(x) = \_C1\, {}_0\mathrm{F}_4(\,;\frac{6}{5},\frac{7}{5},\frac{8}{5},\frac{9}{5};-\frac{a}{3125\,x^5}) + \_C2\, x\, {}_0\mathrm{F}_4(\,;\frac{4}{5},\frac{6}{5},\frac{7}{5},\frac{8}{5};-\frac{a}{3125\,x^5}) + \_C3\, x^2\, {}_0\mathrm{F}_4(\,;\frac{3}{5},\frac{4}{5},\frac{6}{5},\frac{7}{5};-\right.$$

2.1589 ODE No. 1589

$$x^{11/2} y^{(11)}(x) - a y(x) = 0$$

✓ **Mathematica** : cpu = 0.0519046 (sec), leaf count = 670

$$\left\{\left\{y(x) \to \frac{4}{121}(-1)^{2/11} a^{2/11} c_2 x \, {}_0F_{10}\left(;-\frac{7}{11},-\frac{5}{11},-\frac{3}{11},-\frac{1}{11},\frac{1}{11},\frac{3}{11},\frac{5}{11},\frac{7}{11},\frac{9}{11},\frac{13}{11};\frac{2048 a x^{11/2}}{285311670611}\right) - \frac{10485}{}\right.\right.$$

✓ **Maple** : cpu = 9.116 (sec), leaf count = 4339

2.1590 ODE No. 1590

$$(x-a)^5(x-b)^5y^{(5)}(x)-cy(x)=0$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 2.786 (sec), leaf count = 553

$$\left\{y(x)=ODESolStruc\left(e^{\int -4\frac{\_g(\_f)\left((-b-\_f/4)e^{\left(\int \_g(\_f)\,d\_f+\_C1\right)(a-b)}+a+\_f/4\right)}{e^{\left(\int \_g(\_f)\,d\_f+\_C1\right)(a-b)}-1}d\_f+\_C2},[\left\{\frac{1}{(\_g(\_f))^2}\left(\left(\frac{d^3}{d\_f^3}\_g(\_f)\right.\right.\right.\right.$$

2.1591 ODE No. 1591

$$y''(x)-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0652338 (sec), leaf count = 26

$$\left\{\left\{y(x)\to\sqrt[3]{6}\wp\left(\frac{x+c_1}{\sqrt[3]{6}};0,c_2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.017 (sec), leaf count = 12

$$\{y(x)=6\,WeierstrassP(x+\_C1,0,\_C2)\}$$

2.1592 ODE No. 1592

$$y''(x)-6y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0317736 (sec), leaf count = 14

$$\{\{y(x)\to\wp(x+c_1;0,c_2)\}\}$$

✓ **Maple** : cpu = 0.013 (sec), leaf count = 10

$$\{y(x)=WeierstrassP(x+\_C1,0,\_C2)\}$$

2.1593 ODE No. 1593

$$y''(x) - 6y(x)^2 - x = 0$$

✗ **Mathematica** : cpu = 0.179248 (sec), leaf count = 0 , could not solve

```
DSolve[-x - 6*y[x]^2 + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)-6*y(x)^2-x=0,y(x))
```

2.1594 ODE No. 1594

$$y''(x) - 6y(x)^2 + 4y(x) = 0$$

✓ **Mathematica** : cpu = 0.369277 (sec), leaf count = 373

$$\text{Solve}\left[\frac{4\left(\text{Root}\left[4\#1^3-4\#1^2+c_1\&,2\right]-\text{Root}\left[4\#1^3-4\#1^2+c_1\&,3\right]\right)\left(y(x)-\text{Root}\left[4\#1^3-4\#1^2+c_1\&,1\right]\right)(}{\left(c_1+4y(x)^3-4y(x)^2\right)\left(\text{Root}\left[4\#1^3\right.\right.}\right.$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 59

$$\left\{\int^{y(x)}\frac{1}{\sqrt{4\_a^3-4\_a^2+\_C1}}d\_a-x-\_C2=0,\int^{y(x)}-\frac{1}{\sqrt{4\_a^3-4\_a^2+\_C1}}d\_a-x-\_C2=0\right\}$$

2.1595 ODE No. 1595

$$ay(x)^2 + bx + c + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.368615 (sec), leaf count = 0 , could not solve

```
DSolve[c + b*x + a*y[x]^2 + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+a*y(x)^2+b*x+c=0,y(x))
```

2.1596 ODE No. 1596

$$a + y''(x) - 2y(x)^3 - xy(x) = 0$$

✗ **Mathematica** : cpu = 1.1916 (sec), leaf count = 0 , could not solve

```
DSolve[a - x*y[x] - 2*y[x]^3 + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)-2*y(x)^3-x*y(x)+a=0,y(x))
```

2.1597 ODE No. 1597

$$y''(x) - ay(x)^3 = 0$$

✓ **Mathematica** : cpu = 2.40585 (sec), leaf count = 242

$$\left\{\left\{y(x) \to -\frac{\sqrt[4]{2}\sqrt{c_1}\sqrt{\frac{i\sqrt{a}}{\sqrt{c_1}}}\text{sn}\left(\left.\frac{(-1)^{3/4}\sqrt{\sqrt{2}\sqrt{a}\sqrt{c_1}x^2+2\sqrt{2}\sqrt{a}\sqrt{c_1}c_2x+\sqrt{2}\sqrt{a}\sqrt{c_1}c_2^2}}{\sqrt{2}}\right|-1\right)}{\sqrt{a}}\right\},\left\{y(x) \to \frac{\sqrt[4]{2}\sqrt{c_1}\sqrt{\frac{i\sqrt{a}}{\sqrt{c_1}}}\text{sn}\left(\right.\right.\right.$$

✓ **Maple** : cpu = 0.026 (sec), leaf count = 21

$$\left\{y(x) = \_C2\ JacobiSN\left(\left(\frac{x}{2}\sqrt{-2\,a} + \_C1\right)\_C2, i\right)\right\}$$

2.1598 ODE No. 1598

$$-2a^2y(x)^3 + 2abxy(x) - b + y''(x) = 0$$

✗ **Mathematica** : cpu = 3.81814 (sec), leaf count = 0 , could not solve

```
DSolve[-b + 2*a*b*x*y[x] - 2*a^2*y[x]^3 + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)-2*a^2*y(x)^3+2*a*b*x*y(x)-b=0,y(x))
```

2.1599 ODE No. 1599

$$ay(x)^3 + bxy(x) + cy(x) + d + y''(x) = 0$$

✗ **Mathematica** : cpu = 3.66485 (sec), leaf count = 0 , could not solve

```
DSolve[d + c*y[x] + b*x*y[x] + a*y[x]^3 + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+d+b*x*y(x)+c*y(x)+a*y(x)^3=0,y(x))
```

2.1600 ODE No. 1600

$$ay(x)^3 + by(x)^2 + cy(x) + d + y''(x) = 0$$

✓ **Mathematica** : cpu = 2.24601 (sec), leaf count = 1017

$$\text{Solve}\left[\frac{4F\left(\sin^{-1}\left(\sqrt{\frac{(\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,2]-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,4])(y(x)-\text{Root}[3a\#1}{(\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,1]-\text{Root}[3a\#1^4+4b\#1^3+6c\#1^2+12d\#1-6c_1\&,4])(y(x)-\text{Root}[3a\#1}\right)\right.\right.\right.$$

✓ **Maple** : cpu = 0.097 (sec), leaf count = 89

$$\left\{\int^{y(x)} -6\,\frac{1}{\sqrt{-18\,a\_a^4-24\,b\_a^3-36\,c\_a^2-72\,d\_a+36\,\_C1}}d\_a - x - \_C2 = 0, \int^{y(x)} 6\,\frac{}{\sqrt{-18\,a\_a^4-24\,b}}\right.$$

2.1601 ODE No. 1601

$$ax^r y(x)^n + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.0411011 (sec), leaf count = 0 , could not solve

```
DSolve[a*x^r*y[x]^n + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 3.115 (sec), leaf count = 151

$$\left\{y(x) = ODESolStruc\left(\_a\,e^{\int -b(\_a)\,d\_a+\_C1}, [\left\{\frac{d}{d\_a}\_b(\_a) = \frac{\left(a\_b(\_a)\,(n-1)^2\,\_a^n + (r+2)\,(\_a\,(r+1+\right.\right.\right.\right.$$

2.1602 ODE No. 1602

$$(n+1)a^{2n}y(x)^{2n+1}+y''(x)-y(x)=0$$

✓ **Mathematica** : cpu = 87.9984 (sec), leaf count = 46

$$\text{Solve}\left[\left(\int_1^{y(x)}\frac{1}{\sqrt{c_1-K[1]^2\left(a^{2n}K[1]^{2n}-1\right)}}\,dK[1]\right)^2=(c_2+x)^2,y(x)\right]$$

✓ **Maple** : cpu = 0.244 (sec), leaf count = 73

$$\left\{\int^{y(x)}\frac{1}{\sqrt{-a^{2\,n}\_a^{2\,n+2}+\_a^2+\_C1}}d\_a-x-\_C2=0,\int^{y(x)}-\frac{1}{\sqrt{-a^{2\,n}\_a^{2\,n+2}+\_a^2+\_C1}}d\_a-x-\_C\right.$$

2.1603 ODE No. 1603

$$y''(x)-\frac{1}{\left(ay(x)^2+bxy(x)+cx^2+dy(x)+ex+k\right)^{3/2}}=0$$

✗ **Mathematica** : cpu = 60.6976 (sec), leaf count = 0 , could not solve

```
DSolve[-(k + e*x + c*x^2 + d*y[x] + b*x*y[x] + a*y[x]^2)^(-3/2) + Derivative[2][y][x] == 0,
```

✓ **Maple** : cpu = 71.214 (sec), leaf count = 8411

2.1604 ODE No. 1604

$$y''(x)-e^{y(x)}=0$$

✓ **Mathematica** : cpu = 0.0966643 (sec), leaf count = 34

$$\left\{\left\{y(x)\to\log\left(\frac{1}{2}c_1\left(\tanh^2\left(\frac{1}{2}\sqrt{c_1\,(c_2+x)^2}\right)-1\right)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.353 (sec), leaf count = 23

$$\left\{y(x)=\ln\left(\frac{1}{2\_C1^2}\left(\left(\tan\left(\frac{\_C2+x}{2\_C1}\right)\right)^2+1\right)\right)\right\}$$

2.1605 ODE No. 1605

$$ae^x \sqrt{y(x)} + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.513181 (sec), leaf count = 0 , could not solve

```
DSolve[a*E^x*Sqrt[y[x]] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.309 (sec), leaf count = 104

$$\left\{y(x) = ODESolStruc\left(\frac{\_a}{\mathrm{e}^{-2\int \_b(\_a)\,\mathrm{d}\_a - 2\_C1}}, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = (\_b(\_a))^2 (\_b(\_a)\sqrt{\_a}a + 4\_a\,\_b(\_a) + 4)\right.\right.$$

2.1606 ODE No. 1606

$$y''(x) + e^x \sin(y(x)) = 0$$

✗ **Mathematica** : cpu = 1.11676 (sec), leaf count = 0 , could not solve

```
DSolve[E^x*Sin[y[x]] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+exp(x)*sin(y(x))=0,y(x))
```

2.1607 ODE No. 1607

$$a \sin(y(x)) + y''(x) = 0$$

✓ **Mathematica** : cpu = 0.171714 (sec), leaf count = 79

$$\left\{\left\{y(x) \to -2\mathrm{am}\left(\frac{1}{2}\sqrt{(2a + c_1)\,(x + c_2)^{\,2}}|\frac{4a}{2a + c_1}\right)\right\}, \left\{y(x) \to 2\mathrm{am}\left(\frac{1}{2}\sqrt{(2a + c_1)\,(x + c_2)^{\,2}}|\frac{4a}{2a + c_1}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.122 (sec), leaf count = 49

$$\left\{\int^{y(x)} \frac{1}{\sqrt{2\,a\cos(\_a) + \_C1}} d\_a - x - \_C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{2\,a\cos(\_a) + \_C1}} d\_a - x - \_C2 = 0\right\}$$

2.1608 ODE No. 1608

$$a^2 \sin(y(x)) - b \sin(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.052967 (sec), leaf count = 0 , could not solve

```
DSolve[-(b*Sin[x]) + a^2*Sin[y[x]] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+a^2*sin(y(x))-b*sin(x)=0,y(x))
```

2.1609 ODE No. 1609

$$a^2 \sin(y(x)) - bf(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.0361756 (sec), leaf count = 0 , could not solve

```
DSolve[-(b*f[x]) + a^2*Sin[y[x]] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+a^2*sin(y(x))-b*f(x)=0,y(x))
```

2.1610 ODE No. 1610

$$y''(x) - \frac{h\left(\frac{y(x)}{\sqrt{x}}\right)}{x^{3/2}} = 0$$

✗ **Mathematica** : cpu = 300.166 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.295 (sec), leaf count = 92

$$\left\{ y(x) = RootOf\left(-\ln(x) - 2 \int^{\_Z} \frac{1}{\sqrt{\_C1 + 8 \int h(\_g)\, \mathrm{d}\_g + \_g^2}} d\_g + 2\,\_C2 \right) \sqrt{x}, y(x) = RootOf\left(-\ln(x \right.$$

2.1611 ODE No. 1611

$$y''(x) - 3y'(x) - y(x)^2 - 2y(x) = 0$$

✗ **Mathematica** : cpu = 5.38845 (sec), leaf count = 0 , could not solve

```
DSolve[-2*y[x] - y[x]^2 - 3*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.529 (sec), leaf count = 57

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) - 3\_b(\_a) - \_a^2 - 2\_a = 0\right\}, \left\{\_a = y(x), \_b(\_a) =\right.\right.$$

2.1612 ODE No. 1612

$$y''(x) - 7y'(x) - y(x)^{3/2} + 12y(x) = 0$$

✗ **Mathematica** : cpu = 22.2722 (sec), leaf count = 0 , could not solve

```
DSolve[12*y[x] - y[x]^(3/2) - 7*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.318 (sec), leaf count = 57

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) - 7\_b(\_a) - \_a^{\frac{3}{2}} + 12\_a = 0\right\}, \left\{\_a = y(x), \_b(\_a)\right.\right.$$

2.1613 ODE No. 1613

$$6a^2y(x) + 5ay'(x) + y''(x) - 6y(x)^2 = 0$$

✗ **Mathematica** : cpu = 2.20026 (sec), leaf count = 0 , could not solve

```
DSolve[6*a^2*y[x] - 6*y[x]^2 + 5*a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.023 (sec), leaf count = 27

$$\left\{y(x) = WeierstrassP\left(-\frac{\mathrm{e}^{-ax}}{a} + \_C1, 0, \_C2\right)\left(\mathrm{e}^{-ax}\right)^2\right\}$$

2.1614 ODE No. 1614

$$2a^2y(x)+3ay'(x)+y''(x)-2y(x)^3=0$$

✗ **Mathematica** : cpu = 1.49149 (sec), leaf count = 0 , could not solve

```
DSolve[2*a^2*y[x] - 2*y[x]^3 + 3*a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.066 (sec), leaf count = 33

$$\left\{y(x)=\frac{\_C2}{\mathrm{e}^{ax}}JacobiSN\left(\left(-\frac{1}{a}\sqrt{-\mathrm{e}^{-2\,ax}}+\_C1\right)\_C2,i\right)\right\}$$

2.1615 ODE No. 1615

$$-\frac{2(n+1)(n+2)y(x)\left(y(x)^{\frac{n}{n+1}}-1\right)}{n^2}-\frac{(3n+4)y'(x)}{n}+y''(x)=0$$

✗ **Mathematica** : cpu = 119.567 (sec), leaf count = 0 , could not solve

```
DSolve[(-2*(1 + n)*(2 + n)*y[x]*(-1 + y[x]^(n/(1 + n))))/n^2 - ((4 + 3*n)*Derivative[1][y][x
```

✓ **Maple** : cpu = 4.878 (sec), leaf count = 91

$$\left\{y(x)=ODESolStruc\left(\_a,[\left\{\frac{1}{n^2}\left(-2\,(n+2)\,(n+1)\,\_a\,\_a^{\frac{n}{n+1}}+\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a)\,n^2+\left(-3\,n^2-4\,n\right)\_\right.\right.\right.$$

2.1616 ODE No. 1616

$$\frac{1}{4}\left(a^2-1\right)y(x)+ay'(x)+by(x)^n+y''(x)=0$$

✗ **Mathematica** : cpu = 26.5188 (sec), leaf count = 0 , could not solve

```
DSolve[((-1 + a^2)*y[x])/4 + b*y[x]^n + a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[
```

✓ **Maple** : cpu = 1.356 (sec), leaf count = 63

$$\left\{y(x)=ODESolStruc\left(\_a,[\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a)+a\_b(\_a)+b\_a^n+\frac{\_a\,a^2}{4}-\frac{\_a}{4}=0\right\},\left\{\_a=y(x),\_\right.\right.\right.$$

2.1617 ODE No. 1617

$$ay'(x) + bx^r y(x)^n + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.0464304 (sec), leaf count = 0 , could not solve

```
DSolve[b*x^r*y[x]^n + a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+a*diff(y(x),x)+b*x^r*y(x)^n=0,y(x))
```

2.1618 ODE No. 1618

$$ay'(x) - 2a + be^{y(x)} + y''(x) = 0$$

✗ **Mathematica** : cpu = 30.7938 (sec), leaf count = 0 , could not solve

```
DSolve[-2*a + b*E^y[x] + a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.736 (sec), leaf count = 56

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + a\_b(\_a) + be^{-a} - 2a = 0\right\}, \left\{\_a = y(x), \_b(\_a) =\right.\right.$$

2.1619 ODE No. 1619

$$ay'(x) + f(x)\sin(y(x)) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.0585628 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*Sin[y[x]] + a*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+a*diff(y(x),x)+f(x)*sin(y(x))=0,y(x))
```

2.1620 ODE No. 1620

$$y''(x) + y(x)y'(x) - y(x)^3 = 0$$

✗ **Mathematica** : cpu = 122.304 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^3 + y[x]*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.125 (sec), leaf count = 253

$$\left\{\int^{y(x)} \left(\frac{\_a^2}{2} + \frac{1}{2}\left(\sqrt[3]{\_C1 + \sqrt{\_a^6 + \_C1^2}} - \_a^2 \frac{1}{\sqrt[3]{\_C1 + \sqrt{\_a^6 + \_C1^2}}}\right)^2\right)^{-1} d\_a - x - \_C2 = 0, \int^{y(}\right.$$

2.1621 ODE No. 1621

$$ay(x) + y''(x) + y(x)y'(x) - y(x)^3 = 0$$

✗ **Mathematica** : cpu = 100.133 (sec), leaf count = 0 , could not solve

```
DSolve[a*y[x] - y[x]^3 + y[x]*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.625 (sec), leaf count = 1088

$$\left\{ \int^{y(x)} \frac{1}{-63\_a^2 + 63a} \left(\frac{\left(-\frac{1}{2} + \frac{i}{2}\sqrt{3}\right)^3}{2} \left(126 \frac{1}{-\_a^6 + 3a\_a^4 - 3\_a^2 a^2 + 80\_C1^3 + a^3} \sqrt[3]{-4 \left(\_C1\sqrt{5}\sqrt{\frac{}{-\_}} \right.} \right.\right.\right.$$

2.1622 ODE No. 1622

$$2a^2 y(x) + (3a + y(x))y'(x) + ay(x)^2 + y''(x) - y(x)^3 = 0$$

✗ **Mathematica** : cpu = 26.2993 (sec), leaf count = 0 , could not solve

```
DSolve[2*a^2*y[x] + a*y[x]^2 - y[x]^3 + (3*a + y[x])*Derivative[1][y][x] + Derivative[2][y][
```

✓ **Maple** : cpu = 0.527 (sec), leaf count = 817

$$\left\{ y(x) = \frac{1}{\mathrm{e}^{ax}} RootOf\left(\int^{\_Z} \frac{1}{-\_f^6 + \_C1^2} \left(-\left(-1\left(-\_C1\,\_f^{12} + 2\_C1^3\_f^6 + \left(-\_f^6 + \_C1^2\right)^{\frac{5}{2}} - \_C1^5 \right) \right.\right.\right.\right. (-$$

2.1623 ODE No. 1623

$$y(x)\left(f'(x) + 2f(x)^2\right) + (3f(x) + y(x))y'(x) + f(x)y(x)^2 + y''(x) - y(x)^3 = 0$$

✗ **Mathematica** : cpu = 0.45463 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x]^2 - y[x]^3 + y[x]*(2*f[x]^2 + Derivative[1][f][x]) + (3*f[x] + y[x])*Deriva
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+(y(x)+3*f(x))*diff(y(x),x)-y(x)^3+f(x)*y(x)^2+y(x)*(diff(f(x),x)
```

2.1624 ODE No. 1624

$$y(x)\left(af(x)^2-\frac{f''(x)}{f(x)}+3f'(x)+\frac{3f'(x)^2}{f(x)^2}\right)+bf(x)^3-\left(\frac{f'(x)}{f(x)}+f(x)\right)\left(3y'(x)+y(x)^2\right)+y''(x)+y(x)y'(x)-y(x)^3$$

✗ **Mathematica** : cpu = 1.51269 (sec), leaf count = 0 , could not solve

```
DSolve[b*f[x]^3 - y[x]^3 + y[x]*Derivative[1][y][x] - (f[x] + Derivative[1][f][x]/f[x])*(y[x
```

✓ **Maple** : cpu = 2. (sec), leaf count = 131

$$\left\{y(x)=ODESolStruc\left(f\left(RootOf\left(\int \_b(\_a)\ \mathrm{d}\_a+\_C1-\int^{\_Z} f(\_f)\,d\_f\right)\right)\_a,[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=(\_b(\_a\right.\right.$$

2.1625 ODE No. 1625

$$y'(x)\left(y(x)-\frac{3f'(x)}{2f(x)}\right)-\frac{y(x)^2f'(x)}{2f(x)}+y(x)\left(-\frac{f''(x)}{2f(x)}+\frac{f'(x)^2}{f(x)^2}+f(x)\right)+y''(x)-y(x)^3=0$$

✗ **Mathematica** : cpu = 0.981117 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^3 - (y[x]^2*Derivative[1][f][x])/(2*f[x]) + (y[x] - (3*Derivative[1][f][x])/(2*
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+(y(x)-3/2*diff(f(x),x)/f(x))*diff(y(x),x)-y(x)^3-1/2*diff(f(x),x
diff(diff(f(x),x),x))/f(x)*y(x)=0,y(x))
```

2.1626 ODE No. 1626

$$y(x)f'(x)+f(x)y'(x)+y''(x)+2y(x)y'(x)=0$$

✗ **Mathematica** : cpu = 39.7922 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*Derivative[1][f][x] + f[x]*Derivative[1][y][x] + 2*y[x]*Derivative[1][y][x] + De
```

✓ **Maple** : cpu = 0.232 (sec), leaf count = 48

$$\left\{y(x)=ODESolStruc\left(\_b(\_a),[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=-f(\_a)\,\_b(\_a)-(\_b(\_a))^2-\_C1\right\},\{\_a=x,\_b(\_a)=\right.\right.$$

2.1627 ODE No. 1627

$$f(x)\left(y'(x)+y(x)^2\right)-g(x)+y''(x)+2y(x)y'(x)=0$$

✗ **Mathematica** : cpu = 0.299074 (sec), leaf count = 0 , could not solve

```
DSolve[-g[x] + 2*y[x]*Derivative[1][y][x] + f[x]*(y[x]^2 + Derivative[1][y][x]) + Derivative
```

✓ **Maple** : cpu = 0.961 (sec), leaf count = 58

$$\left\{y(x)=ODESolStruc\left(\_b(\_a),\left[\left\{-\int \mathrm{e}^{\int f(\_a)\,\mathrm{d}\_a}g(\_a)\,\mathrm{d}\_a+\left((\_b(\_a))^2+\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\mathrm{e}^{\int f(\_a)\,\mathrm{d}\_a}+\_C\right.\right.\right.$$

2.1628 ODE No. 1628

$$f(x)y(x)-g(x)+y''(x)+3y(x)y'(x)+y(x)^3=0$$

✗ **Mathematica** : cpu = 7.7246 (sec), leaf count = 0 , could not solve

```
DSolve[-g[x] + f[x]*y[x] + y[x]^3 + 3*y[x]*Derivative[1][y][x] + Derivative[2][y][x] == 0, y
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{y(x)=\frac{\frac{\mathrm{d}}{\mathrm{d}x}DESol\left(\left\{-g(x)\_Y(x)+f(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y(x)\right\},\{\_Y(x)\}\right)}{DESol\left(\left\{-g\left(x\right)\_Y\left(x\right)+f\left(x\right)\frac{\mathrm{d}}{\mathrm{d}x}\_Y\left(x\right)+\frac{\mathrm{d}^3}{\mathrm{d}x^3}\_Y\left(x\right)\right\},\{\_Y\left(x\right)\}\right)}\right\}$$

2.1629 ODE No. 1629

$$(f(x)+3y(x))y'(x)+f(x)y(x)^2+y''(x)+y(x)^3=0$$

✗ **Mathematica** : cpu = 0.0376241 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x]^2 + y[x]^3 + (f[x] + 3*y[x])*Derivative[1][y][x] + Derivative[2][y][x] == 0
```

✓ **Maple** : cpu = 0.039 (sec), leaf count = 38

$$\left\{y(x)=\frac{\int \_C1\,\mathrm{e}^{-\int f(x)\,\mathrm{d}x}\,\mathrm{d}x+\_C2}{\iint \_C1\,\mathrm{e}^{-\int f(x)\,\mathrm{d}x}\,\mathrm{d}x\,\mathrm{d}x+\_C2\,x+1}\right\}$$

2.1630 ODE No. 1630

$$-4a^2y(x) - 3ay(x)^2 - b + y''(x) - 3y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 11.0998 (sec), leaf count = 3227

$$\left\{\left\{y(x) \to -\frac{2\left((-1)^{\frac{a^{3/2}\sqrt{4a^3-3b}-2a^3}{4a^3}+1}2^{-\frac{3\left(a^{3/2}\sqrt{4a^3-3b}-2a^3\right)}{4a^3}+\frac{3\sqrt{4a^6-3a^3b}}{4a^3}+1}3^{\frac{a^{3/2}\sqrt{4a^3-3b}-2a^3}{4a^3}-\frac{\sqrt{4a^6-3a^3b}}{4a^3}}a^{-\frac{a^{3/2}\sqrt{4a^3-3b}-2}{2a^3}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.625 (sec), leaf count = 783

$$\left\{\int^{y(x)} -6\,a^2\left(-12\_a\,a^3 - 9\_a^2a^2 + \left(RootOf\left(2\,K_{1/2\,\frac{4\,a^3-3\,b}{\sqrt{4\,a^4-3\,aba}}}\left(-1/2\,\frac{\_Z}{a^2}\right)\_C1\,a^2 + 3\,K_{1/2\,\frac{4\,a^3-3\,b}{\sqrt{4\,a^4-3\,aba}}}\left(-1/2\right.\right.\right.\right.\right.$$

2.1631 ODE No. 1631

$$-(f(x) + 3y(x))y'(x) + f(x)y(x)^2 + y''(x) + y(x)^3 = 0$$

✗ **Mathematica** : cpu = 0.0323435 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x]^2 + y[x]^3 - (f[x] + 3*y[x])*Derivative[1][y][x] + Derivative[2][y][x] == 0
```

✓ **Maple** : cpu = 0.049 (sec), leaf count = 38

$$\left\{y(x) = \frac{-\int \_C1\,\mathrm{e}^{\int f(x)\,\mathrm{d}x}\,\mathrm{d}x - \_C2}{\iint \_C1\,\mathrm{e}^{\int f(x)\,\mathrm{d}x}\,\mathrm{d}x\,\mathrm{d}x + \_C2\,x + 1}\right\}$$

2.1632 ODE No. 1632

$$y''(x) - 2ay(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0624547 (sec), leaf count = 46

$$\left\{\left\{y(x) \to \frac{\sqrt{c_1}\tan\left(\sqrt{a}\sqrt{c_1}x + \sqrt{a}\sqrt{c_1}c_2\right)}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.095 (sec), leaf count = 23

$$\left\{y(x) = \frac{1}{a}\tan\left(\sqrt{a\_C1}\left(\_C2 + x\right)\right)\sqrt{a\_C1}\right\}$$

2.1633 ODE No. 1633

$$ay(x)y'(x) + by(x)^3 + y''(x) = 0$$

✗ **Mathematica** : cpu = 39.0208 (sec), leaf count = 0 , could not solve

```
DSolve[b*y[x]^3 + a*y[x]*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.279 (sec), leaf count = 97

$$\left\{ \int^{y(x)} \left(RootOf\left(-2\,a\_a^2 Artanh\left(\frac{\_a^2 a + 4\,\_Z}{\sqrt{\_a^4\,(a^2 - 8\,b)}} \right) + \_C1\,\sqrt{\_a^4\,(a^2 - 8\,b)} - \ln\left(\_a^4 b + \_Z\,\_a^2 a + 2\,\_Z^2\right) \right.\right.$$

2.1634 ODE No. 1634

$$y'(x)h(x, y(x)) + j(x, y(x)) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.156505 (sec), leaf count = 0 , could not solve

```
DSolve[j[x, y[x]] + h[x, y[x]]*Derivative[1][y][x] + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+h(x,y(x))*diff(y(x),x)+j(x,y(x))=0,y(x))
```

2.1635 ODE No. 1635

$$ay'(x)^2 + by(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 101.488 (sec), leaf count = 0 , could not solve

```
DSolve[b*y[x] + a*Derivative[1][y][x]^2 + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.178 (sec), leaf count = 79

$$\left\{ \int^{y(x)} -2\,\frac{a}{\sqrt{4\,\mathrm{e}^{-2\,a\_a}\,\_C1\,a^2 - 4\,\_a\,ab + 2\,b}}\,d\_a - x - \_C2 = 0, \int^{y(x)} 2\,\frac{a}{\sqrt{4\,\mathrm{e}^{-2\,a\_a}\,\_C1\,a^2 - 4\,\_a\,ab + 2\,b}}\,d\_a \right.$$

2.1636 ODE No. 1636

$$ay'(x)\left|y'(x)\right| + by'(x) + cy(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 36.7426 (sec), leaf count = 0 , could not solve

```
DSolve[c*y[x] + b*Derivative[1][y][x] + a*Abs[Derivative[1][y][x]]*Derivative[1][y][x] + Der
```

✓ **Maple** : cpu = 0.89 (sec), leaf count = 59

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + a\_b(\_a)\left|\_b(\_a)\right| + \_b(\_a)\,b + c\_a = 0\right\}, \left\{\_a = y(\right.\right.$$

2.1637 ODE No. 1637

$$ay'(x)^2 + by'(x) + cy(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 29.9891 (sec), leaf count = 0 , could not solve

```
DSolve[c*y[x] + b*Derivative[1][y][x] + a*Derivative[1][y][x]^2 + Derivative[2][y][x] == 0,
```

✓ **Maple** : cpu = 0.554 (sec), leaf count = 58

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + a(\_b(\_a))^2 + \_b(\_a)\,b + c\_a = 0\right\}, \left\{\_a = y(x), \_b\right.\right.$$

2.1638 ODE No. 1638

$$ay'(x)^2 + b\sin(y(x)) + y''(x) = 0$$

✗ **Mathematica** : cpu = 100.115 (sec), leaf count = 0 , could not solve

```
DSolve[b*Sin[y[x]] + a*Derivative[1][y][x]^2 + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.192 (sec), leaf count = 115

$$\left\{\int^{y(x)} (-4\,a^2 - 1)\frac{1}{\sqrt{16\,\_C1\ \left(a^2 + 1/4\right)^2 \mathrm{e}^{-2\,a\_a} - 16\,b\left(a\sin\left(\_a\right) - 1/2\,\cos\left(\_a\right)\right)\left(a^2 + 1/4\right)}}d\_a - x - \_C2 =\right.$$

2.1639 ODE No. 1639

$$a y'(x) \left|y'(x)\right| + b \sin(y(x)) + y''(x) = 0$$

✗ **Mathematica** : cpu = 41.0368 (sec), leaf count = 0 , could not solve

```
DSolve[b*Sin[y[x]] + a*Abs[Derivative[1][y][x]]*Derivative[1][y][x] + Derivative[2][y][x] ==
```

✓ **Maple** : cpu = 3.636 (sec), leaf count = 56

$$\left\{y(x) = ODESolStruc\left(\_a, \left[\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + a\_b(\_a)\left|\_b(\_a)\right| + b\sin\left(\_a\right) = 0\right\}, \left\{\_a = y(x), \_b\right.\right.\right.$$

2.1640 ODE No. 1640

$$a y(x) y'(x)^2 + b y(x) + y''(x) = 0$$

✗ **Mathematica** : cpu = 200.296 (sec), leaf count = 0 , could not solve

```
DSolve[b*y[x] + a*y[x]*Derivative[1][y][x]^2 + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.191 (sec), leaf count = 70

$$\left\{\int^{y(x)} a\frac{1}{\sqrt{a\left(\mathrm{e}^{-\_a^2 a}\_C1\, a - b\right)}}d\_a - x - \_C2 = 0, \int^{y(x)} -a\frac{1}{\sqrt{a\left(\mathrm{e}^{-\_a^2 a}\_C1\, a - b\right)}}d\_a - x - \_C2 = 0\right\}$$

2.1641 ODE No. 1641

$$g(x) y'(x) + h(y(x)) y'(x)^2 + y''(x) = 0$$

✓ **Mathematica** : cpu = 1.99616 (sec), leaf count = 57

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[\int_1^{\#1} e^{-\int_1^{K[4]} -h(K[1])\,dK[1]}\,dK[4]\&\right]\left[\int_1^x c_1\left(-e^{-\int_1^{K[5]} g(K[2])\,dK[2]}\right)\,dK[5] + c_2\right]\right\}\right\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 29

$$\left\{\int^{y(x)} \mathrm{e}^{\int h(\_b)\,\mathrm{d}\_b} d\_b - \_C1 \int \mathrm{e}^{-\int g(x)\,\mathrm{d}x}\,\mathrm{d}x - \_C2 = 0\right\}$$

2.1642 ODE No. 1642

$$f(x)h(y(x)) + g(x)y'(x) - \frac{j(y(x))y'(x)^2}{h(y(x))} + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.970774 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*h[y[x]] + g[x]*Derivative[1][y][x] - (j[y[x]]*Derivative[1][y][x]^2)/h[y[x]] + D
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)-j(y(x))/h(y(x))*diff(y(x),x)^2+g(x)*diff(y(x),x)+f(x)*h(y(x))=0,
```

2.1643 ODE No. 1643

$$f(x)y'(x) + g(x)j(y(x)) + h(y(x))y'(x)^2 + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.364952 (sec), leaf count = 0 , could not solve

```
DSolve[g[x]*j[y[x]] + f[x]*Derivative[1][y][x] + h[y[x]]*Derivative[1][y][x]^2 + Derivative[
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve((1-D(j)(y(x)))/j(y(x))*diff(y(x),x)^2+f(x)*diff(y(x),x)+diff(diff(y(x),x),x)+g(x)*j(y
```

2.1644 ODE No. 1644

$$h(y(x))y'(x)^2 + j(y(x))y'(x) + k(y(x)) + y''(x) = 0$$

✗ **Mathematica** : cpu = 53.2497 (sec), leaf count = 0 , could not solve

```
DSolve[k[y[x]] + j[y[x]]*Derivative[1][y][x] + h[y[x]]*Derivative[1][y][x]^2 + Derivative[2]
```

✓ **Maple** : cpu = 0.556 (sec), leaf count = 56

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + h(\_a)\left(\_b(\_a)\right)^2 + \_b(\_a) + k(\_a) = 0\right\}, \left\{\_a = y(\right.\right.$$

2.1645 ODE No. 1645

$$\left(y'(x)^2 + 1\right)\left(y'(x)h(x, y(x)) + j(x, y(x))\right) + y''(x) = 0$$

✗ **Mathematica** : cpu = 0.147691 (sec), leaf count = 0 , could not solve

```
DSolve[(j[x, y[x]] + h[x, y[x]]*Derivative[1][y][x])*(1 + Derivative[1][y][x]^2) + Derivativ
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+(diff(y(x),x)^2+1)*(h(x,y(x))*diff(y(x),x)+j(x,y(x)))=0,y(x))
```

2.1646 ODE No. 1646

$$ay(x)\left(y'(x)^2+1\right)^2+y''(x)=0$$

✓ **Mathematica** : cpu = 10.7254 (sec), leaf count = 262

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\frac{\sqrt{\frac{\#1^2(-a)+2c_1+1}{2c_1+1}}\sqrt{2\#1^2a-4c_1}E\left(\sin^{-1}\left(\sqrt{\frac{a}{2c_1+1}}\#1\right)|1+\frac{1}{2c_1}\right)}{\sqrt{\frac{a}{2c_1+1}}\sqrt{\#1^2(-a)+2c_1+1}\sqrt{2-\frac{\#1^2a}{c_1}}}\&\right][c_2+x]\right\},\left\{\right.$$

✓ **Maple** : cpu = 0.178 (sec), leaf count = 94

$$\left\{\int^{y(x)}a(\_a^2+2\_C1)\frac{1}{\sqrt{-(-1+a(\_a^2+2\_C1))a(\_a^2+2\_C1)}}d\_a-x-\_C2=0,\int^{y(x)}-a(\_a^2+2\_\right.$$

2.1647 ODE No. 1647

$$y''(x)-a\left(xy'(x)-y(x)\right)^r=0$$

✓ **Mathematica** : cpu = 52.167 (sec), leaf count = 59

$$\left\{\left\{y(x)\to x\left(\int_1^x\left(\frac{1}{2}aK[2]^{2r}-\frac{1}{2}arK[2]^{2r}+c_1K[2]^{2r-2}\right)^{\frac{1}{1-r}}dK[2]+c_2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.461 (sec), leaf count = 60

$$\left\{y(x)=\left(\int-\frac{x^2(r-1)a-\_C1}{2x^2}2^{\frac{r}{r-1}}\left(-\left(x^2(r-1)a-\_C1\right)^{-1}\right)^{\frac{r}{r-1}}\mathrm{d}x+\_C2\right)x\right\}$$

2.1648 ODE No. 1648

$$y''(x)-kx^ay(x)^by'(x)^c=0$$

✗ **Mathematica** : cpu = 0.0801651 (sec), leaf count = 0 , could not solve

```
DSolve[-(k*x^a*y[x]^b*Derivative[1][y][x]^c) + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 2.059 (sec), leaf count = 205

$$\left\{y(x)=ODESolStruc\left(\_a\,\mathrm{e}^{\int\_b(\_a)\,\mathrm{d}\_a+\_C1},\left[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=\frac{(\_b(\_a))^2}{(a-c+2)^2}\left(-k\_a^b\_b(\_a)(b+c-1)^2\left(-\frac{(a\right.\right.\right.\right.$$

2.1649 ODE No. 1649

$$h(x,y(x))\left(y'(x)-\frac{y(x)}{x}\right)^a+y''(x)=0$$

✗ **Mathematica** : cpu = 2.67046 (sec), leaf count = 0 , could not solve

```
DSolve[h[x, y[x]]*(-(y[x]/x) + Derivative[1][y][x])^a + Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)+(diff(y(x),x)-y(x)/x)^a*h(x,y(x))=0,y(x))
```

2.1650 ODE No. 1650

$$y''(x)-a\sqrt{y'(x)^2+1}=0$$

✓ **Mathematica** : cpu = 0.0216388 (sec), leaf count = 30

$$\left\{\left\{y(x)\to\frac{\sinh(c_1)\sinh(ax)}{a}+\frac{\cosh(c_1)\cosh(ax)}{a}+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.238 (sec), leaf count = 16

$$\left\{y(x)=\frac{\cosh(a(\_C1+x))}{a}+\_C2\right\}$$

2.1651 ODE No. 1651

$$a\left(-\sqrt{y'(x)^2+1}\right)-b+y''(x)=0$$

✓ **Mathematica** : cpu = 0.263059 (sec), leaf count = 414

$$\left\{\left\{y(x)\to \frac{a\text{InverseFunction}\left[\frac{\frac{b\tan^{-1}\left(\frac{\#1 b}{\sqrt{\#1^2+1}\sqrt{a^2-b^2}}\right)}{\sqrt{a^2-b^2}}-\frac{b\tan^{-1}\left(\frac{\#1 a}{\sqrt{a^2-b^2}}\right)}{\sqrt{a^2-b^2}}+\sinh^{-1}(\#1)}{a}\&\right][c_1+x]^2-b\sqrt{\text{InverseFunctio}}}{a^2\sqrt{\text{Inv}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.163 (sec), leaf count = 31

$$\left\{y(x) = \int RootOf\left(x - \int^{\_Z} \left(a\sqrt{\_f^2 + 1} + b\right)^{-1} d\_f + \_C1\right) dx + \_C2\right\}$$

2.1652 ODE No. 1652

$$y''(x) - a\sqrt{by(x)^2 + y'(x)^2} = 0$$

✗ **Mathematica** : cpu = 0.848556 (sec), leaf count = 0 , could not solve

```
DSolve[-(a*Sqrt[b*y[x]^2 + Derivative[1][y][x]^2]) + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.309 (sec), leaf count = 36

$$\left\{y(x) = e^{\int RootOf\left(x - \int^{\_Z}\left(a\sqrt{\_f^2+b} - \_f^2\right)^{-1} d\_f + \_C1\right) dx + \_C2}\right\}$$

2.1653 ODE No. 1653

$$y''(x) - a\left(y'(x)^2 + 1\right)^{3/2} = 0$$

✓ **Mathematica** : cpu = 0.0666366 (sec), leaf count = 75

$$\left\{\left\{y(x) \to c_2 - \frac{i\sqrt{a^2x^2 + 2ac_1x + c_1^2 - 1}}{a}\right\}, \left\{y(x) \to c_2 + \frac{i\sqrt{a^2x^2 + 2ac_1x + c_1^2 - 1}}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 41

$$\left\{y(x) = \frac{1}{a}\left(\left(-1 + (\_C1 + x)^2 a^2\right)\sqrt{-\left(-1 + (\_C1 + x)^2 a^2\right)^{-1}} + \_C2\, a\right)\right\}$$

2.1654 ODE No. 1654

$$y''(x) - 2ax\left(y'(x)^2 + 1\right)^{3/2} = 0$$

✓ **Mathematica** : cpu = 0.277485 (sec), leaf count = 308

$$\left\{\left\{y(x) \to c_2 - \frac{\sqrt{\frac{ax^2+c_1-1}{c_1-1}}\sqrt{\frac{ax^2+c_1+1}{c_1+1}}\left(F\left(i\sinh^{-1}\left(x\sqrt{\frac{a}{c_1+1}}\right)|\frac{c_1+1}{c_1-1}\right) + (c_1-1)\,E\left(i\sinh^{-1}\left(x\sqrt{\frac{a}{c_1+1}}\right)|\frac{c_1+1}{c_1-1}\right)\right)}{\sqrt{\frac{a}{c_1+1}}\sqrt{a^2x^4 + 2ac_1x^2 + c_1^2 - 1}}\right.\right.$$

✓ **Maple** : cpu = 0.187 (sec), leaf count = 38

$$\left\{y(x) = \int \sqrt{-\left(-1 + (x^2 + 2\_C1)^2 a^2\right)^{-1}} a(x^2 + 2\_C1)\, dx + \_C2\right\}$$

2.1655 ODE No. 1655

$$y''(x) - ay(x)\left(y'(x)^2 + 1\right)^{3/2} = 0$$

✓ **Mathematica** : cpu = 0.817191 (sec), leaf count = 350

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{\sqrt{\frac{\#1^2 a + 2c_1 - 2}{c_1 - 1}}\sqrt{\frac{\#1^2 a + 2c_1 + 2}{c_1 + 1}}\left(F\left(i \sinh^{-1}\left(\sqrt{\frac{a}{2c_1+2}}\#1\right)|\frac{c_1+1}{c_1-1}\right) + (c_1 - 1)\, E\left(i \sinh^{-1}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.22 (sec), leaf count = 84

$$\left\{\int^{y(x)} a(\_a^2 + 2\_C1)\frac{1}{\sqrt{4 - a^2(\_a^2 + 2\_C1)^2}} d\_a - x - \_C2 = 0, \int^{y(x)} -a(\_a^2 + 2\_C1)\frac{1}{\sqrt{4 - a^2(\_a^2 -}$$

2.1656 ODE No. 1656

$$y''(x) - a\left(y'(x)^2 + 1\right)^{3/2}(bx + c + y(x)) = 0$$

✗ **Mathematica** : cpu = 100.314 (sec), leaf count = 0 , could not solve

```
DSolve[-(a*(c + b*x + y[x])*(1 + Derivative[1][y][x]^2)^(3/2)) + Derivative[2][y][x] == 0, y
```

✓ **Maple** : cpu = 0.78 (sec), leaf count = 771

$$\left\{y(x) = -bx + RootOf\left(-x + \int^{\_Z} \frac{1}{(\_f^4 a^2 + 4\_f^3 a^2 c + 4\_f^2 a^2 c^2 - 4\_f^2 a^2 \_C1 - 8\_C1\,\_f\, a^2 c + 4\_C1^2 a^2}\right.\right.$$

2.1657 ODE No. 1657

$$y''(x)+y(x)^3y'(x)-y(x)y'(x)\sqrt{4y'(x)+y(x)^4}=0$$

✓ **Mathematica** : cpu = 0.150069 (sec), leaf count = 33

$$\left\{\left\{y(x)\to\sqrt{2}e^{c_1}\tan\left(2\sqrt{2}e^{3c_1}(c_2+x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.268 (sec), leaf count = 35

$$\left\{y(x)=\frac{1}{\_C1}\tan\left(\left(\_C1^{-2}\right)^{\frac{3}{2}}(\_C2+x)\right),y(x)=\frac{1}{\_C1}\tanh\left(\left(\_C1^{-2}\right)^{\frac{3}{2}}(\_C2+x)\right)\right\}$$

2.1658 ODE No. 1658

$$y''(x)-h\left(y'(x),ax+by(x)\right)=0$$

✗ **Mathematica** : cpu = 0.130139 (sec), leaf count = 0 , could not solve

```
DSolve[-h[Derivative[1][y][x], a*x + b*y[x]] + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.143 (sec), leaf count = 115

$$\left\{y(x)=ODESolStruc\left(-\frac{a\left(\int\_b(\_a)\,\mathrm{d}\_a+\_C1\right)-b\_a}{b},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=-h\left(\frac{-a\_b(\_a)+b}{\_b(\_a)\,b},b\_a\right)(\_b(\_\right.\right.\right.$$

2.1659 ODE No. 1659

$$y''(x)-y(x)h\left(x,\frac{y'(x)}{y(x)}\right)=0$$

✗ **Mathematica** : cpu = 10.8227 (sec), leaf count = 0 , could not solve

```
DSolve[-(h[x, Derivative[1][y][x]/y[x]]*y[x]) + Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.093 (sec), leaf count = 60

$$\left\{y(x)=ODESolStruc\left(\mathrm{e}^{\int\_b(\_a)\,\mathrm{d}\_a+\_C1},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=-(\_b(\_a))^2+h(\_a,\_b(\_a))\right\},\left\{\_a=x,\_b(\_a)\right.\right.\right.$$

2.1660 ODE No. 1660

$$y''(x) - x^{n-2} h\left(x^{-n} y(x), x^{1-n} y'(x)\right) = 0$$

✗ **Mathematica** : cpu = 4.70177 (sec), leaf count = 0 , could not solve

```
DSolve[-(x^(-2 + n)*h[y[x]/x^n, x^(1 - n)*Derivative[1][y][x]]) + Derivative[2][y][x] == 0,
```

✓ **Maple** : cpu = 0.944 (sec), leaf count = 125

$$\left\{y(x) = ODESolStruc\left(\frac{\_a}{\mathrm{e}^{-(\int \_b(\_a)\,\mathrm{d}\_a + \_C1)n}}, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = \left(-\_b(\_a)\, h\left(\_a, \frac{\_b(\_a)\,\_a\, n + 1}{\_b(\_a)}\right) + n\_a\,(\right.\right.\right.$$

2.1661 ODE No. 1661

$$8y''(x) + 9y'(x)^4 = 0$$

✓ **Mathematica** : cpu = 0.0316683 (sec), leaf count = 92

$$\left\{\left\{y(x) \to c_2 - \frac{1}{3}\sqrt[3]{-\frac{1}{3}}(9x - 8c_1)^{2/3}\right\}, \left\{y(x) \to \frac{(9x - 8c_1)^{2/3}}{3\sqrt[3]{3}} + c_2\right\}, \left\{y(x) \to \frac{(-1)^{2/3}(9x - 8c_1)^{2/3}}{3\sqrt[3]{3}} + c_2\right\}\right.$$

✓ **Maple** : cpu = 0.085 (sec), leaf count = 51

$$\left\{y(x) = (\_C1 + x)^{\frac{2}{3}} + \_C2, y(x) = \frac{i\sqrt{3} - 1}{2}(\_C1 + x)^{\frac{2}{3}} + \_C2, y(x) = -\frac{i\sqrt{3} + 1}{2}(\_C1 + x)^{\frac{2}{3}} + \_C2\right\}$$

2.1662 ODE No. 1662

$$ay''(x) + cy(x) + h\left(y'(x)\right) = 0$$

✗ **Mathematica** : cpu = 1.43684 (sec), leaf count = 0 , could not solve

```
DSolve[h[Derivative[1][y][x]] + c*y[x] + a*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.4 (sec), leaf count = 56

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + \frac{h(\_b(\_a)) + c\_a}{a} = 0\right\}, \left\{\_a = y(x), \_b(\_a) = \frac{\mathrm{d}}{\mathrm{d}x}y\right.\right.\right.$$

2.1663 ODE No. 1663

$$-xy(x)^n + xy''(x) + 2y'(x) = 0$$

✗ **Mathematica** : cpu = 0.0358626 (sec), leaf count = 0 , could not solve

```
DSolve[-(x*y[x]^n) + 2*Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.959 (sec), leaf count = 125

$$\left\{ y(x) = ODESolStruc\left(\_a\, \mathrm{e}^{\int -\_b(\_a)\, \mathrm{d}\_a + \_C1}, [\left\{ \frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = -\frac{(\_b(\_a))^2 \left(\_b(\_a)\,(n-1)^2\, \_a^n + 2\, \_a\,(n - \right.}{4} \right.$$

2.1664 ODE No. 1664

$$ax^m y(x)^n + xy''(x) + 2y'(x) = 0$$

✗ **Mathematica** : cpu = 0.54054 (sec), leaf count = 0 , could not solve

```
DSolve[a*x^m*y[x]^n + 2*Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 3.272 (sec), leaf count = 155

$$\left\{ y(x) = ODESolStruc\left(\_a\, \mathrm{e}^{\int -\_b(\_a)\, \mathrm{d}\_a + \_C1}, [\left\{ \frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = \frac{\left(a\_b(\_a)\,(n-1)^2\, \_a^n + (m+1)\,(\_a\,(m-n \right.}{(m+1)} \right.$$

2.1665 ODE No. 1665

$$xy''(x) + 2y'(x) + xe^{y(x)} = 0$$

✗ **Mathematica** : cpu = 0.356828 (sec), leaf count = 0 , could not solve

```
DSolve[E^y[x]*x + 2*Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.617 (sec), leaf count = 84

$$\left\{ y(x) = ODESolStruc\left(\_a - 2 \int \_b(\_a)\ \mathrm{d}\_a - 2\, \_C1, [\left\{ \frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = (\mathrm{e}^{-a} - 2)\,(\_b(\_a))^3 + (\_b(\_a))^2 \right\} \right.$$

2.1666 ODE No. 1666

$$ay'(x) + bxe^{y(x)} + xy''(x) = 0$$

✗ **Mathematica** : cpu = 0.580877 (sec), leaf count = 0 , could not solve

```
DSolve[b*E^y[x]*x + a*Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.963 (sec), leaf count = 93

$$\left\{y(x) = ODESolStruc\left(\_a - 2\int \_b(\_a)\ \mathrm{d}\_a - 2\_C1, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = (b\mathrm{e}^{-a} - 2a + 2)(\_b(\_a))^3 + (a - 1\right.\right.$$

2.1667 ODE No. 1667

$$bx^{5-2a}e^{y(x)} + ay'(x) + xy''(x) = 0$$

✗ **Mathematica** : cpu = 0.606557 (sec), leaf count = 0 , could not solve

```
DSolve[b*E^y[x]*x^(5 - 2*a) + a*Derivative[1][y][x] + x*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.548 (sec), leaf count = 121

$$\left\{y(x) = ODESolStruc\left((2a - 6)\int \_b(\_a)\ \mathrm{d}\_a + 2a\_C1 + \_a - 6\_C1, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = (b\mathrm{e}^{-a} + 2a^2 - 8a\right.\right.$$

2.1668 ODE No. 1668

$$xy''(x) - (1 - y(x))y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0719182 (sec), leaf count = 60

$$\left\{\left\{y(x) \to \sqrt{2}\sqrt{c_1 + 2}\tanh\left(\frac{1}{2}\left(\sqrt{2}\sqrt{c_1 + 2}\log(x) - 2\sqrt{2}\sqrt{c_1 + 2}c_2\right)\right) + 2\right\}\right\}$$

✓ **Maple** : cpu = 0.162 (sec), leaf count = 24

$$\left\{y(x) = \frac{1}{\_C1}\left(2\_C1 + \tanh\left(\frac{\ln(x) - \_C2}{2\_C1}\right)\right)\right\}$$

2.1669 ODE No. 1669

$$-x^2y'(x)^2+xy''(x)+2y'(x)+y(x)^2=0$$

✓ **Mathematica** : cpu = 103.623 (sec), leaf count = 126

$$\text{Solve}\left[\int_1^{y(x)}-\frac{x}{c_1e^{xK[1]}+2xK[1]+1}\,dK[1]-\int_1^{x}\left(-\frac{y(x)}{c_1e^{y(x)K[2]}+2y(x)K[2]+1}-\frac{c_1e^{y(x)K[2]}+y(x)K[2]+\right.\right.$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 32

$$\left\{y(x)=\frac{1}{x}RootOf\left(-\ln(x)+\_C2+\int^{-Z}-\left(\mathrm{e}^{-\_f}\_C1-2\_f-1\right)^{-1}d\_f\right)\right\}$$

2.1670 ODE No. 1670

$$a\left(xy'(x)-y(x)\right)^2-b+xy''(x)=0$$

✓ **Mathematica** : cpu = 83.764 (sec), leaf count = 50

$$\left\{\left\{y(x)\to x\left(\int_1^x\frac{\sqrt{-\frac{b}{a}}\tan\left(c_1-a\sqrt{-\frac{b}{a}}K[2]\right)}{K[2]^2}\,dK[2]+c_2\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.398 (sec), leaf count = 35

$$\left\{y(x)=\left(\int\frac{i}{x^2}\tan\left(-i\sqrt{a}\sqrt{b}x+\_C1\right)\sqrt{b}\frac{1}{\sqrt{a}}\,\mathrm{d}x+\_C2\right)x\right\}$$

2.1671 ODE No. 1671

$$2xy''(x)+y'(x)^3+y'(x)=0$$

✓ **Mathematica** : cpu = 0.0359234 (sec), leaf count = 59

$$\left\{\left\{y(x)\to c_2-2ie^{c_1}\sqrt{e^{2c_1}-x}\right\},\left\{y(x)\to c_2+2ie^{c_1}\sqrt{e^{2c_1}-x}\right\}\right\}$$

✓ **Maple** : cpu = 0.092 (sec), leaf count = 35

$$\left\{y(x)=-2\frac{\sqrt{\_C1\,x-1}}{\_C1}+\_C2,y(x)=2\frac{\sqrt{\_C1\,x-1}}{\_C1}+\_C2\right\}$$

2.1672 ODE No. 1672

$$x^2 y''(x) - a(y(x)^n - y(x)) = 0$$

✗ **Mathematica** : cpu = 17.9383 (sec), leaf count = 0 , could not solve

```
DSolve[-(a*(-y[x] + y[x]^n)) + x^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.094 (sec), leaf count = 65

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = (\_b(\_a))^2 (\_a \_b(\_a) a - \_a^n \_b(\_a) a - 1)\right\}, \left\{\_a = y(x), \_b\right.\right.$$

2.1673 ODE No. 1673

$$a\left(e^{y(x)} - 1\right) + x^2 y''(x) = 0$$

✗ **Mathematica** : cpu = 31.1606 (sec), leaf count = 0 , could not solve

```
DSolve[a*(-1 + E^y[x]) + x^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.813 (sec), leaf count = 60

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = (-1 + a(\mathrm{e}^{-a} - 1) \_b(\_a)) (\_b(\_a))^2\right\}, \left\{\_a = y(x), \_b(\_a) =\right.\right.$$

2.1674 ODE No. 1674

$$y(x)\left(a(a+b) + b^2 c^2 x^{2b}\right) - x(2a+b-1)y'(x) + x^2 y''(x) = 0$$

✓ **Mathematica** : cpu = 0.059366 (sec), leaf count = 106

$$\left\{\left\{y(x) \to c_2 2^{-\frac{a+b}{b}} c^{\frac{a+b}{b}-1}\left(x^{2b}\right)^{\frac{a+b}{2b}-\frac{1}{2}} \sin\left(c\sqrt{x^{2b}}\right) + c_1 2^{-\frac{a}{b}} c^{a/b}\left(x^{2b}\right)^{\frac{a}{2b}} \cos\left(c\sqrt{x^{2b}}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 25

$$\left\{y(x) = x^a\left(\sin\left(x^b c\right) \_C1 + \cos\left(x^b c\right) \_C2\right)\right\}$$

2.1675 ODE No. 1675

$$x^k\left(-h\left(x^k y(x), ky(x)+xy'(x)\right)\right)+(a+1)xy'(x)+x^2y''(x)=0$$

✗ **Mathematica** : cpu = 3.51322 (sec), leaf count = 0 , could not solve

```
DSolve[-(x^k*h[x^k*y[x], k*y[x] + x*Derivative[1][y][x]]) + (1 + a)*x*Derivative[1][y][x] +
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x^2*diff(diff(y(x),x),x)+(a+1)*x*diff(y(x),x)-x^k*h(x^k*y(x),x*diff(y(x),x)+k*y(x))=0
```

2.1676 ODE No. 1676

$$a\left(xy'(x)-y(x)\right)^2-bx^2+x^2y''(x)=0$$

✓ **Mathematica** : cpu = 53.3529 (sec), leaf count = 133

$$\left\{\left\{y(x)\to x\left(c_2+\int_1^x \frac{i\sqrt{a}\sqrt{b}Y_1\left(-i\sqrt{a}\sqrt{b}K[2]\right)-i\sqrt{a}\sqrt{b}c_1J_1\left(i\sqrt{a}\sqrt{b}K[2]\right)}{aK[2]\left(c_1J_0\left(i\sqrt{a}\sqrt{b}K[2]\right)+Y_0\left(-i\sqrt{a}\sqrt{b}K[2]\right)\right)}\,dK[2]\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.28 (sec), leaf count = 72

$$\left\{y(x)=\left(\int -\frac{1}{ax}\sqrt{-ab}\left(\_C1\,Y_1\left(\sqrt{-ab}x\right)+J_1\left(\sqrt{-ab}x\right)\right)\left(\_C1\,Y_0\left(\sqrt{-ab}x\right)+J_0\left(\sqrt{-ab}x\right)\right)^{-1}\mathrm{d}x+\_C2\right)x\right.$$

2.1677 ODE No. 1677

$$ay(x)y'(x)^2+bx+x^2y''(x)=0$$

✗ **Mathematica** : cpu = 46.7316 (sec), leaf count = 0 , could not solve

```
DSolve[b*x + a*y[x]*Derivative[1][y][x]^2 + x^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 2.267 (sec), leaf count = 101

$$\left\{y(x)=ODESolStruc\left(\_a\,\mathrm{e}^{\int -\_b(\_a)\,\mathrm{d}\_a+\_C1},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=\left(a\_a^3+b\right)\left(\_b(\_a)\right)^3+\left(2\_a^2a+1\right)\left(\_b(\_a)\right)\right.\right.$$

2.1678 ODE No. 1678

$$x^2 y''(x) - \sqrt{a x^2 y'(x)^2 + b y(x)^2} = 0$$

✗ **Mathematica** : cpu = 1.5267 (sec), leaf count = 0 , could not solve

```
DSolve[-Sqrt[b*y[x]^2 + a*x^2*Derivative[1][y][x]^2] + x^2*Derivative[2][y][x] == 0, y[x], x
```

✓ **Maple** : cpu = 0.265 (sec), leaf count = 60

$$\left\{ y(x) - \mathrm{e}^{\int^{\ln(x)} RootOf\left(\int^{-Z} -y(x)\left(\_a^2 y(x) - \_a\, y(x) - \sqrt{(y(x))^2 (\_a^2 a + b)} \right)^{-1} d\_a - \_b + \_C1 \right) d\_b + \_C2} = 0 \right\}$$

2.1679 ODE No. 1679

$$\left(x^2+1\right) y''(x) + y'(x)^2 + 1 = 0$$

✓ **Mathematica** : cpu = 0.0767423 (sec), leaf count = 33

$$\left\{ \left\{ y(x) \to -x \cot(c_1) + \csc^2(c_1) \log(-x \sin(c_1) - \cos(c_1)) + c_2 \right\} \right\}$$

✓ **Maple** : cpu = 0.152 (sec), leaf count = 27

$$\left\{ y(x) = \frac{x}{\_C1} + \ln(\_C1\, x - 1) + \frac{\ln(\_C1\, x - 1)}{\_C1^2} + \_C2 \right\}$$

2.1680 ODE No. 1680

$$x^4\left(-y'(x)^2\right) + 4x^2 y''(x) + 4y(x) = 0$$

✗ **Mathematica** : cpu = 10.8063 (sec), leaf count = 0 , could not solve

```
DSolve[4*y[x] - x^4*Derivative[1][y][x]^2 + 4*x^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.638 (sec), leaf count = 103

$$\left\{ y(x) = ODESolStruc\left(\frac{\_a}{\left(\mathrm{e}^{\int \_b(\_a)\, \mathrm{d}\_a + \_C1} \right)^2}, \left[\left\{ \frac{\mathrm{d}}{\mathrm{d}\_a} \_b(\_a) = \left(-\_a^2 + 7\,\_a\right) (\_b(\_a))^3 + (\_a - 5)\,(\_b(\_a \right.\right.\right.$$

2.1681 ODE No. 1681

$$ay(x)^3 + 9x^2y''(x) + 2y(x) = 0$$

✗ **Mathematica** : cpu = 3.40334 (sec), leaf count = 0 , could not solve

```
DSolve[2*y[x] + a*y[x]^3 + 9*x^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.056 (sec), leaf count = 31

$$\left\{y(x) = \_C2\ JacobiSN\left(\left(\frac{\sqrt{2}}{2\,x^3}\sqrt{x^{\frac{20}{3}}a} + \_C1\right)\_C2, i\right)\sqrt[3]{x}\right\}$$

2.1682 ODE No. 1682

$$x^3\left(y''(x) + y(x)y'(x) - y(x)^3\right) + 12xy(x) + 24 = 0$$

✗ **Mathematica** : cpu = 22.6122 (sec), leaf count = 0 , could not solve

```
DSolve[24 + 12*x*y[x] + x^3*(-y[x]^3 + y[x]*Derivative[1][y][x] + Derivative[2][y][x]) == 0,
```

✓ **Maple** : cpu = 0.638 (sec), leaf count = 94

$$\left\{y(x) = ODESolStruc\left(\_a\,\mathrm{e}^{\int \_b(\_a)\,\mathrm{d}\_a + \_C1}, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = -(\_b(\_a))^2\left((\_a^3 + \_a^2 - 14\,\_a - 24\right)\_b(\_a\right.\right.\right.$$

2.1683 ODE No. 1683

$$x^3y''(x) - a\left(xy'(x) - y(x)\right)^2 = 0$$

✓ **Mathematica** : cpu = 0.0730561 (sec), leaf count = 26

$$\left\{\left\{y(x) \to -\frac{x\log\left(a\left(-\frac{c_1}{x} - c_2\right)\right)}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 23

$$\left\{y(x) = -\frac{x}{a}\ln\left(\frac{a(\_C1\,x - \_C2)}{x}\right)\right\}$$

2.1684 ODE No. 1684

$$xy(x)\left(a-2x^2y(x)^2+3xy(x)\right)+b+2x^3y''(x)+x^2(2xy(x)+9)y'(x)=0$$

✗ **Mathematica** : cpu = 61.2302 (sec), leaf count = 0 , could not solve

```
DSolve[b + x*y[x]*(a + 3*x*y[x] - 2*x^2*y[x]^2) + x^2*(9 + 2*x*y[x])*Derivative[1][y][x] + 2
```

✓ **Maple** : cpu = 1.717 (sec), leaf count = 100

$$\left\{y(x)=ODESolStruc\left(\_a\,e^{\int \_b(\_a)\,d\_a+\_C1},\left[\left\{\frac{d}{d\_a}\_b(\_a)=\frac{(\_b(\_a))^2\left(\left(-2\,\_a^3+\_a^2+(a-5)\,\_a+b\right)\_\right.\right.\right.\right.}{2}$$

2.1685 ODE No. 1685

$$axy(x)+b-\left(kx^{k-1}-12x^2\right)\left(3y'(x)+y(x)^2\right)+2\left(4x^3-x^k\right)\left(y''(x)+y(x)y'(x)-y(x)^3\right)=0$$

✗ **Mathematica** : cpu = 5.29789 (sec), leaf count = 0 , could not solve

```
DSolve[b + a*x*y[x] - (-12*x^2 + k*x^(-1 + k))*(y[x]^2 + 3*Derivative[1][y][x]) + 2*(4*x^3 -
y[x]^3 + y[x]*Derivative[1][y][x] + Derivative[2][y][x]) == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*(-x^k+4*x^3)*(diff(diff(y(x),x),x)+y(x)*diff(y(x),x)-y(x)^3)-(k*x^(k-
1)-12*x^2)*(3*diff(y(x),x)+y(x)^2)+a*x*y(x)+b=0,y(x))
```

2.1686 ODE No. 1686

$$a^2y(x)^n+x^4y''(x)=0$$

✗ **Mathematica** : cpu = 0.0322203 (sec), leaf count = 0 , could not solve

```
DSolve[a^2*y[x]^n + x^4*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 1.18 (sec), leaf count = 128

$$\left\{y(x)=ODESolStruc\left(\_a\,e^{\int \_b(\_a)\,d\_a+\_C1},\left[\left\{\frac{d}{d\_a}\_b(\_a)=\frac{(\_b(\_a))^2\left(a^2\_b(\_a)\,(n-1)^2\,\_a^n-2\,\_a\,(n-\right.\right.\right.\right.}{4}$$

2.1687 ODE No. 1687

$$x^4 y''(x) - x\left(x^2 + 2y(x)\right) y'(x) + 4y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0676976 (sec), leaf count = 262

$$\left\{\left\{y(x) \to -\frac{x^3\left(i\left(-\frac{\sqrt{-c_1-1}}{\sqrt{c_1}}+\frac{i}{\sqrt{c_1}}\right)\sqrt{c_1}c_2 x^{-1+i\left(-\frac{\sqrt{-c_1-1}}{\sqrt{c_1}}+\frac{i}{\sqrt{c_1}}\right)\sqrt{c_1}} + i\left(\frac{\sqrt{-c_1-1}}{\sqrt{c_1}}+\frac{i}{\sqrt{c_1}}\right)\sqrt{c_1}x^{-1+i\left(\frac{\sqrt{-c_1-1}}{\sqrt{c_1}}+\frac{i}{\sqrt{c_1}}\right.}\right.}{c_2 x^{i\left(-\frac{\sqrt{-c_1-1}}{\sqrt{c_1}}+\frac{i}{\sqrt{c_1}}\right)\sqrt{c_1}} + x^{i\left(\frac{\sqrt{-c_1-1}}{\sqrt{c_1}}+\frac{i}{\sqrt{c_1}}\right)\sqrt{c_1}}}\right.\right.$$

✓ **Maple** : cpu = 0.104 (sec), leaf count = 21

$$\left\{y(x) = x^2(\tanh\left(\_C1\left(\_C2 - \ln(x)\right)\right)\_C1 + 1)\right\}$$

2.1688 ODE No. 1688

$$x^4 y''(x) - x^2 y'(x)\left(y'(x) + x\right) + 4y(x)^2 = 0$$

✓ **Mathematica** : cpu = 249.261 (sec), leaf count = 166

$$\text{Solve}\left[\int_1^{y(x)} \frac{1}{c_1 x^2\left(-e^{\frac{K[1]}{x^2}}\right) + 4K[1] + 2x^2}\,dK[1] - \int_1^x \left(\frac{K[2]\left(c_1 e^{\frac{y(x)}{K[2]^2}} + 2\left(-\frac{y(x)}{K[2]^2} - 1\right)\right)}{c_1 K[2]^2\left(-e^{\frac{y(x)}{K[2]^2}}\right) + 2K[2]^2 + 4y(x)} + 2\left(\frac{}{K[2]^3\left(c_1 e\right.}\right.\right.$$

✓ **Maple** : cpu = 0.113 (sec), leaf count = 32

$$\left\{y(x) = RootOf\left(-\ln(x) + \_C2 - \int^{\_Z}\left(\mathrm{e}^{\_f}\_C1 + 4\_f + 2\right)^{-1} d\_f\right)x^2\right\}$$

2.1689 ODE No. 1689

$$x^4 y''(x) + \left(xy'(x) - y(x)\right)^3 = 0$$

✓ **Mathematica** : cpu = 0.640328 (sec), leaf count = 329

$$\left\{\left\{y(x) \to -ix\log\left(-\frac{\sqrt{-8ic_1x^2 - \sinh(2c_2)} - \cosh(2c_2)}{4c_1x} - \frac{i\sinh(c_2)}{4c_1x} - \frac{i\cosh(c_2)}{4c_1x}\right)\right\}, \left\{y(x) \to -ix\log\left(-\right.\right.\right.$$

✓ **Maple** : cpu = 0.162 (sec), leaf count = 37

$$\left\{y(x) = \left(-\arctan\left(\frac{1}{\sqrt{\_C1\,x^2-1}}\right)+\_C2\right)x, y(x) = \left(\arctan\left(\frac{1}{\sqrt{\_C1\,x^2-1}}\right)+\_C2\right)x\right\}$$

2.1690 ODE No. 1690

$$\sqrt{x}y''(x) - y(x)^{3/2} = 0$$

✗ **Mathematica** : cpu = 22.3958 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^(3/2) + Sqrt[x]*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.837 (sec), leaf count = 99

$$\left\{y(x) = ODESolStruc\left(\frac{\_a}{\left(e^{\int \_b(\_a)\,d\_a+\_C1}\right)^3}, [\left\{\frac{d}{d\_a}\_b(\_a) = -(\_b(\_a))^3\,\_a^{\frac{3}{2}} + 12\,(\_b(\_a))^3\,\_a - 7\,(\_b(\right.\right.$$

2.1691 ODE No. 1691

$$y''(x)\left(ax^2+bx+c\right)^{3/2} - f\left(\frac{y(x)}{\sqrt{ax^2+bx+c}}\right) = 0$$

✗ **Mathematica** : cpu = 61.4586 (sec), leaf count = 0 , could not solve

```
DSolve[-f[y[x]/Sqrt[c + b*x + a*x^2]] + (c + b*x + a*x^2)^(3/2)*Derivative[2][y][x] == 0, y[
```

✓ **Maple** : cpu = 1.267 (sec), leaf count = 254

$$\left\{y(x) = RootOf\left(-2\,a\arctan\left(\frac{2\,ax+b}{\sqrt{4\,ca-b^2}}\right) - 2\int^{\_Z}\frac{a}{\sqrt{4\,\_C1\,a^2 - 4\,c\_g^2a + b^2\_g^2 + 8\int F(\_g)\,d\_g}}d\_g\sqrt{4\right.\right.$$

2.1692 ODE No. 1692

$$x^{\frac{n}{n+1}}y''(x) - y(x)^{\frac{2n+1}{n+1}} = 0$$

✗ **Mathematica** : cpu = 0.0822869 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^((1 + 2*n)/(1 + n)) + x^(n/(1 + n))*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 3.955 (sec), leaf count = 156

$$\left\{y(x) = ODESolStruc\left(\_a\left(e^{\frac{(\int \_b(\_a)\,d\_a+\_C1)(n+2)}{n}}\right)^{-1}, [\left\{\frac{d}{d\_a}\_b(\_a) = 2\,\frac{(\_b(\_a))^2}{n^2}\left(-1/2\,\_a^{\frac{2n+1}{n+1}}\_b(\_a)\,n^2 -\right.\right.\right.$$

2.1693 ODE No. 1693

$$-h(y(x),f(x)y'(x))+f(x)f'(x)y'(x)+f(x)^2y''(x)=0$$

✗ **Mathematica** : cpu = 0.985501 (sec), leaf count = 0 , could not solve

```
DSolve[-h[y[x], f[x]*Derivative[1][y][x]] + f[x]*Derivative[1][f][x]*Derivative[1][y][x] + f
```

✓ **Maple** : cpu = 0.329 (sec), leaf count = 68

$$\left\{y(x)=ODESolStruc\left(\_a,[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=-h\left(\_a,(\_b(\_a))^{-1}\right)(\_b(\_a))^3\right\},\left\{\_a=y(x),\_b(\_a)=\frac{}{f(x)}\right.\right.$$

2.1694 ODE No. 1694

$$y(x)y''(x)-a=0$$

✓ **Mathematica** : cpu = 0.187861 (sec), leaf count = 115

$$\left\{\left\{y(x)\to\exp\left(\frac{-c_1-2a\mathrm{erf}^{-1}\left(-i\sqrt{\frac{2}{\pi}}\sqrt{ae^{\frac{c_1}{a}}(c_2+x)^2}\right)^2}{2a}\right)\right\},\left\{y(x)\to\exp\left(\frac{-c_1-2a\mathrm{erf}^{-1}\left(i\sqrt{\frac{2}{\pi}}\sqrt{ae^{\frac{c_1}{a}}(c\right.\right.\right.$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 54

$$\left\{\int^{y(x)}\frac{1}{\sqrt{2\ln(\_a)a-2a\_C1}}d\_a-x-\_C2=0,\int^{y(x)}-\frac{1}{\sqrt{-2a(\_C1-\ln(\_a))}}d\_a-x-\_C2=0\right\}$$

2.1695 ODE No. 1695

$$y(x)y''(x)-ax=0$$

✗ **Mathematica** : cpu = 25.3638 (sec), leaf count = 0 , could not solve

```
DSolve[-(a*x) + y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.627 (sec), leaf count = 103

$$\left\{y(x)=ODESolStruc\left(\_a\left(\mathrm{e}^{\int\_b(\_a)\,\mathrm{d}\_a+\_C1}\right)^{\frac{3}{2}},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=\frac{(3\_a^2-4a)(\_b(\_a))^3}{4\_a}+2(\_b(\_a))^2\right\},\right.\right.$$

2.1696 ODE No. 1696

$$y(x)y''(x) - ax^2 = 0$$

✗ **Mathematica** : cpu = 24.3159 (sec), leaf count = 0 , could not solve

```
DSolve[-(a*x^2) + y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.513 (sec), leaf count = 100

$$\left\{y(x) = ODESolStruc\left(\_a\left(\mathrm{e}^{\int -\_b(\_a)\,\mathrm{d}\_a+\_C1}\right)^2, [\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a) = \frac{(2\_a^2 - a)\,(\_b(\_a))^3}{\_a} + 3\,(\_b(\_a))^2\right\}, \{\right.\right.$$

2.1697 ODE No. 1697

$$-a + y(x)y''(x) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0622368 (sec), leaf count = 94

$$\left\{\left\{y(x) \to -\frac{\sqrt{2a^2c_2x + a^2c_2^2 + a^2x^2 - e^{2c_1}}}{\sqrt{a}}\right\}, \left\{y(x) \to \frac{\sqrt{2a^2c_2x + a^2c_2^2 + a^2x^2 - e^{2c_1}}}{\sqrt{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.044 (sec), leaf count = 39

$$\left\{y(x) = \sqrt{ax^2 - 2\_C1\,x + 2\_C2}, y(x) = -\sqrt{ax^2 - 2\_C1\,x + 2\_C2}\right\}$$

2.1698 ODE No. 1698

$$-ax - b + y(x)y''(x) + y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0406556 (sec), leaf count = 72

$$\left\{\left\{y(x) \to -\frac{\sqrt{ax^3 + 3bx^2 + 3c_2x + 6c_1}}{\sqrt{3}}\right\}, \left\{y(x) \to \frac{\sqrt{ax^3 + 3bx^2 + 3c_2x + 6c_1}}{\sqrt{3}}\right\}\right\}$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)*y(x)+y(x)^2-a*x-b=0,y(x))
```

2.1699 ODE No. 1699

$$y(x)y''(x)+y'(x)^2-y'(x)=0$$

✓ **Mathematica** : cpu = 0.0375259 (sec), leaf count = 40

$$\left\{\left\{y(x)\to c_1\left(-W\left(-\frac{e^{-\frac{x}{c_1}-\frac{c_2}{c_1}-1}}{c_1}\right)\right)-c_1\right\}\right\}$$

✓ **Maple** : cpu = 0.096 (sec), leaf count = 33

$$\left\{y(x)=-\_C1\left(lambertW\left(-\frac{\mathrm{e}^{-1}}{\_C1}\left(\mathrm{e}^{\frac{\_C2}{\_C1}}\right)^{-1}\left(\mathrm{e}^{\frac{x}{\_C1}}\right)^{-1}\right)+1\right)\right\}$$

2.1700 ODE No. 1700

$$y(x)y''(x)-y'(x)^2+1=0$$

✓ **Mathematica** : cpu = 0.0771144 (sec), leaf count = 44

$$\left\{\left\{y(x)\to -e^{-c_1}\sinh\left(e^{c_1}(c_2+x)\right)\right\},\left\{y(x)\to e^{-c_1}\sinh\left(e^{c_1}(c_2+x)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.331 (sec), leaf count = 86

$$\left\{y(x)=\frac{1}{2}\left(-\_C1\left(\mathrm{e}^{\frac{x}{\_C1}}\right)^2\left(\mathrm{e}^{\frac{\_C2}{\_C1}}\right)^2+\_C1\right)\left(\mathrm{e}^{\frac{\_C2}{\_C1}}\right)^{-1}\left(\mathrm{e}^{\frac{x}{\_C1}}\right)^{-1},y(x)=\frac{1}{2}\left(\_C1\left(\mathrm{e}^{\frac{x}{\_C1}}\right)^2\left(\mathrm{e}^{\frac{\_C2}{\_C1}}\right)^2-\_C1\right)\right.$$

2.1701 ODE No. 1701

$$y(x)y''(x)-y'(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.180394 (sec), leaf count = 97

$$\left\{\left\{y(x)\to\frac{1}{2}e^{-e^{c_1}x-2c_1-e^{c_1}c_2}\left(e^{2e^{c_1}(c_2+x)}+e^{2c_1}\right)\right\},\left\{y(x)\to\frac{1}{2}\left(e^{-e^{c_1}x-2c_1-e^{c_1}c_2}+e^{e^{c_1}x+e^{c_1}c_2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.289 (sec), leaf count = 42

$$\left\{y(x)=\frac{\_C1}{2}\left(\left(\mathrm{e}^{\frac{\_C2}{\_C1}}\right)^2\left(\mathrm{e}^{\frac{x}{\_C1}}\right)^2+1\right)\left(\mathrm{e}^{\frac{\_C2}{\_C1}}\right)^{-1}\left(\mathrm{e}^{\frac{x}{\_C1}}\right)^{-1}\right\}$$

2.1702 ODE No. 1702

$$e^{2x}\left(ay(x)^4+b\right)+e^x y(x)\left(cy(x)^2+d\right)+y(x)y''(x)-y'(x)^2=0$$

✗ **Mathematica** : cpu = 7.33252 (sec), leaf count = 0 , could not solve

```
DSolve[E^x*y[x]*(d + c*y[x]^2) + E^(2*x)*(b + a*y[x]^4) - Derivative[1][y][x]^2 + y[x]*Deriv
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+exp(x)*y(x)*(c*y(x)^2+d)+exp(2*x)*(b+a*y(x)^
```

2.1703 ODE No. 1703

$$y(x)y''(x)-y'(x)^2+y(x)^2(-\log(y(x)))=0$$

✓ **Mathematica** : cpu = 0.0917782 (sec), leaf count = 63

$$\left\{\left\{y(x)\to e^{\frac{1}{2}\left(e^{c_2+x}-c_1e^{-c_2-x}\right)}\right\},\left\{y(x)\to e^{\frac{1}{2}\left(e^{-c_2-x}-c_1e^{c_2+x}\right)}\right\}\right\}$$

✓ **Maple** : cpu = 0.07 (sec), leaf count = 25

$$\left\{y(x)=\mathrm{e}^{-\frac{\mathrm{e}^{2x}}{2\mathrm{e}^{x}}\_C1}\mathrm{e}^{\frac{\_C2}{2\mathrm{e}^{x}}}\right\}$$

2.1704 ODE No. 1704

$$y(x)^2\left(\frac{f''(x)}{f(x)}-\frac{f'(x)^2}{f(x)^2}\right)+f(x)y(x)^3+y(x)y''(x)-y'(x)^2-y'(x)=0$$

✗ **Mathematica** : cpu = 18.3429 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x]^3 - Derivative[1][y][x] - Derivative[1][y][x]^2 + y[x]^2*(-(Derivative[1][f
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2-diff(y(x),x)+f(x)*y(x)^3+y(x)^2*(diff(diff(f
diff(f(x),x)^2/f(x)^2)=0,y(x))
```

2.1705 ODE No. 1705

$$-y(x)f'(x)+f(x)y'(x)+y(x)y''(x)-y'(x)^2-y(x)^3=0$$

✗ **Mathematica** : cpu = 0.231092 (sec), leaf count = 0 , could not solve

```
DSolve[-y[x]^3 - y[x]*Derivative[1][f][x] + f[x]*Derivative[1][y][x] - Derivative[1][y][x]^2
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+f(x)*diff(y(x),x)-diff(f(x),x)*y(x)-
y(x)^3=0,y(x))
```

2.1706 ODE No. 1706

$$-y(x)f''(x)+f'(x)y'(x)+f(x)y(x)^3+y(x)y''(x)-y'(x)^2-y(x)^4=0$$

✗ **Mathematica** : cpu = 0.473108 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x]^3 - y[x]^4 + Derivative[1][f][x]*Derivative[1][y][x] - Derivative[1][y][x]^
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+diff(f(x),x)*diff(y(x),x)-diff(diff(f(x),x),
y(x)^4=0,y(x))
```

2.1707 ODE No. 1707

$$ay(x)y'(x)+by(x)^2+y(x)y''(x)-y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.0717793 (sec), leaf count = 31

$$\left\{\left\{y(x)\to c_2e^{-\frac{bx}{a}-\frac{c_1e^{-ax}}{a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.066 (sec), leaf count = 39

$$\left\{y(x)=1\mathrm{e}^{\frac{\mathrm{e}^{-ax}\_C1}{a}}\mathrm{e}^{\frac{b}{a^2}}\left(\mathrm{e}^{\frac{bx}{a}}\right)^{-1}\left(\mathrm{e}^{\frac{\_C2}{a}}\right)^{-1}\right\}$$

2.1708 ODE No. 1708

$$ay(x)y'(x) - 2ay(x)^2 + by(x)^3 + y(x)y''(x) - y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 46.0999 (sec), leaf count = 0 , could not solve

```
DSolve[-2*a*y[x]^2 + b*y[x]^3 + a*y[x]*Derivative[1][y][x] - Derivative[1][y][x]^2 + y[x]*De
```

✓ **Maple** : cpu = 1.043 (sec), leaf count = 73

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) - \frac{(\_b(\_a))^2 - \_a\,\_b(\_a)\,a - b\_a^3 + 2\,\_a^2 a}{\_a} = 0\right\}, \left\{\right.\right.$$

2.1709 ODE No. 1709

$$2a^2y(x)^2 - (ay(x) - 1)y'(x) + ay(x) - 2b^2y(x)^3 + y(x)y''(x) - y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 61.4858 (sec), leaf count = 0 , could not solve

```
DSolve[a*y[x] + 2*a^2*y[x]^2 - 2*b^2*y[x]^3 - (-1 + a*y[x])*Derivative[1][y][x] - Derivative
```

✓ **Maple** : cpu = 1.977 (sec), leaf count = 84

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) - \frac{2\,b^2\_a^3 - 2\,\_a^2 a^2 + \_a\,\_b(\_a)\,a + (\_b(\_a))^2 - a\_}{\_a}\right.\right.$$

2.1710 ODE No. 1710

$$-y(x)(y(x)+1)\left(b^2y(x)^2 - a^2\right) + (ay(x) - 1)y'(x) + y(x)y''(x) - y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 106.634 (sec), leaf count = 0 , could not solve

```
DSolve[-(y[x]*(1 + y[x])*(-a^2 + b^2*y[x]^2)) + (-1 + a*y[x])*Derivative[1][y][x] - Derivati
```

✓ **Maple** : cpu = 2.734 (sec), leaf count = 91

$$\left\{y(x) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) - \frac{\_a^4b^2 + b^2\_a^3 - \_a^2a^2 - \_a\,\_b(\_a)\,a - \_a\,a^2 + (\_}{\_a}\right.\right.$$

2.1711 ODE No. 1711

$$y(x)^2 \log(y(x)) \left(\cos^2(x) - n^2 \cot^2(x)\right) + y(x)y''(x) - y'(x)^2 + y(x)y'(x)(\tan(x) + \cot(x)) = 0$$

✗ **Mathematica** : cpu = 300.001 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 0.553 (sec), leaf count = 81

$$\left\{ y(x) = 1 \mathrm{e}^{\frac{J_n(\sin(x))\_C1}{\sin(x)\left(J_{n+1}(\sin(x))Y_n(\sin(x)) - J_n(\sin(x))Y_{n+1}(\sin(x))\right)}} \left(\mathrm{e}^{\frac{Y_n(\sin(x))\_C2}{\sin(x)\left(J_{n+1}(\sin(x))Y_n(\sin(x)) - J_n(\sin(x))Y_{n+1}(\sin(x))\right)}} \right)^{-1} \right\}$$

2.1712 ODE No. 1712

$$-f(x)y(x)y'(x) - g(x)y(x)^2 + y(x)y''(x) - y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 10.5896 (sec), leaf count = 70

$$\left\{ \left\{ y(x) \to c_2 \exp\left(\int_1^x \left(c_1 e^{\int_1^{K[3]} f(K[1])\, dK[1]} + e^{\int_1^{K[3]} f(K[1])\, dK[1]} \int_1^{K[3]} g(K[2]) e^{-\int_1^{K[2]} f(K[1])\, dK[1]}\, dK[2] \right) dK[3] \right) \right.$$

✓ **Maple** : cpu = 0.092 (sec), leaf count = 61

$$\left\{ y(x) = \frac{\_C2}{\mathrm{e}^{\_C1 \int \mathrm{e}^{\int f(x)\,\mathrm{d}x}\,\mathrm{d}x}} \mathrm{e}^{\int \mathrm{e}^{\int f(x)\,\mathrm{d}x}\,\mathrm{d}x \int \frac{g(x)}{\mathrm{e}^{\int f(x)\,\mathrm{d}x}}\,\mathrm{d}x} \left(\mathrm{e}^{\int \frac{\int \mathrm{e}^{\int f(x)\,\mathrm{d}x}\,\mathrm{d}x g(x)}{\mathrm{e}^{\int f(x)\,\mathrm{d}x}}\,\mathrm{d}x} \right)^{-1} \right\}$$

2.1713 ODE No. 1713

$$-y(x)\left(g'(x) - y(x)^2 f'(x)\right) + y'(x)\left(f(x)y(x)^2 + g(x)\right) + y(x)y''(x) - y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 20.9776 (sec), leaf count = 0 , could not solve

```
DSolve[-(y[x]*(-(y[x]^2*Derivative[1][f][x]) + Derivative[1][g][x])) + (g[x] + f[x]*y[x]^2)*
```

✓ **Maple** : cpu = 0.333 (sec), leaf count = 54

$$\left\{ y(x) = \mathit{ODESolStruc}\left(\_b(\_a), \left[\left\{ \frac{f(\_a)\left(\_b(\_a)\right)^2 + \_C1\ \_b(\_a) - g(\_a) + \frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)}{\_b\left(\_a\right)} = 0 \right\}, \{\_a = x, \_\right.\right.\right.$$

2.1714 ODE No. 1714

$$y(x)y''(x)+3y(x)y'(x)-3y'(x)^2-y(x)^2=0$$

✓ **Mathematica** : cpu = 0.0653531 (sec), leaf count = 25

$$\left\{\left\{y(x)\to \frac{c_2 e^x}{\sqrt{1-2e^{c_1+x}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 68

$$\left\{y(x)=\frac{1}{2\,\mathrm{e}^{-x}\_C1-2\,\_C2}\sqrt{-2\,(\mathrm{e}^{-x}\_C1-\_C2)\,\mathrm{e}^{x}},y(x)=-\frac{1}{2\,\mathrm{e}^{-x}\_C1-2\,\_C2}\sqrt{-2\,(\mathrm{e}^{-x}\_C1-\_C2)\,\mathrm{e}^{x}}\right\}$$

2.1715 ODE No. 1715

$$y(x)y''(x)-ay'(x)^2=0$$

✓ **Mathematica** : cpu = 0.0368687 (sec), leaf count = 26

$$\left\{\left\{y(x)\to c_2(-ax-c_1+x)^{\frac{1}{1-a}}\right\}\right\}$$

✓ **Maple** : cpu = 0.045 (sec), leaf count = 25

$$\left\{y(x)=\left(\frac{1}{(1-a)\,(\_C1\,x+\_C2)}\right)^{(a-1)^{-1}}\right\}$$

2.1716 ODE No. 1716

$$a(y'(x)^2+1)+y(x)y''(x)=0$$

✓ **Mathematica** : cpu = 0.679589 (sec), leaf count = 172

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\frac{\#1\sqrt{1-e^{2c_1}\#1^{-2a}}\,{}_2F_1\left(\frac{1}{2},-\frac{1}{2a};1-\frac{1}{2a};e^{2c_1}\#1^{-2a}\right)}{\sqrt{e^{2c_1}\#1^{-2a}-1}}\&\right][c_2+x]\right\},\left\{y(x)\to \text{Invers}\right.\right.$$

✓ **Maple** : cpu = 0.216 (sec), leaf count = 68

$$\left\{\int^{y(x)}\frac{1}{\_a^{-a}}\frac{1}{\sqrt{-\_a^{2\,a}+\_C1}}d\_a-x-\_C2=0,\int^{y(x)}-\frac{1}{\_a^{-a}}\frac{1}{\sqrt{-\_a^{2\,a}+\_C1}}d\_a-x-\_C2=0\right\}$$

2.1717 ODE No. 1717

$$ay'(x)^2+by(x)^3+y(x)y''(x)=0$$

✓ **Mathematica** : cpu = 1.59164 (sec), leaf count = 290

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\frac{\sqrt{2a+3}\#1^{a+1}\sqrt{\frac{-2b\#1^{2a+3}+2ac_1+3c_1}{(2a+3)c_1}}\,{}_2F_1\left(\frac{1}{2},\frac{a+1}{2a+3};\frac{a+1}{2a+3}+1;\frac{2b\#1^{2a+3}}{2ac_1+3c_1}\right)}{(a+1)\sqrt{-2b\#1^{2a+3}+2ac_1+3c_1}}\&\right][c_2+x]\right.\right.$$

✓ **Maple** : cpu = 0.272 (sec), leaf count = 107

$$\left\{\int^{y(x)}(2\,a+3)\_a^{2\,a}\frac{1}{\sqrt{-(2\,a+3)\_a^{2\,a}\,(2\,\_a^{2\,a+3}b-\_C1)}}d\_a-x-\_C2=0,\int^{y(x)}(-2\,a-3)\_a^{2\,a}\frac{}{\sqrt{-(2}}\right.$$

2.1718 ODE No. 1718

$$dy(x)^{1-a}+ay'(x)^2+by(x)y'(x)+cy(x)^2+y(x)y''(x)=0$$

✓ **Mathematica** : cpu = 1.49944 (sec), leaf count = 744

$$\left\{\left\{y(x)\to\left(-\frac{ad\exp\left(\frac{1}{2}x\left(\sqrt{-4ac+b^2-4c}+b\right)-\frac{x\left(b\sqrt{-4ac+b^2-4c}-4(a+1)c+b^2\right)}{\sqrt{-4ac+b^2-4c}+b}-\frac{2(a+1)cx}{\sqrt{-4ac+b^2-4c}+b}\right)}{(a+1)c}-\frac{d\exp\left(\frac{1}{2}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.276 (sec), leaf count = 133

$$\left\{y(x)=\mathrm{e}^{-\frac{x}{2\,a+2}\sqrt{(-4\,a-4)c+b^2}}\mathrm{e}^{-\frac{bx}{2\,a+2}}\left(\left(\left(-4\,a-4\right)c^3+b^2c^2\right)\left(d\mathrm{e}^{\frac{x}{2}\left(b+\sqrt{(-4\,a-4)c+b^2}\right)}\sqrt{\left(-4\,a-4\right)c+b^2}+\left(\mathrm{e}^{x\sqrt{(-\right.}\right.\right.\right.\right.$$

2.1719 ODE No. 1719

$$ay'(x)^2 + f(x)y(x)y'(x) + g(x)y(x)^2 + y(x)y''(x) = 0$$

✗ **Mathematica** : cpu = 41.8843 (sec), leaf count = 0 , could not solve

```
DSolve[g[x]*y[x]^2 + f[x]*y[x]*Derivative[1][y][x] + a*Derivative[1][y][x]^2 + y[x]*Derivati
```

✓ **Maple** : cpu = 0.579 (sec), leaf count = 70

$$\left\{y(x) = ODESolStruc\left(e^{\int \_b(\_a)\,d\_a+\_C1}, [\left\{\frac{d}{d\_a}\_b(\_a) = (-a-1)\,(\_b(\_a))^2 - f(\_a)\,\_b(\_a) - g(\_a)\right\}, \left\{\right.\right.$$

2.1720 ODE No. 1720

$$ay'(x)^2 + by(x)^2y'(x) + cy(x)^4 + y(x)y''(x) = 0$$

✗ **Mathematica** : cpu = 94.966 (sec), leaf count = 0 , could not solve

```
DSolve[c*y[x]^4 + b*y[x]^2*Derivative[1][y][x] + a*Derivative[1][y][x]^2 + y[x]*Derivative[2
```

✓ **Maple** : cpu = 0.339 (sec), leaf count = 173

$$\left\{\int^{y(x)} (2\,a+4)\left(\tan\left(RootOf\left(2\_Z\,b\_a^2 - 2\,\ln(\_a)\,a\sqrt{4\,\_a^4ac - \_a^4b^2 + 8\,c\_a^4} - \sqrt{4\,\_a^4ac - \_a^4b^2 + 8\right.\right.\right.\right.$$

2.1721 ODE No. 1721

$$-\frac{ay(x)^3f'(x)}{a+2} + \frac{af(x)^2y(x)^4}{(a+2)^2} - \frac{(a-1)y'(x)^2}{a} - f(x)y(x)^2y'(x) + y(x)y''(x) = 0$$

✗ **Mathematica** : cpu = 0.971718 (sec), leaf count = 0 , could not solve

```
DSolve[(a*f[x]^2*y[x]^4)/(2 + a)^2 - (a*y[x]^3*Derivative[1][f][x])/(2 + a) - f[x]*y[x]^2*De
1 + a)*Derivative[1][y][x]^2)/a + y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(diff(y(x),x),x)*y(x)-(a-1)/a*diff(y(x),x)^2-f(x)*y(x)^2*diff(y(x),x)+a/(a+2)^2*f
a/(a+2)*diff(f(x),x)*y(x)^3=0,y(x))
```

2.1722 ODE No. 1722

$$-2ay(x)\left(y'(x)^2+1\right)^{3/2}+y(x)y''(x)-y'(x)^2-1=0$$

✓ **Mathematica** : cpu = 1.96443 (sec), leaf count = 797

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\frac{\left(\left(4c_1a^2+\sqrt{8c_1a^2+1}+1\right)E\left(i\sinh^{-1}\left(\sqrt{2}\sqrt{\frac{a^2}{-4c_1a^2+\sqrt{8c_1a^2+1}-1}}\#1\right)|\frac{4c_1a^2-\sqrt{8c_1}}{4c_1a^2+\sqrt{8c_1}}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.44 (sec), leaf count = 98

$$\left\{\int^{y(x)}(\_a^2a+\_C1)\frac{1}{\sqrt{-\_a^4a^2-2\_C1\,\_a^2a-\_C1^2+\_a^2}}d\_a-x-\_C2=0,\int^{y(x)}-(\_a^2a+\_C1)\frac{}{\sqrt{-}}\right.$$

2.1723 ODE No. 1723

$$(y(x)+x)y''(x)+y'(x)^2-y'(x)=0$$

✓ **Mathematica** : cpu = 0.860461 (sec), leaf count = 259

$$\left\{\left\{y(x)\to\frac{1}{2}\left(-\sqrt{2}e^{-2c_1}\sqrt{4e^{3c_1}x+e^{2c_1}-4e^{3c_1}c_2}+e^{-c_1}-4c_2+2x\right)\right\},\left\{y(x)\to\frac{1}{2}\left(\sqrt{2}e^{-2c_1}\sqrt{4e^{3c_1}x+e^{2c_1}-4}\right.\right.\right.$$

✓ **Maple** : cpu = 0.13 (sec), leaf count = 16

$$\left\{y(x)=\sqrt{\_C1+2\,x}\_C2+\_C1+x\right\}$$

2.1724 ODE No. 1724

$$(x-y(x))y''(x)+2y'(x)\left(y'(x)+1\right)=0$$

✓ **Mathematica** : cpu = 0.22443 (sec), leaf count = 38

$$\left\{\left\{y(x)\to-\frac{e^{-c_1}\left(e^{c_1}c_2x+e^{c_1}c_2^2+1\right)}{c_2+x}\right\}\right\}$$

✓ **Maple** : cpu = 0.587 (sec), leaf count = 21

$$\left\{y(x)=\frac{\_C2^2-\_C2\,x+\_C1}{\_C2-x}\right\}$$

2.1725 ODE No. 1725

$$(x-y(x))y''(x)-\left(y'(x)+1\right)\left(y'(x)^2+1\right)=0$$

✓ **Mathematica** : cpu = 0.353025 (sec), leaf count = 75

$$\left\{\left\{y(x)\to -\sqrt{-2c_2x+e^{2c_1}-c_2^2-x^2}-c_2\right\},\left\{y(x)\to \sqrt{-2c_2x+e^{2c_1}-c_2^2-x^2}-c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.577 (sec), leaf count = 105

$$\left\{y(x)=x+RootOf\left(-x+\int^{\_Z}(\_C1^2\_f^2-1)\left(2-\_C1^2\_f^2+\_C1\sqrt{-\_C1^2\_f^2+2}\_f\right)^{-1}d\_f+\_C2\right)\right\}$$

2.1726 ODE No. 1726

$$(x-y(x))y''(x)-h\big(y'(x)\big)=0$$

✓ **Mathematica** : cpu = 0.716853 (sec), leaf count = 75

$$\text{Solve}\left[\left\{x=\int\frac{\exp\left(-\int_1^{\text{K\$13546052}}\frac{K[3]-1}{h(K[3])}\,dK[3]-c_1\right)}{h(\text{K\$13546052})}\,d\text{K\$13546052}+c_2,y(x)=x-\exp\left(-\int_1^{\text{K\$13546052}}\frac{K[3]}{h(K[\right.\right.\right.$$

✓ **Maple** : cpu = 0.112 (sec), leaf count = 39

$$\left\{y(x)=x+RootOf\left(-x+\int^{\_Z}\left(-1+RootOf\left(\int^{\_Z}\frac{\_a-1}{h\left(\_a\right)}d\_a+\ln\left(-\_g\right)+\_C1\right)\right)^{-1}d\_g+\_C2\right)\right\}$$

2.1727 ODE No. 1727

$$2y(x)y''(x)+y'(x)^2+1=0$$

✓ **Mathematica** : cpu = 0.182271 (sec), leaf count = 129

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[e^{2c_1}\tan^{-1}\left(\frac{\sqrt{\#1}}{\sqrt{e^{2c_1}-\#1}}\right)-\sqrt{\#1}\sqrt{e^{2c_1}-\#1}\&\right][c_2+x]\right\},\left\{y(x)\to \text{InverseFunc}\right.\right.$$

✓ **Maple** : cpu = 0.222 (sec), leaf count = 87

$$\left\{-\sqrt{y\left(x\right)\left(\_C1-y\left(x\right)\right)}+\frac{\_C1}{2}\arctan\left(1\left(y(x)-\frac{\_C1}{2}\right)\frac{1}{\sqrt{y\left(x\right)\left(\_C1-y\left(x\right)\right)}}\right)-x-\_C2=0,\sqrt{y\left(x\right)\left(\_\right.}\right.$$

2.1728 ODE No. 1728

$$a + 2y(x)y''(x) - y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.00729527 (sec), leaf count = 31

$$\left\{\left\{y(x) \to \frac{x^2(c_1^2 - a)}{4c_2} + c_1 x + c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 24

$$\left\{y(x) = \frac{(\_C1^2 - a)\,x^2}{4\_C2} + \_C1\,x + \_C2\right\}$$

2.1729 ODE No. 1729

$$a + f(x)y(x)^2 + 2y(x)y''(x) - y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 0.0247177 (sec), leaf count = 0 , could not solve

```
DSolve[a + f[x]*y[x]^2 - Derivative[1][y][x]^2 + 2*y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+f(x)*y(x)^2+a=0,y(x))
```

2.1730 ODE No. 1730

$$2y(x)y''(x) - y'(x)^2 - 8y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.489098 (sec), leaf count = 127

$$\left\{\left\{y(x) \to -\frac{1}{2}i\sqrt{c_1}\,\mathrm{ns}\left(\frac{1}{2}\left(-(-1)^{3/4}\sqrt{2}\sqrt[4]{c_1}x - (-1)^{3/4}\sqrt{2}\sqrt[4]{c_1}c_2\right)\middle| -1\right)^2\right\}, \left\{y(x) \to -\frac{1}{2}i\sqrt{c_1}\,\mathrm{ns}\left(\frac{1}{2}\left((-1)^{3/4}\sqrt{2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.098 (sec), leaf count = 53

$$\left\{\int^{y(x)} \frac{1}{\sqrt{4\_a^3 + \_C1\,\_a}}d\_a - x - \_C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{4\_a^3 + \_C1\,\_a}}d\_a - x - \_C2 = 0\right\}$$

2.1731 ODE No. 1731

$$2y(x)y''(x) - y'(x)^2 - 8y(x)^3 - 4y(x)^2 = 0$$

✓ **Mathematica** : cpu = 1.42277 (sec), leaf count = 359

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{2i\#1\sqrt{\frac{c_1}{\#1(2-2\sqrt{1-c_1})}+1}\sqrt{\frac{c_1}{\#1(2\sqrt{1-c_1}+2)}+1}F\left(i\sinh^{-1}\left(\frac{\sqrt{\frac{c_1}{2\sqrt{1-c_1}+2}}}{\sqrt{\#1}}\right)|\frac{\sqrt{1-c_1}+1}{1-\sqrt{1-c_1}}\right.\right.}{\sqrt{\frac{c_1}{2\sqrt{1-c_1}+2}}\sqrt{4\#1^2+4\#1+c_1}}\right.\right.$$

✓ **Maple** : cpu = 0.102 (sec), leaf count = 61

$$\left\{\int^{y(x)} \frac{1}{\sqrt{4\_a^3+\_a\_C1+4\_a^2}}d\_a - x - \_C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{(4\_a^2+\_C1+4\_a)\_a}}d\_a - x - \_C2 =\right.$$

2.1732 ODE No. 1732

$$2y(x)y''(x) - y'(x)^2 - 4(2y(x)+x)y(x)^2 = 0$$

✗ **Mathematica** : cpu = 1.6926 (sec), leaf count = 0 , could not solve

```
DSolve[-4*y[x]^2*(x + 2*y[x]) - Derivative[1][y][x]^2 + 2*y[x]*Derivative[2][y][x] == 0, y[x
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2-4*(x+2*y(x))*y(x)^2=0,y(x))
```

2.1733 ODE No. 1733

$$y(x)^2(ay(x)+b) + 2y(x)y''(x) - y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 2.56242 (sec), leaf count = 437

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{i\sqrt{2}\#1^{3/2}\sqrt{\frac{4c_1}{\#1\left(\sqrt{2ac_1+b^2}-b\right)}+2}\sqrt{1-\frac{2c_1}{\#1\left(\sqrt{2ac_1+b^2}+b\right)}}F\left(i\sinh^{-1}\left(\frac{\sqrt{2}\sqrt{\frac{c_1}{\sqrt{b^2+2ac_1}}}\right.\right.\right.}{\sqrt{\frac{c_1}{\sqrt{2ac_1+b^2}-b}}\sqrt{-\#1\left(\#1^2a+2\#1b-2c_1\right)}}\right.\right.$$

✓ **Maple** : cpu = 0.101 (sec), leaf count = 71

$$\left\{\int^{y(x)} -2\frac{1}{\sqrt{-2\,a\_a^3-4\,b\_a^2+4\_a\_C1}}d\_a - x - \_C2 = 0, \int^{y(x)} 2\frac{1}{\sqrt{-2\,a\_a^3-4\,b\_a^2+4\_a\_C1}}d\_a -\right.$$

2.1734 ODE No. 1734

$$ay(x)^3 + 2y(x)y''(x) - y'(x)^2 + 2xy(x)^2 + 1 = 0$$

✗ **Mathematica** : cpu = 1.61431 (sec), leaf count = 0 , could not solve

```
DSolve[1 + 2*x*y[x]^2 + a*y[x]^3 - Derivative[1][y][x]^2 + 2*y[x]*Derivative[2][y][x] == 0,
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+1+2*x*y(x)^2+a*y(x)^3=0,y(x))
```

2.1735 ODE No. 1735

$$y(x)^2(ay(x) + bx) + 2y(x)y''(x) - y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 1.48101 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]^2*(b*x + a*y[x]) - Derivative[1][y][x]^2 + 2*y[x]*Derivative[2][y][x] == 0, y[x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+(a*y(x)+b*x)*y(x)^2=0,y(x))
```

2.1736 ODE No. 1736

$$2y(x)y''(x) - y'(x)^2 - 3y(x)^4 = 0$$

✓ **Mathematica** : cpu = 8.48839 (sec), leaf count = 285

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{2i\#1^{3/2}\sqrt{(-1)^{5/6}\left(\frac{\sqrt[3]{-c_1}}{\#1}-1\right)}\sqrt{\frac{(-c_1)^{2/3}}{\#1^2}+\frac{\sqrt[3]{-c_1}}{\#1}+1}F\left(\sin^{-1}\left(\frac{\sqrt{-\frac{i\sqrt[3]{-c_1}}{\#1}-(-1)^{5/6}}}{\sqrt[4]{3}}\right.\right.}{\sqrt[4]{3}\sqrt[3]{-c_1}\sqrt{\#1^3+c_1}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.099 (sec), leaf count = 49

$$\left\{\int^{y(x)}\frac{1}{\sqrt{\_a^4+\_C1\,\_a}}d\_a - x - \_C2 = 0, \int^{y(x)}-\frac{1}{\sqrt{\_a^4+\_C1\,\_a}}d\_a - x - \_C2 = 0\right\}$$

2.1737 ODE No. 1737

$$-4\left(a+x^2\right)y(x)^2+b+2y(x)y''(x)-y'(x)^2-3y(x)^4-8xy(x)^3=0$$

✗ **Mathematica** : cpu = 1.29272 (sec), leaf count = 0 , could not solve

```
DSolve[b - 4*(a + x^2)*y[x]^2 - 8*x*y[x]^3 - 3*y[x]^4 - Derivative[1][y][x]^2 + 2*y[x]*Deriv
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+b-4*(x^2+a)*y(x)^2-8*x*y(x)^3-
3*y(x)^4=0,y(x))
```

2.1738 ODE No. 1738

$$2y(x)^2\left(f'(x)+f(x)^2\right)+3f(x)y(x)y'(x)+2y(x)y''(x)-y'(x)^2-8y(x)^3=0$$

✗ **Mathematica** : cpu = 0.52181 (sec), leaf count = 0 , could not solve

```
DSolve[-8*y[x]^3 + 2*y[x]^2*(f[x]^2 + Derivative[1][f][x]) + 3*f[x]*y[x]*Derivative[1][y][x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+3*f(x)*y(x)*diff(y(x),x)+2*(f(x)^2+diff(f(
8*y(x)^3=0,y(x))
```

2.1739 ODE No. 1739

$$f(x)y(x)^2+2y(x)y''(x)+4y(x)^2y'(x)-y'(x)^2+y(x)^4+1=0$$

✗ **Mathematica** : cpu = 0.0546856 (sec), leaf count = 0 , could not solve

```
DSolve[1 + f[x]*y[x]^2 + y[x]^4 + 4*y[x]^2*Derivative[1][y][x] - Derivative[1][y][x]^2 + 2*y
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*diff(diff(y(x),x),x)*y(x)-diff(y(x),x)^2+4*y(x)^2*diff(y(x),x)+1+f(x)*y(x)^2+y(x)^4
```

2.1740 ODE No. 1740

$$2y(x)y''(x)-3y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.027434 (sec), leaf count = 16

$$\left\{\left\{y(x)\to\frac{c_2}{\left(2c_1+x\right)^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 13

$$\left\{y(x)=4\left(\_C1\,x+\_C2\right)^{-2}\right\}$$

2.1741 ODE No. 1741

$$2y(x)y''(x) - 3y'(x)^2 - 4y(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0940466 (sec), leaf count = 17

$$\{\{y(x) \to c_2 \sec^2(2c_1 + x)\}\}$$

✓ **Maple** : cpu = 0.075 (sec), leaf count = 34

$$\left\{y(x) = 4\left(\left(\_C1^2 - \_C2^2\right)(\sin(x))^2 - 2\,\_C1\,\_C2\,\sin(x)\cos(x) + \_C2^2\right)^{-1}\right\}$$

2.1742 ODE No. 1742

$$f(x)y(x)^2 + 2y(x)y''(x) - 3y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 10.9848 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x]^2 - 3*Derivative[1][y][x]^2 + 2*y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.191 (sec), leaf count = 60

$$\left\{y(x) = ODESolStruc\left(e^{\int \_b(\_a)\,d\_a + \_C1}, [\left\{\frac{d}{d\_a}\_b(\_a) = \frac{(\_b(\_a))^2}{2} - \frac{f(\_a)}{2}\right\}, \left\{\_a = x, \_b(\_a) = \frac{\frac{d}{dx}y(x}{y(x)}\right.\right.$$

2.1743 ODE No. 1743

$$y(x)^2\left(ay(x)^3 + 1\right) + 2y(x)y''(x) - 6y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 18.1073 (sec), leaf count = 2761

$$\left\{\text{Solve}\left[-\frac{4\left(F\left(\sin^{-1}\left(\sqrt{\frac{(\text{Root}[4c_1\#1^4+4a\#1^3+1\&,2]-\text{Root}[4c_1\#1^4+4a\#1^3+1\&,4])(y(x)-\text{Root}[4c_1\#1^4+4a\#1^3+1\&,1])}{(\text{Root}[4c_1\#1^4+4a\#1^3+1\&,1]-\text{Root}[4c_1\#1^4+4a\#1^3+1\&,4])(y(x)-\text{Root}[4c_1\#1^4+4a\#1^3+1\&,2])}}\right)\right|-\right.\right.$$

✓ **Maple** : cpu = 0.111 (sec), leaf count = 71

$$\left\{\int^{y(x)} -2\frac{1}{\sqrt{4\,\_C1\,\_a^4 + 4\,a\,\_a^3 + 1}\,\_a}d\_a - x - \_C2 = 0, \int^{y(x)} 2\frac{1}{\sqrt{4\,\_C1\,\_a^4 + 4\,a\,\_a^3 + 1}\,\_a}d\_a - x - \right.$$

2.1744 ODE No. 1744

$$2y(x)y''(x) - y'(x)^2\left(y'(x)^2+1\right) = 0$$

✓ **Mathematica** : cpu = 0.987371 (sec), leaf count = 173

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-ie^{-c_1}\left(\sqrt{\#1}\sqrt{\#1e^{2c_1}-1} - e^{-c_1}\log\left(\sqrt{\#1}e^{2c_1} + e^{c_1}\sqrt{\#1e^{2c_1}-1}\right)\right)\&\right][c_2+x]\right\},$$

✓ **Maple** : cpu = 0.225 (sec), leaf count = 87

$$\left\{-\frac{\_C1}{2}\arctan\left(1\left(y(x)-\frac{\_C1}{2}\right)\frac{1}{\sqrt{y(x)\left(\_C1-y(x)\right)}}\right) - \sqrt{y(x)\left(\_C1-y(x)\right)} - x - \_C2 = 0, \frac{\_C1}{2}\text{arcta}\right.$$

2.1745 ODE No. 1745

$$2(y(x)-a)y''(x) + y'(x)^2 + 1 = 0$$

✓ **Mathematica** : cpu = 0.311073 (sec), leaf count = 204

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\sqrt{2}\left(\frac{1}{2}\sqrt{a-\#1}\sqrt{e^{2c_1}-2(a-\#1)} - \frac{e^{2c_1}\tan^{-1}\left(\frac{\sqrt{2}\sqrt{a-\#1}}{\sqrt{e^{2c_1}-2(a-\#1)}}\right)}{2\sqrt{2}}\right)\&\right][c_2+x]\right.$$

✓ **Maple** : cpu = 0.386 (sec), leaf count = 117

$$\left\{-\frac{\_C1}{2}\arctan\left(1\left(y(x)-a-\frac{\_C1}{2}\right)\frac{1}{\sqrt{-(-y(x)+a)(a+\_C1-y(x))}}\right) - x - \_C2 + \sqrt{-(-y(x)+a)(a}\right.$$

2.1746 ODE No. 1746

$$-ax^2 - bx - c + 3y(x)y''(x) - 2y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 0.0417676 (sec), leaf count = 0 , could not solve

```
DSolve[-c - b*x - a*x^2 - 2*Derivative[1][y][x]^2 + 3*y[x]*Derivative[2][y][x] == 0, y[x], x
```

✓ **Maple** : cpu = 0.596 (sec), leaf count = 207

$$\left\{y(x) = RootOf\left(-2\int^{-Z}\frac{b}{\sqrt{4\_f^{4/3}\_C1\,b^2 - 36\,c\_f^2 a + 9\,b^2\_f^2 - 2}}d\_f\sqrt{4\,ca-b^2} + \_C2\sqrt{4\,ca-b^2} - 2\,b\,a\right.$$

2.1747 ODE No. 1747

$$3y(x)y''(x) - 5y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0288384 (sec), leaf count = 20

$$\left\{\left\{y(x) \to \frac{c_2}{(3c_1 + 2x)^{3/2}}\right\}\right\}$$

✓ **Maple** : cpu = 0.018 (sec), leaf count = 17

$$\left\{-\frac{3}{2}(y(x))^{-\frac{2}{3}} - \_C1\, x - \_C2 = 0\right\}$$

2.1748 ODE No. 1748

$$4y(x)y''(x) - 3y'(x)^2 + 4y(x) = 0$$

✓ **Mathematica** : cpu = 0.0968893 (sec), leaf count = 43

$$\left\{\left\{y(x) \to \frac{\left(c_1^2x^2 + 2c_2c_1^2x + c_2^2c_1^2 - 64\right)^2}{256c_1^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.125 (sec), leaf count = 67

$$\left\{-4\,\frac{\sqrt{\_C1\ (y(x))^{3/2} + 4\,y(x)}}{\sqrt{y(x)}\_C1} - x - \_C2 = 0, 4\,\frac{\sqrt{\_C1\ (y(x))^{3/2} + 4\,y(x)}}{\sqrt{y(x)}\_C1} - x - \_C2 = 0, y(x) = 0\right\}$$

2.1749 ODE No. 1749

$$4y(x)y''(x) - 3y'(x)^2 - 12y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.552593 (sec), leaf count = 181

$$\left\{\left\{y(x) \to \text{InverseFunction}\left[-\frac{4\sqrt{\frac{4\#1^{3/2}}{c_1} + 1}\sqrt{\#1^{3/2}c_1 + 4\#1^3}\,{}_2F_1\left(\frac{1}{6}, \frac{1}{2}; \frac{7}{6}; -\frac{4\#1^{3/2}}{c_1}\right)}{4\#1^2 + \sqrt{\#1}c_1}\&\right][c_2 + x]\right\}, \left\{y(x) \to \text{I}\right.$$

✓ **Maple** : cpu = 0.289 (sec), leaf count = 57

$$\left\{\int^{y(x)} \frac{1}{\sqrt{\_C1\ \_a^{\frac{3}{2}} + 4\,\_a^3}} d\_a - x - \_C2 = 0, \int^{y(x)} -\frac{1}{\sqrt{\_C1\ \_a^{\frac{3}{2}} + 4\,\_a^3}} d\_a - x - \_C2 = 0\right\}$$

2.1750 ODE No. 1750

$$ay(x)^3+by(x)^2+cy(x)+4y(x)y''(x)-3y'(x)^2=0$$

✓ **Mathematica** : cpu = 3.50727 (sec), leaf count = 2281

$$\left\{\text{Solve}\left[-\frac{4F\left(\sin^{-1}\left(\sqrt{\frac{(\text{Root}[a\#1^4+3b\#1^2-3c_1\#1-3c\&,2]-\text{Root}[a\#1^4+3b\#1^2-3c_1\#1-3c\&,4])\left(\sqrt{y(x)}-\text{Root}[a\#1^4+3b\#1^2-3c_1\right.\right.\right.\right.\right.$$

$$\left.\left.\left.\left.\left.\frac{(\text{Root}[a\#1^4+3b\#1^2-3c_1\#1-3c\&,1]-\text{Root}[a\#1^4+3b\#1^2-3c_1\#1-3c\&,4])\left(\sqrt{y(x)}-\text{Root}[a\#1^4+3b\#1^2-3c_1\right.\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.426 (sec), leaf count = 87

$$\left\{\int^{y(x)}-3\frac{1}{\sqrt{9\_C1\,\_a^{3/2}-3\,a\_a^3-9\,b\_a^2+9\,c\_a}}d\_a-x-\_C2=0,\int^{y(x)}3\frac{1}{\sqrt{9\_C1\,\_a^{3/2}-3\,a\_a^3-9}}\right.$$

2.1751 ODE No. 1751

$$y'(x)\left(6y(x)^2-\frac{2y(x)f'(x)}{f(x)}\right)+f(x)y(x)+g(x)y(x)^2+4y(x)y''(x)-2y(x)^2y'(x)-3y'(x)^2+y(x)^4=0$$

✗ **Mathematica** : cpu = 0.707854 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]*y[x] + g[x]*y[x]^2 + y[x]^4 - 2*y[x]^2*Derivative[1][y][x] + (6*y[x]^2 - (2*y[x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(4*diff(diff(y(x),x),x)*y(x)-3*diff(y(x),x)^2+(6*y(x)^2-2*diff(f(x),x)*y(x)/f(x))*diff
2*y(x)^2*diff(y(x),x)+g(x)*y(x)^2+f(x)*y(x)=0,y(x))
```

2.1752 ODE No. 1752

$$ay(x)^2+4y(x)y''(x)-5y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.128914 (sec), leaf count = 26

$$\left\{\left\{y(x)\to c_2\text{sech}^4\left(\frac{1}{4}\sqrt{a}(x-4c_1)\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.096 (sec), leaf count = 33

$$\left\{y(x)=16\frac{\left(e^{1/4\sqrt{a}x}\right)^4a^2}{\left(e^{1/2\sqrt{a}x}\_C1-\_C2\right)^4}\right\}$$

2.1753 ODE No. 1753

$$12y(x)y''(x) - 15y'(x)^2 + 8y(x)^3 = 0$$

✓ **Mathematica** : cpu = 0.322508 (sec), leaf count = 43

$$\left\{\left\{y(x) \to \frac{2304c_1^2}{\left(3c_1^2x^2 + 6c_2c_1^2x + 3c_2^2c_1^2 + 128\right)^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 147

$$\left\{-12\frac{y(x)\left(8\sqrt{y(x)} - \_C1\right)\sqrt{8y(x) - \_C1\sqrt{y(x)}}}{\sqrt{-24\left(y(x)\right)^3 + 3\_C1\left(y(x)\right)^{5/2}\_C1\sqrt{\sqrt{y(x)}\left(8\sqrt{y(x)} - \_C1\right)}}} - x - \_C2 = 0, 12\frac{y(x)\left(\right.}{\sqrt{-24\left(y(x)\right)^3 +}\right.$$

2.1754 ODE No. 1754

$$ny(x)y''(x) - (n-1)y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0342621 (sec), leaf count = 17

$$\{\{y(x) \to c_2(x - c_1n)^n\}\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 15

$$\left\{y(x) = \left(\frac{\_C1\,x + \_C2}{n}\right)^n\right\}$$

2.1755 ODE No. 1755

$$ay(x)y''(x) + by'(x)^2 + c0 + c1y(x) + c2y(x)^2 + c3y(x)^3 + c4y(x)^4 = 0$$

✗ **Mathematica** : cpu = 104.036 (sec), leaf count = 0 , could not solve

```
DSolve[c0 + c1*y[x] + c2*y[x]^2 + c3*y[x]^3 + c4*y[x]^4 + b*Derivative[1][y][x]^2 + a*y[x]*D
```

✓ **Maple** : cpu = 0.341 (sec), leaf count = 418

$$\left\{\int^{y(x)} \frac{(2a+b)(3a+2b)(a+b)(a+2b)b\_a^{2\frac{b}{a}}}{\sqrt{-36\left(a+2/3\,b\right)b(a+b)(a+b/2)\_a^{2\frac{b}{a}}(a+2b)\left(2/3\,b(a+\right.}}\right.$$

2.1756 ODE No. 1756

$$ay(x)y''(x) + by'(x)^2 - \frac{y(x)y'(x)}{\sqrt{c^2+x^2}} = 0$$

✓ **Mathematica** : cpu = 0.287897 (sec), leaf count = 111

$$\left\{\left\{y(x) \to c_2\left(-a^2\left(x\left(\sqrt{c^2+x^2}+x\right)^{\frac{1}{a}}+c_1\right)+a\left(\sqrt{c^2+x^2}+x\right)^{\frac{1}{a}}\left(\sqrt{c^2+x^2}-bx\right)+b\sqrt{c^2+x^2}\left(\sqrt{c^2+x^2}-\right.\right.\right.$$

✓ **Maple** : cpu = 0.121 (sec), leaf count = 75

$$\left\{y(x) = \left(\left(\frac{a}{a+b}\left(\frac{\_C1\ \sqrt[a]{2}ax^{a^{-1}+1}}{a+1}{}_2\mathrm{F}_1(-\frac{1}{2\,a},-\frac{1}{2\,a}-\frac{1}{2};1-a^{-1};-\frac{c^2}{x^2})+\_C2\right)^{-1}\right)^{\frac{a}{a+b}}\right)^{-1}\right\}$$

2.1757 ODE No. 1757

$$(a+2)f(x)y(x)^2y'(x) + ay(x)y''(x) + ay(x)^3y'(x) - (a-1)y'(x)^2 + f(x)^2y(x)^4 = 0$$

✗ **Mathematica** : cpu = 0.876456 (sec), leaf count = 0 , could not solve

```
DSolve[f[x]^2*y[x]^4 + (2 + a)*f[x]*y[x]^2*Derivative[1][y][x] + a*y[x]^3*Derivative[1][y][x
1 + a)*Derivative[1][y][x]^2 + a*y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(a*y(x)*diff(diff(y(x),x),x)-(a-1)*diff(y(x),x)^2+(a+2)*f(x)*y(x)^2*diff(y(x),x)+f(x)^
```

2.1758 ODE No. 1758

$$y''(x)(ay(x)+b) + cy'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0656587 (sec), leaf count = 36

$$\left\{\left\{y(x) \to \frac{(c_1(-(a+c))\,(-c_2-x))^{\frac{a}{a+c}}-b}{a}\right\}\right\}$$

✓ **Maple** : cpu = 0.059 (sec), leaf count = 42

$$\left\{y(x) = \frac{1}{a}\left((\_C1\,x+\_C2)\,(a+c)\left(\frac{1}{(a+c)\,(\_C1\,x+\_C2)}\right)^{\frac{c}{a+c}}-b\right)\right\}$$

2.1759 ODE No. 1759

$$xy(x)y''(x) + xy'(x)^2 - y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0363487 (sec), leaf count = 18

$$\left\{\left\{y(x) \to c_2\sqrt{c_1 + x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.027 (sec), leaf count = 31

$$\left\{y(x) = \sqrt{\_C1\, x^2 + 2\,\_C2}, y(x) = -\sqrt{\_C1\, x^2 + 2\,\_C2}\right\}$$

2.1760 ODE No. 1760

$$ay(x)y'(x) + f(x) + xy(x)y''(x) + xy'(x)^2 = 0$$

✗ **Mathematica** : cpu = 300.042 (sec), leaf count = 0 , timed out

```
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```

✓ **Maple** : cpu = 0.083 (sec), leaf count = 114

$$\left\{y(x) = \frac{\sqrt{2}}{a-1}\sqrt{(a-1)\left(x^{1-a}\int \frac{x^a f(x)}{x}\,\mathrm{d}x + x^{1-a}\_C1 - \int f(x)\,\mathrm{d}x - \_C2\right)}, y(x) = -\frac{\sqrt{2}}{a-1}\sqrt{(a-1)\left(x^{1-a}\right.}\right.$$

2.1761 ODE No. 1761

$$x\left(ay(x)^4 + d\right) + y(x)\left(by(x)^2 + c\right) + xy(x)y''(x) - xy'(x)^2 + y(x)y'(x) = 0$$

✗ **Mathematica** : cpu = 1.68262 (sec), leaf count = 0 , could not solve

```
DSolve[y[x]*(c + b*y[x]^2) + x*(d + a*y[x]^4) + y[x]*Derivative[1][y][x] - x*Derivative[1][y
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(x*y(x)*diff(diff(y(x),x),x)-x*diff(y(x),x)^2+y(x)*diff(y(x),x)+x*(d+a*y(x)^4)+y(x)*(c
```

2.1762 ODE No. 1762

$$ay(x)y'(x) + bxy(x)^3 + xy(x)y''(x) - xy'(x)^2 = 0$$

✗ **Mathematica** : cpu = 52.6456 (sec), leaf count = 0 , could not solve

```
DSolve[b*x*y[x]^3 + a*y[x]*Derivative[1][y][x] - x*Derivative[1][y][x]^2 + x*y[x]*Derivative
```

✓ **Maple** : cpu = 0.911 (sec), leaf count = 108

$$\left\{ y(x) = ODESolStruc\left(\frac{\_a}{\left(e^{\int \_b(\_a)\,d\_a + \_C1}\right)^2}, [\left\{ \frac{d}{d\_a}\_b(\_a) = -2\,\frac{\_b(\_a)\left(1/2 + \_a^2(-1/2\,b\_a + a - 1)\,(\_\right.}{\_a}\right.\right.$$

2.1763 ODE No. 1763

$$ay(x)y'(x) + xy(x)y''(x) + 2xy'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.139131 (sec), leaf count = 35

$$\left\{\left\{y(x) \to c_2 \exp\left(\frac{1}{3}(\log(3x - (a-1)c_1 x^a) - a\log(x))\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 148

$$\left\{ y(x) = \frac{\sqrt[3]{3}}{(a-1)\,x^a}\sqrt[3]{(x^a)^2\,(a-1)^2\,(\_C2\ (a-1)\,x^a - \_C1\,x)}, y(x) = \frac{\sqrt[3]{3}(i\sqrt{3}-1)}{(2\,a-2)\,x^a}\sqrt[3]{(x^a)^2\,(a-1)^2\,(\_C2\ (a-\right.$$

2.1764 ODE No. 1764

$$xy(x)y''(x) - 2xy'(x)^2 + (y(x)+1)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0615825 (sec), leaf count = 52

$$\left\{\left\{y(x) \to \frac{\tan\left(\frac{1}{2}\left(\sqrt{2}\sqrt{c_1}\log(x) - \sqrt{2}\sqrt{c_1}c_2\right)\right)}{\sqrt{2}\sqrt{c_1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.195 (sec), leaf count = 18

$$\left\{ y(x) = \_C1\ \tanh\left(\frac{\ln(x) - \_C2}{2\,\_C1}\right)\right\}$$

2.1765 ODE No. 1765

$$ay(x)y'(x) + xy(x)y''(x) - 2xy'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.124434 (sec), leaf count = 24

$$\left\{\left\{y(x) \to \frac{c_2 x^a}{(a-1)c_1 x^a + x}\right\}\right\}$$

✓ **Maple** : cpu = 0.03 (sec), leaf count = 27

$$\left\{y(x) = -\frac{(a-1)\,x^a}{\_C2\ (a-1)\,x^a - \_C1\,x}\right\}$$

2.1766 ODE No. 1766

$$xy(x)y''(x) - 4xy'(x)^2 + 4y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0451792 (sec), leaf count = 21

$$\left\{\left\{y(x) \to \frac{c_2 x}{\sqrt[3]{c_1 x^3 + 1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 64

$$\left\{y(x) = x\frac{1}{\sqrt[3]{-3\_C2\,x^3 + \_C1}}, y(x) = \frac{\left(i\sqrt{3}-1\right)x}{2}\frac{1}{\sqrt[3]{-3\_C2\,x^3 + \_C1}}, y(x) = -\frac{\left(i\sqrt{3}+1\right)x}{2}\frac{1}{\sqrt[3]{-3\_C2\,x^3 +}}\right.$$

2.1767 ODE No. 1767

$$\left(\frac{ax}{\sqrt{b^2-x^2}} - x\right)y'(x)^2 + xy(x)y''(x) - y(x)y'(x) = 0$$

✓ **Mathematica** : cpu = 0.0749062 (sec), leaf count = 55

$$\left\{\left\{y(x) \to c_2 \exp\left(\frac{c_1 \log\left(a\sqrt{b^2-x^2} - c_1\right)}{a^2} + \frac{\sqrt{b^2-x^2}}{a}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.345 (sec), leaf count = 50

$$\left\{y(x) = \_C2\,\mathrm{e}^{\int -x\sqrt{b^2-x^2}\left(\_C1\,\sqrt{b^2-x^2}+a\left(b^2-x^2\right)\right)^{-1}\mathrm{d}x}\right\}$$

2.1768 ODE No. 1768

$$x(y(x)+x)y''(x)+xy'(x)^2+(x-y(x))y'(x)-y(x)=0$$

✓ **Mathematica** : cpu = 0.11387 (sec), leaf count = 87

$$\left\{\left\{y(x)\to -x-\sqrt{-e^{2c_2}x^2-2ic_1x^2+e^{2c_2}+x^2}\right\},\left\{y(x)\to -x+\sqrt{-e^{2c_2}x^2-2ic_1x^2+e^{2c_2}+x^2}\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 43

$$\left\{y(x)=-x-\sqrt{(-\_C1+1)\,x^2+\_C2},y(x)=-x+\sqrt{(-\_C1+1)\,x^2+\_C2}\right\}$$

2.1769 ODE No. 1769

$$2xy(x)y''(x)-xy'(x)^2+y(x)y'(x)=0$$

✓ **Mathematica** : cpu = 0.0445233 (sec), leaf count = 18

$$\{\{y(x)\to c_2\left(c_1+\sqrt{x}\right)^2\}\}$$

✓ **Maple** : cpu = 0.035 (sec), leaf count = 21

$$\left\{y(x)=\_C1\,\sqrt{x}\_C2+\_C1^2x+\frac{\_C2^2}{4}\right\}$$

2.1770 ODE No. 1770

$$x^2(y(x)-1)y''(x)-2x^2y'(x)^2-2x(y(x)-1)y'(x)-2(y(x)-1)^2y(x)=0$$

✓ **Mathematica** : cpu = 0.756688 (sec), leaf count = 28

$$\left\{\left\{y(x)\to \frac{1}{x^2\left(-\frac{c_1}{x}+c_2-\frac{1}{x^2}\right)}+1\right\}\right\}$$

✓ **Maple** : cpu = 0.062 (sec), leaf count = 26

$$\left\{y(x)=\frac{x(\_C1\,x-\_C2)}{\_C1\,x^2-\_C2\,x-1}\right\}$$

2.1771 ODE No. 1771

$$x^2(y(x)+x)y''(x)-\left(xy'(x)-y(x)\right)^2=0$$

✓ **Mathematica** : cpu = 0.0809385 (sec), leaf count = 21

$$\left\{\left\{y(x)\to c_2xe^{\frac{c_1}{x}}-x\right\}\right\}$$

✓ **Maple** : cpu = 0.162 (sec), leaf count = 22

$$\left\{y(x)=-\frac{x}{\_C2}\left(-\mathrm{e}^{\frac{\_C1}{x}}\mathrm{e}^{-1}+\_C2\right)\right\}$$

2.1772 ODE No. 1772

$$a\left(xy'(x)-y(x)\right)^2+x^2(x-y(x))y''(x)=0$$

✓ **Mathematica** : cpu = 0.925025 (sec), leaf count = 37

$$\left\{\left\{y(x)\to x\left(\left((a-1)\left(\frac{(-1)^{a+1}c_1}{x}-c_2\right)\right)^{\frac{1}{1-a}}+1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.151 (sec), leaf count = 37

$$\left\{\left(x^ay(x)-x^{a+1}\right)(x-y(x))^{-a}-x(a-1)\_C2+\_C1=0\right\}$$

2.1773 ODE No. 1773

$$2x^2y(x)y''(x)+x^2\left(-\left(y'(x)^2+1\right)\right)+y(x)^2=0$$

✓ **Mathematica** : cpu = 0.1845 (sec), leaf count = 44

$$\left\{\left\{y(x)\to\frac{x\left(c_1^2\log^2(x)-2c_2c_1^2\log(x)+c_2^2c_1^2+4\right)}{4c_1}\right\}\right\}$$

✓ **Maple** : cpu = 0.043 (sec), leaf count = 30

$$\left\{y(x)=\frac{x\left(4\_C2^2(\ln(x))^2+4\_C1\ \ln(x)\_C2+\_C1^2+1\right)}{4\_C2}\right\}$$

2.1774 ODE No. 1774

$$ax^2y(x)y''(x)+bx^2y'(x)^2+cxy(x)y'(x)+dy(x)^2=0$$

✓ **Mathematica** : cpu = 1.36766 (sec), leaf count = 93

$$\left\{\left\{y(x)\to c_2\exp\left(-\frac{\log(x)\left(a\sqrt{\frac{a^2-2ac-4ad-4bd+c^2}{a^2}}-a+c\right)-2a\log\left(x^{\sqrt{\frac{a^2-2ac-4ad-4bd+c^2}{a^2}}}+c_1\right)}{2(a+b)}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.253 (sec), leaf count = 136

$$\left\{y(x)=x^{-\frac{1}{2a+2b}\sqrt{(-4a-4b)d+(a-c)^2}}x^{\frac{a}{2a+2b}}x^{-\frac{c}{2a+2b}}\left(\frac{a^2+(-2c-4d)a-4bd+c^2}{(a+b)^2}\left(x^{\frac{1}{a}\sqrt{(-4a-4b)d+(a-c)^2}}\_C1-\right.\right.\right.$$

2.1775 ODE No. 1775

$$-a(x+2)y(x)^2+x(x+1)^2y(x)y''(x)-x(x+1)^2y'(x)^2+2(x+1)^2y(x)y'(x)=0$$

✓ **Mathematica** : cpu = 0.129846 (sec), leaf count = 29

$$\left\{\left\{y(x)\to c_2e^{\frac{-a-c_1}{x}+a\log(x+1)}\right\}\right\}$$

✓ **Maple** : cpu = 0.1 (sec), leaf count = 31

$$\left\{y(x)=\frac{(1+x)^a}{\_C2\,\mathrm{e}^a}\mathrm{e}^{\frac{\_C1}{x}}\left(\mathrm{e}^{\frac{a}{x}}\right)^{-1}\right\}$$

2.1776 ODE No. 1776

$$8\left(1-x^3\right)y(x)y''(x)-4\left(1-x^3\right)y'(x)^2-12x^2y(x)y'(x)+3xy(x)^2=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
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```

✓ **Maple** : cpu = 0.352 (sec), leaf count = 49

$$\left\{y(x)=\frac{x}{\_C1}\left(\_C1\,LegendreQ\left(-\frac{1}{6},\frac{1}{3},\sqrt{-(x-1)\left(x^2+x+1\right)}\right)+\frac{\_C2}{2}LegendreP\left(-\frac{1}{6},\frac{1}{3},\sqrt{-(x-1)\left(x^2+\right.\right.\right.\right.$$

2.1777 ODE No. 1777

$$\mathrm{f0}(x)y(x)y''(x)+\mathrm{f1}(x)y'(x)^2+\mathrm{f2}(x)y(x)y'(x)+\mathrm{f3}(x)y(x)^2=0$$

✗ **Mathematica** : cpu = 49.037 (sec), leaf count = 0 , could not solve

```
DSolve[f3[x]*y[x]^2 + f2[x]*y[x]*Derivative[1][y][x] + f1[x]*Derivative[1][y][x]^2 + f0[x]*y
```

✓ **Maple** : cpu = 0.74 (sec), leaf count = 79

$$\left\{y(x)=ODESolStruc\left(\mathrm{e}^{\int \_b(\_a)\,\mathrm{d}\_a+\_C1},\left[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=\frac{(-f0(\_a)-f1(\_a))\,(\_b(\_a))^2-f2(\_a)\,\_b(\_a)+\right.\right.\right.}{f0\,(\_a)}$$

2.1778 ODE No. 1778

$$y(x)^2y''(x)-a=0$$

✓ **Mathematica** : cpu = 0.523469 (sec), leaf count = 75

$$\text{Solve}\left[\left(\frac{y(x)\sqrt{c_1-\frac{2a}{y(x)}}}{c_1}+\frac{a\log\left(\sqrt{c_1}y(x)\sqrt{c_1-\frac{2a}{y(x)}}-a+c_1y(x)\right)}{c_1^{3/2}}\right)^2=(c_2+x)^2,y(x)\right]$$

✓ **Maple** : cpu = 0.469 (sec), leaf count = 245

$$\left\{y(x)=\frac{\_C1\left(a\_C1+\mathrm{e}^{RootOf\left(csgn(\_C1^{-1})\_C1^4a^2-2\_Z\_C1^3a\mathrm{e}^{-\_Z}-(\mathrm{e}^{-\_Z})^2csgn(\_C1^{-1})\_C1^2-2\mathrm{e}^{-\_Z}csgn(\_C1^{-1})\_C2-2\right.}\right.}{2\,\mathrm{e}^{RootOf\left(csgn(\_C1^{-1})\_C1^4a^2-2\_Z\_C1^3a\mathrm{e}^{-\_Z}-(\mathrm{e}^{-\_Z})^2csgn(\_C1^{-1})\_C1^2-2\,\mathrm{e}^{-\_Z}csgn(\_C1^{-1})\_C2-2\,\mathrm{e}^{-\_Z}csgn\right.}}$$

2.1779 ODE No. 1779

$$ax+y(x)^2y''(x)+y(x)y'(x)^2=0$$

✗ **Mathematica** : cpu = 3.90707 (sec), leaf count = 0 , could not solve

```
DSolve[a*x + y[x]*Derivative[1][y][x]^2 + y[x]^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.543 (sec), leaf count = 112

$$\left\{\ln(x)-\int^{\frac{y(x)}{x}}\frac{\_g^2}{2\_g^3+2a}\left(\sqrt[3]{\frac{a}{\_g^3}}\sqrt{3}\tan\left(RootOf\left(-2\_Z\sqrt{3}+\ln\left(\frac{(\tan(\_Z))^2+1}{(\tan(\_Z))^2+2\sqrt{3}\tan(\_Z)+3}\right)+6\right.\right.\right.\right.$$

2.1780 ODE No. 1780

$$-ax - b + y(x)^2 y''(x) + y(x)y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 0.489132 (sec), leaf count = 0 , could not solve

```
DSolve[-b - a*x + y[x]*Derivative[1][y][x]^2 + y[x]^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.599 (sec), leaf count = 160

$$\left\{ \frac{b \ln(ax+b)}{a} - \int^{\frac{y(x)}{ax+b}} -\frac{\_g^2 b\sqrt{3}}{6\_g^3 a^2 - 6} \left(-3 \tan\left(RootOf\left(6b^2 \int \frac{\_g^2}{\_g^3 a^2 - 1} \left(-\frac{a}{\_g^3 b^3} \right)^{2/3} \mathrm{d}\_g - 2\_Z\sqrt{3} + \ln \right. \right. \right. \right.$$

2.1781 ODE No. 1781

$$\left(y(x)^2 + 1\right) y''(x) + (1 - 2y(x))y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0806457 (sec), leaf count = 19

$$\{\{y(x) \to \tan(\log(-c_1(-c_2 - x)))\}\}$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 11

$$\{y(x) = \tan(\ln(\_C1\, x + \_C2))\}$$

2.1782 ODE No. 1782

$$\left(y(x)^2 + 1\right) y''(x) - 3y(x)y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.086231 (sec), leaf count = 93

$$\left\{ \left\{ y(x) \to -\frac{ic_1(c_2 + x)}{\sqrt{c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 1}} \right\}, \left\{ y(x) \to \frac{ic_1(c_2 + x)}{\sqrt{c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2 - 1}} \right\} \right\}$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 33

$$\left\{ y(x) = \sqrt{-\left(\_C1^2 x^2 + 2\,\_C1\,\_C2\, x + \_C2^2 - 1\right)^{-1}} (\_C1\, x + \_C2) \right\}$$

2.1783 ODE No. 1783

$$\left(y(x)^2+x\right)y''(x)-2\left(x-y(x)^2\right)y'(x)^3+\left(4y(x)y'(x)+1\right)y'(x)=0$$

✓ **Mathematica** : cpu = 1.37395 (sec), leaf count = 26

$$\text{Solve}\left[x=c_2e^{e^{-c_1}y(x)}-y(x)^2,y(x)\right]$$

✓ **Maple** : cpu = 0.174 (sec), leaf count = 23

$$\left\{\frac{-\_C1\,y(x)+\ln\left(x+(y(x))^2\right)+\_C2+2}{y\left(x\right)}=0\right\}$$

2.1784 ODE No. 1784

$$\left(x^2+y(x)^2\right)y''(x)-\left(xy'(x)-y(x)\right)\left(y'(x)^2+1\right)=0$$

✓ **Mathematica** : cpu = 0.260997 (sec), leaf count = 74

$$\text{Solve}\left[\frac{1}{2}\left(i\cot\left(c_1\right)\left(\log\left(1-\frac{iy(x)}{x}\right)-\log\left(1+\frac{iy(x)}{x}\right)\right)+\log\left(1-\frac{iy(x)}{x}\right)+\log\left(1+\frac{iy(x)}{x}\right)\right)=c_2-\log(x)\right.$$

✓ **Maple** : cpu = 0.569 (sec), leaf count = 82

$$\left\{y(x)=\tan\left(RootOf\left(-\left(\mathrm{e}^{\frac{i\_C1\_Z}{-1+\_C1}}\right)^2\left(\mathrm{e}^{\frac{i\_Z}{-1+\_C1}}\right)^2\left(\mathrm{e}^{\frac{\_C2\_C1}{-1+\_C1}}\right)^2\left(x^{\frac{\_C1}{-1+\_C1}}\right)^2+\left(\mathrm{e}^{\frac{\_C2}{-1+\_C1}}\right)^2\left(x^{(-1+\_C1)^{-1}}\right)^2(\cos(\_\right.\right.\right.\right.$$

2.1785 ODE No. 1785

$$\left(x^2+y(x)^2\right)y''(x)-2\left(xy'(x)-y(x)\right)\left(y'(x)^2+1\right)=0$$

✓ **Mathematica** : cpu = 0.356155 (sec), leaf count = 95

$$\left\{\left\{y(x)\to\frac{1}{2}\left(-\sqrt{4x\left(e^{c_2}-x\right)+e^{2c_2}\cot^2\left(c_1\right)}-e^{c_2}\cot\left(c_1\right)\right)\right\},\left\{y(x)\to\frac{1}{2}\left(\sqrt{4x\left(e^{c_2}-x\right)+e^{2c_2}\cot^2\left(c_1\right)}-e^{c_2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.359 (sec), leaf count = 83

$$\left\{y(x)=\frac{1}{2\_C2}\left(\_C1+1-\sqrt{\_C1^2+\left(4\,i\_C2\,x+2\right)\_C1-4\,\_C2^2x^2-4\,i\_C2\,x+1}\right),y(x)=\frac{1}{2\_C2}\left(\_C\right.\right.$$

2.1786 ODE No. 1786

$$f(x)(1-y(x))y(x)y'(x)+2(1-y(x))y(x)y''(x)-(1-2y(x))y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.993964 (sec), leaf count = 95

$$\left\{\left\{y(x)\to \frac{1}{4}\exp\left(-i\int_1^x c_1\left(-e^{-\int_1^{K[3]}\frac{1}{2}f(K[1])\,dK[1]}\right)dK[3]-ic_2\right)\left(1+\exp\left(i\int_1^x c_1\left(-e^{-\int_1^{K[3]}\frac{1}{2}f(K[1])\,dK[1]}\right)dK[3]+ic_2\right)\right)^2\right\}\right\}$$

✓ **Maple** : cpu = 0.164 (sec), leaf count = 42

$$\left\{y(x)=\frac{1}{8\_C2}\left(2\,\mathrm{e}^{\_C1\int \mathrm{e}^{-1/2\int f(x)\,\mathrm{d}x}\,\mathrm{d}x}\_C2+1\right)^2\left(\mathrm{e}^{\_C1\int \mathrm{e}^{-\frac{\int f(x)\,\mathrm{d}x}{2}}\,\mathrm{d}x}\right)^{-1}\right\}$$

2.1787 ODE No. 1787

$$h(y(x))+2(1-y(x))y(x)y''(x)-(1-3y(x))y'(x)^2=0$$

✗ **Mathematica** : cpu = 100.241 (sec), leaf count = 0 , could not solve

```
DSolve[h[y[x]] - (1 - 3*y[x])*Derivative[1][y][x]^2 + 2*(1 - y[x])*y[x]*Derivative[2][y][x]
```

✓ **Maple** : cpu = 0.283 (sec), leaf count = 80

$$\left\{\int^{y(x)}\frac{1}{\_b-1}\frac{1}{\sqrt{\_b\left(\_C1+\int\frac{h(\_b)}{\_b^2(\_b-1)^3}\,\mathrm{d}\_b\right)}}d\_b-x-\_C2=0,\int^{y(x)}-\frac{1}{\_b-1}\frac{1}{\sqrt{\_b\left(\_C1+\int\frac{h(\_b)}{\_b^2(\_b-1)^3}\right.}}\right.$$

2.1788 ODE No. 1788

$$-4(1-y(x))y(x)^2\left(-f'(x)-f(x)^2-g'(x)+g(x)^2\right)+4y(x)y'(x)(f(x)y(x)+g(x))-2(1-y(x))y(x)y''(x)+(1-3y(x$$

✗ **Mathematica** : cpu = 1.55832 (sec), leaf count = 0 , could not solve

```
DSolve[-4*(1 - y[x])*y[x]^2*(-f[x]^2 + g[x]^2 - Derivative[1][f][x] - Derivative[1][g][x]) +
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{\sqrt{y(x)}-2\frac{\frac{\partial}{\partial x}DESol\left(\left\{-1/4\,\mathrm{e}^{-2\int f(x)\,\mathrm{d}x+2\int g(x)\,\mathrm{d}x}\_C1^2\_Y(x)-2\,g(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\right.}{DESol\left(\left\{-1/4\,\mathrm{e}^{-2\int f(x)\,\mathrm{d}x+2\int g(x)\,\mathrm{d}x}\_C1^2\_Y(x)-2\,g(x)\frac{\mathrm{d}}{\mathrm{d}x}\_Y(x)+\frac{\mathrm{d}^2}{\mathrm{d}x^2}\_Y(x)\right\},\{\_Y(x)\}\right)}\right.$$

2.1789 ODE No. 1789

$$4y(x)^2(1-y(x))\left(-f'(x)+f(x)^2-g'(x)-g(x)^2\right)-4y(x)y'(x)(f(x)y(x)+g(x))+(1-y(x))^3\left(\text{f0}(x)^2y(x)^2-\text{f1}(x)^2\right.$$

✗ **Mathematica** : cpu = 10.2525 (sec), leaf count = 0 , could not solve

```
DSolve[(1 - y[x])^3*(-f1[x]^2 + f0[x]^2*y[x]^2) + 4*(1 - y[x])*y[x]^2*(f[x]^2 - g[x]^2 - Der
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(-2*y(x)*(1-y(x))*diff(diff(y(x),x),x)+(1-3*y(x))*diff(y(x),x)^2-4*y(x)*diff(y(x),x)*(
y(x))^3*(f0(x)^2*y(x)^2-f1(x)^2)+4*y(x)^2*(1-y(x))*(f(x)^2-g(x)^2-diff(g(x),x)-
diff(f(x),x))=0,y(x))
```

2.1790 ODE No. 1790

$$-h(y(x))+3(1-y(x))y(x)y''(x)-2(1-2y(x))y'(x)^2=0$$

✓ **Mathematica** : cpu = 22.6974 (sec), leaf count = 182

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[\int_1^{\#1}-\frac{1}{(1-K[2])^{2/3}K[2]^{2/3}\sqrt{2\int_1^{K[2]}-\frac{h(K[1])\exp\left(-2\left(\frac{2}{3}\log(1-K[1])+\frac{2}{3}\log(K[1])\right)\right)}{3(K[1]-1)K[1]}\,dK[1]}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.255 (sec), leaf count = 119

$$\left\{\int^{y(x)}-\frac{\sqrt{9}}{3}\frac{1}{\sqrt{\sqrt[3]{\_b\,(\_b-1)}\,(\_b-1)\left(\_C1-\frac{2}{3}\int\frac{h(\_b)}{\_b(\_b-1)}\left(\_b^2-\_b\right)^{-\frac{4}{3}}\mathrm{d}\_b\right)\_b}}d\_b-x-\_C2=0,\int^{y(x}\right.$$

2.1791 ODE No. 1791

$$-h(y(x))+(1-y(x))y''(x)-3(1-2y(x))y'(x)^2=0$$

✓ **Mathematica** : cpu = 22.4706 (sec), leaf count = 164

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[\int_1^{\#1}-\frac{e^{\frac{1}{2}(12-12K[2])}}{(K[2]-1)^3\sqrt{2\int_1^{K[2]}-\frac{h(K[1])\exp(-2(6(K[1]-1)+3\log(K[1]-1)))}{K[1]-1}\,dK[1]+c_1}}\right.\right.\right.dK[2]$$

✓ **Maple** : cpu = 0.364 (sec), leaf count = 90

$$\left\{\int^{y(x)}\frac{1}{(\_b-1)^3\left(\mathrm{e}^{-\_b}\right)^6}\frac{1}{\sqrt{-2\int\frac{h(\_b)}{\left(\mathrm{e}^{-\_b}\right)^{12}(\_b-1)^7}\,\mathrm{d}\_b+\_C1}}d\_b-x-\_C2=0,\int^{y(x)}-\frac{1}{(\_b-1)^3\left(\mathrm{e}^{-\_b}\right)^6}\frac{}{\sqrt{-2\int}}\right.$$

2.1792 ODE No. 1792

$$a(y(x)-1)y(x)y''(x)+y'(x)^2(by(x)+c)+h(y(x))=0$$

✓ **Mathematica** : cpu = 25.7312 (sec), leaf count = 222

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[\int_1^{\#1}-\frac{K[2]^{-\frac{c}{a}}(1-K[2])^{\frac{1}{2}\left(\frac{2b}{a}+\frac{2c}{a}\right)}}{\sqrt{2\int_1^{K[2]}-\frac{h(K[1])\exp\left(-\frac{2(c\log(K[1])-(b+c)\log(1-K[1]))}{a}\right)}{a(K[1]-1)K[1]}\,dK[1]+c_1}}dK[2]\&\right][c_2+\right.\right.$$

✓ **Maple** : cpu = 0.905 (sec), leaf count = 194

$$\left\{\int^{y(x)}a\frac{1}{\sqrt{a\left(a\_C1-2\int\frac{h(\_b)}{\_b(\_b-1)}\left((\_b-1)^{\frac{b}{a}}\right)^2\left((\_b-1)^{\frac{c}{a}}\right)^2\left(\_b^{\frac{c}{a}}\right)^{-2}\mathrm{d}\_b\right)}}\left(\_b^{\frac{c}{a}}\right)^{-1}\left((\_b-1)^{\frac{-b-c}{a}}\right)^{-1}d\_\right.$$

2.1793 ODE No. 1793

$$a(y(x)-1)y(x)y''(x)-(a-1)(2y(x)-1)y'(x)^2+f(x)(y(x)-1)y(x)y'(x)=0$$

✓ **Mathematica** : cpu = 1.34266 (sec), leaf count = 113

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[-\frac{a(1-\#1)^{-1/a}(-(\#1-1)\#1)^{\frac{1}{a}}\left((a+1)\,{}_2F_1\left(-\frac{1}{a},\frac{1}{a};1+\frac{1}{a};\#1\right)+\#1\,{}_2F_1\left(1+\frac{1}{a},\right.\right.\right.\right.}{a+1}$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 40

$$\left\{\_C1\,\mathrm{e}^{-\frac{fx}{a}}-\_C2+\int^{y(x)}\frac{\sqrt[a]{\_a\,(\_a-1)}}{\_a\,(\_a-1)}d\_a=0\right\}$$

2.1794 ODE No. 1794

$$ab(y(x)-1)y(x)y''(x)+y'(x)^2(-((2ab-a-b)y(x)+(1-a)b))+f(x)(y(x)-1)y(x)y'(x)=0$$

✓ **Mathematica** : cpu = 1.25569 (sec), leaf count = 98

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[-\frac{a\#1^{\frac{1}{a}}\left((a+1)\,{}_2F_1\left(\frac{1}{a},-\frac{1}{b};1+\frac{1}{a};\#1\right)+\#1\,{}_2F_1\left(1+\frac{1}{a},\frac{b-1}{b};2+\frac{1}{a};\#1\right)\right)}{a+1}\&\right]\left[\int_1^x c_1\right.\right.$$

✓ **Maple** : cpu = 0.093 (sec), leaf count = 46

$$\left\{\_C1\,\mathrm{e}^{-\frac{fx}{ab}}-\_C2+\int^{y(x)}\frac{\sqrt[b]{\_a-1}\sqrt[a]{\_a}}{\_a\,(\_a-1)}d\_a=0\right\}$$

2.1795 ODE No. 1795

$$xy(x)^2y''(x)-a=0$$

✓ **Mathematica** : cpu = 0.25193 (sec), leaf count = 116

$$\text{Solve}\left[-\frac{\sqrt{-\frac{2ay(x)}{x}-\frac{2c_1y(x)^2}{x^2}}}{2c_1}-\frac{a\tan^{-1}\left(\frac{\sqrt{2}\sqrt{c_1}\left(\frac{a}{2c_1}+\frac{y(x)}{x}\right)}{\sqrt{-\frac{2ay(x)}{x}-\frac{2c_1y(x)^2}{x^2}}}\right)}{2\sqrt{2}c_1^{3/2}}-c_2-\frac{1}{x}=0,y(x)\right]$$

✓ **Maple** : cpu = 1.037 (sec), leaf count = 529

$$\left\{y(x)=\frac{x\_C1\left(9\,a\_C1+\mathrm{e}^{RootOf\left(243\,csgn\left(\_C1^{-1}\right)\_C1^4a^2x-54\,\_Z\,\mathrm{e}^{-\_Z}ax\_C1^3-3\,csgn\left(\_C1^{-1}\right)\left(\mathrm{e}^{-\_Z}\right)^2\_C1^2x-6\,csgn\left(\_C1^{-1}\right.\right.}\right.}{2\,\mathrm{e}^{RootOf\left(243\,csgn\left(\_C1^{-1}\right)\_C1^4a^2x-54\,\_Z\,\mathrm{e}^{-\_Z}ax\_C1^3-3\,csgn\left(\_C1^{-1}\right)\left(\mathrm{e}^{-\_Z}\right)^2\_C1^2x-6\,csgn\left(\_C1^{-1}\right)\mathrm{e}^{-\_Z}\_C}}$$

2.1796 ODE No. 1796

$$\left(a^2-x^2\right)\left(a^2-y(x)^2\right)y''(x)+\left(a^2-x^2\right)y(x)y'(x)^2-x\left(a^2-y(x)^2\right)y'(x)=0$$

✓ **Mathematica** : cpu = 0.319618 (sec), leaf count = 66

$$\left\{\left\{y(x)\to\frac{1}{2}e^{-c_2}\left(\sqrt{x^2-a^2}+x\right)^{-c_1}\left(a^2\left(\sqrt{x^2-a^2}+x\right)^{2c_1}+e^{2c_2}\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.227 (sec), leaf count = 51

$$\left\{y(x)=\frac{1}{2\_C2}\left(\left(\left(x+\sqrt{-a^2+x^2}\right)^{-C1}\right)^2\_C2^2+a^2\right)\left(\left(x+\sqrt{-a^2+x^2}\right)^{-C1}\right)^{-1}\right\}$$

2.1797 ODE No. 1797

$$(y(x)-1)^3\left(ay(x)^2+b\right)+cxy(x)^2(y(x)-1)+dx^2y(x)^2(y(x)+1)+2x^2y(x)(y(x)-1)y''(x)-x^2(3y(x)-1)y'(x)^2+2xy$$

✗ **Mathematica** : cpu = 24.1162 (sec), leaf count = 0 , could not solve

```
DSolve[c*x*(-1 + y[x])*y[x]^2 + d*x^2*y[x]^2*(1 + y[x]) + (-1 + y[x])^3*(b + a*y[x]^2) + 2*x
1 + y[x])*y[x]*Derivative[1][y][x] - x^2*(-1 + 3*y[x])*Derivative[1][y][x]^2 + 2*x^2*(-
1 + y[x])*y[x]*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*x^2*y(x)*(-1+y(x))*diff(diff(y(x),x),x)-x^2*(3*y(x)-1)*diff(y(x),x)^2+2*x*y(x)*(-
1+y(x))*diff(y(x),x)+(a*y(x)^2+b)*(-1+y(x))^3+c*x*y(x)^2*(-1+y(x))+d*x^2*y(x)^2*(1+y(x))=0,y
```

2.1798 ODE No. 1798

$$x^3y(x)^2y''(x)+(y(x)+x)\left(xy'(x)-y(x)\right)^3=0$$

✗ **Mathematica** : cpu = 37.964 (sec), leaf count = 0 , could not solve

```
DSolve[(x + y[x])*(-y[x] + x*Derivative[1][y][x])^3 + x^3*y[x]^2*Derivative[2][y][x] == 0, y
```

✓ **Maple** : cpu = 0.242 (sec), leaf count = 166

$$\left\{y(x)=RootOf\left(-2\ln(x)-\int^{\_Z}1\left(iY_{i\sqrt{3}}\left(2\sqrt{\_f}\right)\sqrt{3}\_C1\sqrt{\_f}+i\sqrt{3}J_{i\sqrt{3}}\left(2\sqrt{\_f}\right)\sqrt{\_f}+Y_{i\sqrt{3}}\left(2\sqrt{\_f}\right)\_C\right.\right.\right.$$

2.1799 ODE No. 1799

$$y(x)^3 y''(x) - a = 0$$

✓ **Mathematica** : cpu = 1.88176 (sec), leaf count = 88

$$\left\{\left\{y(x) \to -\frac{\sqrt{a + c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2}}{\sqrt{c_1}}\right\}, \left\{y(x) \to \frac{\sqrt{a + c_1^2 x^2 + 2c_2 c_1^2 x + c_2^2 c_1^2}}{\sqrt{c_1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.135 (sec), leaf count = 46

$$\left\{y(x) = \frac{1}{\_C1}\sqrt{\left((\_C2 + x)^2 \_C1^2 + a\right)\_C1}, y(x) = -\frac{1}{\_C1}\sqrt{\left((\_C2 + x)^2 \_C1^2 + a\right)\_C1}\right\}$$

2.1800 ODE No. 1800

$$y(x)\left(y(x)^2 + 1\right) y''(x) + \left(1 - 3y(x)^2\right) y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.493244 (sec), leaf count = 84

$$\left\{\left\{y(x) \to -\frac{\sqrt{-2c_1 x - 2c_2 c_1 - 1}}{\sqrt{2}\sqrt{c_1 x + c_2 c_1}}\right\}, \left\{y(x) \to \frac{\sqrt{-2c_1 x - 2c_2 c_1 - 1}}{\sqrt{2}\sqrt{c_1 x + c_2 c_1}}\right\}\right\}$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 60

$$\left\{y(x) = \frac{1}{2\_C1\, x + 2\_C2}\sqrt{-4\,(\_C1\, x + \_C2)\,(\_C1\, x + \_C2 + 1/2)}, y(x) = -\frac{1}{2\_C1\, x + 2\_C2}\sqrt{-4\,(\_C1\right.$$

2.1801 ODE No. 1801

$$-a^2 x y(x)^2 + 2y(x)^3 y''(x) + y(x)^4 - 1 = 0$$

✗ **Mathematica** : cpu = 43.8007 (sec), leaf count = 0 , could not solve

```
DSolve[-1 - a^2*x*y[x]^2 + y[x]^4 + 2*y[x]^3*Derivative[2][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*y(x)^3*diff(diff(y(x),x),x)+y(x)^4-a^2*x*y(x)^2-1=0,y(x))
```

2.1802 ODE No. 1802

$$-ax^2 - bx - c + 2y(x)^3y''(x) + y(x)^2y'(x)^2 = 0$$

✗ **Mathematica** : cpu = 0.345374 (sec), leaf count = 0 , could not solve

```
DSolve[-c - b*x - a*x^2 + y[x]^2*Derivative[1][y][x]^2 + 2*y[x]^3*Derivative[2][y][x] == 0,
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*y(x)^3*diff(diff(y(x),x),x)+y(x)^2*diff(y(x),x)^2-a*x^2-b*x-c=0,y(x))
```

2.1803 ODE No. 1803

$$-\text{a0}(a-y(x))^2(b-y(x))^2(c-y(x))^2-\text{a2}(a-y(x))^2(c-y(x))^2-\text{a3}(a-y(x))^2(b-y(x))^2+2(a-y(x))(b-y(x))(c-y(x)$$

✓ **Mathematica** : cpu = 18.3646 (sec), leaf count = 10387

$$\left\{\text{Solve}\left[-\frac{2F\left(\sin^{-1}\left(\sqrt{\frac{(\text{Root}[\text{a0}\#1^4+(-a\text{a0}-b\text{a0}-c\text{a0}-c_1)\#1^3+(-\text{a1}-\text{a2}-\text{a3}+a\text{a0}b+a\text{a0}c+\text{a0}bc+ac_1+bc_1+cc_1)\#1^2+(a\text{a2}+c\text{a2}+a\text{a3}}{(\text{Root}[\text{a0}\#1^4+(-a\text{a0}-b\text{a0}-c\text{a0}-c_1)\#1^3+(-\text{a1}-\text{a2}-\text{a3}+a\text{a0}b+a\text{a0}c+\text{a0}bc+ac_1+bc_1+cc_1)\#1^2+(a\text{a2}+c\text{a2}+a\text{a3}}}\right.\right.}{}\right.\right.$$

✓ **Maple** : cpu = 2.665 (sec), leaf count = 115620

result too large to display

2.1804 ODE No. 1804

$$y''(x)\left(-ay(x) - b + 4y(x)^3\right) - \left(6y(x)^2 - \frac{a}{2}\right)y'(x)^2 = 0$$

✓ **Mathematica** : cpu = 2.92522 (sec), leaf count = 415

$$\text{Solve}\left[\frac{2\sqrt{\frac{y(x)-\text{Root}[4\#1^3-\#1a-b\&,1]}{\text{Root}[4\#1^3-\#1a-b\&,3]-\text{Root}[4\#1^3-\#1a-b\&,1]}}\sqrt{\frac{y(x)-\text{Root}[4\#1^3-\#1a-b\&,2]}{\text{Root}[4\#1^3-\#1a-b\&,3]-\text{Root}[4\#1^3-\#1a-b\&,2]}}\left(y(x)-\text{Root}[4\#1\right.}{c_1\sqrt{2ay(x)+2b-8y(x)^3}\sqrt{}}\right.$$

✓ **Maple** : cpu = 0.034 (sec), leaf count = 31

$$\left\{\int^{y(x)}\frac{1}{\sqrt{4\_a^3 - a\_a - b}}d\_a - \_C1\,x - \_C2 = 0\right\}$$

2.1805 ODE No. 1805

$$\left(-ay(x)-b+4y(x)^3\right)\left(f(x)y'(x)+y''(x)\right)-\left(6y(x)^2-\frac{a}{2}\right)y'(x)^2=0$$

✓ **Mathematica** : cpu = 1.80279 (sec), leaf count = 436

$$\text{Solve}\left[\frac{2\sqrt{\frac{y(x)-\text{Root}\left[4\#1^3-\#1a-b\&,1\right]}{\text{Root}\left[4\#1^3-\#1a-b\&,3\right]-\text{Root}\left[4\#1^3-\#1a-b\&,1\right]}}\sqrt{\frac{y(x)-\text{Root}\left[4\#1^3-\#1a-b\&,2\right]}{\text{Root}\left[4\#1^3-\#1a-b\&,3\right]-\text{Root}\left[4\#1^3-\#1a-b\&,2\right]}}\left(y(x)-\text{Root}\left[4\#1\right.\right.}{\sqrt{ay(x)+b-4y(x)^3}\sqrt{\text{Ro}}}$$

✓ **Maple** : cpu = 0.046 (sec), leaf count = 34

$$\left\{\_C1\,\mathrm{e}^{-fx}-\_C2+\int^{y(x)}\frac{1}{\sqrt{4\_a^3-a\_a-b}}d\_a=0\right\}$$

2.1806 ODE No. 1806

$$-f(x)((y(x)-1)y(x)(y(x)-x))^{3/2}+2(1-y(x))\left(x^2-2xy(x)+y(x)\right)y(x)y'(x)-2(1-x)x(1-y(x))(x-y(x))y(x)y'$$

✗ **Mathematica** : cpu = 19.6804 (sec), leaf count = 0 , could not solve

```
DSolve[-((1 - y[x])^2*y[x]^2) - f[x]*((-1 + y[x])*y[x]*(-x + y[x]))^(3/2) + 2*(1 - y[x])*y[x
```

✓ **Maple** : cpu = 5.365 (sec), leaf count = 718

$$\left\{-\frac{\_C1}{2}\int\frac{1}{x-1}\mathrm{e}^{\int\frac{1}{x(x-1)}EllipticE\left(\sqrt{x}\right)\left(EllipticK\left(\sqrt{x}\right)\right)^{-1}\mathrm{d}x}\int 1\int^{y(x)}\frac{1}{\_a\left(\_a-1\right)\left(-\_a+x\right)^2}\sqrt{-\_a\left(\_a-1\right)\left(-\_\right.}\right.$$

2.1807 ODE No. 1807

$$a(1-y(x))^2(x-y(x))^2y(x)^2+bx(1-y(x))^2(x-y(x))^2-c(1-x)(x-y(x))^2y(x)^2-d(1-x)x(1-y(x))^2y(x)^2+2(1-x)^2$$

✗ **Mathematica** : cpu = 36.4782 (sec), leaf count = 0 , could not solve

```
DSolve[b*x*(1 - y[x])^2*(x - y[x])^2 - d*(1 - x)*x*(1 - y[x])^2*y[x]^2 - c*(1 - x)*(x - y[x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(2*x^2*y(x)*(1-x)^2*(1-y(x))*(x-y(x))*diff(diff(y(x),x),x)-x^2*(1-x)^2*(x-
2*x*y(x)-2*y(x)+3*y(x)^2)*diff(y(x),x)^2-2*x*y(x)*(1-x)*(1-y(x))*(x^2+y(x)-2*x*y(x))*diff(y(
y(x))^2*(x-y(x))^2-c*(1-x)*y(x)^2*(x-y(x))^2-d*x*y(x)^2*(1-x)*(1-y(x))^2+a*y(x)^2*(x-
y(x))^2*(1-y(x))^2=0,y(x))
```

2.1808 ODE No. 1808

$$b\sqrt{(1-y(x)^2)\,(1-a^2y(x)^2)}y'(x)^2+\left(y(x)^2-1\right)\left(a^2y(x)^2-1\right)y''(x)+y(x)\left(-2a^2y(x)^2+a^2+1\right)y'(x)^2=0$$

✓ **Mathematica** : cpu = 103.879 (sec), leaf count = 172

$$\text{Solve}\left[\log(x)-b\left(\frac{\log\left(bc_1\sqrt{1-y(x)^2}\sqrt{1-a^2y(x)^2}+\sqrt{y(x)^2-1}\sqrt{a^2y(x)^2-1}\exp\left(\frac{b\sqrt{1-y(x)^2}\sqrt{1-a^2y(x)^2}F(\sin^{-1}}{\sqrt{y(x)^2-1}\sqrt{a^2y(x)^2-}}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.141 (sec), leaf count = 72

$$\left\{\int^{y(x)}\mathrm{e}^{\int\frac{1}{\left(\_b^2-1\right)\left(\_b^2a^2-1\right)}\left(-2\_b^3a^2+\_b\,a^2+b\sqrt{\left(\_b^2-1\right)\left(\_b^2a^2-1\right)}+\_b\right)\mathrm{d}\_b}d\_b-\_C1\,x-\_C2=0\right\}$$

2.1809 ODE No. 1809

$$y''(x)\left(ax^2+2bx+c+y(x)^2\right)^2+dy(x)=0$$

✗ **Mathematica** : cpu = 45.2806 (sec), leaf count = 0 , could not solve

```
DSolve[d*y[x] + (c + 2*b*x + a*x^2 + y[x]^2)^2*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.705 (sec), leaf count = 336

$$\left\{y(x)=RootOf\left(-\int^{\_Z}\frac{a}{-\_f^4ac+\_f^4b^2+\_C1\,\_f^2a^2-c\_f^2a+b^2\_f^2+\_C1\,a^2+d}\sqrt{\left(\_f^2+1\right)\left(-\_f^4ac-\right.}\right.$$

2.1810 ODE No. 1810

$$\sqrt{y(x)}y''(x)-a=0$$

✓ **Mathematica** : cpu = 0.102789 (sec), leaf count = 1677

$$\left\{\left\{y(x)\to\frac{3c_1^2}{16a^2}+\frac{\sqrt[3]{-\frac{221184c_1^6}{a^6}+\frac{159252480x^2c_1^3}{a^2}+\frac{159252480c_2^2c_1^3}{a^2}+\frac{318504960xc_2c_1^3}{a^2}+2293235712a^2x^4+2293235712a^{\right.}}{\right.}\right.\right.$$

✓ **Maple** : cpu = 0.119 (sec), leaf count = 91

$$\left\{\frac{1}{12\,a^2}\left(-3\_C1\,\sqrt{4\,a\sqrt{y\left(x\right)}-\_C1}-\left(4\,a\sqrt{y\left(x\right)}-\_C1\right)^{\frac{3}{2}}\right)-x-\_C2=0,\frac{1}{12\,a^2}\left(3\_C1\,\sqrt{4\,a\sqrt{y\left(x\right)}-\_\right.\right.$$

2.1811 ODE No. 1811

$$\sqrt{x^2+y(x)^2}y''(x)-a\left(y'(x)^2+1\right)^{3/2}=0$$

✗ **Mathematica** : cpu = 300.022 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 3.85 (sec), leaf count = 1862

$$\left\{y(x)=RootOf\left(-\ln\left(x\right)+\int^{-Z}\frac{1}{\_g^2+1}\left(RootOf\left(\arctan\left(\_g\right)+\int^{-Z}\frac{1}{\left(\_f^2a^2+a^2-1\right)\left(\_f^2+1\right)}\left(1+\sqrt{a^2}\right.\right.\right.\right.$$

2.1812 ODE No. 1812

$$y(x)y''(x)(1-\log(y(x)))+y'(x)^2(\log(y(x))+1)=0$$

✓ **Mathematica** : cpu = 0.0271895 (sec), leaf count = 29

$$\left\{\left\{y(x)\to e^{\frac{c_1x+c_2c_1-1}{c_1(c_2+x)}}\right\}\right\}$$

✓ **Maple** : cpu = 0.037 (sec), leaf count = 19

$$\left\{y(x)=\mathrm{e}^{\frac{\_C1\,x+\_C2-1}{\_C1\,x+\_C2}}\right\}$$

2.1813 ODE No. 1813

$$Ay(x)\left(a\sin^2(y(x))+c\right)+y''(x)\left(a\sin^2(y(x))+b\right)+ay'(x)^2\sin(y(x))\cos(y(x))=0$$

✗ **Mathematica** : cpu = 100.863 (sec), leaf count = 0 , could not solve

```
DSolve[A*(c + a*Sin[y[x]]^2)*y[x] + a*Cos[y[x]]*Sin[y[x]]*Derivative[1][y][x]^2 + (b + a*Sin
```

✓ **Maple** : cpu = 0.421 (sec), leaf count = 138

$$\left\{\int^{y(x)}\sqrt{2}\left(b+a(\sin\left(\_a\right))^2\right)\frac{1}{\sqrt{-\left(a\left(\sin\left(\_a\right)\right)^2A-2\,a\_a\,\sin\left(\_a\right)A\cos\left(\_a\right)+\_a^2\left(a+2\,c\right)A-2\,\_C1\right)\left(b+\right.}}\right.$$

2.1814 ODE No. 1814

$$ah(y(x))y'(x)^2+h(y(x))y''(x)+j(y(x))=0$$

✓ **Mathematica** : cpu = 13.0339 (sec), leaf count = 116

$$\left\{\left\{y(x)\to \text{InverseFunction}\left[\int_1^{\#1}-\frac{e^{aK[2]}}{\sqrt{2\int_1^{K[2]}-\frac{e^{2aK[1]}j(K[1])}{h(K[1])}\,dK[1]+c_1}}\,dK[2]\&\right][c_2+x]\right\},\left\{y(x)\to \text{InverseFu}\right.$$

✓ **Maple** : cpu = 0.183 (sec), leaf count = 87

$$\left\{\int^{y(x)}\frac{1}{(h(\_b))^{-a}}\frac{1}{\sqrt{-2\int\frac{((h(\_b))^a)^2}{h(\_b)}\,\mathrm{d}\_b+\_C1}}d\_b-x-\_C2=0,\int^{y(x)}-\frac{1}{(h(\_b))^{-a}}\frac{1}{\sqrt{-2\int 2\frac{((h(\_b))^a)^2}{h(\_b)}\,\mathrm{d}\_}}\right.$$

2.1815 ODE No. 1815

$$h(y(x))^2\left(-j\left(x,\frac{y'(x)}{h(y(x))}\right)\right)+h(y(x))y''(x)-h(y(x))y'(x)^2=0$$

✗ **Mathematica** : cpu = 1.20666 (sec), leaf count = 0 , could not solve

```
DSolve[-(h[y[x]]^2*j[x, Derivative[1][y][x]/h[y[x]]]) - h[y[x]]*Derivative[1][y][x]^2 + h[y[
```

✓ **Maple** : cpu = 0.999 (sec), leaf count = 71

$$\left\{y(x)=ODESolStruc\left(RootOf\left(\int\_b(\_a)\,\mathrm{d}\_a+\_C1-\int^{\_Z}(h(\_f))^{-1}\,d\_f\right),[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=1\right\},\left\{\_a=\right.\right.\right.$$

2.1816 ODE No. 1816

$$x^2(-y(x))y'(x)+y'(x)y''(x)-xy(x)^2=0$$

✗ **Mathematica** : cpu = 63.6853 (sec), leaf count = 0 , could not solve

```
DSolve[-(x*y[x]^2) - x^2*y[x]*Derivative[1][y][x] + Derivative[1][y][x]*Derivative[2][y][x]
```

✓ **Maple** : cpu = 1.231 (sec), leaf count = 46

$$\left\{y(x)=ODESolStruc\left(\_b(\_a),[\left\{-(\_b(\_a))^2\_a^2+\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)^2+\_C1=0\right\},\{\_a=x,\_b(\_a)=y(x\right.\right.\right.$$

2.1817 ODE No. 1817

$$4y'(x)^2 + \left(xy'(x) - y(x)\right) y''(x) = 0$$

✗ **Mathematica** : cpu = 22.361 (sec), leaf count = 0 , could not solve

```
DSolve[4*Derivative[1][y][x]^2 + (-y[x] + x*Derivative[1][y][x])*Derivative[2][y][x] == 0, y
```

✓ **Maple** : cpu = 0.234 (sec), leaf count = 40

$$\left\{y(x) = \mathrm{e}^{\int^{\ln(x)} \mathrm{e}^{RootOf\left(\ln\left(\mathrm{e}^{\_Z}-1\right)\mathrm{e}^{\_Z}+\_C1\,\mathrm{e}^{\_Z}-\_Z\,\mathrm{e}^{\_Z}-\_b\,\mathrm{e}^{\_Z}+2\right)}-1 d\_b+\_C2}\right\}$$

2.1818 ODE No. 1818

$$\left(xy'(x) - y(x)\right) y''(x) - \left(y'(x)^2 + 1\right)^2 = 0$$

✗ **Mathematica** : cpu = 1.46738 (sec), leaf count = 0 , could not solve

```
DSolve[-(1 + Derivative[1][y][x]^2)^2 + (-y[x] + x*Derivative[1][y][x])*Derivative[2][y][x]
```

✓ **Maple** : cpu = 0.4 (sec), leaf count = 66

$$\left\{y(x) = RootOf\left(-\ln(x) + \int^{-Z} \frac{-\_f + RootOf\left(-\tan\left(\_Z^{-1}\right)\_C1\,\_Z + \_f\,\_C1\,\tan\left(\_Z^{-1}\right) + \tan\left(\_Z^{-1}\right)\right.}{\_f^2+1}\right.$$

2.1819 ODE No. 1819

$$ax^3 y'(x) y''(x) + by(x)^2 = 0$$

✗ **Mathematica** : cpu = 90.7413 (sec), leaf count = 0 , could not solve

```
DSolve[b*y[x]^2 + a*x^3*Derivative[1][y][x]*Derivative[2][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.063 (sec), leaf count = 42

$$\left\{y(x) = \mathrm{e}^{\int^{\ln(x)} RootOf\left(-\int^{-Z} \frac{\_a\_a}{\_a\_a^3 - \_a^2 a + b} d\_a - \_b + \_C1\right) d\_b + \_C2}\right\}$$

2.1820 ODE No. 1820

$$y''(x)\left(\mathrm{f1}(x)y'(x)+\mathrm{f2}(x)y(x)\right)+\mathrm{f3}(x)y'(x)^2+\mathrm{f4}(x)y(x)y'(x)+\mathrm{f5}(x)y(x)^2=0$$

✗ **Mathematica** : cpu = 310.942 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.209 (sec), leaf count = 88

$$\left\{y(x)=ODESolStruc\left(\mathrm{e}^{\int -\_b(\_a)\,\mathrm{d}\_a+\_C1},\left[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=\frac{-(\_b(\_a))^3 f1+(-f2-f3)(\_b(\_a))^2-f4(\_a)\_}{\_b(\_a)f1+f2}\right.\right.\right.$$

2.1821 ODE No. 1821

$$\left(x^2+2y(x)^2y'(x)\right)y''(x)+2y(x)y'(x)^3+3xy'(x)+y(x)=0$$

✗ **Mathematica** : cpu = 42.5419 (sec), leaf count = 0 , could not solve

```
DSolve[y[x] + 3*x*Derivative[1][y][x] + 2*y[x]*Derivative[1][y][x]^3 + (x^2 + 2*y[x]^2*Deriv
```

✓ **Maple** : cpu = 2.286 (sec), leaf count = 54

$$\left\{y(x)=ODESolStruc\left(\_b(\_a),\left[\left\{(\_b(\_a))^2\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)^2+\_a^2\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)+\_a\,\_b(\_a)+\_C1=0\right\}\right.\right.\right.$$

2.1822 ODE No. 1822

$$\left(y'(x)^2+y(x)^2\right)y''(x)+y(x)^3=0$$

✓ **Mathematica** : cpu = 1.0383 (sec), leaf count = 371

$$\left\{\left\{y(x)\to c_2\exp\left(\frac{1}{12}\left(-2\sqrt{3}\tan^{-1}\left(\frac{1+2\mathrm{InverseFunction}\left[\frac{\left(\sqrt{3}-i\right)\tan^{-1}\left(\frac{\#1}{\sqrt{\frac{1}{2}\left(1-i\sqrt{3}\right)}}\right)}{\sqrt{6\left(1-i\sqrt{3}\right)}}+\frac{\left(\sqrt{3}+i\right)\tan^{-1}\left(\frac{\#1}{\sqrt{\frac{1}{2}\left(1+i\sqrt{3}\right)}}\right.}{\sqrt{6\left(1+i\sqrt{3}\right)}}\right.}{\sqrt{3}}\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 1.215 (sec), leaf count = 291

$$\left\{y(x)=\left(\_C1+\tan\left(\sqrt{3}x\right)\right)^{\left(2\_C1^2+2\right)^{-1}}\_C2\left(\_C1+\tan\left(\sqrt{3}x\right)\right)^{\frac{\_C1^2}{2\_C1^2+2}}\left(1+\left(\tan\left(\sqrt{3}x\right)\right)^2\right)^{-\frac{\_C1^2}{4\_C1^2+4}}\left(1\right.\right.$$

2.1823 ODE No. 1823

$$y''(x)\left(a\left(xy'(x)-y(x)\right)+y'(x)^2\right)-b=0$$

✗ **Mathematica** : cpu = 0.164471 (sec), leaf count = 0 , could not solve

```
DSolve[-b + (Derivative[1][y][x]^2 + a*(-y[x] + x*Derivative[1][y][x]))*Derivative[2][y][x]
```

✓ **Maple** : cpu = 0.434 (sec), leaf count = 289

$$\left\{y(x)=-\frac{ax^2}{4}+RootOf\left(-x-\int^{\_Z}\frac{1}{\_f^2a^2-4\_f\,b+2\_C1}\sqrt{\left(\_f^2a^2-4\_f\,b+2\_C1\right)\left(a\_f+\sqrt{4\_f\,b-2\right.}\right.}\right.$$

2.1824 ODE No. 1824

$$y''(x)\left(a\sqrt{y'(x)^2+1}-xy'(x)\right)-y'(x)^2-1=0$$

✓ **Mathematica** : cpu = 0.350175 (sec), leaf count = 347

$$\left\{\left\{y(x)\to\frac{-2\sqrt{x^2\left(a^2+c_1^2-x^2\right)}+c_1x\log\left(-c_1\left(\sqrt{x^2\left(a^2+c_1^2-x^2\right)}+c_1x\right)+a^2(-x)+ax^2\right)+c_1x\log\left(c_1\left(\sqrt{\right.}\right.\right.}{}\right.\right.$$

✓ **Maple** : cpu = 0.988 (sec), leaf count = 96

$$\left\{y(x)=\int\frac{1}{a^3-ax^2}\left(-\_C1\,a^2-x\sqrt{a^2\left(\_C1^2+a^2-x^2\right)}\right)\mathrm{d}x+\_C2,y(x)=\int\frac{1}{a^3-ax^2}\left(-\_C1\,a^2+x\sqrt{a^2\right.}\right.$$

2.1825 ODE No. 1825

$$f(x)+y''(x)h\left(y'(x)\right)+j(y(x))y'(x)=0$$

✗ **Mathematica** : cpu = 0.0413042 (sec), leaf count = 0 , could not solve

```
DSolve[f[x] + j[y[x]]*Derivative[1][y][x] + h[Derivative[1][y][x]]*Derivative[2][y][x] == 0,
```

✓ **Maple** : cpu = 1.053 (sec), leaf count = 49

$$\left\{y(x)=ODESolStruc\left(\_f(\_b),\left[\left\{\int^{\_f(\_b)}1d\_a+\int^{\frac{\mathrm{d}}{\mathrm{d}\_b}\_f(\_b)}h(\_a)\,d\_a+\_b\,f+\_C1=0\right\},\{\_b=x,\_f(\right.\right.\right.$$

2.1826 ODE No. 1826

$$-ay(x) - b + y''(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.596331 (sec), leaf count = 119

$$\left\{\text{Solve}\left[\frac{(ay(x)+b)^2\,{}_2F_1\left(\frac{1}{2},\frac{2}{3};\frac{5}{3};-\frac{4(b+ay(x))^{3/2}}{3ac_1}\right)^2}{a^2c_1} = (c_2+x)^2, y(x)\right], \text{Solve}\left[\frac{(ay(x)+b)^2\,{}_2F_1\left(\frac{1}{2},\frac{2}{3};\frac{5}{3};\frac{4(b+ay(x)}{3ac_1}\right.\right.\right.$$

✓ **Maple** : cpu = 0.375 (sec), leaf count = 173

$$\left\{\int^{y(x)} \sqrt{3}a \frac{1}{\sqrt{a\left(4\_a\sqrt{a\_a+b}a + 4\sqrt{a\_a+b}b - \_C1\right)}} d\_a - x - \_C2 = 0, \int^{y(x)} -3\frac{a}{\sqrt{-12\left((a\_a+b)^{3/2}-\right.}}\right.$$

2.1827 ODE No. 1827

$$a^2y''(x)^2 - 2axy''(x) + y'(x) = 0$$

✗ **Mathematica** : cpu = 0.770927 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x] - 2*a*x*Derivative[2][y][x] + a^2*Derivative[2][y][x]^2 == 0, y[x
```

✓ **Maple** : cpu = 9.289 (sec), leaf count = 81

$$\left\{y(x) = \int RootOf\left(-\int_{\_g}^{\_Z}\left(x\sqrt{x^2-\_f} - x^2 + 2\,a\_f\right)^{-1} \mathrm{d}\_f + \_C1\right)\mathrm{d}x + \_C2, y(x) = \int RootOf\left(-\int_{\_g}^{\_Z}\right.\right.$$

2.1828 ODE No. 1828

$$2\left(x^2+1\right)y''(x)^2 + 2y'(x)\left(y'(x)+x\right) - x\left(4y'(x)+x\right)y''(x) - 2y(x) = 0$$

✓ **Mathematica** : cpu = 0.0102068 (sec), leaf count = 32

$$\left\{\left\{y(x) \to -\frac{1}{2}\sqrt{c_2 - c_1^2}x^2 + c_1x + c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.597 (sec), leaf count = 59

$$\left\{y(x) = \frac{\_C1\,x^2}{2} + \_C2\,x + \_C1^2 + \_C2^2, y(x) = \frac{x}{2}\left(\_C1 + \frac{Arcsinh(x)}{4}\right)\sqrt{x^2+1} - \frac{3\,x^2}{16} + \_C1^2 + \frac{\_C1\,A}{}\right.$$

2.1829 ODE No. 1829

$$3x^2y''(x)^2+4y'(x)^2-2\left(3xy'(x)+y(x)\right)y''(x)=0$$

✓ **Mathematica** : cpu = 0.00648732 (sec), leaf count = 24

$$\left\{\left\{y(x)\to \frac{c_1^2x^2}{c_2}+c_1x+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.391 (sec), leaf count = 32

$$\left\{y(x)=x^{\frac{2\sqrt{3}}{3}}\_C1\,x,y(x)=\frac{\_C1^2x^2}{\_C2}+\_C1\,x+\_C2\right\}$$

2.1830 ODE No. 1830

$$(2-9x)x^2y''(x)^2+6y(x)y''(x)-36xy'(x)^2-6(1-6x)xy'(x)y''(x)=0$$

✓ **Mathematica** : cpu = 0.0281239 (sec), leaf count = 24

$$\left\{\left\{y(x)\to \frac{c_1^2x^3}{c_2}+c_1x+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.552 (sec), leaf count = 304

$$\left\{y(x)=\frac{27\_C1\,\sqrt{5}\sqrt{4x}}{4}\left(\left(9\,x-1\right)\sqrt{9}+9\,\sqrt{9\,x^2-2\,x}\right)^{-\frac{2\sqrt{9}}{9}}\left(\left(9\,x-1\right)\sqrt{9}+9\,\sqrt{9\,x^2-2\,x}\right)^{-\frac{5\sqrt{9}}{18}}\sqrt{1\left(\frac{4}{5}+\sqrt{1}\right.}\right.$$

2.1831 ODE No. 1831

$$y(x)(xF(0,2)+xF(2,0))y''(x)+xF(2,2)y''(x)^2+xF(1,1)y''(x)+y'(x)\left((xF(1,2)+xF(2,1))y''(x)+y(x)(xF(0,1\right.$$

✗ **Mathematica** : cpu = 299.999 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.269 (sec), leaf count = 163

$$\left\{y(x)=ODESolStruc\left(\mathrm{e}^{\int \_b(\_a)\,\mathrm{d}\_a+\_C1},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)=\frac{1}{2\,\left(F_{2,2}\right)(\_a)}\left(\sqrt{\left(\left(\left(F_{2,1}\right)(\_a)\right)^2+2\,\left(F_{1,2}\right)(\_a)\,(F\right.\right.\right.\right.$$

2.1832 ODE No. 1832

$$y(x)y''(x)^2 - ae^{2x} = 0$$

✗ **Mathematica** : cpu = 0.658236 (sec), leaf count = 0 , could not solve

```
DSolve[-(a*E^(2*x)) + y[x]*Derivative[2][y][x]^2 == 0, y[x], x]
```

✓ **Maple** : cpu = 0.976 (sec), leaf count = 117

$$\left\{ y(x) = ODESolStruc\left(\_a \left(e^{-\frac{2\int \_b(\_a)\,d\_a}{3} - \frac{2\_C1}{3}} \right)^{-1}, [\left\{ \frac{d}{d\_a}\_b(\_a) = -\frac{(\_b(\_a))^3}{9\_a}\left(-4\_a^2 + 9\sqrt{a\_a}\right) + \frac{4(\_}{} \right.\right.$$

2.1833 ODE No. 1833

$$y''(x)^2\left(a^2y(x)^2 - b^2\right) + y'(x)^2\left(a^2y'(x)^2 - 1\right) - 2a^2y(x)y'(x)^2y''(x) = 0$$

✗ **Mathematica** : cpu = 300.107 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 3.877 (sec), leaf count = 145

$$\left\{ y(x) = \_C1, y(x) = b\left(e^{\frac{\_C2+x}{b}\sqrt{\_C1^2a^2-1}} - \_C1 \right)\frac{1}{\sqrt{\_C1^2a^2-1}}, y(x) = \frac{b}{a}\tan\left(\frac{\_C1 - x}{ab}\sqrt{a^2} \right)\frac{}{\sqrt{\left(\tan\left(\frac{\_C1}{a}\right.\right.}} \right.$$

2.1834 ODE No. 1834

$$\left(x^2y(x)y''(x) + x^2\left(-y'(x)^2\right) + y(x)^2\right)^2 - 4xy(x)\left(xy'(x) - y(x)\right)^3 = 0$$

✗ **Mathematica** : cpu = 16.9983 (sec), leaf count = 0 , could not solve

```
DSolve[-4*x*y[x]*(-y[x] + x*Derivative[1][y][x])^3 + (y[x]^2 - x^2*Derivative[1][y][x]^2 + x
```

✓ **Maple** : cpu = 0.497 (sec), leaf count = 82

$$\left\{ y(x) = ODESolStruc\left(e^{\int \_b(\_a)\,d\_a + \_C1}, [\left\{ \frac{d}{d\_a}\_b(\_a) = \frac{1}{\_a^2}\left(2\sqrt{\_a\,(\_a\,\_b\,(\_a) - 1)}\_b(\_a)\,\_a - 2\sqrt{\_} \right.\right.\right.$$

2.1835 ODE No. 1835

$$32y''(x)\left(xy''(x)-y'(x)\right)^3+\left(2y(x)y''(x)-y'(x)^2\right)^3=0$$

✓ **Mathematica** : cpu = 0.113418 (sec), leaf count = 143

$$\left\{\left\{y(x)\to\frac{1}{4}\left(-\frac{8c_1^3}{\sqrt[3]{3}\sqrt[3]{\sqrt{3}\sqrt{27c_1^{10}c_2^{10}-64c_1^9c_2^9}-9c_1^5c_2^5}}+\frac{c_1^2}{c_2}-\frac{2\sqrt[3]{\sqrt{3}\sqrt{27c_1^{10}c_2^{10}-64c_1^9c_2^9}-9c_1^5c_2^5}}{3^{2/3}c_2^3}\right)x^2+c_1x+c\right.\right.$$

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.1836 ODE No. 1836

$$\sqrt{ay''(x)^2+by'(x)^2}+cy(x)y''(x)+dy'(x)^2=0$$

✗ **Mathematica** : cpu = 14.4779 (sec), leaf count = 0 , could not solve

```
DSolve[d*Derivative[1][y][x]^2 + c*y[x]*Derivative[2][y][x] + Sqrt[b*Derivative[1][y][x]^2 +
```

✓ **Maple** : cpu = 0.451 (sec), leaf count = 100

$$\left\{y(x)=ODESolStruc\left(\_a,\left[\left\{\frac{\_b(\_a)}{-c^2\_a^2+a}\left(\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\left(-c^2\_a^2+a\right)-\_a\,cd\_b(\_a)+\sqrt{\left(\_b\left(\_a\right)\right)^2ad^2\right.\right.\right.\right.$$

2.1837 ODE No. 1837

$$y^{(3)}(x)-a^2\left(y'(x)^5+2y'(x)^3+y'(x)\right)=0$$

✗ **Mathematica** : cpu = 10.941 (sec), leaf count = 0 , could not solve

```
DSolve[-(a^2*(Derivative[1][y][x] + 2*Derivative[1][y][x]^3 + Derivative[1][y][x]^5)) + Deri
```

✓ **Maple** : cpu = 0.369 (sec), leaf count = 95

$$\left\{y(x)=\int RootOf\left(-3\int^{\_Z}\frac{1}{\sqrt{3\,a^2\_f^6+9\,\_f^4a^2+9\,\_f^2a^2+9\,\_C1}}d\_f+x+\_C2\right)\mathrm{d}x+\_C3,y(x)=\int R\right.$$

2.1838 ODE No. 1838

$$y^{(3)}(x)+y(x)y''(x)-y'(x)^2+1=0$$

✗ **Mathematica** : cpu = 0.0332906 (sec), leaf count = 0 , could not solve

```
DSolve[1 - Derivative[1][y][x]^2 + y[x]*Derivative[2][y][x] + Derivative[3][y][x] == 0, y[x]
```

✓ **Maple** : cpu = 0.657 (sec), leaf count = 73

$$\left\{y(x)=ODESolStruc\left(\_a,[\left\{\left(\frac{\mathrm{d}^2}{\mathrm{d}\_a^2}\_b(\_a)\right)(\_b(\_a))^2+\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)^2\_b(\_a)+\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_\right.\right.$$

2.1839 ODE No. 1839

$$y^{(3)}(x)-y(x)y''(x)+y'(x)^2=0$$

✗ **Mathematica** : cpu = 0.0300543 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x]^2 - y[x]*Derivative[2][y][x] + Derivative[3][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.911 (sec), leaf count = 116

$$\left\{y(x)=ODESolStruc\left(\mathrm{e}^{\int \_g(\_f)\,\mathrm{d}\_f+\_C2},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_f}\_g(\_f)=6\,\frac{\_g(\_f)\,(\_g(\_f)\,\_f+1)\,(1/6+(\_f-1/6)\,\_g(\_}{\_f}\right.\right.$$

2.1840 ODE No. 1840

$$ay(x)y''(x)+y^{(3)}(x)=0$$

✗ **Mathematica** : cpu = 0.0275537 (sec), leaf count = 0 , could not solve

```
DSolve[a*y[x]*Derivative[2][y][x] + Derivative[3][y][x] == 0, y[x], x]
```

✓ **Maple** : cpu = 0.976 (sec), leaf count = 129

$$\left\{y(x)=ODESolStruc\left(\mathrm{e}^{\int \_g(\_f)\,\mathrm{d}\_f+\_C2},[\left\{\frac{\mathrm{d}}{\mathrm{d}\_f}\_g(\_f)=\frac{\_g(\_f)\left(6\,(\_g(\_f))^2\,\_f^2+2\,(\_g(\_f))^2\,\_f\,a+7\_\right.\right.\right.}{\_f}$$

2.1841 ODE No. 1841

$$-f(x)+x^2y^{(3)}(x)+xy''(x)+(2xy(x)-1)y'(x)+y(x)^2=0$$

✗ **Mathematica** : cpu = 0.0869958 (sec), leaf count = 0 , could not solve

```
DSolve[-f[x] + y[x]^2 + (-1 + 2*x*y[x])*Derivative[1][y][x] + x*Derivative[2][y][x] + x^2*De
```

✓ **Maple** : cpu = 0.625 (sec), leaf count = 60

$$\left\{y(x)=ODESolStruc\left(\_b(\_a),[\left\{\_a^2\frac{\mathrm{d}^2}{\mathrm{d}\_a^2}\_b(\_a)+\_a\left(\_b(\_a)\right)^2-\_a\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)-\int f(\_a)\,\mathrm{d}\_a+\_C\right.\right.$$

2.1842 ODE No. 1842

$$x^2y^{(3)}(x)+x(y(x)-1)y''(x)+xy'(x)^2+(1-y(x))y'(x)=0$$

✓ **Mathematica** : cpu = 0.166539 (sec), leaf count = 286

$$\left\{\left\{y(x)\to\frac{2x\left(c_3\left(J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}}\left(-\frac{1}{2}ix\sqrt{c_1}\right)-\frac{1}{4}i\sqrt{c_1}x\left(J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}-1}\left(-\frac{1}{2}ix\sqrt{c_1}\right)-J_{\frac{\sqrt{c_2+2}}{\sqrt{2}}+1}\left(-\frac{1}{2}ix\sqrt{c_1}\right)\right)\right)+Y_{\frac{\sqrt{c_2+2}}{\sqrt{2}}}\left(-\frac{1}{2}\right.\right.\right.}{c_3xJ_{\frac{\sqrt{c_2+2}}{\sqrt{2}}}\left(-\frac{1}{2}ix\sqrt{c_1}\right)+xY_{\frac{\sqrt{c_2+2}}{\sqrt{2}}}\left(-\frac{1}{2}i\right.}$$

✓ **Maple** : cpu = 0.655 (sec), leaf count = 190

$$\left\{\ln(x)+2\int^{y(x)}\left(2\left(RootOf\left(-2\,Y_{1/2\sqrt{4+\_C1}}\left(1/2\sqrt{2}\_Z\right)\sqrt{4+\_C1}\_C2+2\,Y_{1/2\sqrt{4+\_C1}}\left(1/2\sqrt{2}\_Z\right)\_C2\right.\right.\right.\right.$$

2.1843 ODE No. 1843

$$y^{(3)}(x)y(x)+y(x)^3y'(x)-y'(x)y''(x)=0$$

✓ **Mathematica** : cpu = 2.8853 (sec), leaf count = 409

$$\left\{\left\{y(x)\to\text{InverseFunction}\left[-\frac{2i\sqrt{\frac{\#1^2}{2\left(\sqrt{c_2^2-c_1}-c_2\right)}+1}\sqrt{1-\frac{\#1^2}{2\left(c_2+\sqrt{c_2^2-c_1}\right)}}F\left(i\sinh^{-1}\left(\frac{\sqrt{\frac{1}{\sqrt{c_2^2-c_1}-c_2}}\#1}{\sqrt{2}}\right)\right|\frac{c_2-\sqrt{c_2^2}}{c_2+\sqrt{c_2^2}}\right.\right.\right.}{\sqrt{\frac{1}{\sqrt{c_2^2-c_1}-c_2}}\sqrt{-\frac{\#1^4}{2}+2\#1^2c_2-2c_1}}\right.\right.$$

✓ **Maple** : cpu = 0.316 (sec), leaf count = 77

$$\left\{\int^{y(x)}-2\frac{1}{\sqrt{-\_a^4+4\_C2\,\_a^2-4\_C2^2+4\_C1}}d\_a-x-\_C3=0,\int^{y(x)}2\frac{1}{\sqrt{-\_a^4+4\_C2\,\_a^2-4\_C}}\right.$$

2.1844 ODE No. 1844

$$4y(x)^2y^{(3)}(x)+15y'(x)^3-18y(x)y'(x)y''(x)=0$$

✗ **Mathematica** : cpu = 0.0742646 (sec), leaf count = 0 , could not solve

```
DSolve[15*Derivative[1][y][x]^3 - 18*y[x]*Derivative[1][y][x]*Derivative[2][y][x] + 4*y[x]^2
```

✓ **Maple** : cpu = 0.292 (sec), leaf count = 17

$$\left\{y(x)=\frac{\_C3}{\left(-4+\left(\_C2+x\right)^2\_C1\right)^2}\right\}$$

2.1845 ODE No. 1845

$$9y(x)^2y^{(3)}(x)+40y'(x)^3-45y(x)y'(x)y''(x)=0$$

✗ **Mathematica** : cpu = 0.0725492 (sec), leaf count = 0 , could not solve

```
DSolve[40*Derivative[1][y][x]^3 - 45*y[x]*Derivative[1][y][x]*Derivative[2][y][x] + 9*y[x]^2
```

✓ **Maple** : cpu = 0.27 (sec), leaf count = 17

$$\left\{y(x)=\_C3\left(-9+\left(\_C2+x\right)^2\_C1\right)^{-\frac{3}{2}}\right\}$$

2.1846 ODE No. 1846

$$2y^{(3)}(x)y'(x)-3y'(x)^2=0$$

✓ **Mathematica** : cpu = 0.0411539 (sec), leaf count = 51

$$\left\{\{y(x)\to c_1\},\left\{y(x)\to\sqrt{\frac{2}{3}}e^{-\sqrt{\frac{3}{2}}x}\left(c_1e^{\sqrt{6}x}-c_2\right)+c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.011 (sec), leaf count = 28

$$\left\{y(x)=\_C1,y(x)=\_C1+\_C2\,\mathrm{e}^{\frac{\sqrt{6}x}{2}}+\_C3\,\mathrm{e}^{-\frac{\sqrt{6}x}{2}}\right\}$$

2.1847 ODE No. 1847

$$y^{(3)}(x)\left(y'(x)^2+1\right)-3y'(x)y''(x)^2=0$$

✓ **Mathematica** : cpu = 0.123073 (sec), leaf count = 95

$$\left\{\left\{y(x)\to c_3-\frac{i\sqrt{c_1^2x^2+2c_2c_1^2x+c_2^2c_1^2-1}}{c_1}\right\},\left\{y(x)\to c_3+\frac{i\sqrt{c_1^2x^2+2c_2c_1^2x+c_2^2c_1^2-1}}{c_1}\right\}\right\}$$

✓ **Maple** : cpu = 0.27 (sec), leaf count = 49

$$\left\{y(x)=-\sqrt{-\_C2^2-2\_C2\,x-x^2+\_C1}+\_C3,y(x)=\sqrt{-\_C2^2-2\_C2\,x-x^2+\_C1}+\_C3\right\}$$

2.1848 ODE No. 1848

$$y^{(3)}(x)\left(y'(x)^2+1\right)-y''(x)^2\left(a+3y'(x)\right)=0$$

✗ **Mathematica** : cpu = 299.996 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.503 (sec), leaf count = 789

$$\left\{y(x)=\int\frac{\sin\left(RootOf\left(\mathrm{e}^{2\,a\_Z}\_C1^2\_C2^2a^4+2\,\mathrm{e}^{2\,a\_Z}\_C1^2\_C2\,a^4x+\mathrm{e}^{2\,a\_Z}\_C1^2a^4x^2+2\,\mathrm{e}^{2\,a\_Z}\_C1^2\_C2^{2}\right.\right.}{\cos\left(RootOf\left(\mathrm{e}^{2\,a\_Z}\_C1^2\_C2^2a^4+2\,\mathrm{e}^{2\,a\_Z}\_C1^2\_C2\,a^4x+\mathrm{e}^{2\,a\_Z}\_C1^2a^4x^2+2\,\mathrm{e}^{2\,a\_Z}\_C1^2\_C2\right.\right.}$$

2.1849 ODE No. 1849

$$y^{(3)}(x)y''(x)-a\sqrt{b^2y''(x)^2+1}=0$$

✓ **Mathematica** : cpu = 0.584097 (sec), leaf count = 426

$$\left\{\left\{y(x)\to\frac{\frac{\left(a^2b^4x^2+2ab^4c_1x+b^4c_1^2-1\right)^{3/2}}{3ab^2}+\frac{\sqrt{a^2b^4x^2+2ab^4c_1x+b^4c_1^2-1}}{ab^2}-\frac{c_1\log\left(\sqrt{a^2b^4x^2+2ab^4c_1x+b^4c_1^2-1}+ab^2x+b^2c_1\right)}{a}-x\log}{2ab^3}\right.\right.$$

✓ **Maple** : cpu = 0.19 (sec), leaf count = 197

$$\left\{y(x)=\_C2\,x+\int\frac{1}{2\,b}\left(-1\ln\left(\sqrt{\left(1+b^2\left(\_C1+x\right)a\right)\left(-1+b^2\left(\_C1+x\right)a\right)}+\left(\_C1+x\right)b^4a^2\frac{1}{\sqrt{a^2b^4}}\right)\frac{1}{\sqrt{a^2b^{4}}}\right.\right.$$

2.1850 ODE No. 1850

$$y^{(4)}(x)y'(x) - y^{(3)}(x)y''(x) + y^{(3)}(x)y'(x)^3 = 0$$

✗ **Mathematica** : cpu = 0.08374 (sec), leaf count = 0 , could not solve

```
DSolve[Derivative[1][y][x]^3*Derivative[3][y][x] - Derivative[2][y][x]*Derivative[3][y][x] +
```

✓ **Maple** : cpu = 1.597 (sec), leaf count = 164

$$\left\{ y(x) = ODESolStruc\left(\int \frac{\_j(\_h)}{e^{\int \_j(\_h)\,d\_h + \_C2}\,\_h}\,d\_h + \_C3, [\left\{ \frac{d}{d\_h}\_j(\_h) = \frac{\_j(\_h)\left(12\,(\_j(\_h))^2\,\_h^2 + 3\_\right.\right.\right.$$

2.1851 ODE No. 1851

$$y'(x)^3\left(f'(x)y'(x) + f(x)y''(x)\right) - y''(x)\left(f''(x)y'(x) + 2f'(x)y''(x) + f(x)y^{(3)}(x)\right) + y'(x)\left(f^{(3)}(x)y'(x) + 3f''(x)y\right.$$

✗ **Mathematica** : cpu = 0.841836 (sec), leaf count = 0 , could not solve

```
DSolve[2*q[x]*Sin[y[x]]*Derivative[1][y][x]^2 + Derivative[1][y][x]^3*(Derivative[1][f][x]*D
(Derivative[1][q][x]*Derivative[1][y][x]) + q[x]*Derivative[2][y][x]) - Derivative[2][y][x]*
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve(diff(y(x),x)*(diff(diff(diff(f(x),x),x),x)*diff(y(x),x)+3*diff(diff(f(x),x),x)*diff(d
diff(diff(y(x),x),x)*f*diff(diff(diff(y(x),x),x),x)+diff(y(x),x)^3*(diff(f(x),x)*diff(y(x),x
diff(q(x),x)*diff(y(x),x))*cos(y(x))=0,y(x))
```

2.1852 ODE No. 1852

$$3y^{(4)}(x)y''(x) - 5y^{(3)}(x)^2 = 0$$

✓ **Mathematica** : cpu = 0.0354652 (sec), leaf count = 28

$$\left\{\left\{y(x) \to c_2\left(-\sqrt{3c_1 + 2x}\right) + c_4 x + c_3\right\}\right\}$$

✓ **Maple** : cpu = 0.321 (sec), leaf count = 30

$$\left\{ y(x) = 3\,(\_C2 + x)\,\sqrt{6}\,\_C1^2\sqrt{-\frac{\_C1}{\_C2 + x}} + \_C3\,x + \_C4 \right\}$$

2.1853 ODE No. 1853

$$40y^{(3)}(x)^3+9y^{(5)}(x)y''(x)^2-45y^{(4)}(x)y^{(3)}(x)y''(x)=0$$

✗ **Mathematica** : cpu = 0.0718904 (sec), leaf count = 0 , could not solve

```
DSolve[40*Derivative[3][y][x]^3 - 45*Derivative[2][y][x]*Derivative[3][y][x]*Derivative[4][y
```

✓ **Maple** : cpu = 0.681 (sec), leaf count = 110

$$\left\{y(x)=\int\int RootOf\left(-\int^{\_Z}\left(RootOf\left(-20\ln(\_f)+\int^{\_Z}\_k\left(\mathrm{e}^{RootOf(81\_k^2\mathrm{e}^{-\_Z}+20\,\mathrm{e}^{-\_Z}\ln(\mathrm{e}^{-\_Z}+27)-40\,\mathrm{e}^{-\_Z}\ln(2)-20}\right.\right.\right.\right.$$

2.1854 ODE No. 1854

$$y^{(n)}(x)-f\left(y^{(n-1)}(x)\right)=0$$

✗ **Mathematica** : cpu = 0.0955335 (sec), leaf count = 0 , could not solve

```
DSolve[-f[Derivative[-1 + n][y][x]] + Derivative[n][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
unable to handle ODEs of undefined differential order
```

2.1855 ODE No. 1855

$$y^{(n)}(x)-f\left(y^{(n-2)}(x)\right)=0$$

✗ **Mathematica** : cpu = 0.0328686 (sec), leaf count = 0 , could not solve

```
DSolve[-f[Derivative[-2 + n][y][x]] + Derivative[n][y][x] == 0, y[x], x]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
unable to handle ODEs of undefined differential order
```

2.1856 ODE No. 1856

$$\{x'(t)=ax(t),y'(t)=b\}$$

✓ **Mathematica** : cpu = 0.00625597 (sec), leaf count = 22

$$\{\{x(t)\to c_1e^{at},y(t)\to bt+c_2\}\}$$

✓ **Maple** : cpu = 0.033 (sec), leaf count = 19

$$\{\{x(t)=\_C1\,\mathrm{e}^{at},y(t)=bt+\_C2\}\}$$

2.1857 ODE No. 1857

$$\{x'(t) = ay(t), y'(t) = -ax(t)\}$$

✓ **Mathematica** : cpu = 0.0365144 (sec), leaf count = 39

$$\{\{x(t) \to c_2 \sin(at) + c_1 \cos(at), y(t) \to c_2 \cos(at) - c_1 \sin(at)\}\}$$

✓ **Maple** : cpu = 0.048 (sec), leaf count = 35

$$\{\{x(t) = \_C1 \sin(at) + \_C2 \cos(at), y(t) = -\sin(at) \_C2 + \cos(at) \_C1\}\}$$

2.1858 ODE No. 1858

$$\{x'(t) = ay(t), y'(t) = bx(t)\}$$

✓ **Mathematica** : cpu = 0.0104497 (sec), leaf count = 182

$$\left\{\left\{x(t) \to \frac{1}{2}c_1 e^{-\sqrt{a}\sqrt{b}t}\left(e^{2\sqrt{a}\sqrt{b}t}+1\right) + \frac{\sqrt{a}c_2 e^{-\sqrt{a}\sqrt{b}t}\left(e^{2\sqrt{a}\sqrt{b}t}-1\right)}{2\sqrt{b}}, y(t) \to \frac{\sqrt{b}c_1 e^{-\sqrt{a}\sqrt{b}t}\left(e^{2\sqrt{a}\sqrt{b}t}-1\right)}{2\sqrt{a}} + \frac{1}{2}c_2 e\right.\right.$$

✓ **Maple** : cpu = 0.053 (sec), leaf count = 64

$$\left\{\left\{x(t) = \_C1\, \mathrm{e}^{\sqrt{a}\sqrt{b}t} + \_C2\, \mathrm{e}^{-\sqrt{a}\sqrt{b}t}, y(t) = 1\sqrt{b}\left(\_C1\, \mathrm{e}^{\sqrt{a}\sqrt{b}t} - \_C2\, \mathrm{e}^{-\sqrt{a}\sqrt{b}t}\right)\frac{1}{\sqrt{a}}\right\}\right\}$$

2.1859 ODE No. 1859

$$\{x'(t) = ax(t) - y(t), y'(t) = ay(t) + x(t)\}$$

✓ **Mathematica** : cpu = 0.00674746 (sec), leaf count = 51

$$\{\{x(t) \to c_1 e^{at}\cos(t) - c_2 e^{at}\sin(t), y(t) \to c_1 e^{at}\sin(t) + c_2 e^{at}\cos(t)\}\}$$

✓ **Maple** : cpu = 0.039 (sec), leaf count = 37

$$\{\{x(t) = \mathrm{e}^{at}(\_C1 \sin(t) + \_C2 \cos(t)), y(t) = \mathrm{e}^{at}(\sin(t) \_C2 - \cos(t) \_C1)\}\}$$

2.1860 ODE No. 1860

$$\{x'(t) = ax(t) + by(t), y'(t) = by(t) + cx(t)\}$$

✓ **Mathematica** : cpu = 0.0456982 (sec), leaf count = 696

$$\left\{\left\{x(t) \to \frac{c_1\left(a\left(-e^{\frac{1}{2}t\left(-\sqrt{a^2-2ab+b^2+4bc}+a+b\right)}\right)+ae^{\frac{1}{2}t\left(\sqrt{a^2-2ab+b^2+4bc}+a+b\right)}+be^{\frac{1}{2}t\left(-\sqrt{a^2-2ab+b^2+4bc}+a+b\right)}+\sqrt{a^2}\right.\right.\right.$$

✓ **Maple** : cpu = 0.084 (sec), leaf count = 177

$$\left\{\left\{x(t) = \_C1\,\mathrm{e}^{\frac{t}{2}\left(a+b+\sqrt{b^2+(-2a+4c)b+a^2}\right)}+\_C2\,\mathrm{e}^{\frac{t}{2}\left(a+b-\sqrt{b^2+(-2a+4c)b+a^2}\right)}, y(t) = \frac{1}{2b}\left(-\_C2\left(a-b+\sqrt{b^2+\right.\right.\right.\right.$$

2.1861 ODE No. 1861

$$\{ax'(t) + by'(t) = \alpha x(t) + \beta y(t), bx'(t) - ay'(t) = \beta x(t) - \alpha y(t)\}$$

✓ **Mathematica** : cpu = 0.0130863 (sec), leaf count = 183

$$\left\{\left\{x(t) \to c_2 e^{\frac{t(a\alpha+b\beta)}{a^2+b^2}}\sin\left(\frac{t(a\beta-\alpha b)}{a^2+b^2}\right)+c_1 e^{\frac{t(a\alpha+b\beta)}{a^2+b^2}}\cos\left(\frac{t(a\beta-\alpha b)}{a^2+b^2}\right), y(t) \to c_2 e^{\frac{t(a\alpha+b\beta)}{a^2+b^2}}\cos\left(\frac{t(a\beta-\alpha b)}{a^2+b^2}\right)-\right.\right.$$

✓ **Maple** : cpu = 0.109 (sec), leaf count = 152

$$\left\{\left\{x(t) = \_C1\,\mathrm{e}^{\frac{((i\beta+\alpha)a-b(i\alpha-\beta))t}{a^2+b^2}}+\_C2\,\mathrm{e}^{-\frac{((i\beta-\alpha)a-b(i\alpha+\beta))t}{a^2+b^2}}, y(t) = i\left(\_C1\,\mathrm{e}^{\frac{((i\beta+\alpha)a-b(i\alpha-\beta))t}{a^2+b^2}}-\_C2\,\mathrm{e}^{-\frac{((i\beta-\alpha)a-b(i\alpha+\right.\right.\right.$$

2.1862 ODE No. 1862

$$\{x'(t) = -y(t), y'(t) = 2x(t) + 2y(t)\}$$

✓ **Mathematica** : cpu = 0.05656 (sec), leaf count = 52

$$\{\{x(t) \to c_1 e^t(\cos(t) - \sin(t)) - c_2 e^t \sin(t), y(t) \to 2c_1 e^t \sin(t) + c_2 e^t(\sin(t) + \cos(t))\}\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 39

$$\{\{x(t) = \mathrm{e}^t(\sin(t)\,\_C1 + \cos(t)\,\_C2), y(t) = -\mathrm{e}^t((\_C1 + \_C2)\cos(t) + \sin(t)\,(\_C1 - \_C2))\}\}$$

2.1863 ODE No. 1863

$$\{x'(t)+3x(t)+4y(t)=0, 2x(t)+y'(t)+5y(t)=0\}$$

✓ **Mathematica** : cpu = 0.00763349 (sec), leaf count = 84

$$\left\{\left\{x(t)\to \frac{1}{3}c_1e^{-7t}\left(2e^{6t}+1\right)-\frac{2}{3}c_2e^{-7t}\left(e^{6t}-1\right), y(t)\to \frac{1}{3}c_2e^{-7t}\left(e^{6t}+2\right)-\frac{1}{3}c_1e^{-7t}\left(e^{6t}-1\right)\right\}\right\}$$

✓ **Maple** : cpu = 0.038 (sec), leaf count = 35

$$\left\{\left\{x(t)=\_C1\,\mathrm{e}^{-7\,t}+\_C2\,\mathrm{e}^{-t}, y(t)=\_C1\,\mathrm{e}^{-7\,t}-\frac{\_C2\,\mathrm{e}^{-t}}{2}\right\}\right\}$$

2.1864 ODE No. 1864

$$\{x'(t)=-5x(t)-2y(t), y'(t)=x(t)-7y(t)\}$$

✓ **Mathematica** : cpu = 0.0131151 (sec), leaf count = 59

$$\{\{x(t)\to c_1e^{-6t}(\sin(t)+\cos(t))-2c_2e^{-6t}\sin(t), y(t)\to c_1e^{-6t}\sin(t)+c_2e^{-6t}(\cos(t)-\sin(t))\}\}$$

✓ **Maple** : cpu = 0.041 (sec), leaf count = 44

$$\left\{\left\{x(t)=\mathrm{e}^{-6\,t}(\sin(t)\,\_C1+\cos(t)\,\_C2), y(t)=-\frac{\mathrm{e}^{-6\,t}((\_C1-\_C2)\cos(t)-\sin(t)\,(\_C1+\_C2))}{2}\right\}\right\}$$

2.1865 ODE No. 1865

$$\{x'(t)=\mathrm{a1}x(t)+\mathrm{b1}y(t)+\mathrm{c1}, y'(t)=\mathrm{a2}x(t)+\mathrm{b2}y(t)+\mathrm{c2}\}$$

✓ **Mathematica** : cpu = 1.19653 (sec), leaf count = 2062

$$\left\{\left\{x(t)\to -\frac{\mathrm{b1}e^{-\frac{1}{2}\left(\mathrm{a1}+\mathrm{b2}+\sqrt{\mathrm{a1}^2-2\mathrm{b2a1}+\mathrm{b2}^2+4\mathrm{a2b1}}\right)t}\left(\frac{2\left(\left(\mathrm{a1}-\mathrm{b2}+\sqrt{\mathrm{a1}^2-2\mathrm{b2a1}+\mathrm{b2}^2+4\mathrm{a2b1}}\right)\mathrm{c2}-2\mathrm{a2c1}\right)e^{\sqrt{\mathrm{a1}^2-2\mathrm{b2a1}+\mathrm{b2}^2+4\mathrm{a2b1}}t}}{-\mathrm{a1}-\mathrm{b2}+\sqrt{\mathrm{a1}^2-2\mathrm{b2a1}+\mathrm{b2}^2+4\mathrm{a2b1}}}\right.}{2\left(\mathrm{a1}^2\right.}\right.\right.$$

✓ **Maple** : cpu = 0.136 (sec), leaf count = 224

$$\left\{\left\{x(t)=\mathrm{e}^{\frac{t}{2}\left(a1+b2+\sqrt{a1^2-2\,a1\,b2+4\,b1\,a2+b2^2}\right)}\_C2+\mathrm{e}^{\frac{t}{2}\left(a1+b2-\sqrt{a1^2-2\,a1\,b2+4\,b1\,a2+b2^2}\right)}\_C1+\frac{c2\,b1-c1\,b2}{a1\,b2-b1\,a2}, y\right.\right.$$

2.1866 ODE No. 1866

$$\{x'(t) + 2y(t) = 3t, y'(t) - 2x(t) = 4\}$$

✓ **Mathematica** : cpu = 0.0281447 (sec), leaf count = 132

$$\left\{\left\{x(t) \to -c_2 \sin(2t) + c_1 \cos(2t) + \cos(2t)\left(\frac{3}{2}t\sin(2t) - \frac{5}{4}\cos(2t)\right) - \sin(2t)\left(\frac{5}{4}\sin(2t) + \frac{3}{2}t\cos(2t)\right), y(t) \to \right.\right.$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 39

$$\left\{\left\{x(t) = \sin(2\,t)\_C2 + \cos(2\,t)\_C1 - \frac{5}{4}, y(t) = -\cos(2\,t)\_C2 + \sin(2\,t)\_C1 + \frac{3\,t}{2}\right\}\right\}$$

2.1867 ODE No. 1867

$$\{-t^2 + x'(t) + y(t) + 6t + 1 = 0, y'(t) - x(t) = -3t^2 + 3t + 1\}$$

✓ **Mathematica** : cpu = 0.0816527 (sec), leaf count = 124

$$\{\{x(t) \to -c_2 \sin(t) + c_1 \cos(t) + \cos(t)\left(\left(3t^2 - t - 13\right)\cos(t) + (t-12)t\sin(t)\right) - \sin(t)\left(\left(-3t^2 + t + 13\right)\sin(t)\right.\right.$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 42

$$\{\{x(t) = \sin(t)\_C2 + \cos(t)\_C1 + 3\,t^2 - t - 13, y(t) = t^2 - \cos(t)\_C2 + \sin(t)\_C1 - 12\,t\}\}$$

2.1868 ODE No. 1868

$$\{x'(t) + 3x(t) - y(t) = e^{2t}, x(t) + y'(t) + 5y(t) = e^t\}$$

✓ **Mathematica** : cpu = 0.0446468 (sec), leaf count = 162

$$\left\{\left\{x(t) \to c_1 e^{-4t}(t+1) + c_2 e^{-4t}t - e^t(t+1)\left(\frac{t}{5} + \frac{1}{36}e^t(6t-7) - \frac{1}{25}\right) + e^t t\left(\frac{t}{5} + \frac{1}{36}e^t(6t-1) + \frac{4}{25}\right), y(t) \to \right.\right.$$

✓ **Maple** : cpu = 0.073 (sec), leaf count = 64

$$\left\{\left\{x(t) = \mathrm{e}^{-4\,t}\_C2 + \mathrm{e}^{-4\,t}t\_C1 + \frac{7\,\mathrm{e}^{2\,t}}{36} + \frac{\mathrm{e}^t}{25}, y(t) = -\frac{\mathrm{e}^{2\,t}}{36} - \mathrm{e}^{-4\,t}\_C2 - \mathrm{e}^{-4\,t}t\_C1 + \mathrm{e}^{-4\,t}\_C1 + \frac{4\,\mathrm{e}^t}{25}\right\}\right\}$$

2.1869 ODE No. 1869

$$\left\{x'(t)+2x(t)+y'(t)+y(t)=t+e^{2t},x'(t)-x(t)+y'(t)+3y(t)=e^t-1\right\}$$

✓ **Mathematica** : cpu = 0.108355 (sec), leaf count = 118

$$\left\{\left\{x(t)\to \frac{5}{72}\left(c_1e^{-7t/5}+\frac{12\left(5712t+833e^t+2352e^{2t}-5508\right)}{20825}\right)+\frac{1}{5}\left(t-e^t+e^{2t}+1\right),y(t)\to \frac{5}{48}\left(c_1e^{-7t/5}+\right.\right.\right.$$

✓ **Maple** : cpu = 0.06 (sec), leaf count = 51

$$\left\{\left\{x(t)=\frac{5\,\mathrm{e}^{2\,t}}{17}-\frac{\mathrm{e}^t}{6}+\frac{3\,t}{7}-\frac{1}{49}+\mathrm{e}^{-\frac{7\,t}{5}}\_C1,y(t)=-\frac{\mathrm{e}^{2\,t}}{17}+\frac{\mathrm{e}^t}{4}+\frac{t}{7}-\frac{26}{49}+\frac{3\,\_C1}{2}\mathrm{e}^{-\frac{7\,t}{5}}\right\}\right\}$$

2.1870 ODE No. 1870

$$\left\{x'(t)+y'(t)-y(t)=e^t,2x'(t)+y'(t)+2y(t)=\cos(t)\right\}$$

✓ **Mathematica** : cpu = 0.126078 (sec), leaf count = 122

$$\left\{\left\{x(t)\to -\frac{3}{4}c_2\left(e^{4t}-1\right)+c_1+\frac{1}{68}e^{-4t}\left(e^{4t}-1\right)\left(34e^t+3\sin(t)-12\cos(t)\right)+\frac{1}{4}\left(2e^{-3t}+2e^t+\frac{3}{17}e^{-4t}\sin(t)+\right.\right.\right.$$

✓ **Maple** : cpu = 0.113 (sec), leaf count = 47

$$\left\{\left\{x(t)=\frac{5\,\sin\left(t\right)}{17}-\frac{3\,\cos\left(t\right)}{17}+\mathrm{e}^t+\frac{\mathrm{e}^{4\,t}\_C1}{4}+\_C2,y(t)=\frac{4\,\cos\left(t\right)}{17}-\frac{\sin\left(t\right)}{17}-\frac{2\,\mathrm{e}^t}{3}-\frac{\mathrm{e}^{4\,t}\_C1}{3}\right\}\right\}$$

2.1871 ODE No. 1871

$$\left\{4x'(t)+2x(t)+9y'(t)+31y(t)=e^t,3x'(t)+x(t)+7y'(t)+24y(t)=3\right\}$$

✓ **Mathematica** : cpu = 0.160463 (sec), leaf count = 180

$$\left\{\left\{x(t)\to -c_2e^{-4t}\sin(t)+c_1e^{-4t}(\cos(t)-\sin(t))+\frac{1}{442}\left(3\left(153e^t-754\right)\sin(t)+31\left(17e^t-78\right)\cos(t)\right)(\cos(t)-\right.\right.$$

✓ **Maple** : cpu = 0.077 (sec), leaf count = 62

$$\left\{\left\{x(t)=\mathrm{e}^{-4\,t}\sin\left(t\right)\_C2+\mathrm{e}^{-4\,t}\cos\left(t\right)\_C1-\frac{93}{17}+\frac{31\,\mathrm{e}^t}{26},y(t)=\frac{\left(\left(-221\,\_C1-221\,\_C2\right)\cos\left(t\right)+221\,\sin\left(t\right)\right.}{221}\right.\right.$$

2.1872 ODE No. 1872

$$\{4x'(t)+11x(t)+9y'(t)+31y(t)=e^t,3x'(t)+8x(t)+7y'(t)+24y(t)=e^{2t}\}$$

✓ **Mathematica** : cpu = 0.0577196 (sec), leaf count = 162

$$\left\{\left\{x(t)\to -c_1e^{-4t}(t-1)-c_2e^{-4t}t-e^tt\left(-\frac{4t}{5}+\frac{1}{36}e^t(30t+19)-\frac{11}{25}\right)-e^t(t-1)\left(\frac{4t}{5}-\frac{1}{36}e^t(30t+49)+\frac{31}{25}\right.\right.\right.$$

✓ **Maple** : cpu = 0.068 (sec), leaf count = 65

$$\left\{\left\{x(t)=\mathrm{e}^{-4\,t}\_C2+\mathrm{e}^{-4\,t}t\_C1-\frac{49\,\mathrm{e}^{2\,t}}{36}+\frac{31\,\mathrm{e}^t}{25},y(t)=\frac{19\,\mathrm{e}^{2\,t}}{36}-\mathrm{e}^{-4\,t}\_C2-\mathrm{e}^{-4\,t}t\_C1-\mathrm{e}^{-4\,t}\_C1-\frac{11\,\mathrm{e}^t}{25}\right\}\right\}$$

2.1873 ODE No. 1873

$$\{4x'(t)+44x(t)+9y'(t)+49y(t)=t,3x'(t)+34x(t)+7y'(t)+38y(t)=e^t\}$$

✓ **Mathematica** : cpu = 0.0448097 (sec), leaf count = 322

$$\left\{\left\{x(t)\to \frac{1}{5}c_1e^{-6t}\left(4e^{5t}+1\right)-\frac{1}{5}c_2e^{-6t}\left(e^{5t}-1\right)-\frac{1}{5}e^{-6t}\left(e^{5t}-1\right)\left(\frac{16}{5}e^{6t}\left(\frac{t}{6}-\frac{1}{36}\right)+4e^{2t}-\frac{4e^{7t}}{7}-\frac{31}{5}e^t(t-1)\right.\right.\right.$$

✓ **Maple** : cpu = 0.063 (sec), leaf count = 52

$$\left\{\left\{x(t)=\_C2\,\mathrm{e}^{-t}+\mathrm{e}^{-6\,t}\_C1-\frac{56}{9}+\frac{19\,t}{3}-\frac{29\,\mathrm{e}^t}{7},y(t)=-\_C2\,\mathrm{e}^{-t}+4\,\mathrm{e}^{-6\,t}\_C1+\frac{55}{9}+\frac{24\,\mathrm{e}^t}{7}-\frac{17\,t}{3}\right\}\right\}$$

2.1874 ODE No. 1874

$$\{x'(t)=f(t)x(t)+g(t)y(t),y'(t)=f(t)y(t)-g(t)x(t)\}$$

✓ **Mathematica** : cpu = 0.141167 (sec), leaf count = 131

$$\left\{\left\{x(t)\to c_2e^{\text{Integrate}[f(K[2]),\{K[2],1,t\},\text{Assumptions}\to\text{True}]}\sin(\text{Integrate}[g(K[1]),\{K[1],1,t\},\text{Assumptions}\to\text{True}])+\right.\right.$$

✓ **Maple** : cpu = 0.458 (sec), leaf count = 57

$$\left\{\left\{x(t)=\mathrm{e}^{\int\tan(\_C1-\int g(t)\,\mathrm{d}t)g(t)+f(t)\,\mathrm{d}t}\_C2,y(t)=\mathrm{e}^{\int\tan(\_C1-\int g(t)\,\mathrm{d}t)g(t)+f(t)\,\mathrm{d}t}\tan\left(\_C1-\int g(t)\,\mathrm{d}t\right)\_C2\right\}\right\}$$

2.1875 ODE No. 1875

$$\{f(t)(ax(t)+by(t))+x'(t)=g(t), f(t)(cx(t)+dy(t))+y'(t)=h(t)\}$$

✗ **Mathematica** : cpu = 0.00728535 (sec), leaf count = 0 , could not solve

```
DSolve[{f[t]*(a*x[t] + b*y[t]) + Derivative[1][x][t] == g[t], f[t]*(c*x[t] + d*y[t]) + Deriv
```

✓ **Maple** : cpu = 1.264 (sec), leaf count = 1447

$$\left\{\left\{x(t)=1\left(-\int \frac{\left(\frac{\mathrm{d}}{\mathrm{d}t}f(t)\right)g(t)-f(t)\left(\frac{\mathrm{d}}{\mathrm{d}t}g(t)-f(t)\left(bh(t)-g(t)\,d\right)\right)}{\left(f\left(t\right)\right)^2}\mathrm{e}^{\frac{\int f(t)\,\mathrm{d}t}{2}\left(-\sqrt{\frac{-a^2+2\,da-4\,bc-d^2}{da-bc}}\sqrt{-da+bc}+a+d\right)}\,\mathrm{d}t\right.\right.$$

2.1876 ODE No. 1876

$$\left\{x'(t)=x(t)\cos(t), y'(t)=x(t)e^{-\sin(t)}\right\}$$

✓ **Mathematica** : cpu = 0.104512 (sec), leaf count = 41

$$\left\{\left\{x(t)\to c_1 e^{\sin(t)}, y(t)\to c_1 \text{Integrate}\left[e^{\sin(K[1])-\sin(K[1])}, \{K[1],1,t\}, \text{Assumptions}\to \text{True}\right]+c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.139 (sec), leaf count = 18

$$\left\{\left\{x(t)=\_C2\,\mathrm{e}^{\sin(t)}, y(t)=\_C2\,t+\_C1\right\}\right\}$$

2.1877 ODE No. 1877

$$\{tx'(t)+y(t)=0, x(t)+ty'(t)=0\}$$

✓ **Mathematica** : cpu = 0.0057952 (sec), leaf count = 31

$$\left\{\left\{x(t)\to c_1 t+\frac{c_2}{t}, y(t)\to \frac{c_2}{t}-c_1 t\right\}\right\}$$

✓ **Maple** : cpu = 0.036 (sec), leaf count = 31

$$\left\{\left\{x(t)=\frac{\_C1\,t^2+\_C2}{t}, y(t)=\frac{-\_C1\,t^2+\_C2}{t}\right\}\right\}$$

2.1878 ODE No. 1878

$$\{tx'(t)+2x(t)=t,-(t+2)x(t)+ty'(t)-ty(t)=-t\}$$

✓ **Mathematica** : cpu = 0.0121632 (sec), leaf count = 39

$$\left\{\left\{x(t)\to \frac{c_1}{t^2}+\frac{t}{3},y(t)\to -\frac{c_1}{t^2}+c_2e^t-\frac{t}{3}\right\}\right\}$$

✓ **Maple** : cpu = 0.058 (sec), leaf count = 39

$$\left\{\left\{x(t)=\frac{t}{3}+\frac{\_C2}{t^2},y(t)=\frac{3\_C1\,\mathrm{e}^t t^2-t^3-3\_C2}{3t^2}\right\}\right\}$$

2.1879 ODE No. 1879

$$\{tx'(t)+2(x(t)-y(t))=t,x(t)+ty'(t)+5y(t)=t^2\}$$

✓ **Mathematica** : cpu = 0.0627834 (sec), leaf count = 58

$$\left\{\left\{x(t)\to \frac{c_1}{t^4}+\frac{c_2}{t^3}+\frac{1}{30}t(2t+9),y(t)\to -\frac{c_1}{t^4}-\frac{c_2}{2t^3}+\frac{1}{60}t(8t-3)\right\}\right\}$$

✓ **Maple** : cpu = 0.056 (sec), leaf count = 54

$$\left\{\left\{x(t)=\frac{2t^6+9t^5+30\_C2\,t+30\_C1}{30t^4},y(t)=\frac{8t^6-3t^5-30\_C2\,t-60\_C1}{60t^4}\right\}\right\}$$

2.1880 ODE No. 1880

$$\{t^2(1-\sin(t))x'(t)=t^2y(t)+tx(t)(1-2\sin(t)),t^2(1-\sin(t))y'(t)=x(t)(t\cos(t)-\sin(t))+ty(t)(1-t\cos(t))$$

✗ **Mathematica** : cpu = 0.0225802 (sec), leaf count = 0 , could not solve

```
DSolve[{t^2*(1 - Sin[t])*Derivative[1][x][t] == t*(1 - 2*Sin[t])*x[t] + t^2*y[t], t^2*(1 - S
```

✓ **Maple** : cpu = 0.083 (sec), leaf count = 23

$$\{\{x(t)=t(\_C2\,t+\_C1),y(t)=\sin(t)\_C1+\_C2\,t\}\}$$

2.1881 ODE No. 1881

$$\{x'(t)+y'(t)+y(t)=f(t),x''(t)+x(t)+y''(t)+y'(t)+y(t)=g(t)\}$$

✓ **Mathematica** : cpu = 0.0316251 (sec), leaf count = 44

$$\{\{x(t)\to -f''(t)-f'(t)-f(t)+g'(t)+g(t),y(t)\to f''(t)+f(t)-g'(t)\}\}$$

✓ **Maple** : cpu = 0.029 (sec), leaf count = 48

$$\left\{\left\{x(t)=-\frac{\mathrm{d}}{\mathrm{d}t}f(t)+g(t)-f(t)-\frac{\mathrm{d}^2}{\mathrm{d}t^2}f(t)+\frac{\mathrm{d}}{\mathrm{d}t}g(t),y(t)=f(t)+\frac{\mathrm{d}^2}{\mathrm{d}t^2}f(t)-\frac{\mathrm{d}}{\mathrm{d}t}g(t)\right\}\right\}$$

2.1882 ODE No. 1882

$$\{2x'(t)-3x(t)+y'(t)=0,x''(t)+y'(t)-2y(t)=e^{2t}\}$$

✓ **Mathematica** : cpu = 0.444027 (sec), leaf count = 928

$$\left\{\left\{x(t)\to \frac{1}{46}e^{t/2}c_1\left(23\cos\left(\frac{\sqrt{23}t}{2}\right)+23e^{t/2}-3\sqrt{23}\sin\left(\frac{\sqrt{23}t}{2}\right)\right)+\frac{e^{3t/2}\left(23e^{t/2}\cos\left(\frac{\sqrt{23}t}{2}\right)-7\sqrt{23}e^{t/2}\sin\left(\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.086 (sec), leaf count = 99

$$\left\{\left\{x(t)=\frac{\mathrm{e}^{2t}}{4}+\_C1\,\mathrm{e}^{t}+\_C2\,\mathrm{e}^{\frac{t}{2}}\cos\left(\frac{\sqrt{23}t}{2}\right)+\_C3\,\mathrm{e}^{\frac{t}{2}}\sin\left(\frac{\sqrt{23}t}{2}\right),y(t)=-\frac{7}{4}\mathrm{e}^{\frac{t}{2}}\left(\frac{\_C3\sqrt{23}}{7}+\_C2\right)\cos\right.\right.$$

2.1883 ODE No. 1883

$$\{x'(t)+x(t)-y'(t)=2t,x''(t)-9x(t)+y'(t)+3y(t)=\sin(2t)\}$$

✓ **Mathematica** : cpu = 0.579432 (sec), leaf count = 614

$$\left\{\left\{x(t)\to \frac{1}{16}c_1e^{-3t}\left(20e^{4t}t+7e^{4t}+9\right)+\frac{1}{16}c_2e^{-3t}\left(4e^{4t}t+3e^{4t}-3\right)-\frac{3}{16}c_3e^{-3t}\left(4e^{4t}t-e^{4t}+1\right)+\frac{e^{-4t}\left(20e^{4t}t+\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.112 (sec), leaf count = 80

$$\left\{\left\{x(t)=-\frac{2\cos\left(2t\right)}{325}+4-\frac{36\sin\left(2t\right)}{325}+2t+\_C1\,\mathrm{e}^{t}+\_C2\,\mathrm{e}^{-3t}+\_C3\,t\mathrm{e}^{t},y(t)=\frac{16\cos\left(2t\right)}{325}-\frac{37\sin\left(2t\right)}{325}\right.\right.$$

2.1884 ODE No. 1884

$$\{x'(t) - x(t) + 2y(t) = 0, x''(t) - 2y'(t) = 2t - \cos(2t)\}$$

✓ **Mathematica** : cpu = 0.18922 (sec), leaf count = 226

$$\left\{\left\{x(t) \to 7\left(c_2 + t^2 - \frac{1}{2}\sin(2t)\right) + 8\left(c_1 e^{t/2} + c_2\left(e^{t/2} - 1\right) + \frac{1}{68}e^{-t/2}\left(e^{t/2}\cos(2t) - 2\left(17\left(2e^{t/2}t^2 + e^{t/2}(t+2)\right.\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.107 (sec), leaf count = 69

$$\left\{\left\{x(t) = \frac{\sin(2\,t)}{34} + \frac{2\cos(2\,t)}{17} - t^2 + 2\,\_C1\,\mathrm{e}^{t/2} - 4\,t + \_C2, y(t) = \frac{\cos(2\,t)}{34} + \frac{9\sin(2\,t)}{68} - t + \frac{\_C1}{2}\mathrm{e}^{\frac{t}{2}} + 2 -\right.\right.$$

2.1885 ODE No. 1885

$$\{tx'(t) - ty'(t) - 2y(t) = 0, tx''(t) + 2x'(t) + tx(t) = 0\}$$

✗ **Mathematica** : cpu = 0.0222964 (sec), leaf count = 0 , could not solve

```
DSolve[{-2*y[t] + t*Derivative[1][x][t] - t*Derivative[1][y][t] == 0, t*x[t] + 2*Derivative[
```

✓ **Maple** : cpu = 0.098 (sec), leaf count = 47

$$\left\{\left\{x(t) = \frac{\sin(t)\,\_C2 + \_C3\,\cos(t)}{t}, y(t) = \frac{(\_C3\,t + 2\,\_C2)\cos(t) + (\_C2\,t - 2\,\_C3)\sin(t) + \_C1}{t^2}\right\}\right\}$$

2.1886 ODE No. 1886

$$\{ay(t) + x''(t) = 0, y''(t) - a^2 y(t) = 0\}$$

✓ **Mathematica** : cpu = 0.0206132 (sec), leaf count = 115

$$\left\{\left\{x(t) \to -\frac{c_4 e^{-at}\left(-2ate^{at} + e^{2at} - 1\right)}{2a^2} - \frac{c_3 e^{-at}\left(e^{at} - 1\right)^2}{2a} + c_2 t + c_1, y(t) \to \frac{1}{2}c_3 e^{-at}\left(e^{2at} + 1\right) + \frac{c_4 e^{-at}\left(e^{2at} -\right.\right.\right.$$

✓ **Maple** : cpu = 0.065 (sec), leaf count = 49

$$\left\{\left\{x(t) = \frac{-\_C4\,\mathrm{e}^{-at} - \_C3\,\mathrm{e}^{at} + a(\_C1\,t + \_C2)}{a}, y(t) = \_C3\,\mathrm{e}^{at} + \_C4\,\mathrm{e}^{-at}\right\}\right\}$$

2.1887 ODE No. 1887

$$\left\{x''(t) = ax(t) + by(t), y''(t) = cx(t) + dy(t)\right\}$$

✓ **Mathematica** : cpu = 0.533673 (sec), leaf count = 5748

$$\left\{\left\{x(t) \to \frac{e^{-\frac{\sqrt{a+d-\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}-\frac{\sqrt{a+d+\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}}\left(e^{\frac{\sqrt{a+d-\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}}a - e^{\frac{\sqrt{a+d+\sqrt{a^2-2da+d^2+4bct}}}{\sqrt{2}}}a - e^{\sqrt{2}\sqrt{}}\right.\right.\right.$$

✓ **Maple** : cpu = 0.14 (sec), leaf count = 360

$$\left\{\left\{x(t) = \_C1\,\mathrm{e}^{-\frac{t}{2}\sqrt{-2\sqrt{a^2-2\,da+4\,bc+d^2}+2\,a+2\,d}} + \_C2\,\mathrm{e}^{\frac{t}{2}\sqrt{-2\sqrt{a^2-2\,da+4\,bc+d^2}+2\,a+2\,d}} + \_C3\,\mathrm{e}^{-\frac{t}{2}\sqrt{2\sqrt{a^2-2\,da+4\,bc+}}}\right.\right.$$

2.1888 ODE No. 1888

$$\left\{x''(t) = \mathrm{a1}x(t) + \mathrm{b1}y(t) + \mathrm{c1}, y''(t) = \mathrm{a2}x(t) + \mathrm{b2}y(t) + \mathrm{c2}\right\}$$

✓ **Mathematica** : cpu = 24.9947 (sec), leaf count = 37858

too large to display

✓ **Maple** : cpu = 0.269 (sec), leaf count = 457

$$\left\{\left\{x(t) = \_C4\,\mathrm{e}^{\frac{t}{2}\sqrt{2\sqrt{a1^2-2\,a1\,b2+4\,b1\,a2+b2^2}+2\,a1+2\,b2}} + \_C3\,\mathrm{e}^{-\frac{t}{2}\sqrt{2\sqrt{a1^2-2\,a1\,b2+4\,b1\,a2+b2^2}+2\,a1+2\,b2}} + \_C2\,\mathrm{e}^{\frac{t}{2}\sqrt{}}\right.\right.$$

2.1889 ODE No. 1889

$$\left\{x''(t) + x(t) + y(t) = -5, -4x(t) + y''(t) - 3y(t) = -3\right\}$$

✓ **Mathematica** : cpu = 0.100531 (sec), leaf count = 554

$$\left\{\left\{x(t) \to -\frac{1}{4}c_4e^{-t}\left(e^{2t}t + t - e^{2t} + 1\right) - \frac{1}{2}c_1e^{-t}\left(e^{2t}t - t - e^{2t} - 1\right) - \frac{1}{2}c_2e^{-t}\left(e^{2t}t + t - 2e^{2t} + 2\right) - \frac{1}{4}c_3e^{-t}\left(e^{2t}\right.\right.\right.$$

✓ **Maple** : cpu = 0.062 (sec), leaf count = 60

$$\left\{\left\{x(t) = (\_C4\,t + \_C2)\,\mathrm{e}^{-t} + 18 + (\_C3\,t + \_C1)\,\mathrm{e}^{t}, y(t) = ((-2\,t+2)\,\_C4 - 2\,\_C2)\,\mathrm{e}^{-t} - 23 + ((-2\,t-2)\right.\right.$$

2.1890 ODE No. 1890

$$\left\{x''(t) = c^2x(t)\left(3\cos^2(at+b)-1\right)+\frac{3}{2}c^2y(t)\sin(2abt), y''(t) = \frac{3}{2}c^2x(t)\sin(2abt)+c^2y(t)\left(3\sin^2(at+b)-1\right)\right\}$$

✗ **Mathematica** : cpu = 0.0096881 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[2][x][t] == c^2*(-1 + 3*Cos[b + a*t]^2)*x[t] + (3*c^2*Sin[2*a*b*t]*y[t])/
1 + 3*Sin[b + a*t]^2)*y[t]}, {x[t], y[t]}, t]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{\left\{x(t) = DESol\left(\left\{\frac{d^4}{dt^4}\_Y(t)+\left(-2\frac{ab\cos(atb)}{\sin(atb)}+2\frac{ab\sin(atb)}{\cos(atb)}\right)\frac{d^3}{dt^3}\_Y(t)+\left(2\frac{(\sin(atb))^2b^2a^2}{(\cos(atb))^2}+2\frac{a^2b^2(c\right.\right.\right.\right.}{(\sin}$$

2.1891 ODE No. 1891

$$\{x''(t)+6x(t)+7y(t)=0, 3x(t)+y''(t)+2y(t)=2t\}$$

✓ **Mathematica** : cpu = 0.438306 (sec), leaf count = 766

$$\left\{\left\{x(t)\to -\frac{7}{60}c_4e^{-t}\left(3e^{2t}-2e^t\sin(3t)-3\right)+\frac{1}{60}c_2e^{-t}\left(9e^{2t}+14e^t\sin(3t)-9\right)-\frac{7}{20}c_3e^{-t}\left(e^{2t}-2e^t\cos(3t)+1\right)\right.\right.$$

✓ **Maple** : cpu = 0.059 (sec), leaf count = 64

$$\left\{\left\{x(t)=\frac{14\,t}{9}+\_C1\,e^t+\_C2\,\cos(3\,t)+\_C3\,e^{-t}+\_C4\,\sin(3\,t), y(t)=-\_C1\,e^t+\frac{3\_C2\,\cos(3\,t)}{7}-\_C3\right.\right.$$

2.1892 ODE No. 1892

$$\{-ay'(t)+bx(t)+x''(t)=0, ax'(t)+by(t)+y''(t)=0\}$$

✓ **Mathematica** : cpu = 0.393302 (sec), leaf count = 4815

$$\left\{\left\{x(t)\to \frac{e^{-\frac{\sqrt{-a^2-2b-\sqrt{a^2(a^2+4b)}}t}{\sqrt{2}}-\frac{\sqrt{-a^2-2b+\sqrt{a^2(a^2+4b)}}t}{\sqrt{2}}}\left(e^{\frac{\sqrt{-a^2-2b-\sqrt{a^2(a^2+4b)}}t}{\sqrt{2}}}a^2-e^{\frac{\sqrt{-a^2-2b+\sqrt{a^2(a^2+4b)}}t}{\sqrt{2}}}a^2-e^{\sqrt{2}\sqrt{-}}\right.}{}\right.\right.$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 463

$$\left\{\left\{x(t) = \_C1\, \mathrm{e}^{-\frac{t}{2}\sqrt{-2a^2-2\sqrt{a^2(a^2+4b)}-4b}} + \_C2\, \mathrm{e}^{\frac{t}{2}\sqrt{-2a^2-2\sqrt{a^2(a^2+4b)}-4b}} + \_C3\, \mathrm{e}^{-\frac{t}{2}\sqrt{-2a^2+2\sqrt{a^2(a^2+4b)}-4b}} +\right.\right.$$

2.1893 ODE No. 1893

$$\{-\mathrm{A0}y'(t) + \mathrm{a1}x''(t) + \mathrm{b1}x'(t) + \mathrm{c1}x(t) = \mathrm{B0}e^{i\omega t}, \mathrm{A0}x'(t) + \mathrm{a2}y''(t) + \mathrm{b2}y'(t) + \mathrm{c2}y(t) = 0\}$$

✗ **Mathematica** : cpu = 299.998 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.276 (sec), leaf count = 1579

$$\left\{\left\{x(t) = \frac{\left(a2\ a1\ \left(RootOf\left(a1\ a2\ \_Z^4 + (a1\ b2 + b1\ a2)\ \_Z^3 + \left(A^2 + a1\ c2 + c1\ a2 + b1\ b2\right)\ \_Z^2 + (c2\ b1 +\right.\right.\right.\right.}{}$$

2.1894 ODE No. 1894

$$\{a(x'(t) - y'(t)) + \mathrm{b1}x(t) + x''(t) = \mathrm{c1}e^{i\omega t}, a(y'(t) - x'(t)) + \mathrm{b2}y(t) + y''(t) = \mathrm{c2}e^{i\omega t}\}$$

✗ **Mathematica** : cpu = 300. (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 1.103 (sec), leaf count = 1056

$$\left\{\left\{x(t) = \frac{\mathrm{e}^{i\omega t}\left(-c1\ \omega^2 + i(c1 + c2)\ a\omega + c1\ b2\right)}{\omega^4 - 2\,ia\omega^3 + (-b1 - b2)\,\omega^2 + i\,(b1 + b2)\,a\omega + b1\ b2} + \_C1\, \mathrm{e}^{RootOf\left(\_Z^4+2\,a\_Z^3+(b1+b2)\_Z^2+(ab1+b2\right.}\right.\right.$$

2.1895 ODE No. 1895

$$\{\mathrm{a11}x''(t) + \mathrm{a12}y''(t) + \mathrm{b11}x'(t) + \mathrm{b12}y'(t) + \mathrm{c11}x(t) + \mathrm{c12}y(t) = 0, \mathrm{a21}x''(t) + \mathrm{a22}y''(t) + \mathrm{b21}x'(t) + \mathrm{b22}y'(t) +$$

✓ **Mathematica** : cpu = 0.454314 (sec), leaf count = 7517

✓ **Maple** : cpu = 0.25 (sec), leaf count = 1008

$$\left\{\left\{x(t) = \sum_{\_a=1}^{4} \mathrm{e}^{RootOf\left((a22\ a11-a21\ a12)\_Z^4+(a11\ b22-a12\ b21-a21\ b12+b11\ a22)\_Z^3+(c22\ a11-a12\ c21-a21\ c12+a22\ c11+b\right.}\right.\right.$$

2.1896 ODE No. 1896

$$\left\{x''(t)-2x'(t)-y'(t)+y(t)=0,2x'(t)-x(t)+y^{(3)}(t)-y''(t)=t\right\}$$

✓ **Mathematica** : cpu = 0.196471 (sec), leaf count = 1132

$$\left\{\left\{x(t)\to \frac{1}{64}e^{-t}\left(2e^{2t}t^2-6e^{2t}t+7e^{2t}+1\right)\left(e^t(1-t)+e^{-t}\left(-2t^3-8t^2-17t-17\right)\right)+\frac{1}{64}e^{-t}\left(2e^{2t}t^2+6e^{2t}t+e\right.\right.\right.$$

✓ **Maple** : cpu = 0.068 (sec), leaf count = 67

$$\left\{\left\{x(t)=-\frac{2\_C2\,\mathrm{e}^{-t}}{3}+\frac{\left(-9\_C5\,t^2-6\_C4\,t-3\_C3-18\_C5\right)\mathrm{e}^{t}}{3}-t-2,y(t)=\_C2\,\mathrm{e}^{-t}-2+\left(\_C5\,t^3-\right.\right.\right.$$

2.1897 ODE No. 1897

$$\left\{x''(t)+y''(t)+y'(t)=\sinh(2t),2x''(t)+y''(t)=2t\right\}$$

✓ **Mathematica** : cpu = 0.108845 (sec), leaf count = 284

$$\left\{\left\{x(t)\to \frac{1}{4}c_4e^{-2t}\left(2e^{2t}t-e^{2t}+1\right)+c_2t+c_1+t\left(\frac{t^2}{2}+\frac{t}{2}-\frac{e^{4t}}{8}+e^{2t}\left(\frac{t}{2}-\frac{1}{4}\right)\right)+\frac{1}{48}e^{-2t}\left(-4e^{2t}\left(4t^2-3t+3\right)\right.\right.\right.$$

✓ **Maple** : cpu = 0.169 (sec), leaf count = 86

$$\left\{\left\{x(t)=\frac{\left(-12\,t+12\_C2-15\right)\mathrm{e}^{-2\,t}}{48}+\frac{t^3}{6}+\frac{t^2}{4}+\_C3\,t+\_C4-\frac{\cosh\left(2\,t\right)}{16}-\frac{\sinh\left(2\,t\right)}{16},y(t)=\frac{\left(4\,t-4\_C2\right.\right.\right.$$

2.1898 ODE No. 1898

$$\left\{x''(t)-x'(t)+y'(t)=0,x''(t)-x(t)+y''(t)=0\right\}$$

✓ **Mathematica** : cpu = 0.04227 (sec), leaf count = 420

$$\left\{\left\{x(t)\to -\frac{1}{5}c_1e^{\frac{t}{2}-\frac{\sqrt{5}t}{2}}\left(\sqrt{5}e^{\sqrt{5}t}-5e^{\frac{\sqrt{5}t}{2}+\frac{t}{2}}-\sqrt{5}\right)+\frac{c_2e^{\frac{t}{2}-\frac{\sqrt{5}t}{2}}\left(e^{\sqrt{5}t}-1\right)}{\sqrt{5}}-\frac{1}{10}c_4e^{\frac{t}{2}-\frac{\sqrt{5}t}{2}}\left(5e^{\sqrt{5}t}+\sqrt{5}e^{\sqrt{5}t}-10\right.\right.\right.$$

✓ **Maple** : cpu = 0.074 (sec), leaf count = 71

$$\left\{\left\{x(t)=\frac{\_C4\,\left(\sqrt{5}-1\right)}{2}\mathrm{e}^{-\frac{\left(\sqrt{5}-1\right)t}{2}}-\frac{\_C3\,\left(\sqrt{5}+1\right)}{2}\mathrm{e}^{\frac{\left(\sqrt{5}+1\right)t}{2}}+\_C1\,\mathrm{e}^{t},y(t)=\_C2+\_C3\,\mathrm{e}^{\frac{\left(\sqrt{5}+1\right)t}{2}}+\_C4\,\mathrm{e}^{-\left(\right.\right.\right.\right.$$

2.1899 ODE No. 1899

$$\{x'(t) = 2x(t), y'(t) = 3x(t) - 2y(t), z'(t) = 2y(t) + 3z(t)\}$$

✓ **Mathematica** : cpu = 0.0111399 (sec), leaf count = 112

$$\left\{\left\{x(t) \to c_1 e^{2t}, y(t) \to \frac{3}{4}c_1 e^{-2t}\left(e^{4t} - 1\right) + c_2 e^{-2t}, z(t) \to \frac{3}{10}c_1 e^{-2t}\left(2e^t + 3e^{2t} + 4e^{3t} + 1\right)\left(e^t - 1\right)^2 + \frac{2}{5}c_2 e^{-2t}(e\right.\right.$$

✓ **Maple** : cpu = 0.089 (sec), leaf count = 52

$$\left\{\left\{x(t) = \_C3\, \mathrm{e}^{2t}, y(t) = \frac{3\_C3\, \mathrm{e}^{2t}}{4} + \mathrm{e}^{-2t}\_C2, z(t) = \_C1\, \mathrm{e}^{3t} - \frac{3\_C3\, \mathrm{e}^{2t}}{2} - \frac{2\,\mathrm{e}^{-2t}\_C2}{5}\right\}\right\}$$

2.1900 ODE No. 1900

$$\{x'(t) = 4x(t), y'(t) = x(t) - 2y(t), z'(t) = x(t) - 4y(t) + z(t)\}$$

✓ **Mathematica** : cpu = 0.0102724 (sec), leaf count = 94

$$\left\{\left\{x(t) \to c_1 e^{4t}, y(t) \to \frac{1}{6}c_1 e^{-2t}\left(e^{6t} - 1\right) + c_2 e^{-2t}, z(t) \to \frac{1}{9}c_1 e^{-2t}\left(e^{3t} + e^{6t} - 2\right) - \frac{4}{3}c_2 e^{-2t}\left(e^{3t} - 1\right) + c_3 e^t\right\}\right\}$$

✓ **Maple** : cpu = 0.084 (sec), leaf count = 50

$$\left\{\left\{x(t) = \_C3\, \mathrm{e}^{4t}, y(t) = \frac{\_C3\, \mathrm{e}^{4t}}{6} + \mathrm{e}^{-2t}\_C2, z(t) = \frac{\_C3\, \mathrm{e}^{4t}}{9} + \_C1\, \mathrm{e}^t + \frac{4\,\mathrm{e}^{-2t}\_C2}{3}\right\}\right\}$$

2.1901 ODE No. 1901

$$\{x'(t) = y(t) - z(t), y'(t) = x(t) + y(t), z'(t) = x(t) + z(t)\}$$

✓ **Mathematica** : cpu = 0.0105463 (sec), leaf count = 105

$$\{\{x(t) \to c_2\left(e^t - 1\right) + c_3\left(1 - e^t\right) + c_1, y(t) \to c_1\left(e^t - 1\right) + c_2\left(e^t t + 1\right) + c_3\left(-e^t t + e^t - 1\right), z(t) \to c_1\left(e^t - 1\right) +$$

✓ **Maple** : cpu = 0.072 (sec), leaf count = 43

$$\{\{x(t) = \_C2 + \_C3\, \mathrm{e}^t, y(t) = (\_C3\, t + \_C1)\, \mathrm{e}^t - \_C2, z(t) = ((t-1)\, \_C3 + \_C1)\, \mathrm{e}^t - \_C2\}\}$$

2.1902 ODE No. 1902

$$\{x'(t) - y(t) + z(t) = 0, -x(t) + y'(t) - y(t) = t, -x(t) + z'(t) - z(t) = t\}$$

✓ **Mathematica** : cpu = 0.0151966 (sec), leaf count = 226

$$\{\{x(t) \to c_2(e^t - 1) + c_3(1 - e^t) + c_1 + e^{-t}(1 - e^t)(-t - 1) + e^{-t}(e^t - 1)(-t - 1), y(t) \to c_3(-e^t t + e^t - 1) +$$

✓ **Maple** : cpu = 0.065 (sec), leaf count = 51

$$\{\{x(t) = \_C2 + \_C3\, \mathrm{e}^t, y(t) = (\_C3\, t + \_C1)\, \mathrm{e}^t - t - \_C2 - 1, z(t) = ((t - 1)\, \_C3 + \_C1)\, \mathrm{e}^t - t - \_C2 -$$

2.1903 ODE No. 1903

$$\{ax'(t) = bc(y(t) - z(t)), by'(t) = ac(z(t) - x(t)), cz'(t) = ab(x(t) - y(t))\}$$

✓ **Mathematica** : cpu = 0.088717 (sec), leaf count = 1304

$$\left\{\left\{x(t) \to \frac{e^{-i\sqrt{a^2+b^2+c^2}t}\left(2e^{i\sqrt{a^2+b^2+c^2}t}a^2 + b^2e^{2i\sqrt{a^2+b^2+c^2}t} + c^2e^{2i\sqrt{a^2+b^2+c^2}t} + b^2 + c^2\right)c_1}{2\left(a^2+b^2+c^2\right)} - \frac{be^{-i\sqrt{a^2+b^2+c^2}t}\left(-\right.\right.\right.$$

✓ **Maple** : cpu = 0.155 (sec), leaf count = 299

$$\left\{\left\{x(t) = \_C1 + \_C2\, \sin\left(\sqrt{a^2+b^2+c^2}t\right) + \_C3\, \cos\left(\sqrt{a^2+b^2+c^2}t\right), y(t) = \frac{1}{b\left(b^2+c^2\right)}\left(\_C1\, b^3 + \left(\left(-\_\right.\right.\right.\right.$$

2.1904 ODE No. 1904

$$\{x'(t) = cy(t) - bz(t), y'(t) = az(t) - cx(t), z'(t) = bx(t) - ay(t)\}$$

✓ **Mathematica** : cpu = 0.0659729 (sec), leaf count = 1445

$$\left\{\left\{x(t) \to \frac{e^{-\sqrt{-a^2-b^2-c^2}t}\left(2e^{\sqrt{-a^2-b^2-c^2}t}a^2 + b^2e^{2\sqrt{-a^2-b^2-c^2}t} + c^2e^{2\sqrt{-a^2-b^2-c^2}t} + b^2 + c^2\right)c_1}{2\left(a^2+b^2+c^2\right)} - \frac{e^{-\sqrt{-a^2-b^2-c^2}t}\right.\right.\right.$$

✓ **Maple** : cpu = 0.098 (sec), leaf count = 257

$$\left\{\left\{x(t) = \_C1 + \_C2\, \sin\left(\sqrt{a^2+b^2+c^2}t\right) + \_C3\, \cos\left(\sqrt{a^2+b^2+c^2}t\right), y(t) = \frac{1}{a\left(b^2+c^2\right)}\left(\left(-a^2b\_C3 + ac\right.\right.\right.\right.$$

2.1905 ODE No. 1905

$$\{x'(t) = h(t)y(t) - g(t)z(t), y'(t) = f(t)z(t) - h(t)x(t), z'(t) = g(t)x(t) - f(t)y(t)\}$$

✗ **Mathematica** : cpu = 0.00739479 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == h[t]*y[t] - g[t]*z[t], Derivative[1][y][t] == -
(h[t]*x[t]) + f[t]*z[t], Derivative[1][z][t] == g[t]*x[t] - f[t]*y[t]}, {x[t], y[t], z[t]},
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , result contains DESol

$$\left\{\left\{x(t) = DESol\left(\left\{\frac{\mathrm{d}^3}{\mathrm{d}t^3}\_Y(t) + \left(-2\frac{h(t)\left(\frac{\mathrm{d}}{\mathrm{d}t}h(t)\right)f(t)}{(h(t))^2 f(t) + f(t)(g(t))^2 + \left(\frac{\mathrm{d}}{\mathrm{d}t}h(t)\right)g(t) - h(t)\frac{\mathrm{d}}{\mathrm{d}t}g(t)} - 2\frac{}{(h(t))^2 f(t)}\right.\right.\right.\right.$$

2.1906 ODE No. 1906

$$\{x'(t) = x(t) + y(t) - z(t), y'(t) = -x(t) + y(t) + z(t), z'(t) = x(t) - y(t) + z(t)\}$$

✓ **Mathematica** : cpu = 0.0504369 (sec), leaf count = 278

$$\left\{\left\{x(t) \to \frac{1}{3}c_1 e^t\left(2\cos\left(\sqrt{3}t\right) + 1\right) - \frac{1}{3}c_2 e^t\left(-\sqrt{3}\sin\left(\sqrt{3}t\right) + \cos\left(\sqrt{3}t\right) - 1\right) - \frac{1}{3}c_3 e^t\left(\sqrt{3}\sin\left(\sqrt{3}t\right) + \cos\left(\sqrt{3}\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.086 (sec), leaf count = 120

$$\left\{\left\{x(t) = \mathrm{e}^t\left(\sin\left(\sqrt{3}t\right)\_C2 + \cos\left(\sqrt{3}t\right)\_C3 + \_C1\right), y(t) = \frac{\mathrm{e}^t\left(\_C2\sqrt{3} - \_C3\right)\cos\left(\sqrt{3}t\right)}{2} + \frac{\mathrm{e}^t\left(-\_C3\sqrt{3}\right.\right.\right.\right.$$

2.1907 ODE No. 1907

$$\{x'(t) = -3x(t) + 48y(t) - 28z(t), y'(t) = -4x(t) + 40y(t) - 22z(t), z'(t) = -6x(t) + 57y(t) - 31z(t)\}$$

✓ **Mathematica** : cpu = 0.0101415 (sec), leaf count = 179

$$\{\{x(t) \to c_1(-e^t)\left(2e^{2t} - 3\right) + 6c_2 e^t\left(2e^t + 3e^{2t} - 5\right) - 2c_3 e^t\left(4e^t + 5e^{2t} - 9\right), y(t) \to -2c_1 e^t\left(e^{2t} - 1\right) + c_2 e^t\left(3e^t\right.\right.\right.\right.$$

✓ **Maple** : cpu = 0.069 (sec), leaf count = 66

$$\left\{\left\{x(t) = \_C1\,\mathrm{e}^t + \_C2\,\mathrm{e}^{2t} + \_C3\,\mathrm{e}^{3t}, y(t) = \frac{2\_C1\,\mathrm{e}^t}{3} + \frac{\_C2\,\mathrm{e}^{2t}}{4} + \_C3\,\mathrm{e}^{3t}, z(t) = \_C1\,\mathrm{e}^t + \frac{\_C2\,\mathrm{e}^{2t}}{4} + \frac{3\_}{}\right.\right.\right.\right.$$

2.1908 ODE No. 1908

$$\{x'(t) = 6x(t) - 72y(t) + 44z(t), y'(t) = 4x(t) - 4y(t) + 26z(t), z'(t) = 6x(t) - 63y(t) + 38z(t)\}$$

✓ **Mathematica** : cpu = 0.0207054 (sec), leaf count = 551

$$\left\{\left\{x(t) \to -36c_2\text{RootSum}\left[\#1^3 - 40\#1^2 + 1714\#1 + 1404\&, \frac{2\#1e^{\#1t} + e^{\#1t}}{3\#1^2 - 80\#1 + 1714}\&\right] + 4c_3\text{RootSum}\left[\#1^3 - 4\right.\right.$$

✓ **Maple** : cpu = 0.749 (sec), leaf count = 1213

$$\left\{\left\{x(t) = \_C2\, \mathrm{e}^{\frac{\left(\left(263474+18\sqrt{351406311}\right)^{\frac{2}{3}}+80\sqrt[3]{263474+18\sqrt{351406311}}-3542\right)t}{6\sqrt[3]{263474+18\sqrt{351406311}}}} \sin\left(\frac{\sqrt{3}t\left(\sqrt[3]{4}\sqrt[3]{\left(131737+9\sqrt{351406311}\right)^2}+\right.\right.\right.\right.$$

2.1909 ODE No. 1909

$$\{x'(t) = ax(t) + \beta z(t) + gy(t), y'(t) = \alpha z(t) + by(t) + gx(t), z'(t) = \alpha y(t) + \beta x(t) + cz(t)\}$$

✓ **Mathematica** : cpu = 0.057912 (sec), leaf count = 1630

$$\left\{\left\{x(t) \to -c_2\text{RootSum}\left[\#1^3 - a\#1^2 - b\#1^2 - c\#1^2 - \alpha^2\#1 - \beta^2\#1 - g^2\#1 + ab\#1 + ac\#1 + bc\#1 + a\alpha^2 +\right.\right.\right.$$

✓ **Maple** : cpu = 27.579 (sec), leaf count = 33085

too large to display

2.1910 ODE No. 1910

$$\{tx'(t) = 2x(t) - t, t^3y'(t) = t^2y(t) - x(t) + t, t^4z'(t) = t^3z(t) - t^2y(t) - x(t) + t\}$$

✓ **Mathematica** : cpu = 0.0104151 (sec), leaf count = 39

$$\left\{\left\{x(t) \to c_3t^2 + t, y(t) \to c_2t + c_3, z(t) \to c_1t + \frac{c_3}{t} + c_2\right\}\right\}$$

✓ **Maple** : cpu = 0.109 (sec), leaf count = 37

$$\left\{\left\{x(t) = \_C3\, t^2 + t, y(t) = \_C2\, t + \_C3, z(t) = \frac{\_C1\, t^2 + \_C2\, t + \_C3}{t}\right\}\right\}$$

2.1911 ODE No. 1911

$$\{atx'(t) = bc(y(t) - z(t)), bty'(t) = ac(z(t) - x(t)), ctz'(t) = ab(x(t) - y(t))\}$$

✗ **Mathematica** : cpu = 0.0310907 (sec), leaf count = 0 , could not solve

```
DSolve[{a*t*Derivative[1][x][t] == b*c*(y[t] - z[t]), b*t*Derivative[1][y][t] == a*c*(-
x[t] + z[t]), c*t*Derivative[1][z][t] == a*b*(x[t] - y[t])}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 0.159 (sec), leaf count = 308

$$\left\{\left\{x(t) = \_C1 + \_C2 \sin\left(\sqrt{a^2+b^2+c^2}\ln(t)\right) + \_C3 \cos\left(\sqrt{a^2+b^2+c^2}\ln(t)\right), y(t) = \frac{1}{b\left(b^2+c^2\right)}\left(\sqrt{a^2+\right.\right.\right.$$

2.1912 ODE No. 1912

$$\{\mathrm{x1}'(t) = a\mathrm{x2}(t) + b\mathrm{x3}(t)\cos(ct) + b\mathrm{x4}(t)\sin(ct), \mathrm{x2}'(t) = -a\mathrm{x1}(t) + b\mathrm{x3}(t)\sin(ct) - b\mathrm{x4}(t)\cos(ct), \mathrm{x3}'(t) = a\mathrm{x4}($$

✗ **Mathematica** : cpu = 0.0638185 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x1][t] == a*x2[t] + b*Cos[c*t]*x3[t] + b*Sin[c*t]*x4[t], Derivative[1]
(a*x1[t]) + b*Sin[c*t]*x3[t] - b*Cos[c*t]*x4[t], Derivative[1][x3][t] == -(b*Cos[c*t]*x1[t])
(b*Sin[c*t]*x1[t]) + b*Cos[c*t]*x2[t] - a*x3[t]}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 2.798 (sec), leaf count = 2956

$$\left\{\left\{x1(t) = \_C2 + \_C3 \sin(ct) + \_C4 \cos(ct), x2(t) = -\cos(ct)\_C3 + \sin(ct)\_C4 + \_C1, x3(t) = \frac{b(\cos(c\right.\right.\right.$$

2.1913 ODE No. 1913

$$\{x'(t) = -x(t)(x(t) + y(t)), y'(t) = y(t)(x(t) + y(t))\}$$

✓ **Mathematica** : cpu = 0.0369515 (sec), leaf count = 64

$$\{\{y(t) \to -\sqrt{c_1}\cot\left(\sqrt{c_1}t - \sqrt{c_1}c_2\right), x(t) \to -\sqrt{c_1}\tan\left(\sqrt{c_1}t - \sqrt{c_1}c_2\right)\}\}$$

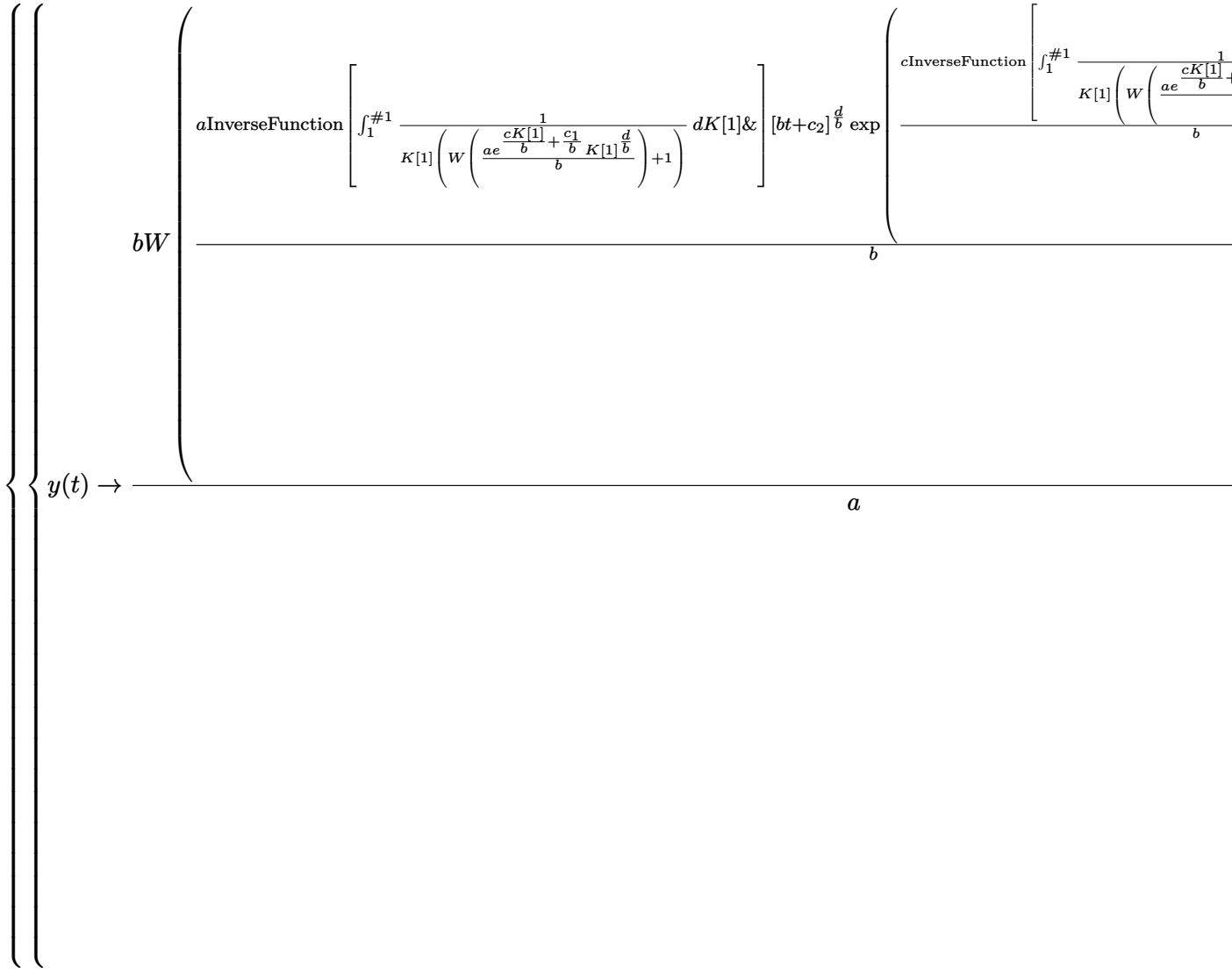
✓ **Maple** : cpu = 0.135 (sec), leaf count = 57

$$\left\{[\{x(t) = 0\}, \left\{y(t) = (\_C1 - t)^{-1}\right\}], [\left\{x(t) = \frac{1}{\_C1}\tanh\left(\frac{\_C2 + t}{\_C1}\right)\right\}, \left\{y(t) = \frac{-(x(t))^2 - \frac{\mathrm{d}}{\mathrm{d}t}x(t)}{x(t)}\right\}]\right\}$$

2.1914 ODE No. 1914

$$\left\{x'(t)=x(t)(ay(t)+b),y'(t)=y(t)(cx(t)+d)\right\}$$

✓ **Mathematica** : cpu = 0.648937 (sec), leaf count = 201



✓ **Maple** : cpu = 0.411 (sec), leaf count = 92

$$\left\{[\{x(t)=0\},\left\{y(t)=\_C1\,\mathrm{e}^{dt}\right\}],[\left\{x(t)=RootOf\left(-\int^{\_Z}\frac{1}{b\_a}\left(lambertW\left(\frac{\mathrm{e}^{-1}}{b}\mathrm{e}^{\frac{c\_a}{b}}\_a^{\frac{d}{b}}\mathrm{e}^{-\frac{C1}{b}}\right)+1\right)^{-1}d\_a+\right.\right.$$

2.1915 ODE No. 1915

$$\{x'(t) = x(t)(a(px(t) + qy(t)) + \alpha), y'(t) = y(t)(b(px(t) + qy(t)) + \beta)\}$$

✗ **Mathematica** : cpu = 300.001 (sec), leaf count = 0 , timed out

```
$Aborted
```

✓ **Maple** : cpu = 11.342 (sec), leaf count = 147

$$\left\{[\{x(t) = 0\}, \left\{y(t) = \frac{\beta}{\mathrm{e}^{-\beta t} \_C1\, \beta - q b}\right\}], [\left\{x(t) = ODESolStruc\left(\_b(\_a), [\left\{\left(\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)(\_b(\_a))^{\frac{-a-b}{a}}\right.\right.\right.\right.$$

2.1916 ODE No. 1916

$$\{x'(t) = h(a - x(t))(c - x(t) - y(t)), y'(t) = k(b - y(t))(c - x(t) - y(t))\}$$

✗ **Mathematica** : cpu = 250.037 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == h*(a - x[t])*(c - x[t] - y[t]), Derivative[1][y][t] == k*(b -
```

✓ **Maple** : cpu = 0.579 (sec), leaf count = 180

$$\left\{[\{x(t) = a\}, \left\{y(t) = \frac{(c-a)\,\mathrm{e}^{k(t+\_C1)(-c+a+b)} - b}{-1 + \mathrm{e}^{k(t+\_C1)(-c+a+b)}}\right\}], [\left\{x(t) = RootOf\left(-\int^{\_Z} \frac{1}{\_a - a}\left((\_a - a)^{-\frac{k}{h}} h\_a + (\right.\right.\right.\right.$$

2.1917 ODE No. 1917

$$\{x'(t) = y(t)^2 - \cos(x(t)), y'(t) = y(t)(-\sin(x(t)))\}$$

✗ **Mathematica** : cpu = 250.044 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == -Cos[x[t]] + y[t]^2, Derivative[1][y][t] == -(Sin[x[t]]*y[t])
```

✓ **Maple** : cpu = 0.858 (sec), leaf count = 109

$$\left\{[\left\{x(t) = RootOf\left(2\int^{\_Z}\left(\tan\left(RootOf\left(-3\sqrt{-(\cos(\_f))^2}\ln\left(9/4\,\frac{(\cos(\_f))^2}{(\cos(\_Z))^2}\right) + 3\,\_C1\sqrt{-(\cos(\_f))^2}\right.\right.\right.\right.\right.\right.$$

2.1918 ODE No. 1918

$$\left\{x'(t) = -x(t)y(t)^2 + x(t) + y(t), y'(t) = x(t)^2 y(t) - x(t) - y(t)\right\}$$

✗ **Mathematica** : cpu = 0.0884219 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t] + y[t] - x[t]*y[t]^2, Derivative[1][y][t] == -
x[t] - y[t] + x[t]^2*y[t]}, {x[t], y[t]}, t]
```

✓ **Maple** : cpu = 2.155 (sec), leaf count = 184

$$\left\{[\{x(t) = 0\}, \{y(t) = 0\}], [\left\{x(t) = ODESolStruc\left(\_a, [\left\{\frac{1}{2\_a^2}\left(\sqrt{(4\_a^2 - 4\_a\_b(\_a) + 1)(\_a^3 + \_a - \_b\right.\right.\right.\right.$$

2.1919 ODE No. 1919

$$\left\{x'(t) = x(t)\left(-\left(x(t)^2 + y(t)^2\right)\right) + x(t) + y(t), y'(t) = -y(t)\left(x(t)^2 + y(t)^2\right) - x(t) + y(t)\right\}$$

✗ **Mathematica** : cpu = 0.108395 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t] + y[t] - x[t]*(x[t]^2 + y[t]^2), Derivative[1][y][t] ==
x[t] + y[t] - y[t]*(x[t]^2 + y[t]^2)}, {x[t], y[t]}, t]
```

✓ **Maple** : cpu = 3.442 (sec), leaf count = 203

$$\left\{[\{x(t) = 0\}, \{y(t) = 0\}], [\left\{x(t) = ODESolStruc\left(\_a, [\left\{\frac{1}{2\_a^3}\left(\sqrt{-(4\_a^4 + 4\_a\_b(\_a) - 4\_a^2 - 1)(2\_a\right.\right.\right.\right.$$

2.1920 ODE No. 1920

$$\left\{x'(t) = x(t)\left(x(t)^2 + y(t)^2 - 1\right) - y(t), y'(t) = y(t)\left(x(t)^2 + y(t)^2 - 1\right) + x(t)\right\}$$

✗ **Mathematica** : cpu = 0.0834446 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == -y[t] + x[t]*(-1 + x[t]^2 + y[t]^2), Derivative[1][y][t] == x
1 + x[t]^2 + y[t]^2)}, {x[t], y[t]}, t]
```

✓ **Maple** : cpu = 3.463 (sec), leaf count = 205

$$\left\{[\{x(t) = 0\}, \{y(t) = 0\}], [\left\{x(t) = ODESolStruc\left(\_a, [\left\{\frac{1}{2\_a^3}\left(\sqrt{-(4\_a^4 - 4\_a^2 - 4\_a\_b(\_a) - 1)(4\_a\right.\right.\right.\right.$$

2.1921 ODE No. 1921

$$\left\{x'(t) = -y(t)\left(x(t)^2+y(t)^2\right), y'(t) = \left(\begin{cases} x(t)^2+y(t)^2 & x(t)^2+y(t)^2 \geq 2x(t) \\ \left(x(t)^2+y(t)^2\right)\left(\frac{x(t)}{2} - \frac{y(t)^2}{2x(t)}\right) & \text{True} \end{cases}\right)\right\}$$

✗ **Mathematica** : cpu = 2.45122 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == -(y[t]*(x[t]^2 + y[t]^2)), Derivative[1][y][t] == Piecewise[{
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve({diff(x(t),t) = -y(t)*(x(t)^2+y(t)^2), diff(y(t),t) = piecewise(2*x(t) <= x(t)^2+y(t)
1/2*y(t)^2/x(t))*(x(t)^2+y(t)^2))})
```

2.1922 ODE No. 1922

$$\left\{x'(t) = \left(\begin{cases} \sin\left(\frac{1}{x(t)^2+y(t)^2}\right) x(t)\left(x(t)^2+y(t)^2-1\right) & x(t)^2+y(t)^2 \neq 1 \\ 0 & \text{True} \end{cases}\right) - y(t), y'(t) = \left(\begin{cases} \sin\left(\frac{1}{x(t)^2 \ldots}\right. \end{cases}\right.\right.$$

✗ **Mathematica** : cpu = 11.349 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == Piecewise[{{Sin[(x[t]^2 + y[t]^2)^(-1)]*x[t]*(-
1 + x[t]^2 + y[t]^2), x[t]^2 + y[t]^2 != 1}}, 0] - y[t], Derivative[1][y][t] == Piecewise[{{
1)]*y[t]*(-1 + x[t]^2 + y[t]^2), x[t]^2 + y[t]^2 != 1}}, 0] + x[t]}, {x[t], y[t]}, t]
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.1923 ODE No. 1923

$$\left\{\left(t^2+1\right)x'(t) = y(t) - tx(t), \left(t^2+1\right)y'(t) = -x(t) - ty(t)\right\}$$

✓ **Mathematica** : cpu = 0.0124748 (sec), leaf count = 53

$$\left\{\left\{x(t) \to \frac{c_1}{t^2+1} + \frac{c_2 t}{t^2+1}, y(t) \to \frac{c_2}{t^2+1} - \frac{c_1 t}{t^2+1}\right\}\right\}$$

✓ **Maple** : cpu = 0.04 (sec), leaf count = 35

$$\left\{\left\{x(t) = \frac{\_C1\, t + \_C2}{t^2+1}, y(t) = \frac{-\_C2\, t + \_C1}{t^2+1}\right\}\right\}$$

2.1924 ODE No. 1924

$$\left\{\left(-t^2+x(t)^2+y(t)^2\right)x'(t)=-2tx(t),\left(-t^2+x(t)^2+y(t)^2\right)y'(t)=-2ty(t)\right\}$$

✓ **Mathematica** : cpu = 0.070973 (sec), leaf count = 191

$$\left\{\left\{y(t)\to\frac{c_1\left(e^{c_2}-\sqrt{-4c_1^2t^2+e^{2c_2}-4t^2}\right)}{2\left(c_1^2+1\right)},x(t)\to\frac{e^{c_2}-\sqrt{-4c_1^2t^2+e^{2c_2}-4t^2}}{2\left(c_1^2+1\right)}\right\},\left\{y(t)\to\frac{c_1\left(\sqrt{-4c_1^2t^2+e^{2c}\right.}\right.}{2\left(c_1^2+\right.}\right.$$

✓ **Maple** : cpu = 0.331 (sec), leaf count = 180

$$\left\{[\{x(t)=0\},\left\{y(t)=\frac{1}{2\_C1}\left(1+\sqrt{-4\_C1^2t^2+1}\right),y(t)=\frac{1}{2\_C1}\left(1-\sqrt{-4\_C1^2t^2+1}\right)\right\}],[\left\{x(t)=\frac{1}{2\_C\right.}\right.$$

2.1925 ODE No. 1925

$$\left\{ay'(t)+tx'(t)-x(t)+y'(t)^2=0,x'(t)y'(t)+ty'(t)-y(t)=0\right\}$$

✗ **Mathematica** : cpu = 8.3664 (sec), leaf count = 0 , could not solve

```
DSolve[{-x[t] + t*Derivative[1][x][t] + a*Derivative[1][y][t] + Derivative[1][y][t]^2 == 0,
y[t] + t*Derivative[1][y][t] + Derivative[1][x][t]*Derivative[1][y][t] == 0}, {x[t], y[t]},
```

✓ **Maple** : cpu = 0.312 (sec), leaf count = 194

$$\left\{[\left\{x(t)=-\frac{t^2}{3}\right\},\left\{y(t)=-\frac{t^3}{27\,a}\right\}],[\{x(t)=\_C1\,t+\_C2\},\left\{y(t)=-\frac{\left(\frac{\mathrm{d}}{\mathrm{d}t}x(t)+t\right)\left(\left(\frac{\mathrm{d}}{\mathrm{d}t}x(t)\right)^2+t\frac{\mathrm{d}}{\mathrm{d}t}x(t)-x(t\right.\right.}{a}\right.\right.$$

2.1926 ODE No. 1926

$$\left\{x(t)=f\left(x'(t),y'(t)\right)+tx'(t),y(t)=g\left(x'(t),y'(t)\right)+ty'(t)\right\}$$

✗ **Mathematica** : cpu = 0.00648956 (sec), leaf count = 0 , could not solve

```
DSolve[{x[t] == f[Derivative[1][x][t], Derivative[1][y][t]] + t*Derivative[1][x][t], y[t] ==
```

✓ **Maple** : cpu = 0.115 (sec), leaf count = 96

$$\left\{[\left\{\int RootOf\left(t\frac{\mathrm{d}}{\mathrm{d}t}y(t)+g\left(\_Z,\frac{\mathrm{d}}{\mathrm{d}t}y(t)\right)-y(t)\right)\,\mathrm{d}t+\_C1=tRootOf\left(t\frac{\mathrm{d}}{\mathrm{d}t}y(t)+g\left(\_Z,\frac{\mathrm{d}}{\mathrm{d}t}y(t)\right)-y(t)\right)+f\right.\right.$$

2.1927 ODE No. 1927

$$\left\{x''(t) = ae^{2x(t)} + e^{-2x(t)}\cos^2(y(t)) - e^{-x(t)}, y''(t) = e^{-2x(t)}\sin(y(t))\cos(y(t)) - \tan(y(t))\sec^2(y(t))\right\}$$

✗ **Mathematica** : cpu = 0.00983657 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[2][x][t] == -E^(-x[t]) + a*E^(2*x[t]) + Cos[y[t]]^2/E^(2*x[t]), Derivativ
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , could not solve

```
dsolve({diff(diff(x(t),t),t) = a*exp(2*x(t))-exp(-x(t))+exp(-2*x(t))*cos(y(t))^2, diff(diff(
2*x(t))*sin(y(t))*cos(y(t))-sin(y(t))/cos(y(t))^3})
```

2.1928 ODE No. 1928

$$\left\{x''(t) = \frac{kx(t)}{(x(t)^2 + y(t)^2)^{3/2}}, y''(t) = \frac{ky(t)}{(x(t)^2 + y(t)^2)^{3/2}}\right\}$$

✗ **Mathematica** : cpu = 0.00717016 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[2][x][t] == (k*x[t])/(x[t]^2 + y[t]^2)^(3/2), Derivative[2][y][t] == (k*y
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

2.1929 ODE No. 1929

$$\left\{x''(t) = -\frac{cy(t)x'(t)f\left(\sqrt{x'(t)^2 + y'(t)^2}\right)}{\sqrt{x'(t)^2 + y'(t)^2}}, y''(t) = -\frac{cy(t)y'(t)f\left(\sqrt{x'(t)^2 + y'(t)^2}\right)}{\sqrt{x'(t)^2 + y'(t)^2}} - g\right\}$$

✗ **Mathematica** : cpu = 0.00884494 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[2][x][t] == -((c*f[Sqrt[Derivative[1][x][t]^2 + Derivative[1][y][t]^2]]*y
g - (c*f[Sqrt[Derivative[1][x][t]^2 + Derivative[1][y][t]^2]]*y[t]*Derivative[1][y][t])/Sqrt
```

✓ **Maple** : cpu = 4.038 (sec), leaf count = 116

$$\left\{[\left\{y(t) = ODESolStruc\left(\_a, [\left\{\left(\frac{\mathrm{d}}{\mathrm{d}\_a}\_b(\_a)\right)\_b(\_a) + 1\left(C(\_a)f\left(\sqrt{(\_b(\_a))^2}\right)\_b(\_a) + g\sqrt{(\_b(\_a)\right.\right.\right.\right.$$

2.1930 ODE No. 1930

$$\{x'(t) = y(t) - z(t), y'(t) = x(t)^2 + y(t), z'(t) = x(t)^2 + z(t)\}$$

✓ **Mathematica** : cpu = 0.0412764 (sec), leaf count = 308

$$\left\{\left\{x(t) \to e^{-c_3}\left(e^{c_3}c_1 + e^t\right), y(t) \to c_2\left(e^{-c_3}\left(e^{c_3}c_1 + e^t\right) - c_1\right) + \left(e^{-c_3}\left(e^{c_3}c_1 + e^t\right) - c_1\right)\left(-\frac{c_1^2}{e^{-c_3}\left(e^{c_3}c_1 + e^t\right) - c_1}\right.\right.\right.$$

✓ **Maple** : cpu = 0.05 (sec), leaf count = 45

$$\left\{\left[\left\{x(t) = \_C2 + \_C3\,\mathrm{e}^t\right\}, \left\{y(t) = \left(\int (x(t))^2\,\mathrm{e}^{-t}\,\mathrm{d}t + \_C1\right)\mathrm{e}^t\right\}, \left\{z(t) = -\frac{\mathrm{d}}{\mathrm{d}t}x(t) + y(t)\right\}\right]\right\}$$

2.1931 ODE No. 1931

$$\{ax'(t) = (b-c)y(t)z(t), by'(t) = (c-a)x(t)z(t), cz'(t) = (a-b)x(t)y(t)\}$$

✓ **Mathematica** : cpu = 5.51101 (sec), leaf count = 10101

$$\left\{\left\{\left\{x(t) \to \frac{\sqrt{2}b^2\sqrt{a(a-c)}c_1 \mathrm{sn}\left(\frac{\frac{\sqrt{2}\sqrt{a}\sqrt{a-c}c\sqrt{c_2}t}{\sqrt{b}\sqrt{b-c}} - \frac{\sqrt{2}\sqrt{a}\sqrt{b}\sqrt{a-c}\sqrt{c_2}t}{\sqrt{b-c}} - \frac{\sqrt{2}\sqrt{a}\sqrt{a-c}c\sqrt{c_2}c_3}{\sqrt{b}\sqrt{b-c}} + \frac{\sqrt{2}\sqrt{a}\sqrt{b}\sqrt{a-c}\sqrt{c_2}c_3}{\sqrt{b-c}}}{a} \middle| -\frac{(a-b)bc_1}{(a-c)cc_2}\right)}{(a-c)\sqrt{b(b-c)c_1}} - \frac{\sqrt{2}b\sqrt{a(a-c)}}{a}\right.\right.\right.$$

✓ **Maple** : cpu = 0.828 (sec), leaf count = 1117

$$\left\{\left[\{x(t) = 0\}, \{y(t) = 0\}, \{z(t) = \_C1\}\right], \left[\{x(t) = 0\}, \{y(t) = \_C1\}, \{z(t) = 0\}\right], \left[\{x(t) = \_C1\}, \{y(t) = 0\}, \{\right.\right.$$

2.1932 ODE No. 1932

$$\{x'(t) = x(t)(y(t) - z(t)), y'(t) = y(t)(z(t) - x(t)), z'(t) = z(t)(x(t) - y(t))\}$$

✗ **Mathematica** : cpu = 2.29574 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t]*(y[t] - z[t]), Derivative[1][y][t] == y[t]*(-
x[t] + z[t]), Derivative[1][z][t] == (x[t] - y[t])*z[t]}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 1.132 (sec), leaf count = 383

$$\left\{[\{x(t) = 0\}, \{y(t) = 0\}, \{z(t) = \_C1\}], [\{x(t) = 0\}, \left\{y(t) = \frac{\_C1\, \mathrm{e}^{-\_C2\, \_C1\, \mathrm{e}^{-\_C1\, t}}}{-1 + \mathrm{e}^{-\_C2\, \_C1\, \mathrm{e}^{-\_C1\, t}}}\right\}, \left\{z(t) = \frac{\frac{\mathrm{d}}{\mathrm{d}t} y(t)}{y(t)}\right\}], [\{x(t\right.$$

2.1933 ODE No. 1933

$$\{x'(t) + y'(t) = x(t)y(t), y'(t) + z'(t) = y(t)z(t), x'(t) + z'(t) = x(t)z(t)\}$$

✗ **Mathematica** : cpu = 126.899 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] + Derivative[1][y][t] == x[t]*y[t], Derivative[1][y][t] + Deriva
```

✓ **Maple** : cpu = 2.514 (sec), leaf count = 17738

too large to display

2.1934 ODE No. 1934

$$\left\{x'(t) = \frac{x(t)^2}{2} - \frac{y(t)}{24}, y'(t) = 2x(t)y(t) - 3z(t), z'(t) = 3x(t)z(t) - \frac{y(t)^2}{6}\right\}$$

✗ **Mathematica** : cpu = 73.2859 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t]^2/2 - y[t]/24, Derivative[1][y][t] == 2*x[t]*y[t] - 3*z[
y[t]^2/6 + 3*x[t]*z[t]}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 1.358 (sec), leaf count = 377

$$\left\{[\{y(t) = 0\}, \left\{x(t) = -2\left(-2\,\_C1 + t\right)^{-1}\right\}, \{z(t) = 0\}], [\left\{y(t) = 256\left(\_C1\, t + \_C2\right)^{-4}\right\}, \left\{x(t) = \frac{1}{6\, y(t)}\left(-\sqrt{\right.\right.\right.$$

2.1935 ODE No. 1935

$$\left\{x'(t)=x(t)\left(y(t)^2-z(t)^2\right),y'(t)=y(t)\left(z(t)^2-x(t)^2\right),z'(t)=z(t)\left(x(t)^2-y(t)^2\right)\right\}$$

✗ **Mathematica** : cpu = 0.0536469 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t]*(y[t]^2 - z[t]^2), Derivative[1][y][t] == y[t]*(-
x[t]^2 + z[t]^2), Derivative[1][z][t] == (x[t]^2 - y[t]^2)*z[t]}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 2.187 (sec), leaf count = 741

$$\left\{[\{x(t)=0\},\{y(t)=0\},\{z(t)=\_C1\}],[\{x(t)=0\},\left\{y(t)=\frac{1}{\left(\mathrm{e}^{-\_C2-\_C1}\right)^2\left(\mathrm{e}^{-\_C1\,t}\right)^2-1}\sqrt{\left(\left(\mathrm{e}^{-\_C2-\_C1}\right)^2\left(\mathrm{e}^{-\_C1\,t}\right.\right.\right.\right.$$

2.1936 ODE No. 1936

$$\left\{x'(t)=x(t)\left(y(t)^2-z(t)^2\right),y'(t)=-y(t)\left(x(t)^2+z(t)^2\right),z'(t)=z(t)\left(x(t)^2+y(t)^2\right)\right\}$$

✗ **Mathematica** : cpu = 0.0496151 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t]*(y[t]^2 - z[t]^2), Derivative[1][y][t] == -
(y[t]*(x[t]^2 + z[t]^2)), Derivative[1][z][t] == (x[t]^2 + y[t]^2)*z[t]}, {x[t], y[t], z[t]}
```

✓ **Maple** : cpu = 0.778 (sec), leaf count = 704

$$\left\{[\{x(t)=0\},\{y(t)=0\},\{z(t)=\_C1\}],[\{x(t)=0\},\left\{y(t)=\frac{1}{\left(\mathrm{e}^{-\_C2-\_C1}\right)^2\left(\mathrm{e}^{-\_C1\,t}\right)^2-1}\sqrt{-\left(\mathrm{e}^{-\_C1\,t}\right)^4\_C1\ (\mathrm{e}-}\right.\right.$$

2.1937 ODE No. 1937

$$\left\{x'(t)=-x(t)y(t)^2+x(t)+y(t),y'(t)=x(t)^2y(t)-x(t)-y(t),z'(t)=y(t)^2-x(t)^2\right\}$$

✗ **Mathematica** : cpu = 0.262389 (sec), leaf count = 0 , could not solve

```
DSolve[{Derivative[1][x][t] == x[t] + y[t] - x[t]*y[t]^2, Derivative[1][y][t] == -
x[t] - y[t] + x[t]^2*y[t], Derivative[1][z][t] == -x[t]^2 + y[t]^2}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 0.93 (sec), leaf count = 242

$$\left\{[\{x(t)=0\},\{y(t)=0\},\{z(t)=\_C1\}],[\left\{x(t)=ODESolStruc\left(\_a,[\left\{\frac{1}{2\,\_a^2}\left(\sqrt{(4\,\_a^2-4\,\_a\,\_b\,(\_a)+1)\,(}\right.\right.\right.\right.$$

2.1938 ODE No. 1938

$$\left\{x''(t)=\frac{x(t)f'(r)}{r},y''(t)=\frac{y(t)f'(r)}{r},z''(t)=\frac{z(t)f'(r)}{r}\right\}$$

✓ **Mathematica** : cpu = 0.00939403 (sec), leaf count = 137

$$\left\{\left\{x(t)\to c_1e^{-\frac{t\sqrt{f'(r)}}{\sqrt{r}}}+c_2e^{\frac{t\sqrt{f'(r)}}{\sqrt{r}}},y(t)\to c_3e^{-\frac{t\sqrt{f'(r)}}{\sqrt{r}}}+c_4e^{\frac{t\sqrt{f'(r)}}{\sqrt{r}}},z(t)\to c_5e^{-\frac{t\sqrt{f'(r)}}{\sqrt{r}}}+c_6e^{\frac{t\sqrt{f'(r)}}{\sqrt{r}}}\right\}\right\}$$

✓ **Maple** : cpu = 0.127 (sec), leaf count = 101

$$\left\{\left\{x(t)=\_C5\,e^{t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}}+\_C6\,e^{-t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}},y(t)=\_C3\,e^{t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}}+\_C4\,e^{-t\sqrt{\frac{d}{dr}F(r)}\frac{1}{\sqrt{r}}},z(t)=\_C1\,e^{t\sqrt{}}\right.\right.$$

2.1939 ODE No. 1939

$\{(x(t)-y(t))(x(t)-z(t))x'(t)=f(t),(y(t)-x(t))(y(t)-z(t))y'(t)=f(t),(z(t)-x(t))(z(t)-y(t))z'(t)=f(t$

✗ **Mathematica** : cpu = 0.0304514 (sec), leaf count = 0 , could not solve

```
DSolve[{(x[t] - y[t])*(x[t] - z[t])*Derivative[1][x][t] == f[t], (-x[t] + y[t])*(y[t] - z[t]
x[t] + z[t])*(-y[t] + z[t])*Derivative[1][z][t] == f[t]}, {x[t], y[t], z[t]}, t]
```

✓ **Maple** : cpu = 1.591 (sec), leaf count = 899

$$\left\{\left[\left\{x(t)=\int 3\frac{f(t)}{\_C1^3+11664\,\_C2^2-23328\,\_C2\,\int f(t)\,dt+11664\,\left(\int f(t)\,dt\right)^2}\left(\left(-i\sqrt{3}-1\right)\left(\left(1+108\sqrt{\right.\right.\right.\right.\right.\right.$$

2.1940 ODE No. 1940

$\{\mathrm{x1}'(t)\sin(\mathrm{x2}(t))=\mathrm{x4}(t)\sin(\mathrm{x3}(t))+\mathrm{x5}(t)\cos(\mathrm{x3}(t)),\mathrm{x2}'(t)=\mathrm{x4}(t)\cos(\mathrm{x3}(t))-\mathrm{x5}(t)\sin(\mathrm{x3}(t)),\mathrm{x1}'(t)\cos(\mathrm{x2}(t$

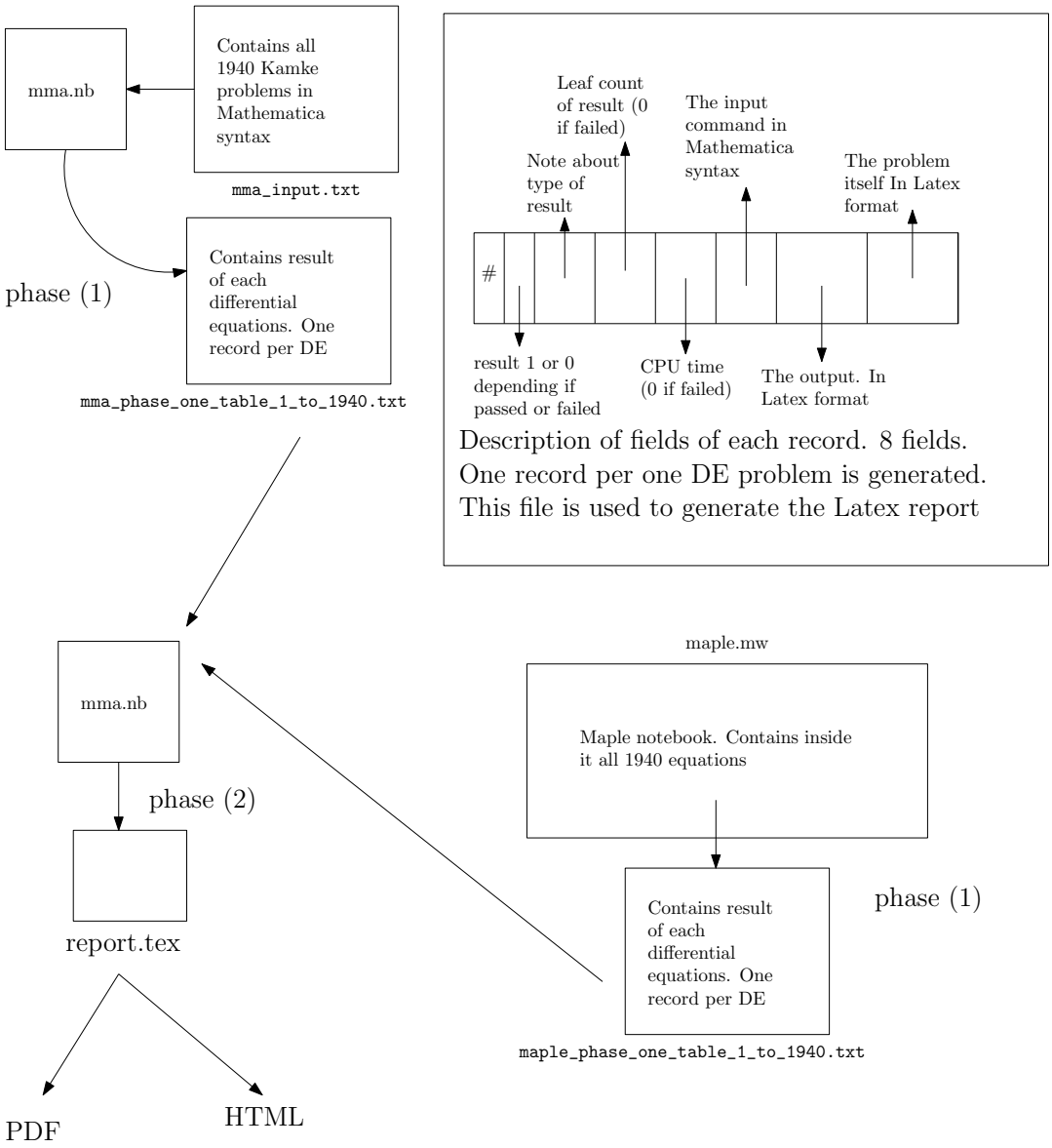
✗ **Mathematica** : cpu = 0.0089515 (sec), leaf count = 0 , could not solve

```
DSolve[{Sin[x2[t]]*Derivative[1][x1][t] == Sin[x3[t]]*x4[t] + Cos[x3[t]]*x5[t], Derivative[1
(a*(1 - lambda)*x5[t]) + Derivative[1][x4][t] == -(m*Cos[x3[t]]*Sin[x2[t]]), a*(1 - lambda)*
```

✗ **Maple** : cpu = 0. (sec), leaf count = 0 , exception

```
time expired
```

3 Appendix



Kamke Differential equations build process

Nasser M. Abbasi (design.ipe)